

$$1) a) \frac{a(t)}{a_0} = \frac{1}{10^6} \quad n_e(0) \sim 2 \text{ m}^{-3} = 2 \times 10^{-1} \text{ m}^{-3}$$

$$n = \frac{N}{V}, \quad V \propto a(t)^3 \Rightarrow n \propto \frac{1}{a(t)^3}$$

$$\frac{n(t)}{n_0} = \left(\frac{a_0}{a(t)} \right)^3 = (10^6)^3 = 10^{18}$$

$$n(t) = 10^{18} n_0 = 10^{18} \times 2 \times 10^{-1} = \boxed{2 \times 10^{17} \text{ m}^{-3}}$$

b) Relativistic?

$$T \propto \frac{1}{a(t)}$$

$$\frac{T(t)}{T_0} = \frac{a_0}{a(t)} \rightarrow T(t) = 10^6 T_0 \sim \boxed{3 \cdot 10^6 \text{ K}}$$

$$KE \text{ (in eq.)} = kT = 2.3 \times 10^2 \text{ eV} = 2.3 \times 10^{-4} \text{ MeV}$$

$$\boxed{KE \ll mc^2 \Rightarrow NR}$$

$$c) \quad \sigma_T = 6.7 \times 10^{-29} \text{ m}^2$$

$$\lambda_{\text{eff}} = \frac{1}{n \sigma} = \boxed{7.5 \times 10^{10} \text{ m}}$$

$$d) \quad t = \frac{1}{v} = \boxed{248 \text{ s}}$$

count: $\sim 1.3 \times 10^9$ cell
ok assumption