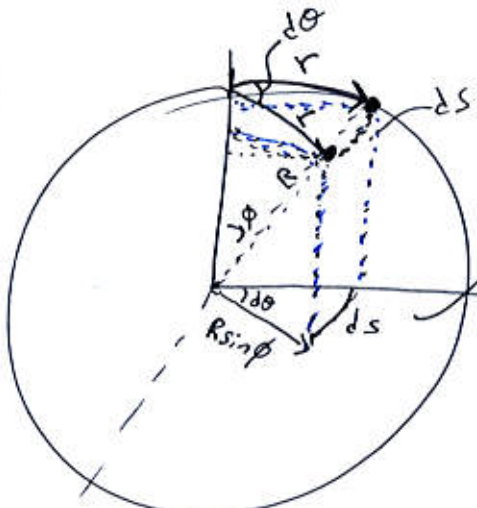


2) - Alternate Solution

a)



$R\phi = r \rightarrow \phi = r/R$

$ds = R \sin \phi d\theta$

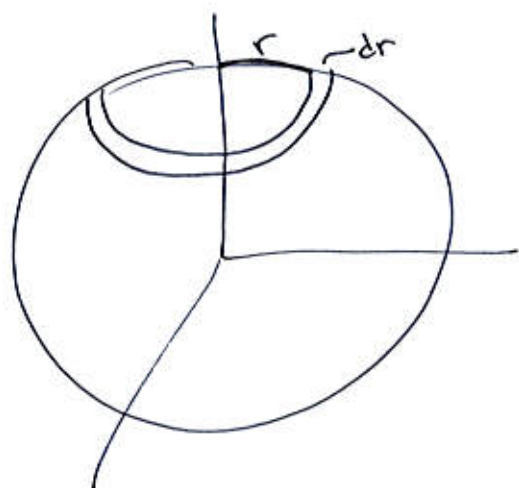
$\rightarrow \boxed{d\theta = \frac{ds}{R \sin(r/R)}}$

b) C is ds as $d\theta \rightarrow 2\pi$:

$$ds = R \sin(r/R) d\theta$$

$$\rightarrow \boxed{C = 2\pi R \sin(r/R)}$$

c) $N = nA(r) \rightarrow A = \text{surface area of sphere}$
 integrate rings of area $= C \times dr$:



$$dA = 2\pi R \sin(r/R) dr$$

$$A = 2\pi R^2 \int_0^r \sin(r/R) dr$$

$$= 2\pi R^2 (-\cos(r/R)) \Big|_0^r \times R$$

$$= 2\pi R^2 (\cos(0) - \cos(r/R))$$

$$= 2\pi R^2 (1 - \cos(r/R))$$

$$\rightarrow \boxed{N = 2\pi n R^2 (1 - \cos(r/R))}$$