

# Galaxy Zoo Hubble: the evolution of red disc galaxies since $z = 1$

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4 December 2017

## ABSTRACT

We study the evolution of the passive disc population from  $z = 1$  to  $z = 0.3$  in a sample of 20,000 galaxies from the COSMOS field and morphologically classified by the Galaxy Zoo: Hubble project. We find that the fraction of disc galaxies that are red, as well as the fraction of red sequence galaxies that are discs, decreases for the most massive galaxies ( $\log(M/M_\odot) > 11$ ) but increases for lower masses. Our observations are consistent with a physical scenario in which more massive galaxies are more likely to enter a red disc phase, and more massive red discs are more likely to morphologically transform into ellipticals than their less massive counterparts. This paper also introduces a new method for using artificially-redshifted galaxies to quantify the redshift-bias in Galaxy Zoo classifications in order to accurately measure the fraction of disc galaxies as a function of redshift.

## 1 INTRODUCTION

Passive, red discs are an unconventional class of galaxies. They do not adhere to the standard bimodality of the colour-morphology relationship, whereby most galaxies tend to exist in one of two populations: blue, late-type discs exhibiting active star formation, and red, early-type ellipticals showing little to no signs of recent star formation (Strateva et al. 2001; Baldry et al. 2004; Correa et al. 2017). The division between the two populations is particularly apparent when represented visually on a colour-magnitude or colour-colour diagram. Galaxies tend to populate in two distinct regions: the “red sequence” in the upper band, which contains predominantly early-type galaxies, and the “blue cloud” in the lower, containing mostly late-type spirals. This relationship has been shown to hold for  $\gtrsim 85\%$  of galaxies out to  $z \sim 1$  (Bell et al. 2004; Cirasuolo et al. 2007; Mignoli et al. 2009) and possibly beyond (Giallongo et al. 2005; van Dokkum et al. 2006; Franzetti et al. 2007; Cassata et al. 2008).

The relatively tight correlation between galaxy colour (which traces the stellar population characteristics) and morphology (which traces dynamical history) suggests an evolutionary link between the two. In the simplest interpre-

tation, it could be hypothesized that galaxies tend to begin their lives as young, star-forming discs, until some mechanism (secular or external) causes star-formation to cease while the galaxy simultaneously undergoes a morphological transformation from disc to spheroidal. The growing evidence for a significant population of galaxies which breaks this relationship, however, mandates more nuanced interpretations of this model.

The passive disc population has been identified as an observable that may improve the understanding of the mechanisms driving the empirically indicated, albeit currently putative, evolutionary link between colour and morphology since their initial discovery. In one of the earliest documented reports of this class of red disc-like objects, van den Bergh (1976) identified a set of spirals in the Virgo cluster which were forming stars “much less vigorously” than the other galaxies of the same type, which were dubbed “anemic spirals”. Analysis of this population suggested the possibility of “gentle” quenching mechanisms which could shut off star-formation without disrupting the morphology, (in contrast to violent processes such as mergers, which are capable of destroying the disc (Bell et al. 2004; Negroponte & White 1983; De Lucia et al. 2006; Springel et al. 2005)). The low

gas content in the anemic spirals suggested that subtle environmental factors played a role in stripping the gas required for ongoing star-formation, a process commonly known now as ram-pressure stripping (Gunn & Gott 1972; Steinhauser et al. 2016).

Subsequent studies have investigated whether other possible mechanisms could lead to the formation of passive discs, and how significant a contribution this population makes to understanding the full picture of galaxy evolution. Environment is believed to play a strong role in their formation; for instance, many studies find passive spirals preferentially occupying high-density environments (e.g. Dressler et al. (1999); Poggianti et al. (1999); Goto et al. (2003); Deng et al. (2009); Hughes & Cortese (2009); Fraser-McKelvie et al. (2017)). Moran et al. (2006) model the star-formation histories of passive spirals at  $z \sim 0.4$  and find them to be consistent with models for spirals affected by gas-starvation (Larson, R.B., Tinsley, B.M. and Caldwell 1980; Quilis et al. 2000; Bekki et al. 2002). Environment plays a significant factor in this scenario, whereby the interaction of the galaxy with the intra-cluster medium halts the accretion of gas onto the galaxy, inhibiting star-formation and causing a quench without significantly disrupting the morphology. Their results did not imply that starvation was the only mechanism responsible for building up the population of discs in the red sequence, but the authors do conclude that passive discs are indeed an important transition population.

Masters et al. (2010) is one of the few studies which finds no strong correlation of passive discs with environment, but does not rule out environment playing a significant role in their creation. They also find strong evidence for quenching via completely secular processes; namely their sample of passive discs being more massive and having a higher bar fraction than their star-forming counterparts. Massive galaxies are more likely to have been assembling for sufficiently long times to consume all of their gas, without environmental stripping being a direct factor. This option could explain the observed correlations with density and passivity, given that higher-density regions were more likely to have been assembled at earlier times. Secondly, Masters et al. (2010) observed a significantly higher bar fraction in passive spirals (67%) than star-forming spirals (27%). Bars are known for their ability to efficiently drive gas to the centres of galaxies via a redistribution of angular momentum throughout the disc (Sellwood & Wilkinson 1993; Shlosman et al. 1989; Ann & Thakur 2005), which could increase central star-formation (Hawarden et al. 1986; Ho et al. 1997) or feed the central supermassive black hole (Athanasoula 1992; Friedli & Benz 1993; Galloway et al. 2015). The excess of bars in passive discs therefore suggests that bars were responsible for quickly using up the gas in the galaxy, resulting in subsequent quenching.

Passive discs have thus far been proposed as both a final stage of galactic evolution, driven by secular and external processes capable of exhausting gas required for star-formation, and as a transition phase of galaxies toward a final evolution to red spheroidal, driven by processes which quench and morphologically transform on different timescales, or multiple separate processes acting independently. Understanding the significance of the passive disc population is therefore unquestionably an important key to understanding galaxy evolution as a whole. Bundy et al.

(2010) investigate this subject by measuring the different morphological contributions to the red sequence since  $z = 1$ , and estimate as many as 60% of all galaxies go through a passive disc phase. They do not quantify which of these subsequently evolve to spheroidal galaxies and which persist as discs for the remainder of their lifetimes, but the decaying contribution of passive discs until as late as  $z = 0.3$  was evidence that some fraction of these did indeed transform to ellipticals.

This paper investigates the evolution of the passive disc population from  $z = 1$  to  $z = 0.3$  using galaxies identified in the COSMOS field with morphological classifications from Galaxy Zoo: Hubble. We measure the fractional contribution of red discs, blue discs, red ellipticals, and blue ellipticals with respect to the total population as functions of both redshift and stellar mass. In addition, we will measure the evolution of both the fraction of discs which are passive and the fraction of the red sequence galaxies which are discs. We assess the mass-dependence of the significance of the red disc population, and discuss the likelihoods of the red disc phase being a transitory stage or an end-point of a typical galaxy’s evolutionary path.

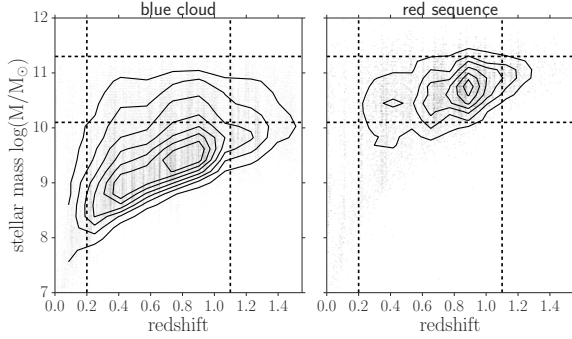
Section 2 describes our methods for selecting disc galaxies and separating the sample into active / passive populations using a colour-colour diagnostic. In Section 3 we describe a new method of correcting for redshift bias in the classification of disc galaxies by Galaxy Zoo volunteers using an artificially-redshifted set of images. In Section 4 we present our results for the fraction of disc galaxies which are red, and the fraction of red sequence galaxies that are discs, as functions of mass and redshift. We compare our findings with results from the literature and discuss their implications in Section 5. Our main conclusions are outlined in Section 6. We adopt a  $\Lambda$ CDM cosmology throughout this paper of  $\Omega_m = 0.31$  and  $H_0 = 68 \text{ km s}^{-1}\text{Mpc}^{-1}$  (Planck Collaboration et al. 2015).

## 2 DATA

The parent sample of galaxies in this paper is drawn from the Galaxy Zoo: Hubble (GZH) catalog (Willett et al. 2016), which provides morphological classifications for galaxies sourced from the HST Legacy Surveys. From the main catalog we select galaxies with imaging from the Cosmic Evolution Survey (COSMOS, Scoville et al. (2007)) in the redshift range  $0.2 < z < 1$ . Stellar masses and rest frame NUV-r and r-J colours are taken from the UltraVISTA catalog (McCracken et al. 2012; Ilbert et al. 2013).

### 2.1 Sample Selection

We identify a mass-limited sample of 20,811 galaxies within  $0.2 < z < 1.1$  and  $10.1 < \log(M/M_\odot) < 11.3$ , indicated by the dashed lines in Figure 1. We categorise the galaxies as disc-like or elliptical using the morphological classifications provided by GZH. In the Galaxy Zoo project, volunteers classify galaxy images by answering simple questions prompted via an online interface. We use the question, “Is the galaxy simply smooth and rounded, with no sign of features or a disk” to classify a galaxy as disc-like by applying a threshold on the fraction of users to answer “features or



**Figure 1.** The box enclosed by the dotted lines displays our mass-limited sample, defined as  $0.2 < z < 1.1$  and  $10.1 < \log(M/M_\odot) < 11.3$ . Blue cloud (left-panel) and red sequence (right-panel) galaxies are plotted separately to illustrate the difference in limiting magnitudes for galaxies whose fluxes are dominated by I-band vs. V-band light respectively. The redshift cut was chosen to ensure morphological classifications are reliable, and the stellar mass cut was chosen to ensure a complete sample of both red sequence and blue cloud galaxies out to  $z = 1$ . **Left:** Black contours show counts for the blue cloud sample, with the outermost contour starting at  $N=200$  and separated by intervals of 200. **Right:** Black contours show counts for the red sequence sample, with the outermost contour starting at  $N=50$  and separated by intervals of 50.

disk”,  $f_{\text{features}} \geq 0.3$ . For a thorough discussion of the full set of questions and corresponding morphological classifications available in GZH, see Willett et al. (2016). We also exclude mergers and irregulars from the analysis by applying cuts of  $f_{\text{irregular}} > 0.3$  and  $f_{\text{merger}} > 0.5$  for galaxies which have at least 20 “yes” votes for the question, “Is there anything odd?”.

To classify the galaxies as passive or star-forming, a method similar to that described by Ilbert et al. (2013) (hereafter I13) was used, which implements a rest-frame NUV- $r$  versus  $r$ - $J$  diagnostic. NUV- $r$  colors perform better than pure optical colors (like  $u$ - $r$ ) in separating the blue cloud from the red sequence, due to NUV bands exhibiting a greater sensitivity to low levels of star-formation (Martin et al. 2007; Wyder et al. 2007). This makes it an excellent probe for stellar populations with light-weighted age of  $10^8$  year, while  $r$  is primarily sensitive to those of  $10^9$  year (Arnouts et al. 2007). NUV -  $r$  has thus been shown to be very well correlated, and an excellent indicator of, current vs. past star formation activity (Martin et al. 2005; Salim et al. 2005).

The demarcation line to separate the passive and star-forming populations at  $z = 1$  is adopted from I13, which defines the red sequence galaxies as those which satisfy:  $M_{\text{NUV}} - M_r > 3(M_r - M_J) + 1$  and  $M_{\text{NUV}} - M_r > 3.1$ . I13 applies this criteria to all galaxies in a range of  $0.2 < z < 3$ , although it performs best at separating the two populations in the redshift bin  $0.7 < z < 1.2$ , where  $> 98\%$  of galaxies identified as quiescent exhibited specific star formation rates less than  $\log(\text{sSFR}) = -11$  (see Figure 3 of I13). This performance justifies our use of the I13 separation criteria for galaxies at  $z = 1$ , but we compute the evolution of the demarcation lines as a function of redshift to  $z = 0$ .

The evolution of  $r$ - $J$  and NUV- $r$  colours was derived using a stellar population synthesis model from Bruzual &

Charlot (2003). An instantaneous-burst model was chosen from the Padova 1994 track to represent the colour evolution of a passively evolving galaxy, with a metallicity  $Z = 0.008 = 0.4Z_\odot$ . A linear fit was generated for each colour within the range  $0 < z < 2$ , and the slopes for each were used to redefine the population separators in five redshift bins with widths  $\Delta z = 0.2$ . We explicitly define one bin bracketing a central redshift  $z = 0.007$  in order to coincide with the sample of SDSS galaxies used to identify completeness in disc detection (FERENGI2, Section 3). The remaining four bins coincide with the HST sample, with central values  $z = [0.30, 0.50, 0.70, 0.90]$ . The red sequence galaxies are thus defined in these bins as those that satisfy:

$$M_{\text{NUV}} - M_r > 3.1 + a_1(z) \quad (1)$$

$$M_{\text{NUV}} - M_r > 3(M_r - M_J + a_2(z)) + a_1(z) + 1 \quad (2)$$

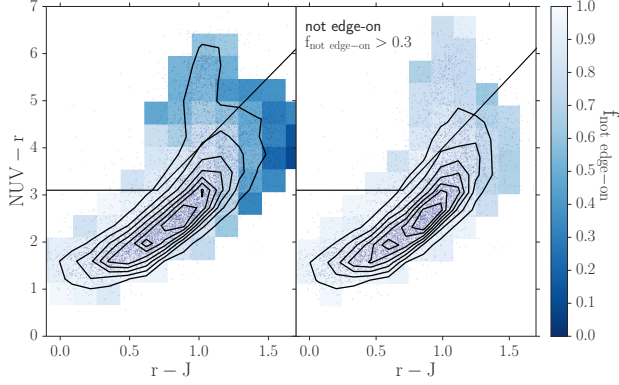
where  $a_1(z) = [0.54, 0.38, 0.27, 0.16, 0.05]$  and  $a_2(z) = [0.19, 0.14, 0.10, 0.06, 0.02]$ . We note that the evolution of the demarcation lines from  $z = 1$  to  $z \sim 0$  is very minimal, and our final results do not change if we perform the separation using the  $z = 1$  definition.

After separating the sample by color, it was observed that the red sequence region of the sample was dominated by highly-inclined galaxies, shown in Figure 2. Given that spectral colour of a galaxy’s combined stellar population should be independent of the angle in which it is observed, it is clear that the inclined galaxy colours are strongly affected by dust-reddening. Although we are not using dust-corrected colours in our colour-colour separation, inclination has shown to have an affect on colours even in those which dust-corrected has been attempted (Morselli et al. 2016; Devour & Bell 2017). We therefore remove highly inclined discs from the sample using an inclination limit defined by GZH vote fractions:  $f_{\text{not edge-on}} > 0.3$  and  $N_{\text{not edge-on}} > 10$  (right panel of Figure 2).

For clarity, the preceding discussion has rigorously enforced the convention that the terms “blue” and “red” refer exclusively to observed spectral colours. Similarly, “active” and “passive” were reserved to describe galaxies with ongoing or quenched star-formation. Hereafter, we relax this strict terminology and conflate “red” and “blue” with “passive” and “active”, respectively.

### 3 CORRECTING FOR INCOMPLETENESS IN DISK DETECTION

In this work, we identify disc galaxies in our sample using a cut of  $f_{\text{features}} \geq 0.3$ , such that galaxies meeting this criterion are considered to have distinguishable features or disc structure (additional cuts are also placed to eliminate highly inclined, irregular, and merging galaxies; see Section 2.1), and galaxies which do not are considered to be elliptical. However, it has been empirically established that distinguishing disc structure from spheroidal becomes increasingly challenging in high redshift galaxies (for both experts and novice classifiers alike), for which features are less resolved and more difficult to identify. Willett et al. (2016) show using

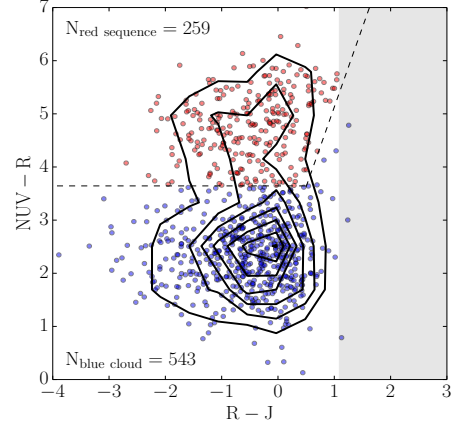


**Figure 2.** The effect of reddening for highly inclined galaxies. On the left panel is the distribution of  $f_{\text{edge-on,no}}$ , which is the fraction of Galaxy Zoo users who voted “no” in response to the question “Could this be a galaxy viewed edge-on?”. This vote correlates with inclination angle, such that low values represent highly inclined galaxies, and high values represent face-on galaxies. The bins are colored such that darker blue bins have a higher fraction of highly inclined galaxies, and white bins have high fractions of face-on galaxies. There is an obvious bias towards redder colours for galaxies with high inclination angles (low votes for  $f_{\text{edge-on,no}}$ ). We therefore implement a cut of  $f_{\text{edge-on,no}} > 0.3$  to ensure that observed red colours are an indicator of a lack of star-formation, and not dust-reddening (right panel).

a set of artificially-redshifted simulated galaxy images classified in Galaxy Zoo that vote fractions for a nominally featured galaxy at  $z = 0$  can differ sufficiently from those for the same galaxy at  $z = 1$  to change its morphological classification to elliptical (we will show the same in Section 3.1). This result implies that applying a redshift-independent  $f_{\text{features}}$  cut to identify discs will increasingly underestimate their true number at increasing redshift intervals. A set of artificially redshifted images was used to quantify and correct for this incompleteness in disc and elliptical detection. We describe this dataset in the next section.

### 3.1 FERENGI2 set of artificially redshifted galaxy images

FERENGI2 is a set of simulated galaxy images created using the FERENGI code (Barden et al. 2008). These were created from a parent sample of 936 nearby ( $z < 0.01$ ) SDSS galaxies, all of which had been previously classified in Galaxy Zoo 2 and were cross-matched against 2MASS (Skrutskie et al. 2006) to obtain  $J$  magnitudes and GALEX (Martin et al. 2005) to obtain NUV magnitudes, which were necessary to define a colour-colour separation using as similar as possible a criterion to that applied to the COSMOS sample. An “evolution factor” of  $e = -1$  was applied, which brightens each galaxy linearly with redshift:  $M' = M + ez$ , where  $M'$  is the corrected magnitude. This correction is performed to mimic the known physical increase of galaxy magnitude with redshift (Lilly et al. 1998; Loveday et al. 2011), and the value  $e = -1$  was chosen based on an analysis of spectra template models provided by Brinchmann et al. (2004), which showed that typical galaxies tend to evolve in brightness by one magnitude per redshift. Each galaxy was artificially red-



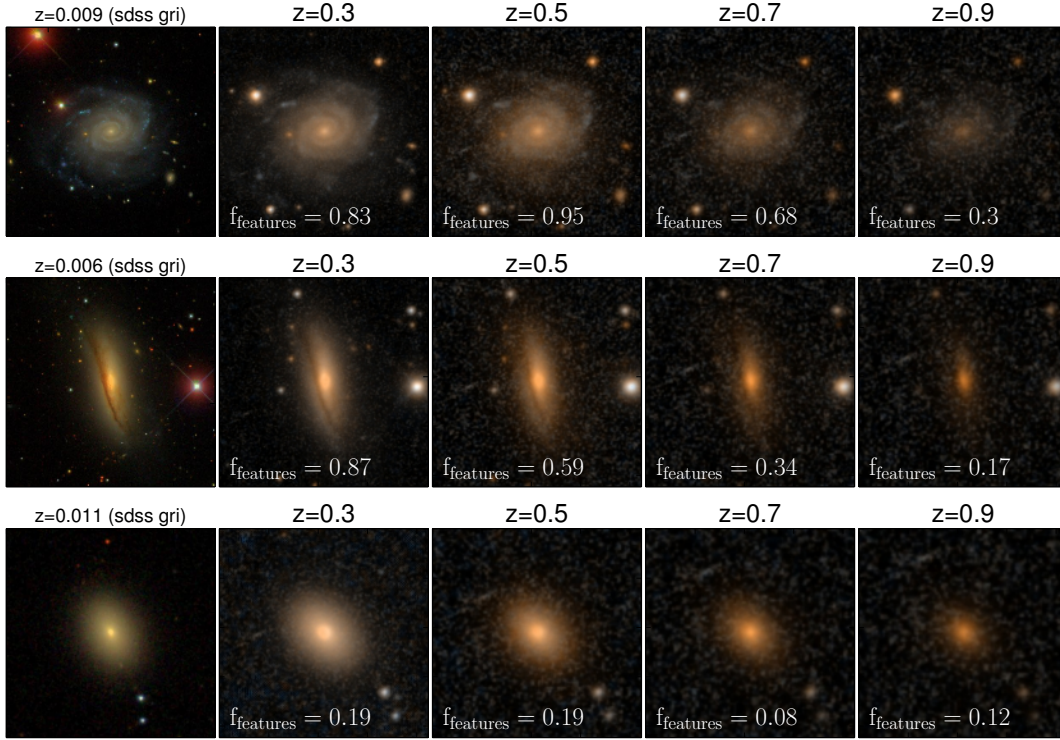
**Figure 3.** Separation of the passive population (red sequence) and active population (blue cloud) of the FERENGI2 sample. The gray shaded region represents the  $R-J$  limit of the sample. Combining the limit of  $r < 17$  that was adopted for the GZ2 dataset (of which the FERENGI2 galaxies are a subset), with the 2MASS magnitude limit of  $J < 15.91$ , yields a limiting colour for the FERENGI2 sample  $R - J < 1.1$ .

shifted to appear at 8 different distances between  $z = 0.3$  and  $z = 1$  in intervals of  $\Delta z = 0.1$  and processed to mimic *HST* imaging parameters, giving a total of 7,488 images (3 examples are shown in Figure 4). The set was then classified in Galaxy Zoo using the same decision tree as used for GZH. Highly inclined disc galaxies were removed from the sample by excluding any with  $N_{\text{edgeon}} > 20$  and  $f_{\text{not edge-on}} > 0.3$ , using the vote fraction associated with the real galaxy image measured in GZ2. This was to exclude those which may be mis-classified due to dust-reddening. Using the NUV- $J$ - $R$  selection method described in section 2.1, the remaining sample was divided into subsets of red sequence galaxies (259 per redshift bin) and blue cloud galaxies (543 per each redshift bin) (see Figure 3).

### 3.2 Measuring the completeness in disc and elliptical detection, $\xi$

The FERENGI2 dataset was used to measure the completeness/contamination in visual disc/elliptical detection, from which correction factors  $\xi_D$  and  $\xi_E$  were derived. These are defined as the number of discs/ellipticals detected divided by the true number of discs/ellipticals expected to exist in a given redshift interval:  $\xi_D(z) = N_{\text{discs detected}}/N_{\text{discs true}}$ , and  $\xi_E(z) = N_{\text{ellipticals detected}}/N_{\text{ellipticals true}}$ .

The completeness values  $\xi_D(z)$  and contamination values  $\xi_E(z)$  were computed for each of the 8 redshifts represented in the FERENGI2 dataset. An example calculation of  $\xi_D$  in the  $z = 0.7$  bin is shown in Figure 5. Each point represents a FERENGI2 galaxy, where the y-axis indicates values of  $f_{\text{features}}$  measured in the image redshifted to  $z = 0.7$ , and the x-axis indicates values of  $f_{\text{features}}$  measured in the same galaxy redshifted to  $z = 0.3$ . Disk galaxies are identified as those for which  $f_{\text{features}} \geq 0.3$ . Since, on average,  $f_{\text{features}}$  decreases for the same galaxy when it is viewed at higher redshifts, the number of galaxies meeting this thresh-



**Figure 4.** Example images of three galaxies artificially redshifted with the FERENGI code. The left image in each row is a real SDSS gri-composite image; the four to the right are images generated by FERENGI at varying redshifts, processed to mimic *HST/COSMOS* imaging. The  $f_{\text{features}}$  vote fraction for each simulated image is given; this value tends to decrease for each galaxy as it is processed to be viewed at higher redshifts.

old is always lower at higher redshifts than at  $z = 0.3$ . This is indicated by the dotted lines: galaxies to the right of the vertical dashed line at  $f_{\text{features}, z=0.3} = 0.3$  are identified as discs at  $z = 0.3$ ; their sum is considered the “true” number of discs,  $N_{\text{true}}$ . Similarly, the galaxies above the horizontal line at  $f_{\text{features}, z=0.7} = 0.3$  are identified as discs at  $z = 0.7$ ; their sum is the “detected” number of discs at  $z = 0.7$ , or  $N_{\text{discs detected}}$ . The figure makes it obvious that  $N_{\text{discs detected}}$  is much lower than  $N_{\text{discs true}}$ , emphasizing the increasing difficulty in detecting features at higher redshifts. Their ratio is the completeness  $\xi_D$ ; in this example  $\xi_D(z = 0.7) = 0.61$ , meaning only 61% of discs were detected at this redshift. This process was repeated for the elliptical galaxies in each bin, defined as those with  $f_{\text{features}} < 0.3$ . Conversely for the ellipticals,  $N_{\text{ellipticals, detected}}$  is always lower than  $N_{\text{ellipticals, true}}$ , yielding contamination factors  $\xi_E > 1$  in each redshift bin. Measurements of  $\xi_D$  and  $\xi_E$  for each redshift interval are shown in the right panels of Figure 6.

It was possible that completeness/contamination in disc/elliptical detection may be a function of other parameters in addition to redshift. For example, at fixed redshift, it is a reasonable supposition that features could be easier to detect in galaxies that have higher mass, radius, or surface brightness. To test whether these parameters also impact the number of discs/ellipticals detected,  $\xi_D$  and  $\xi_E$  were measured in fixed redshift bins as functions of surface brightness, effective radius, and mass. The surface brightness was

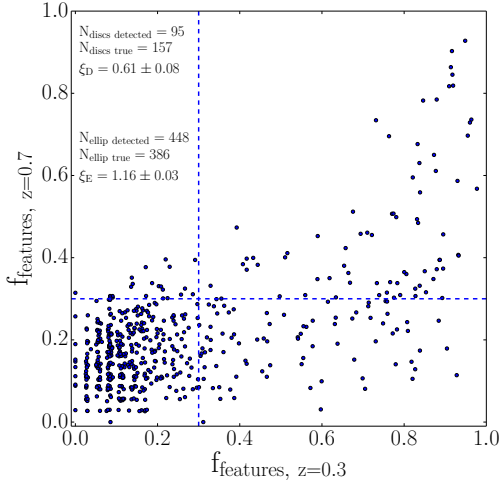
calculated as  $\mu = m + 2.5 \times \log_{10}(2 \times (b/a) \times \pi R_e^2)$ , using `MAG_AUTO`,  $b/a$  and  $R_e$ , derived by the `SEXTRACTOR` (Bertin & Arnouts 1996) utility using the  $I_{814W}$  band images. The effective radius used was the 50% `FLUX_RADIUS` converted to kpc, and the masses used were the `MEDIAN` values in the MPA-JHU DR7 catalog (Kauffmann et al. 2003). Similar to Willett et al. (2016), who found no effect on  $f_{\text{features}}$  with surface brightness, we did not detect any effect on  $\xi_D$  or  $\xi_E$  with any of the above parameters.

As a final check, we computed  $\xi_D$  and  $\xi_E$  as functions of redshift for the blue cloud and the red sequence separately, to detect any color-dependence on disc/elliptical detection; results are shown in the left panel of Figure 6.  $\xi_{RD}$  and  $\xi_{BD}$  refer to the completeness of red and blue disc galaxies, and  $\xi_{RE}/\xi_{BE}$  refer to the contamination of red and blue ellipticals. No significant difference was detected between the two populations, which is apparent from the overlapping  $1\sigma$  errors on the plot.  $\xi_D$  and  $\xi_E$  were computed for the combined red and blue populations in bins of redshift between 0.3 and 1.0 with widths  $\Delta z = 0.1$ . Linear relationships for  $\xi_D$  and  $\xi_E$  as functions of redshift were derived:

$$\begin{aligned}\xi_D(z) &= (-0.97 \pm 0.04)(z) + 1.29 \pm 0.02 \\ \xi_E(z) &= (0.32 \pm 0.02)(z) + 0.90 \pm 0.01\end{aligned}\quad (3)$$

where the errors represent the  $1\sigma$  deviations on the fit of the slope and intercept for each equation. These corrections





**Figure 5.** Example calculation of completeness/contamination  $\xi_D/\xi_E$  at redshift  $z = 0.7$ . Points represent GZ classifications of FERENG12 images. The y-axis corresponds to the value of  $f_{\text{features}}$  measured at the galaxy redshifted to  $z = 0.7$ , and the x-axis corresponds to the value of  $f_{\text{features}}$  measured at the galaxy redshifted to  $z = 0.3$ . On average, the  $f_{\text{features}}$  is lower at the higher redshift, indicating classifiers on average have more difficulty identifying features in images modelling higher redshifts. The dotted lines correspond to the threshold  $f_{\text{features}}=0.3$ , above which a galaxy is considered to have a disc. Galaxies to the right of the vertical dashed line were identified as discs at the lowest redshift  $z = 0.3$ . The total number of such galaxies is denoted  $N_{\text{discs true}}$ , and is defined to represent the true number of disc-like galaxies. Galaxies above the horizontal dash line were identified as discs at the higher redshift  $z = 0.7$ , and their total number is denoted  $N_{\text{discs detected}}$ . The ratio  $\xi_D = N_{\text{discs detected}}/N_{\text{discs true}}$  is the completeness value; in this example, only 61% of discs were detected at  $z = 0.7$ . Conversely, a contamination of 1.16% of ellipticals were detected. Errors on the displayed  $\xi_D$  and  $\xi_E$  are 95% Bayesian binomial confidence intervals (Cameron 2013)

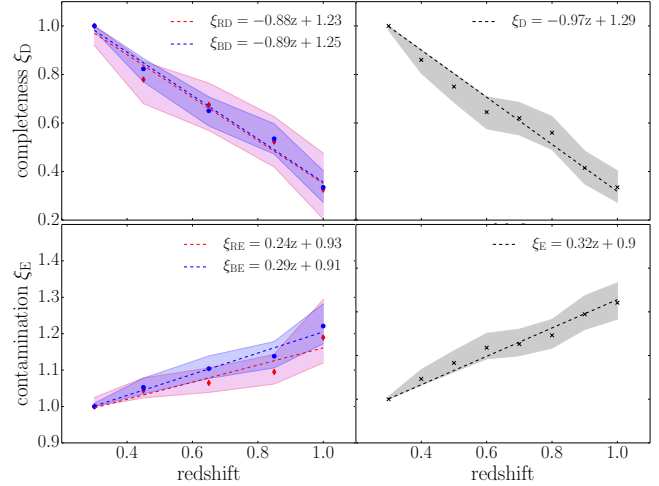
were used to calculate the corrected number of each color-morphological type as follows:

$$\begin{aligned} N'_{BD}(z) &= N_{BD}(z) \times \xi_D^{-1}(z) \\ N'_{RD}(z) &= N_{RD}(z) \times \xi_D^{-1}(z) \\ N'_{BE}(z) &= N_{BE}(z) \times \xi_E^{-1}(z) \\ N'_{RE}(z) &= N_{RE}(z) \times \xi_E^{-1}(z) \end{aligned} \quad (4)$$

where unprimed numbers refer to the raw number counts of blue disks (BD), red disks (RD), blue ellipticals (BE), and red ellipticals (RE) in a given redshift interval in the GZH sample, and primed numbers represent the completeness/contamination-corrected values. Tables of all raw and corrected counts in bins of stellar mass and redshift are given in Appendix B.

## 4 RESULTS

In this section we present our results for the evolution of the fraction of star-forming and quenched disc and ellipti-

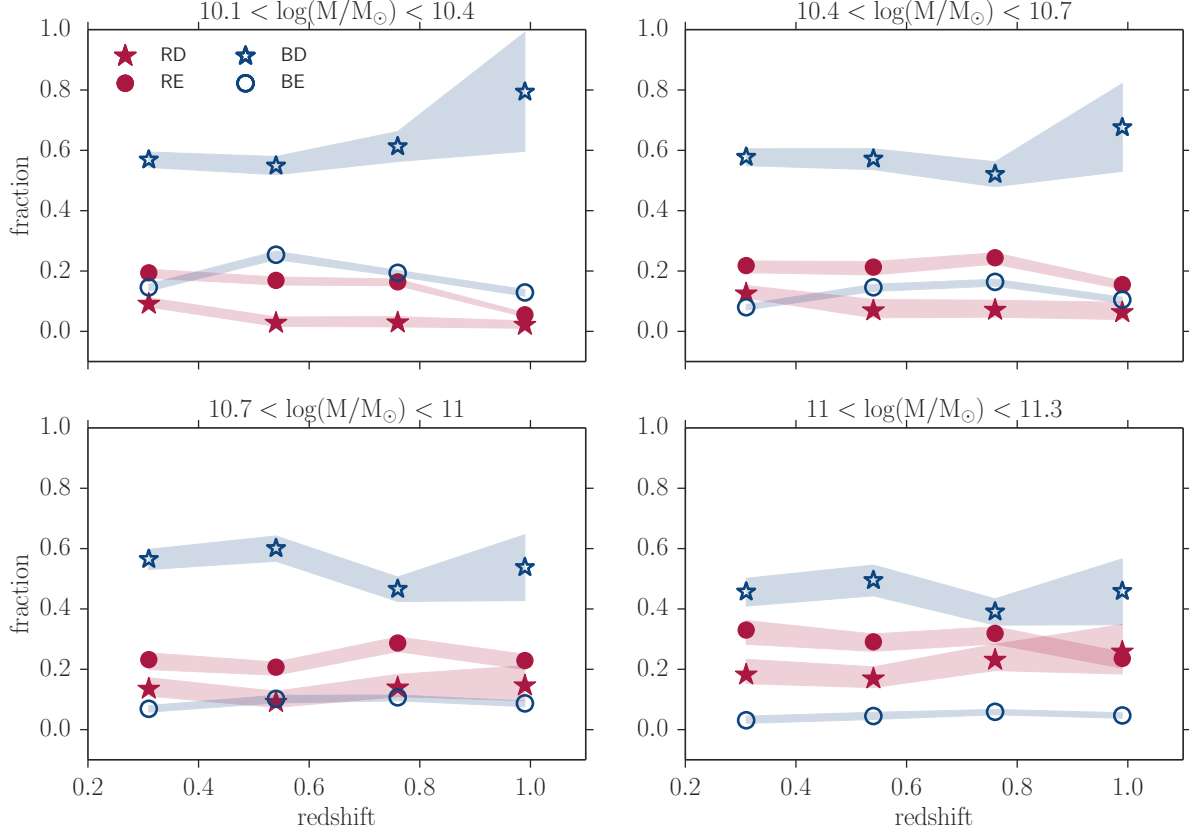


**Figure 6. Left:** Completeness  $\xi_{RD}$  and  $\xi_{BD}$  (top) and contamination  $\xi_{RE}$  and  $\xi_{BE}$  (bottom) as functions of redshift for red sequence and blue cloud FERENG12 galaxies separately. All show a clear dependence on  $\xi$  with redshift, but there is no strong difference in completeness for the red and blue populations. **Right:** Completeness  $\xi_D$  (top) and  $\xi_E$  (bottom) as a function of redshift for all FERENG12 galaxies (red and blue combined). The equation representing the linear fit for each is displayed. Shaded regions represent the 95% Bayesian binomial confidence intervals around each point (Cameron 2013).

cal galaxies from  $z = 1$  to  $z = 0.3$  in a sample of 20,811 *COSMOS* galaxies morphologically classified in GZH. In Figure 7, we divide our sample into four bins of galaxy stellar mass and plot how the fractional contributions of all four colour-morphology permutations vary as a function of redshift, using the corrected number counts (Equation 4). In discussing these results, we refer to increases/decreases in these fractions with respect to *increasing* cosmic time; that is, from right to left in the plots shown in Figures 78.

In Figure 7 we find blue discs are the plurality population at each redshift for all mass bins. At fixed redshift, the abundance of the red disc population is maximised in the highest mass bin and decreases monotonically towards lower masses. Red ellipticals tend to significantly outnumber red discs except in the highest mass/redshift bin, where the population sizes are almost equal. Blue ellipticals represent an insignificant fraction for galaxies with mass  $\log(M/M_\odot) > 10.7$ , but begin to outnumber the red disc population at lower masses.

Red disc galaxies are presumed to form primarily from blue discs galaxies which have quenched without undergoing a morphological transformation. If this is true, and if the resulting quenched discs do not continue in their evolution, one would expect a “pile up” of red discs at later times, resulting in an increasing fraction at lower redshift. This trend is observed in the two lowest mass bins, however there is no large change in the fractional contribution of red disks to the total population in the  $\log(M/M_\odot) \sim 10.85$  bin, and even a small decrease in the highest mass bin. If we assume that red discs are continuously produced from blue discs, even at a small rate, then a constant or decreasing fraction can only be explained if their numbers are simultaneously being



**Figure 7.** Evolution of four types of galaxy populations since  $z = 1$ : blue discs (blue open stars), red discs (red closed stars), blue ellipticals (blue open circles), and red ellipticals (red closed circles). Each point represents the fraction of the indicated type with respect to the total population, such that all points in a given redshift, mass bin sum to 1. Statistical errors were calculated as propagations of multinomial counting errors and the errors associated with the functional fits to the correction terms  $\xi_D$  and  $\xi_E$ . Systematic errors were calculated by bootstrapping the classifier votes for each galaxy and re-calculating the fractional contributions of each type; errors were taken as the  $1\sigma$  dispersion in the fractions. The total error, represented by the shaded regions, is the statistical and systematic errors added in quadrature.

depleted, presumably by a morphological transformation to red elliptical.

To better assess the evolution of the red disk population with respect to all discs and to the red sequence, we define to fractional quantities: the red disc fraction  $f_{R|D}$ , and the red sequence disc fraction,  $f_{D|R}$ , defined explicitly:

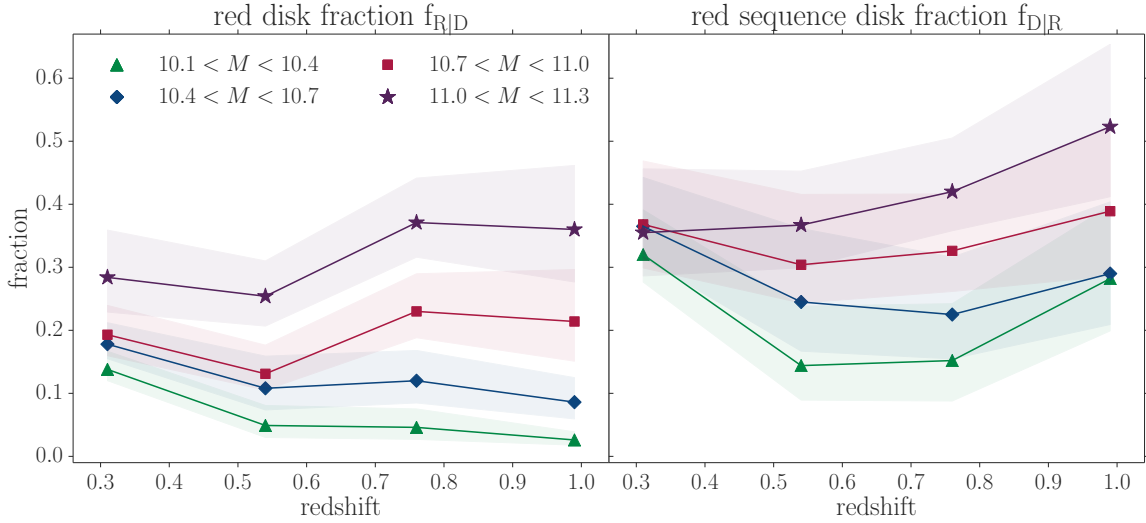
$$f_{R|D} = \frac{N'_{RD}}{N'_{RD} + N'_{BD}} \quad (5)$$

$$f_{D|R} = \frac{N'_{RD}}{N'_{RD} + N'_{RE}} \quad (6)$$

Maintaining an identical subdivision of our parent sample in  $M_* - z$  space, equations 5 (left-panel) and 6 (right-panel) were evaluated for each subsample to yield the curves plotted in Figure 8. We observe a mass-dependence in both fractions. At fixed redshift, both  $f_{R|D}$  and  $f_{D|R}$  tend to increase with increasing mass; this is a consequence of the higher abundance of red discs observed at high masses, as seen in Figure 7.

Given the large errors on some of the fractions (particularly for  $f_{D|R}$ ), we check whether  $f_{R|D}$  and  $f_{D|R}$  increase,

decrease, or remain constant as functions of redshift in each mass bin by fitting the data to a linear function and evaluating if their slope is consistent with zero, defined as such if zero exists within the  $1\sigma$  errors on the slope. We find that the red disc fraction  $f_{R|D}$  decreases for the highest mass bin, is constant for  $\log(M/M_\odot) \sim 10.85$ , and increases for the two lower mass bins  $\log(M/M_\odot) < 0.7$ . An increase in  $f_{R|D}$  could be driven by the increase of red discs or a depletion of blue discs; Figure 7 shows the increase may be driven more from the latter at  $z \sim 1$ , and the former at lower redshift. On the right, we find a decrease in the red sequence disc fraction  $f_{D|R}$  for all masses in the interval from  $z \sim 1$  to  $z \sim 0.8$ . Figure 7 shows that this is mainly driven by the increase in red ellipticals during this time, which is consistent with higher merger rates at this epoch (Molina et al. 2016). From  $z \sim 0.8$  to  $z \sim 0.3$ ,  $f_{D|R}$  continues to decrease for galaxies  $\log(M/M_\odot) > 11$ , becomes constant for galaxies  $\log(M/M_\odot) \sim 10.85$ , and increases for the lower mass bins. Figure 7 reveals that the enhancement of  $f_{D|R}$  among the low mass population is driven more by increases in the proportion of red discs, and rather than a depletion of red ellipticals. The increase of  $f_{R|D}$  and  $f_{D|R}$  with redshift ob-



**Figure 8.** **Left:** Red disc fraction ( $f_{R|D} = N'_{RD}/(N'_{RD} + N'_{BD})$ , equation 5) vs redshift in four mass bins. **Right:** Red sequence disc fraction ( $f_{D|R} = N'_{RD}/(N'_{RD} + N'_{RE})$ , equation 6) vs redshift in four mass bins. Statistical errors were calculated as propagations of multinomial counting errors and the errors associated with the functional fits to the correction terms  $\xi_D$  and  $\xi_E$ . Systematic errors were calculated by bootstrapping the classifier votes for each galaxy and re-calculating the fractional contributions of each type; errors were taken as the  $1\sigma$  dispersion in the fractions. The total error, represented by the shaded regions, is the statistical and systematic errors added in quadrature.

served at low masses, coupled with the constant or decreasing trends for high masses, suggests that low mass red disc galaxies may be more likely to remain as such, while more massive red disc galaxies are more likely to evolve further via a morphological transformation. We explore the potential drivers of these trends in terms of different evolutionary quenching pathways in detail in Section 5.

The downward trend we observe in the red sequence disc fraction  $f_{D|R}$  for massive galaxies is in agreement with Bundy et al. (2010) (hereafter B10) who perform a similar analysis of the morphological makeup of the red sequence. As stated previously, a downward trend of  $f_{D|R}$  represents either a depletion of the total pool of red discs (via a transformation to elliptical), but could also be an indication of an increase in the pool of red ellipticals (which could result from blue or red discs transforming morphology). In contrast, an upward trend is only possible via a pile-up of red discs, which is what we observe for the lower mass bins, and is in disagreement with B10. At the lowest redshift bin ( $z \sim 0.3$ ), we measure similar absolute fractions of discs occupying the red sequence for all masses. However, B10 find the contribution of low mass galaxies to increase at higher lookback time to  $z = 1$ , while we find a decreasing contribution.

The fact that our results agree for the highest mass at all redshifts, but only at the lowest redshift for lower masses, suggests the differences may be attributed in biases in morphological classification. B10 segregates early and late-type disc galaxies using ZEST (Scarlata et al. 2007) morphologies, which they acknowledge are biased towards disc classification for faint apparent magnitudes, which tend to be associated with the lowest mass, highest redshift objects. This bias could influence their observed increase in red sequence discs toward  $z = 1$  for low masses. Conversely, GZ classifications tend to be biased towards elliptical morphologies at

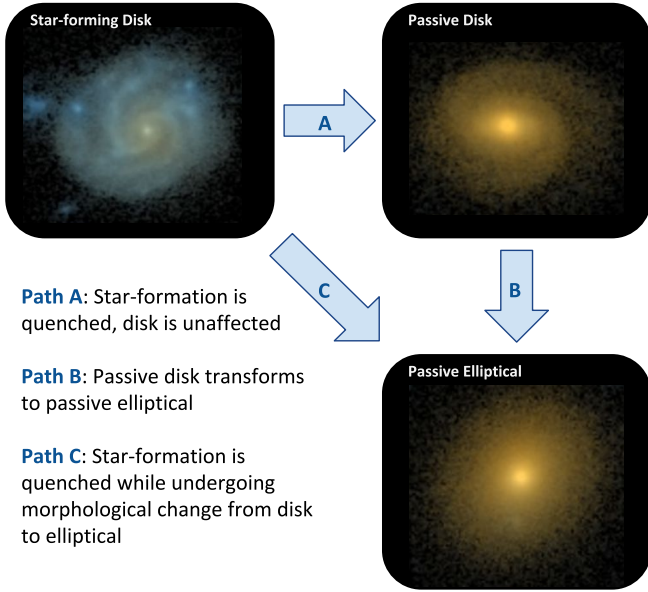
fainter magnitudes. Our attempt to quantify and correct for this effect is described in Section 3.1, but an underestimation of our correction function may have driven the apparently decreasing abundance of disc galaxies observed at increasing redshift for low masses. However, it has been shown that red disc galaxies in the local Universe tend to be more massive, as in Masters et al. (2010). If this is true at all epochs, we would not expect such a significant contribution by red discs to the low-mass galaxy population as found in B10.

## 5 DISCUSSION

We have examined the evolution of red disc galaxies since  $z = 1$  in Figures 7 and 8. Different trends in the abundance of red discs for distinct stellar mass bins are observed, which are consistent with a physical scenario in which 1) more massive galaxies undergo morphological transformations to elliptical at a higher rate than their less massive counterparts (implied by the decrease/increase of  $f_{D|R}$  from  $z = 1$  to  $z = 0.3$  for high/low mass bins), and 2) more massive galaxies are more likely to enter a red disc phase to begin with (implied by the higher proportion of red discs in the high mass bin of Figure 7).

Figure 9 is a simple schematic of dominant quenching pathways for typical galaxies. Path A represents the creation of red discs via a quenching mechanism which does not transform the morphology of a blue star-forming disc. Path B represents a morphological transformation of a red disc to a red elliptical galaxy. Path C represents the quenching of blue discs via a mechanism which simultaneously invokes a morphological transformation. If all galaxies adhered to the standard color-morphology relationship, one could deduce that all galaxies follow this path. The existence of the red disc population asserts that Path A is also a viable channel. If these were the only two channels, we would expect pile





**Figure 9.** Cartoon representing three common evolutionary pathways of star-forming disc galaxies. Path A represents an active star-forming galaxy which quenches without destroying the disc, becoming a red disc. Path B represents a red disc morphologically transition to red elliptical. Path C represents a blue discs simultaneously quenching and morphologically transforming to become a red elliptical.

ups of red discs at all masses as the Universe evolves. We observed such pile ups for low mass red disc galaxies (Figures 7 and 8), but not for massive galaxies. This suggests that Path B, the depletion of red discs via a later morphological transformation, is necessary to deplete the pool and counteract the pile up effect, and has increasing significance in higher mass galaxies.

### 5.1 Red disc fraction ( $f_{R|D}$ ) and red sequence disc fraction ( $f_{D|R}$ ): limiting cases

To help understand the influences of the different quenching mechanisms Paths A, B, and C (Figure 9), we explore limiting cases of the relative rates of these pathways and their influence on the red disc and red sequence disc fractions. A summary of these effects are displayed in Table 1. As in the previous section, we only discuss increases/decreases in fractions with *increasing* cosmic time; that is, from right to left in the plots shown in Figure 8.

#### 5.1.1 Limiting case 1: Path A only

In this scenario, blue discs may quench and retain their disc structure, but no morphological transformation occurs for either type. This results a depletion in the the number of blue discs at an equivalent rate as the build-up of red discs. A decrease in blue discs and increase in red discs both result in increases in  $f_{R|D}$ , so we would observe only increasing values of  $f_{R|D}$  in Figure 8. Similarly, an increase in red discs coupled with no change in red ellipticals would result in a pure increase of the fraction of discs on the red sequence,  $f_{D|R}$ .

The creation of red discs via Path A requires quenching mechanisms which do not significantly alter the disc’s morphology. Possible mechanisms include mass-quenching or AGN-feedback, which both induce quenching by cutting of the galaxy’s gas reservoir required for ongoing star-formation. Mass-quenching occurs when a galaxy halo grows to a critical mass that induces virial shocks which heat the gas (Schawinski et al. 2007; Birnboim & Dekel 2003; Cattaneo et al. 2006). Since this type occurs in high mass galaxies, this could explain the increasing abundance of red discs observed in the higher mass bins (Figure 7). Dilution of gas in massive galaxies due to such shock-induced heating can cause it to become more vulnerable to AGN feedback (Dekel & Birnboim 2006), whereby accretion onto the galaxy’s supermassive black hole generates strong outflows of energetic material and hard, non-thermal radiation. These AGN-driven winds may then terminate star-formation by heating the gas or expelling it completely from the galaxy, causing a quench. Such a process is not likely to induce a morphological transformation, and therefore could be another valid mechanism for creating a quenched disc.

Red discs can also be the product of merger events. Simulations have shown cases of rotationally supported discs surviving or reforming after a major merger. This seems to be possible under conditions such that the progenitor discs are gas-dominated (Governato et al. 2009; Springel & Hernquist 2005); for Robertson et al. (2006) discs were only reformed if the gas-fractions exceeded  $f_{gas} > 0.5$ . Under these conditions, it would be more likely to form low-mass discs, given that gas fraction tends to anti-correlated with stellar mass (Kannappan 2004; Bell & De Jong 2000). Perhaps this mechanism could explain some portion of the low-mass red disc population. However, regrown discs in these simulations tend to exhibit star-formation activity. If the merger-disc regrowth event enhances star-formation only briefly, then perhaps the remaining gas is used up on a shorter time-scale, leading to a low-mass red disc. Sparre & Springel (2017) find that although most of the new discs were star-forming, some were immediately quenched in simulations which incorporated particularly strong AGN feedback.

#### 5.1.2 Limiting case 2: Path B only

Path B represents the depletion of red discs as they morphologically evolve to build up the population of red ellipticals. If blue discs are no longer quenching to build up the population of red discs, then we would only observe decreases in both  $f_{R|D}$  and  $f_{D|R}$  as the number of red discs decreases, blue discs remain constant, and red ellipticals increase.

Our results suggests that Path B, the morphological transformation of red discs, is more common for high mass red discs than their low mass counterparts. It has been long suggested that major-mergers are the dominant mechanism for transforming the majority disc-like galaxies to an elliptical morphology (Toomre 1977; Schweizer 1982; Schweizer et al. 1990), with multiple minor-mergers being the second-most dominant (Bundy et al. 2009; Hopkins et al. 2010a). Studies using observations of close pairs have shown the galaxy merger rate increases with mass, both in the local Universe (Xu et al. 2004; Patton & Atfield 2008; Domingue et al. 2009; Robotham et al. 2014; Casteels et al. 2014) and out to  $z \sim 1$  (Xu et al. 2012; Bundy et al. 2009), which

agrees with predictions from both empirical models and dynamical simulations (Hopkins et al. 2010b,a; Maller et al. 2006). Casteels et al. (2014) find the merger rate is as much as three times higher for massive ( $\log(M/M_\odot) \sim 11.25$ ) than for lower mass ( $\log(M/M_\odot) \sim 8.25$ ) galaxies, using a similar mass range probed in our study. The increasing merger rate with mass may explain why massive red disc galaxies do not tend to stay in this phase long before merging, while low mass galaxies which become red discs are more persistent in that phase.

### 5.1.3 Limiting case 3: Path C only

We now consider the scenario in which blue disc galaxies only quench via processes which simultaneously destroy their discs. The most extreme consequence of this scenario is of course a complete absence of red disc galaxies, which would give  $f_{R|D} = f_{D|R} = 0$  for all redshifts. Allowing for an initial population of red discs, we can explore how  $f_{R|D}$  and  $f_{D|R}$  would evolve if Path C were to suddenly become the only option.

The evolution of  $f_{R|D}$  is dependent on the growth/depletion of red and blue discs. In this scenario red discs are not building up, nor are they transforming morphologically; therefore their number remains constant, and the evolution of  $f_{R|D}$  is solely dependent on the blue discs. If blue discs only evolve via path C, their number could only decrease, leading to an overall increase of  $f_{R|D}$ .  $f_{D|R}$  in this scenario is only affected by the net change of red ellipticals, whose numbers are increasing via Path C. Therefore this scenario would give a decrease of  $f_{D|R}$ .

### 5.1.4 Limiting case 4: No quenching pathways, only mass growth via star-formation

Even in the limiting scenario in which there are no quenching mechanisms or morphological transformations, the fractions in Figures 7 and 8 would evolve due to star-formation in the blue discs. In a given mass bin, blue discs may enter from a lower mass bin or exit to enter a higher mass bin as they continuously increase their mass via star-formation. The net rate of blue galaxies entering/leaving a mass bin via star-formation can be estimated by the mass derivative of the mass function of blue galaxies times the specific star-formation rate  $d\phi_{blue}/dm \times sSFR(m, t)$  (Peng et al. 2010). Using a Schechter (1976) mass function,  $d\phi_{blue}/dm = (1 + \alpha_s) - m/M^*$  with  $\alpha_s = -1.4$  and  $M^* = 10.28$  ( $\log(M/M_\odot)$ ) (Ichikawa & Matsuoka 2017) and specific star-formation rate given by Peng et al. (2010)  $sSFR(t) = 2.5(\frac{t}{3.5\text{Gyr}})^{-2.2}\text{Gyr}^{-1}$ , we find the net rate of change of blue discs *due to star-formation only* is always positive for the masses and redshifts considered in Figure 8.

Therefore, in the absence of quenching, we would observe a steady increase of the fraction of blue discs in Figure 7. The flatness observed suggests that their numbers are depleting via Paths B or C at similar rates as their numbers are replenishing each bin via star-formation. In  $f_{R|D}$  we would only observe a decrease as the number of blue discs increased, and  $f_{D|R}$  would remain constant as the number of blue discs do not enter the equation.

net effect on:	$f_{R D}$	$f_{D R}$
Path A only	↑	↑
Path B only	↓	↓
Path C only	↑	↓
star-formation only	↓	no effect

**Table 1.** Net effects on the red disc fraction  $f_{R|D}$  and red sequence disc fraction  $f_{D|R}$  for limiting single-scenario cases of transformative pathways A, B, C (Figure 9) and mass growth via star-formation. ↑ represents an increase in respective fractions with increasing cosmic time / decreasing redshift (right to left in Figure 8). This information can be used to find the dominant effects driving the trends in Figure 8.

## 5.2 Identifying the dominant transformative pathways as a function of mass

[This is the dryest of the dry sections and to be honest I'm not sure if this should be laid out all in words or if it's best summarizing all of this in another table] In the context of the above discussion outlining the net effects of Paths A, B, C, and mass growth via star-formation, we will summarize the trends observed in Figure 8 for each stellar mass bin and identify the most probable drivers of the trends.

### 5.2.1 $11.0 < \log(M/M_\odot) < 11.3$

For galaxies in the highest mass bin,  $f_{R|D}$  decreases from 0.36 to 0.28 since  $z = 1$ . This suggests that the rate of occurrence of Path B, the morphological transformation of red discs to elliptical, is strong with respect to paths A or C. Via Table 1 it is possible that star-formation has an impact in this trend, however it is not expected to be the dominant driver given the flatness of the fraction of blue discs observed in Figure 7.

$f_{D|R}$  decreases from 0.52 to 0.36, which could be driven by Path B or C. Given that a dominant Path C would cause an increase in  $f_{R|D}$  (opposite of what we observe), it is more likely that Path B is the primary driver of this decrease.

### 5.2.2 $10.7 < \log(M/M_\odot) < 11.0$

For galaxies in the second highest mass bin,  $f_{R|D}$  is consistent with a slope of zero. This suggests that the rate of Path B is on par with the combined rates of A and C. As with the highest mass, star-formation is not expected to be a dominant contribution due to the flatness of the blue disc fraction in Figure 7.

$f_{D|R}$  is also consistent with a slope of zero. This suggests Path A is significantly strong to balance the decreasing effects of Paths B and C.

### 5.2.3 $10.4 < \log(M/M_\odot) < 10.7$

For galaxies in the second lowest mass bin,  $f_{R|D}$  increases from 0.09 to 0.12. This indicates that paths A and C are dominating, meaning path B is less dominant as compared to the higher masses.

$f_{D|R}$  increases from 0.29 to 0.37. This indicates that Path A dominates over both B and C.

### 5.2.4 $10.1 < \log(M/M_\odot) < 10.4$

$f_{R|D}$  increases from 0.03 to 0.14, indicating path B is not significant compared to A and C.

$f_{D|R}$  is consistent with a slope of zero, indicating the rate of Path A is comparable to the combined effect of B and C.

A summary of the above breakdown is as follows: Path B, the depletion of red discs via a morphological transformation to elliptical, operates at a higher frequency for more massive galaxies than the lower mass galaxies. In other words, lower mass galaxies are more likely to remain in a red disc phase, while high mass red discs are more likely to merge and transition to elliptical. Path A, the creation of red discs, is strongest for high masses, given by the trends of  $f_{R|D}$ ,  $f_{D|R}$  and the larger abundance of red discs in the higher mass bins.

### 5.3 Looking forward: developing a model to reproduce observations

Through observations of the evolution of the red disc population since  $z = 1$ , we have deduced that massive galaxies are more likely to both enter a red disc phase and subsequently exit the stage via a morphological transformation, while low mass discs which enter a passive stage are more likely to remain in that phase than continue their evolution. To quantify and verify this interpretation would require further work, such as a semi-analytical model which could reproduce these observations given parameters describing the rate of occurrences of the different evolutionary pathways shown in Figure 9. A complete model is beyond the scope of this work, but an example of a simple toy-model approach is given in Appendix A. Our simple model was not able to constrain values for all parameters implemented, but it did detect a mass-dependence on the rate at which blue discs transform to red discs, which agrees with our interpretations thus far.

## 6 CONCLUSIONS

We have investigated the population of passive disc galaxies across a range of stellar masses and redshifts from  $z=1$  to the present epoch. We used morphological classifications from Galaxy Zoo: Hubble and rest-frame colours from UltraVISTA. Using data from artificially-redshifted FERENGI2 images to quantify the known redshift bias in the GZ classifications, we derived expressions to correct the incompleteness in the number of discs and ellipticals detected as a function of redshift. The relative population statistics were described in terms of the fraction of disc galaxies that are red  $f_{R|D}$  and the fraction of disc galaxies on the red sequence  $f_{D|R}$ . Our main conclusions are as follows:

- $f_{R|D}$  and  $f_{D|R}$  decrease from  $z = 1$  to  $z = 0.3$  for massive galaxies, and increase for the least massive galaxies.
- Low mass galaxies which experience a passive disc phase are more likely than massive galaxies to remain discs, while massive galaxies are more likely to continue their evolution by transforming to passive ellipticals. Additional data are required to properly constrain semi-analytic models that

might further elucidate the physical processes that generate the observed population trends.

## ACKNOWLEDGEMENTS

The data in this paper are the result of the efforts of the Galaxy Zoo Hubble volunteers, without whom none of this work would be possible. Their efforts are individually acknowledged at [authors.galaxyzoo.org](http://authors.galaxyzoo.org). Please contact the author(s) to request access to research materials discussed in this paper.

MG, CS, MB, and LF gratefully acknowledge support from the US National Science Foundation Grant AST1413610. RS gratefully acknowledges funding from the Ogden Trust.

This publication makes use of data products from the Two Micron All Sky Survey, which is a joint project of the University of Massachusetts and the Infrared Processing and Analysis Center/California Institute of Technology, funded by the National Aeronautics and Space Administration and the National Science Foundation.

This project made heavy use of the Astropy packages in Python (Robitaille et al. 2013), the *seaborn* plotting package (Waskom et al. 2015), and the Tool for OPERations on Catalogues And Tables (TOPCAT), which can be found at [www.starlink.ac.uk/topcat/](http://www.starlink.ac.uk/topcat/) (Taylor 2005).

Funding for the SDSS and SDSS-II has been provided by the Alfred P. Sloan Foundation, the Participating Institutions, the National Science Foundation, the U.S. Department of Energy, the National Aeronautics and Space Administration, the Japanese Monbukagakusho, the Max Planck Society, and the Higher Education Funding Council for England. The SDSS website is <http://www.sdss.org/>.

The SDSS is managed by the Astrophysical Research Consortium for the Participating Institutions. The Participating Institutions are the American Museum of Natural History, Astrophysical Institute Potsdam, University of Basel, University of Cambridge, Case Western Reserve University, University of Chicago, Drexel University, Fermilab, the Institute for Advanced Study, the Japan Participation Group, Johns Hopkins University, the Joint Institute for Nuclear Astrophysics, the Kavli Institute for Particle Astrophysics and Cosmology, the Korean Scientist Group, the Chinese Academy of Sciences (LAMOST), Los Alamos National Laboratory, the Max-Planck-Institute for Astronomy (MPIA), the Max-Planck-Institute for Astrophysics (MPA), New Mexico State University, Ohio State University, University of Pittsburgh, University of Portsmouth, Princeton University, the United States Naval Observatory and the University of Washington.

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## APPENDIX A: TOY-MODEL APPROACH TO CONSTRAIN RATES OF DIFFERENT EVOLUTIONARY PATHWAYS

Our observations of the fractional evolution of different morphological and activity types of galaxies since  $z = 1$  are well-suited for the implementation of a model to constrain the frequencies of different evolutionary pathways. Here we present a toy model designed to reproduce our observations, given different sets of input parameters. This pilot study is expected to initiate further development of a sophisticated, semi-analytic model to describe and constrain potential rates of quenching and morphological evolution.

We implement a model to track the change in  $f_{R|D}$  and  $f_{D|R}$ , given a range of parameters representing the quenching and morphological transformation rates for galaxies at fixed stellar mass. We begin by considering the rate of change in the number of blue discs ( $dN_{BD}/dt$ ), red discs ( $dN_{RD}/dt$ ), and red ellipticals ( $dN_{RE}/dt$ ). In a given mass bin, the change in numbers for each population will depend on several parameters, illustrated visually in Figure 9.

### A1 Blue Disks

Galaxies in a blue bin may transition into a red disc bin via a quenching process that does not destroy its disc; we define this rate as  $r_{BD \rightarrow RD}$ , representing the fraction of blue galaxies to transition to red discs per Gyr (path A in Figure 9). Blue galaxies may also exit a bin via a quenching process which *does* destroy the disc; this fraction per Gyr we define as  $r_{BD \rightarrow RE}$  (path C in Figure 9).

The number of galaxies in a blue disc bin will also change due to star formation, which brings active galaxies from a lower mass bin into the current mass bin. To account for this term we use the formalism outlined by Peng et al. (2010), in which this rate of change is given by  $(\alpha + \beta)sSFR$ . Here  $\alpha = d\phi_{blue}/dm$  is the derivative of the mass function for blue galaxies, which equates to  $\alpha = (1 + \alpha_s) - m/M^*$  for a mass function described by the Schechter (1976) function. We use best-fit parameters for blue galaxies measured by Ichikawa & Matsuoka (2017), which give  $\alpha_s = -1.4$  and  $M^* = 10.28$  ( $\log(M/M_\odot)$ ). Following the method of Peng et al. (2010), we let  $\beta = 0$ , both for simplicity, and because their conclusions found not to be strongly dependent on  $\beta$ . Finally, the specific star-formation rate is given by  $sSFR(t) = 2.5(\frac{t}{3.5 \text{ Gyr}})^{-2.2} \text{ Gyr}^{-1}$  (Peng et al. 2010).

Accounting for all sources and sinks of blue discs entering or exiting a bin of given mass, the rate of change of blue discs can be written fully as:

$$\left. \frac{dN_{BD}}{dt} \right|_m = \left( -r_{BD \rightarrow RD} - r_{BD \rightarrow RE} - \alpha(m)sSFR(t) \right) N_{BD} \quad (\text{A1})$$

#### A1.1 Red Disks

Galaxies exiting a blue bin as they quenched without disrupting their discs enter the pool of red discs, increasing  $N_{RD}$  for a given mass bin. Red discs also may undergo a morphological transformation, depleting the pool of red discs as they enter the red elliptical bin (path B in Figure 9). The fraction of galaxies to undergo this pathway per

Gyr is denoted as  $r_{RD \rightarrow RE}$ . Combining these factors gives the expression:

$$\left. \frac{dN_{RD}}{dt} \right|_m = +r_{BD \rightarrow RD}N_{BD} - r_{RD \rightarrow RE}N_{RD} \quad (\text{A2})$$

### A2 Red Ellipticals

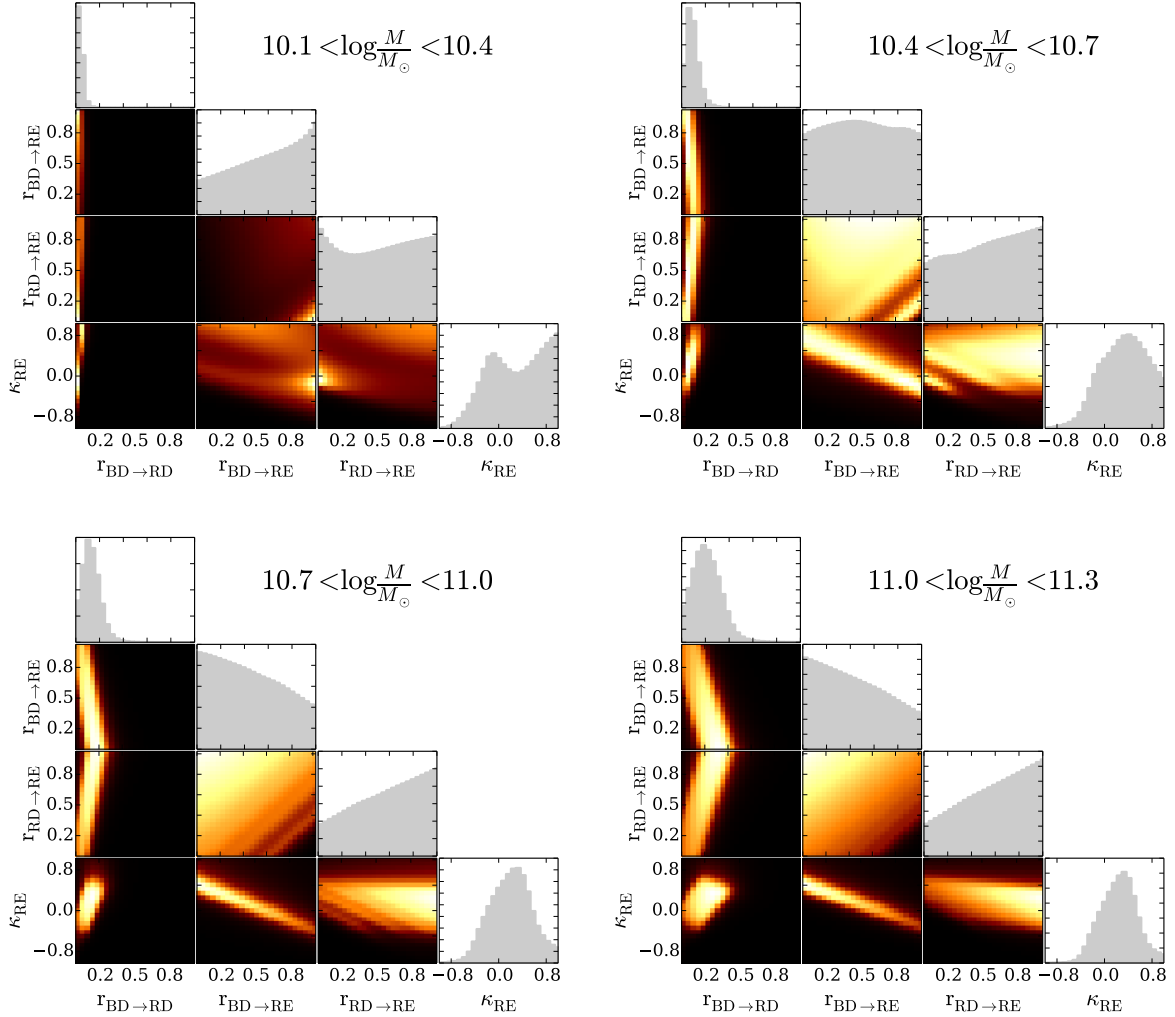
In this simple model, it is assumed that red, passive ellipticals are the final state in a typical galaxy's evolution. Therefore  $N_{RE}$  will always be increasing from the transformation from blue discs and red discs to red ellipticals ( $r_{BD \rightarrow RE}$ ,  $r_{RD \rightarrow RE}$ ). However, the number of red ellipticals *in a single mass bin* may still decrease due to ellipticals at the given mass merging to enter a bin of red ellipticals at a higher mass. Similarly, their number can increase as ellipticals from a lower mass bin merge to enter the current mass bin. A complete, semi-analytic model would consider this full range of possibilities and couple the resulting equations appropriately amongst all mass bins. For the purposes of simplicity, we opted to represent the total, net rate of change of the number of red ellipticals as a single parameter,  $\kappa_{RE}$ , which we note may be positive or negative, depending on whether more ellipticals are entering or leaving the given mass bin.

$$\left. \frac{dN_{RE}}{dt} \right|_m = \kappa_{RE}N_{RE} \quad (\text{A3})$$

We exclude the contribution from blue ellipticals from the model for maximum simplicity, and because they represent only a small fraction of the total population at most masses. A complete version of the model would include this population. We initialize our model using the observed relative numbers of blue discs, red discs, and red ellipticals measured at  $z = 1$ , then use the model to compute their evolution to  $z = 0.3$  using a range of values for each of the four parameters in four mass bins. For  $r_{BD \rightarrow RD}$ ,  $r_{BD \rightarrow RE}$ , and  $r_{RD \rightarrow RE}$ , we test 25 values between 0 and 1, and 25 values between -1 and 1 for  $\kappa_{RE}$ . We note that a complete model would explore time-varying rates, but we only experiment with static parameters. For each mass bin, the model was evaluated for each permutation of the four rate parameters. The success of each run was evaluated using a  $\chi^2$  metric; these results are shown for each mass bin in the corner-plot in Figure A1. The bins are weighted by  $1/\chi^2$ , such that white regions represent the rate parameters that yield the lowest  $\chi^2$ , and black representing the largest.

We find a strong mass dependence on the fraction of blue galaxies to quench to red discs ( $r_{BD \rightarrow RD}$ ), or Path A in Figure 9. Our observations of  $f_{R|D}$  and  $f_{D|R}$  are most closely reproduced when  $r_{BD \rightarrow RD} = [0.05, 0.07, 0.1, 0.2] \text{ Gyr}^{-1}$  for masses  $\log(M/M_\odot) = [10.25, 10.55, 10.85, 11.0]$ . These values for  $r_{BD \rightarrow RD}$  correspond to the peaks of the 1-D histograms shown in Figure A1. This increase of  $r_{BD \rightarrow RD}$  with mass could suggest either: 1) more massive galaxies are more likely to undergo quenching processes which do not destroy their discs, or 2) less massive galaxies simply quench less frequently overall, via any pathway.

Analysis of the next parameter in the low mass bin,  $r_{BD \rightarrow RE}$ , suggests that the former is more likely, given the peak of  $r_{BD \rightarrow RE}$  at  $> 0.9 \text{ Gyr}^{-1}$ . The high rate of low-mass blue discs quenching to red ellipticals is evidence that they



**Figure A1.** Results of the grid-search for the best-fit rate parameters  $r_{BD \rightarrow RD}$ ,  $r_{BD \rightarrow RE}$ ,  $r_{RD \rightarrow RE}$ , and  $\kappa_{RE}$  for four mass bins. The units for all rate parameters is  $\text{Gyr}^{-1}$ . 25 equally-spaced values were tested between (0,1) for each parameter, with the exception of  $\kappa_{RE}$  which was tested for 25 values between (-1,1); these are represented by the 25 bins on each axis. Each bin is weighted by  $1/\chi^2$ , such that white regions correspond to parameters which produced the lowest  $\chi^2$ , and black representing the highest. There is a strong result in the dependence of  $r_{BD \rightarrow RD}$  with mass, such that the fraction of blue discs which transition to red discs (ie, quench without disrupting the disc), increases for more massive galaxies. The other parameters are less constrained by this model; therefore a more complex semi-analytic model will be necessary for obtaining the precise values of these rates, and is the subject of future work.

do not quench any less frequently than high mass galaxies, and the increase of  $r_{BD \rightarrow RD}$  with mass is indeed consistent with quenching processes less likely to destroy the disc of massive galaxies. However, this result is not nearly as constrained, given the broad distribution of similarly likely values for this parameter.  $r_{BD \rightarrow RE}$  is even less constrained for all higher masses. The degeneracies evident in this rate and  $r_{RD \rightarrow RE}$  make it clear that our model is not sufficient to constrain the relative frequencies of the processes involved in quenching and morphological transformations; a larger dataset or a full semi-analytic treatment with the adjust-

ments we have described thus far would be necessary to paint the full picture.

## APPENDIX B: DATA TABLES

Here we provide the raw and corrected counts of four morphology/colour types of galaxies: red discs, blue discs, red ellipticals, and blue ellipticals. Counts are divided into four tables representing data for the four mass bins used in Figures 7 and 8. In each table, the counts are further subdivided into four redshift bins corresponding to the bins used

10.1 < log(M/M <sub>⊙</sub> ) < 10.4				
redshift	0.31	0.54	0.76	0.99
N <sub>RD</sub>	66 ± 8	23 ± 5	36 ± 6	17 ± 4
N' <sub>RD</sub>	66 ± 8	30 ± 6	65 ± 11	51 ± 14
N <sub>BD</sub>	411 ± 14	445 ± 16	754 ± 22	629 ± 18
N' <sub>BD</sub>	416 ± 17	582 ± 30	1368 ± 96	1920 ± 266
N <sub>RE</sub>	197 ± 12	262 ± 14	561 ± 20	213 ± 13
N' <sub>RE</sub>	141 ± 9	178 ± 10	365 ± 13	132 ± 8
N <sub>BE</sub>	148 ± 11	394 ± 16	665 ± 21	504 ± 18
N' <sub>BE</sub>	106 ± 8	269 ± 11	433 ± 14	312 ± 12
N <sub>total</sub>	822 ± 23	1124 ± 27	2016 ± 37	1363 ± 29
N' <sub>total</sub>	731 ± 22	1060 ± 34	2232 ± 99	2418 ± 266

**Table B1.** Raw (unprimed) and corrected (primed) number counts of four morphology/colour categories in four redshift bins for galaxies with stellar masses within  $10.1 < \log(M/M_{\odot}) < 10.4$ .

10.4 < log(M/M <sub>⊙</sub> ) < 10.7				
redshift	0.31	0.54	0.76	0.99
N <sub>RD</sub>	76 ± 8	46 ± 7	83 ± 9	44 ± 7
N' <sub>RD</sub>	76 ± 8	60 ± 9	150 ± 19	134 ± 27
N <sub>BD</sub>	351 ± 13	381 ± 15	611 ± 21	470 ± 18
N' <sub>BD</sub>	355 ± 15	498 ± 26	1109 ± 81	1434 ± 201
N <sub>RE</sub>	186 ± 12	272 ± 14	799 ± 22	530 ± 18
N' <sub>RE</sub>	133 ± 8	185 ± 9	520 ± 15	329 ± 12
N <sub>BE</sub>	68 ± 12	186 ± 12	537 ± 20	359 ± 16
N' <sub>BE</sub>	48 ± 6	127 ± 8	349 ± 13	222 ± 10
N <sub>total</sub>	681 ± 21	885 ± 24	2030 ± 37	1403 ± 31
N' <sub>total</sub>	615 ± 20	871 ± 31	2130 ± 85	2121 ± 204

**Table B2.** Raw (unprimed) and corrected (primed) number counts of four morphology/colour categories in four redshift bins for galaxies with stellar masses within  $10.4 < \log(M/M_{\odot}) < 10.7$ .

in the same figures, and the redshift displayed is the central redshift value of the bins. Corrected counts are derived for each redshift interval using  $\xi_D(z)$  for discs and  $\xi_E(z)$  for ellipticals, as explained in Section 3. Errors for the raw numbers represent multinomial counting errors, while errors on the corrected numbers are multinomial counting errors propagated with the errors associated with the fits for  $\xi_D$  and  $\xi_E$ .

10.7 < log(M/M <sub>⊙</sub> ) < 11.0				
redshift	0.31	0.54	0.76	0.99
N <sub>RD</sub>	53 ± 7	40 ± 6	118 ± 10	78 ± 9
N' <sub>RD</sub>	53 ± 7	52 ± 8	214 ± 23	238 ± 41
N <sub>BD</sub>	222 ± 10	265 ± 12	396 ± 17	287 ± 15
N' <sub>BD</sub>	224 ± 12	346 ± 20	718 ± 56	876 ± 127
N <sub>RE</sub>	128 ± 10	175 ± 11	680 ± 19	602 ± 17
N' <sub>RE</sub>	92 ± 7	119 ± 8	442 ± 13	373 ± 11
N <sub>BE</sub>	38 ± 6	86 ± 9	254 ± 14	228 ± 14
N' <sub>BE</sub>	27 ± 4	58 ± 6	165 ± 10	141 ± 9
N <sub>total</sub>	441 ± 17	566 ± 19	1448 ± 31	1195 ± 28
N' <sub>total</sub>	398 ± 16	577 ± 24	1541 ± 62	1630 ± 134

**Table B3.** Raw (unprimed) and corrected (primed) number counts of four morphology/colour categories in four redshift bins for galaxies with stellar masses within  $10.7 < \log(M/M_{\odot}) < 11.0$ .

11.0 < log(M/M <sub>⊙</sub> ) < 11.3				
redshift	0.31	0.54	0.76	0.99
N <sub>RD</sub>	29 ± 5	33 ± 5	89 ± 9	71 ± 8
N' <sub>RD</sub>	29 ± 5	43 ± 7	161 ± 19	216 ± 38
N <sub>BD</sub>	73 ± 7	97 ± 8	151 ± 11	126 ± 10
N' <sub>BD</sub>	73 ± 7	126 ± 11	274 ± 26	384 ± 60
N <sub>RE</sub>	74 ± 7	109 ± 8	343 ± 13	319 ± 12
N' <sub>RE</sub>	53 ± 5	74 ± 5	223 ± 8	198 ± 8
N <sub>BE</sub>	7 ± 3	17 ± 4	64 ± 8	63 ± 7
N' <sub>BE</sub>	5 ± 2	11 ± 3	41 ± 5	39 ± 5
N <sub>total</sub>	183 ± 11	256 ± 13	647 ± 20	579 ± 19
N' <sub>total</sub>	162 ± 10	256 ± 15	701 ± 34	839 ± 72

**Table B4.** Raw (unprimed) and corrected (primed) number counts of four morphology/colour categories in four redshift bins for galaxies with stellar masses within  $11.0 < \log(M/M_{\odot}) < 11.3$ .