

Galaxy Zoo Hubble: the evolution of red disk galaxies since $z = 1.0$

Melanie A. Galloway¹

¹*School of Physics and Astronomy, University of Minnesota, 116 Church St. SE, Minneapolis, MN 55455, USA*

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ABSTRACT

We study the evolution of the passive disk population from $z = 1$ to $z = 0.3$ in a sample of 14,000 galaxies from the COSMOS field and morphologically classified by the Galaxy Zoo: Hubble project. We find the fraction of disks occupying the red sequence, as well as the fraction of disk galaxies that are red, to decrease for the most massive galaxies ($\log(M/M_\odot) > 11$) but increase for lower masses. We interpret the trends in these fractions by identifying four dominant drivers of the change in numbers for each population: the rate of blue disks quenching to become red disks, the rate of red disks transforming to red ellipticals, the rate of blue disks quenching while morphologically transforming to red ellipticals, and the net elliptical merger rate. We develop a toy model to simulate the evolution of the passive disk fractions using a range of input rate parameters. Using the best-fit results of the model, we estimate that 20 \pm error % of massive galaxies go through a passive disk phase, and this fraction decreases with mass. This paper also introduces a new method for using artificially-redshifted galaxies to quantify the redshift-bias in Galaxy Zoo classifications in order to accurately measure the fraction of disk galaxies as a function of redshift.

1 INTRODUCTION

Passive, red disks are an unconventional class of galaxies. They do not adhere to the standard bimodality of the color-morphology relationship, whereby most galaxies tend to exist in one of two populations: blue, late-type disks exhibiting active star formation, and red, early-type ellipticals showing little to no signs of recent star formation (Strateva et al. 2001; Baldry et al. 2004; Correa et al. 2017). The division between the two populations is particularly apparent when represented visually on a color-magnitude or color color diagram. Galaxies tend to populate in two distinct regions: the “red sequence” in the upper band, which contains predominantly early-type galaxies, and the “blue cloud” in the lower, containing mostly late-type spirals. This relationship has been shown to hold for $\sim 85\%$ of galaxies out to $z \sim 1$ (Bell et al. 2004; Cirasuolo et al. 2007; Mignoli et al. 2009) and possibly beyond (Giallongo et al. 2005; van Dokkum et al. 2006; Franzetti et al. 2007; Cassata et al. 2008).

The relatively tight correlation between galaxy color (which traces the stellar content) and morphology (which traces dynamical history) suggests an evolutionary link between the two. In the simplest interpretation, it could be deduced that galaxies tend to begin their lives as young, star-forming disks, until some mechanism (secular or external) causes star-formation to cease while the galaxy simultaneously undergoes a morphological transformation from disk to spheroidal. The growing evidence for a significant popu-

lation of galaxies which breaks this relationship, however, insists on more nuanced interpretations of this model.

The passive disk population has been a matter of interest for understanding the mechanisms driving the evolutionary link between color and morphology since their initial discovery. In one of the earliest documented reports of this class, van den Bergh (1976) identified a set of spirals in the Virgo cluster which were forming stars “much less vigorously” than the other galaxies of the same type, which were dubbed “anemic spirals”. Analysis of this population suggested the possibility of “gentle” quenching mechanisms which could shut off star-formation without disrupting the morphology (in contrast to violent processes such as mergers, which are capable of destroying the disk (Bell et al. 2004; Negroponte & White 1983; De Lucia et al. 2006; Springel et al. 2005)). The low gas content in the anemic spirals suggested that subtle environmental factors played a role in stripping the gas required to continue star-formation, a process commonly known now as ram-pressure stripping (Gunn & E. and Gott, III 1972; Steinhauser et al. 2016).

Other studies have since investigated other possible mechanisms could lead to the formation of passive disks, and how significant of a contribution this population makes to understanding the full picture of galaxy evolution. Environment is believed to play a strong role in thier formation; many studies for instance find passive spirals preferentially in high-density environments (Dressler et al. 1999; Poggianti et al. 1999; Goto et al. 2003; Deng et al. 2009; Hughes & Cortese 2009). Moran et al. (2006) model the star-formation

histories of passive spirals at $z \sim 0.4$ and find them to be consistent with models for spirals affected by gas-starvation (Larson, R.B., Tinsley, B.M. and Caldwell 1980; Quilis et al. 2000; Bekki et al. 2002). Environment plays a significant factor in this scenario, whereby the interaction of the galaxy with the intra-cluster medium halts the accretion of gas onto the galaxy, inhibiting star-formation and causing a quench without disrupting the morphology significantly. Their results did not argue that starvation was the only mechanism responsible for building up the population of disks in the red sequence, but do conclude that passive disks are indeed an important transition population.

Masters et al. (2010) is one of the few studies which finds no strong correlation of passive disks with environment, but do not rule out environment playing a significant contribution in their creation. They also find strong evidence for quenching via completely secular processes; given by their sample of passive disks being more massive and having a higher bar fraction than their star-forming counterparts. Massive galaxies are more likely to have been assembling for very long times, allowing sufficient time to use up all of their gas, without environment being a direct factor. This option could explain the observed correlations with density and passivity, given that higher-density regions were more likely to have been assembled at earlier times. Secondly, Masters et al. (2010) observed a significantly higher bar fraction in passive spirals (67%) than star-forming spirals (27%). Bars are known for their ability to efficiently drive gas to the centers of galaxies via a redistribution of angular momentum throughout the disk (Sellwood & Wilkinson 1993; Shlosman et al. 1989; Ann & Thakur 2005), which could increase central star-formation (Hawarden et al. 1986; Ho et al. 1997) or feed the central supermassive black hole (Athanasoula 1992; Friedli & Benz 1993). The excess of bars in passive disks then suggests that bars were responsible for quickly using up the gas in the galaxy, resulting in subsequent quenching.

Passive disks have thus far been proposed as both a final stage of galactic evolution, driven by secular and external processes capable of exhausting gas required for star-formation, and as a transition phase of galaxies toward a final evolution to red spheroidal, driven by processes which quench and morphologically transform on different timescales, or multiple separate processes acting independently. Understanding the significance of the passive disk population is therefore unquestionably an important key to understanding galaxy evolution as a whole. Bundy et al. (2010) investigates this subject by measuring the different morphological contributions to the red sequence since $z = 1$, and estimate as high as 60% of all galaxies go through a passive disk phase. It was not quantified which of these further evolve to spheroidal and which stay disks for the remainder of their lifetimes, but the decaying contribution of passive disks to $z = 0.3$ was evidence that some fraction of these did indeed transform to elliptical.

This paper will investigate the evolution of the passive disk population from $z = 1$ to $z = 0.3$ using galaxies identified in the COSMOS field with morphological classifications from Galaxy Zoo: Hubble. We will measure the fraction of disks which are passive and the fraction of the red sequence occupied by disks as functions of mass and redshift, and argue that three factors drive the evolution of these fractions:

1) the rate of blue disks quenching to form passive disks, 2) the rate of blue disks quenching and simultaneously transforming to elliptical, 3) the rate of red disks transforming to red ellipticals, and 4) the net merger rate of ellipticals. We will implement a simple toy model to simulate the evolution of the relative abundances of red disks, blue disks, and red ellipticals, in order to quantify these rate parameters. We will use the results to estimate the fraction of galaxies that enter a red disk phase, and discuss the likelihoods of the red disk phase being a transitory stage or an end-point of a typical galaxy’s evolutionary path.

Section 2 will describe our methods for selecting disk galaxies and separating the sample into active / passive populations using a color-color diagnostic. In Section 3 we describe a new method of correcting for redshift bias in the detection of disk galaxies with Galaxy Zoo classifications using an artificially-redshifted set of images. In Section 4 we present our results of the fraction of disk galaxies which are red, and the fraction of red sequence galaxies that are disks, as functions of mass and redshift. Here we also explain our toy-model for measuring the dominant evolutionary pathways taken by galaxies in different bins of mass. We compare our findings with results from the literature and discuss their implications in Section 5. Our main conclusions are outlined in Section 6. We adopt a Λ CDM cosmology throughout this paper of $\Omega_m = 0.31$ and $H_0 = 68 \text{ km s}^{-1}\text{Mpc}^{-1}$ (Planck Collaboration et al. 2015).

2 DATA

The parent sample of galaxies in this paper is drawn from the Galaxy Zoo: Hubble (GZH) catalog (Willett et al. 2016), which provides morphological classifications for galaxies sourced from the HST Legacy Surveys. From the main catalog we select galaxies with imaging from the Cosmic Evolution Survey (COSMOS, Scoville et al. (2007)) in the redshift range $0 < z < 1$. Rest frame NUV-r and r-J colors are taken from the UltraVISTA catalog (McCracken et al. 2012; Ilbert et al. 2013).

2.1 Sample Selection

We identify a sample of 14,663 disk and elliptical galaxies using the morphological classifications provided by GZH. Mergers and irregulars are excluded from the analysis by applying cuts of $f_{\text{irregular}} > 0.3$ and $f_{\text{merger}} > 0.5$ for galaxies which have at least 20 “yes” votes for the question, “Is there anything odd?”. Last, we apply an inclination limit using $f_{\text{not edge-on}} > 0.3$ and $N_{\text{not edge-on}} > 10$. Before applying this cut, it was observed that the red sequence region of the sample was dominated by highly-inclined galaxies, shown in Figure 1. Given that galaxy color should be independent of the angle in which it is observed, it is clear that the inclined galaxy colors are strongly affected by dust-reddening. While we are not using dust-corrected colors in our color-color separation, inclination has shown to have an affect on colors even in those which dust-corrected has been attempted (Morselli et al. 2016; Devour & Bell 2017). By limiting the sample to face-on galaxies, this bias should be removed (right panel of Figure 1).

To classify the galaxies as quiescent or star-forming,

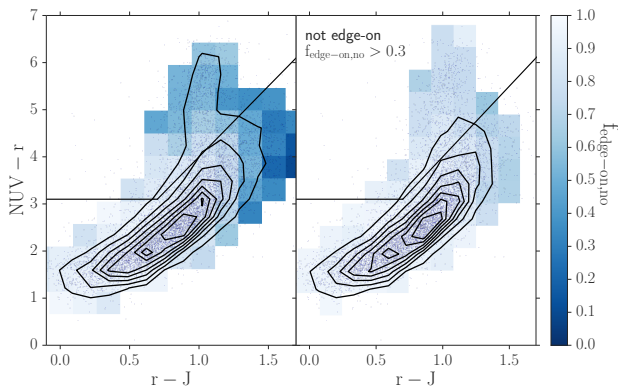


Figure 1. The effect of reddening for highly inclined galaxies. On the left panel is the distribution of $f_{\text{edge-on,no}}$, which is the fraction of Galaxy Zoo users who voted “no” in response to the question “Could this be a galaxy viewed edge-on?”. This vote correlates with inclination angle, such that low values represent highly inclined galaxies, and high values represent face-on galaxies. The bins are colored such that darker blue bins have a higher fraction of highly inclined galaxies, and white bins have high fractions of face-on galaxies. There is an obvious bias towards redder colors for galaxies with high inclination angles (low votes for $f_{\text{edge-on,no}}$). We therefore implement a cut of $f_{\text{edge-on,no}} > 0.3$ to ensure that observed red colors are an indicator of a lack of star-formation, and not dust-reddening.[Note: I’m not sure the right panel is particularly useful; it’s really just showing the distribution is mostly smoothed out after setting the cut. Keep?]

a method similar to that described by Ilbert et al. (2013) (hereafter I13) was used, which implements a rest-frame $\text{NUV}-r$ versus $r-J$ diagnostic. Here are some reasons these colors are great ($\text{NUV}-r$): (Arnouts et al. 2007; Salim et al. 2005; Wyder et al. 2007), (Martin et al. 2007)

The demarcation line to separate the quiescent and active populations at $z = 1$ is adopted from I13, which defines the quiescent galaxies as those which satisfy: $M_{\text{NUV}} - M_r > 3(M_r - M_J) + 1$ and $M_{\text{NUV}} - M_r > 3.1$. I13 applies this criteria to all galaxies in a range of $0.2 < z < 3$, although it performs best at separating the two populations in the redshift bin $0.7 < z < 1.2$, where $> 98\%$ of galaxies identified as quiescent exhibited star formation rates less than $\log(SFR) = -11$ (see Figure 3 of I13). Therefore this work uses the I13 separation criteria at $z = 1$, and computes the evolution of the demarcation lines as a function of redshift to $z = 0$.

The evolution of $r-J$ and $\text{NUV}-r$ colors was measured using a stellar population synthesis model from Bruzual & Charlot (2003). An instantaneous-burst model (ssp) was chosen from the Padova1994 track to represent the color evolution of a passively evolving galaxy, with a metallicity $Z = 0.008 = .4Z_{\odot}$, which is the typical metallicity of passive galaxies with mass $9 < \log(M_*/M_{\odot}) < 10$ (Peng et al. (2015), Figure 2a), chosen to correspond to the median mass of the sample ($\log(M_*/M_{\odot}) = 9.7$). A linear fit was generated for each color within the range $0 < z < 2$, and the slopes for each were used to redefine the demarcation lines in five redshift bins: one with central value $z = 0.007$ (used to classify the SDSS ferengi2 sample), and four with central values $z = [0.30, 0.50, 0.70, 0.90]$ with widths $\Delta z = 0.2$. The

quiescent galaxies are thus defined in these bins as those that satisfy:

$$M_{\text{NUV}} - M_r > 3.1 + a_1(z) \quad (1)$$

$$M_{\text{NUV}} - M_r > 3(M_r - M_J + a_2(z)) + a_1(z) + 1 \quad (2)$$

where $a_1(z) = [0.54, 0.38, 0.27, 0.16, 0.05]$ and $a_2(z) = [0.19, 0.14, 0.10, 0.06, 0.02]$.

We note that the evolution of the demarcation lines from $z = 1$ to $z \sim 0$ is very minimal, and our final results do not change if we perform the separation using static lines.

In describing our methods for separating active and passive populations using a color-color separation technique, we have used terminology such that blue/red have been used to describe colors explicitly, while active/passive have been used to describe ongoing/quenched star-formation. The remainder of this paper will assume that the color cuts described in this section adequately separated the active and passive populations, and for convenience the terms red/blue will be used interchangeably with passive/active. k thanks!

3 CORRECTING FOR INCOMPLETENESS IN DISK DETECTION

In this work, we study the growth of the red sequence population by evaluating the fraction of passive disks as a function of redshift, $N_{\text{red disks}}/(N_{\text{red disks}} + N_{\text{blue disks}})$, as well as the fraction of disks occupying the red sequence, $N_{\text{red disks}}/(N_{\text{red disks}} + N_{\text{red ellipticals}})$. To accurately measure these fractions, the number of disks populating each redshift interval must be known with confidence. To identify disk galaxies in our sample, we set a cut of $f_{\text{features}} \geq 0.3$, such that galaxies meeting this criteria are considered to have distinguishable features or disk structure (additional cuts are also placed to eliminate clumpy, highly inclined, and merging galaxies; see Section 2.1). However, it is known that distinguishing disk structure from spheroidal becomes increasingly challenging at high redshifts (for both experts and novice classifiers alike), where features are less resolved and more difficult to identify. Willett et al. (2016) show using a set of artificially-redshifted simulated galaxy images classified in Galaxy Zoo that vote fractions for the same galaxy can be drastically different measured at $z = 1$ from $z = 0$, often enough to change its morphological classification (we will show the same in Section 3.1). Therefore it is predicted that applying a f_{features} cut to identify disks will increasingly underestimate their true number at increasing redshift intervals. A set of artificially redshifted images was used to quantify and correct for this incompleteness in disk detection, described in the next section.

3.1 FERENGI2 set of artificially redshifted galaxy images

FERENGI2 is a set of simulated galaxy images created using the FERENGI code (Barden et al. 2008). These were created from a parent sample of 936 nearby ($z < 0.01$) SDSS galaxies, all of which had been previously classified in Galaxy Zoo 2 and were cross-matched in 2MASS (Skrutskie et al.

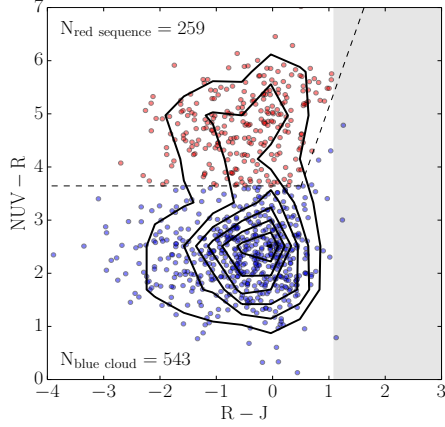


Figure 2. Separation of the quiescent population (red sequence) and active population (blue cloud) of the FERENG12 sample. The gray shaded region represents the R-J limit of the sample; since FERENG12 is a subset of GZ2, for which a limit of $r < 17$ was implemented, and the magnitude limit of 2MASS is $J < 15.91$, the FERENG12 sample is limited to $R-J < 1.1$.

2006) for J magnitudes and GALEX (Martin et al. 2005) for NUV magnitudes, which were necessary to create a color-color separation using a method as similar as possible to that of the COSMOS sample. An evolution factor of $e = -1$ was applied, which brightens each galaxy linearly with redshift: $M' = M + ez$, where M' is the corrected magnitude. This correction is performed to mimic the known physical increase of galaxy magnitude with redshift (Lilly et al. 1998; Loveday et al. 2011), and the value $e = -1$ was chosen based on an analysis of spectra template models provided by Brinchmann et al. (2004), which showed that typical galaxies tend to evolve in brightness by one magnitude per redshift. Each galaxy was artificially redshifted 8 times from $z = 0.3$ to $z = 1$ in intervals of $\Delta z = 0.1$ and processed to mimic *HST* imaging parameters, giving a total of 7,488 images (3 examples are shown in Figure 3). The set was then classified in Galaxy Zoo using the same decision tree as used for Galaxy Zoo Hubble. 134 highly inclined disk galaxies were removed from the sample by excluding any with $N_{\text{edgeon}} > 20$ and $f_{\text{not edge-on}} \geq 0.6$, using the vote fraction associated with the real galaxy image measured in GZ2. This cut was shown in Galloway et al. (2015) to correlate well with inclination angle $\cos(a/b) < 67^\circ$. This was to exclude those which may be mis-classified due to dust-reddening. Using the NUV-J-R selection method described in section 2.1, the remaining sample was divided into a set of red sequence galaxies (259 per redshift bin) and blue cloud (543 per each redshift bin) (see Figure 2).

3.2 Measuring ξ

The FERENG12 set was used to measure the incompleteness in disk detection, from which a correction factor ξ was derived. This is defined as the number of disks detected divided by the true number of disks expected to exist in a given redshift interval: $\xi(z) = N_{\text{detected}}/N_{\text{true}}$. Acknowledging that the completeness in disk detection may depend on

galaxy color, the corrected fraction of passive disks can then be calculated as:

$$f_{R|D} = \frac{N_{RD} \times \xi_{\text{red}}^{-1}}{N_{RD} \times \xi_{\text{red}}^{-1} + N_{BD} \times \xi_{\text{blue}}^{-1}} \quad (3)$$

If there is no color bias in disk detection, $\xi_{\text{red}} = \xi_{\text{blue}}$, and this term cancels out, leaving the fraction unchanged. If there is a bias, however, the ξ terms do not cancel, and the incompleteness in disk detection could have a large effect on the red disk fraction. Therefore a careful measurement of ξ is estimated for both red and blue disk galaxies using the FERENG12 set of simulated images.

The completeness values $\xi_{\text{red}}(z)$ and $\xi_{\text{blue}}(z)$ were computed in varying bins of redshift for the red sequence and blue cloud galaxies separately. An example calculation of ξ_{blue} in the $z = 0.7$ bin is shown in Figure 4. Each point represents a FERENG12 galaxy, where the y-axis indicates the value of f_{features} measured in the image redshifted to $z = 0.7$, and the x-axis indicates the value of f_{features} measured in the same galaxy redshifted to $z = 0.3$. Disk galaxies are identified as those for which $f_{\text{features}} \geq 0.3$. Since, on average, f_{features} decreases for the same galaxy as it is viewed at higher redshifts, the number of galaxies meeting this threshold is generally fewer at higher redshifts than lower redshifts. This is indicated by the dotted lines: galaxies to the right of the vertical dashed line at $f_{\text{features}, z=0.3} = 0.3$ are identified as disks at $z = 0.3$; their sum is considered the “true” number of disks, N_{true} . Similarly, the galaxies above the horizontal line at $f_{\text{features}, z=0.7} = 0.3$ are identified as disks at $z = 0.7$; their sum is the “detected” number of disks at $z = 0.7$, or N_{detected} . As obvious in the figure, N_{detected} is in general much lower than N_{true} , emphasizing the increasing difficulty in detecting features at higher redshifts. Their ratio is the completeness ξ ; in this example $\xi_{\text{blue}}(z = 0.7) = 0.61$, meaning only 61% of disks were detected at this redshift.

It was hypothesized that the completeness in disk detection may be a function of other parameters in addition to redshift. At fixed redshift, for example, it is reasonable to guess that features could be easier to detect galaxies that have higher mass, radius, or surface brightness. To test whether these parameters also impact the number of disks detected, the completeness was measured in fixed redshift bins as a function of surface brightness, effective radius, and mass. The surface brightness was calculated as $\mu = m + 2.5 * \log_{10}(2 \times (b/a) \times \pi R_e^2)$, using SEXTRACTOR outputs `MAG_AUTO`, `b/a` and `R_e` measured in the I_{814W} band images. The effective radius used was the 50% `FLUX_RADIUS` converted in to kpc, and the masses used were the `MEDIAN` values in the MPA-JHU DR7 catalog (Kauffmann et al. 2003).

Figure 5 shows completeness as a function of redshift and surface brightness, for the red sequence and blue cloud galaxies. 8 redshift bins were further divided into bins of surface brightness with varying widths, where the sizes were chosen to satisfy that $N_{\text{detected}} + N_{\text{true}} \geq 10$ in each bin. This was chosen as a compromise between having a sufficient number of galaxies in each bin to compute the completeness fraction $\xi = N_{\text{detected}}/N_{\text{true}}$, and to have enough bins of surface brightness to measure a trend with confidence of completeness as a function of μ . Visual inspection of the data did not suggest any relationship between the two. To be sure,

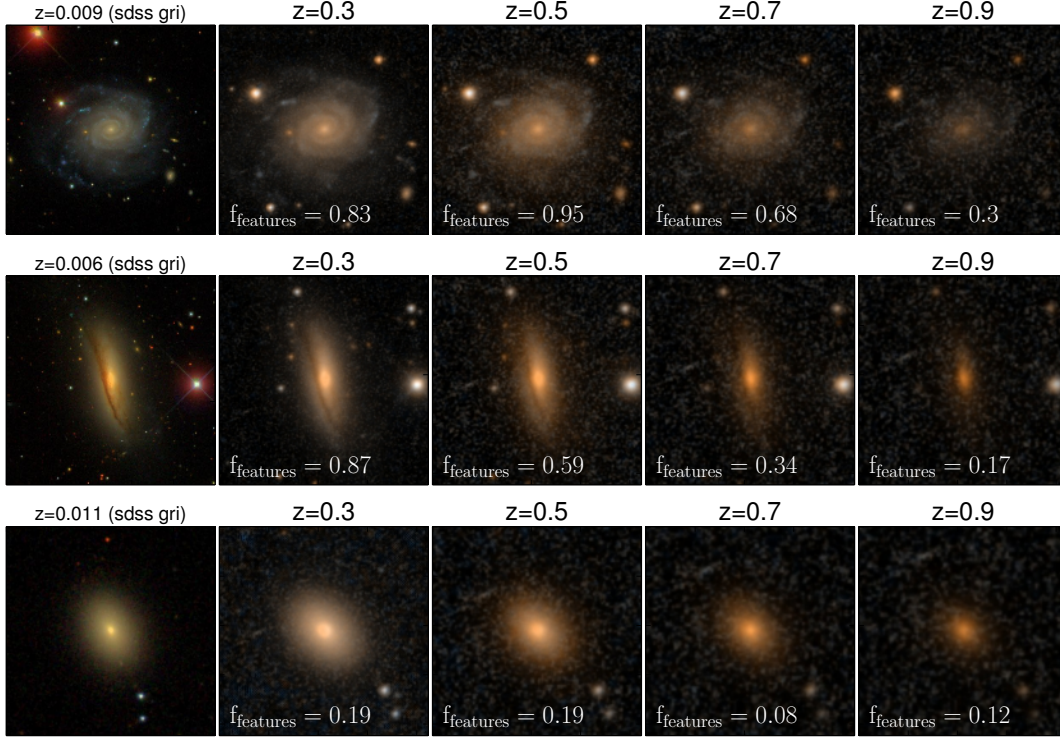


Figure 3. Example images of three galaxies artificially redshifted with the FERENGI code. The left image in each row is a real SDSS gri-composite image; the four to the right are images generated by FERENGI at varying redshifts, processed to mimic *HST/COSMOS* imaging. The f_{features} vote fraction for each simulated image is given; this value tends to decrease for each galaxy as it is processed to be viewed at higher redshifts.

the data were fit to a linear function in each redshift bin. For each fit, a p-value representing a hypothesis test whose null hypothesis is that the slope is zero was computed. Only one reached the criteria $p < 0.05$, but with a low R^2 value of 0.28 which is not considered large enough to represent a good fit. This process was repeated using effective radius and mass as parameters, with the same results. Therefore only redshift was used as a parameter which impacted completeness value with confidence.

The completeness values ξ_{red} and ξ_{blue} were then measured as a function of redshift for the red sequence and blue cloud FERENGI2 galaxies; results are shown in Figure 6. No significant difference was detected for the two functions, which is apparent from the overlapping $1 - \sigma$ errors on the plot. Therefore ξ was computed for all galaxies in bins of redshift between 0.3 and 1.0 with widths $\Delta z = 0.1$; from here a linear relationship for ξ as a function of redshift was derived: $\xi(z) = -0.9 \pm x(z) + 1.2 \pm y$. This correction was used to calculate the fraction of disks on the red sequence:

$$f_{D|R} = \frac{N_{RD} \times \xi^{-1}}{N_{RD} + N_{RE}} \quad (4)$$

4 RESULTS

In this section we present our results of the evolution of disc galaxies from $z = 1$ to $z = 0.2$ in a sample of 27,355

COSMOS galaxies morphologically classified in GZH. We will show x , y , and z and talk about it.

4.1 The evolving passive disk fractions: $f_{R|D}$ and $f_{D|R}$

The change in the relative number densities of active/passive disk/elliptical galaxies traces the dominant evolutionary pathways they follow at different mass thresholds. In Figure 7 we measure these using the fractions defined in the previous section, $f_{R|D}$ (left panel) and $f_{D|R}$ (right panel) for four mass bins. We observe significantly different trends in $f_{R|D}$ for the two highest mass bins ($\log(M/M_{\odot}) > 10.7$): for higher-mass galaxies, the fraction of red disks vs. all disks, within error, is either relatively flat or exhibits a small decrease, while the lower-mass galaxies have trends which increase sharply from $z = 1$ to $z = 0.3$. Similarly for the fraction of red disks on the red sequence: the highest mass bin $\log(M/M_{\odot}) > 11.0$ decreases in $f_{D|R}$, while the lowest-mass bin increases sharply from $f_{D|R} \sim 0.05$ to ~ 0.2 .

To gain a more intuitive understanding of how the trends of these fractions depend on the different possible evolutionary pathways and their transition rates, it is helpful to rewrite them in a reduced form: $f_{R|D} = (1 + \frac{N_{BD}}{N_{RD}})^{-1}$; $f_{D|R} = (1 + \frac{N_{RE}}{N_{RD}})^{-1}$. Using the former as an example: at zeroth order, it can be seen that if the number of red disks increases at a higher rate than an increase in blue disks in some time interval, the overall fraction $f_{R|D}$ would also

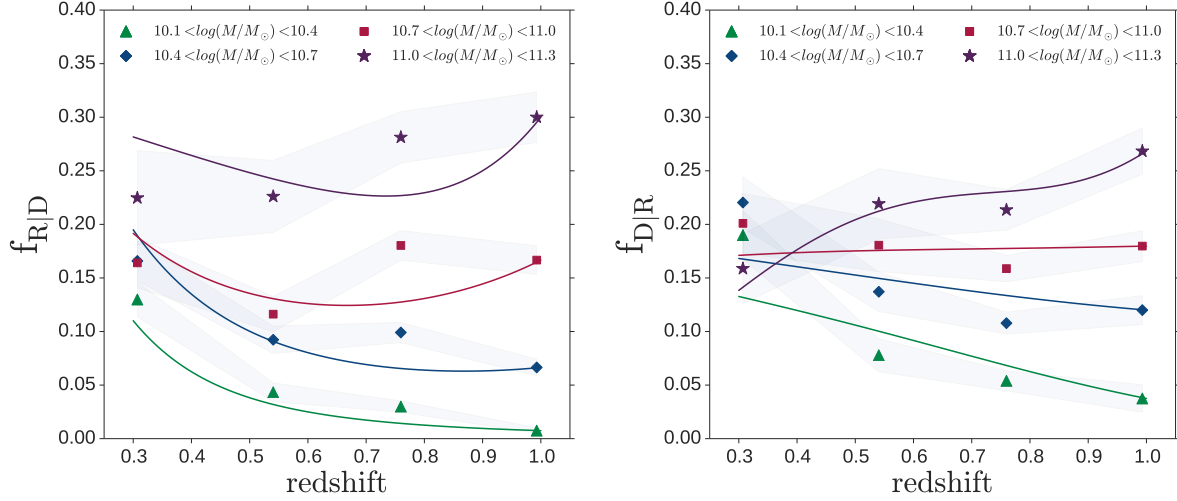


Figure 7. **Left:** Passive disk fraction ($N_{\text{red disks}}/(N_{\text{red disks}} + N_{\text{blue disks}})$) vs redshift in four mass bins. **Right:** Fraction of disks on the red sequence ($N_{\text{red disks}}/(N_{\text{red disks}} + N_{\text{red ellipticals}})$) vs redshift in four mass bins. The solid lines represent the evolution of the fractions computed by the toy-model described in Section 4 using rate parameters which yielded the lowest χ^2 .

increase. For a single mass bin, this scenario would be consistent with a model in which blue galaxies are quenching faster than they are entering the mass bin via star formation. A strong decrease in $f_{R|D}$ would, in contrast, indicate a higher rate of red disks exiting the mass bin than the blue disks; the strength of the decrease would depend on the relative frequencies of blue galaxies quenching to form new red disks and red disks merging to form red ellipticals. The precise relative values of these rates cannot be deduced by a simple by-eye analysis of the fraction, however.

We therefore implement a simple toy model to track the change in $f_{R|D}$ and $f_{D|R}$, given a range of parameters representing the quenching and morphological transformation rates for galaxies at fixed stellar mass. We begin by considering the rate of change in the number of blue disks (dN_{BD}/dt), red disks (dN_{RD}/dt), and red ellipticals (dN_{RE}/dt). In a given mass bin, the change in numbers for each population will depend on several parameters, illustrated visually in Figure 8.

4.1.1 Blue Disks

First, galaxies in a blue bin may transition into a red disk bin via a quenching process that does not destroy its disk; we define this rate as $r_{BD \rightarrow RD}$, representing the fraction of blue galaxies to transition to red disks per Gyr (path A in Figure 8). Blue galaxies may also exit a bin via a quenching process which *does* destroy the disk; this fraction per Gyr we define as $r_{BD \rightarrow RE}$ (path C in Figure 8).

The number of galaxies in a blue disk bin will also change due to star formation, which brings active galaxies from a lower mass bin into the current mass bin. To account for this term we use the formalism outlined by Peng et al. (2010), in which this rate of change is given by $(\alpha + \beta)sSFR$. Here $\alpha = d\phi_{\text{blue}}/dm$ is the derivative of the mass function for blue galaxies, which equates to $\alpha = (1 + \alpha_s) - m/M^*$ for a mass function described by the Schechter (1976) function. We use best-fit parameters

for blue galaxies measured by Johnpaperetal, which give $\alpha_s = -1.4$ and $M^* = 10.28$ ($\log(M/M_\odot)$). Following the method of Peng et al. (2010), we let $\beta = 0$, both for simplicity, and because their conclusions found not to be strongly dependent on β . Last, the specific star-formation rate is given by $sSFR(t) = 2.5(\frac{t}{3.5 \text{ Gyr}})^{-2.2} \text{ Gyr}^{-1}$ (Peng et al. 2010).

Accounting for all sources and sinks of blue disks entering or exiting a bin of given mass, the rate of change of blue disks can be written fully as:

$$\left. \frac{dN_{BD}}{dt} \right|_m = \left(-r_{BD \rightarrow RD} - r_{BD \rightarrow RE} - \alpha(m)sSFR(t) \right) N_{BD} \quad (5)$$

4.1.2 Red Disks

Galaxies exiting a blue bin as they quenched without disrupting their disks enter the pool of red disks, increasing N_{RD} for a given mass bin. Red disks also may undergo a morphological transformation, depleting the pool of red disks as they enter the red elliptical bin (path B in Figure 8). The fraction of galaxies to undergo this pathway per Gyr is denoted as $r_{RD \rightarrow RE}$. Combining these factors gives the expression:

$$\left. \frac{dN_{RD}}{dt} \right|_m = +r_{BD \rightarrow RD}N_{BD} - r_{RD \rightarrow RE}N_{RD} \quad (6)$$

4.1.3 Red Ellipticals

In this simple model, it is assumed that red, passive ellipticals are the final state in a typical galaxy's evolution. Therefore N_{RE} will always be increasing from the transformation from blue disks and red disks to red ellipticals ($r_{BD \rightarrow RE}$, $r_{RD \rightarrow RE}$). However, the number of red ellipticals in a single mass bin may still decrease due to ellipticals at the given mass merging to enter a bin of red ellipticals at

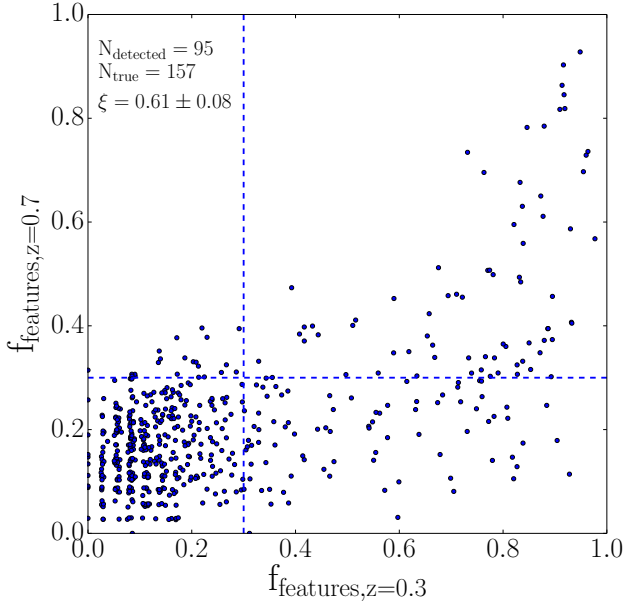


Figure 4. Example calculation of completeness ξ at redshift $z = 0.7$. Points represent FERENG12 images classified in Galaxy Zoo. The y-axis corresponds to the value of f_{features} measured at the galaxy redshifted to $z = 0.7$, and the x-axis corresponds to the value of f_{features} measured at the galaxy redshifted to $z = 0.3$. On average, the f_{features} is lower at the higher redshift, indicating users on average have more difficulty identifying features in images at higher redshifts. The dotted lines correspond to $f_{\text{features}}=0.3$, the threshold above which a galaxy is considered to have a disk. Galaxies to the right of the vertical dashed line were identified as disks at the lowest redshift $z = 0.3$, the total number defined as N_{true} , the true number of disks. Galaxies above the horizontal dash line were identified as disks at the higher redshift $z = 0.7$, the total number defined as N_{detected} . The ratio $\xi = N_{\text{detected}}/N_{\text{true}}$ is the completeness value; in this example, only 61% of disks were detected at $z = 0.7$.

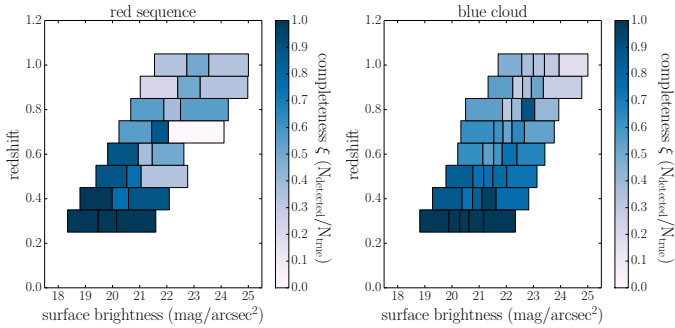


Figure 5. Completeness ξ as a function of redshift and surface brightness for red sequence (left) and blue cloud galaxies (right). In each redshift bin, galaxies were binned by surface brightness in varying widths such that $N_{\text{detected}} + N_{\text{true}} \geq 10$ in each bin. The completeness ξ was computed in each z, μ bin, represented by the colors. Darker colors represent a completeness of 1, such that all disks were detected, while fainter colors represent a completeness near 0, representing a failure to detect disks. ξ tends to decrease with redshift, but no correlation of ξ with surface brightness is observed at fixed redshift.

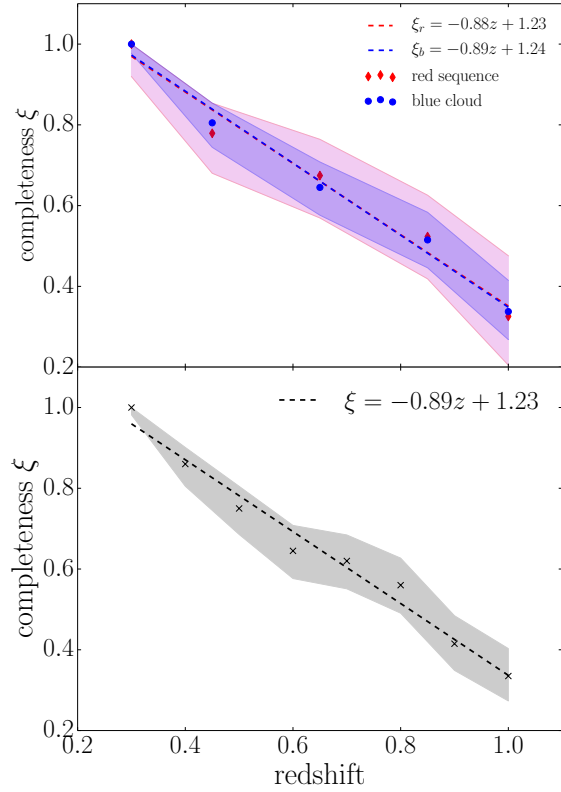


Figure 6. Top: Completeness ξ as a function of redshift for red sequence and blue cloud FERENG12 galaxies separately. Both populations show a strong dependence on ξ with redshift, but are indistinguishable from each other. **Bottom:** Completeness as a function of redshift for all FERENG12 galaxies (red and blue combined). The equation representing the linear fit is displayed.

a higher mass. Similarly, their number can increase as ellipticals from a lower mass bin merge to enter the current mass bin. A complete, semi-analytic model would consider this full range of possibilities and couple the resulting equations appropriately amongst all mass bins. For the purposes of this simple model, we opted to represent the total, net rate of change of the number of red ellipticals as a single parameter, κ_{RE} , which we note may be positive or negative, depending on whether more ellipticals are entering or leaving the given mass bin.

$$\left. \frac{dN_{RE}}{dt} \right|_m = \kappa_{RE} N_{RE} \quad (7)$$

We exclude the contribution from blue ellipticals from the model because they represent only a small fraction of the total population (find references which quantify this.) We initialize our model using the observed relative numbers of blue disks, red disks, and red ellipticals measured at $z = 1$, then use the model to compute their evolution to $z = 0.3$ using a range of values for each of the four parameters in four mass bins. For $r_{BD \rightarrow RD}$, $r_{BD \rightarrow RE}$, and $r_{RD \rightarrow RE}$, we test 25 values between 0 and 1, and 25 values between -1 and 1 for κ_{RE} . We note that a complete model would explore time-varying rates, but for the purposes of simplicity

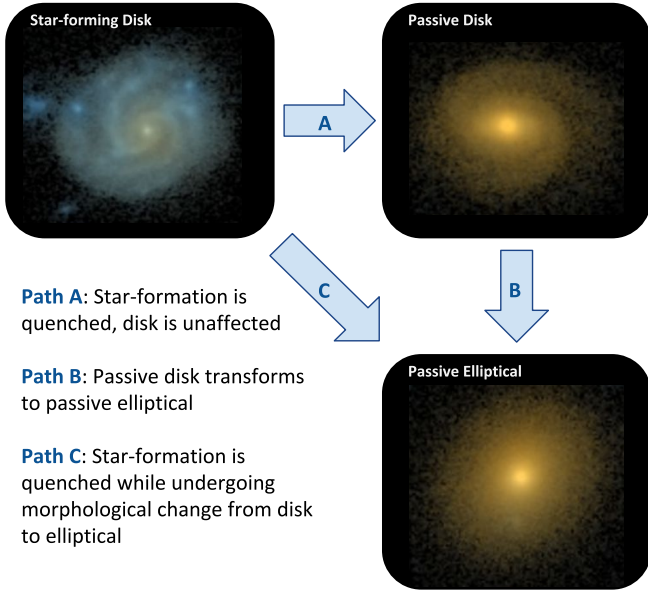


Figure 8. Cartoon representing three evolutionary pathways represented in the toy-model described in Section 4. Path A represents an active star-forming galaxy which quenches without destroying the disk, becoming a red disk; the fraction of blue galaxies to follow this track is represented by $r_{BD \rightarrow RD}$ in the model. Path B represents a red disk morphologically transition to red elliptical; the fraction of red galaxies to follow this track is $r_{RD \rightarrow RE}$. Path C represents a blue disks simultaneously quenching and morphologically transforming to become a red elliptical; the fraction of blue galaxies to follow this track is $r_{BD \rightarrow RE}$. (The fourth driver of the relative numbers of different morphological types is κ_{RE} , the net merger rate of ellipticals in a given mass bin, and is not represented in the cartoon.)

in our toy-model we only experiment with static parameters. For each mass bin, the model was implemented for each permutation of the four rate parameters. The success of each run was evaluated using a χ^2 metric; these results are shown for each mass bin in the corner-plot in Figure 9. The bins are weighted by $1/\chi^2$, such that white regions represent the rate parameters that yield the lowest χ^2 , and black representing the largest.

We find a strong mass dependence on the fraction of blue galaxies to quench to red disks ($r_{BD \rightarrow RD}$), or Path A in Figure 8. Our observations of $f_{R|D}$ and $f_{D|R}$ are most closely reproduced when $r_{BD \rightarrow RD} = [0.05, 0.07, 0.1, 0.2] \text{ Gyr}^{-1}$ for masses $\log(M/M_\odot) = [10.25, 10.55, 10.85, 11.0]$. [Note: need to measure peaks explicitly, current values are by-eye. Also calculate 1-sig errors.] These values for $r_{BD \rightarrow RD}$ correspond to the peaks of the 1-D histograms shown in Figure 9. This increase of $r_{BD \rightarrow RD}$ with mass could suggest either: 1) more massive galaxies are more likely to undergo quenching processes which do not destroy their disks, or 2) less massive galaxies simply quench less frequently overall, via any pathway.

Analysis of the next parameter in the low mass bin, $r_{BD \rightarrow RE}$, suggests that the former is more likely, given the peak of $r_{BD \rightarrow RE}$ at $> 0.9 \text{ Gyr}^{-1}$. The high rate of low-mass blue disks quenching to red ellipticals is evidence that they do not quench any less frequently than high mass galaxies, and the increase of $r_{BD \rightarrow RD}$ with mass is indeed con-

sistent with quenching processes less likely to destroy the disk of massive galaxies. However, this result is not nearly as constrained, given the broad distribution of likelihoods for this parameter. $r_{BD \rightarrow RE}$ is even less constrained for all higher masses. The degeneracies evident in this rate and $r_{RD \rightarrow RE}$ make it clear that our model is not sufficient to constrain the relative frequencies of the processes involved in quenching and morphological transformations; a more sophisticated model with the adjustments we have described thus far would be necessary to paint the full picture.

5 DISCUSSION

We have explored the evolution of the passive disk population since $z = 1$ by quantifying their abundances in terms of the fraction of disk galaxies that are red $f_{R|D}$ and the fraction of the red sequence occupied by disks $f_{D|R}$. For both fractions, we observed dependencies on both mass and redshift; this is a strong indication that passive disks play an important role in understanding the processes involved in the quenching and morphological transformation of galaxies. We identified three pathways to describe the evolution of a star-forming disk: $r_{BD \rightarrow RD}$ (the rate of blue disks quenching to red disks), $r_{BD \rightarrow RE}$ (the rate of blue disks quenching and transforming directly to red ellipticals), and $r_{RD \rightarrow RE}$ (the rate of red disks transforming to red ellipticals), and we argue that the relative frequencies of these rates drive the trends in $f_{R|D}$ and $f_{D|R}$. To begin quantifying the occurrences of each of the pathways, we developed a toy model to reproduce $f_{R|D}$ and $f_{D|R}$ given some set of rates. Our model was able to constrain $r_{BD \rightarrow RD}$ to a reasonable degree of certainty, but the rest would require a more sophisticated model to deduce.

An analysis of $r_{BD \rightarrow RD}$ provides an estimate for the fraction of galaxies to go through a passive disk phase. For the most massive galaxies, we find $r_{BD \rightarrow RD} = 0.20 \pm 0.1 \text{ Gyr}^{-1}$, indicating that 20% of massive galaxies become red disks at some point in their lifetime. Whether these 20% tend to stay red disks or tend to evolve to ellipticals is unclear without a more solid constraint on $r_{RD \rightarrow RE}$. Using the same logic for the other three mass bins, we can find that [5%, 7%, 10%] of galaxies with masses [10.25, 10.55, 10.85] become red disks in their lifetimes. These estimates are in agreement with Bundy et al. (2010) (hereafter B10) who estimate an upper limit of 60% of massive galaxies to experience a red disk phase. Their estimation comes from a different approach to ours, via an analysis of the mass function of galaxies with different morphologies and the fractional contribution of disks on the red sequence $f_{D|R}$.

Our estimation of the significance of the passive disk population is in agreement with B10 for the most massive galaxies, as is the downward trend in $f_{D|R}$ with redshift from $z = 1$ to $z = 0.3$. As suggested previously, a downward trend of $f_{D|R}$ represents either a depletion of the total pool of red disks (via a transformation to elliptical), but could also be an indication of an increase in the pool of red ellipticals (which could result from blue or red disks transforming morphology). In contrast, an upward trend is only possible via a pile-up of red disks, which is what we observe for the lower mass bins. Thus far our results are then consistent with a physical scenario in which 1) more mas-

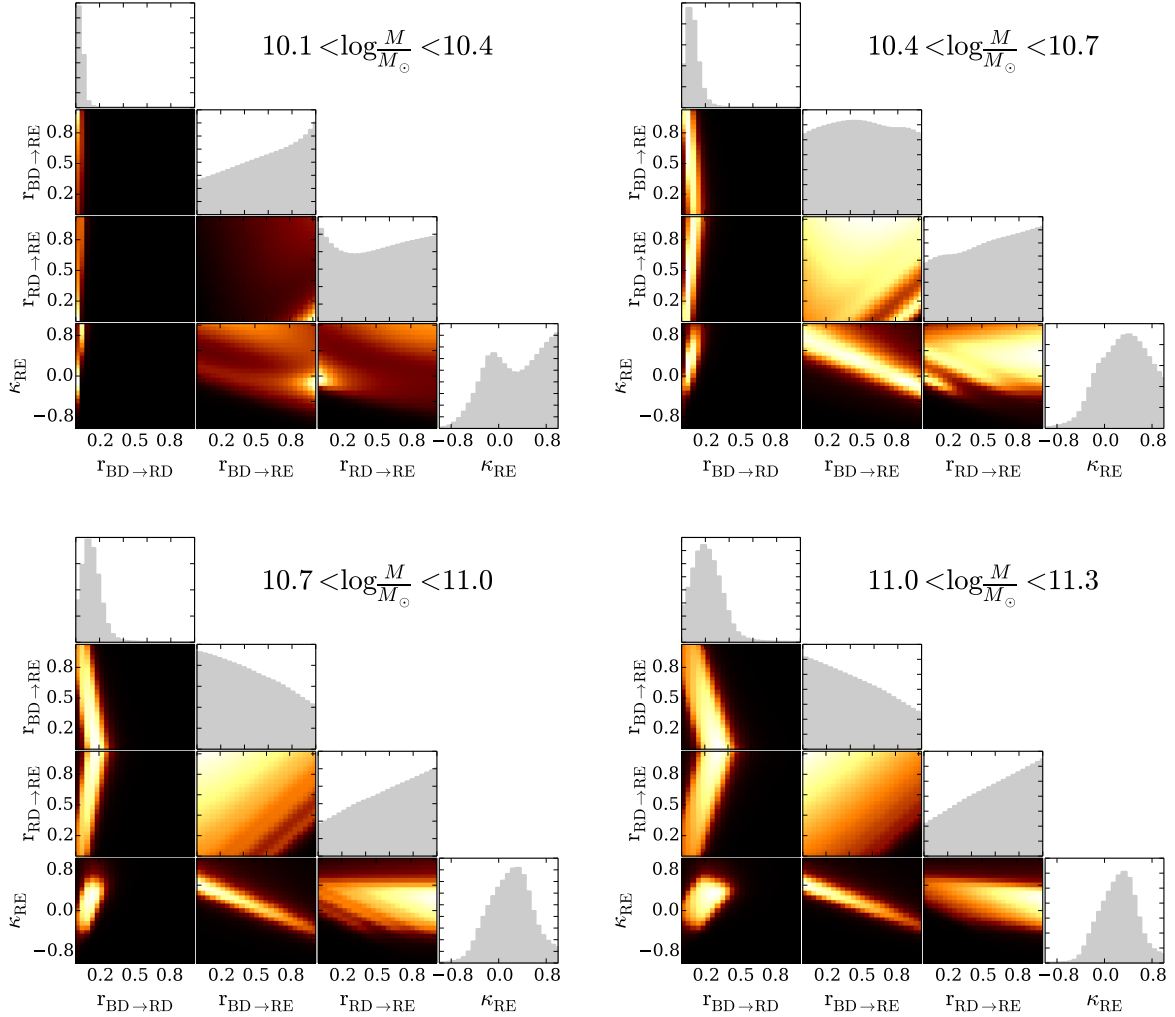


Figure 9. Results of the grid-search for the best-fit rate parameters $r_{BD \rightarrow RD}$, $r_{BD \rightarrow RE}$, $r_{RD \rightarrow RE}$, and κ_{RE} for four mass bins. The units for all rate parameters is Gyr^{-1} . 25 equally-spaced values were tested between (0,1) for each parameter, with the exception of κ_{RE} which was tested for 25 values between (-1,1); these are represented by the 25 bins on each axis. Each bin is weighted by $1/\chi^2$, such that white regions correspond to parameters which produced the lowest χ^2 , and black representing the highest. There is a strong result in the dependence of $r_{BD \rightarrow RD}$ with mass, such that the fraction of blue disks which transition to red disks (ie, quench without disrupting the disk), increases for more massive galaxies. The other parameters are less constrained by this model; therefore a more complex semi-analytic model will be necessary for obtaining the precise values of these rates, and is the subject of future work.

sive galaxies are more likely to become passive disks (given by the increase of $r_{BD \rightarrow RD}$ with increasing mass), and 2) less massive galaxies who enter a red disk phase are more likely than massive galaxies to stay in that phase, rather than transform to elliptical (given by the increase of $f_{D|R}$ from $z = 1$ to $z = 0.3$ for low mass bins).

Our first point is in agreement with literature which explores the unimodality of disk galaxies across a CMD (Schawinski et al. 2014; Powell et al. 2017). The smooth transition from the blue cloud to the red sequence in the distribution of low to medium mass disk galaxies is evi-

dence for slow quenching timescales. For higher mass disk galaxies, the unimodality is broken, suggesting a more rapid quenching. This could be due to a higher merger rate for more massive galaxies, or as suggested by Schawinski et al. (2014), evidence for a mass-quenching effect, in which the galaxy’s halo reaches a critical mass whereby the gas is inhibited from cooling sufficiently to continue star-formation (Kormendy & Kennicutt 2004; Dekel & Birnboim 2006; Peng et al. 2010). This result is also consistent with B10, who observe the strongest decrease in $f_{D|R}$ from $z = 1$ to $z = 0.3$ for their most massive galaxies.

Our second point is in disagreement with B10, who observe downward trends in $f_{D|R}$ in low mass galaxies. At the lowest redshift bin ($z \sim 0.3$), we measure similar absolute fractions of disks occupying the red sequence for all masses. However, B10 find their contribution to increase at higher lookback time to $z = 1$, while we find a decreasing contribution. The fact that our results agree for the highest mass at all redshifts, but only at the lowest redshift for lower masses, suggests the differences may be attributed in biases in morphological classification. B10 indentifies early and late-type disk galaxies using ZEST (Scarlata et al. 2007) morphologies, which they acknowledge are biased towards disk classification for faint apparent magnitudes, which tend to be attributed to the lowest mass, highest redshift objects. This bias could influence their observed increase in red sequence disks toward $z = 1$ for low masses. On the opposite end, GZ classifications tend to be biased towards elliptical morphologies at fainter magnitudes. We attempted to quantify and correct for this effect as described in Section 3.1, but if our correction was under-estimated, that may have driven the decreasing abundance of disk galaxies observed at increasing redshift for low masses. However, it has been shown in the local Universe that red disk galaxies tend to be more massive, as in Masters et al. (2011). If this is true at all epochs, we would not expect such a significant contribution of red disks for low mass galaxies as found in B10.

Add? More discussion of quenching mechanisms. Find place to discuss possibility of disks surviving/re-forming from mergers (Sparre & Springel 2016; Springel & Hernquist 2005; Robertson et al. 2006; Governato et al. 2009)

6 CONCLUSIONS

We have investigated the influence of the passive disk population by measuring the relative abundances of blue disks, red disks, and red ellipticals since $z = 1$ using morphological classifications from Galaxy Zoo: Hubble and rest-frame colors from UltraVISTA. Using data from artificially-redshifted FERENGI2 images to quantify the known redshift bias in the GZ classifications, we implemented a correction to the incompleteness in the number of disks detected as a function of redshift. The relative numbers were measured in terms of the fraction of disk galaxies that are red $f_{R|D}$ and the fraction of disk galaxies on the red sequence $f_{D|R}$. A simple toy-model was developed to simulate the evolution of these fractions as a function of the rates of three dominant evolutionary pathways: $r_{BD \rightarrow RD}$, the rate of blue disks quenching to red disks, $r_{BD \rightarrow RE}$, the rate of blue disks quenching and transforming directly to red ellipticals, and $r_{RD \rightarrow RE}$, the rate of red disks transforming to red ellipticals. Our main conclusions are as follows:

- $f_{R|D}$ and $f_{D|R}$ decrease from $z = 1$ to $z = 0.3$ for massive galaxies, and increase for the least massive galaxies.
- We estimate as high as 20% (+-error) of massive ($\log(M/M_\odot) > 11$) galaxies experience a passive disk phase. This fraction decreases with mass, down to 5+- % for galaxies $\log(M/M_\odot) < 10.4$.
- Low mass galaxies which experience a passive disk phase are more likely than massive galaxies to remain disks, while massive galaxies are more likely to continue thier evolution by transforming to passive ellipticals. To quantify and

validate this result would require a more sophisticated model than the simple approached used in this project.

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This project made heavy use of the Astropy packages in Python (Robitaille et al. 2013), the *seaborn* plotting package (Waskom et al. 2015), and the Tool for Operations on Catalogues And Tables (TOPCAT), which can be found at www.starlink.ac.uk/topcat/ (Taylor 2005).

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