

$$H = \text{angular momentum} = I \cdot pqr$$

$$\dot{H} = \sum M$$

$$\dot{H} = I pqr = I ((pqr)' + \text{cross}(pqr, H)) ??$$

$$\Rightarrow pqr = I^{-1} \sum M$$

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Total angular momentum

$$H = \underbrace{\frac{I_{\text{sat}}}{I_{\text{sat}}} \cdot pqr}_{\text{Sat angular accel}} + I_r 1B \cdot \omega_1 \cdot n_1 + I_r 2B \cdot \omega_2 \cdot n_2 + I_r 3B \cdot \omega_3 \cdot n_3$$

$$\begin{bmatrix} p \\ q \\ r \end{bmatrix} \times \begin{bmatrix} H_1 \\ H_2 \\ H_3 \end{bmatrix}$$

$$= \begin{bmatrix} qH_3 - rH_2 \\ rH_1 - pH_3 \\ pH_2 - qH_1 \end{bmatrix}$$

?

$$\text{Sat angular accel} = \frac{I^{-1}}{\text{total sat}} (-I_r M N \text{ - Reaction-wheels - cross } (pqr, H))$$

inertia of
RW in body
frame
about RW's
CoM

$$I_{r_1} B \cdot \dot{\omega}_1 \cdot n_1 + I_{r_2} B \cdot \dot{\omega}_2 \cdot n_2 + I_{r_3} B \cdot \dot{\omega}_3 \cdot n_3$$

'resistive' torque due to
changing angular velocity
about an axis with angular
momentum, I think

$$I = I_{\text{sat}} + I_{\text{sat}} B g + I_r 1B g + I_r 2B g$$

$$I_r 1B g = I_r 1B + m_r \cdot (s_r z') \cdot s_r z$$

$$I_r 1B + I_r 2B + I_r 3B$$

$$= \text{skew}(r)$$

$$T_r = \text{skew}(r)$$

(rotation of RW, unit

$$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = \text{aligned with } z$$

principle
off-axis distance

$$\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} = \text{turn off in } z \text{ direction}$$

from Sat CoM

$$\begin{bmatrix} I_{11} & I_{12} & 0 \\ 0 & I_{22} & I_{23} \\ 0 & 0 & I_{33} \end{bmatrix} \dot{\omega}_1 \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} I_{11} & 0 & 0 \\ 0 & I_{22} & 0 \\ 0 & 0 & I_{33} \end{bmatrix} \dot{\omega}_1 \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \xrightarrow{\Sigma} \begin{bmatrix} (I_{r_1} B)_{11} & \dot{\omega}_1 \\ (I_{r_2} B)_{21} & \dot{\omega}_2 \\ (I_{r_3} B)_{31} & \dot{\omega}_3 \end{bmatrix} = \begin{bmatrix} (I_{r_1} B)_{11} & \dot{\omega}_1 \\ (I_{r_2} B)_{21} & \dot{\omega}_2 \\ (I_{r_3} B)_{31} & \dot{\omega}_3 \end{bmatrix} \begin{bmatrix} \dot{\omega}_1 \\ \dot{\omega}_2 \\ \dot{\omega}_3 \end{bmatrix}$$

