```
In [1]: data <- read.csv2("SpotifyProjet.csv")</pre>
In [2]: str(data)
         'data.frame': 116 obs. of 16 variables:
                            : Factor w/ 91 levels "070 shake","50 cent",..: 17 3 28 84 87 77 54 19 52 60 ...

: Factor w/ 116 levels "\"2:30\"","\"911\"",..: 50 37 71 47 98 70 9 46 105 67 ...

: Factor w/ 19 levels "Acoustic","Afro",..: 16 14 17 16 17 1 11 3 16 18 ...
          $ ï..Artist
          $ Title
          $ Genre
          $ Danceability
                            : num 0.502 0.749 0.664 0.805 0.645 0.365 0.778 0.782 0.509 0.743 ...
                              : num 0.64 0.491 0.609 0.498 0.534 0.273 0.695 0.559 0.544 0.622 ...
          $ Energy
                              : int 6 10 1 7 6 4 4 6 5 4 ...
          $ Key
          $ Loudness
                              : num -9.7 -9.65 -6.51 -7.93 -10.8 ...
          $ Mode
                              : int 0110000000..
          $ Speechiness
                              : num 0.0286 0.0403 0.0707 0.0737 0.0479 0.038 0.0913 0.0767 0.0307 0.136 ...
          $ Acousticness
                             : num 0.0313 0.02 0.304 0.0203 0.157 0.94 0.175 0.125 0.63 0.904 ...
          $ Instrumentalness: num 2.16e-06 8.99e-03 0.00 2.37e-05 0.00 4.31e-01 0.00 0.00 1.48e-01 1.66e-05 ...
          $ Liveness
                            : num 0.154 0.159 0.0926 0.085 0.0863 0.109 0.15 0.385 0.1 0.143 ...
          $ Valence
                              : num 0.449 0.536 0.194 0.636 0.463 0.238 0.472 0.685 0.206 0.317 ...
                              : num 211 293 211 214 226 ...
          $ Duration
                              : num 132 120 130 121 105 ...
          $ Tempo
                              : Factor w/ 2 levels "No", "Yes": 2 2 2 2 2 2 2 2 2 2 ...
          $ Liked
```

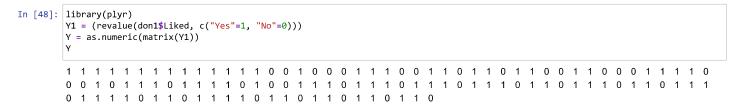
On enlève les 3 premières colonnes de notre dataframe pour simplifier l'étude

In [47]: #don1 représente l'ensemble des données sans les deux premières colonnes Artist et titre
 don1=data[,-(1:3)]
 #don représente nos données en enlevant la variable Liked que l'on va transformer en nombre binaire et remettre dans don
 don=don1[,-13]
 don

	_										_
Danceability		Key	Loudness		<u> </u>		Instrumentalness		Valence	Duration	Tempo
0.502	0.6400	6	-9.702	0	0.0286	0.031300	2.16e-06	0.1540	0.449	210.730	131.551
0.749	0.4910	10	-9.655	1	0.0403	0.020000	8.99e-03	0.1590	0.536	292.613	119.528
0.664	0.6090	1	-6.509	1	0.0707	0.304000	0.00e+00	0.0926	0.194	210.560	130.041
0.805	0.4980	7	-7.927	0	0.0737	0.020300	2.37e-05	0.0850	0.636	214.215	121.006
0.645	0.5340	6	-10.800	0	0.0479	0.157000	0.00e+00	0.0863	0.463	226.467	105.020
0.365	0.2730	4	-16.526	0	0.0380	0.940000	4.31e-01	0.1090	0.238	248.695	132.285
0.778	0.6950	4	-6.865	0	0.0913	0.175000	0.00e+00	0.1500	0.472	132.780	149.996
0.782	0.5590	6	-7.106	0	0.0767	0.125000	0.00e+00	0.3850	0.685	188.344	129.992
0.509	0.5440	5	-6.798	0	0.0307	0.630000	1.48e-01	0.1000	0.206	241.747	71.502
0.743	0.6220	4	-5.332	0	0.1360	0.904000	1.66e-05	0.1430	0.317	183.133	140.054
0.501	0.0958	0	-15.605	1	0.0433	0.770000	0.00e+00	0.2980	0.204	248.808	108.741
0.653	0.7020	4	-10.106	0	0.1170	0.023200	3.36e-02	0.0864	0.258	211.559	169.950
0.762	0.7290	6	-8.076	0	0.0679	0.481000	1.37e-04	0.1080	0.482	225.040	119.956
0.657	0.6430	8	-6.661	0	0.0433	0.482000	2.08e-06	0.1890	0.394	251.670	82.516
0.845	0.7170	5	-6.771	0	0.2110	0.666000	0.00e+00	0.1100	0.686	160.893	122.491
0.417	0.9340	7	-3.908	0	0.1130	0.000278	1.50e-03	0.1320	0.287	210.240	127.066
0.537	0.7460	10	-5.507	0	0.1500	0.023600	1.01e-06	0.1560	0.252	198.267	170.062
0.834	0.6240	9	-8.565	0	0.0838	0.072900	0.00e+00	0.1060	0.831	232.373	115.981
0.824	0.5880	6	-6.400	0	0.0924	0.692000	1.04e-04	0.1490	0.513	209.438	98.027
0.838	0.5250	10	-3.562	1	0.0665	0.345000	1.92e-06	0.0771	0.884	134.256	144.981
0.828	0.5210	10	-5.583	1	0.1370	0.858000	0.00e+00	0.1300	0.369	200.475	106.009
0.675	0.5620	7	-7.678	1	0.0352	0.233000	0.00e+00	0.0816	0.309	256.533	130.098
0.685	0.7060	11	-7.020	0	0.0545	0.089400	2.87e-02	0.0986	0.640	172.293	155.989
0.637	0.6430	4	-6.571	1	0.0519	0.130000	1.80e-06	0.1420	0.533	200.690	97.008
0.625	0.6040	10	-7.415	0	0.3390	0.257000	2.06e-05	0.1290	0.372		174.089
0.518	0.5720	10	-6.706	0	0.0416	0.050300	2.41e-05	0.1290	0.291	196.767	130.053
0.693	0.4940	1	-7.252	0	0.1080	0.139000	1.87e-04	0.1110	0.302		135.022
0.445	0.3670	0	-13.086	1	0.0452	0.761000	7.50e-02	0.0987	0.202	165.592	
0.610	0.5080	8	-6.682	0	0.1520	0.297000	0.00e+00	0.3840	0.758	137.876	178.818
0.421	0.1310	0	-18.435	1	0.0382	0.952000	4.53e-03	0.1090	0.120	291.796	137.446
											137.440
0.506	0.553		7 754		0.2050	 6 <b>.</b> 45e-01	0.00-100				
0.506		10	-7.751	0	0.3850		0.00e+00	0.1220	0.3290	237.459	173.603
0.699	0.668	5	-4.272	0	0.0336	1.54e-01	3.20e-06	0.3620	0.3140	148.230	144.105
0.604	0.260	11	-10.498	1	0.0373	8.41e-01	9.33e-05	0.3270	0.3180	185.689	100.901
0.633	0.526	6	-8.433	0	0.1050	4 <u>.</u> 53e-04	1.36e-04	0.0800	0.2760	156,522	91.970
0.485	0.627	1	-9.702	0	0.0416	7.37e-02	1.14e-05	0.3380	0.3590	198.635	92.163
0.618	0.793	0	-5.711	1	0.0601	2.04e-01	1.54e-02	0.1260	0.4590	347.526	101.015
0.725	0.534	11	-6.238	1	0.0946	7 <u>.</u> 52e-02	0.00e+00	0.0919	0.5580	219.320	91.974
0.735	0.795	11	-6.523	0	0.1130	2.96e-02	3.18e-05	0.0678	0.9050	188.918	122.000
0.748	0.627	7	-6.029	1	0.0639	1.31e-01	0.00e+00	0.0852	0.5240	188.491	120.963
0.671	0.501	4	-13.119	1	0.0594	3.42e-01	0.00e+00	0.1940	0.8600	214.880	87.040
0.664	0.771	0	-5.779	1	0.0533	1.55e-02	9.60e-06	0.4600	0.7630	265.600	109.945
0.765	0.402	6	-6.387	1	0.0557	1.78e-02	1.84e-05	0.1100	0.3530	188.854	87.054
0.319	0.995	0	-2.940	1	0.0848	6.53e-04	0.00e+00	0.2740	0.3340	126.520	155.232
0.515	0.479	3	<b>-</b> 7.458	1	0.0261	5.44e-01	5.98e-03	0.1910	0.2840	209.274	88.964
0.548	0.450	7	-7.582	1	0.0472	4.55e-01	0.00e+00	0.1010	0.3290	161.290	185.960
0.766	0.622	5	-5.292	0	0.1010	6.39e-02	0.00e+00	0.2070	0.6790	191.493	140.076
0.490	0.386	8	-6.160	1	0.0357	7.52e-01	0.00e+00	0.1040	0.2330	221.824	80.599
0.180	0.934	4	-8.699	1	0.1150	3.32e-05	5.51e-04	0.0702	0.4330	130.267	197.043
0.583	0.621	5	-6.902	0	0.0479	9.72e-03	1.06e-03	0.1810	0.3990	323.480	140.036
0.896	0.675	1	-3.908	1	0.1240	3 <u>.</u> 46e-01	8.11e-06	0.2620	0.6590	213.989	131.999
0.785	0.871	4	-2.692	0	0.2650	1.44e-01	0.00e+00	0.3090	0.3150	290.427	87.248
0.644	0.211	0	-13.966	1	0.0394	8.98e-01	9.70e-02	0.0757	0.4070	169.045	140.058
0.391	0.205	9	-14.148	1	0.0452	7 <u>.</u> 63e-01	2.47e-03	0.3640	0.1140	315.716	78.004
0.502	0.898	2	-8.912	1	0.0469	1.64e-03	0.00e+00	0.3360	0.7650	120.333	117.246

Danceability	Energy	Key	Loudness	Mode	Speechiness	Acousticness	Instrumentalness	Liveness	Valence	Duration	Tempo
0.646	0.770	2	-6.596	0	0.2260	2.49e-03	0.00e+00	0.0715	0.6810	236.133	99.165
0.681	0.514	1	-6.272	0	0.0676	1.91e-01	2.07e-02	0.0983	0.1450	194.120	150.979
0.754	0.702	10	-6.378	0	0.2640	3.12e-01	0.00e+00	0.2890	0.3830	230.800	145.959
0.666	0.542	8	-6.429	1	0.0392	2.70e-01	0.00e+00	0.0765	0.0771	228.787	120.134
0.507	0.790	0	-7.307	0	0.0294	2.33e-01	1.39e-01	0.1450	0.6000	320.467	147.065
0.667	0.659	2	-4.932	1	0.0298	1.13e-01	0.00e+00	0.3250	0.5750	203.440	89.128

On transforme l'output Liked en 0 et 1



In [49]: #Y est La variable Liked codée en 0 ou 1
don\$Y = Y
don

Danceability	Energy	Key	Loudness	Mode	Speechiness	Acousticness	Instrumentalness	Liveness	Valence	Duration	Tempo	Y
0.502	0.6400	6	-9.702	0	0.0286	0.031300	2.16e-06	0.1540	0.449	210.730	131.551	1
0.749	0.4910	10	-9.655	1	0.0403	0.020000	8.99e-03	0.1590	0.536	292.613	119.528	1
0.664	0.6090	1	-6.509	1	0.0707	0.304000	0.00e+00	0.0926	0.194	210.560	130.041	1
0.805	0.4980	7	-7.927	0	0.0737	0.020300	2.37e-05	0.0850	0.636	214.215	121.006	1
0.645	0.5340	6	-10.800	0	0.0479	0.157000	0.00e+00	0.0863	0.463	226.467	105.020	1
0.365	0.2730	4	-16.526	0	0.0380	0.940000	4.31e-01	0.1090	0.238	248.695	132.285	1
0.778	0.6950	4	-6.865	0	0.0913	0.175000	0.00e+00	0.1500	0.472	132.780	149.996	1
0.782	0.5590	6	-7.106	0	0.0767	0.125000	0.00e+00	0.3850	0.685	188.344	129.992	1
0.509	0.5440	5	-6.798	0	0.0307	0.630000	1.48e-01	0.1000	0.206	241.747	71.502	1
0.743	0.6220	4	-5.332	0	0.1360	0.904000	1.66e-05	0.1430	0.317	183.133	140.054	1
0.501	0.0958	0	-15.605	1	0.0433	0.770000	0.00e+00	0.2980	0.204	248.808	108.741	1
0.653	0.7020	4	-10.106	0	0.1170	0.023200	3.36e-02	0.0864	0.258	211.559	169.950	1
0.762	0.7290	6	-8.076	0	0.0679	0.481000	1.37e-04	0.1080	0.482	225.040	119.956	1
0.657	0.6430	8	-6.661	0	0.0433	0.482000	2.08e-06	0.1890	0.394	251.670	82.516	1
0.845	0.7170	5	-6.771	0	0.2110	0.666000	0.00e+00	0.1100	0.686	160.893	122.491	0
0.417	0.9340	7	-3.908	0	0.1130	0.000278	1.50e-03	0.1100	0.287			0
										210.240	127.066 170.062	
0.537	0.7460	10	-5.507	0	0.1500	0.023600	1.01e-06 0.00e+00	0.1560	0.252			1
0.834	0.6240	9	-8.565	0	0.0838	0.072900		0.1060	0.831	232.373	115.981	0
0.824	0.5880	6	-6.400	0	0.0924	0.692000	1.04e-04	0.1490	0.513	209.438	98.027	0
0.838	0.5250	10	-3.562	1	0.0665	0.345000	1.92e-06	0.0771	0.884	134.256	144.981	0
0.828	0.5210	10	-5.583	1	0.1370	0.858000	0.00e+00	0.1300	0.369	200.475	106.009	1
0.675	0.5620	7	-7.678	1	0.0352	0.233000	0.00e+00	0.0816	0.309	256.533	130.098	1
0.685	0.7060	11	-7.020	0	0.0545	0.089400	2.87e-02	0.0986	0.640	172.293	155.989	1
0.637	0.6430	4	-6.571	1	0.0519	0.130000	1.80e-06	0.1420	0.533	200.690	97.008	0
0.625	0.6040	10	-7.415	0	0.3390	0.257000	2.06e-05	0.1290	0.372	169.722	174.089	0
0.518	0.5720	10	-6.706	0	0.0416	0.050300	2.41e-05	0.1290	0.291	196.767	130.053	1
0.693	0.4940	1	-7.252	0	0.1080	0.139000	1.87e-04	0.1110	0.302	241.842	135.022	1
0.445	0.3670	0	-13.086	1	0.0452	0.761000	7.50e-02	0.0987	0.202	165.592	155.675	0
0.610	0.5080	8	-6.682	0	0.1520	0.297000	0.00e+00	0.3840	0.758	137.876	178.818	1
0.421	0.1310	0	-18.435	1	0.0382	0.952000	4.53e-03	0.1090	0.120	291.796	137.446	1
0.506	0.553	10	-7.751	0	0.3850	6.45e-01	0.00e+00	0.1220	0.3290	237.459	173.603	0
0.699	0.668	5	-4.272	0	0.0336	1.54e-01	3.20e-06	0.3620	0.3140	148.230	144.105	1
0.604	0.260	11	-10.498	1	0.0373	8.41e-01	9.33e-05	0.3270	0.3180	185.689	100.901	1
0.633	0.526	6	-8.433	0	0.1050	4.53e-04	1.36e-04	0.0800	0.2760	156.522	91.970	1
0.485	0.627	1	-9.702	0	0.0416	7.37e-02	1.14e-05	0.3380	0.3590	198.635	92.163	0
0.618	0.793	0	-5.711	1	0.0601	2.04e-01	1.54e-02	0.1260	0.4590	347.526	101.015	1
0.725	0.534	11	-6.238	1	0.0946	7.52e-02	0.00e+00	0.0919	0.5580	219.320	91.974	1
0.735	0.795	11	-6.523	0	0.1130	2.96e-02	3.18e-05	0.0678	0.9050	188.918	122.000	1
0.748	0.627	7	-6.029	1	0.0639	1.31e-01	0.00e+00	0.0852	0.5240	188.491	120.963	1
0.671	0.501	4	-13.119	1	0.0594	3.42e-01	0.00e+00	0.1940	0.8600	214.880	87.040	0
0.664	0.771	0	-5.779	1	0.0533	1.55e-02	9.60e-06	0.4600	0.7630	265.600	109.945	1
0.765	0.402	6	-6.387	1	0.0557	1.78e-02	1.84e-05	0.1100	0.3530	188.854	87.054	1
0.319	0.995	0	-2.940	1	0.0848	6.53e-04	0.00e+00	0.2740	0.3340	126.520	155.232	0
0.515	0.479	3	-7.458	1	0.0261	5.44e-01	5.98e-03	0.1910	0.2840	209.274	88.964	1
0.548	0.450	7	-7.582	1	0.0472	4.55e-01	0.00e+00	0.1010	0.3290	161.290	185.960	1
0.766	0.622	5	-5.292	0	0.1010	6.39e-02	0.00e+00	0.2070	0.6790	191.493	140.076	1
0.490	0.386	8	-6.160	1	0.0357	7.52e-01	0.00e+00	0.1040	0.2330	221.824	80.599	1
0.180	0.934	4	-8.699	1	0.1150	3.32e-05	5.51e-04	0.0702	0.4330	130.267	197.043	0
0.583	0.621	5	-6.902	0	0.0479	9.72e-03	1.06e-03	0.1810	0.3990	323.480	140.036	1
0.896	0.675	1	-3.908	1	0.1240	3.46e-01	8.11e-06	0.2620	0.6590	213.989	131.999	1
0.785	0.871	4	-2.692	0	0.2650	1.44e-01	0.00e+00	0.3090	0.3150	290.427	87.248	0
0.644	0.211	0	-13.966	1	0.0394	8.98e-01	9.70e-02	0.0757	0.4070	169.045	140.058	1
0.391	0.205	9	-14.148	1	0.0452	7.63e-01	2.47e-03	0.3640	0.1140	315.716	78.004	1
0.502	0.898	2	-8.912	1	0.0469	1.64e-03	0.00e+00	0.3360	0.7650	120.333	117.246	0

Danceability	Energy	Key	Loudness	Mode	Speechiness	Acousticness	Instrumentalness	Liveness	Valence	Duration	Tempo	Υ
0.646	0.770	2	-6.596	0	0.2260	2.49e-03	0.00e+00	0.0715	0.6810	236.133	99.165	1
0.681	0.514	1	-6.272	0	0.0676	1.91e-01	2.07e-02	0.0983	0.1450	194.120	150.979	1
0.754	0.702	10	-6.378	0	0.2640	3.12e-01	0.00e+00	0.2890	0.3830	230.800	145.959	0
0.666	0.542	8	-6.429	1	0.0392	2.70e-01	0.00e+00	0.0765	0.0771	228.787	120.134	1
0.507	0.790	0	-7.307	0	0.0294	2.33e-01	1.39e-01	0.1450	0.6000	320.467	147.065	1
0.667	0.659	2	-4.932	1	0.0298	1.13e-01	0.00e+00	0.3250	0.5750	203.440	89.128	0

Regression multiple afin de pouvoir tester une méthode par la suite :

```
In [8]: fit.lm = lm(Y\sim., data=don)
         summary(fit.lm)
         Call:
         lm(formula = Y \sim ., data = don)
         Residuals:
                      10 Median
             Min
                                        30
                                                Max
         -0.8823 -0.3050 0.1146 0.2604 0.7412
         Coefficients:
                             Estimate Std. Error t value Pr(>|t|)
                            1.375e+00 4.833e-01 2.844 0.00537 ** 7.516e-01 3.302e-01 2.276 0.02491 *
         (Intercept)
         Danceability
         Energy
                           -6.739e-01 3.772e-01 -1.786 0.07697 .
                            5.717e-03 1.115e-02 0.513 0.60917
         Kev
         Loudness
                            1.710e-02 2.056e-02 0.832 0.40749
                           -1.131e-01 8.532e-02 -1.325 0.18807
-1.760e+00 6.056e-01 -2.906 0.00448 **
         Mode
         Speechiness
                           -1.845e-01 1.867e-01 -0.989 0.32517
         Acousticness
        Instrumentalness 1.415e-01 2.982e-01 0.475 0.63611
Liveness -5.129e-01 2.860e-01 -1.793 0.07587
         Valence
                           -7.207e-01 2.203e-01 -3.271 0.00146 **
         Duration
                           -2.980e-06 2.022e-06 -1.474 0.14364
                           -1.998e-06 1.826e-06 -1.094 0.27663
         Tempo
         Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
         Residual standard error: 0.4127 on 103 degrees of freedom
                                           Adjusted R-squared: 0.2226
         Multiple R-squared: 0.3037,
         F-statistic: 3.744 on 12 and 103 DF, p-value: 0.0001045
```

Méthode 0 : Utilisation de la fonction Step qui se base sur l'AIC

```
In [9]: step(fit.lm)
                       Dt Sum ot Sq
                                      RSS
        <none>
                                   18.054 -199.79
        - Mode
                           0.32511 18.379 -199.72
        - Energy
                           0.33471 18.389 -199.66
        - Duration
                           0.33790 18.392 -199.64
                       1
        - Liveness
                       1
                           0.72818 18.782 -197.20
        - Danceability 1 1.43819 19.492 -192.90
        - Speechiness 1
                           1.61784 19.672 -191.83
                       1 2.07747 20.131 -189.15
        - Valence
        Call:
        lm(formula = Y ~ Danceability + Energy + Mode + Speechiness +
            Liveness + Valence + Duration, data = don)
        Coefficients:
         (Intercept) Danceability
                                                                Speechiness
                                         Energy
                                                         Mode
                         8.903e-01
           9.493e-01
                                      -3.179e-01
                                                    -1.168e-01
                                                                  -1.843e+00
            Liveness
                           Valence
                                       Duration
          -5.754e-01
                        -7.371e-01
                                      -2.816e-06
```

```
-5.754e-01 -7.371e-01 -2.816e-06

In [10]: library(leaps)
```

Méthode 1 : Choix de meilleurs sous-ensembles

"package 'leaps' was built under R version 3.6.3"

Warning message:

```
In [11]: reg.mod=regsubsets(Y~., data=don, nvmax=12)
         reg.sum= summary(reg.mod)
         reg.sum
         Subset selection object
         Call: regsubsets.formula(Y \sim ., data = don, nvmax = 12)
         12 Variables (and intercept)
                          Forced in Forced out
         Danceability
                               FALSE
                                          FALSE
         Energy
                               FALSE
                                          FALSE
                               FALSE
                                          FALSE
         Key
         Loudness
                               FALSE
                                          FALSE
         Mode
                               FALSE
                                          FALSE
         Speechiness
                               FALSE
                                          FALSE
         Acousticness
                               FALSE
                                          FALSE
         Instrumentalness
                               FALSE
                                          FALSE
         Liveness
                               FALSE
                                          FALSE
         Valence
                               FALSE
                                          FALSE
         Duration
                               FALSE
                                          FALSE
         Tempo
                               FALSE
                                          FALSE
         1 subsets of each size up to 12
         Selection Algorithm: exhaustive
                   Danceability Energy Key Loudness Mode Speechiness Acousticness
            (1)
            (1)
         2
         3
            (1)
                                        . . . . .
                                                     . .
                   "*"
                                                          "*"
         4
            (1)
         5
            (1)
                    "*"
                                                          n * n
                   "*"
                                                     . .
                                                          "*"
         6
            (1)
                    "*"
         7
            (1)
                                 "*"
                                                     "*"
                                                          "*"
         8
            (1)
                                        . . . . .
                   "*"
                                 "*"
                                                                      "*"
            (1)
                                                     "*"
                                                          "*"
         10
             (1)
                   *"
                                 "*"
                                        . . . . . . . . .
                                                     "*"
                                                         "*"
                                                                      "*"
         11
                   "*"
         12
             (1)
                    Instrumentalness Liveness Valence Duration
                                                      . .
                                     "*"
                                              "*"
            (1)
         2
                                     . .
                                                      . .
         3
                                     *"
                                              "*"
         4
            (1)
                                     "*"
                                              "*"
                                                      "*"
            (1)
                                     "*"
                                              "*"
                                                      "*"
         6
            (1)
                                     "*"
                                              "*"
                                                      "*"
            (1)
                                     "*"
         8
            (1)
                                     "*"
                                              "*"
                                                      "*"
                                                               "*"
            (1)
                                     n*n
                                              "*"
                                                      "*"
                                                               "*"
         10
            (1)
                                     "*"
                                              "*"
                                                      "*"
                                                               "*"
            (1)
         11
            (1)"*"
                                     "*"
In [12]: which.max(reg.sum$adjr2)
In [13]: par(mfrow=c(1,2))
         plot(reg.sum$rss,xlab="Number of Variables",ylab="RSS",type="l")
         plot(reg.sum$adjr2,xlab="Number of Variables",ylab="Adjusted RSq",type="l")
         points(7,reg.sum$adjr2[7], col="red",cex=2,pch=20)
                22
                                                                        20
                2
          CO
```

```
In [104]: coef(reg.mod,7)
                      (Intercept) 0.94930854265269
                    Danceability 0.890278781821163
                         Energy -0.317889103744736
                          Mode -0.116798447920091
                    Speechiness -1.84286440239108
                       Liveness -0.575396979295119
                        Valence -0.737075868494187
                        Duration -2.81552562161636e-06
In [14]: set.seed(2226947)
          #valeurs1=matrix(data=c("Valeur K", "Taux d'erreur"), ncol=2, byrow = TRUE)
          for (j in 1:4){
              train_data <- don[-((j*29 -28):(j*29)), ]</pre>
              test_data <- don[((j*29 -28):(j*29)), ]
              regsub= regsubsets(Y~., data = train_data, nvmax=12)
              summary(regsub)
                      # number of folds
In [15]: k = 4
          set.seed(2226947)
          folds = sample(1:k, nrow(don), replace = TRUE)
          err = matrix(NA, k, 12, dimnames = list(NULL, paste(1:12)))
In [16]: predict.regsubsets = function(object, newdata, id,...){
                form = as.formula(object$call[[2]])
                mat = model.matrix(form, newdata)
                coefi = coef(object,id=id)
                xvars = names(coefi)
                mat[,xvars]%*%coefi
In [17]: # Outer loop iterates over all folds
          for(j in 1:k){
              # The perform best subset selection on the full dataset, minus the jth fold
              best_fit = regsubsets(Y~., data = don[folds!=j,], nvmax=12)
              # Inner Loop iterates over each size i
              for(i in 1:12){
                  # Predict the values of the current fold from the "best subset" model on i predictors
                  pred = predict(best_fit, don[folds==j,], id=i)
                  # Calculate the MSE, store it in the matrix we created above
                  err[j,i] = mean((don$Y[folds==j]-pred)^2)
              }
          }
```

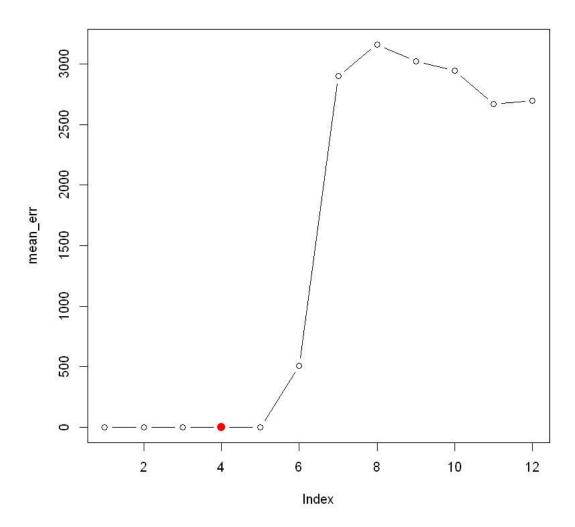
```
In [18]: # Take the mean of over all folds for each model size
    mean_err = apply(err, 2, mean)
    err
    mean_err

# Find the model size with the smallest cross-validation error
    min = which.min(mean_err)

# Plot the cross-validation error for each model size, highlight the min
    plot(mean_err, type='b')
    points(min, mean_err[min][1], col = "red", cex = 2, pch = 20)
```

1	2	3	4	5	ь	,	8	9	10	11	12
0.2636625	0.2623522	0.2380631	0.2409974	0.2431175	0.2477781	0.2469477	2.394767e-01	0.2490127	0.2552201	0.2377066	0.2386266
0.2319110	0.2421341	0.2204401	0.2226099	0.2276376	0.2493920	0.2648501	2.634830e-01	0.2177543	0.2142297	0.2142856	0.2146316
0.1885998	0.1892376	0.1819801	0.1715273	0.1854597	2030.6439699	2046.0261804	2.574892e+03	2238.9425856	2159.8729943	2187.2199480	2240.9495701
0.2088486	0.2177904	0.2043900	0.1895745	0.1911745	0.1912477	9552.0751883	1.006546e+04	9853.6208938	9609.7455420	8496.8821390	8539.9992016

- 1 0.223255479090055
- 2 0.227878589570813
- **3** 0.211218336716169
- 4 0.206177270259003
- **5** 0.211847317739552
- **6** 507.833096919807
- **7** 2899.65329162691
- **8** 3160.21375103754
- 9 3023.25756159433
- **10** 2942.52199651893
- **11** 2671.1385197973
- **12** 2695.35050748879

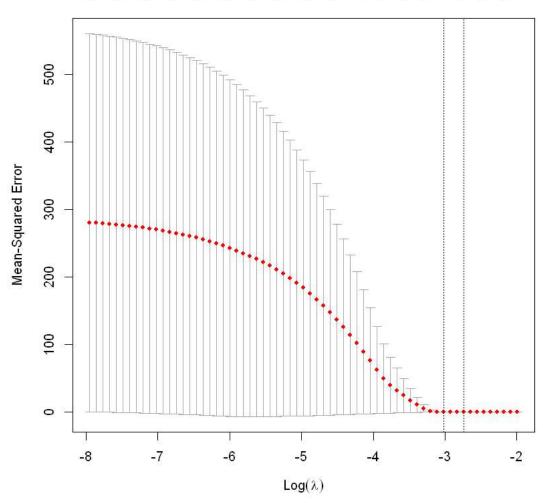


```
In [19]: reg_best = regsubsets(Y~., data = don, nvmax = 12)
          coef(reg_best, 4)
                       (Intercept)
                                   0.712607038565121
                     Danceability
                                   0.971118873548491
                    Speechiness
                                   -1.71083426848013
                                   -0.745126085550979
                        Liveness
                         Valence
                                   -0.844130615704666
In [20]: library(glmnet)
          Warning message: "package 'glmnet' was built under R version 3.6.3"Loading required package: Matrix
          Warning message:
          "package 'Matrix' was built under R version 3.6.3"Loaded glmnet 4.1-1
          Méthode 2 : Lasso
In [23]: #Lasso :
          grid<-10^seq(10,-2,length=100)</pre>
In [24]: x<-model.matrix(Y~.,don)</pre>
```

In [25]: lasso.mod<-glmnet(x,Y,alpha=1,lambda=grid)</pre>

```
In [26]: cv_out=cv.glmnet(x,Y,alpha=1)
plot(cv_out)
```

## 12 12 12 12 12 12 12 12 12 12 11 9 8 8 7 5 3 3



In [27]: bestlam<-cv\_out\$lambda.min # la valeur de lambda pour laquelle MSE est min
bestlam</pre>

## 0.0490970546599512

```
In [32]:
    set.seed(2226947)
    #valeurs1=matrix(data=c("Valeur K", "Taux d'erreur"), ncol=2, byrow = TRUE)
    mse = rep(0,4)
    for (j in 1:4){
        train_data_1 <- don[-((j*29-28):(j*29)), -13]
        result_data1 = don[-((j*29-28):(j*29)), 13]
        test_data_1 <- don[((j*29-28):(j*29)), 13]

        lasso.mod<-glmnet(train_data_1,result_data1,alpha=1,lambda=grid)
        lasso.pred=predict(lasso.mod,s=bestlam,newx=as.matrix(test_data_1))
        mse[j]=mean((lasso.pred-test_data1)^2)
    }
    mse
    mean(mse)</pre>
```

 $0.188687702447149 \quad 77.3451253953816 \quad 0.202030558423769 \quad 0.172628834125863$ 

19.4771181225946

```
In [33]: out=glmnet(x,Y,alpha=1,lambda=grid)
         lasso.coef=predict(out,type="coefficients",s=bestlam)[1:13,]
         lasso.coef
         lasso.coef[lasso.coef!=0]
                     (Intercept) 0.92748592906131
                     (Intercept)
                               0
                   Danceability
                               0.271120821289483
                       Energy
                                -0.235840801289313
                               0
                          Key
                     Loudness
                               n
                         Mode -0.00127613658312779
                  Speechiness -0.581987728471468
                  Acousticness 0
               Instrumentalness 0
                      Liveness -0.408923572338646
                       Valence -0.352546883641634
                      Duration -1.7719889127453e-07
                     (Intercept) 0.92748592906131
                   Danceability 0.271120821289483
                       Energy -0.235840801289313
                         Mode -0.00127613658312779
                  Speechiness -0.581987728471468
                      Liveness -0.408923572338646
                       Valence
                               -0.352546883641634
                      Duration -1.7719889127453e-07
In [40]: don_stdv <-scale(don[,-13])</pre>
         don_std <- data.frame(don_stdv)</pre>
         don_std$Y=Y
         str(don_std)
         'data.frame': 116 obs. of 13 variables:
          $ Danceability : num -0.9567 0.7342 0.1523 1.1175 0.0222 ...
          $ Energy
                           : num 0.2492 -0.5264 0.0878 -0.49 -0.3026 ...
                           : num 0.134 1.222 -1.227 0.406 0.134 ...
          $ Key
          $ Loudness
                           : num -0.693 -0.677 0.363 -0.106 -1.056 ...
          $ Mode
                          : num -0.979 1.013 1.013 -0.979 -0.979 ...
          $ Speechiness
                           : num -0.823 -0.655 -0.218 -0.175 -0.545 ...
                          : num -0.94266 -0.98193 0.00489 -0.98089 -0.5059 ...
          $ Acousticness
          $ Instrumentalness: num -0.3 -0.237 -0.3 -0.3 -0.3 ...
          $ Liveness : num -0.171 -0.136 -0.594 -0.647 -0.638 ...
          $ Valence
                           : num 0.0232 0.4199 -1.1397 0.8759 0.087 ...
                           : num -0.0929 -0.0887 -0.0929 -0.0927 -0.0921 ...
          $ Duration
                           : num -0.0925 -0.0931 -0.0926 -0.093 -0.0937 ...
          $ Tempo
                           : num 111111111...
In [42]:
         1 library(class)
         Warning message:
         "package 'class' was built under R version 3.6.3"
```

Méthode 3 : KNN

```
In [46]: #KNN - 4-FOLD
           K=50
           #Recherche du k optimal :
           set.seed(2226947)
           valeurs1=matrix(data=c("Valeur K", "Taux d'erreur"), ncol=2, byrow = TRUE)
           taux_err1 <- rep(0,4)</pre>
           for(i in 1:K){
           for (j in 1:4){
           train_data2 <- don_std[-((j*29-28):(j*29)), -13]
test_data2 <- don_std[((j*29-28):(j*29)), -13]
class_entr2 <- don[-((j*29 -28):(j*29)), 13]
           class_test2 <- don[((j*29-28):(j*29)), 13]</pre>
           knn_fold = knn(train=train_data2, test=test_data2, cl=class_entr2,k=i, prob=TRUE)
           taux_err1[j] = mean(knn_fold != don[((j*29-28):(j*29)), 13])
                valeurs1 = rbind(valeurs1, c(i,mean(taux_err1)))
           valeurs1
           valeurs1[8,] #taux d'erreur de K=7
           min(valeurs1)
```

Valeur K	Taux d'erreur
1	0.310344827586207
2	0.387931034482759
3	0.267241379310345
4	0.293103448275862
5	0.28448275862069
6	0.318965517241379
7	0.258620689655172
8	0.301724137931034
9	0.28448275862069
10	0.28448275862069
11	0.293103448275862
12	0.267241379310345
13	0.327586206896552
14	0.301724137931034
15	0.310344827586207
16	0.318965517241379
17	0.327586206896552
18	0.318965517241379
19	0.318965517241379
20	0.318965517241379
21	0.310344827586207
22	0.310344827586207
23	0.318965517241379
24	0.318965517241379
25	0.318965517241379
26	0.318965517241379
27	0.318965517241379
28	0.318965517241379
29	0.318965517241379
30	0.318965517241379
31	0.318965517241379
32	0.318965517241379
33	0.318965517241379
34	0.318965517241379
35	0.318965517241379
36	0.318965517241379
37	0.318965517241379
38	0.318965517241379
39	0.318965517241379
40	0.318965517241379
41	0.318965517241379
42	0.318965517241379
43	0.318965517241379
44	0.318965517241379
45	0.318965517241379
46	0.318965517241379
47	0.318965517241379
48	0.318965517241379
49	0.318965517241379
50	0.318965517241379

'7' '0.258620689655172'

'0.258620689655172'

```
In [101]: # KNN 4-FOLD AVEC LA MEILLEURE VALEUR DE K =7
          valeurs7=matrix(data=c("Valeur K", "Taux d'erreur"), ncol=2, byrow = TRUE)
          taux_err7 <- rep(0,4)</pre>
          for (j in 1:4){
          train_data7 <- don_std[-((j*29-28):(j*29)), -13]</pre>
          test_data7<- don_std[((j*29-28):(j*29)), -13]
          class_entr7 <- don[-((j*29 -28):(j*29)), 13]
          class_test7 <- don[((j*29-28):(j*29)), 13]</pre>
          knn_fold7 = knn(train=train_data7, test=test_data7, cl=class_entr7,k=7, prob=TRUE)
          taux_err7[j] = mean(knn_fold7 != class_test7)
              print(table(class_test7, knn_fold7))
              valeurs7 = rbind(valeurs7, c(i,mean(taux_err7)))
                     knn_fold7
          class_test7 0 1
                    0 1
                    1 0 21
                     knn_fold7
          class_test7 0 1
                    0 5 7
                    1 0 17
                     knn fold7
          class_test7 0 1
                    0 2 7
                    1 2 18
                     knn fold7
          class_test7 0 1
                    0 3 5
                    1 2 19
In [79]: don_entr<-don[-(20:67),]</pre>
          don test<-don[20:67,]</pre>
          Méthode 4 : Régression logsitique
In [80]: fit.logb<-glm(Y~., family=binomial,data=don_entr)</pre>
          summary(fit.logb)
          glm(formula = Y ~ ., family = binomial, data = don_entr)
          Deviance Residuals:
                       1Q Median
                                          3Q
                                                  Max
          -1.9972 -0.2461
                            0.2480 0.5591
          Coefficients:
                             Estimate Std. Error z value Pr(>|z|)
          (Intercept)
                            2.213919 6.082697 0.364 0.7159
                            7.796753 3.690739 2.113
-8.224604 4.383401 -1.876
          Danceability
                                                           0.0346
                                                           0.0606 .
          Energy
                            0.7694
          Key
          Loudness
                                                           0.2204
                            -0.094241 0.996176 -0.095
                                                           0.9246
                           -12.241213 6.368891 -1.922
-3.018936 1.947207 -1.550
          Speechiness
                                                           0.0546
          Acousticness
                                                           0.1210
          Instrumentalness 15.960012 17.289584 0.923
                                                           0.3560
          Liveness
                            -2.143883
                                       3.328173 -0.644
                                                           0.5195
          Valence
                            -3.440900
                                       2.475330 -1.390
                                                           0.1645
                             0.009314
                                        0.010276
                                                   0.906
                                                           0.3647
          Duration
          Tempo
                             0.027366
                                       0.019143 1.430
                                                           0.1528
          Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
          (Dispersion parameter for binomial family taken to be 1)
              Null deviance: 78.597 on 67 degrees of freedom
          Residual deviance: 48.603 on 55 degrees of freedom
          AIC: 74.603
          Number of Fisher Scoring iterations: 8
```

```
In [84]: prev_log<-predict(fit.logb,don_test,type="response")</pre>
       prev_log
                       20 0.959155111141887
                       21 0.790405663732002
                       22
                          0.980406096197397
                       23
                           0.91446117997479
                       24
                           0.758107074966233
                       25
                           0.386991486841755
                       26
                           0.940638125553914
                       27
                           0.987507137948899
                       28
                           0.886055353768732
                       29
                           0.648264980966115
                       30
                           0.830376824937906
                       31
                           0.789047748002245
                           0.999995291875837
                       32
                       33
                           0.942056324160013
                       34
                           0.801213170809787
                       35
                           0.998326323031655
                       36
                           0.965973243448102
                       37
                           0.754595467980921
                       38
                       39
                          0.967936375023105
                       40
                          0.475888096414484
                       41
                           0.597018097146328
                       42
                           0.953385273112769
                       43
                           0.95193225168022
                       44
                           0.866276120588576
                       45
                           0.172194845919893
                       46
                           0.0435694259610064
                       47
                           0.770990416843536
                       48
                           0.995800587587766
                       49
                           0.925726194264064
                       50
                           0.730027461048904
                           0.955976892713729
                       51
                       52
                           0.49170981758672
                       53
                           0.365466749806417
                       54
                           0.920154651538289
                       55
                           0.852398080708586
                       56
                           0.945360700128469
                       57
                           0.838819264648668
                       58
                       59
                          0.977575356028909
                       60
                           0.946215577053556
                       61
                           0.87239427332388
                       62
                           0.560601882604612
                       63
                           0.905773620957902
                       64
                           0.798818171878527
                       65
                           0.607289708182485
                       66
                           0.995132549492187
                       67
                           0.792292410261354
In [93]: test_y<-don_test$Y</pre>
        prev_y<-rep(0,length(test_y))</pre>
       prev_y[prev_log >=0.8] =1
       prev_y
       test_y
        0 1
            0
```

0 1 1

```
In [94]: | taux_err_log = mean(prev_y != test_y)
         # Matrice de confusion
         confus_log<-table(prev_y,test_y)</pre>
         confus_log
               test y
         prev_y 0 1
              0 9 9
              1 10 20
In [57]: library(boot)
         Warning message:
         "package 'boot' was built under R version 3.6.3"
In [58]: fit.log<-glm(Y~., family=binomial, data=don)</pre>
         summary(fit.log)
         glm(formula = Y ~ ., family = binomial, data = don_std)
         Deviance Residuals:
             Min
                       1Q Median
                                         3Q
         -2.1402 -0.6821 0.4230 0.7021 1.8255
         Coefficients:
                          Estimate Std. Error z value Pr(>|z|)
         (Intercept)
                          0.96816 0.81050 1.195 0.23228
                                      0.33692 2.301 0.02138 * 0.47525 -1.687 0.09165 .
         Danceability
                           0.77535
         Energy
                          -0.80163
                                      Key
                           0.04767
         Loudness
                           0.30139
                          -0.35033
                                      0.28337 -1.236 0.21635
         Mode
                                      0.26938 -2.619 0.00883 **
0.36072 -1.180 0.23819
         Speechiness
                          -0.70539
                          -0.42548
         Acousticness
         Instrumentalness 0.38703
                                       0.47971 0.807 0.41978
         Liveness
                         -0.43767
                                       0.25931 -1.688 0.09144 .
                                      0.32785 -3.093 0.00198 **
         Valence
                          -1.01396
                                      2.61873 -0.258 0.79641
7.83008 -0.100 0.92051
         Duration
                          -0.67561
         Tempo
                          -0.78135
         Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 145.25 on 115 degrees of freedom
         Residual deviance: 104.81 on 103 degrees of freedom
         AIC: 130.81
         Number of Fisher Scoring iterations: 10
In [59]: #Regression Logistique - 4-FOLD
         set.seed(2226947)
         cv.errlo1k<-cv.glm(don_std,fit.log, K=4)</pre>
         cv.errlo1k$delta
         Warning message:
         "glm.fit: fitted probabilities numerically 0 or 1 occurred"
         0.208909643066211 \quad 0.200356772895736
 In [ ]:
```