# C4W3\_Assignment

October 23, 2022

# 1 Week 3: Using RNNs to predict time series

Welcome! In the previous assignment you used a vanilla deep neural network to create forecasts for generated time series. This time you will be using Tensorflow's layers for processing sequence data such as Recurrent layers or LSTMs to see how these two approaches compare.

Let's get started!

```
[1]: import tensorflow as tf
import numpy as np
import matplotlib.pyplot as plt
from dataclasses import dataclass
```

## 1.1 Generating the data

The next cell includes a bunch of helper functions to generate and plot the time series:

```
[2]: def plot_series(time, series, format="-", start=0, end=None):
         plt.plot(time[start:end], series[start:end], format)
         plt.xlabel("Time")
         plt.ylabel("Value")
         plt.grid(False)
     def trend(time, slope=0):
         return slope * time
     def seasonal_pattern(season_time):
         """Just an arbitrary pattern, you can change it if you wish"""
         return np.where(season_time < 0.1,</pre>
                         np.cos(season_time * 6 * np.pi),
                         2 / np.exp(9 * season_time))
     def seasonality(time, period, amplitude=1, phase=0):
         """Repeats the same pattern at each period"""
         season_time = ((time + phase) % period) / period
         return amplitude * seasonal_pattern(season_time)
     def noise(time, noise_level=1, seed=None):
         rnd = np.random.RandomState(seed)
```

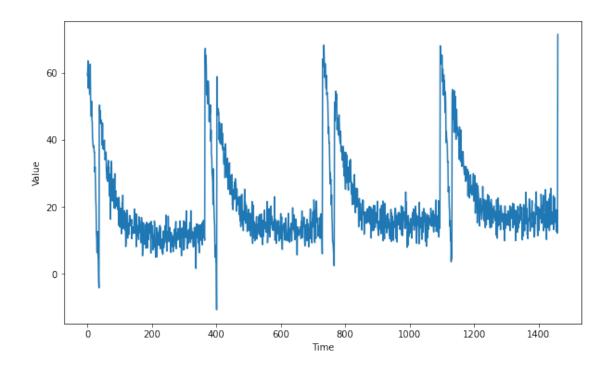
```
return rnd.randn(len(time)) * noise_level
```

You will be generating the same time series data as in last week's assignment.

Notice that this time all the generation is done within a function and global variables are saved within a dataclass. This is done to avoid using global scope as it was done in during the first week of the course.

If you haven't used dataclasses before, they are just Python classes that provide a convenient syntax for storing data. You can read more about them in the docs.

```
[3]: def generate_time_series():
         # The time dimension or the x-coordinate of the time series
         time = np.arange(4 * 365 + 1, dtype="float32")
         # Initial series is just a straight line with a y-intercept
         y_intercept = 10
         slope = 0.005
         series = trend(time, slope) + y_intercept
         # Adding seasonality
         amplitude = 50
         series += seasonality(time, period=365, amplitude=amplitude)
         # Adding some noise
         noise_level = 3
         series += noise(time, noise_level, seed=51)
         return time, series
     # Save all "global" variables within the G class (G stands for global)
     @dataclass
     class G:
         TIME, SERIES = generate_time_series()
         SPLIT_TIME = 1100
         WINDOW SIZE = 20
         BATCH SIZE = 32
         SHUFFLE_BUFFER_SIZE = 1000
     # Plot the generated series
     plt.figure(figsize=(10, 6))
     plot_series(G.TIME, G.SERIES)
     plt.show()
```



## 1.2 Processing the data

Since you already coded the train\_val\_split and windowed\_dataset functions during past week's assignments, this time they are provided for you:

```
[4]: def train_val_split(time, series, time_step=G.SPLIT_TIME):
    time_train = time[:time_step]
    series_train = series[:time_step]
    time_valid = time[time_step:]
    series_valid = series[time_step:]
    return time_train, series_train, time_valid, series_valid

# Split the dataset
time_train, series_train, time_valid, series_valid = train_val_split(G.TIME, G.
→SERIES)
```

```
def windowed_dataset(series, window_size=G.WINDOW_SIZE, batch_size=G.

BATCH_SIZE, shuffle_buffer=G.SHUFFLE_BUFFER_SIZE):
    dataset = tf.data.Dataset.from_tensor_slices(series)
    dataset = dataset.window(window_size + 1, shift=1, drop_remainder=True)
    dataset = dataset.flat_map(lambda window: window.batch(window_size + 1))
    dataset = dataset.shuffle(shuffle_buffer)
```

```
dataset = dataset.map(lambda window: (window[:-1], window[-1]))
  dataset = dataset.batch(batch_size).prefetch(1)
  return dataset

# Apply the transformation to the training set
dataset = windowed_dataset(series_train)
```

# 1.3 Defining the model architecture

Now that you have a function that will process the data before it is fed into your neural network for training, it is time to define you layer architecture. Unlike previous weeks or courses in which you define your layers and compile the model in the same function, here you will first need to complete the create\_uncompiled\_model function below.

This is done so you can reuse your model's layers for the learning rate adjusting and the actual training.

Hint: - Fill in the Lambda layers at the beginning and end of the network with the correct lamda functions. - You should use SimpleRNN or Bidirectional(LSTM) as intermediate layers. - The last layer of the network (before the last Lambda) should be a Dense layer.

```
print("Your current architecture is compatible with the windowed dataset! : _{\hookrightarrow})")
```

Your current architecture is compatible with the windowed dataset! :)

## 1.4 Adjusting the learning rate - (Optional Exercise)

As you saw in the lecture you can leverage Tensorflow's callbacks to dinamically vary the learning rate during training. This can be helpful to get a better sense of which learning rate better acommodates to the problem at hand.

Notice that this is only changing the learning rate during the training process to give you an idea of what a reasonable learning rate is and should not be confused with selecting the best learning rate, this is known as hyperparameter optimization and it is outside the scope of this course.

For the optimizers you can try out: - tf.keras.optimizers.Adam - tf.keras.optimizers.SGD with a momentum of 0.9

```
[9]: # Run the training with dynamic LR lr_history = adjust_learning_rate()
```

```
80.3207 - lr: 1.1220e-06
Epoch 3/100
11.6177 - lr: 1.2589e-06
Epoch 4/100
7.0964 - lr: 1.4125e-06
Epoch 5/100
6.3190 - lr: 1.5849e-06
Epoch 6/100
5.5773 - lr: 1.7783e-06
Epoch 7/100
4.8556 - lr: 1.9953e-06
Epoch 8/100
4.6122 - lr: 2.2387e-06
Epoch 9/100
4.4485 - lr: 2.5119e-06
Epoch 10/100
4.2913 - lr: 2.8184e-06
Epoch 11/100
4.2977 - lr: 3.1623e-06
Epoch 12/100
4.2715 - lr: 3.5481e-06
Epoch 13/100
4.2094 - lr: 3.9811e-06
Epoch 14/100
4.2873 - lr: 4.4668e-06
Epoch 15/100
4.2684 - lr: 5.0119e-06
Epoch 16/100
4.1821 - lr: 5.6234e-06
Epoch 17/100
4.1637 - lr: 6.3096e-06
Epoch 18/100
```

```
4.3310 - lr: 7.0795e-06
Epoch 19/100
4.5457 - lr: 7.9433e-06
Epoch 20/100
4.2573 - lr: 8.9125e-06
Epoch 21/100
4.2988 - lr: 1.0000e-05
Epoch 22/100
4.4316 - lr: 1.1220e-05
Epoch 23/100
3.9612 - lr: 1.2589e-05
Epoch 24/100
4.0928 - lr: 1.4125e-05
Epoch 25/100
4.6058 - lr: 1.5849e-05
Epoch 26/100
4.3846 - lr: 1.7783e-05
Epoch 27/100
4.1123 - lr: 1.9953e-05
Epoch 28/100
4.7654 - lr: 2.2387e-05
Epoch 29/100
4.1545 - lr: 2.5119e-05
Epoch 30/100
4.6095 - lr: 2.8184e-05
Epoch 31/100
3.7910 - lr: 3.1623e-05
Epoch 32/100
4.5838 - lr: 3.5481e-05
Epoch 33/100
6.1131 - lr: 3.9811e-05
Epoch 34/100
```

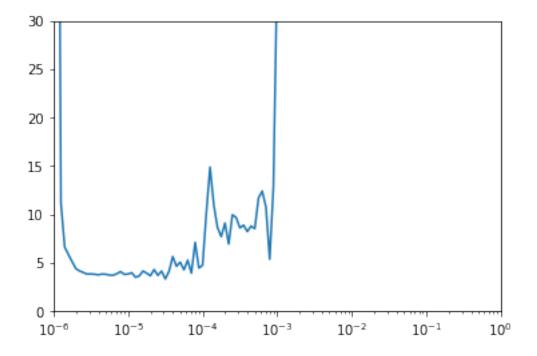
```
5.1060 - lr: 4.4668e-05
Epoch 35/100
5.5266 - lr: 5.0119e-05
Epoch 36/100
4.7391 - lr: 5.6234e-05
Epoch 37/100
5.7311 - lr: 6.3096e-05
Epoch 38/100
4.3902 - lr: 7.0795e-05
Epoch 39/100
7.5773 - lr: 7.9433e-05
Epoch 40/100
4.9217 - lr: 8.9125e-05
Epoch 41/100
5.2072 - lr: 1.0000e-04
Epoch 42/100
10.6153 - lr: 1.1220e-04
Epoch 43/100
15.3638 - lr: 1.2589e-04
Epoch 44/100
11.4745 - lr: 1.4125e-04
Epoch 45/100
9.1185 - lr: 1.5849e-04
Epoch 46/100
8.1830 - lr: 1.7783e-04
Epoch 47/100
9.5797 - lr: 1.9953e-04
Epoch 48/100
7.4095 - lr: 2.2387e-04
Epoch 49/100
10.4378 - lr: 2.5119e-04
Epoch 50/100
```

```
10.1574 - lr: 2.8184e-04
Epoch 51/100
9.0834 - lr: 3.1623e-04
Epoch 52/100
9.3576 - lr: 3.5481e-04
Epoch 53/100
8.7014 - lr: 3.9811e-04
Epoch 54/100
9.2701 - lr: 4.4668e-04
Epoch 55/100
8.9999 - lr: 5.0119e-04
Epoch 56/100
12.1681 - lr: 5.6234e-04
Epoch 57/100
12.8851 - lr: 6.3096e-04
Epoch 58/100
11.2423 - lr: 7.0795e-04
Epoch 59/100
5.8399 - lr: 7.9433e-04
Epoch 60/100
13.3141 - lr: 8.9125e-04
Epoch 61/100
35.8332 - lr: 0.0010
Epoch 62/100
120.2769 - lr: 0.0011
Epoch 63/100
130.7647 - lr: 0.0013
Epoch 64/100
267.1174 - lr: 0.0014
Epoch 65/100
284.1199 - lr: 0.0016
Epoch 66/100
```

```
188.3031 - lr: 0.0018
Epoch 67/100
185.1639 - lr: 0.0020
Epoch 68/100
220.0926 - lr: 0.0022
Epoch 69/100
284.5424 - lr: 0.0025
Epoch 70/100
407.7316 - lr: 0.0028
Epoch 71/100
446.2873 - lr: 0.0032
Epoch 72/100
772.7006 - lr: 0.0035
Epoch 73/100
772.4696 - lr: 0.0040
Epoch 74/100
1578.0363 - lr: 0.0045
Epoch 75/100
34/34 [============== ] - Os 11ms/step - loss: 1720.3474 - mae:
1720.8474 - lr: 0.0050
Epoch 76/100
1113.7627 - lr: 0.0056
Epoch 77/100
3050.2092 - lr: 0.0063
Epoch 78/100
1506.5011 - lr: 0.0071
Epoch 79/100
1891.8737 - lr: 0.0079
Epoch 80/100
34/34 [============= ] - Os 11ms/step - loss: 1820.5300 - mae:
1821.0300 - lr: 0.0089
Epoch 81/100
1737.1301 - lr: 0.0100
Epoch 82/100
```

```
2283.1929 - lr: 0.0112
Epoch 83/100
2491.6643 - lr: 0.0126
Epoch 84/100
2519.9956 - lr: 0.0141
Epoch 85/100
2641.4548 - lr: 0.0158
Epoch 86/100
5145.7021 - lr: 0.0178
Epoch 87/100
5443.8745 - lr: 0.0200
Epoch 88/100
7482.8149 - lr: 0.0224
Epoch 89/100
7763.6680 - lr: 0.0251
Epoch 90/100
4619.3062 - lr: 0.0282
Epoch 91/100
6344.5508 - lr: 0.0316
Epoch 92/100
5999.7407 - lr: 0.0355
Epoch 93/100
6803.8169 - lr: 0.0398
Epoch 94/100
11263.4092 - lr: 0.0447
Epoch 95/100
12073.3525 - lr: 0.0501
Epoch 96/100
34/34 [============= ] - Os 11ms/step - loss: 9505.7109 - mae:
9506.2109 - lr: 0.0562
Epoch 97/100
18697.9102 - lr: 0.0631
Epoch 98/100
```

[10]: (1e-06, 1.0, 0.0, 30.0)



#### 1.5 Compiling the model

Now that you have trained the model while varying the learning rate, it is time to do the actual training that will be used to forecast the time series. For this complete the <code>create\_model</code> function below.

Notice that you are reusing the architecture you defined in the create\_uncompiled\_model earlier. Now you only need to compile this model using the appropriate loss, optimizer (and learning rate).

Hint: - The training should be really quick so if you notice that each epoch is taking more than a few seconds, consider trying a different architecture.

• If after the first epoch you get an output like this: loss: nan - mae: nan it is very likely that your network is suffering from exploding gradients. This is a common problem if you used SGD as optimizer and set a learning rate that is too high. If you encounter this problem consider lowering the learning rate or using Adam with the default learning rate.

```
[11]: def create_model():
    tf.random.set_seed(51)
    model = create_uncompiled_model()
    ### START CODE HERE
    model.compile(loss="mse",
           optimizer=tf.keras.optimizers.SGD(lr=1e-6, momentum=0.9),
           metrics=["mae"])
    ### END CODE HERE
    return model
[12]: # Save an instance of the model
  model = create_model()
  # Train it
  history = model.fit(dataset, epochs=50)
  Epoch 1/50
  18.9790
  Epoch 2/50
  6.9187
  Epoch 3/50
  5.3318
  Epoch 4/50
  4.9056
  Epoch 5/50
  4.7825
  Epoch 6/50
  4.3117
  Epoch 7/50
  4.5582
```

```
Epoch 8/50
3.9755
Epoch 9/50
4.2777
Epoch 10/50
34/34 [================= ] - Os 9ms/step - loss: 29.9700 - mae:
3.6528
Epoch 11/50
3.7188
Epoch 12/50
3.9782
Epoch 13/50
4.1121
Epoch 14/50
3.7819
Epoch 15/50
3.8409
Epoch 16/50
3.5885
Epoch 17/50
3.5767
Epoch 18/50
3.8065
Epoch 19/50
3.8507
Epoch 20/50
3.7383
Epoch 21/50
3.5258
Epoch 22/50
3.5362
Epoch 23/50
3.6739
```

```
Epoch 24/50
3.4966
Epoch 25/50
3.4531
Epoch 26/50
3.6216
Epoch 27/50
3.5980
Epoch 28/50
3.7671
Epoch 29/50
3.6116
Epoch 30/50
3.6268
Epoch 31/50
3.4295
Epoch 32/50
3.3643
Epoch 33/50
3.4387
Epoch 34/50
3.5234
Epoch 35/50
3.6178
Epoch 36/50
3.4591
Epoch 37/50
3.2743
Epoch 38/50
3.5253
Epoch 39/50
3.6499
```

```
Epoch 40/50
3.4120
Epoch 41/50
34/34 [=============== ] - Os 9ms/step - loss: 25.9236 - mae:
3.3600
Epoch 42/50
34/34 [================= ] - Os 9ms/step - loss: 30.4249 - mae:
3.7784
Epoch 43/50
3.5972
Epoch 44/50
3.3618
Epoch 45/50
3.3935
Epoch 46/50
34/34 [=============== ] - Os 9ms/step - loss: 26.5164 - mae:
3.3780
Epoch 47/50
3.3753
Epoch 48/50
3.4874
Epoch 49/50
3.2364
Epoch 50/50
3.2770
```

#### 1.6 Evaluating the forecast

Now it is time to evaluate the performance of the forecast. For this you can use the compute\_metrics function that you coded in a previous assignment:

```
[13]: def compute_metrics(true_series, forecast):
    mse = tf.keras.metrics.mean_squared_error(true_series, forecast).numpy()
    mae = tf.keras.metrics.mean_absolute_error(true_series, forecast).numpy()
    return mse, mae
```

At this point only the model that will perform the forecast is ready but you still need to compute the actual forecast.

#### 1.7 Faster model forecasts

In the previous week you used a for loop to compute the forecasts for every point in the sequence. This approach is valid but there is a more efficient way of doing the same thing by using batches of data. The code to implement this is provided in the model\_forecast below. Notice that the code is very similar to the one in the windowed\_dataset function with the differences that:

- The dataset is windowed using window\_size rather than window\_size + 1
- No shuffle should be used
- No need to split the data into features and labels
- A model is used to predict batches of the dataset

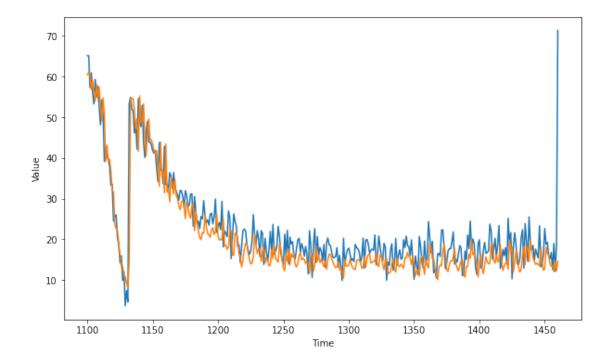
```
[14]: def model_forecast(model, series, window_size):
    ds = tf.data.Dataset.from_tensor_slices(series)
    ds = ds.window(window_size, shift=1, drop_remainder=True)
    ds = ds.flat_map(lambda w: w.batch(window_size))
    ds = ds.batch(32).prefetch(1)
    forecast = model.predict(ds)
    return forecast
```

```
[15]: # Compute the forecast for all the series
rnn_forecast = model_forecast(model, G.SERIES, G.WINDOW_SIZE).squeeze()

# Slice the forecast to get only the predictions for the validation set
rnn_forecast = rnn_forecast[G.SPLIT_TIME - G.WINDOW_SIZE:-1]

# Plot it
plt.figure(figsize=(10, 6))

plot_series(time_valid, series_valid)
plot_series(time_valid, rnn_forecast)
```



#### **Expected Output:**

A series similar to this one:

```
[16]: mse, mae = compute_metrics(series_valid, rnn_forecast)
    print(f"mse: {mse:.2f}, mae: {mae:.2f} for forecast")
```

mse: 34.25, mae: 3.94 for forecast

To pass this assignment your forecast should achieve an MAE of 4.5 or less.

- If your forecast didn't achieve this threshold try re-training your model with a different architecture (you will need to re-run both create\_uncompiled\_model and create\_model functions) or tweaking the optimizer's parameters.
- If your forecast did achieve this threshold run the following cell to save your model in a tar file which will be used for grading and after doing so, submit your assignment for grading.
- This environment includes a dummy SavedModel directory which contains a dummy model trained for one epoch. To replace this file with your actual model you need to run the next cell before submitting for grading.
- Unlike last week, this time the model is saved using the SavedModel format. This is done because the HDF5 format does not fully support Lambda layers.

```
[17]: # Save your model in the SavedModel format model.save('saved_model/my_model')
```

```
# Compress the directory using tar
! tar -czvf saved_model.tar.gz saved_model/
```

```
INFO:tensorflow:Assets written to: saved_model/my_model/assets
saved_model/
saved_model/my_model/
saved_model/my_model/keras_metadata.pb
saved_model/my_model/variables/
saved_model/my_model/variables/variables.data-00000-of-00001
saved_model/my_model/variables/variables.index
saved_model/my_model/saved_model.pb
saved_model/my_model/assets/
```

## Congratulations on finishing this week's assignment!

You have successfully implemented a neural network capable of forecasting time series leveraging Tensorflow's layers for sequence modelling such as RNNs and LSTMs! This resulted in a forecast that matches (or even surpasses) the one from last week while training for half of the epochs.

Keep it up!