

Análisis Discriminante Lineal

Melissa Ortega Galarza

2022-05-18

Cargamos las librerías

```
install.packages("MASS")
```

```
library(MASS)
```

Se cargan los datos iris

```
Z<-as.data.frame(iris)
```

Se define la matriz de datos y la variable

```
x<-Z[,1:4]  
y<-Z[,5]
```

Definir como n y p el número de flores y variables

```
n<-nrow(x)  
p<-ncol(x)
```

Se aplica el Análisis discriminante lineal (LDA)

Cross validation (cv): clasificación óptima

```
lda.iris<-lda(y~.,data=x, CV=TRUE)
```

`lda.iris$class` contiene las clasificaciones hechas por CV usando LDA.

```
lda.iris$class

## [1] setosa setosa setosa setosa setosa setosa
## [7] setosa setosa setosa setosa setosa setosa
## [13] setosa setosa setosa setosa setosa setosa
## [19] setosa setosa setosa setosa setosa setosa
## [25] setosa setosa setosa setosa setosa setosa
## [31] setosa setosa setosa setosa setosa setosa
## [37] setosa setosa setosa setosa setosa setosa
## [43] setosa setosa setosa setosa setosa setosa
## [49] setosa setosa versicolor versicolor versicolor versicolor
## [55] versicolor versicolor versicolor versicolor versicolor versicolor
## [61] versicolor versicolor versicolor versicolor versicolor versicolor
## [67] versicolor versicolor versicolor versicolor virginica versicolor
## [73] versicolor versicolor versicolor versicolor versicolor versicolor
## [79] versicolor versicolor versicolor versicolor versicolor virginica
## [85] versicolor versicolor versicolor versicolor versicolor versicolor
## [91] versicolor versicolor versicolor versicolor versicolor versicolor
## [97] versicolor versicolor versicolor versicolor virginica virginica
## [103] virginica virginica virginica virginica virginica virginica
## [109] virginica virginica virginica virginica virginica virginica
## [115] virginica virginica virginica virginica virginica virginica
## [121] virginica virginica virginica virginica virginica virginica
## [127] virginica virginica virginica virginica virginica virginica
## [133] virginica versicolor virginica virginica virginica virginica
## [139] virginica virginica virginica virginica virginica virginica
## [145] virginica virginica virginica virginica virginica virginica
## Levels: setosa versicolor virginica
```

Creación de la tabla de clasificaciones buenas y malas

```
table.lda<-table(y,lda.iris$class)
table.lda

##
## y      setosa versicolor virginica
## setosa    50         0         0
## versicolor  0        48         2
## virginica  0         1        49
```

Proporcion de errores

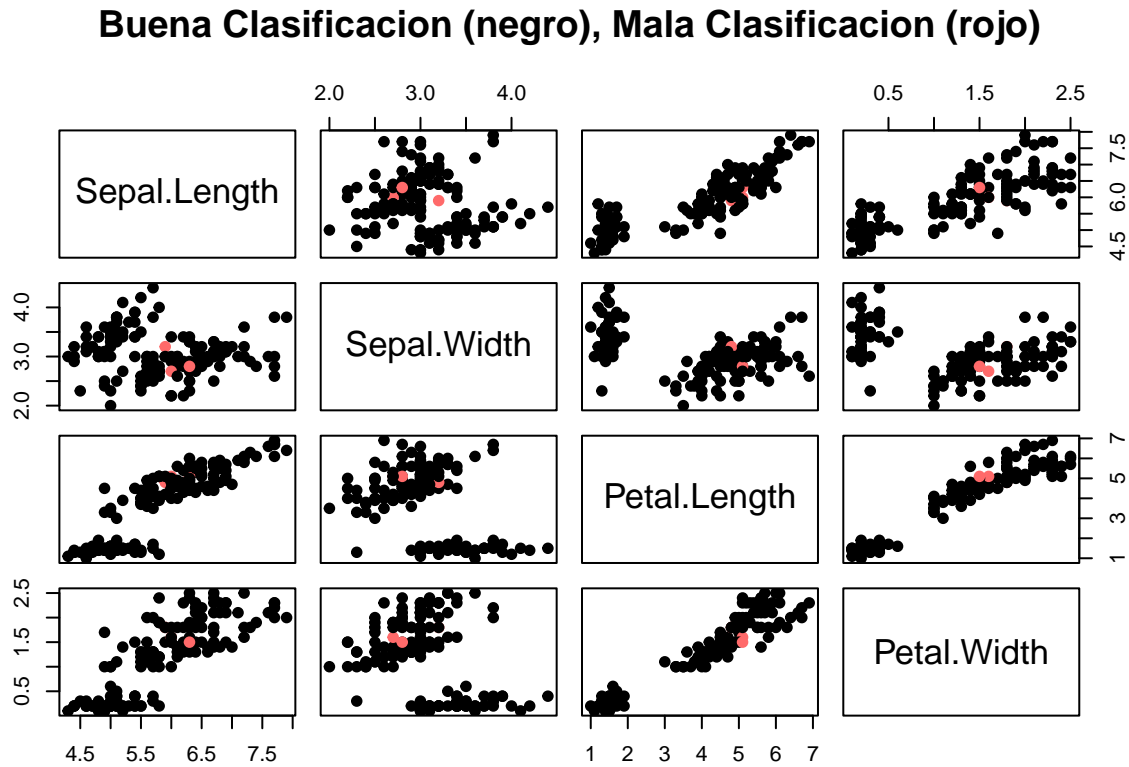
```
mis.lda<- n-sum(y==lda.iris$class)
mis.lda/n

## [1] 0.02
```

Scater plot

Buenas clasificaciones en negro y malas en rojo

```
col.lda.iris<-c("indianred1", "black")[1*(y==lda.iris$class)+1]  
pairs(x,main="Buena Clasificacion (negro), Mala Clasificacion (rojo)",  
      pch=19,col=col.lda.iris)
```



Probabilidad de pertenencia a uno de los tres grupos

```
lda.iris$posterior
```

##	setosa	versicolor	virginica
## 1	1.000000e+00	5.087494e-22	4.385241e-42
## 2	1.000000e+00	9.588256e-18	8.888069e-37
## 3	1.000000e+00	1.983745e-19	8.606982e-39
## 4	1.000000e+00	1.505573e-16	5.101765e-35
## 5	1.000000e+00	2.075670e-22	1.739832e-42
## 6	1.000000e+00	5.332271e-21	8.674906e-40
## 7	1.000000e+00	1.498839e-18	3.999205e-37
## 8	1.000000e+00	5.268133e-20	1.983027e-39
## 9	1.000000e+00	2.280729e-15	1.293376e-33
## 10	1.000000e+00	1.504085e-18	5.037348e-38
## 11	1.000000e+00	1.296140e-23	4.023338e-44
## 12	1.000000e+00	2.171874e-18	3.223111e-37
## 13	1.000000e+00	1.996136e-18	6.109118e-38
## 14	1.000000e+00	1.604055e-19	2.549802e-39
## 15	1.000000e+00	2.843397e-31	1.593594e-54
## 16	1.000000e+00	2.330545e-28	3.074132e-49
## 17	1.000000e+00	5.136116e-25	3.269819e-45
## 18	1.000000e+00	5.747697e-21	2.253825e-40
## 19	1.000000e+00	2.187125e-22	4.069438e-42
## 20	1.000000e+00	3.297882e-22	9.802494e-42
## 21	1.000000e+00	1.757286e-19	8.150916e-39
## 22	1.000000e+00	2.027767e-20	3.730752e-39
## 23	1.000000e+00	5.650696e-25	6.509776e-46
## 24	1.000000e+00	8.618517e-15	7.014744e-32
## 25	1.000000e+00	1.520334e-15	1.857885e-33
## 26	1.000000e+00	2.936141e-16	8.159510e-35
## 27	1.000000e+00	4.557392e-17	5.510803e-35
## 28	1.000000e+00	2.079675e-21	2.831513e-41
## 29	1.000000e+00	1.232321e-21	1.082692e-41
## 30	1.000000e+00	1.153050e-16	4.267126e-35
## 31	1.000000e+00	2.584595e-16	9.537258e-35
## 32	1.000000e+00	2.878754e-19	5.473623e-38
## 33	1.000000e+00	2.247070e-27	4.047137e-49
## 34	1.000000e+00	2.620949e-29	1.970538e-51
## 35	1.000000e+00	1.493279e-17	2.047516e-36
## 36	1.000000e+00	2.146308e-21	1.550216e-41
## 37	1.000000e+00	1.673983e-24	1.322398e-45
## 38	1.000000e+00	3.810942e-23	9.131835e-44
## 39	1.000000e+00	5.423320e-17	1.146137e-35
## 40	1.000000e+00	2.414191e-20	6.552342e-40
## 41	1.000000e+00	1.417602e-21	3.569675e-41
## 42	1.000000e+00	8.956712e-11	4.968454e-28
## 43	1.000000e+00	2.125837e-18	2.395462e-37
## 44	1.000000e+00	1.101293e-15	1.403899e-32
## 45	1.000000e+00	2.285363e-17	5.214629e-35
## 46	1.000000e+00	2.087086e-16	1.027948e-34
## 47	1.000000e+00	2.588201e-22	3.634491e-42
## 48	1.000000e+00	3.643000e-18	4.504970e-37
## 49	1.000000e+00	3.000767e-23	1.346233e-43

```

## 50 1.000000e+00 3.171862e-20 7.860312e-40
## 51 3.157725e-18 9.998716e-01 1.284247e-04
## 52 1.753919e-19 9.991816e-01 8.184018e-04
## 53 2.551962e-22 9.951044e-01 4.895626e-03
## 54 2.742687e-22 9.995996e-01 4.004477e-04
## 55 4.854978e-23 9.951404e-01 4.859638e-03
## 56 9.575747e-23 9.982973e-01 1.702702e-03
## 57 4.467689e-22 9.838631e-01 1.613691e-02
## 58 5.922943e-14 9.999999e-01 8.584221e-08
## 59 8.088509e-20 9.998655e-01 1.344590e-04
## 60 1.767441e-20 9.994314e-01 5.686054e-04
## 61 3.330661e-18 9.999987e-01 1.314516e-06
## 62 8.331100e-20 9.991631e-01 8.369389e-04
## 63 4.614428e-18 9.999989e-01 1.117671e-06
## 64 1.290071e-23 9.939163e-01 6.083745e-03
## 65 5.229707e-14 9.999984e-01 1.593028e-06
## 66 3.393529e-17 9.999528e-01 4.721492e-05
## 67 7.983370e-24 9.763990e-01 2.360097e-02
## 68 3.119288e-16 9.999991e-01 8.659241e-07
## 69 3.847473e-28 9.390462e-01 6.095377e-02
## 70 1.678698e-17 9.999966e-01 3.360127e-06
## 71 1.302246e-28 1.772727e-01 8.227273e-01
## 72 1.113263e-16 9.999902e-01 9.801197e-06
## 73 1.634947e-29 7.868347e-01 2.131653e-01
## 74 3.331093e-22 9.995073e-01 4.926830e-04
## 75 1.013127e-17 9.999741e-01 2.594176e-05
## 76 2.949236e-18 9.999081e-01 9.193549e-05
## 77 7.224891e-23 9.979459e-01 2.054146e-03
## 78 2.386376e-27 6.569495e-01 3.430505e-01
## 79 4.473658e-23 9.922840e-01 7.716012e-03
## 80 7.145460e-12 1.000000e+00 1.241414e-08
## 81 1.333306e-17 9.999970e-01 3.044209e-06
## 82 1.119894e-15 9.999997e-01 2.916503e-07
## 83 1.748156e-16 9.999961e-01 3.876682e-06
## 84 1.125494e-33 9.924153e-02 9.007585e-01
## 85 1.191672e-24 9.474667e-01 5.253333e-02
## 86 1.983291e-20 9.924721e-01 7.527887e-03
## 87 4.531906e-21 9.980100e-01 1.989996e-03
## 88 2.035626e-23 9.993358e-01 6.642410e-04
## 89 7.813451e-18 9.999440e-01 5.603286e-05
## 90 8.212308e-21 9.998033e-01 1.967487e-04
## 91 6.631189e-23 9.992802e-01 7.197827e-04
## 92 7.049062e-22 9.979525e-01 2.047473e-03
## 93 4.490728e-18 9.999881e-01 1.188058e-05
## 94 2.600275e-14 9.999999e-01 8.745690e-08
## 95 6.422939e-21 9.996751e-01 3.248823e-04
## 96 2.159263e-17 9.999804e-01 1.956029e-05
## 97 3.823305e-19 9.998801e-01 1.199041e-04
## 98 2.089502e-18 9.999504e-01 4.963639e-05
## 99 9.013113e-11 1.000000e+00 9.943306e-09
## 100 6.167377e-19 9.999219e-01 7.813051e-05
## 101 1.335977e-53 3.188548e-09 1.000000e+00
## 102 9.949508e-38 1.209398e-03 9.987906e-01
## 103 1.950796e-42 2.774428e-05 9.999723e-01

```

```

## 104 3.081602e-38 1.232592e-03 9.987674e-01
## 105 5.411117e-46 1.807449e-06 9.999982e-01
## 106 5.887455e-50 5.662591e-07 9.999994e-01
## 107 1.203272e-32 8.794800e-02 9.120520e-01
## 108 1.774038e-42 1.735541e-04 9.998264e-01
## 109 1.924345e-42 2.617818e-04 9.997382e-01
## 110 1.851248e-46 1.352651e-07 9.999999e-01
## 111 4.379051e-32 1.446014e-02 9.855399e-01
## 112 2.052671e-37 1.776421e-03 9.982236e-01
## 113 9.704392e-39 2.172029e-04 9.997828e-01
## 114 2.386650e-40 2.251253e-04 9.997749e-01
## 115 8.048237e-46 8.410965e-07 9.999992e-01
## 116 1.008588e-39 2.840103e-05 9.999716e-01
## 117 2.811294e-35 6.595206e-03 9.934048e-01
## 118 7.282186e-45 1.296566e-06 9.999987e-01
## 119 1.004644e-64 2.647509e-10 1.000000e+00
## 120 3.160887e-33 3.033047e-01 6.966953e-01
## 121 1.719583e-42 6.688965e-06 9.999933e-01
## 122 6.252717e-37 9.870164e-04 9.990130e-01
## 123 2.627103e-51 7.704580e-07 9.999992e-01
## 124 1.504499e-31 1.070121e-01 8.929879e-01
## 125 3.688147e-39 9.571422e-05 9.999043e-01
## 126 2.426533e-36 3.398007e-03 9.966020e-01
## 127 3.865436e-30 2.055755e-01 7.944245e-01
## 128 3.606381e-30 1.437670e-01 8.562330e-01
## 129 8.371636e-44 1.376281e-05 9.999862e-01
## 130 2.937738e-32 1.589920e-01 8.410080e-01
## 131 6.294581e-42 1.714027e-04 9.998286e-01
## 132 5.466934e-36 7.736441e-04 9.992264e-01
## 133 1.208158e-45 3.051435e-06 9.999969e-01
## 134 5.464475e-29 7.876238e-01 2.123762e-01
## 135 9.884011e-35 1.578198e-01 8.421802e-01
## 136 6.515088e-46 1.990735e-06 9.999980e-01
## 137 2.840394e-44 7.895048e-07 9.999992e-01
## 138 7.160822e-35 7.053731e-03 9.929463e-01
## 139 1.782247e-29 2.122042e-01 7.877958e-01
## 140 3.640914e-36 9.289807e-04 9.990710e-01
## 141 5.881132e-45 1.108009e-06 9.999989e-01
## 142 2.122304e-35 6.157433e-04 9.993843e-01
## 143 9.949508e-38 1.209398e-03 9.987906e-01
## 144 9.585800e-46 9.978596e-07 9.999990e-01
## 145 2.206003e-46 2.038879e-07 9.999998e-01
## 146 1.133074e-38 8.851900e-05 9.999115e-01
## 147 8.781586e-36 7.084468e-03 9.929155e-01
## 148 7.108984e-35 3.342993e-03 9.966570e-01
## 149 3.096565e-40 1.338572e-05 9.999866e-01
## 150 3.585667e-33 2.058806e-02 9.794119e-01

```

Grafico de probabilidades

```
plot(1:n, lda.iris$posterior[,1],  
     main="Probabilidades a posterior",  
     pch=20, col="cyan",  
     xlab="Numero de observaciones", ylab="Probabilidades")  
points(1:n, lda.iris$posterior[,2],  
       pch=20, col="green")  
points(1:n, lda.iris$posterior[,3],  
       pch=20, col="orange")
```

Probabilidades a posterior

