

#### **SHORTHAND METHOD**

If we specify  $V_{GS}$  to be one-half the pinch-off value  $V_P$ ,

$$I_{D} = I_{DSS} \left( 1 - \frac{V_{GS}}{V_{P}} \right)^{2}$$

$$= I_{DSS} \left( \frac{1 - V_{P}/2}{V_{P}} \right)^{2} = I_{DSS} \left( 1 - \frac{1}{2} \right)^{2} = I_{DSS}(0.5)^{2}$$

$$= I_{DSS}(0.25)$$

and

and

$$I_D = \frac{I_{DSS}}{4} \bigg|_{V_{GS} = V_P/2}$$

If we choose  $I_D = I_{DSS}/2$ 

$$V_{GS} = V_P \left( 1 - \sqrt{\frac{I_D}{I_{DSS}}} \right)$$

$$= V_P \left( 1 - \sqrt{\frac{I_{DSS}/2}{I_{DSS}}} \right) = V_P (1 - \sqrt{0.5}) = V_P (0.293)$$

$$V_{GS} \approx 0.3 V_P |_{I_D = I_{DSS}/2}$$

| V <sub>GS</sub> Versus I <sub>D</sub> Using Shockley's<br>Equation |             |
|--|-------------|
| $V_{GS}$   | $I_D$       |
| 0  | $I_{DSS}$   |
| $0.3V_P$   | $I_{DSS}/2$ |
| $0.5V_P$   | $I_{DSS}/4$ |
| $V_P$  | 0 mA        |

#### **SHORTHAND METHOD**

**EXAMPLE 6.1** Sketch the transfer curve defined by  $I_{DSS} = 12 \text{ mA}$  and  $V_P = -6 \text{ V}$ .

**Solution:** Two plot points are defined by

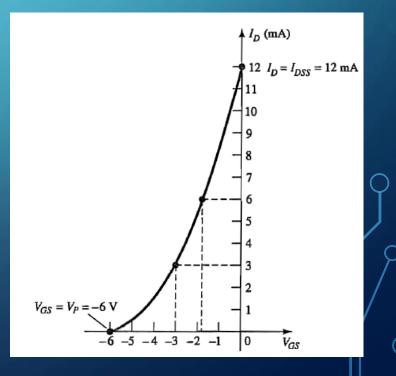
$$I_{DSS} = 12 \text{ mA}$$
 and  $V_{GS} = 0 \text{ V}$ 

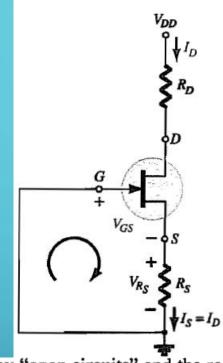
and  $I_D = 0 \, \mathrm{mA}$  and  $V_{GS} = V_P$ 

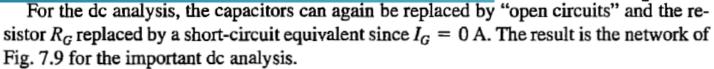
At  $V_{GS} = V_P/2 = -6 \text{ V}/2 = -3 \text{ V}$  the drain current is determined by  $I_D = I_{DSS}/4 = 12 \text{ mA}/4 = 3 \text{ mA}$ . At  $I_D = I_{DSS}/2 = 12 \text{ mA}/2 = 6 \text{ mA}$  the gate-to-source voltage is determined by  $V_{GS} \cong 0.3V_P = 0.3(-6 \text{ V}) = -1.8 \text{ V}$ . All four plot points are well defined on Fig. 6.18 with the complete transfer curve.

#### $V_{GS}$ Versus $I_D$ Using Shockley's Equation

| $V_{GS}$ | $I_D$       |
|----------|-------------|
| 0        | $I_{DSS}$   |
| $0.3V_P$ | $I_{DSS}/2$ |
| $0.5V_P$ | $I_{DSS}/4$ |
| $V_P$    | 0 mA        |







The current through  $R_S$  is the source current  $I_S$ , but  $I_S = I_D$  and

$$V_{R_S} = I_D R_S$$

For the indicated closed loop of Fig. 7.9, we find that

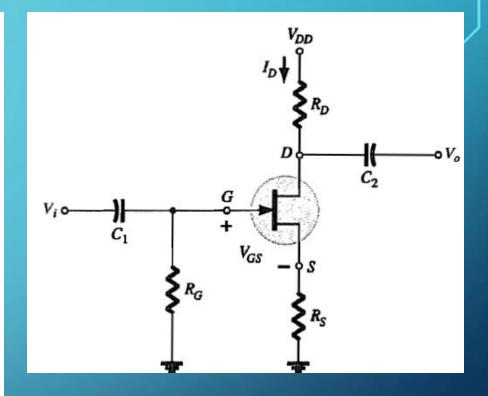
$$-V_{GS} - V_{R_S} = 0$$
$$V_{GS} = -V_{R_S}$$

and

or

$$V_{GS} = -I_D R_S$$

(7.10)



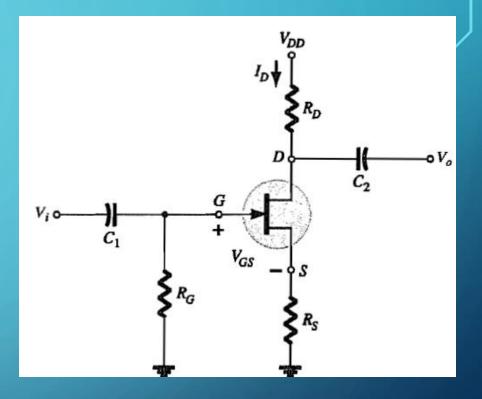


$$V_{DS} = V_{DD} - I_D(R_S + R_D)$$

$$V_S = I_D R_S$$

$$V_G = 0$$
 V

$$V_D = V_{DS} + V_S = V_{DD} - V_{R_D}$$



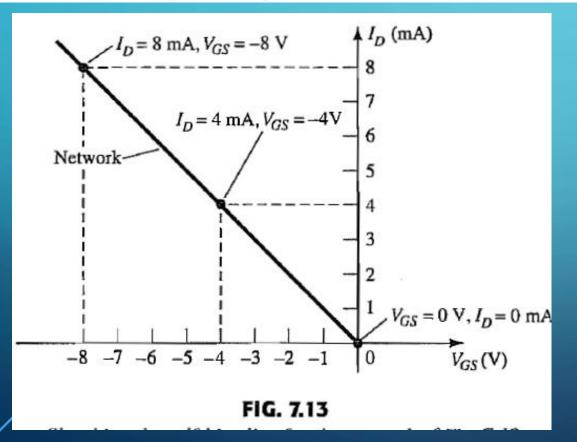
a. The gate-to-source voltage is determined by

$$V_{GS} = -I_D R_S$$

Choosing  $I_D = 4 \text{ mA}$ , we obtain

$$V_{GS} = -(4 \text{ mA})(1 \text{ k}\Omega) = -4 \text{ V}$$

The result is the plot of Fig. 7.13 as defined by the network.



Determine the following for the network of Fig. 7.12: EXAMPLE 7.2

a. 
$$V_{GSQ}$$
.

b. 
$$I_{D_Q}$$

d. 
$$V_s$$
.

e. 
$$V_G$$
.

f. 
$$V_D$$
.

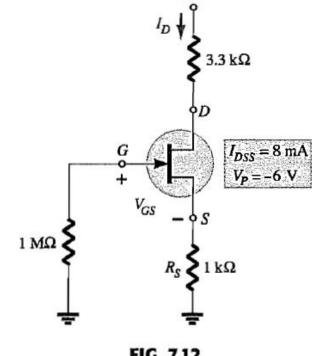


FIG. 7.12

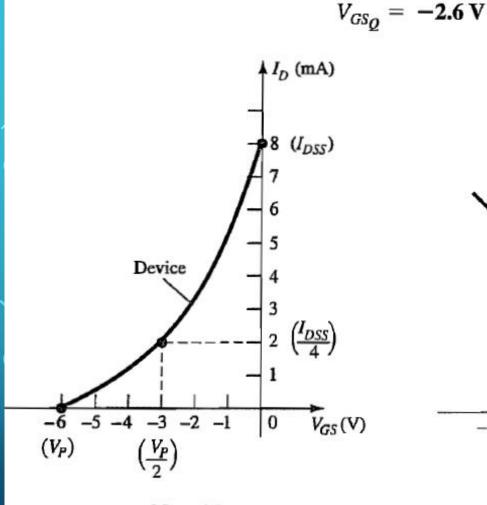


FIG. 7.14

Sketching the device characteristics for the JFET of Fig. 7.12.

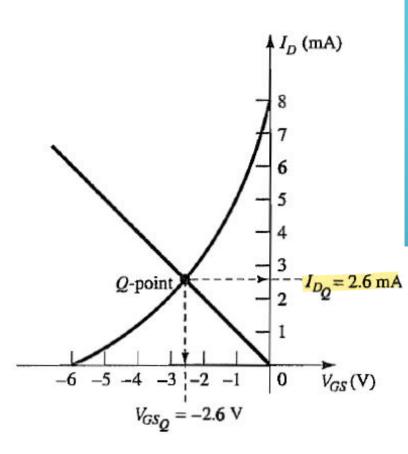


FIG. 7.15

Determining the Q-point for the network of

Fig. 7.12. e. Eq. (7.13): 
$$V_G = \mathbf{0} \mathbf{V}$$
  
f. Eq. (7.14):  $V_D = V_{DS} + V_S = 8.82 \,\mathrm{V} + 2.6 \,\mathrm{V} = 11.42 \,\mathrm{V}$   
or  $V_D = V_{DD} - I_D R_D = 20 \,\mathrm{V} - (2.6 \,\mathrm{mA})(3.3 \,\mathrm{k}\Omega) = 11.42 \,\mathrm{V}$ 

**EXAMPLE 7.2** Determine the following for the network of Fig. 7.12:

a.  $V_{GS_Q}$ .

b.  $I_{D_Q}$ .

c.  $V_{DS}$ .

d.  $V_S$ .

e.  $V_G$ .

f.  $V_D$ .  $Q_{GS} = 8 \text{ mA}$   $Q_{GS} = 8 \text{ mA}$ 

b. At the quiescent point

$$I_{D_{\underline{Q}}} = 2.6 \,\mathrm{mA}$$

$$R_{\mathrm{s}} + R_{\mathrm{p}}$$

FIG. 7.12

c. Eq. (7.11): 
$$V_{DS} = V_{DD} - I_D(R_S + R_D)$$
  
=  $20 \text{ V} - (2.6 \text{ mA})(1 \text{ k}\Omega + 3.3 \text{ k}\Omega)$   
=  $20 \text{ V} - 11.18 \text{ V}$   
=  $8.82 \text{ V}$ 

= 8.82 V  
d. Eq. (7.12): 
$$V_S = I_D R_S$$
  
=  $(2.6 \text{ mA})(1 \text{ k}\Omega)$   
= 2.6 V

$$I_G \cong 0 \text{ A}$$
 
$$V_{R_G} = I_G R_G = (0 \text{ A}) R_G = 0 \text{ V}$$

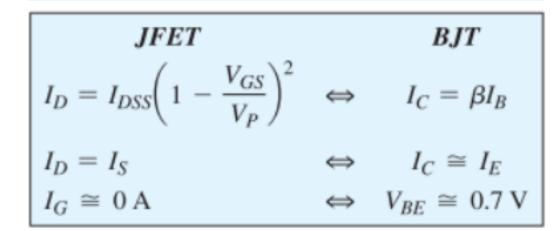
$$-V_{GG} - V_{GS} = 0$$
$$V_{GS} = -V_{GG}$$

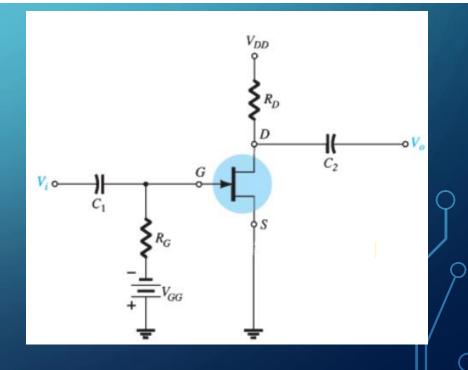
$$I_D = I_{DSS} \left( 1 - \frac{V_{GS}}{V_P} \right)^2$$

$$+V_{DS} + I_D R_D - V_{DD} = 0$$

$$V_{DS} = V_{DD} - I_D R_D$$

$$V_S = 0 \text{ V}$$



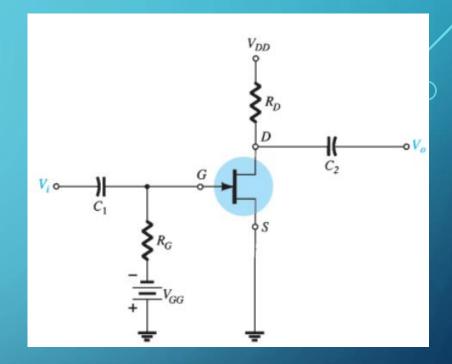


$$V_{DS} = V_D - V_S$$
  
$$V_D = V_{DS} + V_S = V_{DS} + 0 \text{ V}$$

$$V_D = V_{DS}$$

$$V_{GS} = V_G - V_S$$
$$V_G = V_{GS} + V_S = V_{GS} + 0 \text{ V}$$

$$V_G = V_{GS}$$



Determine the following for the network of Fig. 7.6:

- a.  $V_{GS_Q}$ .
- b.  $I_{D_Q}$ .
- c.  $V_{DS}$ .
- e.  $V_G$ .
- f.  $V_{S}$ .

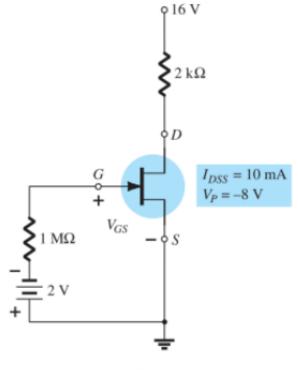


FIG. 7.6 Example 7.1.

a. 
$$V_{GS_Q} = -V_{GG} = -2 \text{ V}$$

b. 
$$I_{D_Q} = I_{DSS} \left( 1 - \frac{V_{GS}}{V_P} \right)^2 = 10 \text{ mA} \left( 1 - \frac{-2 \text{ V}}{-8 \text{ V}} \right)^2$$
  
=  $10 \text{ mA} (1 - 0.25)^2 = 10 \text{ mA} (0.75)^2 = 10 \text{ mA} (0.5625)$   
=  $\mathbf{5.625 \text{ mA}}$ 

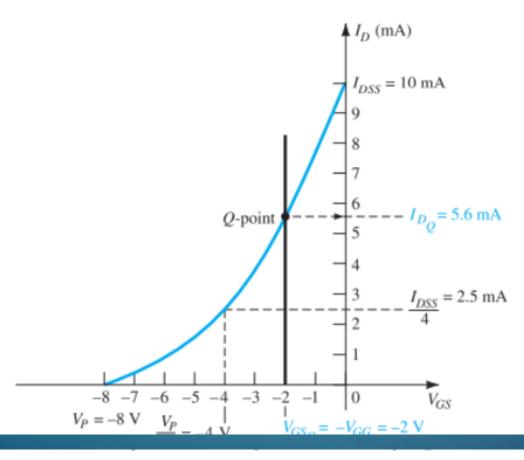
c. 
$$V_{DS} = V_{DD} - I_D R_D = 16 \text{ V} - (5.625 \text{ mA})(2 \text{ k}\Omega)$$
  
=  $16 \text{ V} - 11.25 \text{ V} = 4.75 \text{ V}$ 

d. 
$$V_D = V_{DS} = 4.75 \text{ V}$$

e. 
$$V_G = V_{GS} = -2 \text{ V}$$
  
f.  $V_S = 0 \text{ V}$ 

f. 
$$V_S = \mathbf{0} \mathbf{V}$$

**Graphical Approach** The resulting Shockley curve and the vertical line at  $V_{GS} = -2 \text{ V}$  are provided in Fig. 7.7. It is certainly difficult to read beyond the second place without



significantly increasing the size of the figure, but a solution of 5.6 mA from the graph of Fig. 7.7 is quite acceptable.

a. Therefore,

$$V_{GS_O} = -V_{GG} = -2 \text{ V}$$

b. 
$$I_{D_Q} = 5.6 \text{ mA}$$

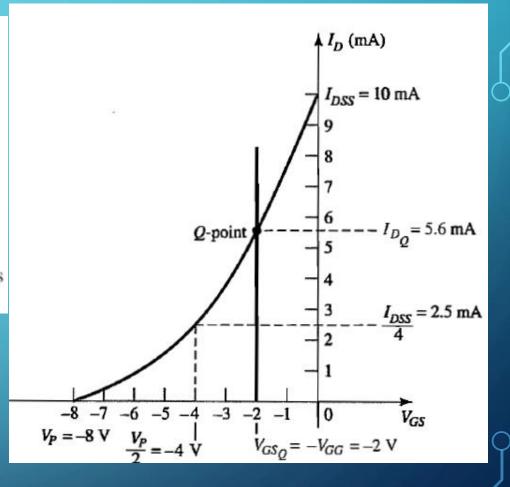
c. 
$$V_{DS} = V_{DD} - I_D R_D = 16 \text{ V} - (5.6 \text{ mA})(2 \text{ k}\Omega)$$
  
=  $16 \text{ V} - 11.2 \text{ V} = 4.8 \text{ V}$ 

d. 
$$V_D = V_{DS} = 4.8 \text{ V}$$

e. 
$$V_G = V_{GS} = -2 \text{ V}$$

f. 
$$V_S = \mathbf{0} \mathbf{V}$$

The results clearly confirm the fact that the mathematical and graphical approaches generate solutions that are quite close.



#### FET BIASING (VOLTAGE DIVIDER BIAS CONFIGURATION)

$$I_G \cong 0 \text{ A}$$

$$V_G = \frac{R_2 V_{DD}}{R_1 + R_2}$$

$$V_G - V_{GS} - V_{R_S} = 0$$
$$V_{GS} = V_G - V_{R_S}$$

$$V_{GS} = V_G - I_D R_S$$

$$V_{GS} = V_G - I_D R_S$$
  
=  $V_G - (0 \text{ mA}) R_S$ 

$$V_{GS} = V_G|_{I_D = 0 \text{ mA}}$$

$$V_{GS} = V_G - I_D R_S$$
$$0 V = V_G - I_D R_S$$

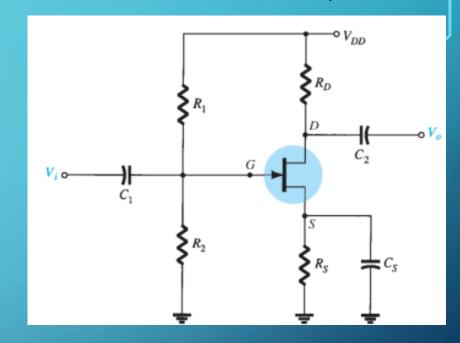
$$I_D = \frac{V_G}{R_S} \bigg|_{V_{GS} = 0 \text{ V}}$$

$$V_{DS} = V_{DD} - I_D(R_D + R_S)$$

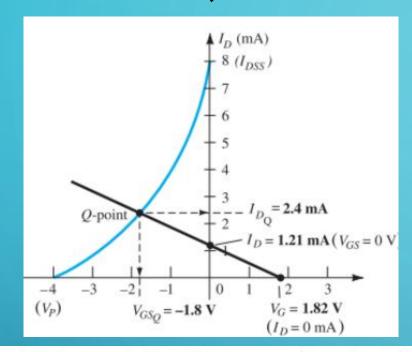
$$V_D = V_{DD} - I_DR_D$$

$$V_S = I_DR_S$$

$$I_{R_1} = I_{R_2} = \frac{V_{DD}}{R_1 + R_2}$$



#### FET BIASING (VOLTAGE DIVIDER BIAS CONFIGURATION)



a. For the transfer characteristics, if  $I_D = I_{DSS}/4 = 8 \text{ mA}/4 = 2 \text{ mA}$ , then  $V_{GS} = V_P/2 = -4 \text{ V}/2 = -2 \text{ V}$ . The resulting curve representing Shockley's equation appears in Fig. 7.22. The network equation is defined by

$$V_G = \frac{R_2 V_{DD}}{R_1 + R_2}$$

$$= \frac{(270 \text{ k}\Omega)(16 \text{ V})}{2.1 \text{ M}\Omega + 0.27 \text{ M}\Omega}$$

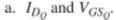
$$= 1.82 \text{ V}$$

$$V_{GS} = V_G - I_D R_S$$

$$= 1.82 \text{ V} - I_D (1.5 \text{ k}\Omega)$$

and

**EXAMPLE 7.4** Determine the following for the network of Fig. 7.21:



b. 
$$V_D$$
.

c. 
$$V_S$$
.

d. 
$$V_{DS}$$
.



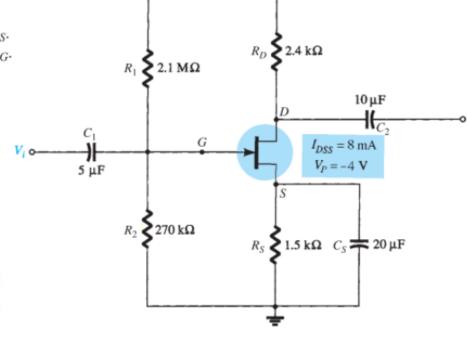
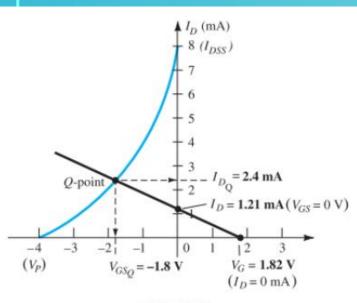


FIG. 7.21 Example 7.4

#### FET BIASING (VOLTAGE DIVIDER BIAS CONFIGURATION)



#### FIG. 7.22

Determining the Q-point for the network of Fig. 7.21.

When  $I_D = 0 \text{ mA}$ ,

$$V_{GS} = +1.82 \text{ V}$$

When  $V_{GS} = 0 \text{ V}$ ,

and

$$I_D = \frac{1.82 \text{ V}}{1.5 \text{ k}\Omega} = 1.21 \text{ mA}$$

The resulting bias line appears on Fig. 7.22 with quiescent values of

$$I_{D_Q} = 2.4 \text{ mA}$$
  
 $V_{GS_Q} = -1.8 \text{ V}$ 

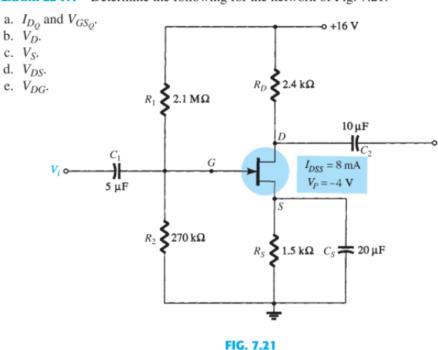
b. 
$$V_D = V_{DD} - I_D R_D$$
  
= 16 V - (2.4 mA)(2.4 k $\Omega$ )  
= 10.24 V

c. 
$$V_S = I_D R_S = (2.4 \text{ mA})(1.5 \text{ k}\Omega)$$
  
= **3.6 V**

 $= 6.64 \, V$ 

d. 
$$V_{DS} = V_{DD} - I_D(R_D + R_S)$$
  
= 16 V - (2.4 mA)(2.4 k $\Omega$  + 1.5 k $\Omega$ )  
= **6.64 V**  
or  $V_{DS} = V_D - V_S = 10.24 \text{ V} - 3.6 \text{ V}$ 

**EXAMPLE 7.4** Determine the following for the network of Fig. 7.21:



Example 7.4.

e. Although seldom requested, the voltage  $V_{DG}$  can easily be determined using

$$V_{DG} = V_D - V_G$$
  
= 10.24 V - 1.82 V  
= **8.42 V**

# Thank You!