



# IRE 215: SENSOR TECHNOLOGY

## LECTURE-2: STATIC AND DYNAMIC CHARACTERISTICS

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# LECTURE CONTENTS

- Dynamic characteristics
- Example of dynamic systems
- Different types of inputs
- Natural vs. forced response



# Dynamic Characteristics

Behavior of a system with time when some input is given to the system.

For a dynamic system model, response variables change with time (transient response).

Input can be static or dynamic.

# Example of Dynamic Systems



$T$  = temperature of the thermometer

$T_L$  = temperature of hot water

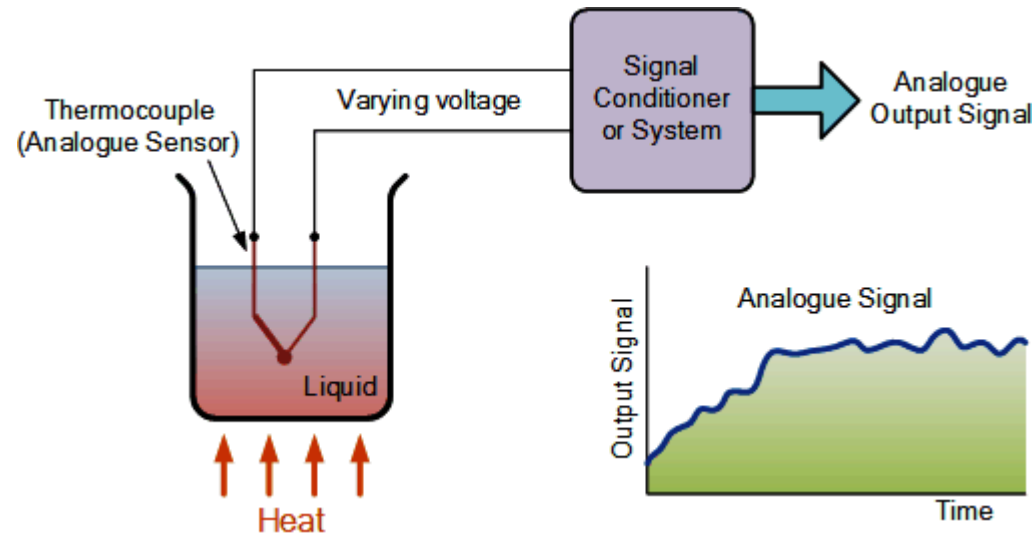
$T$  changes with time just after dipping the thermometer in hot water until  $T = T_L$

Thermometer in hot water

System model:

$$RC \frac{dT}{dt} + T = T_L$$

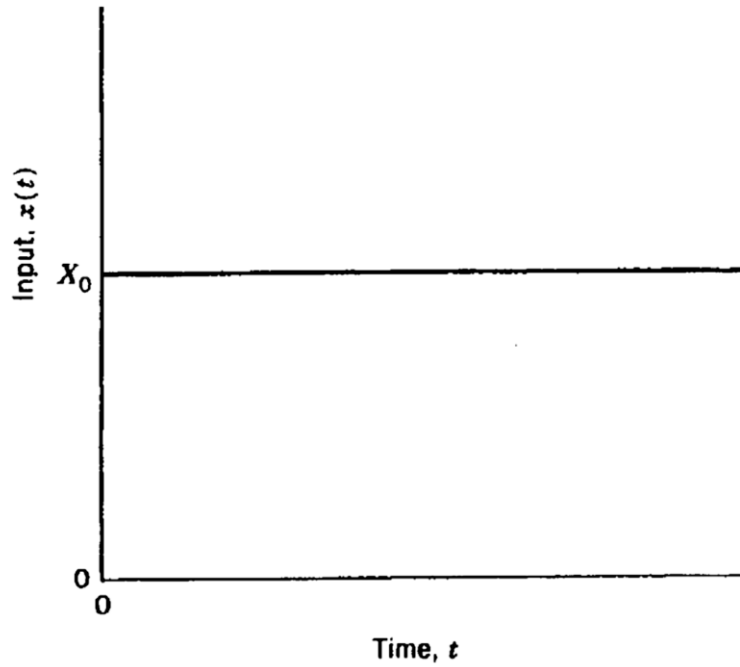
# Example of Dynamic Systems



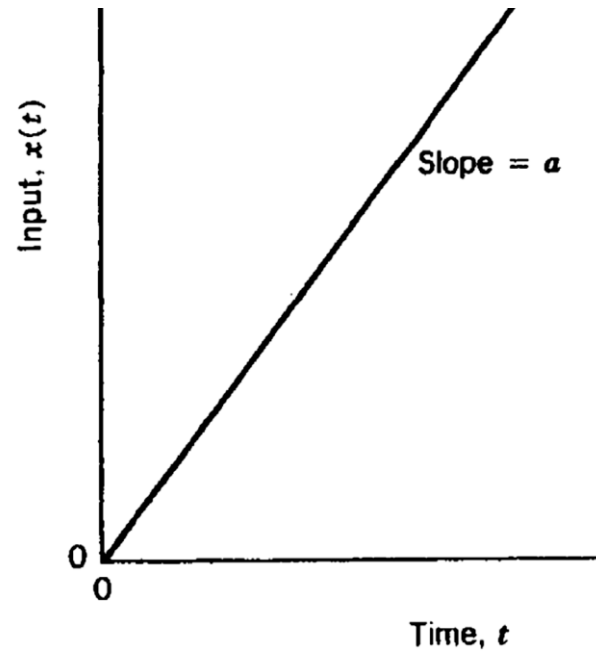
Thermocouple in hot liquid

In this case, input and output (response) both are dynamic

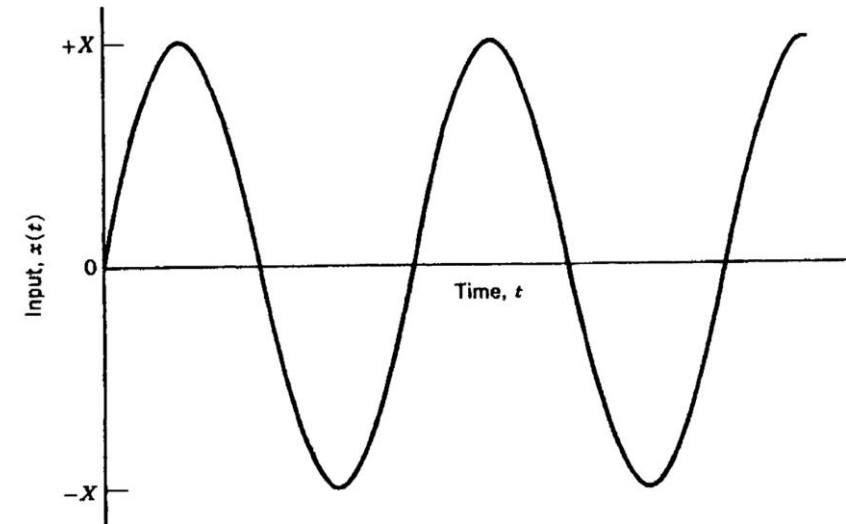
# DIFFERENT TYPES OF INPUTS



Step change      $x = 0$       $t < 0$   
                       $x = x_0$       $t > 0$



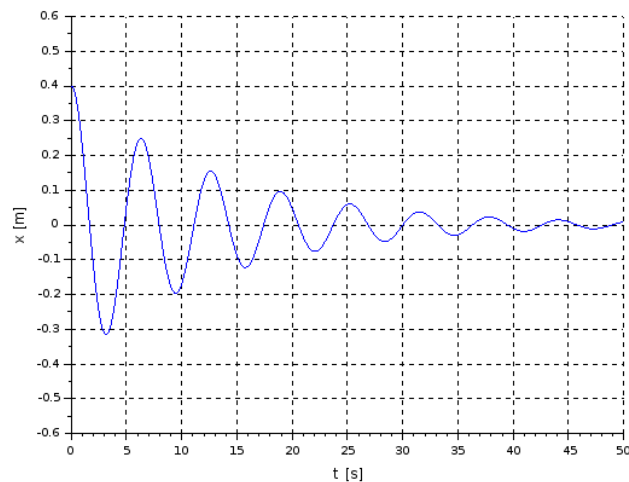
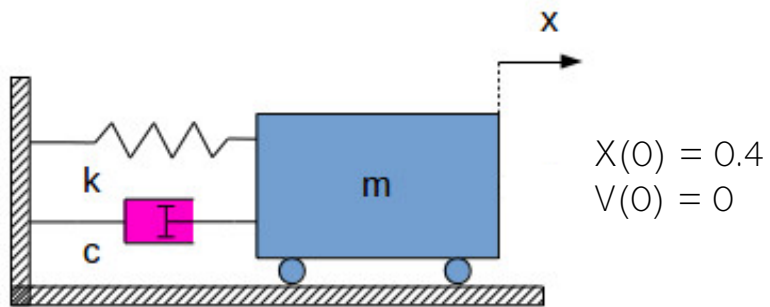
Ramp      $x = 0$       $t < 0$   
                   $x = at$       $t \geq 0$



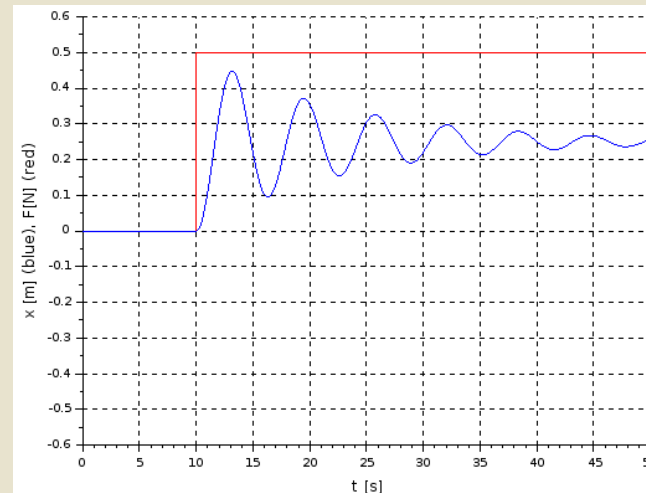
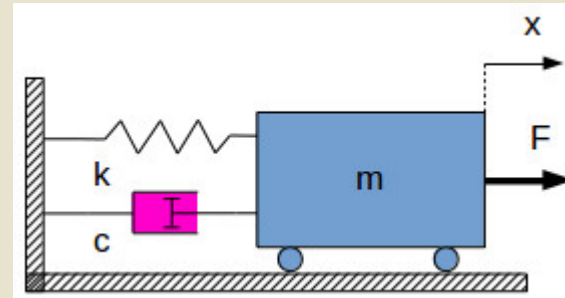
Sinusoidal      $x = X \sin(\omega t)$       $t > 0$

# NATURAL VS. FORCED RESPONSE

System's response to initial conditions when there is no input.



System's response to an external stimulus with zero initial conditions.



# ZERO-ORDER INSTRUMENT

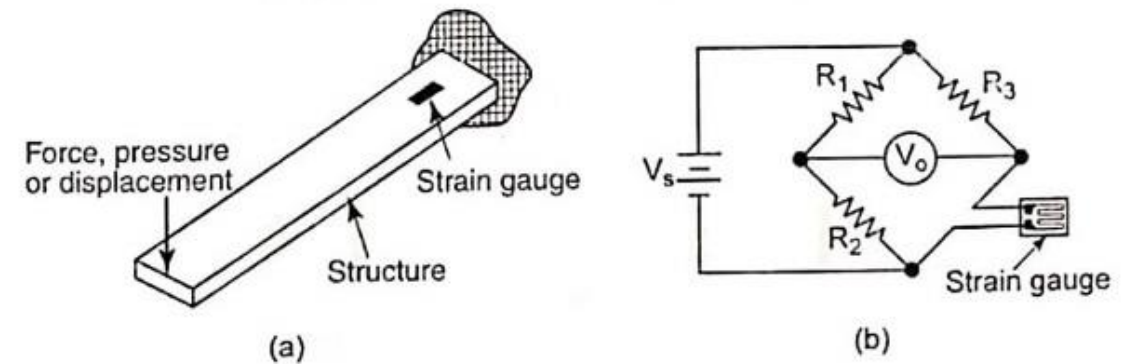
The definition of a zero-order instrument is one that has a dynamic response behavior that can be expressed in the form:

$$y = Kx(t)$$

$K$  = static gain/ steady-state gain

There is no delay

Example



*Strain gauge with Wheatstone bridge circuit*

$$\Delta R = FR\epsilon$$

$F$  is the gauge factor

$R$  is the resistance of the gauge wire



# FIRST-ORDER INSTRUMENT

The definition of a first-order instrument is one that has a dynamic response behavior that can be expressed in the form:

$$\tau \frac{dy}{dt} + y = Kx$$

$\tau$  = time constant    How fast system will react to changes in its input

Initial condition:  $y = 0$  at  $t = 0$

Solution:  $\frac{y}{Kx_0} = 1 - e^{-t/\tau}$

Time delay exists

In one time-constant, the response achieves 63.2% of its final value.

Example



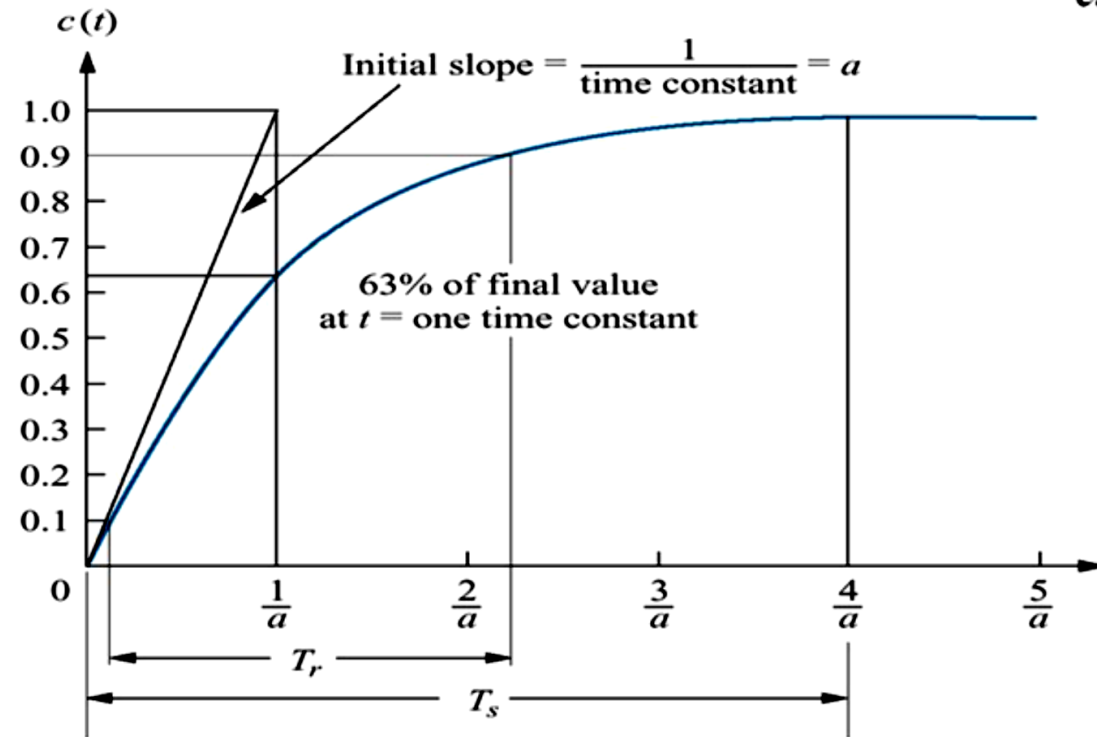
Thermometer in hot water

$$RC \frac{dT}{dt} + T = T_L$$

# STEP RESPONSE OF A FIRST-ORDER INSTRUMENT

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First – order system  $\tau = \frac{1}{a}$



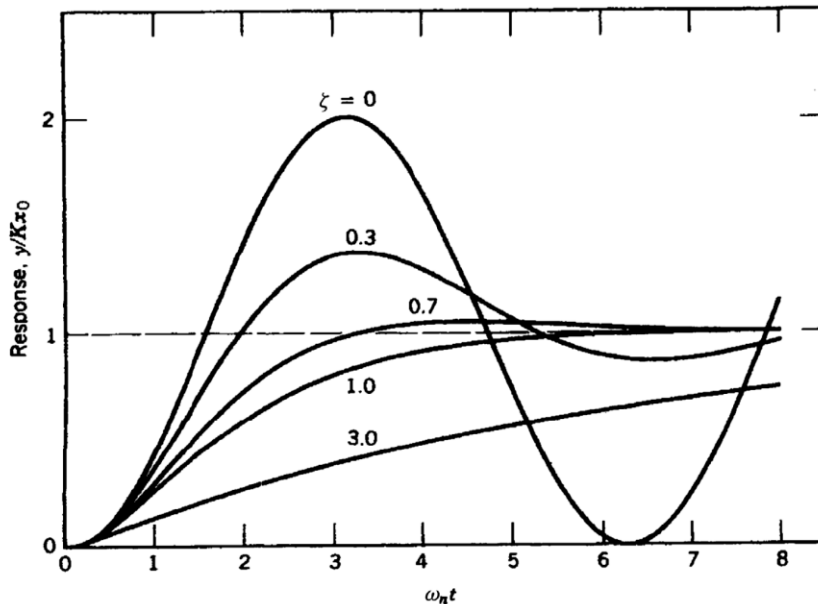
$T_r$  = Rise time (time taken to rise to some percentage of steady –state output e.g., from 10% to 90% of steady-state value)

$T_s$  = Settling time (Time taken for the output to settle to within some percentage e.g., 2% of steady state value)

# SECOND-ORDER INSTRUMENT

The definition of a second-order instrument is one that has a dynamic response behavior that can be expressed in the form:

$$\frac{d^2y}{dt^2} + 2\zeta\omega_n \frac{dy}{dt} + \omega_n^2 y = K\omega_n^2 x(t)$$



$\zeta$  = damping factor

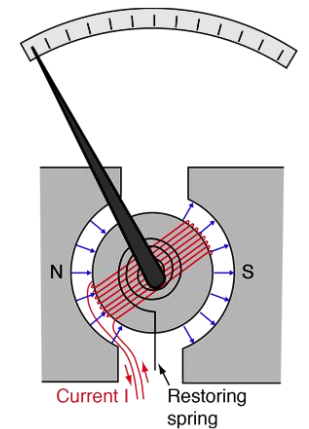
$\omega_n$  = natural frequency

$\zeta < 1$ : *underdamped*

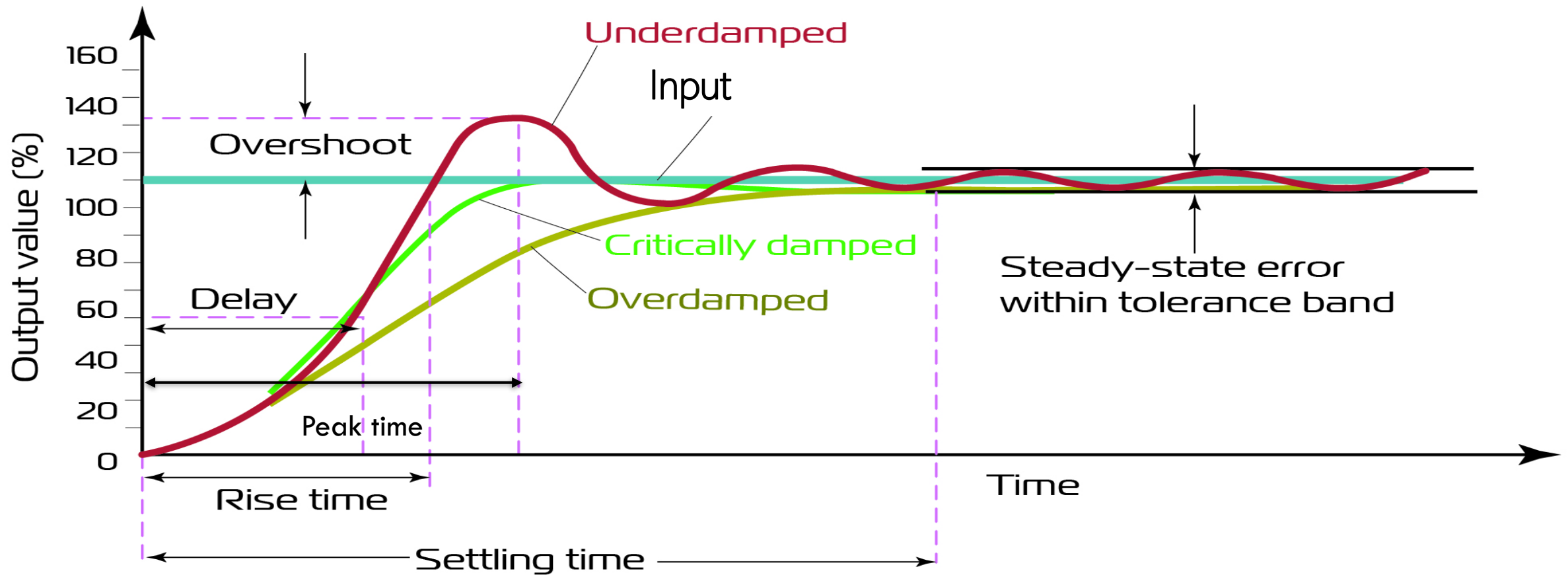
$\zeta = 1$ : *critically damped*

$\zeta > 1$ : *overdamped*

## Example



Moving coil Galvanometer



## STEP RESPONSE CHARACTERISTICS OF SECOND-ORDER INSTRUMENT

# DEFINITIONS

**Response time:** The time at which the transducers gives an output corresponding to some specified percentage e.g., 95% of the input value.

**Time constant:** 63.2% of the response time. The bigger the time constant, the slower the reaction to a changing input signal.

**Peak time:** Time taken by a system to give the first peak in the response.

**Overshoot:** The maximum amount by which the response overshoots the steady-state value.

**Rise time:** Time taken by a signal to change from a specified low value to a specified high value. These percentages are commonly the 10% and 90%.

**Settling time:** Time taken for the output to settle to within some percentage e.g., 2% of the steady-state value.

