```
1 // GRAPH.HPP
2
3 #pragma once
 4
5 #include <omp.h>
6 #include <fstream>
7 #include <functional>
8 #include <iostream>
 9 #include <queue>
10 #include <sstream>
11 #include <string>
12 #include <tuple>
13 #include <vector>
15 // Generic representation of a graph implemented with an adjacency matrix
16 struct Graph {
17
       using Node = int;
18
19
       int task threshold = 60;
20
       int max depth rdfs = 10'000;
2.1
22
       std::vector<std::vector<int>> adj_matrix;
23
24
       // Returns if an edge between two nodes exists
25
       bool edge exists(Node n1, Node n2) { return adj matrix[n1][n2] > 0; }
2.6
2.7
        // Returns the number of nodes of the graph
28
        int n nodes() { return adj matrix.size(); }
29
30
        // Returns the number of nodes of the graph
        int size() { return n nodes(); }
31
32
33
        // Sequential implementation of the iterative version of depth first search.
34
        void dfs(Node src, std::vector<int>& visited) {
35
            std::vector<Node> queue{src};
36
            while (!queue.empty()) {
37
                Node node = queue.back();
38
                queue.pop_back();
40
                if (!visited[node]) {
                    visited[node] = true;
41
42
                    for (int next node = 0; next node < n nodes(); next node++)</pre>
43
                        if (edge exists(node, next node) && !visited[next node])
44
                            queue.push back(next node);
45
46
            }
47
48
49
       // Sequential implementation of the recursive version of depth first search.
50
       void rdfs(Node src, std::vector<int>& visited, int depth = 0) {
51
            visited[src] = true;
            for (int node = 0; node < n_nodes(); node++) {
52
53
                if (edge exists(src, node) && !visited[node]) {
54
                    // Limit recursion depth to avoid stack overflow error
55
                    if (depth <= max depth rdfs)</pre>
                        rdfs(node, visited, depth + 1);
57
                        dfs(node, visited);
58
59
                }
60
            }
61
62
63
       // Parallel implementation of the iterative version of depth first search.
        // The general idea is that the main thread extracts the last node from the
64
        // queue and check the neighbors of the node in parallel. Each of these threads
65
66
       // have a private queue where neighbors still not visited are added. At the end,
       // threads concatenate their private queue to the main queue.
67
68
       void p_dfs(Node src, std::vector<int>& visited) {
69
            std::vector<Node> queue{src};
70
            while (!queue.empty()) {
71
                Node node = queue.back();
72
                queue.pop_back();
73
74
                if (!visited[node]) {
```

```
75
                     visited[node] = true;
 76
 77
     #pragma omp parallel shared(queue, visited)
 78
                     {
 79
                         // Every thread has a private queue to avoid continuous lock
 80
                         // checking to update the main one
 81
                         std::vector<Node> private queue;
 82
 83 #pragma omp for nowait schedule(static)
 84
                         for (int next node = 0; next node < n nodes(); next node++)</pre>
                             if (edge exists(node, next node) && !visited[next node])
 85
 86
                                 private_queue.push_back(next_node);
 87
 88
    // Append at the end of master queue the private queue of the thread
 89
    #pragma omp critical(queue update)
 90
                         queue.insert(queue.end(), private queue.begin(), private queue.end());
 91
                     }
 92
                 }
 93
             }
 94
         }
 95
         // Parallel implementation of the iterative version of depth first search.
 96
 97
         // The general idea is that the main thread extracts the last node from the
 98
         // queue and check the neighbors of the node in parallel. Each of these
 99
         // threads have a private queue where neighbors still not visited are added.
100
         // At the end, threads concatenate their private queue to the main queue.
101
         // **Important**: this version implements node level locks.
102
         void p_dfs_with_locks(Node src, std::vector<int>& visited,
103
                               std::vector<omp lock t>& node locks) {
104
             // Note: Since C++11, different elements in the same container can be
105
             // modified concurrently by different threads, except for the elements
106
             // of std::vector<bool>
            //
107
             // Possible explanation of why here:
108
109
             // https://stackoverflow.com/a/33617530/2691946
110
             // This is why we use a vector of int.
111
112
             std::vector<Node> queue{src};
113
             while (!queue.empty()) {
114
                 Node node = queue.back();
115
                 queue.pop_back();
116
117
                 bool already visited = atomic test visited(node, visited, &node locks[node]);
118
119
                 if (!already visited) {
120
                     atomic set visited(node, visited, &node locks[node]);
121
122 #pragma omp parallel shared(queue, visited)
123
124
                         // Every thread has a private queue to avoid continuos lock
125
                         // checking to update the main one
126
                         std::vector<Node> private_queue;
127
128
    #pragma omp for nowait
129
                         for (int next node = 0; next node < n nodes(); next node++) {
130
                             // Check if the edge exists is a non-blocking request,
131
                             // so it's better to do it before than checking if the
132
                             // node is already visited
133
                             if (edge exists(node, next node)) {
134
                                 if (atomic test visited(next node, visited, &node locks[next node])) {
135
                                     private_queue.push_back(next_node);
136
                                 }
137
                             }
138
                         }
139
140 // Append at the end of master queue the private queue of the thread
141 #pragma omp critical(queue update)
                         queue.insert(queue.end(), private queue.begin(), private queue.end());
142
143
144
                 }
145
             }
146
         }
147
148
         // Parallel implementation of the recursive version of depth first search.
149
         // This version automatically initialize locks
```

```
150
         void p rdfs(Node src, std::vector<int>& visited) {
151
           // Initialize locks
152
            std::vector<omp_lock_t> node_locks;
153
            node locks.reserve(size());
154
             for (int node = 0; node < n_nodes(); node++) {</pre>
155
                omp lock t lock;
157
                 node locks[node] = lock;
                 omp init lock(&(node locks[node]));
158
159
160
#pragma omp parallel shared(src, visited, node_locks)
162 #pragma omp single
163
            p_rdfs(src, visited, node_locks);
164
165
             // Destory locks
166
             for (int node = 0; node < n_nodes(); node++) omp_destroy_lock(&(node_locks[node]));</pre>
167
168
         // Parallel implementation of the recursive version of depth first search,
169
170
         // full version with locks
171
         void p_rdfs(Node src, std::vector<int>& visited, std::vector<omp_lock_t>& node_locks,
172
                     int depth = 0) {
173
             atomic set visited(src, visited, &node locks[src]);
174
175
             // Number of tasks in parallel executing at this level of depth
176
             int task_count = 0;
177
178
             for (int node = 0; node < n nodes(); node++) {</pre>
179
                 if (edge_exists(src, node) && !atomic_test_visited(node, visited, &node_locks[node])) {
180
                     // Limit the number of parallel tasks both horizontally (for
181
                     // checking neighbors) and vertically (between recursive
182
                     // calls).
183
                     11
184
                     // Fallback to iterative version if one of these limits are
185
                     // reached
186
                     if (depth <= max_depth_rdfs && task_count <= task_threshold) {</pre>
187
                         task_count++;
188
189 #pragma omp task untied default(shared) firstprivate(node)
190
191
                             p_rdfs(node, visited, node_locks, depth + 1);
192
                             task count--;
193
194
195
                     } else {
196
                         // Fallback to parallel iterative version
197
                         p_dfs_with_locks(node, visited, node_locks);
198
199
                 }
200
201
202 #pragma omp taskwait
203
204
205
         // Serial implementation of the Dijkstra algorithm without early exit condition.
206
        // Note: It does not use a priority queue.
207
208
         std::pair<std::vector<Node>, std::vector<Node>> dijkstra(Node src) {
209
             std::vector<Node> queue;
210
            queue.push_back(src);
211
212
             std::vector<Node> came_from(size(), -1);
             std::vector<Node> cost_so_far(size(), -1);
213
214
215
             came from[src] = src;
216
             cost_so_far[src] = 0;
217
218
             while (!queue.empty()) {
219
                 Node current = queue.back();
220
                 queue.pop back();
221
222
                 for (int next = 0; next < n_nodes(); next++) {</pre>
223
                     if (edge_exists(current, next)) {
224
                         int new_cost = cost_so_far[current] + adj_matrix[current][next];
```

```
225
226
                         if (cost_so_far[next] == -1 || new_cost < cost_so_far[next]) {</pre>
227
                              cost_so_far[next] = new_cost;
                             queue.push back(next);
229
                             came from[next] = current;
230
                         }
                    }
231
232
                }
233
234
235
             return std::make_pair(came_from, cost_so_far);
236
237
        inline std::vector<omp_lock_t> initialize_locks() {
238
239
             std::vector<omp lock t> node locks;
240
             node locks.reserve(n nodes());
241
242
             for (int node = 0; node < n_nodes(); node++) {</pre>
243
                 omp lock t lock;
244
                 node locks[node] = lock;
245
                 omp init lock(&(node locks[node]));
246
247
248
             return node locks;
249
250
251
        // Parallel implementation of the Dijkstra algorithm without early exit
252
        // condition using node level locks. As expected, it performs very poorly
253
        // Note: It does not use a priority queue.
254
255
        std::pair<std::vector<Node>, std::vector<Node>> p_dijkstra(Node src) {
256
             std::vector<Node> queue;
2.57
             queue.push_back(src);
258
259
             std::vector<Node> came from(size(), -1);
260
             std::vector<Node> cost so far(size(), -1);
261
262
             came_from[src] = src;
263
             cost_so_far[src] = 0;
265
            auto node_locks = initialize_locks();
266
2.67
             while (!queue.empty()) {
                 Node current = queue.back();
268
269
                 queue.pop_back();
270
271 #pragma omp parallel shared(queue, node_locks)
272 #pragma omp for
273
                 for (int next = 0; next < n_nodes(); next++) {</pre>
274
                     if (edge exists(current, next)) {
275
                         omp set lock(&node locks[current]);
276
                         auto cost_so_far_current = cost_so_far[current];
2.77
                         omp_unset_lock(&node_locks[current]);
278
                         int new_cost = cost_so_far_current + adj_matrix[current][next];
279
280
281
                         omp_set_lock(&node_locks[next]);
282
                         auto cost_so_far_next = cost_so_far[next];
283
                         omp unset lock(&node locks[next]);
284
285
                         if (cost_so_far_next == -1 || new_cost < cost_so_far_next) {</pre>
                             omp set lock(&node locks[next]);
287
                              cost_so_far[next] = new_cost;
288
                             came_from[next] = current;
289
                             omp unset lock(&node locks[next]);
290
291 #pragma omp critical(queue_update)
                             queue.push back(next);
293
                         }
294
                     }
295
                 }
296
             }
297
298
             // Destory locks
299
             for (int node = 0; node < n nodes(); node++) omp destroy lock(&(node locks[node]));</pre>
```

```
300
301
            return std::make_pair(came_from, cost_so_far);
302
303
304
        // Reconstruct path from the destination to the source
305
        std::vector<Node> reconstruct_path(Node src, Node dst, std::vector<Node> origins) {
306
           auto current node = dst;
307
            std::vector<Node> path;
308
309
            while (current node != src) {
310
                path.push back(current node);
311
                current_node = origins.at(current_node);
312
313
314
            path.push back(src);
315
            reverse (path.begin(), path.end());
316
317
            return path;
318
       }
319
320
      private:
        // Return true if a node is already visited using a node level lock
321
        inline bool atomic_test_visited(Node node, const std::vector<int>& visited, omp_lock_t* lock) {
322
323
            omp set lock(lock);
            bool already_visited = visited.at(node);
324
325
            omp_unset_lock(lock);
326
327
            return already_visited;
328
329
330
        // Set that a node is already visited using a node level lock
        inline void atomic set visited (Node node, std::vector<int>& visited, omp lock t* lock) {
331
332
            omp_set_lock(lock);
333
            visited[node] = true;
334
            omp unset lock(lock);
335
        }
336 };
337
338 // Import graph from a file
339 Graph import graph (std::string& path) {
340
        Graph graph;
341
342
        std::ifstream file(path);
343
        if (!file.is open()) {
344
            throw std::invalid argument("Input file does not exist or is not readable.");
345
346
347
        std::string line;
348
        // Read one line at a time into the variable line
349
350
        while (getline(file, line)) {
351
           std::vector<int> lineData;
352
            std::stringstream lineStream(line);
353
354
            // Read an integer at a time from the line
355
            int value:
356
            while (lineStream >> value) lineData.push_back(value);
357
            lineData.shrink_to_fit(); // Usefull?
358
359
            graph.adj matrix.push back(lineData);
360
        }
361
362
        graph.adj_matrix.shrink_to_fit();
363
364
        return graph;
365 }
```

```
1 // MAIN.CPP
2.
3 #include <array>
4 #include <chrono>
5 #include <functional>
6 #include <string>
7 #include <vector>
8
9 #include "graph.hpp"
10
11 using std::chrono::duration cast;
12 using std::chrono::high resolution clock;
13 using std::chrono::milliseconds;
15 std::string bench traverse(std::function<void()> traverse fn) {
16
       auto start = high_resolution_clock::now();
17
       traverse fn();
18
       auto stop = high resolution clock::now();
19
20
       // Subtract stop and start timepoints and cast it to required unit.
       // Predefined units are nanoseconds, microseconds, milliseconds, seconds,
2.1
22
       // minutes, hours. Use duration cast() function.
23
       auto duration = duration cast<milliseconds>(stop - start);
24
25
       // To get the value of duration use the count() member function on the
26
       // duration object
27
       return std::to_string(duration.count());
28 }
29
30 void full bench (Graph& graph) {
       int num test = 1;
31
       std::array<int, 6> num_threads{{1, 2, 4, 8, 16, 32}};
32
33
34
       std::vector<Graph::Node> visited(graph.size(), false);
35
       Graph::Node src = 0;
36
37
       // Explicitly disable dynamic teams as we are going to set a fixed number of
       // threads
38
39
       omp set dynamic(0);
40
       // TODO: find a better way to avoid code repetition
41
42
       std::cout << "Number of nodes: " << graph.size() << "\n\n";</pre>
43
44
45
       for (int i = 0; i < num test; i++) {
           std::cout << "\t"
46
47
                      << "Execution " << i + 1 << std::endl;
48
            std::cout << "Sequential iterative DFS: "</pre>
49
                      << bench traverse([&] { graph.dfs(src, visited); }) << "ms\n";</pre>
51
52
           // We cannot pass a copy of the vector, so we "reset" it every time
53
            std::fill(visited.begin(), visited.end(), false);
54
55
            std::cout << "Sequential recursive DFS: "</pre>
                      << bench_traverse([&]() { graph.rdfs(src, visited); }) << "ms\n";</pre>
57
           std::cout << "Dijkstra: " << bench traverse([&] { graph.dijkstra(0); }) << "ms\n";</pre>
59
60
           for (const auto n : num_threads) {
61
               std::fill(visited.begin(), visited.end(), false);
62
63
               std::cout << "Using " << n << " threads..." << std::endl;
64
               // Set to use N threads
65
66
               omp_set_num_threads(n);
67
68
                // Should we change also this?
69
               // graph.task threshold = n;
70
                std::cout << "Parallel iterative DFS: "</pre>
71
72
                          << bench_traverse([&] { graph.p_dfs(src, visited); }) << "ms\n";</pre>
73
74
                std::fill(visited.begin(), visited.end(), false);
```

```
75
 76
                std::cout << "Parallel recursive DFS: "</pre>
 77
                          << bench_traverse([&] { graph.p_rdfs(src, visited); }) << "ms\n";</pre>
 78
 79
                std::cout << "Parallel Dijkstra: " << bench traverse([&] { graph.p dijkstra(0); })</pre>
                          << "ms\n";
 80
           }
 82
 83
            std::fill(visited.begin(), visited.end(), false);
 84
            std::cout << std::endl;</pre>
 85
 86
        }
 87 }
 88
 89 int main(int argc, const char** argv) {
 90
        // TODO: Add a CLI? Also, we should accept more input files and process them separately
        if (argc < 2) {
 91
            std::cout << "Input file not specified.\n";</pre>
 93
            return 1;
 94
        }
 95
        std::string file_path = argv[1];
 96
 97
 98
       auto graph = import graph(file path);
 99
100
       full bench(graph);
101
102
        return 0;
103 }
104
105 /*
106
107 OUTPUT:
108
109 Number of nodes: 1000
110
111
            Execution 1
112 Sequential iterative DFS: 64ms
113 Sequential recursive DFS: 39ms
114 Dijkstra: 72ms
115 Using 1 threads...
116 Parallel iterative DFS: 61ms
117 Parallel recursive DFS: 63ms
118 Parallel Dijkstra: 79ms
119 Using 2 threads...
120 Parallel iterative DFS: 44ms
121 Parallel recursive DFS: 37ms
122 Parallel Dijkstra: 89ms
123 Using 4 threads...
124 Parallel iterative DFS: 37ms
125 Parallel recursive DFS: 25ms
126 Parallel Dijkstra: 256ms
127 Using 8 threads...
128 Parallel iterative DFS: 36ms
129 Parallel recursive DFS: 15ms
130 Parallel Dijkstra: 257ms
131 Using 16 threads...
132 Parallel iterative DFS: 80ms
133 Parallel recursive DFS: 15ms
134 Parallel Dijkstra: 532ms
135 Using 32 threads...
136 Parallel iterative DFS: 186ms
137 Parallel recursive DFS: 21ms
138 Parallel Dijkstra: 481ms
139 */
```