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$$\begin{cases} 8x + (y^2 - 1)(y + 3) = (y + 1)^3 - 2y \\ \left(x + \frac{3}{4}\right)^2 - x\left(x + \frac{1}{4}\right) = 2x + y - 1 \end{cases}$$

$$\begin{cases} 8x + y^3 + 3y^2 - y - 3 = y^3 + 3y^2 + 3y + 1 - 2y \\ \cancel{x^2} + \frac{3}{2}x + \frac{9}{16} - \cancel{x^2} - \frac{1}{4}x = 2x + y - 1 \quad \leadsto 24x + 9 - 4x = 32x + 16y - 16 \end{cases}$$

$$\begin{cases} 8x - 2y = 4 \\ -12x - 16y = -25 \end{cases}$$

$\leadsto$

$$\begin{cases} 4x - y = 2 \\ 12x + 16y = 25 \end{cases}$$

(3) Riduzione

$$\begin{cases} 12x - 3y = 6 \\ 12x + 16y = 25 \end{cases} \quad \uparrow - \quad \leadsto 19y = 19 \quad y = 1$$

$$4x - 1 = 2 \quad 4x = 3 \quad \leadsto x = \frac{3}{4} \quad P = \left(\frac{3}{4}; 1\right)$$

(2) Confronto

$$\begin{cases} 12x = 6 + 3y \\ 12x = 25 - 16y \end{cases} \quad \leadsto 6 + 3y = 25 - 16y \quad 19y = 19 \quad y = 1$$

(1) Sostituzione

$$\begin{cases} y = 4x - 2 \\ 12x + 16(4x - 2) = 25 \end{cases}$$

$$12x + 64x - 32 = 25$$

$$76x = 57$$

$$x = \frac{57}{76} = \frac{3}{4}$$

(4) Cramer

$$\begin{cases} 4x - y = 2 \\ 12x + 16y = 25 \end{cases}$$

$$D = \begin{pmatrix} 4 & -1 \\ 12 & 16 \end{pmatrix}$$

$$\text{Det}(D) = 4 \cdot 16 - (-1) \cdot 12 = 64 + 12 = 76$$

$$D_x = \begin{pmatrix} 2 & -1 \\ 25 & 16 \end{pmatrix} \quad \det(D_x) = 25 + 32 = 57$$

$$D_y = \begin{pmatrix} 4 & 2 \\ 12 & 25 \end{pmatrix} \quad \det(D_y) = 100 - 24 = 76$$

$$y = \frac{\det(D_y)}{\det(D)} = \frac{76}{76} = 1$$

$$x = \frac{\det(D_x)}{\det(D)} = \frac{57}{76} = \frac{3}{4}$$