

Pag 640 n 528

$$\frac{1}{2} \log_a 8x - [\log_a 8x]^2 < \frac{1}{2}$$

$$\log_a 8x = t$$

$$\frac{1}{2} t - t^2 < \frac{1}{2}$$

$$-2t^2 + t - 1 < 0$$

$$2t^2 - t + 1 > 0$$

$$\Delta = 1 - 8 = -7 < 0$$

$$\forall t \in \mathbb{R}$$

Dato che  $\log_a 8x = t$  vale per ogni valore di  $x$  purché soddisfi le condizioni di esistenza  $8x > 0$  cioè  $x > 0$

n 529

$$\log_2 (\log_3 (x+4)) > 0$$

$$\log_3 (x+4) > 1$$

$$x+4 > 3 \rightsquigarrow \boxed{x > -1}$$

$$\text{C.E. : } \begin{cases} x+4 > 0 \\ \log_3 (x+4) > 0 \end{cases}$$

$$\begin{cases} x > -4 \\ x+4 > 1 \rightsquigarrow x > -3 \end{cases}$$

$$\rightsquigarrow \boxed{x > -3}$$

Sol:  $x > -1$   
 $(-1; +\infty)$

n 530:  $\frac{4 - \log_2 x}{\log_2 (x-2)} \geq 0$

$$\text{C.E. : } \begin{cases} x > 0 \rightsquigarrow x > 0 \\ x-2 > 0 \rightsquigarrow x > 2 \end{cases}$$

$$\boxed{x > 2}$$

$$N \geq 0 \quad 4 - \log_2 x \geq 0$$

$$\log_2 x \leq 4$$

$$x \leq 2^4$$

$$D > 0 \quad \log_2 (x-2) > 0$$

$$x-2 > 1$$

$$x > 3$$

		3		16	
N	+		+		-
D	-		+		+
	-		+		-

Sol finale:  $3 < x \leq 16$   
 $(3; 16]$

$$\boxed{3 < x \leq 16}$$

Prog 641 n 549

$$\begin{cases} \log_2(4^x - 2) < 1 \\ \log_2 x + 2 > 0 \end{cases}$$

$$\begin{cases} \frac{1}{2} < x < 1 \\ x > \frac{1}{4} \end{cases}$$

Sol:

$$\frac{1}{2} < x < 1$$

$$\left(\frac{1}{2}; 1\right)$$

(I)  $4^x - 2 < 2$   
 $4^x < 4^1$   
 $x < 1$

Cf.  $4^x > 2 \rightarrow 2^{2x} > 2$   
 $\rightarrow 2x > 1$   $x > \frac{1}{2}$

$\Rightarrow$  con b.c.e.  $\frac{1}{2} < x < 1$

(II)  $\log_2 x > \frac{\log_2(2^{-2})}{-2}$   
 $x > 2^{-2} = \frac{1}{4}$

Cf.  $x > 0$

$\Rightarrow$  con b.c.e.  $x > \frac{1}{4}$

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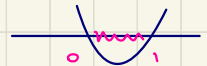
$$\left| \left(\frac{2}{5}\right)^x - \left(\frac{5}{2}\right)^{-2x} \right| < 2$$

$$\left| \left(\frac{2}{5}\right)^x - \left(\frac{2}{5}\right)^{2x} \right| < 2$$

$$\left(\frac{2}{5}\right)^x = B$$

$$|B - B^2| < 2$$

Caso a:  $B - B^2 \geq 0 \Rightarrow B^2 - B \leq 0 \Rightarrow B(B-1) \leq 0$   
 $B = 0, B = 1$



$0 \leq B \leq 1$

$B - B^2 < 2 \Rightarrow B^2 - B + 2 > 0 \quad \forall B \in \mathbb{R} \Rightarrow$  Sol a.  $0 \leq B \leq 1$   
 $\Delta = 1 - 8 = -7 < 0$

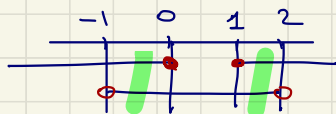
Caso b:  $B - B^2 \leq 0 \Rightarrow B \leq 0 \vee B \geq 1$

$$B^2 - B < 2 \quad \Leftrightarrow \quad B^2 - B - 2 < 0$$

$$(B-2)(B+1) < 0$$

$$\underline{-1 < B < 2}$$

La interseco con le condizioni del caso B.



$$\underline{\text{Sol b}} : \underline{-1 < B \leq 0 \vee 1 \leq B < 2}$$

Unisco Sol a e Sol b :

$$\underline{-1 < B < 2}$$

Mi ricordo  $B = \left(\frac{2}{5}\right)^x$

$$-1 < \left(\frac{2}{5}\right)^x$$

Sempre vero : esponenziale sempre  $> 0$

$$\left(\frac{2}{5}\right)^x < 2$$

$$x > \log_{\frac{2}{5}} 2 = \frac{\log 2}{\log \frac{2}{5}} = \frac{\log 2}{\log(2) - \log(5)}$$

$$||3^x| + 2^x| + 5^x| > 0$$

$$\sqrt[3]{|3+2^x|} > 1$$