Arithmetic types of C language

Basics of Programming 1

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Content

Chapter 1

Functions

Segmentation – motivation

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Let's create a program, that prints out the sum of the squares of all positive numbers, that are smaller than 12! $(1^2 + 2^2 + \cdots + 11^2)$

```c
#include <stdio.h> /* for printf */

int main(void)
{
  int i, sum; /* aux. variable and sum of squares*/

  sum = 0;                          /* initialization */
  for (i = 1; i < 12; i = i+1) /* i = 1,2,...,11 */
    sum = sum + i*i;                /* summing */

  printf("The square sum: %d\n", sum);
  return 0;
}
```

link

Segmentation – motivation

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```c
int main(void) {
  int i, sum1, sum2, sum3;

  sum1 = 0;              /* for 12 */
  for (i = 1; i < 12; i = i+1)
    sum1 = sum1 + i*i;

  sum2 = 0;              /* for 24 */
  for (i = 1; i < 24; i = i+1)
    sum2 = sum2 + i*i;

  sum3 = 0;              /* for 30 */
  for (i = 1; i < 30; i = i+1)
    sum3 = sum3 + i*i;

  printf("%d, %d, %d\n",
    sum1, sum2, sum3);
  return 0;
}
```

link

Let's create a program, that will perform the previous tasks with numbers 12, 24 and 30!
Our solution

- was made by Copy+Paste+correct
- many possibilities for mistakes, errors
- long program
- it is hard to manage

Is it possible in a more smarter way?

Functions

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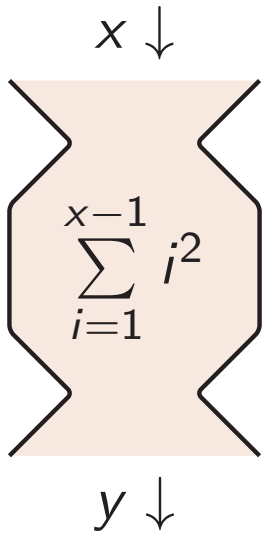
The function

- Standalone program segment
- For operations that occur frequently
- We can run it (call it) with different arguments
- Calculates something, and gives back the result for the program that called it



Functions – solution

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```c
int squaresum(int n) /* function definition */
{
  int i, sum = 0;
  for (i = 1; i < n; i = i+1)
    sum = sum + i*i;
  return sum;
}

int main(void) /* main program */
{
  int sum1, sum2, sum3;

  sum1 = squaresum(12); /* function call */
  sum2 = squaresum(24);
  sum3 = squaresum(30);

  printf("%d, %d, %d\n", sum1, sum2, sum3);
  return 0;
}
```

link

Function definition

Syntax of a function definition

```
<type of return value>
<function identifier> (<list of formal parameters>)
<block>
```

```
1  int squaresum(int n)
2  {
3    int i, sum = 0;
4    for (i = 1; i < n; i = i+1)
5      sum = sum + i*i;
6    return sum;
7  }
```

Function definition

Type of the return value:

- The type of the calculated value

```
1  double average(int a, int b)
2  {
3    return 0.5 * (a + b);
4  }
```

- or `void` (empty), if the function does not calculate anything

```
1  void print_point(double x, double y)
2  {
3    printf("(%.3f, %.3f)", x, y); /* (2.000, 4.123) */
4  }
```

- because sometimes we don't care about the calculated value, only about the "side effect" (secondary effect).

A remark: Primary and secondary effects

Primary the function calculates and gives back the return value

Secondary the function "performs some more things" (prints on screen, writes to file, plays an MP3, launches a missile...)

- Some programming languages make a clear distinction between different program segments:

  function where the primary effect is the important

  procedure no primary effect, but the secondary effect is important

- In C language there is only function. Procedures are represented by functions with empty (`void`) return value.
- Generally, we should try to separate the primary and secondary effects!

Function definition

Formal list of parameters

- Comma-separted list of declaration of parameters one-by-one, so we can reference them inside the function

```
1 double volume(double x, double y, double z)
2 {
3   return x*y*z;
4 }
```

- The number of parameters can be 0, 1, 2, . . . as much as you want (127 ☺)
- If there are 0 parameters, we denote it with `void`

```
1 double read_next_positive(void)
2 {
3   double input;
4   do scanf("%lf", &input) while (input <= 0);
5   return input;
6 }
```

Function definition

The `return` statement

- it gives a return value, it terminates the execution of the function's block, and returns to the point of calling
- there can be more of it, but it will cause to (terminate and) return to the point of calling at the first execution.

```
1  double distance(double a, double b)
2  {
3    double dist = b - a;
4    if (dist < 0)
5      return -dist;
6    return dist;
7  }
```

- it can also occur in a `void`-type function `return;`

Function call

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```
1 double distance(double a, double b)
2 {
3   ...
4 }
```

Syntax of a function call

<function identifier> (<actual argument expr.>)

```
1 double x = distance(2.0, 3.0); /* x will be 1.0 */
```

```
1 double a = 1.0;
2 double x = distance(2.5-1.0, a); /* x will be 0.5 */
```

```
1 double pos = read_next_positive(); /* empty () */
```

The main program as a function

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```c
int main(void) /* now we understand, what this is */
{
  ...
  return 0;
}
```

The main program is also a function

- it is called by the operation system at the start of the program
- it does not get any arguments (we will change this later)
- it returns with integer (`int`) value
  - Traditionally, if execution was OK, it gives 0-t, otherwise an error code

```
Process returned 0 (0x0)   execution time:  0.001 s
press ENTER to continue.
```

Mechanism of function call

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```c
/* Area of a rectangle */
int area(int x, int y)
{
  int S;
  S = x * y;
  return S;
}

/* Main program */
int main(void)
{
  int a, b, T;
  a = 2;                /* base */
  b = 3;              /* height */
  T = area(a, b); /* area */
  return 0;
}
```

register: 0

Mechanism of function call

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Passing parameters by value

- Functions receive the value of the actual argument expressions.
- Parameters can be used as variables, that have an initial value assigned at the point of calling.
- Functions may modify the values of the parameters, but this has no effect on the calling program segment.

Visibility and life-cycle of variables

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Local variables

1. parameters of functions
2. variables declared inside a function

- They are created when entering into the function, and are erased when returning from the function.
- They are invisible for program segments outside of the function. (also for the calling segment!)

Global variables – only for emergency cases!

Variables declared outside of functions (even outside of `main()`)

- They exist throughout the life-cycle of the program.
- They are visible for everyone and can be modified by anyone!
- In case of conflicts, the local variable masks out the global one.

Riddle

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What will the following program print on the screen?

```c
#include <stdio.h>

int a, b;

void func(int a)
{
  a = 2;
  b = 3;
}

int main(void)
{
  a = 1;
  func(a);
  printf("a: %d, b: %d\n", a, b);
  return 0;
}
```

link

A complex task

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Let's create a C program, that asks two integer numbers from the user (`low` < `high`), and lists all prime numbers between these two numbers..

- Pseudo-code of the solution broken into segments:

mainprogram

```
IN: low, high
FOR EACH i
  between low and high
  IF primetest(i) TRUE
    OUT: i
```

primetest(p)

```
FOR EACH i
  between 2 and root of p
  IF i divides p
    return FALSE
return TRUE
```

- Notice the role of the two *i* and *p*

Complex task – solution


```c
#include <stdio.h> /* scanf, printf */

int low, high; /* global variables */

void read(void) /* inputting function */
{
  printf("Give a small and a larger number!\n");
  scanf("%d%d", &low, &high);
}

int isprime(int p) /* primetest function. */
{
  int i;
  for (i=2; i*i<=p; i=i+1) /* i from 2 to root of p */
    /* if p is dividable by i, not a prime */
    if (p%i == 0)
      return 0;
  return 1; /* if we get here, it is a prime */
}
```

Complex task – solution

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```
20
21  int main()
22  {
23    int i;
24
25    read(); /* we read the limits with a function */
26
27    printf("Primes between %d and %d:\n", low, high);
28    for (i=low; i<=high; i=i+1)
29    {
30      if (isprime(i)) /* we test with a function */
31        printf("%d\n", i);
32    }
33
34    return 0;
35  }
```

link

Design principles

- Functions and programs communicate via parameters and return values.
- Except when this is their special task, functions
  - do not print on the screen,
  - do not read from keyboard,
  - do not use global variables.

Chapter 2

Arithmetic types of C

Types – Introduction

Type is

- Set of values
- Operations
- Representation

In a real computer – the set of values is limited

- We can not represent arbitrary large numbers
- We can not represent numbers with arbitrary accuracy
  $\pi \neq 3.141592654$
- We must know the limits of what can be represented, in order to store our data
  - without any loss of information or
  - with an acceptable level of information loss, without wasting memory

Types of C language

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- void
- scalar
  - arithmetic
    - integer: integer, character, enumerated
    - floating-point
  - pointer
- function
- union
- compound
  - array
  - structure
- Today we will learn about them

Binary representation of integers

- Binary representation of unsigned integers stored in 8 bits

dec	2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0	hex
0	0	0	0	0	0	0	0	0	0x00
1	0	0	0	0	0	0	0	1	0x01
2	0	0	0	0	0	0	1	0	0x02
3	0	0	0	0	0	0	1	1	0x03
⋮	⋮							⋮	⋮
127	0	1	1	1	1	1	1	1	0x7F
128	1	0	0	0	0	0	0	0	0x80
129	1	0	0	0	0	0	0	1	0x81
⋮	⋮							⋮	⋮
253	1	1	1	1	1	1	0	1	0xFD
254	1	1	1	1	1	1	1	0	0xFE
255	1	1	1	1	1	1	1	1	0xFF

The overflow

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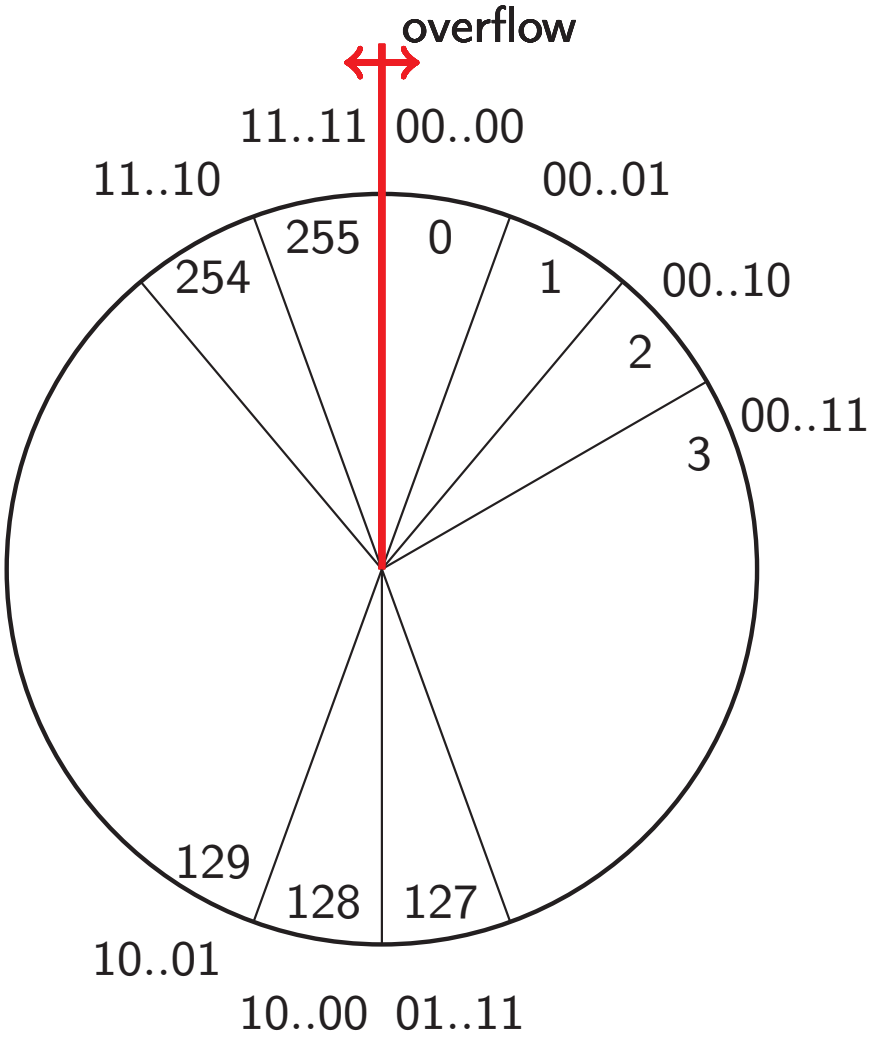

- In case of unsigned integers stored in 8 bits
  - 255+1 = 0
  - 255+2 = 1
  - 2-3 = 255
- "modulo 256 arithmetic"
  - We always see the remainder of the result divided by 256

Two's complement representation of integers

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- Two's complement representation of signed integers stored in 8 bits

dec	2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0	hex
0	0	0	0	0	0	0	0	0	0x00
1	0	0	0	0	0	0	0	1	0x01
2	0	0	0	0	0	0	1	0	0x02
3	0	0	0	0	0	0	1	1	0x03
⋮	⋮							⋮	⋮
127	0	1	1	1	1	1	1	1	0x7F
−128	1	0	0	0	0	0	0	0	0x80
−127	1	0	0	0	0	0	0	1	0x81
⋮	⋮							⋮	⋮
−3	1	1	1	1	1	1	0	1	0xFD
−2	1	1	1	1	1	1	1	0	0xFE
−1	1	1	1	1	1	1	1	1	0xFF

The overflow

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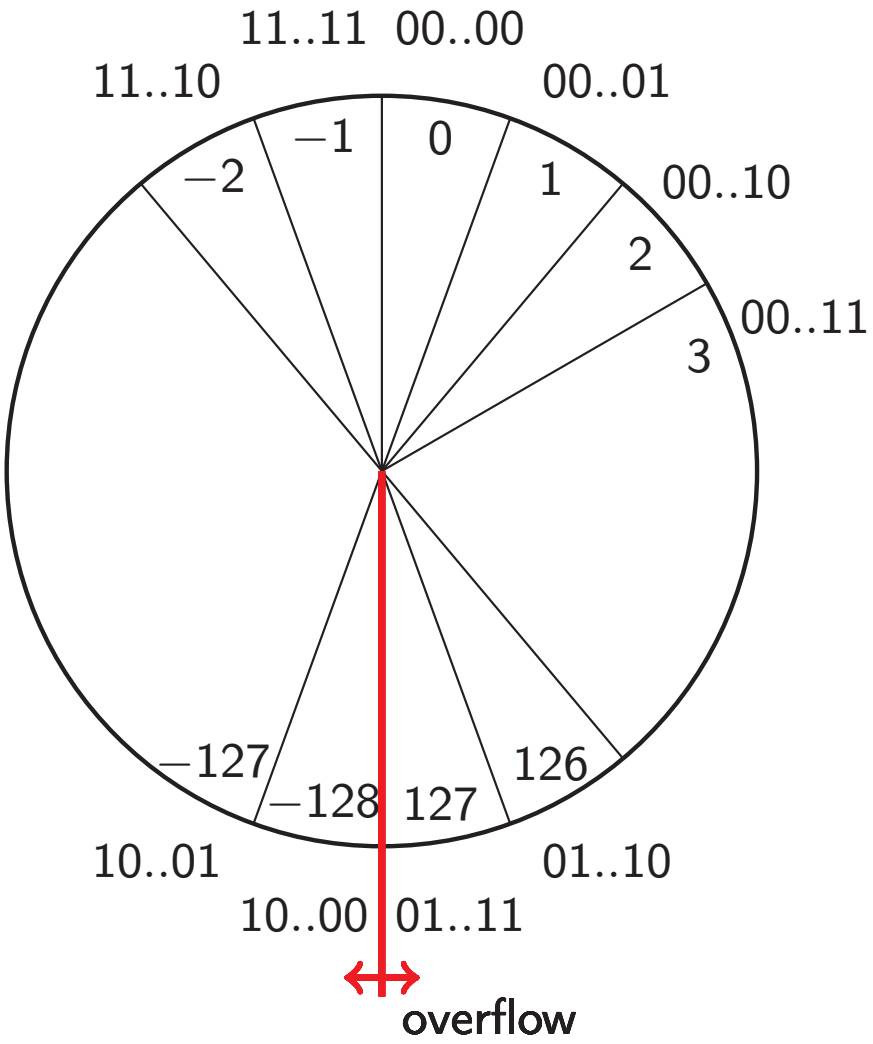

- In case of signed integers stored in 8 bits
  - 127+1 = -128
  - 127+2 = -127
  - -127-3 = 126
- on the other hand
  - 2-3 = -1

Integer types in C

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type	bit[1]	<limits.h>		printf
signed char	8	CHAR_MIN	CHAR_MAX	%hhd[2]
unsigned char	8	0	UCHAR_MAX	%hhu[2]
signed short int	16	SHRT_MIN	SHRT_MAX	%hd
unsigned short int	16	0	USHRT_MAX	%hu
signed int	32	INT_MIN	INT_MAX	%d
unsinged int	32	0	UINT_MAX	%u
signed long int	32	LONG_MIN	LONG_MAX	%ld
unsigned long int	32	0	ULONG_MAX	%lu
signed long long int[2]	64	LLONG_MIN	LLONG_MAX	%lld
unsigned long long int[2]	64	0	ULLONG_MAX	%llu

[1] Typical values, the standard only determines the minimum

[2] since the C99 standard

Declaration of integers

- Defaults
  - The `signed` sign-specifier can be omitted

```
1  int i;            /* signed int */
2  long int l;       /* signed long int */
```

  - If there is sign- or length-modifier, the `int` can be omitted.

```
1  unsigned u;         /* unsigned int */
2  short s;            /* signed short int */
```

Integer types

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- An example on how to use the previous table: a program that runs for a very long time[3]

```c
#include <limits.h> /* for integer limits */
#include <stdio.h>  /* for printf */

int main(void)
{ /* almost all long long int */
  long long i;

  for (i = LLONG_MIN; i < LLONG_MAX; i = i+1)
    printf("%lld\n", i);

  return 0;
}
```

link

[3] provided that `long long int` is 64 bit long, the program runs for 585 000 years if the computer prints 1 million numbers per second

Integer constants

- Specifying integer constants

```
1  int i1=0, i2=123, i4=-33;                /* decimal */
2  int o1=012, o2=01234567;                 /* octal */
3  int h1=0x1a, h2=0x7fff, h3=0xAa1B        /* hexadecimal */
4
5  long l1=0x1al, l2=-33L;                  /* l or L */
6
7  unsigned u1=33u, u2=45U;                 /* u or U */
8  unsigned long ul1=33uL, ul2=123lU; /* l and u */
```

- If neither u or l is specified, the first type that is big enough is taken:
  1. `int`
  2. `unsigned int` – in case of hexa and octal constants
  3. `long`
  4. `unsigned long`

Why do we need to know the limits of number representations?

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Let's determine the following value!

$$\binom{15}{12} = \frac{15!}{12! \cdot (15-12)!}$$

(What is the number of possibilities of selecting 12 out of 15 different chocolates?)

- The value of the numerator is $15! = 1\ 307\ 674\ 368\ 000$
- The value of the denominator is $12! \cdot 3! = 2\ 874\ 009\ 600$
- None of them can be represented as a 32 bits `int`!
- But with simplifying the expression

$$\frac{15 \cdot 14 \cdot 13}{3 \cdot 2 \cdot 1} = \frac{2730}{6} = 455$$

all parts can be calculated without any problem, even on 12 bits.

Representing characters – The ASCII table

- 128 characters, that can be indexed with numbers 0x00–0x7f

Code	00	10	20	30	40	50	60	70
+00	NUL	DLE	␣	0	@	P	‘	p
+01	SOH	DC1	!	1	A	Q	a	q
+02	STX	DC2	"	2	B	R	b	r
+03	ETX	DC3	#	3	C	S	c	s
+04	EOT	DC4	$	4	D	T	d	t
+05	ENQ	NAK	%	5	E	U	e	u
+06	ACK	SYN	&	6	F	V	f	v
+07	BEL	ETB	’	7	G	W	g	w
+08	BS	CAN	(	8	H	X	h	x
+09	HT	EM	)	9	I	Y	i	y
+0a	LF	SUB	*	:	J	Z	j	z
+0b	VT	ESC	+	;	K	[	k	{
+0c	FF	FS	,	<	L	\	l	|
+0d	CR	GS	-	=	M	]	m	}
+0e	SO	RS	.	>	N	^	n	~
+0f	SI	US	/	?	O	_	o	DEL

Storing, printing and reading characters

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- Characters (indexes of the ASCII table) are stored in `char` type
- Printing of the elements of the ASCII table is done with `%c` format code.

```
1 char ch = 0x61; /* hex 61 = dec 97 */
2 printf("%d: %c\n", ch, ch);
3 ch = ch+1; /* its value will be hex 62 = dec 98  */
4 printf("%d: %c\n", ch, ch);
```

- Output of the program

```
97:  a
98:  b
```

- Does it mean we have to learn the ASCII-codes to be able to print characters?

Character constants

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- A character placed between apostrophes is equivalent to its ASCII-code

```
1 char ch = 'a'; /* 0x61 ASCII-code is copied to ch */
2 printf("%d: %c\n", ch, ch);
3 ch = ch+1;
4 printf("%d: %c\n", ch, ch);
```

```
97:  a
98:  b
```

- Beware! '0' $\neq$ 0 !

```
1 char n = '0'; /* 0x30 ASCII-code is copied to ch !!! */
2 printf("%d: %c\n", n, n);
```

```
48:  0
```

Character constants

- Special character constants – that would be hard to type...

0x00	`\0`	null character (NUL)
0x07	`\a`	bell (BEL)
0x08	`\b`	backspace (BS)
0x09	`\t`	tabulator (HT)
0x0a	`\n`	line feed (LF)
0x0b	`\v`	vertical tab (VT)
0x0c	`\f`	form feed (FF)
0x0d	`\r`	carriage return (CR)
0x22	`\”`	quotation mark
0x27	`\’`	apostrophe
0x5c	`\\`	backslash

Character or integer number?

- In C language characters are equivalent to integer numbers
- It will be decided only at the moment of displaying how an integer value is printed: as a number or as a character (`%d` or `%c`)
- We can perform the same operations on characters as on integers (adding, subtracting, etc...)
- But what is the point in adding-subtracting characters?

Operations with characters

Let's write a program, that reads characters as long as a new line character has not arrived. After this the program should print out the sum of the read (scanned) digits.

```
1  char c;
2  int sum = 0;
3  do
4  {
5    scanf("%c", &c);                  /* reading */
6    if (c >= '0' && c <= '9')         /* if numerical digit */
7      sum = sum + (c-'0');            /* summing */
8  }
9  while (c != '\n');                  /* stop condition */
10 printf("The sum is: %d\n", sum);
```

```
The airplane has landed at 12:35 this afternoon
The sum is:  11
```

Operations with characters

Let's write a function, that converts the lowercase letters of the English alphabet to uppercase, but leaves all other characters unchanged.

```
1  char toupper(char c)
2  {
3    if (c >= 'a' && c <= 'z') /* if lowercase */
4    {
5      return c - 'a' + 'A';
6    }
7    return c;
8  }
```

Floating-point types

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- Normal form

$$23.2457 = (-1)^{0} \cdot 2.3245700 \cdot 10^{+001}$$
$$-0.001822326 = (-1)^{1} \cdot 1.8223260 \cdot 10^{-003}$$

Representation of the normal form

- Floating-point fractional = sign bit + mantissa + exponent
  1. sign bit: 0–positive, 1–negative
  2. mantissa: unsigned integer (without the decimal comma), because of normalization, the first digit is ≥ 1
  3. exponent (or order, characteristic): signed integer

Floating-point types

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- Binary normal form

$$5.0 = 1.25 \cdot 4 = (-1)^{0} \cdot 1.0100_{\mathrm{b}} \cdot 2^{010_{\mathrm{b}}}$$

0	0100	010

Representation of binary normal form

- Floating-point fractional = sign bit + mantissa + exponent
  1. sign bit: 0–positive, 1–negative
  2. mantissa: unsigned integer (without the **binary comma**), because of normalization, the first digit is $= 1$, so we don't store it[4].
  3. exponent: signed integer

[4] the leading bit is implicit

Floating-point types in C

- Floating-point types of C

type	typical values bits	mantissa	exponent	printf/scanf
`float`	32 bits	23 bits	8 bits	`%f`
`double`	64 bits	52 bits	11 bits	`%f`/`%lf`
`long double`	128 bits	112 bits	15 bits	`%Lf`

- Floating-point constants

```
1 float       f1=12.3f , f2=12.F , f3=.5f , f4=1.2e-3F ;
2 double      d1=12.3  , d2=12.  , d3=.5  , d4=1.2e-3  ;
3 long double l1=12.3l , l2=12.L , l3=.5l , l4=1.2e-3L ;
```

- In C we use decimal point and not a comma!

Representation accuracy of integer types

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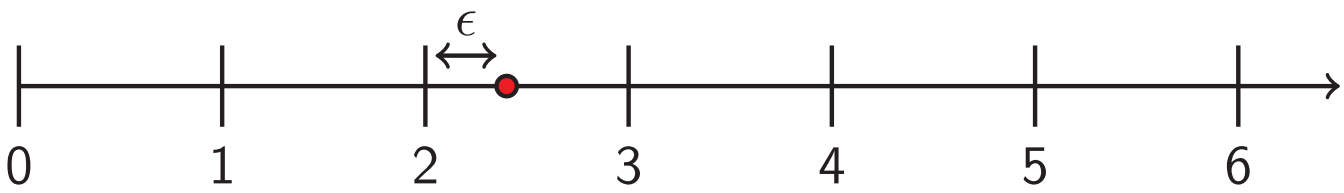

Absolute accuracy of number representation

It is the maximal ϵ error of representing an arbitrary real number with the closest integer

- The absolute accuracy of representing with integer types is 0.5

Representation accuracy of floating-point numbers

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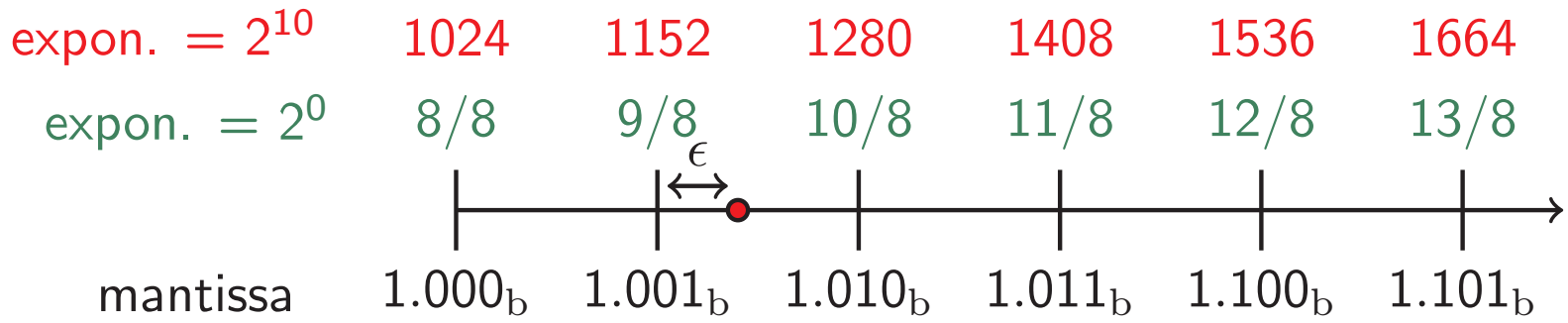

- in this example
  - The (absolute) representation accuracy of the mantissa is $1/16$
  - If the exponent is 2^0, the representation accuracy is $1/16$
  - If the exponent is 2^{10}, the representation accuracy is $2^{10}/16 = 64$
- There is no absolute, only relative accuracy, that is, in this present case, 3 bits.

Consequences of finite number representation

- As the floating-point number representation is not accurate, we must not check the equality of results of operations!

$$\frac{22}{7} + \frac{3}{7} \neq \frac{25}{7}$$

instead

$$\left| \frac{22}{7} + \frac{3}{7} - \frac{25}{7} \right| < \varepsilon$$

- The exponent will magnify the rounding error of the finite long mantissa, thus the large numbers are much less accurate than small numbers. The errors of the large numbers can "eat up" the small ones:

$$A + a - A \neq a$$

Consequences of the binary representation of numbers

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- A decimal finite number might not be finite in binary form, eg.:

$$0{,}1_{\mathrm{d}} = 0{,}0\overline{0011}_{\mathrm{b}}$$

- How many times will be this cycle repeated?

```
1  double d;
2  for (d = 0.0; d < 1.0; d = d+0.1) /* 10? 11? */
3  {
4    ...
5  }
```

- The good solution is:

```
1  double d;
2  double eps = 1e-3; /* what is the right eps for here? */
3  for (d = 0.0; d < 1.0-eps; d = d+0.1) /* 10 times */
4  {
5    ...
6  }
```

Thank you for your attention.