

# Dynamic data structures – Linked lists

## Basics of Programming 1



G. Horváth, A.B. Nagy, Z. Zsóka, P. Fiala, A. Vitéz

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- 1 Dynamic data structures
  - Self-referencing structure
- 2 Singly linked lists
  - Definition
  - Traversing
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  - Insertion
  - Deleting

# Chapter 1

## Dynamic data structures

# Dynamic data structure – motivation

- We are writing a chess program, in which there is undo option for arbitrary number of moves.
- The undo-list is the log of the game, its elements are the moves.
  - Which piece
  - From where
  - Where to
  - Who is captured (removed)
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  - Who is captured (removed)
- For logging we use the memory we really need, no more.
- The final length of the log will be known only at the end of the game.
- We have to increase the amount of allocated memory with each step (or reduce it, if we undo a move).

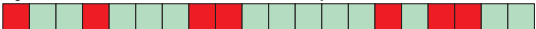
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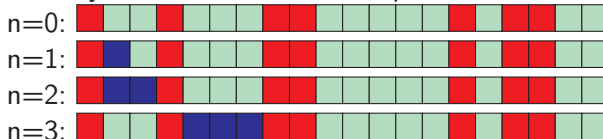
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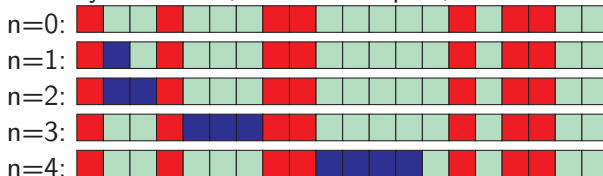
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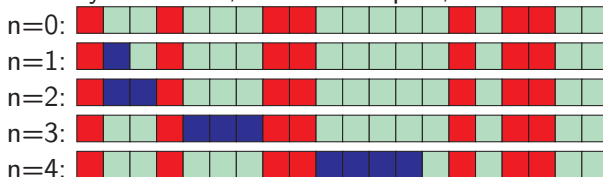
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# Dyanmic data structure – motivation

- If we use `realloc` for resizing an array, it may cause many unnecessary copying of data.

memory:  – free,  – occupied,  – our array



- We need a data structure that does not use continuous blocks of memory, and its structure changes dynamically during the lifecycle of the program.

# Dynamic data structure

Dynamic data structure:

- its size or structure changes during the lifecycle of the program
- it is realized with self-referencing structure

## Self-referencing structure

A compound data structure, that contains pointers pointing to itself

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1 typedef struct listelem {  
2     int data;                /* the data we store */  
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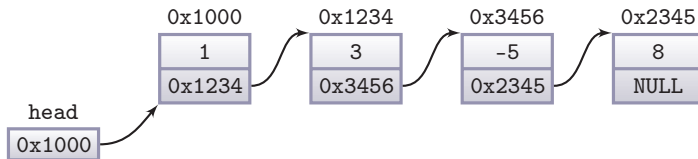
- next points to a structure that is of the same type, as the one containing the pointer itself.
- `struct listelem` structure is renamed to `listelem`, but when declaring `next`, we must use the long name (because the compiler doesn't know, what nickname we will give to it).

## Chapter 2

### Singly linked lists



# Linked list



- List of `listelem` type variables
- Memory is allocated dynamically, separately for each element
- Elements do not form a continuous block in memory
- Each element contains the address of the next element
- The first element is defined by the `head` pointer
- The last element points to nowhere (`NULL`)

# Linked list

## ■ Empty list

head

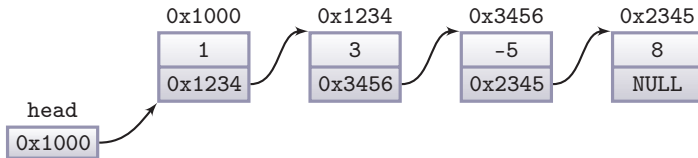
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# Linked list

## ■ Empty list



- List is a self-referencing (recursive) data structure. Each element points to a list.



# List or array

- The array
  - occupies as much memory, as needed for storing the data
  - needs a continuous block of memory
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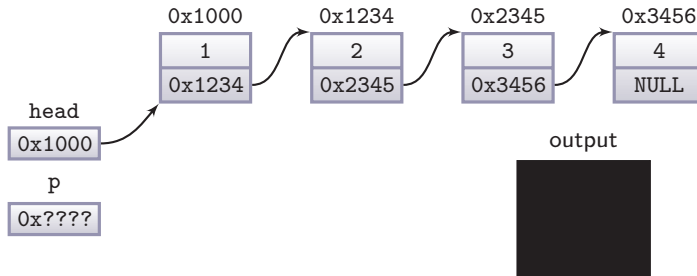
## ■ The list

- elements store the address of the next element, this may need a lot of memory
- can make use of gaps in the fragmented memory
- only the next element can be accessed immediately
- inserting a new element involves only a little work

# Traversing a list

- For traversing we need an auxiliary pointer (p), that will run along the list.

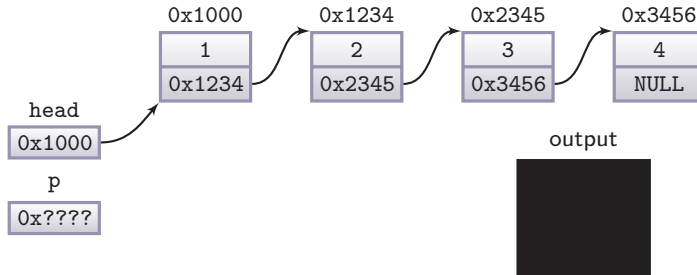
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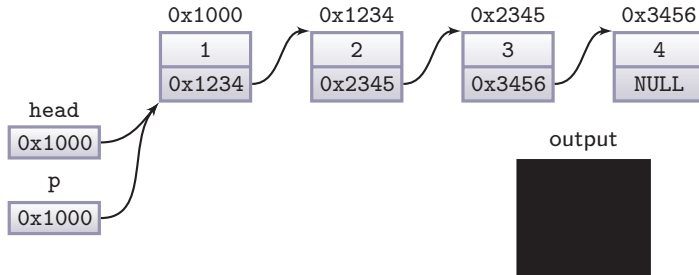
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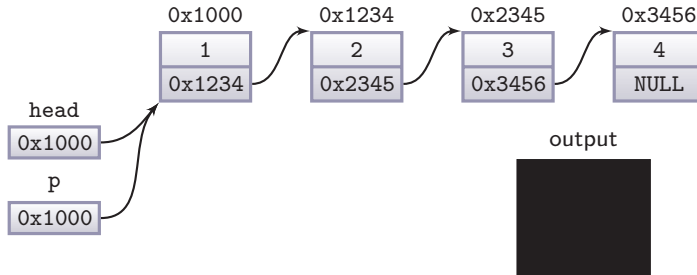




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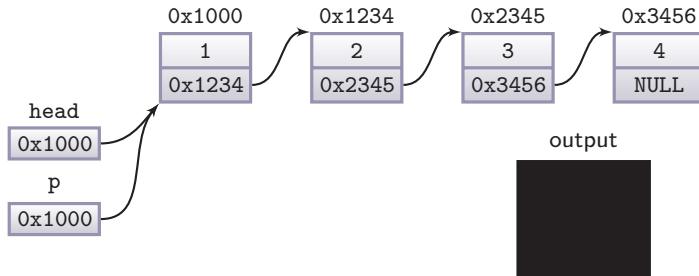
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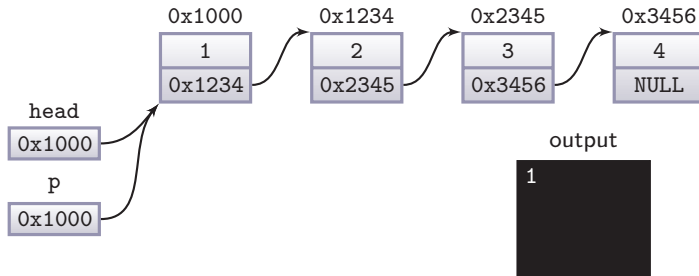
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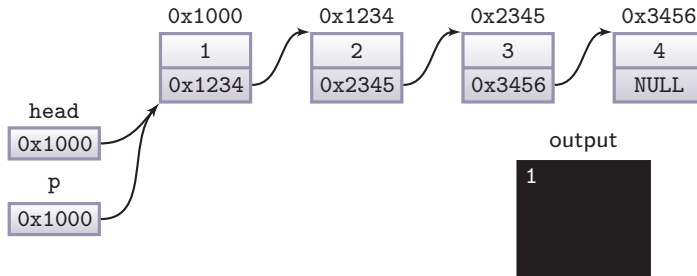
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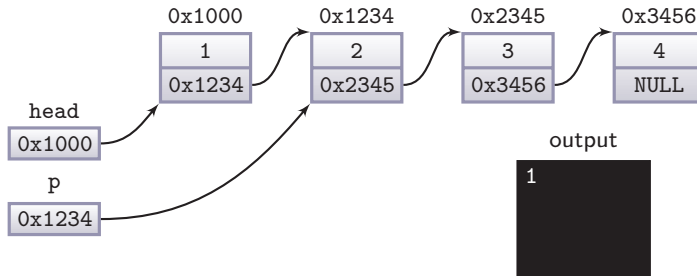
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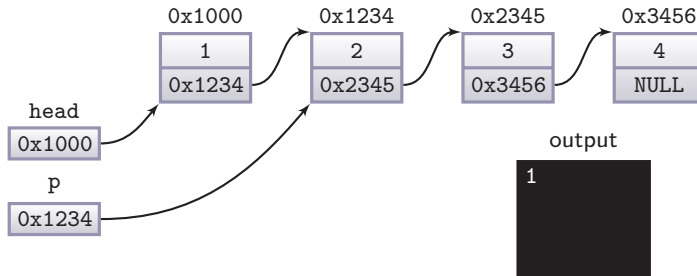
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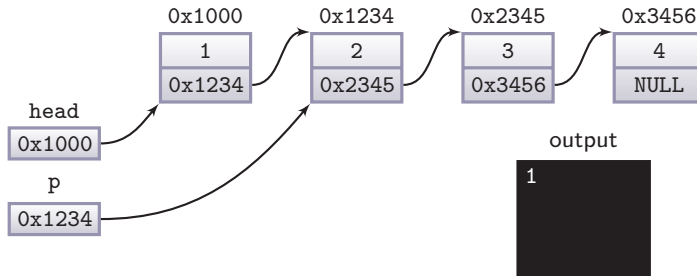
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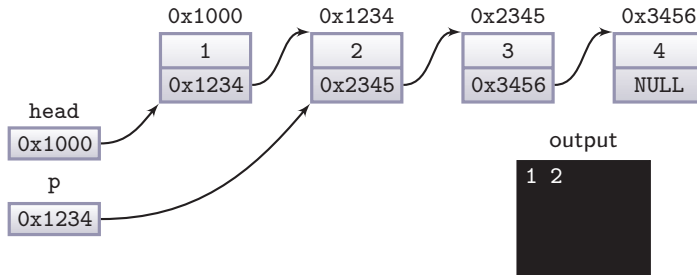
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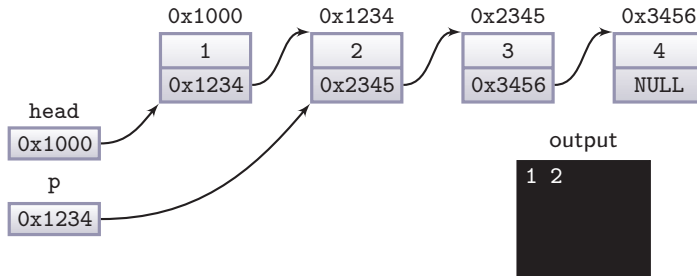




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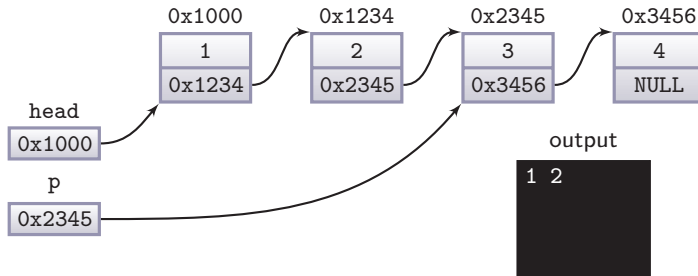
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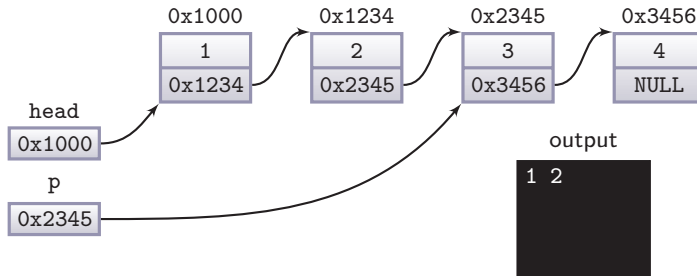
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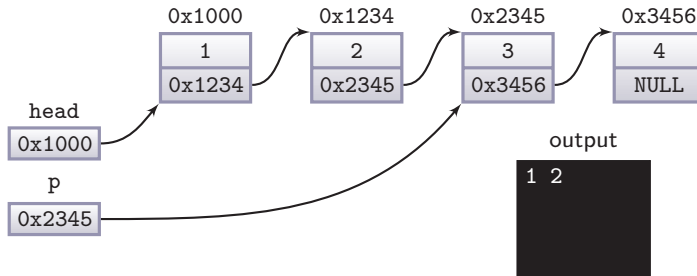
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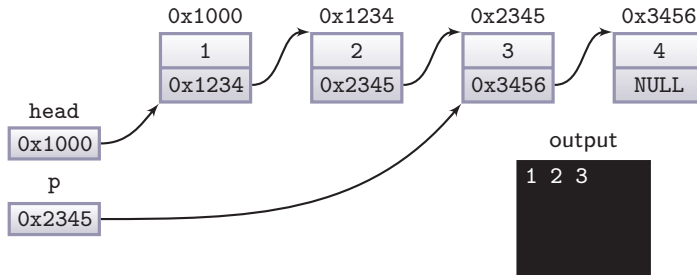
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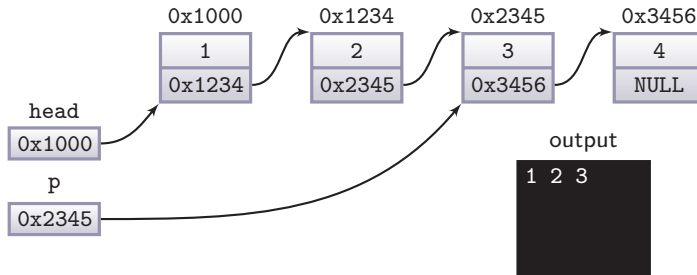
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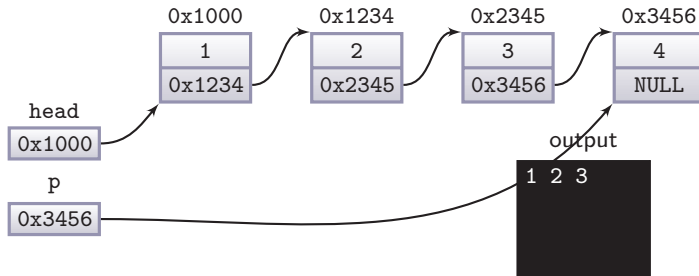
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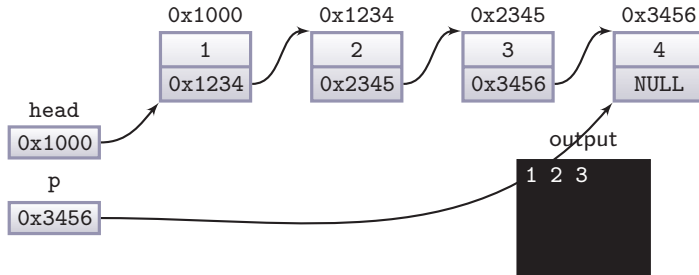
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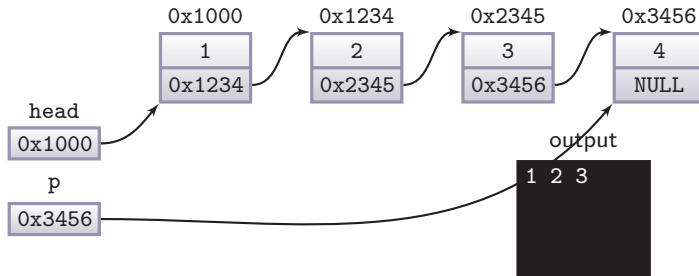




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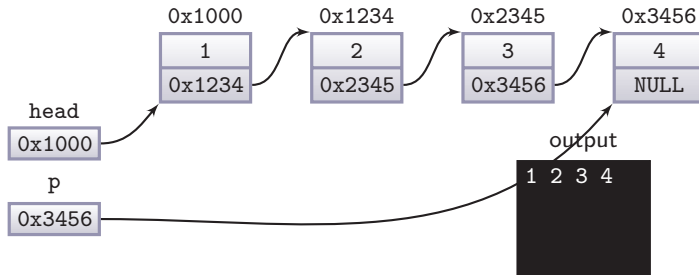
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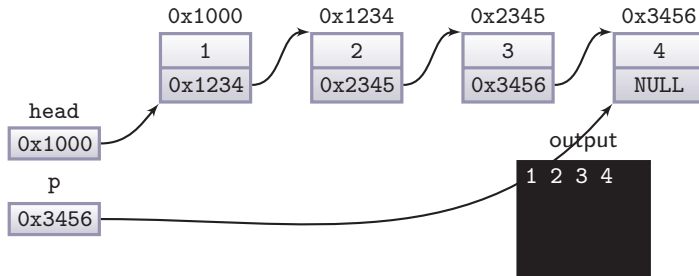
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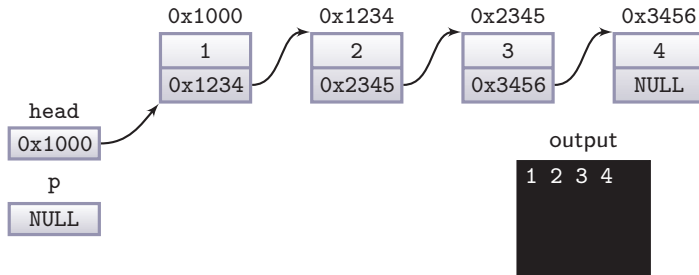
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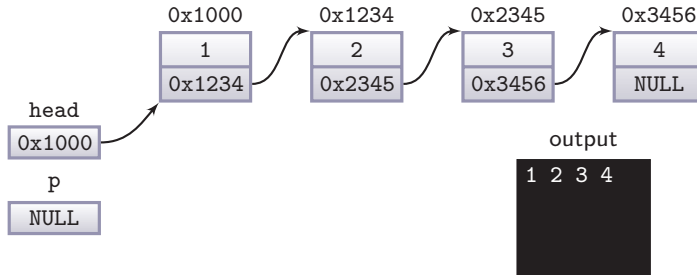
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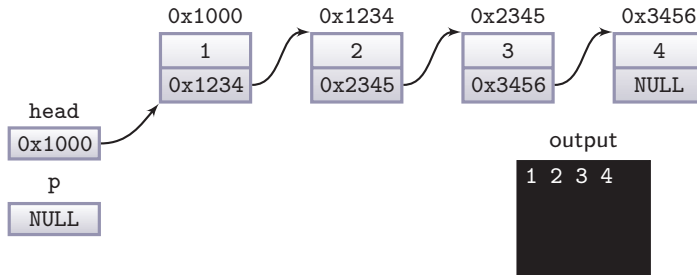
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2     listelem *p = head;  
3     while (p != NULL)  
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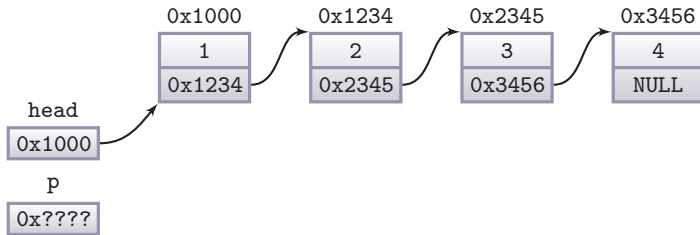
- the same with `for` loop

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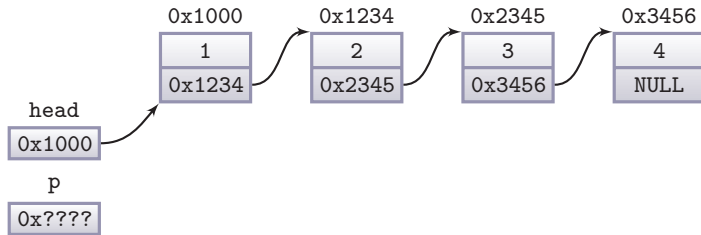
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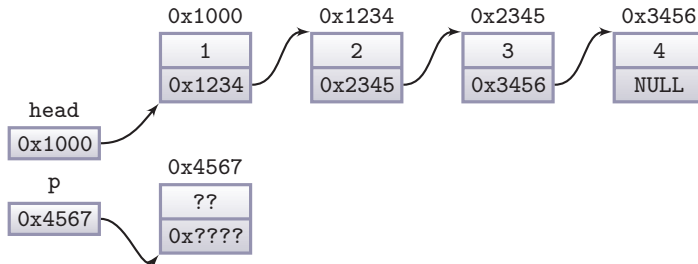
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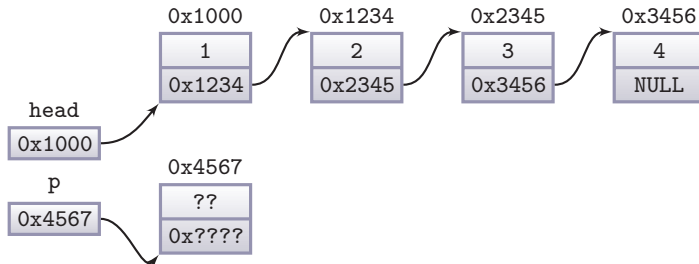
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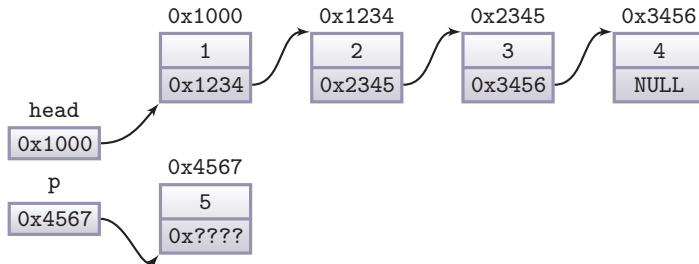
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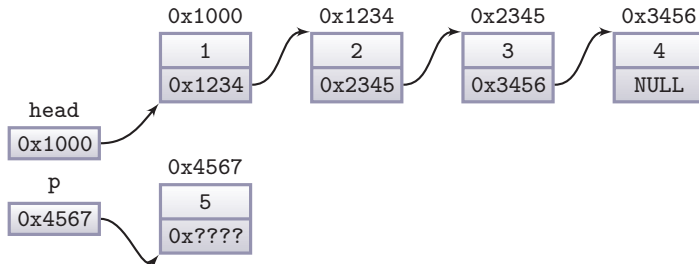
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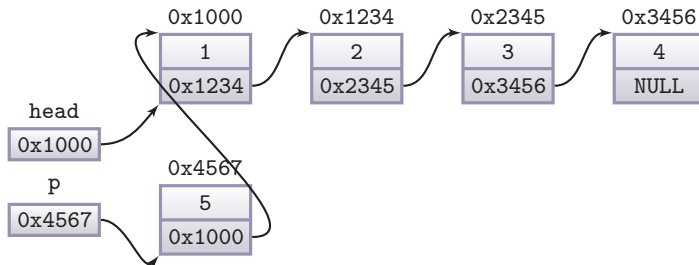
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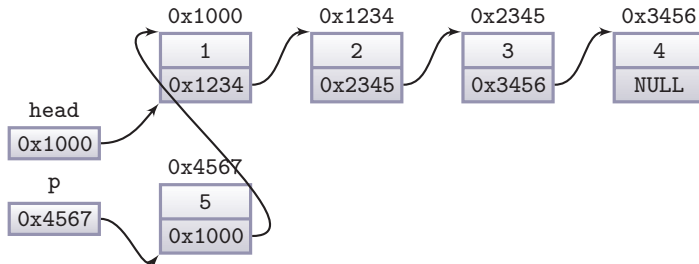
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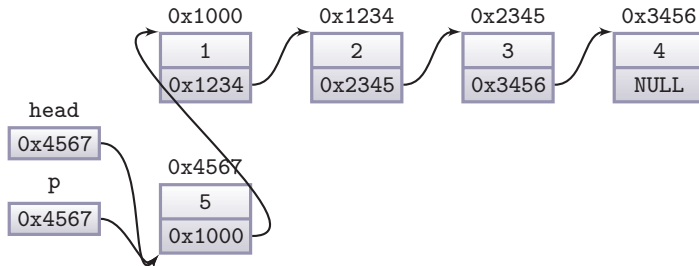
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1 p = (listelem*)malloc(sizeof(listelem));  
2 p->data = 5;  
3 p->next = head;  
4 head = p;
```





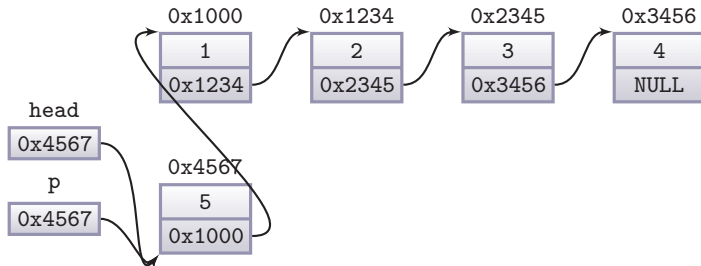
# Inserting element to the front of the list

```
1 p = (listelem*)malloc(sizeof(listelem));  
2 p->data = 5;  
3 p->next = head;  
4 head = p;
```



# Inserting element to the front of the list

```
1 p = (listelem*)malloc(sizeof(listelem));  
2 p->data = 5;  
3 p->next = head;  
4 head = p;
```



# Inserting element to the front of the list, with a function

- As the starting address is changed when inserting, we have to return it (pass it back)

```
1 listelem *push_front(listelem *head, int d)
2 {
3     listelem *p = (listelem*)malloc(sizeof(listelem));
4     p->data = d;
5     p->next = head;
6     head = p;
7     return head;
8 }
```

[link](#)

# Inserting element to the front of the list, with a function

- As the starting address is changed when inserting, we have to return it (pass it back)

```
1 listelem *push_front(listelem *head, int d)
2 {
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4     p->data = d;
5     p->next = head;
6     head = p;
7     return head;
8 }
```

[link](#)

- Usage of function

```
1 listelem *head = NULL;          /* empty list */
2 head = push_front(head, 2);      /* head is changed! */
3 head = push_front(head, 4);
```

# Inserting element to the front of the list, with a function

- Another option is to pass the starting address by its address

```
1 void push_front(listelem **head, int d)
2 {
3     listelem *p = (listelem*)malloc(sizeof(listelem));
4     p->data = d;
5     p->next = *head;
6     *head = p; /* *head is changes, this is not lost */
7 }
```

[link](#)

# Inserting element to the front of the list, with a function

- Another option is to pass the starting address by its address

```
1 void push_front(listelem **head, int d)
2 {
3     listelem *p = (listelem*)malloc(sizeof(listelem));
4     p->data = d;
5     p->next = *head;
6     *head = p; /* *head is changes, this is not lost */
7 }
```

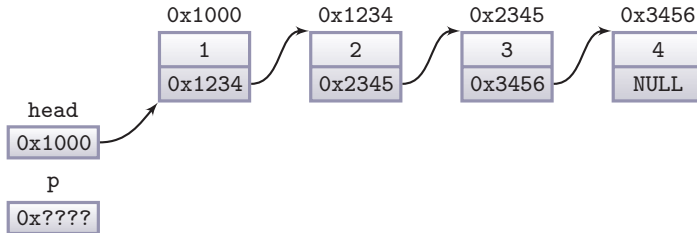
[link](#)

- In this case the usage of the function is:

```
1 listelem *head = NULL; /* empty list */
2 push_front(&head, 2); /* calling with address */
3 push_front(&head, 4);
```

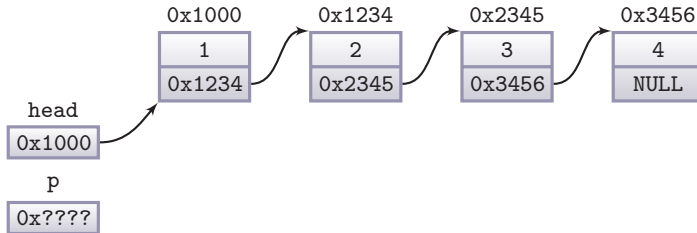
# Deleting element from the front of the list

```
1 p = head;  
2 head = head->next;  
3 free(p);
```



# Deleting element from the front of the list

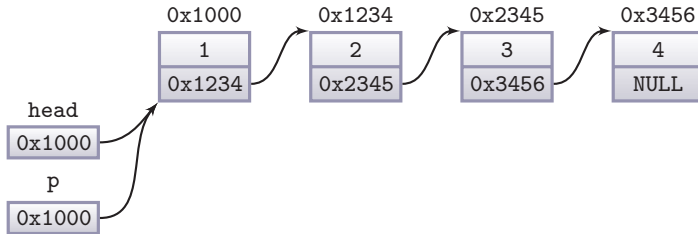
```
1 p = head;  
2 head = head->next;  
3 free(p);
```





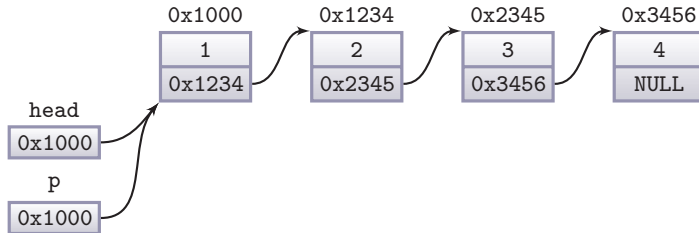
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```
1 p = head;  
2 head = head->next;  
3 free(p);
```



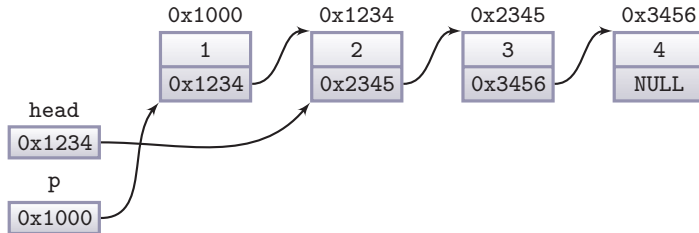
# Deleting element from the front of the list

```
1 p = head;  
2 head = head->next;  
3 free(p);
```



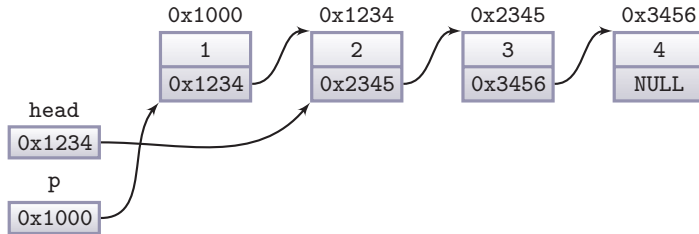
# Deleting element from the front of the list

```
1 p = head;  
2 head = head->next;  
3 free(p);
```



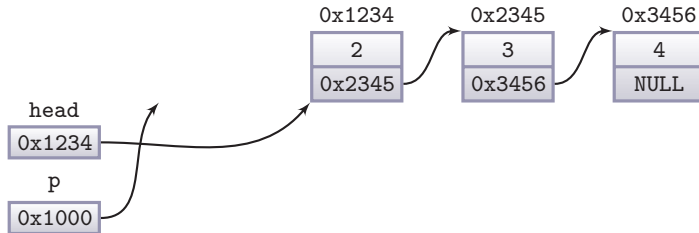
# Deleting element from the front of the list

```
1 p = head;  
2 head = head->next;  
3 free(p);
```



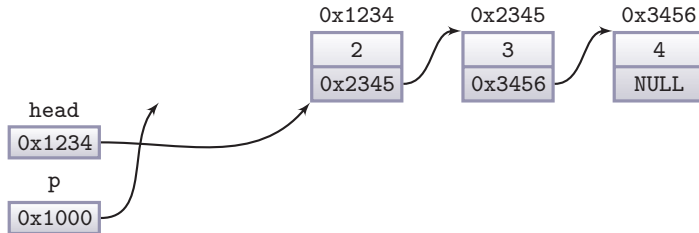
# Deleting element from the front of the list

```
1 p = head;  
2 head = head->next;  
3 free(p);
```



# Deleting element from the front of the list

```
1 p = head;  
2 head = head->next;  
3 free(p);
```



# Deleting element from front of the list with a function

```
1 listelem *pop_front(listelem *head)
2 {
3     if (head != NULL) /* not empty */
4     {
5         listelem *p = head;
6         head = head->next;
7         free(p);
8     }
9     return head;
10 }
```

[link](#)

- An empty list must be handled separately

## Deleting element from front of the list with a function

```
1 listelem *pop_front(listelem *head)
2 {
3     if (head != NULL) /* not empty */
4     {
5         listelem *p = head;
6         head = head->next;
7         free(p);
8     }
9     return head;
10 }
```

[link](#)

- An empty list must be handled separately
- Of course we could use the solution when calling the function with the address of head



# Stack

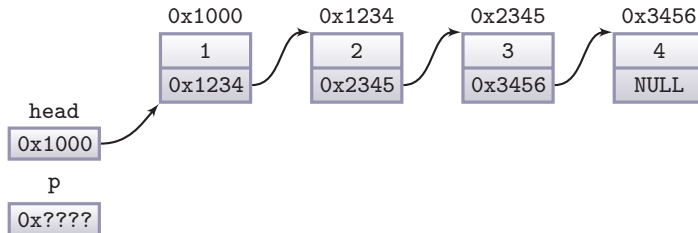
- What we have so far is already enough for storing the undo-list

```
1 listelem *head = NULL;           /* empty list */
2 head = push_front(head, 2);      /* step */
3 head = push_front(head, 4);      /* step */
4 printf("The last inserted element: %d\n", head->data);
5 head = pop_front(head);          /* undo */
6 head = push_front(head, 5);      /* step */
7 head = pop_front(head);          /* step */
8 head = pop_front(head);          /* step */
```

- The stack is a LIFO: Last In, First Out
- We can access the last inserted element first

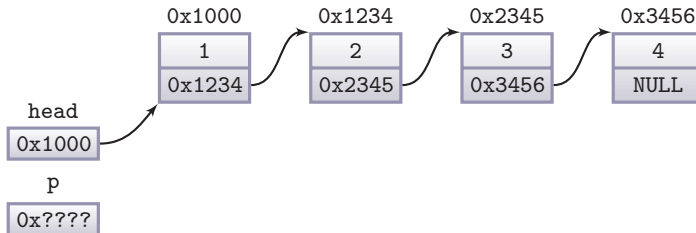
# Inserting element to the end of the list

```
1 for (p = head; p->next != NULL; p = p->next);  
2 p->next = (listelem*)malloc(sizeof(listelem));  
3 p->next->data = 5;  
4 p->next->next = NULL;
```



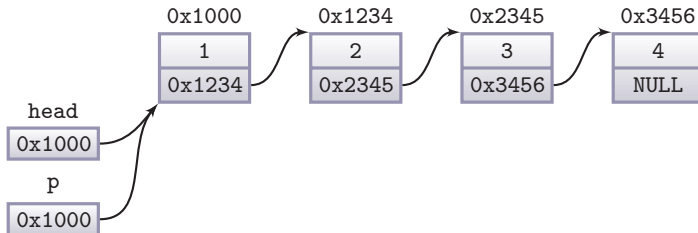
# Inserting element to the end of the list

```
1 for (p = head; p->next != NULL; p = p->next);  
2 p->next = (listelem*)malloc(sizeof(listelem));  
3 p->next->data = 5;  
4 p->next->next = NULL;
```



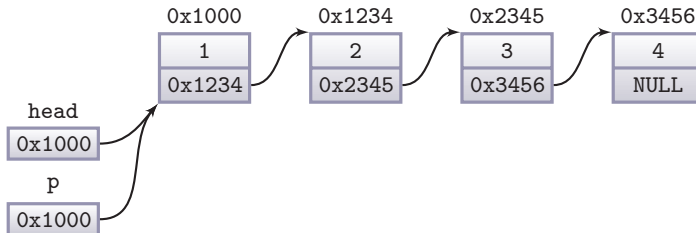
# Inserting element to the end of the list

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3 p->next->data = 5;  
4 p->next->next = NULL;
```



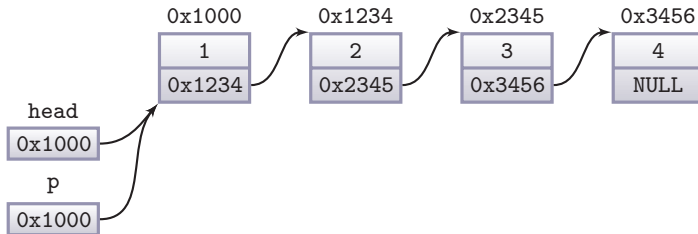
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```



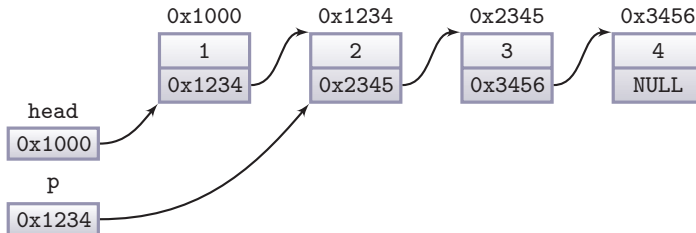
# Inserting element to the end of the list

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1 for (p = head; p->next != NULL; p = p->next);  
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```



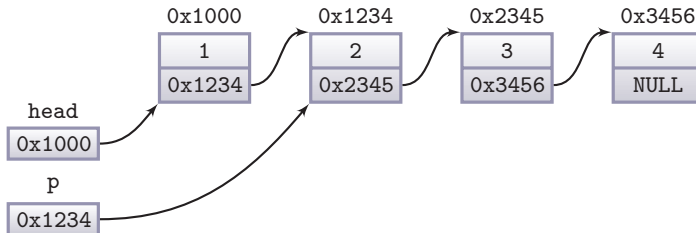
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4 p->next->next = NULL;
```



# Inserting element to the end of the list

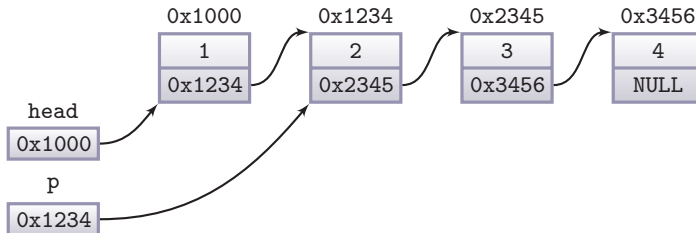
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3 p->next->data = 5;  
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```





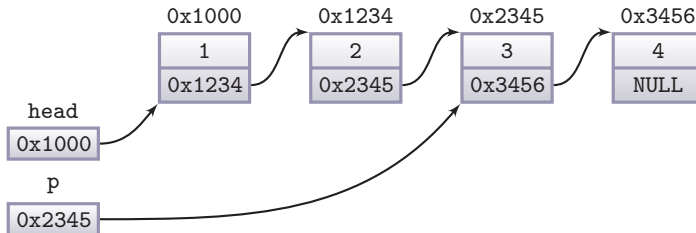
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```
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```



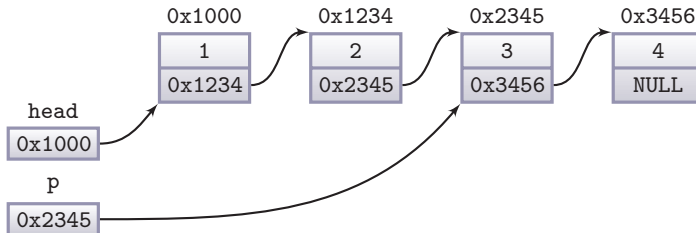
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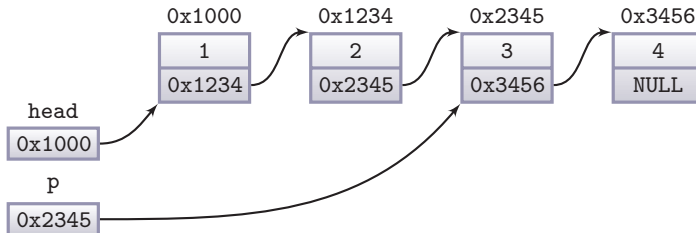
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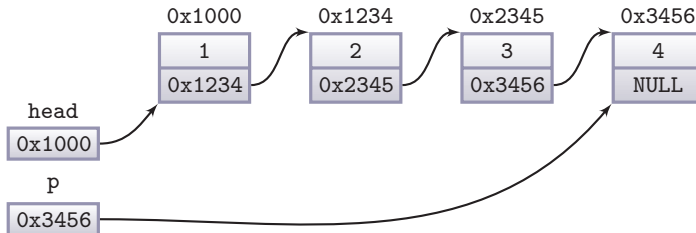
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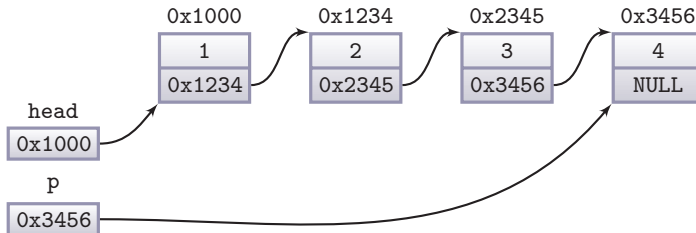
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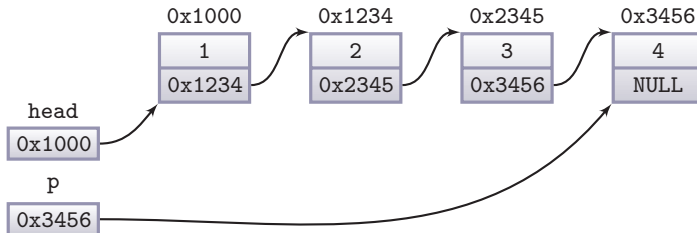
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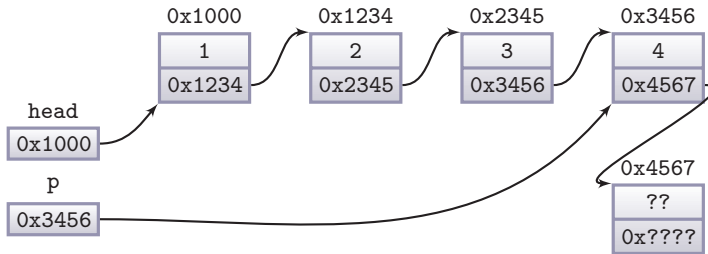
# Inserting element to the end of the list

```
1 for (p = head; p->next != NULL; p = p->next);  
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3 p->next->data = 5;  
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```



# Inserting element to the end of the list

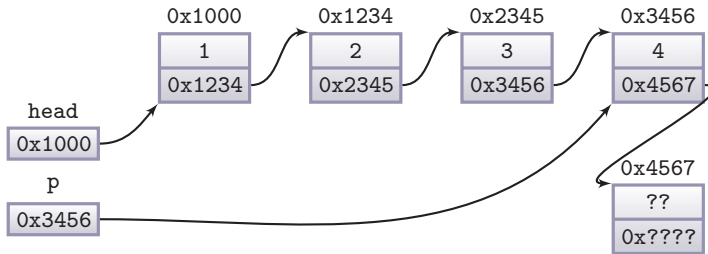
```
1 for (p = head; p->next != NULL; p = p->next);  
2 p->next = (listelem*)malloc(sizeof(listelem));  
3 p->next->data = 5;  
4 p->next->next = NULL;
```





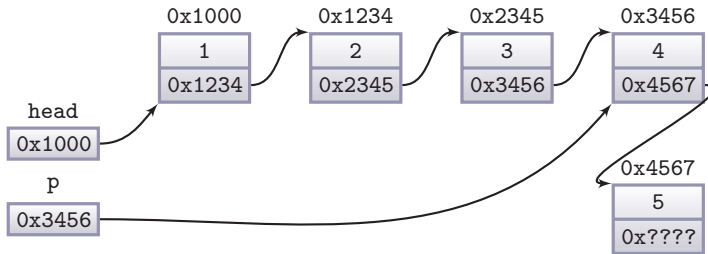
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```
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2 p->next = (listelem*)malloc(sizeof(listelem));  
3 p->next->data = 5;  
4 p->next->next = NULL;
```



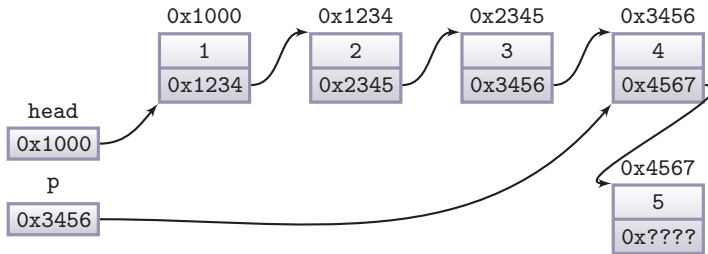
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4 p->next->next = NULL;
```



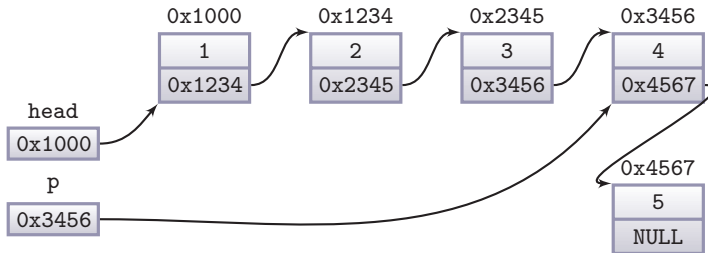
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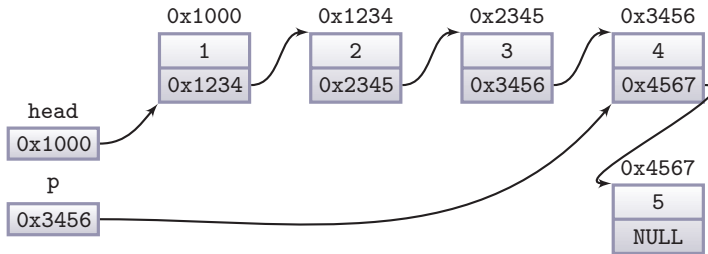
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```



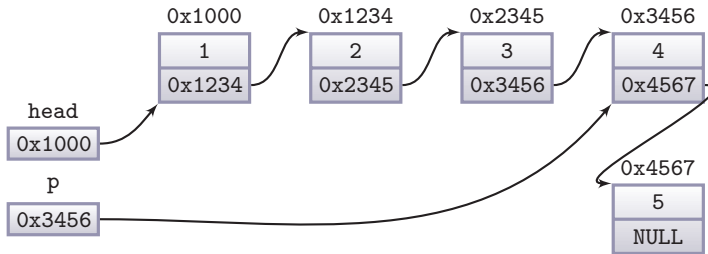
# Inserting element to the end of the list

```
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2 p->next = (listelem*)malloc(sizeof(listelem));  
3 p->next->data = 5;  
4 p->next->next = NULL;
```



# Inserting element to the end of the list

```
1 for (p = head; p->next != NULL; p = p->next);  
2 p->next = (listelem*)malloc(sizeof(listelem));  
3 p->next->data = 5;  
4 p->next->next = NULL;
```



- If the list is empty, checking `p->next != NULL` is not possible, this case must be managed separately!

## Inserting element to the end of the list with a function

```
1 listelem *push_back(listelem *head, int d)
2 {
3     listelem *p;
4
5     if (head == NULL) /* empty list should be
6                         managed separately */
7         return push_front(head, d);
8
9     for (p = head; p->next != NULL; p = p->next);
10    p->next = (listelem*)malloc(sizeof(listelem));
11    p->next->data = d;
12    p->next->next = NULL;
13    return head;
14 }
```

[link](#)

```
1 listelem *head = NULL;
2 head = push_back(head, 2);
```

# Inserting element into a sorted list

- If we have to traverse and process our data several times, it is worth sorting it
- Arrays:
  - re-locating a single element involves a lot of data movements
  - we fill up the array and order it afterwards



# Inserting element into a sorted list

- If we have to traverse and process our data several times, it is worth sorting it
- Arrays:
  - re-locating a single element involves a lot of data movements
  - we fill up the array and order it afterwards
- Lists:
  - re-locating a single element involves only the modification of pointers, the elements will remain at the same address in the memory
  - it is better to build up our list in a sorted way

# Inserting element into a sorted list

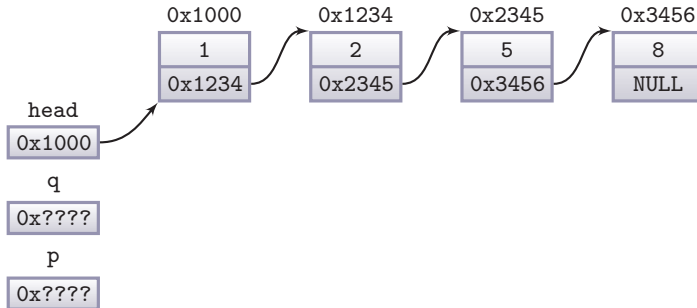
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- The new element must be inserted before the first element that is larger than it
- In the present structure each element "can see" only behind itself, so we cannot insert element before another

# Inserting element into a sorted list

- If we have to traverse and process our data several times, it is worth sorting it
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  - re-locating a single element involves a lot of data movements
  - we fill up the array and order it afterwards
- Lists:
  - re-locating a single element involves only the modification of pointers, the elements will remain at the same address in the memory
  - it is better to build up our list in a sorted way
- The new element must be inserted before the first element that is larger than it
- In the present structure each element "can see" only behind itself, so we cannot insert element before another
- We will use two pointers for traversing the list, one of them will be one step behind (delayed)
- We will insert after the delayed pointer

# Inserting element (4) into a sorted list

```
1 q = head; p = q->next;
2 while (p != NULL && p->data <= data) { /* shortcut */
3     q = p; p = p->next;
4 }
5 q->next = (listelem*)malloc(sizeof(listelem));
6 q->next->data = 4;
7 q->next->next = p;
```

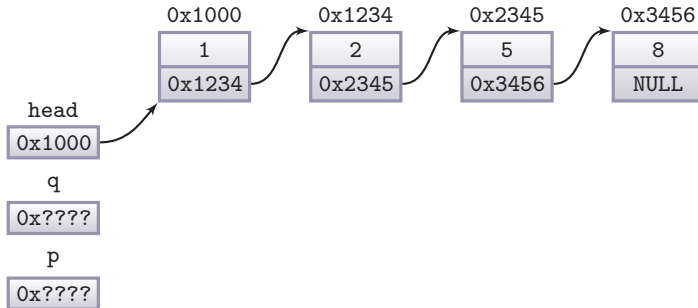


# Inserting element (4) into a sorted list

```

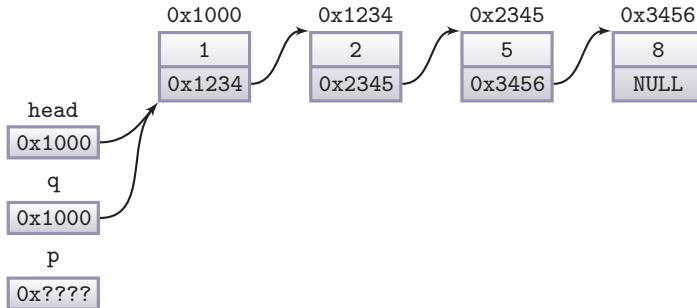
1  q = head;  p = q->next;
2  while (p != NULL && p->data <= data) { /* shortcut */
3      q = p;  p = p->next;
4  }
5  q->next = (listelem*)malloc(sizeof(listelem));
6  q->next->data = 4;
7  q->next->next = p;

```



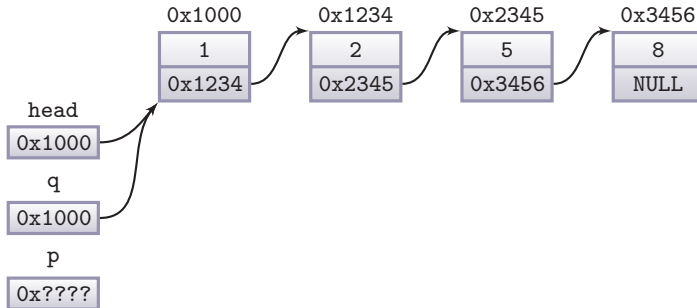
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1 q = head; p = q->next;
2 while (p != NULL && p->data <= data) { /* shortcut */
3     q = p; p = p->next;
4 }
5 q->next = (listelem*)malloc(sizeof(listelem));
6 q->next->data = 4;
7 q->next->next = p;
```



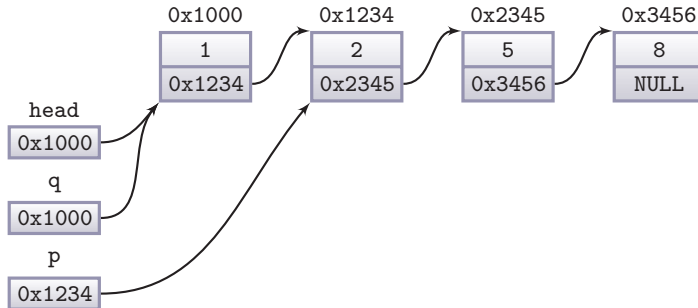
# Inserting element (4) into a sorted list

```
1 q = head; p = q->next;  
2 while (p != NULL && p->data <= data) { /* shortcut */  
3     q = p; p = p->next;  
4 }  
5 q->next = (listelem*)malloc(sizeof(listelem));  
6 q->next->data = 4;  
7 q->next->next = p;
```



# Inserting element (4) into a sorted list

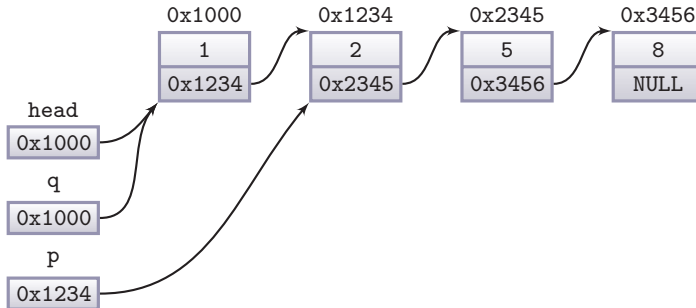
```
1 q = head; p = q->next;  
2 while (p != NULL && p->data <= data) { /* shortcut */  
3     q = p; p = p->next;  
4 }  
5 q->next = (listelem*)malloc(sizeof(listelem));  
6 q->next->data = 4;  
7 q->next->next = p;
```





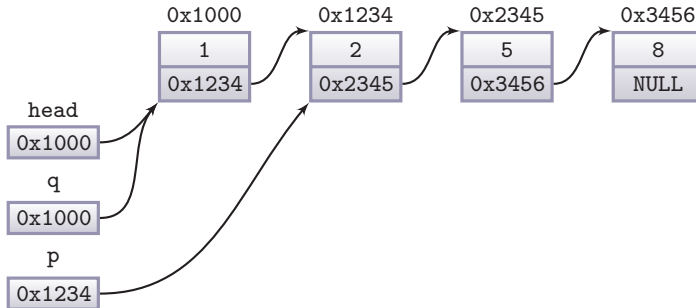
# Inserting element (4) into a sorted list

```
1 q = head; p = q->next;
2 while (p != NULL && p->data <= data) { /* shortcut */
3     q = p; p = p->next;
4 }
5 q->next = (listelem*)malloc(sizeof(listelem));
6 q->next->data = 4;
7 q->next->next = p;
```



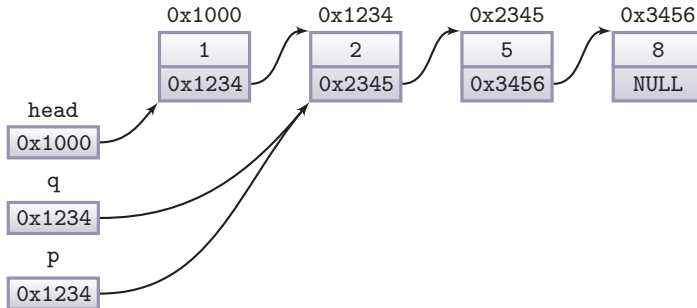
# Inserting element (4) into a sorted list

```
1 q = head; p = q->next;
2 while (p != NULL && p->data <= data) { /* shortcut */
3     q = p; p = p->next;
4 }
5 q->next = (listelem*)malloc(sizeof(listelem));
6 q->next->data = 4;
7 q->next->next = p;
```



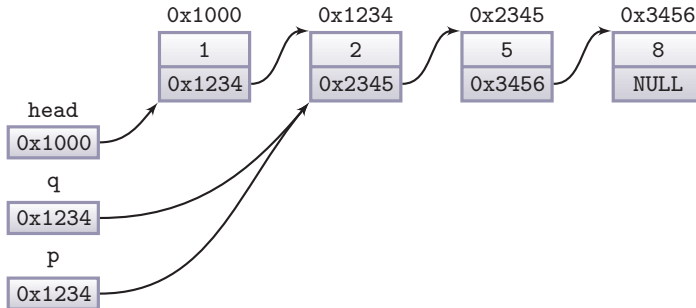
# Inserting element (4) into a sorted list

```
1 q = head; p = q->next;
2 while (p != NULL && p->data <= data) { /* shortcut */
3     q = p; p = p->next;
4 }
5 q->next = (listelem*)malloc(sizeof(listelem));
6 q->next->data = 4;
7 q->next->next = p;
```



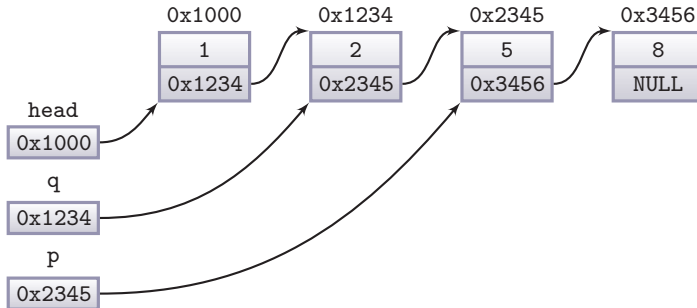
# Inserting element (4) into a sorted list

```
1 q = head; p = q->next;
2 while (p != NULL && p->data <= data) { /* shortcut */
3     q = p; p = p->next;
4 }
5 q->next = (listelem*)malloc(sizeof(listelem));
6 q->next->data = 4;
7 q->next->next = p;
```



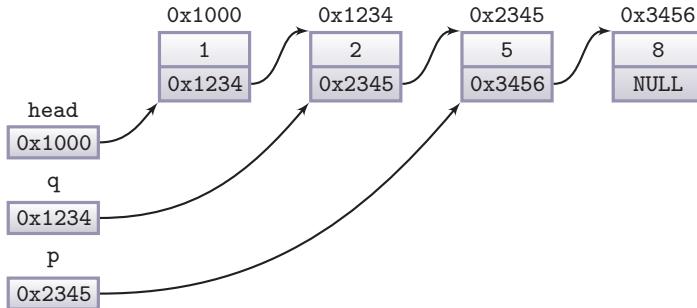
# Inserting element (4) into a sorted list

```
1 q = head; p = q->next;
2 while (p != NULL && p->data <= data) { /* shortcut */
3     q = p; p = p->next;
4 }
5 q->next = (listelem*)malloc(sizeof(listelem));
6 q->next->data = 4;
7 q->next->next = p;
```



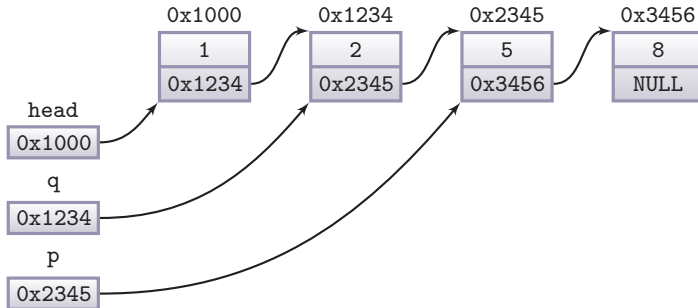
# Inserting element (4) into a sorted list

```
1 q = head; p = q->next;
2 while (p != NULL && p->data <= data) { /* shortcut */
3     q = p; p = p->next;
4 }
5 q->next = (listelem*)malloc(sizeof(listelem));
6 q->next->data = 4;
7 q->next->next = p;
```



# Inserting element (4) into a sorted list

```
1 q = head; p = q->next;
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3     q = p; p = p->next;
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5 q->next = (listelem*)malloc(sizeof(listelem));
6 q->next->data = 4;
7 q->next->next = p;
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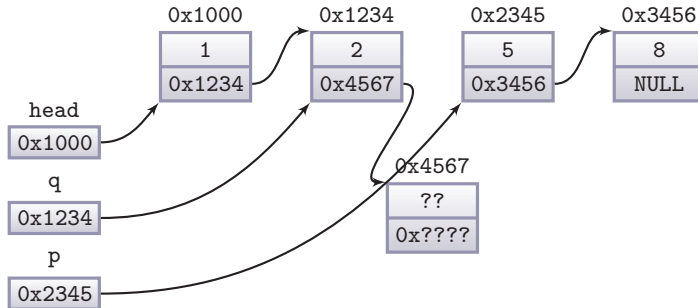


# Inserting element (4) into a sorted list

```

1  q = head;  p = q->next;
2  while (p != NULL && p->data <= data) { /* shortcut */
3      q = p;  p = p->next;
4  }
5  q->next = (listelem*)malloc(sizeof(listelem));
6  q->next->data = 4;
7  q->next->next = p;

```



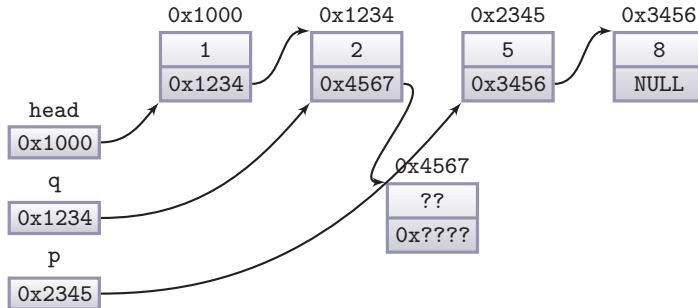


# Inserting element (4) into a sorted list

```

1  q = head;  p = q->next;
2  while (p != NULL && p->data <= data) { /* shortcut */
3      q = p;  p = p->next;
4  }
5  q->next = (listelem*)malloc(sizeof(listelem));
6  q->next->data = 4;
7  q->next->next = p;

```

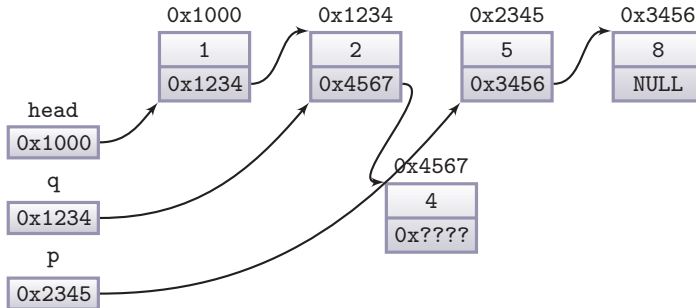


# Inserting element (4) into a sorted list

```

1  q = head;  p = q->next;
2  while (p != NULL && p->data <= data) { /* shortcut */
3      q = p;  p = p->next;
4  }
5  q->next = (listelem*)malloc(sizeof(listelem));
6  q->next->data = 4;
7  q->next->next = p;

```

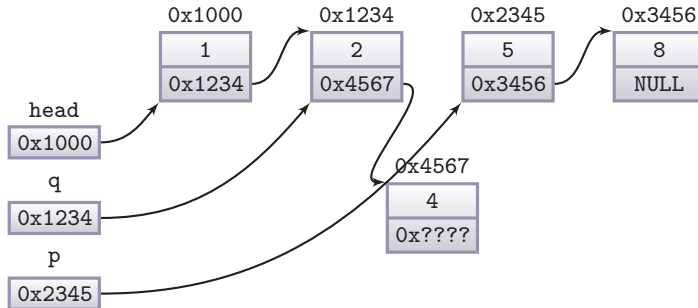


# Inserting element (4) into a sorted list

```

1  q = head;  p = q->next;
2  while (p != NULL && p->data <= data) { /* shortcut */
3      q = p;  p = p->next;
4  }
5  q->next = (listelem*)malloc(sizeof(listelem));
6  q->next->data = 4;
7  q->next->next = p;

```

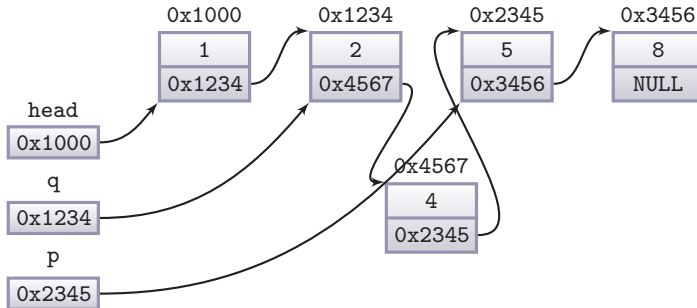


# Inserting element (4) into a sorted list

```

1  q = head;  p = q->next;
2  while (p != NULL && p->data <= data) { /* shortcut */
3      q = p;  p = p->next;
4  }
5  q->next = (listelem*)malloc(sizeof(listelem));
6  q->next->data = 4;
7  q->next->next = p;

```

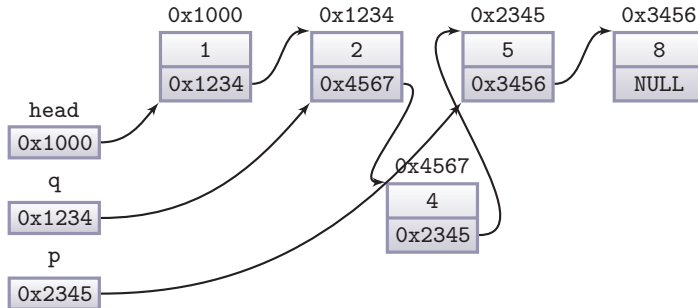


# Inserting element (4) into a sorted list

```

1  q = head;  p = q->next;
2  while (p != NULL && p->data <= data) { /* shortcut */
3      q = p;  p = p->next;
4  }
5  q->next = (listelem*)malloc(sizeof(listelem));
6  q->next->data = 4;
7  q->next->next = p;

```



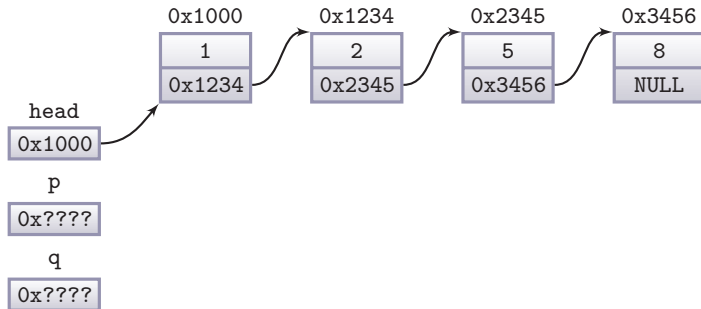
# Inserting element into a sorted list with a function

```
1 listelem *insert_sorted(listelem *head, int d)
2 {
3     listelem *p, *q;
4
5     if (head == NULL || head->data > d) /* shortcut */
6         return push_front(head, d);
7
8     q = head;
9     p = q->next;
10    while (p != NULL && p->data <= d) /* shortcut */ {
11        q = p; p = p->next;
12    }
13    q->next = (listelem*)malloc(sizeof(listelem));
14    q->next->data = d;
15    q->next->next = p;
16    return head;
17 }
```

[link](#)

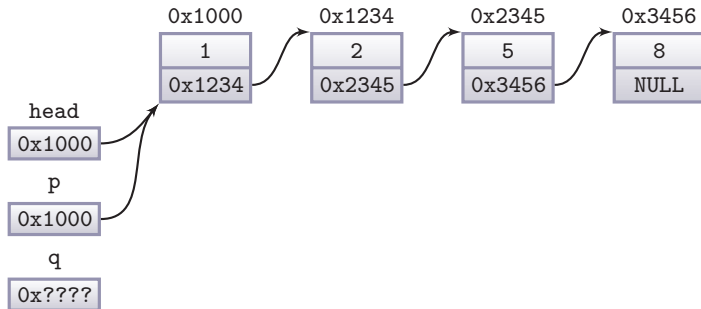
## Inserting element (4) into a sorted list by replacement

- The delayed pointer can be saved (omitted), if we insert behind the selected element, and after that we replace the data.



## Inserting element (4) into a sorted list by replacement

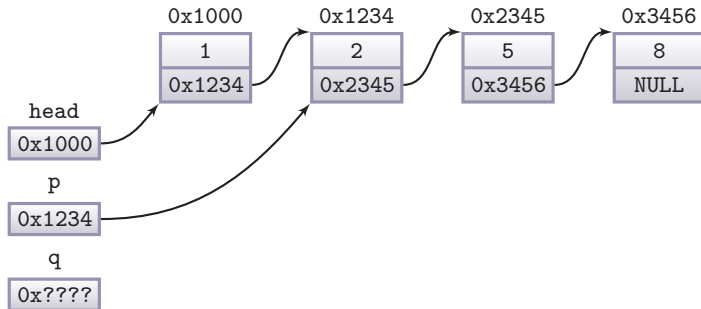
- The delayed pointer can be saved (omitted), if we insert behind the selected element, and after that we replace the data.





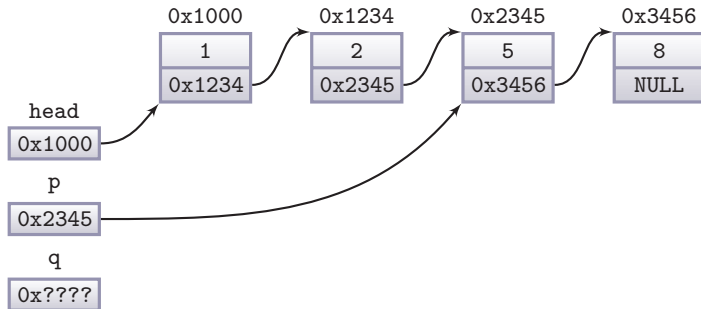
## Inserting element (4) into a sorted list by replacement

- The delayed pointer can be saved (omitted), if we insert behind the selected element, and after that we replace the data.



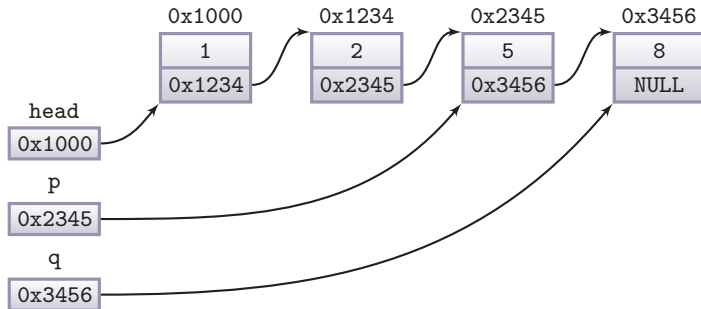
# Inserting element (4) into a sorted list by replacement

- The delayed pointer can be saved (omitted), if we insert behind the selected element, and after that we replace the data.



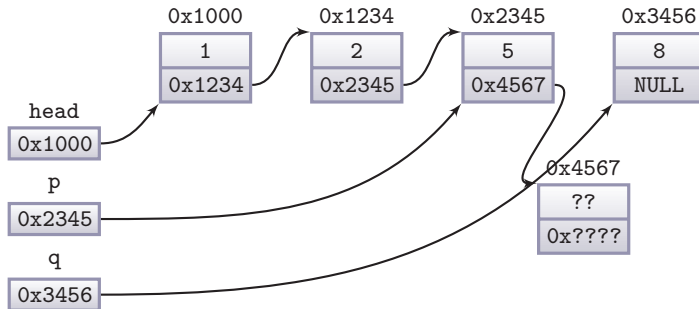
# Inserting element (4) into a sorted list by replacement

- The delayed pointer can be saved (omitted), if we insert behind the selected element, and after that we replace the data.



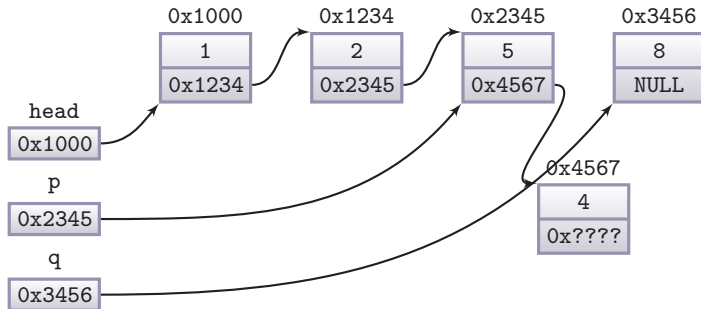
## Inserting element (4) into a sorted list by replacement

- The delayed pointer can be saved (omitted), if we insert behind the selected element, and after that we replace the data.



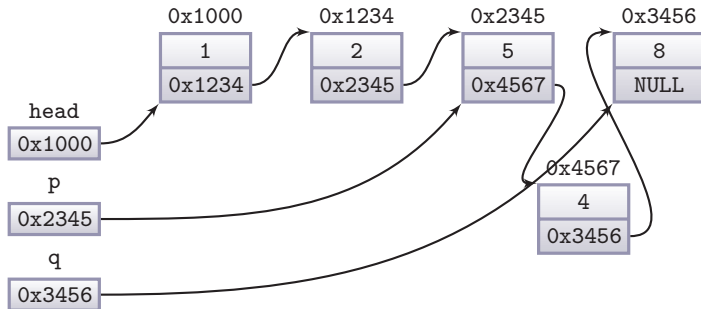
## Inserting element (4) into a sorted list by replacement

- The delayed pointer can be saved (omitted), if we insert behind the selected element, and after that we replace the data.



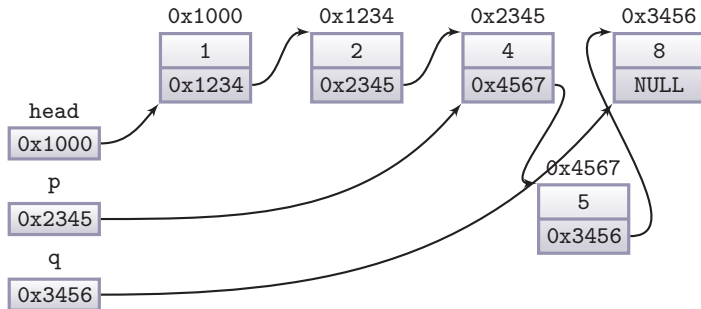
## Inserting element (4) into a sorted list by replacement

- The delayed pointer can be saved (omitted), if we insert behind the selected element, and after that we replace the data.



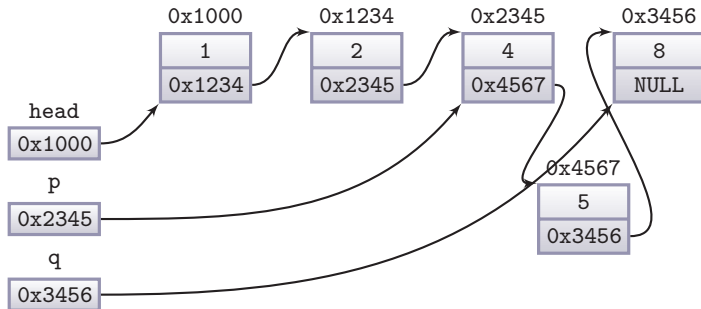
## Inserting element (4) into a sorted list by replacement

- The delayed pointer can be saved (omitted), if we insert behind the selected element, and after that we replace the data.



# Inserting element (4) into a sorted list by replacement

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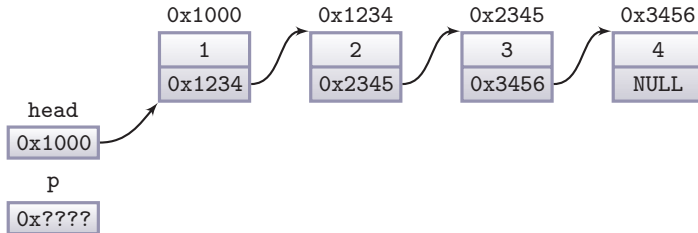


- This algorithm can be used only if we may modify the existing part of the list – others do not refer to it. But in many times this is not like that!



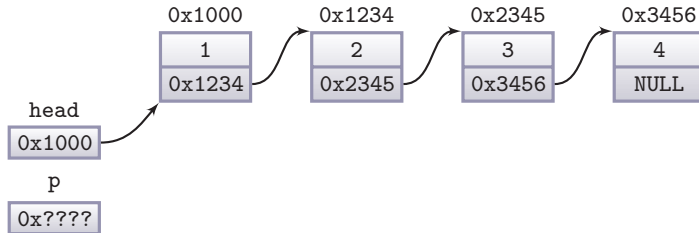
# Deleting element from the end of the list

```
1 p = head;
2 while (p->next->next != NULL)
3     p = p->next;
4 free(p->next);
5 p->next = NULL;
```



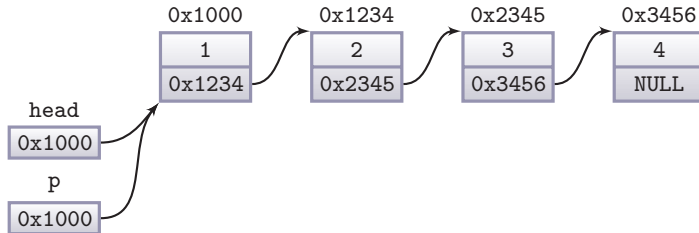
# Deleting element from the end of the list

```
1 p = head;  
2 while (p->next->next != NULL)  
3     p = p->next;  
4 free(p->next);  
5 p->next = NULL;
```



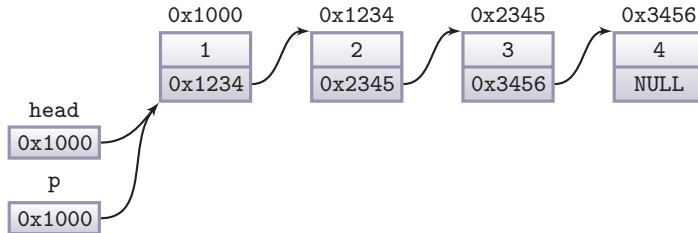
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```
1 p = head;  
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3     p = p->next;  
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5 p->next = NULL;
```



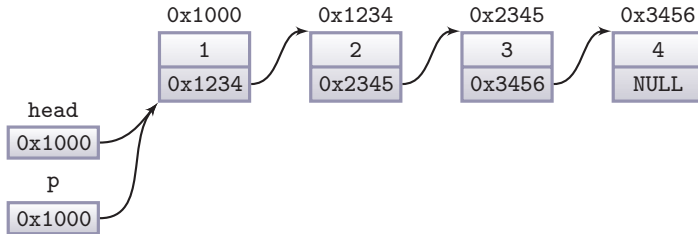
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```
1 p = head;  
2 while (p->next->next != NULL)  
3     p = p->next;  
4 free(p->next);  
5 p->next = NULL;
```



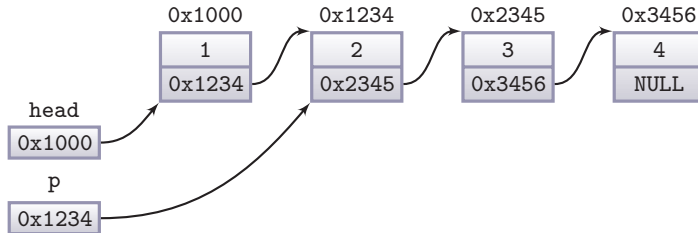
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```
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2 while (p->next->next != NULL)  
3     p = p->next;  
4 free(p->next);  
5 p->next = NULL;
```



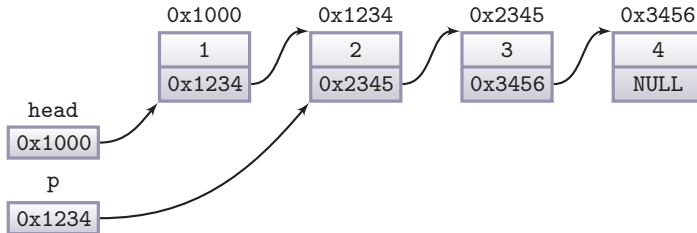
# Deleting element from the end of the list

```
1 p = head;  
2 while (p->next->next != NULL)  
3     p = p->next;  
4 free(p->next);  
5 p->next = NULL;
```



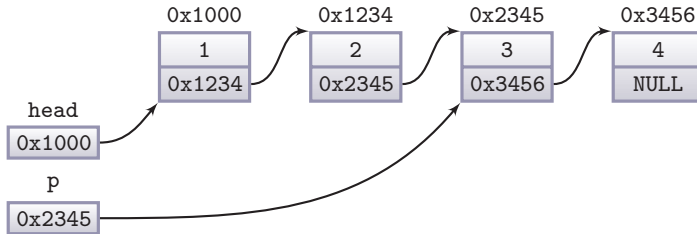
# Deleting element from the end of the list

```
1 p = head;  
2 while (p->next->next != NULL)  
3     p = p->next;  
4 free(p->next);  
5 p->next = NULL;
```



# Deleting element from the end of the list

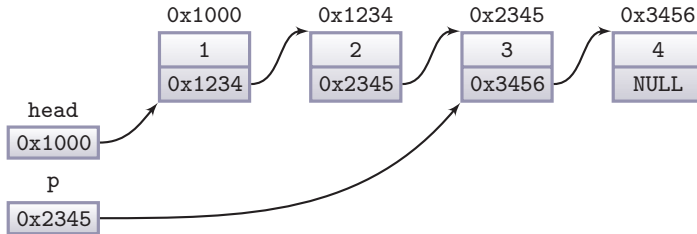
```
1 p = head;  
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3     p = p->next;  
4 free(p->next);  
5 p->next = NULL;
```





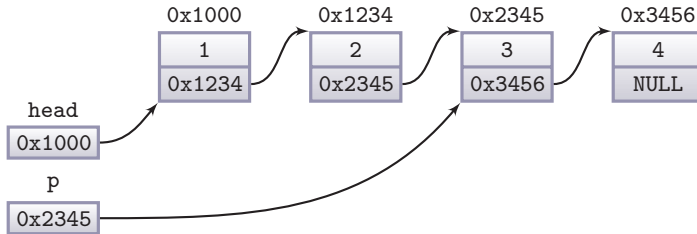
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3     p = p->next;  
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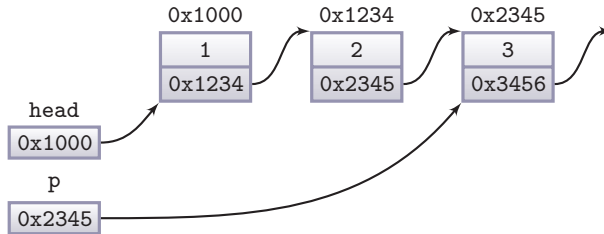
# Deleting element from the end of the list

```
1 p = head;  
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3     p = p->next;  
4     free(p->next);  
5     p->next = NULL;
```



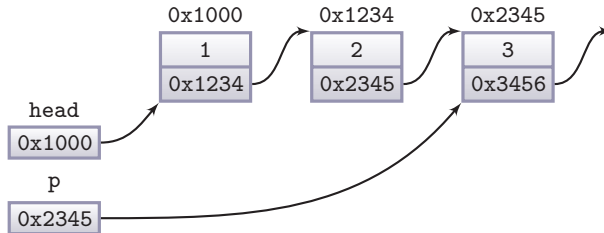
# Deleting element from the end of the list

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1 p = head;  
2 while (p->next->next != NULL)  
3     p = p->next;  
4     free(p->next);  
5     p->next = NULL;
```



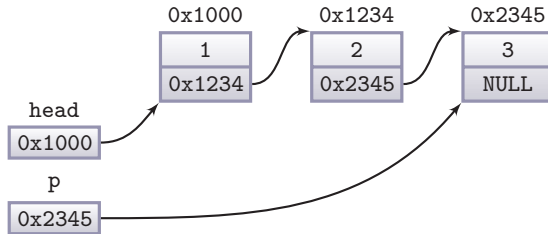
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3     p = p->next;  
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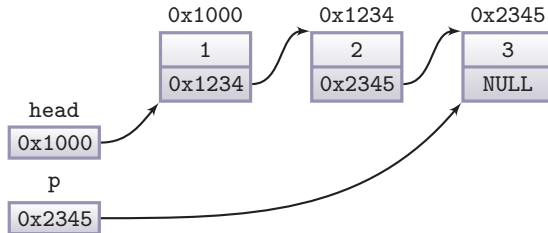
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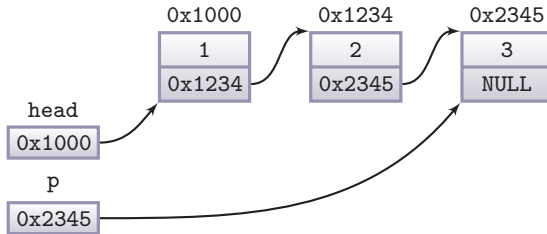
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```



# Deleting element from the end of the list

```
1 p = head;  
2 while (p->next->next != NULL)  
3     p = p->next;  
4 free(p->next);  
5 p->next = NULL;
```



- If the list is empty or it contains only one element, the expression `p->next->next` doesn't make any sense.

# Deleting element from the end of the list with a

```
1 listelem *pop_back(listelem *head)
2 {
3     listelem *p;
4
5     if (head == NULL ) /* empty */
6         return head;
7
8     if (head->next == NULL) /* only one element */
9         return pop_front(head);
10
11     for (p = head; p->next->next != NULL; p = p->next);
12     free(p->next);
13     p->next = NULL;
14     return head;
15 }
```

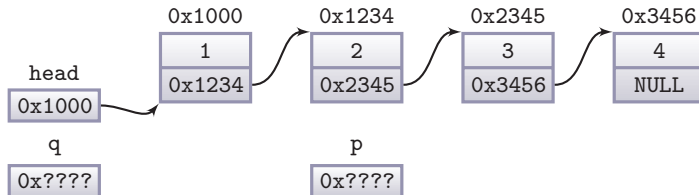
[link](#)



# Deleting a given element from list

## ■ Deleting the data = 3 element

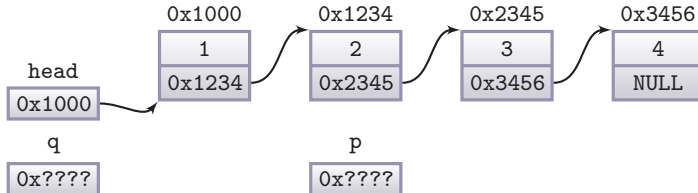
```
1 q = head; p = head->next;
2 while (p != NULL && p->data != data) {
3     q = p; p = p->next;
4 }
5 if (p != NULL) { /* now we have it */
6     q->next = p->next;
7     free(p);
8 }
```



# Deleting a given element from list

## ■ Deleting the data = 3 element

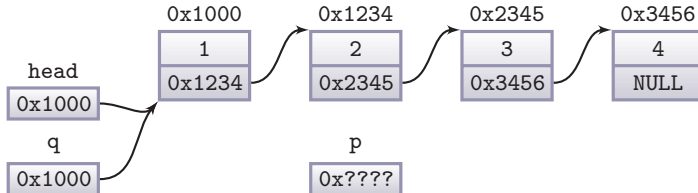
```
1 q = head; p = head->next;
2 while (p != NULL && p->data != data) {
3     q = p; p = p->next;
4 }
5 if (p != NULL) { /* now we have it */
6     q->next = p->next;
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```



# Deleting a given element from list

## ■ Deleting the data = 3 element

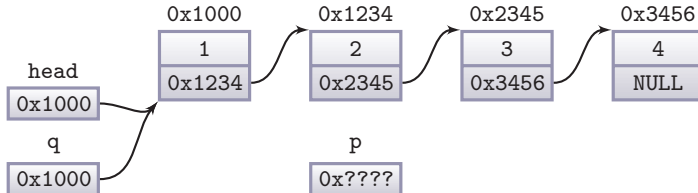
```
1 q = head; p = head->next;
2 while (p != NULL && p->data != data) {
3     q = p; p = p->next;
4 }
5 if (p != NULL) { /* now we have it */
6     q->next = p->next;
7     free(p);
8 }
```



# Deleting a given element from list

## ■ Deleting the data = 3 element

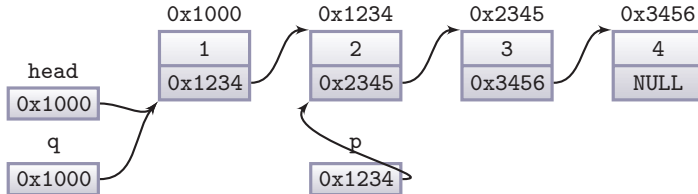
```
1 q = head; p = head->next;  
2 while (p != NULL && p->data != data) {  
3     q = p; p = p->next;  
4 }  
5 if (p != NULL) { /* now we have it */  
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8 }
```



# Deleting a given element from list

## ■ Deleting the data = 3 element

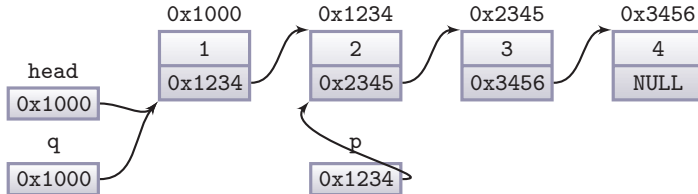
```
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3     q = p; p = p->next;  
4 }  
5 if (p != NULL) { /* now we have it */  
6     q->next = p->next;  
7     free(p);  
8 }
```



# Deleting a given element from list

## ■ Deleting the data = 3 element

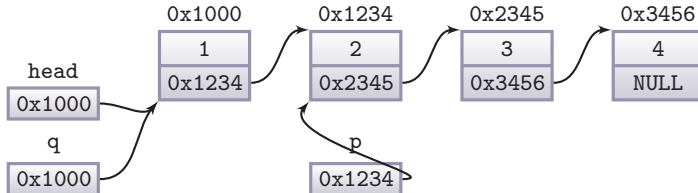
```
1 q = head; p = head->next;
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4 }
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# Deleting a given element from list

## ■ Deleting the data = 3 element

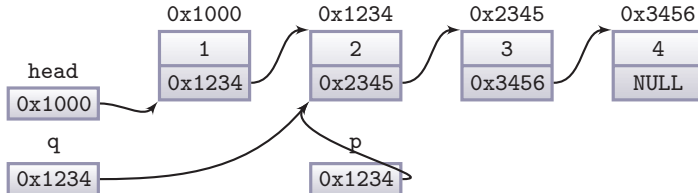
```
1 q = head; p = head->next;
2 while (p != NULL && p->data != data) {
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```



# Deleting a given element from list

## ■ Deleting the data = 3 element

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2 while (p != NULL && p->data != data) {
3     q = p; p = p->next;
4 }
5 if (p != NULL) { /* now we have it */
6     q->next = p->next;
7     free(p);
8 }
```

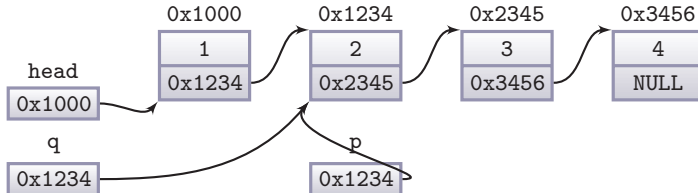




# Deleting a given element from list

## ■ Deleting the data = 3 element

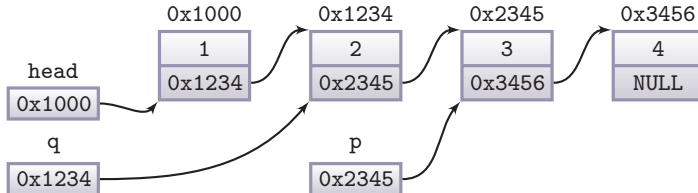
```
1 q = head; p = head->next;
2 while (p != NULL && p->data != data) {
3     q = p; p = p->next;
4 }
5 if (p != NULL) { /* now we have it */
6     q->next = p->next;
7     free(p);
8 }
```



# Deleting a given element from list

## ■ Deleting the data = 3 element

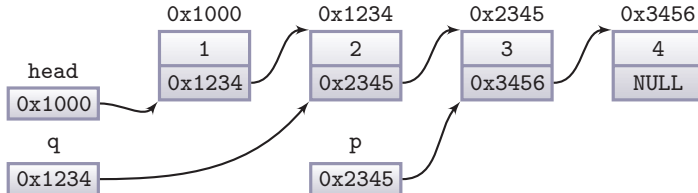
```
1 q = head; p = head->next;
2 while (p != NULL && p->data != data) {
3     q = p; p = p->next;
4 }
5 if (p != NULL) { /* now we have it */
6     q->next = p->next;
7     free(p);
8 }
```



# Deleting a given element from list

## ■ Deleting the data = 3 element

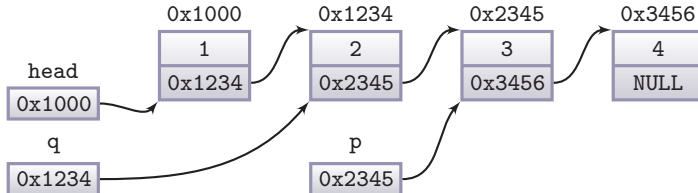
```
1 q = head; p = head->next;
2 while (p != NULL && p->data != data) {
3     q = p; p = p->next;
4 }
5 if (p != NULL) { /* now we have it */
6     q->next = p->next;
7     free(p);
8 }
```



# Deleting a given element from list

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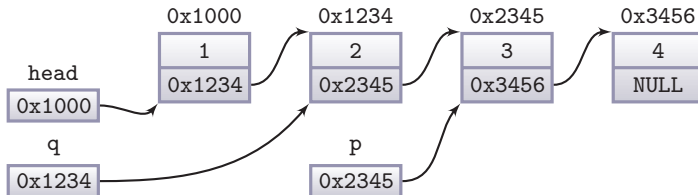
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1 q = head; p = head->next;
2 while (p != NULL && p->data != data) {
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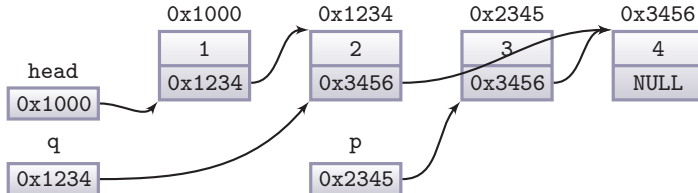
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3     q = p; p = p->next;
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# Deleting a given element from list

## ■ Deleting the data = 3 element

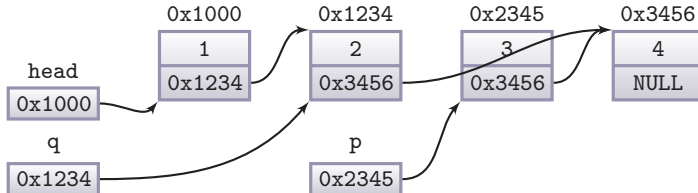
```
1 q = head; p = head->next;
2 while (p != NULL && p->data != data) {
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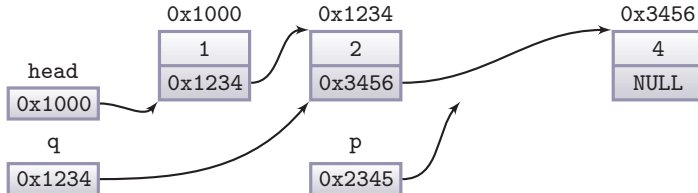
```
1 q = head; p = head->next;
2 while (p != NULL && p->data != data) {
3     q = p; p = p->next;
4 }
5 if (p != NULL) { /* now we have it */
6     q->next = p->next;
7     free(p);
8 }
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# Deleting a given element from list

## ■ Deleting the data = 3 element

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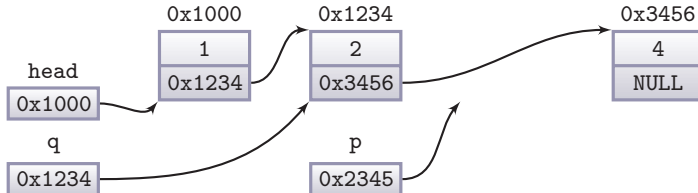




# Deleting a given element from list

## ■ Deleting the data = 3 element

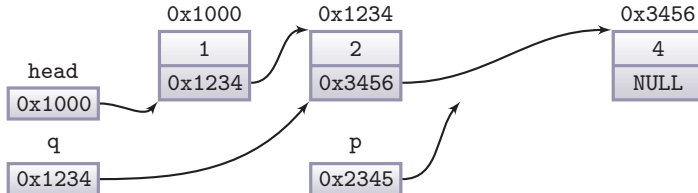
```
1 q = head; p = head->next;
2 while (p != NULL && p->data != data) {
3     q = p; p = p->next;
4 }
5 if (p != NULL) { /* now we have it */
6     q->next = p->next;
7     free(p);
8 }
```



# Deleting a given element from list

## ■ Deleting the data = 3 element

```
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2 while (p != NULL && p->data != data) {
3     q = p; p = p->next;
4 }
5 if (p != NULL) { /* now we have it */
6     q->next = p->next;
7     free(p);
8 }
```



## ■ If the list is empty, or we have to delete the first element, this does not work

# Deleting a given element from list

```
1 listelem *delete_elem(listelem *head, int d)
2 {
3     listelem *p = head;
4
5     if (head == NULL) return head;
6
7     if (head->data == d) return pop_front(head);
8
9     while (p->next != NULL && p->next->data != d)
10         p = p->next;
11     if (p->next != NULL)
12     {
13         listelem *q = p->next;
14         p->next = q->next;
15         free(q);
16     }
17     return head;
18 }
```

[link](#)

# Deleting an entire list

```
1 void dispose_list(listelem *head)
2 {
3     while (head != NULL)
4         head = pop_front(head);
5 }
```

[link](#)

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- We have everything we need, but it was really cumbersome, because
  - we can insert element only after (behind) an element
  - we can delete only an element behind another element
  - empty lists and lists with only one element must be handled separately when inserting or deleting



Thank you for your attention.