## Homework 1

## MLE, MAP ESTIMATES; LINEAR AND LOGISTIC REGRESSION

CMU 10-701: MACHINE LEARNING (SPRING 2017)

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### Part A: Multiple Choice Questions

- 1. For each case listed below, what type of machine learning problem does it belong to?
  - (a) Advertisement selection system, which can predict the probability whether a customer will click on an ad or not based on the search history.

Answer:

(b) U.S post offices use a system to automatically recognize handwriting on the envelope.

Answer:

(c) Reduce dimensionality using principal components analysis (PCA).

Answer:

(d) Trading companies try to predict future stock market based on current market conditions.

Answer:

(e) Repair a digital image that has been partially damaged.

Answer:

Type of machine learning problem:

- A. Supervised learning: Classification
- B. Supervised learning: Regression
- C. Unsupervised learning
- 2. For four statements below, which one is wrong?
  - A. In maximum a posterior (MAP) estimate, data overwhelms the prior if we have enough data.
  - B. There are no parameters in non-parameter models.
  - C.  $P(X \cap Y \cap Z) = P(Z|X \cap Y)P(Y|X)P(X)$ .
  - D. Compared with parametric models, non-parameter models are flexible, since they don't make strong assumptions.

#### Answer:

3. There are about 12% people in U.S. having breast cancer during ehir lifetime. One patient has a positive result for the medical test. Suppose the sensitivity of this test is 90%, meaning the test will be positive with probability 0.9 if one really has cancer. The false positive is likely to be 2%. Then what is the probability this patient actually having cancer based on Bayes Theorem?

A. 90%

B. 61%

C. 38%

D. 11%

#### Answer:

4. What is the most suitable error function for gradient descent using logistic regression?

- A. The negative log-likelihood function
- B. The number of mistakes
- C. The squared error
- D. The log-likelihood function

#### Answer:

## Part B, Problem 1: Bias-Variance Decomposition

Consider a p-dimensional vector  $\vec{x} \in \mathbb{R}^p$  drawn from a Gaussian distribution with an identity covariance matrix  $\Sigma = I_p$  and an unknown mean  $\vec{\mu}$ , i.e.  $\vec{x} \sim \mathcal{N}(\vec{\mu}, I_p)$ . Our goal is to evaluate the effectiveness of an estimator  $\hat{\vec{\mu}} = f(\vec{x})$  of the mean from only a single sample (i.e. n = 1) by measuring its mean squared error  $\mathbb{E}[||\hat{\vec{\mu}} - \vec{\mu}||^2]$ , where  $||\cdot||^2$  is the squared Euclidean norm and the expectation is taken over the data generating distribution.

Note that for any estimator  $\hat{\vec{\theta}}$  of a parameter vector  $\vec{\theta}$ , its mean squared error can be decomposed as:

$$\mathbb{E}[||\hat{\vec{\theta}} - \vec{\theta}||^2]$$

## Part B, Problem 2: Linear Regression

## Part B, Problem 3: MLE, MAP and Logistic Regression

# Part B, Problem 3: Programming Exercise