

Task_3:

1)

a) As binary classification function is used there is only one output 0 or 1
zero for the negative classes and one for the positive classes

The first input points:

$$\text{Output} = W1.X1 + W2.X2 + b = 2 * 2 + -1 * 4 + 0.5 = 0.5$$

$$\therefore 0.5 > 0$$

\therefore The class label =1

The second input points:

$$\text{Output} = W1.X1 + W2.X2 + b = 2 * 4 + -1 * 2 + 0.5 = 6.5$$

$$\therefore 6.5 > 0$$

\therefore The class label =1

The third input points:

$$\text{Output} = W1.X1 + W2.X2 + b = 2 * 2 + -1 * 2 + 0.5 = 2.5 > 0$$

$$\therefore 2.5 > 0$$

\therefore The class label =1

b) To find the decision boundary we need to equal the equation to zero

$$W1.X1 + W2.X2 + b = 0$$

$$2.X1 + -1.X2 + 0.5 = 0$$

$$X2 = 2.X1 + 0.5$$

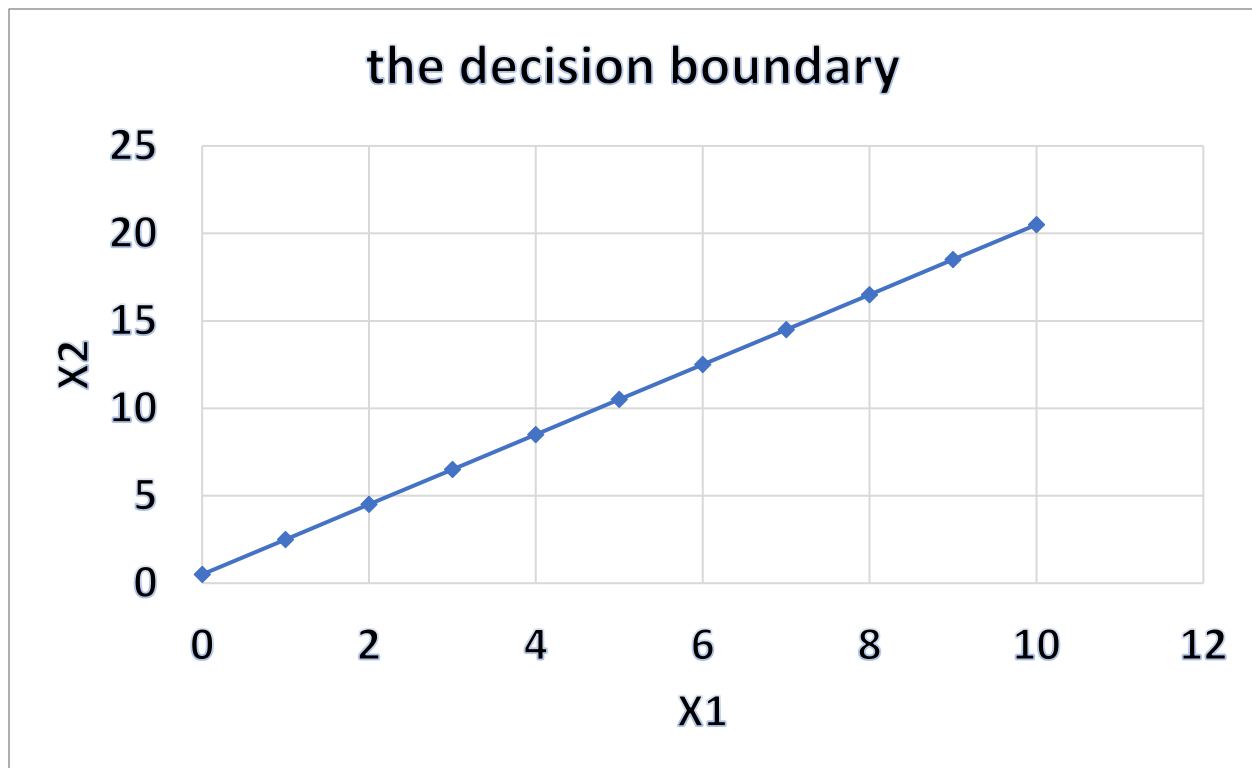


Figure 1.1

c) the limitations of the perceptron algorithm:

1. Only works with linearly separable data
2. Limited to binary classification
3. It is a single layer algorithm which can not model complex functions as it lacks hidden layers

2)

a)

Input layer: 4 neurons

Output layer: 2 neurons

Hidden layers: 12 neurons

Total neurons = 18

b) 4 hidden layers

c)

Learnable Parameters:

1. From input layer to the first hidden layer

Total for this layer = input layer neurons * first hidden layer neurons + first hidden layer neurons

$$= 4 * 2 + 2 = 10$$

2. From first hidden layer to second hidden layer

$$\text{Total for this layer} = 2 * 4 + 4 = 12$$

3. From second hidden layer to third hidden layer

$$\text{Total for this layer} = 4 * 2 + 2 = 10$$

4. From third hidden layer to fourth hidden layer

$$\text{Total for this layer} = 4 * 2 + 4 = 12$$

5. From fourth hidden layer to output layer

$$\text{Total for this layer} = 4 * 2 + 2 = 10$$

$$\text{Total learnable parameters} = 54$$

3)

The padded array = [0, 3, 4, 6, 3, 2, 3, 4, 0]

The filter = [1, 2, -1]

$$\text{Output_1} = 1 * 0 + 2 * 3 + -1 * 4 = 2$$

$$\text{Output_2} = 1 * 3 + 2 * 4 + -1 * 6 = 5$$

$$\text{Output_3} = 1 * 4 + 2 * 6 + -1 * 3 = 13$$

$$\text{Output_4} = 1 * 6 + 2 * 3 + -1 * 2 = 10$$

$$\text{Output_5} = 1 * 3 + 2 * 2 + -1 * 3 = 4$$

$$\text{Output_6} = 1 * 2 + 2 * 3 + -1 * 4 = 4$$

$$\text{Output_7} = 1 * 3 + 2 * 4 + -1 * 0 = 11$$

The convolved array = [2, 5, 13, 10, 4, 4, 11]

4)

The expected output length = $[(L(\text{in}) + 2P - K)/S] + 1$

K: Kernel or filter size, $K = F$

P: convolution padding size, $P = 0$

S: convolution stride, Assume $S = 1$

➤ So, the formula without padding: $L(\text{out}) = L(\text{in}) - F + 1$

The filter here can overlap with the input array when there are enough elements in the input array

➤ By adding padding into the input array for maintaining a constant output size and making the input size equals to the output size

$$L(\text{out}) = L(\text{in})$$

$$L(\text{in}) + 2P - F + 1 = L(\text{in})$$

$$P = 0.5(F - 1)$$

By providing an example

Assume $L(\text{in}) = 6$ & $F = 3$

$$P = 0.5(3 - 1) = 1 \text{ (one element of padding on each side)}$$

$$L(\text{out}) = 6 + 2(1) - 3 + 1 = 6$$

5)

By letting stride = 1

8	19	1
13	1	16
-10	28	20

6)

Alex Net has 5 convolution layers and 3 fully connected layers as shown in the figure below:

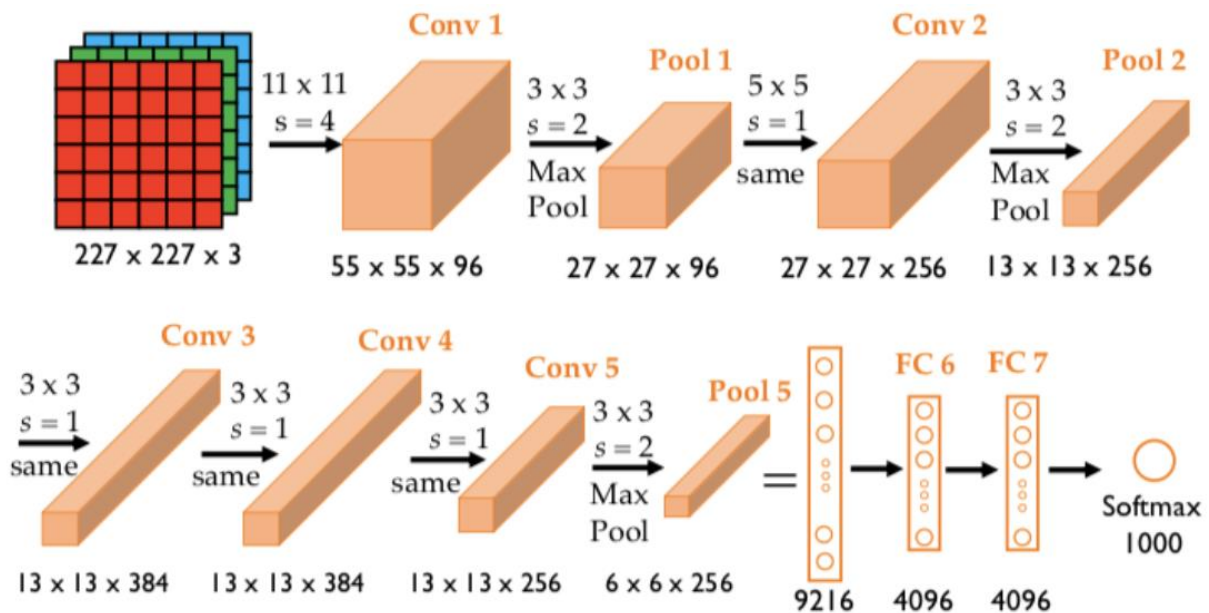


Figure 6.1

Input image shape: 512x512x3

Parameters = (filter width×filter height×number of input channels+1)
×number of Filters

Number of parameters of Conv1 = $(11 * 11 * 96 * 3 + 1) * 96 = 34,944$

Pool1

Number of parameters of Conv2 = $(5 * 5 * 96 + 1) * 256 = 614,656$

Pool2

Number of parameters of Conv3 = $(3 * 3 * 256 + 1) * 384 = 885,120$

Number of parameters of Conv4 = $(3 * 3 * 384 + 1) * 384 = 1,327,488$

Number of parameters of Conv5 = $(3 * 3 * 384 + 1) * 256 = 884,992$

Pool3

Number of parameters of neurons = 4096

Number of parameters of Fully connected layer1 = $(13 * 13 * 256 + 1) * 4096$

$$= 177,213,440$$

$$\text{Number of parameters of neurons} = 4096$$

$$\text{Number of parameters of Fully connected layer2} = (4096+1) * 4096 = 16,781,312$$

$$\text{Number of parameters of neurons} = 1000$$

$$\text{Number of parameters of Fully connected layer3} = (4096+1) * 1000 = 4,097,000$$

$$\begin{aligned} \text{Total parameters} = & 34,944 + 614,656 + 885,120 + 1,327,488 + 884,992 + \\ & 177,213,440 + 16,781,312 + 4,097,000 \end{aligned}$$