Compiling from F_i^+ to JavaScript

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Syntax of F_i^+

Types
$$A,B,C ::= \top \mid \bot \mid \mathbb{Z} \mid X \mid A \rightarrow B \mid \forall X*A. \ B \mid \{\ell:A\} \mid A \& B$$
 Expressions
$$e ::= \{\} \mid n \mid x \mid \mathbf{fix} \ x:A. \ e \mid \lambda x:A. \ e:B \mid e_1 \ e_2 \mid \Lambda X*A. \ e:B \mid e \ A$$

$$\mid \{\ell = e\} \mid e.\ell \mid e_1 \ , e_2 \mid e:A$$
 Type indices
$$T ::= \mathbb{Z} \mid \overrightarrow{T} \mid T^{\forall} \mid \{\ell:T\} \mid T_1 \& T_2$$
 JavaScript code
$$J ::= \varnothing \mid J_1; J_2 \mid \mathsf{code}$$
 Destinations
$$dst ::= \mathbf{nil} \mid y? \mid z$$

$\boxed{\Gamma; dst \vdash e \Leftrightarrow A \leadsto J \mid z}$

(Type-directed compilation)

```
J-Rcd
                                                                                                    J-Proj
                                                                                       \Gamma; \mathbf{nid} \vdash e \Rightarrow A \leadsto J_1 \mid y
\underline{y : A \bullet \{\ell\}} \leadsto J_2 \mid z : B
\overline{\Gamma; z \vdash e.\ell} \Rightarrow B \leadsto J_1; J_2 \mid z
                     \frac{\Gamma : |A|}{\Gamma ; \mathbf{nil} \vdash e \Rightarrow A \leadsto J \mid y}
\frac{\Gamma ; \mathbf{ril} \vdash e \Rightarrow A \leadsto J \mid y}{\Gamma ; z \vdash \{\ell = e\} \Rightarrow \{\ell : A\} \leadsto \mathsf{code} \mid z}
                                        T = \{\ell : |A|\}
                      J-Merge
                               \begin{array}{l} \Gamma;z\vdash e_1 \,\Rightarrow\, A \,\leadsto\, J_1\mid z \\ \Gamma;z\vdash e_2 \,\Rightarrow\, B \,\leadsto\, J_2\mid z \end{array}
                                                                                                  J-Anno
                                                                                \frac{\Gamma; dst \vdash e \Leftarrow A \leadsto J \mid z}{\Gamma; dst \vdash e : A \Rightarrow A \leadsto J \mid z}
                       \frac{\Gamma \vdash A * B}{\Gamma; z \vdash e_1, e_2 \Rightarrow A \& B \leadsto J_1; J_2 \mid z}
    J-Def
    /* J-VarOpt */
/* J-Nil */
                                                                                                                  z[T] = (X, y) => {
var z = {};
                                                        var z = x;
                                                                                                                   J; return y0;
                                                         copy(y, x);
J;
                                                                                                                  };
/* J-Opt */
                                                        /* J-Fix */
                                                                                                                 /* J-Rcd */
var z = y || {};
                                                                                                                  z.__defineGetter__(T, () => {
                                                        var x = z;
                                                                                                                     delete this[T];
/* J-Int */
                                                        /* J-Abs */
                                                                                                                     return this[T] = y;
                                                         z[T] = (x, y) \Rightarrow \{
z[T] = n;
                                                                                                                  });
                                                         J; return y0;
/* J-Var */
                                                                                                                  /* J-Def */
copy(z, x);
                                                                                                                  export var x = \{\};
                                                        /* J-TAbs */
                                                                                                                  J1; J2;
```

Copying properties n.b. there seems to be some alternatives:

- Object.assign(dst, src) does not properly copy getters;
- Object.defineProperties(dst, Object.getOwnPropertyDescriptors(src)) is proper but slow;
- Object.setPrototypeOf(dst, src) does the prototype trick but is even slower.

```
function copy(dst, src) {
  if (dst === undefined) return;
  for (const prop in src) {
    var getter = src.__lookupGetter__(prop);
    if (getter) dst.__defineGetter__(prop, getter);
    else dst[prop] = src[prop];
  }
}
```

$$\boxed{\Gamma; dst \vdash x : A \bullet p \leadsto J \mid z : B}$$

(Distributive application)

A-NIL
$$\Gamma; z \vdash x : A \bullet p \leadsto J \mid z : B$$

$$\Gamma: \mathbf{nil} \vdash x : A \bullet p \Longrightarrow \mathbf{code} \mid z : B$$

A-TOP
$$\frac{|A|}{\Gamma: z \vdash x : A \bullet p \rightsquigarrow \varnothing |z:}$$

A-Arrow

$$T = |\overrightarrow{B}|$$

$$y : C <:^{+} y_{0} : A \leadsto J_{1}$$

$$\Gamma; dst \vdash x : A \to B \bullet y_{0} : A \leadsto J_{2} \mid z : B$$

$$\Gamma; dst \vdash x : A \to B \bullet y : C \leadsto \mathsf{code} \mid z : B$$

$$\frac{A = C \qquad T = |B|}{\Gamma; z_0? \vdash x : A \to B \bullet y : C \leadsto \mathsf{code} \mid z : B}$$

A-All

$$\frac{\Gamma \vdash A * C}{T = |B|^{\forall} \quad Ts = \mathbf{itoa} \mid C \mid}$$
$$\Gamma; z \vdash x : \forall X * A. B \bullet C \leadsto \mathsf{code} \mid z : B[X \mapsto C]$$

A-Allnil

A-Allnil
$$\Gamma \vdash A * C$$

$$T = |B|^{\forall} \quad Ts = \mathbf{itoa} \mid C \mid$$

$$\Gamma; \mathbf{nil} \vdash x : \forall X * A. B \bullet C \implies \mathsf{code} \mid z : B[X \mapsto C]$$

$$\Gamma; \mathbf{z} \vdash x : A \bullet p \implies J_1 \mid z : A'$$

$$\Gamma; z \vdash x : B \bullet p \implies J_2 \mid z : B'$$

$$\Gamma; z \vdash x : A \& B \bullet p \implies J_1; J_2 \mid z : A' \& B'$$

$$\cfrac{A\text{-}\mathsf{ArrowEquiv}}{A = C \qquad T = |\overrightarrow{B}|}$$

$$\cfrac{\Gamma; z \vdash x : A \to B \bullet y : C \leadsto \mathsf{code} \mid z : B}$$

A-ArrowNil

$$A = C \qquad T = |\overrightarrow{B}| \qquad \qquad A = C \qquad T = |\overrightarrow{B}|$$

$$\Gamma; z_0? \vdash x : A \to B \bullet y : C \leadsto \mathsf{code} \mid z : B \qquad \qquad \Gamma; \mathsf{nil} \vdash x : A \to B \bullet y : C \leadsto \mathsf{code} \mid z : B$$

$$\frac{\Gamma; z \vdash x : A \bullet p \leadsto J_1 \mid z : A'}{\Gamma; z \vdash x : B \bullet p \leadsto J_2 \mid z : B'}$$

$$\frac{\Gamma; z \vdash x : A \& B \bullet p \leadsto J_1; J_2 \mid z : A' \& B'}{\Gamma; z \vdash x : A \& B \bullet p \leadsto J_1; J_2 \mid z : A' \& B'}$$

/* A-All */ x[T](Ts, z);

$$x:A \bullet \{\ell\} \leadsto J \mid z:B$$

(Distributive projection)

/* A-ArrowEquiv */

var z = x[T](y);

x[T](y, z);

$$\begin{array}{c|c} \text{P-TOP} & \text{P-RcdEq} \\ \hline 1A \lceil & T = \{\ell : |A|\} \\ \hline x : A \bullet \{\ell\} \leadsto \varnothing \mid z : \top \end{array} \begin{array}{c} \text{P-RcdEq} \\ \hline x : \{\ell : A\} \bullet \{\ell\} \leadsto \mathsf{code} \mid z : A \end{array} \begin{array}{c} \text{P-RcdNeq} \\ \hline \ell_1 \neq \ell_2 & T = \{\ell : |A|\} \\ \hline x : \{\ell_1 : A\} \bullet \{\ell_2\} \leadsto \varnothing \mid z : \top \end{array}$$

 $x: A \bullet \{\ell\} \leadsto J_1 \mid z: A'$ $x: B \bullet \{\ell\} \leadsto J_2 \mid z: B'$ $x: A \& B \bullet \{\ell\} \leadsto J_1; J_2 \mid z: A' \& B'$

```
x:A<:^{\pm}y:B\leadsto J
                                                                                                                                                                    (Coercive subtyping)
              S-Equiv
                                                                                                                                         T = |A|
                                                                                                                                           x: \bot <:^{\pm} y: A \leadsto \mathsf{code}
              \overline{x:A<:^+y:B} \leadsto \mathsf{code}
       S-Split
                          B_1 \triangleleft B \rhd B_2
       y_1:B_1 \vartriangleright z:B \vartriangleleft y_2:B_2 \leadsto J_3
        \begin{array}{c} x:A<:^{\pm}y_1:B_1\rightsquigarrow J_1\\ x:A<:^{\pm}y_2:B_2\rightsquigarrow J_2\\ \hline x:A<:^{\pm}z:B\rightsquigarrow \mathtt{code} \end{array}
                                                                          \frac{S\text{-Int}}{x:\mathbb{Z}<:^{\pm}\ y:\mathbb{Z}\ \leadsto\ \mathsf{code}} \qquad \frac{S\text{-Var}}{x:X<:^{\pm}\ y:X\ \leadsto\ \mathsf{code}}
             S-Arrow
                           T_1 = \overrightarrow{|A_2|} T_2 = \overrightarrow{|B_2|}
                                                                               S-All
            T_{1} = |A_{2}| \qquad T_{2} = |B_{2}| \qquad S-ALL
T_{3} = \mathbf{itoa} |A_{1}| \qquad T_{1} = |A_{2}|^{\forall}
x_{1} : B_{1} <:^{+} y_{1} : A_{1} \leadsto J_{1} \qquad T_{2} = |B_{2}|^{\forall} \quad B_{1} <: A_{1}
x_{2} : A_{2} <:^{+} y_{2} : B_{2} \leadsto J_{2} \qquad x_{0} : A_{2} <:^{+} y_{0} : B_{2} \leadsto J
x : A_{1} \to A_{2} <:^{\pm} y : B_{1} \to B_{2} \leadsto \mathbf{code}
T_{2} = |B_{2}|^{\forall} \quad B_{1} <: A_{1}
x_{0} : A_{2} <:^{+} y_{0} : B_{2} \leadsto J
x : \forall X * A_{1} . A_{2} <:^{\pm} y : \forall X * B_{1} . B_{2} \leadsto \mathbf{code}
    S-RCD
                         T_1 = \{\ell : |A|\}
    T_{2} = \{\ell : |B|\}  S-ANDL S-ANDR x_{0} : A <:^{+} y_{0} : B \leadsto J  x : \{\ell : A\} <:^{\pm} y : \{\ell : B\} \leadsto \mathsf{code}  S-ANDR x : A <:^{-} y : C \leadsto J  x : A \& B <:^{\pm} y : C \leadsto J  x : A \& B <:^{\pm} y : C \leadsto J 
/* S-Equiv */
                                                                                                                                          y[T2] = (X, y0) => {
                                                                    /* S-Var */
                                                                                                                                            var x0 = x[T1](X);
copy(y, x);
                                                                     copy(y, x);
                                                                                                                                              y0 = y0 || {};
/* S-Bot */
                                                                                                                                              J; return y0;
                                                                     /* S-Arrow */
y[T] = null;
                                                                                                                                          };
                                                                     y[T2] = (x1, y2) => {
                                                                     var y1 = {}; J1;
/* S-Split */
                                                                                                                                          /* S-Rcd */
                                                                   var x2 = x[T1](y1);
y2 = y2 || {};
var y1 = {}; // if y1 != z
                                                                                                                                          y.__defineGetter__(T2, () => {
var y2 = {}; // if y2 != z
                                                                                                                                           var x0 = x[T1];
```

J2; return y2;

/* S-All */

J1; J2; J3;

/* S-Int */

y[T] = x[T];

 $var y0 = {}; J;$

delete this[T];

});

return this[T] = y0;

```
x:A \vartriangleright z:C \vartriangleleft y:B \leadsto J
```

};

(Coercive merging)

```
M-Arrow
                                                                      T = |\overrightarrow{B}|
T_1 = |\overrightarrow{B_1}| \quad T_2 = |\overrightarrow{B_2}|
y_1 : B_1 \rhd y : B \vartriangleleft y_2 : B_2 \leadsto J
x_1 : A \to B_1 \rhd z : A \to B \vartriangleleft x_2 : A \to B_2 \leadsto \mathsf{code}
        M-And
         z:A \vartriangleright z:A \& B \vartriangleleft z:B \leadsto \varnothing
                                  M\text{-}ALL
                                                          T = |B|^{\forall}
T_1 = |B_1|^{\forall} \quad T_2 = |B_2|^{\forall}
                                                     y_1:B_1 \vartriangleright y:B \vartriangleleft y_2:B_2 \leadsto J
                                  \overline{x_1: \forall X*A.\ B_1\ \rhd\ z: \forall X*A.\ B\ \vartriangleleft\ x_2: \forall X*A.\ B_2\ \leadsto\ \mathsf{code}}
                                        M-Rcd
                                                                    T = \{\ell : |A|\}
                                                                  T_1 = \{\ell : |A_1|\}\

T_2 = \{\ell : |A_2|\}
                                       \frac{y_1:A_1 \vartriangleright y:A \vartriangleleft y_2:A_2 \leadsto J}{x_1:\{\ell:A_1\} \vartriangleright z:\{\ell:A\} \vartriangleleft x_2:\{\ell:A_2\} \leadsto \mathsf{code}}
                                                    /* M-All */
                                                                                                          /* M-Rcd */
/* M-Arrow */
z[T] = (p, y) => {
                                                     z[T] = (X, y) => \{
                                                                                                          z.__defineGetter__(T, () => {
   y = y || {};
                                                      y = y || {};
                                                                                                            var y = {};
   x1[T1](p, y1);
                                                     x1[T1](X, y1);
                                                                                                             copy(y1, x1[T1]);
   x2[T2](p, y2);
                                                       x2[T2](X, y2);
                                                                                                             copy(y2, x2[T2]);
   J; return y;
                                                        J; return y;
                                                                                                             J;
                                                     };
                                                                                                             delete this[T];
                                                                                                             return this[T] = y;
```

});