

# Compiling from $F_i^+$ to JavaScript

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## Syntax of $F_i^+$

Types	$A, B, C ::= \top \mid \perp \mid \mathbb{Z} \mid X \mid A \rightarrow B \mid \forall X * A. B \mid \{\ell : A\} \mid A \& B$
Expressions	$e ::= \{\} \mid n \mid x \mid \mathbf{fix} \ x : A. e \mid \lambda x : A. e : B \mid e_1 \ e_2 \mid \Lambda X * A. e : B \mid e \ A$ $\mid \{\ell = e\} \mid e.\ell \mid e_1, e_2 \mid e : A$
Type indices	$T ::= \mathbb{Z} \mid \vec{T} \mid T^\vee \mid \{\ell : T\} \mid T_1 \& T_2$
JavaScript code	$J ::= \emptyset \mid J_1; J_2 \mid \mathbf{code}$
Destinations	$dst ::= \mathbf{nil} \mid y? \mid z$

$$\boxed{\Gamma; dst \vdash e \Leftrightarrow A \rightsquigarrow J \mid z}$$

(Type-directed compilation)

$\frac{\text{J-NIL} \quad \Gamma; z \vdash e \Leftrightarrow A \rightsquigarrow J \mid z}{\Gamma; \mathbf{nil} \vdash e \Leftrightarrow A \rightsquigarrow \mathbf{code} \mid z}$	$\frac{\text{J-OPT} \quad \Gamma; z \vdash e \Leftrightarrow A \rightsquigarrow J \mid z}{\Gamma; y? \vdash e \Leftrightarrow A \rightsquigarrow \mathbf{code} \mid z}$	$\frac{\text{J-TOP}}{\Gamma; z \vdash \{\} \Rightarrow \top \rightsquigarrow \emptyset \mid z}$
$\frac{\text{J-TOPABS} \quad \overline{\phantom{A \rightarrow B \rightsquigarrow \emptyset \mid z}} \mid B[ \quad \Gamma; z \vdash \lambda x : A. e : B \Rightarrow A \rightarrow B \rightsquigarrow \emptyset \mid z$	$\frac{\text{J-TOPTABS} \quad \overline{\phantom{A \rightarrow B \rightsquigarrow \emptyset \mid z}} \mid B[ \quad \Gamma; z \vdash \Lambda X * A. e : B \Rightarrow \forall X * A. B \rightsquigarrow \emptyset \mid z$	
$\frac{\text{J-TOPRCD} \quad \Gamma \vdash e \Rightarrow A \quad \overline{\phantom{A \rightsquigarrow \emptyset \mid z}} \mid A[ \quad \Gamma; z \vdash \{\ell = e\} \Rightarrow \{\ell : A\} \rightsquigarrow \emptyset \mid z$	$\frac{\text{J-INT} \quad T =  \mathbb{Z}  \quad \overline{\phantom{A \rightsquigarrow \emptyset \mid z}} \quad \Gamma; z \vdash n \Rightarrow \mathbb{Z} \rightsquigarrow \mathbf{code} \mid z$	$\frac{\text{J-VAR} \quad x : A \in \Gamma}{\Gamma; z \vdash x \Rightarrow A \rightsquigarrow \mathbf{code} \mid z}$
$\frac{\text{J-VAROPT} \quad x : A \in \Gamma}{\Gamma; y? \vdash x \Rightarrow A \rightsquigarrow \mathbf{code} \mid z}$	$\frac{\text{J-VARNIL} \quad x : A \in \Gamma}{\Gamma; \mathbf{nil} \vdash x \Rightarrow A \rightsquigarrow \emptyset \mid x}$	$\frac{\text{J-FIX} \quad \Gamma, x : A; z \vdash e \Leftarrow A \rightsquigarrow J \mid z}{\Gamma; z \vdash \mathbf{fix} \ x : A. e \Rightarrow A \rightsquigarrow \mathbf{code} \mid z}$
$\frac{\text{J-ABS} \quad T = \overrightarrow{ B } \quad \Gamma, x : A; y? \vdash e \Leftarrow B \rightsquigarrow J \mid y_0}{\Gamma; z \vdash \lambda x : A. e : B \Rightarrow A \rightarrow B \rightsquigarrow \mathbf{code} \mid z}$	$\frac{\text{J-APP} \quad \Gamma; \mathbf{nil} \vdash e_1 \Rightarrow A \rightsquigarrow J_1 \mid x \quad \Gamma; \mathbf{nil} \vdash e_2 \Rightarrow B \rightsquigarrow J_2 \mid y \quad \Gamma; dst \vdash x : A \bullet y : B \rightsquigarrow J_3 \mid z : C}{\Gamma; dst \vdash e_1 \ e_2 \Rightarrow C \rightsquigarrow J_1; J_2; J_3 \mid z}$	
$\frac{\text{J-TABS} \quad T =  B ^\vee \quad \Gamma, X * A; y? \vdash e \Leftarrow B \rightsquigarrow J_2 \mid y_0}{\Gamma; z \vdash \Lambda X * A. e : B \Rightarrow \forall X * A. B \rightsquigarrow \mathbf{code} \mid z}$	$\frac{\text{J-TAPP} \quad \Gamma; \mathbf{nil} \vdash e \Rightarrow B \rightsquigarrow J_1 \mid y \quad \Gamma; dst \vdash y : B \bullet A \rightsquigarrow J_2 \mid z : C}{\Gamma; dst \vdash e \ A \Rightarrow C \rightsquigarrow J_1; J_2 \mid z}$	

$\text{J-RCD} \quad \frac{T = \{\ell :  A \} \quad \Gamma; \mathbf{nil} \vdash e \Rightarrow A \rightsquigarrow J \mid y}{\Gamma; z \vdash \{\ell = e\} \Rightarrow \{\ell : A\} \rightsquigarrow \mathbf{code} \mid z}$	$\text{J-PROJ} \quad \frac{\Gamma; \mathbf{nil} \vdash e \Rightarrow A \rightsquigarrow J_1 \mid y \quad y : A \bullet \{\ell\} \rightsquigarrow J_2 \mid z : B}{\Gamma; z \vdash e.\ell \Rightarrow B \rightsquigarrow J_1; J_2 \mid z}$	
$\text{J-MERGE} \quad \frac{\Gamma; z \vdash e_1 \Rightarrow A \rightsquigarrow J_1 \mid z \quad \Gamma; z \vdash e_2 \Rightarrow B \rightsquigarrow J_2 \mid z \quad \Gamma \vdash A * B}{\Gamma; z \vdash e_1, e_2 \Rightarrow A \& B \rightsquigarrow J_1; J_2 \mid z}$	$\text{J-ANNO} \quad \frac{\Gamma; dst \vdash e \Leftarrow A \rightsquigarrow J \mid z}{\Gamma; dst \vdash e : A \Rightarrow A \rightsquigarrow J \mid z}$	
$\text{J-DEF} \quad \frac{\Gamma; x \vdash e_1 \Rightarrow A \rightsquigarrow J_1 \mid x \quad \Gamma, x : A; z \vdash e_2 \Rightarrow B \rightsquigarrow J_2 \mid z}{\Gamma; z \vdash x = e_1; e_2 \Rightarrow B \rightsquigarrow \mathbf{code} \mid z}$	$\text{J-SUB} \quad \frac{\Gamma; \mathbf{nil} \vdash e \Rightarrow A \rightsquigarrow J_1 \mid x \quad x : A <^+ y : B \rightsquigarrow J_2}{\Gamma; y \vdash e \Leftarrow B \rightsquigarrow J_1; J_2 \mid y}$	$\text{J-SUBEQUIV} \quad \frac{A \doteq B \quad \Gamma; dst \vdash e \Rightarrow A \rightsquigarrow J \mid z}{\Gamma; dst \vdash e \Leftarrow B \rightsquigarrow J \mid z}$
<pre> /* J-Nil */ var z = {}; J;  /* J-Opt */ var z = y    {}; J;  /* J-Int */ z[T] = n;  /* J-Var */ copy(z, x); </pre>	<pre> /* J-VarOpt */ var z = x; if (y) copy(y, x);  /* J-Fix */ var x = z; J;  /* J-Abs */ z[T] = (x, y) =&gt; {   J; return y0; };  /* J-TAbs */ </pre>	<pre> z[T] = (X, y) =&gt; {   J; return y0; };  /* J-Rcd */ z.__defineGetter__(T, () =&gt; {   J;   delete this[T];   return this[T] = y; });  /* J-Def */ export var x = {}; J1; J2; </pre>

**Copying properties** n.b. there seems to be some alternatives:

- `Object.assign(dst, src)` does not properly copy getters;
- `Object.defineProperties(dst, Object.getOwnPropertyDescriptors(src))` is proper but slow;
- `Object.setPrototypeOf(dst, src)` does the prototype trick but is even slower.

```

function copy(dst, src) {
  for (const prop in src) {
    var getter = src.__lookupGetter__(prop);
    if (getter) dst.__defineGetter__(prop, getter);
    else dst[prop] = src[prop];
  }
}

```

$$\boxed{\Gamma; dst \vdash x : A \bullet p \rightsquigarrow J \mid z : B}$$

(Distributive application)

$$\frac{\text{A-NIL} \quad \Gamma; z \vdash x : A \bullet p \rightsquigarrow J \mid z : B}{\Gamma; \mathbf{nil} \vdash x : A \bullet p \rightsquigarrow \mathbf{code} \mid z : B}$$

$$\frac{\text{A-OPT} \quad \Gamma; z \vdash x : A \bullet p \rightsquigarrow J \mid z : B}{\Gamma; y? \vdash x : A \bullet p \rightsquigarrow \mathbf{code} \mid z : B}$$

$$\frac{\text{A-TOP} \quad \top A \top}{\Gamma; z \vdash x : A \bullet p \rightsquigarrow \emptyset \mid z : \top}$$

A-ARROW

$$\frac{\begin{array}{c} T = \overrightarrow{|B|} \\ y : C <:^+ y_0 : A \rightsquigarrow J_1 \\ \Gamma; dst \vdash x : A \rightarrow B \bullet y_0 : A \rightsquigarrow J_2 \mid z : B \end{array}}{\Gamma; dst \vdash x : A \rightarrow B \bullet y : C \rightsquigarrow \mathbf{code} \mid z : B}$$

A-ARROWEQUIV

$$\frac{A \models C \quad T = \overrightarrow{|B|}}{\Gamma; z \vdash x : A \rightarrow B \bullet y : C \rightsquigarrow \mathbf{code} \mid z : B}$$

A-ARROWOPT

$$\frac{A \models C \quad T = \overrightarrow{|B|}}{\Gamma; z_0? \vdash x : A \rightarrow B \bullet y : C \rightsquigarrow \mathbf{code} \mid z : B}$$

A-ARROWNIL

$$\frac{A \models C \quad T = \overrightarrow{|B|}}{\Gamma; \mathbf{nil} \vdash x : A \rightarrow B \bullet y : C \rightsquigarrow \mathbf{code} \mid z : B}$$

A-ALL

$$\frac{\begin{array}{c} \Gamma \vdash A * C \\ T = |B|^\forall \quad Ts = \mathbf{itoa} \mid C \end{array}}{\Gamma; z \vdash x : \forall X * A. B \bullet C \rightsquigarrow \mathbf{code} \mid z : B[X \mapsto C]}$$

A-ALLOPT

$$\frac{\begin{array}{c} \Gamma \vdash A * C \\ T = |B|^\forall \quad Ts = \mathbf{itoa} \mid C \end{array}}{\Gamma; y? \vdash x : \forall X * A. B \bullet C \rightsquigarrow \mathbf{code} \mid z : B[X \mapsto C]}$$

A-ALLNIL

$$\frac{\begin{array}{c} \Gamma \vdash A * C \\ T = |B|^\forall \quad Ts = \mathbf{itoa} \mid C \end{array}}{\Gamma; \mathbf{nil} \vdash x : \forall X * A. B \bullet C \rightsquigarrow \mathbf{code} \mid z : B[X \mapsto C]}$$

A-AND

$$\frac{\begin{array}{c} \Gamma; z \vdash x : A \bullet p \rightsquigarrow J_1 \mid z : A' \\ \Gamma; z \vdash x : B \bullet p \rightsquigarrow J_2 \mid z : B' \end{array}}{\Gamma; z \vdash x : A \& B \bullet p \rightsquigarrow J_1; J_2 \mid z : A' \& B'}$$

```
/* A-Nil */
var z = {};
J;
```

```
/* A-Opt */
var z = y || {};
J;
```

```
/* A-Arrow */
var y0 = {};
J1; J2;
```

```
/* A-ArrowEquiv */
x[T](y, z);
```

```
/* A-ArrowOpt */
var z = x[T](y, z0);
```

```
/* A-ArrowNil */
var z = x[T](y);
```

```
/* A-All */
x[T](Ts, z);
```

```
/* A-AllOpt */
var z = x[T](Ts, y);
```

```
/* A-All */
var z = x[T](Ts);
```

$$\boxed{x : A \bullet \{\ell\} \rightsquigarrow J \mid z : B}$$

(Distributive projection)

$$\frac{\text{P-TOP} \quad \top A \top}{x : A \bullet \{\ell\} \rightsquigarrow \emptyset \mid z : \top}$$

$$\frac{\text{P-RCD EQ} \quad T = \{\ell : |A|\}}{x : \{\ell : A\} \bullet \{\ell\} \rightsquigarrow \mathbf{code} \mid z : A}$$

$$\frac{\text{P-RCD NEQ} \quad \ell_1 \neq \ell_2 \quad T = \{\ell : |A|\}}{x : \{\ell_1 : A\} \bullet \{\ell_2\} \rightsquigarrow \emptyset \mid z : \top}$$

P-AND

$$\frac{\begin{array}{c} x : A \bullet \{\ell\} \rightsquigarrow J_1 \mid z : A' \\ x : B \bullet \{\ell\} \rightsquigarrow J_2 \mid z : B' \end{array}}{x : A \& B \bullet \{\ell\} \rightsquigarrow J_1; J_2 \mid z : A' \& B'}$$

```
/* P-RcdEq */
var z = x[T]; /* or */ if (y) copy(y, x[T]);
```

$$\boxed{x : A <:^{\pm} y : B \rightsquigarrow J}$$

(Coercive subtyping)

$$\frac{\text{S-EQUIV} \quad A \doteq B}{x : A <:^+ y : B \rightsquigarrow \text{code}}$$

$$\frac{\text{S-TOP} \quad \top B \top}{x : A <:^{\pm} y : B \rightsquigarrow \emptyset}$$

$$\frac{\text{S-BOT} \quad T = |A|}{x : \perp <:^{\pm} y : A \rightsquigarrow \text{code}}$$

$$\frac{\text{S-INT} \quad T = |\mathbb{Z}|}{x : \mathbb{Z} <:^{\pm} y : \mathbb{Z} \rightsquigarrow \text{code}}$$

$$\frac{\text{S-ARROW} \quad \begin{array}{l} T_1 = \overrightarrow{|A_2|} \quad T_2 = \overrightarrow{|B_2|} \\ Ts = \mathbf{itoa} \mid A_1 \mid \\ x_1 : B_1 <:^+ y_1 : A_1 \rightsquigarrow J_1 \\ x_2 : A_2 <:^+ y_2 : B_2 \rightsquigarrow J_2 \end{array}}{x : A_1 \rightarrow A_2 <:^{\pm} y : B_1 \rightarrow B_2 \rightsquigarrow \text{code}}$$

$$\frac{\text{S-ALL} \quad \begin{array}{l} T_1 = |A_2|^{\forall} \\ T_2 = |B_2|^{\forall} \quad B_1 <: A_1 \\ x_0 : A_2 <:^+ y_0 : B_2 \rightsquigarrow J \end{array}}{x : \forall X * A_1. A_2 <:^{\pm} y : \forall X * B_1. B_2 \rightsquigarrow \text{code}}$$

$$\frac{\text{S-RCD} \quad \begin{array}{l} T_1 = \{\ell : |A|\} \\ T_2 = \{\ell : |B|\} \\ x_0 : A <:^+ y_0 : B \rightsquigarrow J \end{array}}{x : \{\ell : A\} <:^{\pm} y : \{\ell : B\} \rightsquigarrow \text{code}}$$

$$\frac{\text{S-SPLIT} \quad \begin{array}{l} B_1 \triangleleft B \triangleright B_2 \\ y_1 : B_1 \triangleright z : B \triangleleft y_2 : B_2 \rightsquigarrow J_3 \\ x : A <:^{\pm} y_1 : B_1 \rightsquigarrow J_1 \\ x : A <:^{\pm} y_2 : B_2 \rightsquigarrow J_2 \end{array}}{x : A <:^{\pm} z : B \rightsquigarrow \text{code}}$$

$$\frac{\text{S-ANDL} \quad x : A <:^- y : C \rightsquigarrow J}{x : A \& B <:^{\pm} y : C \rightsquigarrow J}$$

$$\frac{\text{S-ANDR} \quad x : B <:^- y : C \rightsquigarrow J}{x : A \& B <:^{\pm} y : C \rightsquigarrow J}$$

```
/* S-Equiv */
copy(y, x);

/* S-Bot */
y[T] = null;

/* S-Int */
y[T] = x[T];

/* S-Arrow */
y[T2] = (x1, y2) => {
  var y1 = {}; J1;
```

```
var x2 = x[T1](y1);
y2 = y2 || {};
J2; return y2;
};

/* S-All */
y[T2] = (X, y0) => {
  var x0 = x[T1](X);
  y0 = y0 || {};
  J; return y0;
};
```

```
/* S-Rcd */
y.__defineGetter__(T2, () => {
  var x0 = x[T1];
  var y0 = {}; J;
  delete this[T];
  return this[T] = y0;
});

/* S-Split */
var y1 = {}; // if y1 != z
var y2 = {}; // if y2 != z
J1; J2; J3;
```

$$\boxed{x : A \triangleright z : C \triangleleft y : B \rightsquigarrow J}$$

(Coercive merging)

$$\begin{array}{c} \text{M-AND} \\ \hline z : A \triangleright z : A \& B \triangleleft z : B \rightsquigarrow \emptyset \end{array} \quad \begin{array}{c} \text{M-ARROW} \\ \hline \begin{array}{c} T = \overrightarrow{|B|} \\ T_1 = \overrightarrow{|B_1|} \quad T_2 = \overrightarrow{|B_2|} \\ y_1 : B_1 \triangleright y : B \triangleleft y_2 : B_2 \rightsquigarrow J \end{array} \\ \hline x_1 : A \rightarrow B_1 \triangleright z : A \rightarrow B \triangleleft x_2 : A \rightarrow B_2 \rightsquigarrow \text{code} \end{array}$$

$$\begin{array}{c} \text{M-ALL} \\ \hline \begin{array}{c} T = |B|^{\forall} \\ T_1 = |B_1|^{\forall} \quad T_2 = |B_2|^{\forall} \\ y_1 : B_1 \triangleright y : B \triangleleft y_2 : B_2 \rightsquigarrow J \end{array} \\ \hline x_1 : \forall X * A. B_1 \triangleright z : \forall X * A. B \triangleleft x_2 : \forall X * A. B_2 \rightsquigarrow \text{code} \end{array}$$

$$\begin{array}{c} \text{M-RCD} \\ \hline \begin{array}{c} T = \{\ell : |A|\} \\ T_1 = \{\ell : |A_1|\} \\ T_2 = \{\ell : |A_2|\} \\ y_1 : A_1 \triangleright y : A \triangleleft y_2 : A_2 \rightsquigarrow J \end{array} \\ \hline x_1 : \{\ell : A_1\} \triangleright z : \{\ell : A\} \triangleleft x_2 : \{\ell : A_2\} \rightsquigarrow \text{code} \end{array}$$

```

/* M-Arrow */
z[T] = (p, y) => {
  y = y || {};
  var y1 = {}; // if y1 != y
  var y2 = {}; // if y2 != y
  x1[T1](p, y1);
  x2[T2](p, y2);
  J; return y;
};

/* M-All */
z[T] = (X, y) => {
  y = y || {};
  var y1 = {}; // if y1 != y
  var y2 = {}; // if y2 != y
  x1[T1](X, y1);
  x2[T2](X, y2);
  J; return y;
};

/* M-Rcd */
z.__defineGetter__(T, () => {
  var y = {};
  var y1 = {}; // if y1 != y
  var y2 = {}; // if y2 != y
  copy(y1, x1[T1]);
  copy(y2, x2[T2]);
  J;
  delete this[T];
  return this[T] = y;
});

```