## Lesson I. R language Programming Environment

Ruth Gómez Graciani 2017/10/16

1 - Create a vector called v and assign the values (3.14, 123, 0.01)

```
v <- c(3.14, 123, 0.01)
v
```

- [1] 3.14 123.00 0.01
- 2- Create a new vector that stores three values: v, 123 and v

```
a <- c(v, 123, v)
a
```

- [1] 3.14 123.00 0.01 123.00 3.14 123.00 0.01
- 3- Calculate the square root of vector v and store it in a new varieble

```
my_sqrt <- sqrt(v)
my_sqrt</pre>
```

- [1] 1.772005 11.090537 0.100000
- 4- Now calculate the value of v divided by my\_sqrt

```
v / my_sqrt
```

- [1] 1.772005 11.090537 0.100000
- 5- Add this two vectors: (1, 2, 3, 4) and (0,100). What do you see? Can two vectors of different length be added?

```
c(1, 2, 3, 4) + c(0, 100)
```

[1] 1 102 3 104

Yes, they can, because the largest vector is a multiple from the smaller one. The small vector is repeated twice in order to add it to the first one.

6- Create a sequence of numbers from 1 to 19 using the : operator

```
1:19
```

- [1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19
- 7- Now use seq() to create a sequence from 1 to 10 incrementing by 0.5

```
seq(1, 10, 0.5)
```

```
[1] 1.0 1.5 2.0 2.5 3.0 3.5 4.0 4.5 5.0 5.5 6.0 6.5 7.0 7.5 [15] 8.0 8.5 9.0 9.5 10.0
```

### 8- Use seq() to generate a list of 50 numbers between 50 and 999 and store the list in n

```
n <- seq(50, 999, length.out = 50)
n

[1] 50.00000 69.36735 88.73469 108.10204 127.46939 146.83673 166.20408
[8] 185.57143 204.93878 224.30612 243.67347 263.04082 282.40816 301.77551
[15] 321.14286 340.51020 359.87755 379.24490 398.61224 417.97959 437.34694
[22] 456.71429 476.08163 495.44898 514.81633 534.18367 553.55102 572.91837
```

[29] 592.28571 611.65306 631.02041 650.38776 669.75510 689.12245 708.48980

[36] 727.85714 747.22449 766.59184 785.95918 805.32653 824.69388 844.06122

[43] 863.42857 882.79592 902.16327 921.53061 940.89796 960.26531 979.63265

[50] 999.00000

## 9- Apply the length() function to the variable n. Which is the result?

```
length(n)
```

[1] 50

The result is the number of elements inside the vector

#### 10- Now generate a new list of numbers starting from 1 that has the same length as n variable

```
b <- list(1:length(n))
b

[[1]]
[1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23
[24] 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46
[47] 47 48 49 50
```

## 11- Create a vector with 100 zeros

```
c <- rep(0, 100)
c
```

## 12- Create a new vector with 10 repetitions of the vector ("a", "b", "c")

```
d <- rep(c('a', 'b', 'c'), 10)
d</pre>
```

```
[1] "a" "b" "c" "a" "b" [18] "c" "a" "b" "c" "a" "b" "c" "a" "b" "c"
```

## 13- Now create a new vector that contains 10 a letters, then 10 b's, then 10 c's and save it into a variable called abc

```
abc <- c(rep('a', 10), rep('b', 10), rep('c', 10))
abc
```

14- Create a vector with the values (1,100,-25,365) and save it into v1 variable

```
v1 <- c(1, 100, -25, 365)
v1
```

[1] 1 100 -25 365

15- now create a new variable bool that gets the result of v1<1. What is the result of this operation? What kind of value you see?

```
bool <- v1 < 1
bool
```

[1] FALSE FALSE TRUE FALSE

The result of the operation is TRUE when the inequality is accomplished, and FALSE when not, for each value of the vector. The value is a logical operator, as we can see when the str() function is used:

```
str(bool)
```

logi [1:4] FALSE FALSE TRUE FALSE

16- Now take abc variable from question 13 and generate a single string value. That is, something like: (a,b,c) -> "abc"

```
abc <- paste(abc, collapse="")
abc</pre>
```

[1] "aaaaaaaaabbbbbbbbbbbccccccccc"

17- Create a new matrix with 4 rows and 5 columns from a new vector that contains the values from 1 to 20. Store the results in variable m1

```
e <- c(1:20)
m1 <- matrix(e, 4,5)
m1</pre>
```

```
[,1] [,2] [,3] [,4] [,5]
[1,]
              5
                         13
        1
                    9
                               17
[2,]
         2
              6
                   10
                               18
[3,]
              7
         3
                         15
                               19
                   11
[4,]
                   12
                         16
                               20
```

18- Now create a vector called students with the values ("Ana", "John", "Pedro", "Joan") and create a new matrix adding students as a new column to m1 matrix. What happens to numeric values?

```
names <- c("Ana", "John", "Pedro", "Joan")
m2 <- matrix(c(m1, names), 4, 6)
m2</pre>
```

```
[,1] [,2] [,3] [,4] [,5] [,6]
[1,] "1" "5" "9" "13" "17" "Ana"
[2,] "2" "6" "10" "14" "18" "John"
```

```
[3,] "3" "7" "11" "15" "19" "Pedro" [4,] "4" "8" "12" "16" "20" "Joan"
```

The numerical values have been converted into characters

19- Now create a new data.frame() called df with students vector and m1 matrix. What difference do you see with the previous matrix?

```
df <- data.frame(m1, names)
df

X1 X2 X3 X4 X5 names
1 1 5 9 13 17 Ana
2 2 6 10 14 18 John
3 3 7 11 15 19 Pedro
4 4 8 12 16 20 Joan
```

The data frame can contain different value types

20- create a new vector with the labels "name", "age", "weight", "bp", "rate", "test". Now use colnames() to set the colnames attribute of our data frame df. Show your final data frame

```
labels <- c("name", "age", "weight", "bp", "rate",</pre>
                                                              "test")
colnames(df) <- labels</pre>
df
  name age weight bp rate test
        5
               9 13
                       17
2
     2
         6
               10 14
                       18 John
3
     3
        7
               11 15
                       19 Pedro
               12 16
                       20 Joan
```

21- Calculate the mean of a vector with values (10,11,12)

```
f <- c(10, 11, 12)
mean(f)
```

[1] 11

22- Now create a new function call new\_mean that receives a vector as a parameter, then calculates the sum of the vector, the length of the vector and return the mean of the vector.

```
new_mean <- function(vector) {
   summatory <- sum(vector)
   numofels <- length(vector)
   return(summatory / numofels)
}</pre>
```

[1] 11

23- Use sample() function to simulate a rolling dice. That is, randomly select four numbers between 1 and 6 with replacement.

```
sample(1:6, 4, replace = T)
[1] 3 3 2 2
```

24- Simulate 50 flips of an unfair two-sided coin. The probabilities here are 0.7 for heads and 0.3 for tails. Use sample() to draw a sample of size 50. Store the results in variable flip. How would you test if the results follow the probability defined?

```
coin <- c('heads', 'tails')
prob <- c(0.7, 0.3)
flip <- sample(coin, 50, prob, replace = T)
table(flip) / 50</pre>
```

flip heads tails 0.76 0.24

The table function counts the number of elements inside the vector, and dividing it by the total number of elements we obtain the proportion or probability.

25- How would you generate 10 random numbers from a standard normal distribution with a mean of 150 and a standard deviation of 10?

```
rnorm(10, 150, 10)
[1] 153.8044 161.9649 155.7712 141.4974 149.9645 146.6390 133.8690
[8] 153.0872 156.9581 144.0788
```

26- Now, how would you generate 100 sets of random numbers like the previous question? Save results in a variable called rp

```
rp <- matrix(nrow = 10, ncol = 100)

for(i in c(1:100)){
   rp[,i] <- rnorm(10, 150, 10)
}</pre>
```

The variable rp is partially below:

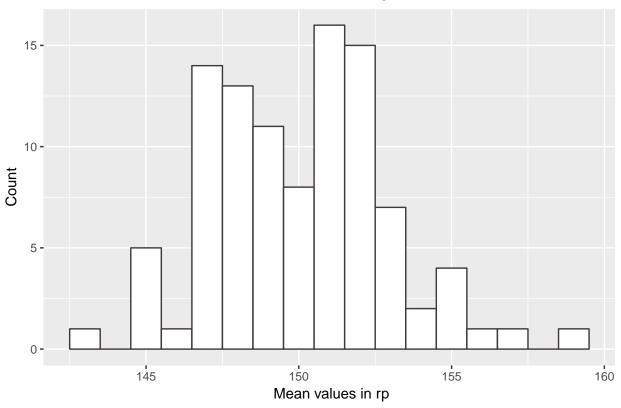
```
rp[, 1:7]
```

```
[,1]
                   [,2]
                            [,3]
                                     [,4]
                                              [,5]
                                                       [,6]
                                                                 [,7]
[1,] 155.6068 128.4530 139.9639 154.1272 145.3829 154.3041 170.2646
[2,] 163.3918 148.5872 147.9112 145.1162 136.7339 146.2670 134.2923
[3,] 153.1232 161.8548 154.4478 150.2554 158.0417 140.5964 138.3372
[4,] 155.3566 152.9047 159.8612 159.8668 146.0425 152.4472 143.3294
[5,] 144.7562 146.1484 166.5159 149.9225 149.1509 167.9533 152.9628
[6,] 160.7775 145.1480 151.2256 164.8705 140.6693 142.7230 149.3720
[7,] 153.3194 134.0981 144.6437 153.9233 139.8999 136.8646 164.7200
[8,] 150.0817 129.7899 127.9302 137.0922 143.3862 143.6082 169.3335
[9,] 147.7537 148.5211 158.0424 168.2934 160.9372 158.9686 142.8980
[10,] 142.3939 138.0353 145.6404 131.9598 142.9629 158.1975 144.1507
```

## 27- Use colMeans() function to find the mean of each column of rp and plot a histogram

```
g <- colMeans(rp)
g
  [1] 152.6561 143.3540 149.6182 151.5427 146.3207 150.1930 150.9661
  [8] 152.1399 148.1855 148.2643 153.6168 149.1662 147.2132 147.2310
 [15] 154.9003 147.5356 149.1392 150.9641 149.5153 151.6042 152.5015
 [22] 147.3567 147.2072 150.9011 149.0650 150.5195 154.6107 153.4940
 [29] 148.5115 146.7496 145.3730 150.8139 145.2589 156.7448 149.3824
 [36] 151.8090 148.5999 151.2534 151.4975 151.8104 150.0578 150.7099
 [43] 151.9483 151.1235 149.6095 153.0261 146.5054 147.9153 152.0663
 [50] 147.0389 151.7898 147.1539 153.1301 150.8094 148.6969 148.3457
 [57] 158.6595 147.5801 146.6578 149.3462 147.2353 150.6897 154.9952
 [64] 150.6263 148.0364 152.9054 152.2251 146.6150 147.5554 145.1319
 [71] 145.3735 153.5770 149.5338 147.0499 155.7634 147.6419 150.4548
 [78] 152.0469 151.9221 152.0631 147.4626 150.1326 150.7960 144.6105
 [85] 146.9673 149.0312 151.9039 151.0038 152.2482 151.7074 148.4264
 [92] 149.3717 155.1098 148.6090 147.6420 150.9007 153.1502 147.5074
 [99] 150.9319 148.1107
ggplot()+
 aes(g)+
 geom_histogram(binwidth=1, colour="#413839", fill="white")+
 labs(title="Mean values histogram", x = " Mean values in rp", y = "Count" )+
theme(plot.title = element_text(hjust = 0.5))
```

## Mean values histogram



28- Create a vector X with 10 values and calculate the cumulative sums for this vector using a for loop.

```
X <- sample(100, 10)
X

[1] 69 67 37  2 94 73 18 82 56 75

for (i in c(2:length(X))) {
   X[i] <- X[i] + X[i - 1]
}
X</pre>
```

[1] 69 136 173 175 269 342 360 442 498 573

29- Create two vectors, Z1 and Z2. Z1 is a vector of 20 elements filled with 20 random numbers from a standard normal distribution. Z2 is a string of 20 zeros. Design a for loop that counts from 1 to 20. For each value, it has to evaluate if the value is greater than 0. For all those values, it must write a 1 in the same position of the vector Z2. For lower than 0 values it must write a -1. Is it possible to do the same thing using which()? How would you do it?

With the for loop

```
Z1 <- rnorm(20)
Z2 <- rep(0, 20)
for (i in c(1:20)) {
  if (Z1[i] > 0) {
    Z2[i] <- 1
  } else{
    Z2[i] <- -1
  }
}</pre>
```

With which()

```
Z2 <- rep(0,20)
Z2[which(Z1 > 0)] <- 1
Z2[which(Z1 < 0)] <- -1
```

30- Now we are going to import a data file:plants.csv and use read.table()function to store the new table in an object called plants

```
plants <- read.table("plants2017_10_13D19_4_42 (1).csv", sep = ",")
```

31- How do you find the rows and columns of the variable plants? And the size in bytes?

As we can see below, there is a large number of rows:

```
nrow(plants)
[1] 5166
ncol(plants)
```

[1] 10

A small subset of the row names will be displayed. All the column names will be displayed

```
rownames(plants)[1:10]
 [1] "1" "2"
               "3"
                                               "9"
colnames(plants)
 [1] "Scientific_Name"
                                                      "Active_Growth_Period"
                              "Duration"
                                                      "pH_Max"
 [4] "Foliage_Color"
                              "pH_Min"
 [7] "Precip_Min"
                              "Precip_Max"
                                                      "Shade_Tolerance"
[10] "Temp_Min_F"
The size in bytes:
object.size(plants)
```

933520 bytes

## 32- How would you see the first rows of the experiment?

## head(plants)

	Scientific_Name			Duration		Active_Growth_Period	
1		Abe:	lmoschus	3	<na></na>		<na></na>
2	Abelmoso	hus es	culentus	Annual, Pe	erennial		<na></na>
3			Abies	3	<na></na>		<na></na>
4		Abies 1	balsamea	n Pe	erennial	Spring and	Summer
5	Abies balsamea	a var. 1	balsamea	n Pe	erennial		<na></na>
6			Abutilon	ı	<na></na>		<na></na>
	Foliage_Color	pH_Min	pH_Max	Precip_Min	Precip_Max	Shade_Tole	cance
1	<na></na>	NA	NA	NA	NA		<na></na>
2	<na></na>	NA	NA	NA	NA		<na></na>
3	<na></na>	NA	NA	NA	NA		<na></na>
4	Green	4	6	13	60	Tole	erant
5	<na></na>	NA	NA	NA	NA		<na></na>
6	<na></na>	NA	NA	NA	NA		<na></na>
	Temp_Min_F						
1	NA						
2	NA						
3	NA						
4	-43						
5	NA						
6	NA						

# 33- What information is summary() providing when applied to the experiment variable? What NA plants\$Precip\_Minmeans? What information is str() providing?

summary() shows basic statistical values of the vector. In this case, I have assumed that one of the experiment variables is pH\_Min.

## summary(plants\$pH\_Min)

```
Min. 1st Qu. Median Mean 3rd Qu. Max. NA's 3.000 4.500 5.000 4.997 5.500 7.000 4327
```

NA states fot Not Available (it is missing data)

str() provides the type of variable and the elements that can be found inside it. As an example, we can see that str is a datagfarme and therefore it can contain different types of values.

```
str(plants, strict.width="cut")
'data.frame':
               5166 obs. of 10 variables:
$ Scientific Name
                      : Factor w/ 5166 levels "Abelmoschus",..: 1 2 3 4 ...
$ Duration
                       : Factor w/ 8 levels "Annual", "Annual, Biennial",...
 $ Active_Growth_Period: Factor w/ 8 levels "Fall, Winter and Spring",.....
                       : Factor w/ 6 levels "Dark Green", "Gray-Green", .....
 $ Foliage Color
 $ pH Min
                       : num NA NA NA 4 NA NA NA 7 NA ...
 $ pH_Max
                       : num NA NA NA 6 NA NA NA NA 8.5 NA ...
 $ Precip Min
                       : int NA NA NA 13 NA NA NA NA 4 NA ...
                       : int NA NA NA 60 NA NA NA NA 20 NA ...
 $ Precip_Max
 $ Shade_Tolerance
                       : Factor w/ 3 levels "Intermediate",..: NA NA NA 3..
 $ Temp_Min_F
                       : int NA NA NA -43 NA NA NA NA -13 NA ...
```

# 34- Create a function to calculate the minimum $Temp\_Min\_F$ and the average $Precip\_Min$ of the table plants

There are already functions to calculate the minimum and average values of a vector, I have assumed that the function has to retrieve both at the same time, from the columns specified, when a datafarme is provided.

```
Calculate_plants <- function(plants){
  minimum <- min(plants$Temp_Min_F, na.rm = TRUE)
  average <- mean(plants$Precip_Min, na.rm = TRUE)
  return(c(minimum, average))
}</pre>
Calculate_plants(plants)
```

```
[1] -79.00000 25.56884
```

#### To be evaluated:

#### Create a function that:

- Creates a 20 by 20 matrix of 0 values
- Places in a random position inside the matrix one vector of size 6 and represents it with six consecutive "1" values. This vector will be our ship
- Receives two vectors of six values as inputs. X and Y. Both vectors store six values between 1 and 20 and represent coordinates in the matrix
- The function returns a vector with six values depending if the coordinates have hit or miss our ship. Example=("hit", "miss", "miss", "miss", "hit")

Make the number of ships in the matrix a parameter given by the user and export the matrix to a text file.

The ships can be vertical or horizontal, but they can't overlap.

```
Battleship <- function(X, Y, ships) {
  # Create the empty matrix
  m1 <- matrix(0, 20, 20)
  # Iterate over ships
  for (s in c(1:ships)) {</pre>
```

```
# We avoid solapping ships
    done <- F
    while (done == F) {
      # Place in a random position, and random direction
      variablenum \leftarrow c(1:6) + sample(c(1:14), 1)
      fixnum \leftarrow sample(c(1:20), 1)
      random <- sample(c(1:2))</pre>
      order <- list()
      order[[random[1]]] <- variablenum</pre>
      order[[random[2]]] <- fixnum</pre>
      if (sum(m1[order[[1]], order[[2]]]) == 0) {
        m1[order[[1]], order[[2]]] <- c(rep(1, 6))
        done <- T
    }
  }
  # Creates result
  result <- as.factor(diag(m1[X, Y]))
  levels(result) <- c('miss', 'hit')</pre>
  # Export matrix and return result
  write.table(m1, 'matrix.txt', col.names = F,row.names = F,quote = F)
  return(as.character(result))
}
```

Here there is an example of the result of the function:

```
Battleship(c(1, 4, 15, 6, 17, 11), c(10, 14, 16, 2, 7, 20), 3)
```

```
[1] "hit" "miss" "miss" "miss" "miss" "miss"
```

The generated file looks like this (I am using engine = 'bash'):

```
cat matrix.txt
```

```
 \  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  
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