Lesson I. R language Programming Environment

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1 - Create a vector called v and assign the values (3.14, 123, 0.01)

```
v <- c(3.14, 123, 0.01)
v
```

- [1] 3.14 123.00 0.01
- 2- Create a new vector that stores three values: v, 123 and v

```
a <- c(v, 123, v)
a
```

- [1] 3.14 123.00 0.01 123.00 3.14 123.00 0.01
- 3- Calculate the square root of vector v and store it in a new varieble

```
my_sqrt <- sqrt(v)
my_sqrt</pre>
```

- [1] 1.772005 11.090537 0.100000
- 4- Now calculate the value of v divided by my_sqrt

```
v / my_sqrt
```

- [1] 1.772005 11.090537 0.100000
- 5- Add this two vectors: (1, 2, 3, 4) and (0,100). What do you see? Can two vectors of different length be added?

```
c(1, 2, 3, 4) + c(0, 100)
```

[1] 1 102 3 104

Yes, they can, because the largest vector is a multiple from the smaller one. The small vector is repeated twice in order to add it to the first one.

6- Create a sequence of numbers from 1 to 19 using the : operator

```
1:19
```

- [1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19
- 7- Now use seq() to create a sequence from 1 to 10 incrementing by 0.5

```
seq(1, 10, 0.5)
```

```
[1] 1.0 1.5 2.0 2.5 3.0 3.5 4.0 4.5 5.0 5.5 6.0 6.5 7.0 7.5 [15] 8.0 8.5 9.0 9.5 10.0
```

8- Use seq() to generate a list of 50 numbers between 50 and 999 and store the list in n

```
n <- seq(50, 999, length.out = 50)
n

[1] 50.00000 69.36735 88.73469 108.10204 127.46939 146.83673 166.20408
[8] 185.57143 204.93878 224.30612 243.67347 263.04082 282.40816 301.77551
[15] 321.14286 340.51020 359.87755 379.24490 398.61224 417.97959 437.34694
[22] 456.71429 476.08163 495.44898 514.81633 534.18367 553.55102 572.91837
```

[29] 592.28571 611.65306 631.02041 650.38776 669.75510 689.12245 708.48980

[36] 727.85714 747.22449 766.59184 785.95918 805.32653 824.69388 844.06122

[43] 863.42857 882.79592 902.16327 921.53061 940.89796 960.26531 979.63265

[50] 999.00000

9- Apply the length() function to the variable n. Which is the result?

```
length(n)
```

[1] 50

The result is the number of elements inside the vector

10- Now generate a new list of numbers starting from 1 that has the same length as n variable

```
b <- list(1:length(n))
b

[[1]]
[1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23
[24] 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46
[47] 47 48 49 50
```

11- Create a vector with 100 zeros

```
c <- rep(0, 100)
c
```

12- Create a new vector with 10 repetitions of the vector ("a", "b", "c")

```
d <- rep(c('a', 'b', 'c'), 10)
d</pre>
```

```
[1] "a" "b" "c" "a" "b" [18] "c" "a" "b" "c" "a" "b" "c" "a" "b" "c"
```

13- Now create a new vector that contains 10 a letters, then 10 b's, then 10 c's and save it into a variable called abc

```
abc <- c(rep('a', 10), rep('b', 10), rep('c', 10))
abc
```

14- Create a vector with the values (1,100,-25,365) and save it into v1 variable

```
v1 <- c(1, 100, -25, 365)
v1
```

[1] 1 100 -25 365

15- now create a new variable bool that gets the result of v1<1. What is the result of this operation? What kind of value you see?

```
bool <- v1 < 1
bool
```

[1] FALSE FALSE TRUE FALSE

The result of the operation is TRUE when the inequality is accomplished, and FALSE when not, for each value of the vector. The value is a logical operator, as we can see when the str() function is used:

```
str(bool)
```

logi [1:4] FALSE FALSE TRUE FALSE

16- Now take abc variable from question 13 and generate a single string value. That is, something like: (a,b,c) -> "abc"

```
abc <- paste(abc, collapse="")
abc</pre>
```

[1] "aaaaaaaaabbbbbbbbbbbccccccccc"

17- Create a new matrix with 4 rows and 5 columns from a new vector that contains the values from 1 to 20. Store the results in variable m1

```
e <- c(1:20)
m1 <- matrix(e, 4,5)
m1</pre>
```

```
[,1] [,2] [,3] [,4] [,5]
[1,]
              5
                         13
        1
                    9
                               17
[2,]
         2
              6
                   10
                               18
[3,]
              7
         3
                         15
                               19
                   11
[4,]
                   12
                         16
                               20
```

18- Now create a vector called students with the values ("Ana", "John", "Pedro", "Joan") and create a new matrix adding students as a new column to m1 matrix. What happens to numeric values?

```
names <- c("Ana", "John", "Pedro", "Joan")
m2 <- matrix(c(m1, names), 4, 6)
m2</pre>
```

```
[,1] [,2] [,3] [,4] [,5] [,6]
[1,] "1" "5" "9" "13" "17" "Ana"
[2,] "2" "6" "10" "14" "18" "John"
```

```
[3,] "3" "7" "11" "15" "19" "Pedro" [4,] "4" "8" "12" "16" "20" "Joan"
```

The numerical values have been converted into characters

19- Now create a new data.frame() called df with students vector and m1 matrix. What difference do you see with the previous matrix?

```
df <- data.frame(m1, names)
df

X1 X2 X3 X4 X5 names
1 1 5 9 13 17 Ana
2 2 6 10 14 18 John
3 3 7 11 15 19 Pedro
4 4 8 12 16 20 Joan
```

The data frame can contain different value types

20- create a new vector with the labels "name", "age", "weight", "bp", "rate", "test". Now use colnames() to set the colnames attribute of our data frame df. Show your final data frame

```
labels <- c("name", "age", "weight", "bp", "rate",</pre>
                                                              "test")
colnames(df) <- labels</pre>
df
  name age weight bp rate test
        5
               9 13
                       17
2
     2
         6
               10 14
                       18 John
3
     3
        7
               11 15
                       19 Pedro
               12 16
                       20 Joan
```

21- Calculate the mean of a vector with values (10,11,12)

```
f <- c(10, 11, 12)
mean(f)
```

[1] 11

22- Now create a new function call new_mean that receives a vector as a parameter, then calculates the sum of the vector, the length of the vector and return the mean of the vector.

```
new_mean <- function(vector) {
   summatory <- sum(vector)
   numofels <- length(vector)
   return(summatory / numofels)
}</pre>
```

[1] 11

23- Use sample() function to simulate a rolling dice. That is, randomly select four numbers between 1 and 6 with replacement.

```
sample(1:6, 4, replace = T)
[1] 3 3 6 5
```

24- Simulate 50 flips of an unfair two-sided coin. The probabilities here are 0.7 for heads and 0.3 for tails. Use sample() to draw a sample of size 50. Store the results in variable flip. How would you test if the results follow the probability defined?

```
coin <- c('heads', 'tails')
prob <- c(0.7, 0.3)
flip <- sample(coin, 50, prob, replace = T)
table(flip) / 50</pre>
```

flip heads tails 0.62 0.38

The table function counts the number of elements inside the vector, and dividing it by the total number of elements we obtain the proportion or probability.

25- How would you generate 10 random numbers from a standard normal distribution with a mean of 150 and a standard deviation of 10?

```
rnorm(10, 150, 10)
[1] 155.6031 164.6120 167.8707 154.0799 152.0535 129.6693 177.4067
[8] 149.2280 151.2564 148.9029
```

26- Now, how would you generate 100 sets of random numbers like the previous question? Save results in a variable called rp

```
rp <- matrix(nrow = 10, ncol = 100)

for(i in c(1:100)){
   rp[,i] <- rnorm(10, 150, 10)
}</pre>
```

The variable **rp** is partially below:

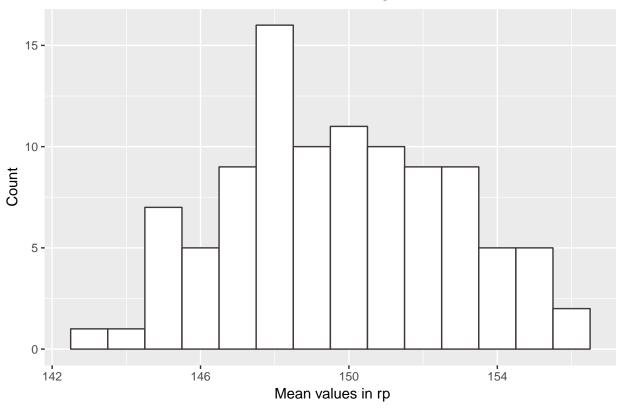
```
rp[, 1:7]
```

```
[,1]
                   [,2]
                            [,3]
                                     [,4]
                                              [,5]
                                                       [,6]
                                                                 [,7]
[1,] 140.0669 143.3637 145.1863 152.2051 145.7332 151.4134 158.8728
[2,] 160.8110 148.3547 138.9019 165.2508 148.3254 147.4687 140.5276
[3,] 155.5592 146.9632 161.6654 162.8191 149.4475 150.3197 154.3862
[4,] 158.0649 129.1716 159.2442 136.0860 169.1818 152.7116 139.8331
[5,] 148.8197 141.4025 138.7841 144.6775 131.1346 173.8950 165.7094
[6,] 149.0578 144.6640 157.8662 167.9812 163.0143 148.2588 156.8001
[7,] 142.7917 161.1891 143.7631 154.8161 144.1854 156.8680 158.2100
[8,] 139.7568 132.0696 168.0300 149.4341 156.7158 166.8079 142.2932
[9,] 164.4519 151.1789 149.1910 149.7222 151.6728 141.7211 140.8171
[10,] 142.9706 151.1849 137.0063 132.8108 144.3284 159.2679 151.6787
```

27- Use colMeans() function to find the mean of each column of rp and plot a histogram

```
g <- colMeans(rp)
g
  [1] 150.2351 144.9542 149.9639 151.5803 150.3739 154.8732 150.9128
  [8] 151.9642 146.7104 150.9722 146.7402 146.3249 148.7724 148.3713
 [15] 152.0814 148.0033 152.6465 148.8175 145.7716 153.0002 147.0953
 [22] 148.2386 153.5236 144.4476 148.2192 147.8983 149.1783 148.0680
 [29] 153.6397 152.5251 151.4461 149.8321 152.6800 149.0938 147.6887
 [36] 148.2227 149.7528 149.2105 149.7470 146.8988 148.1423 151.5602
 [43] 152.7502 147.0374 150.8670 154.4379 146.6294 151.0045 151.6000
 [50] 144.8649 144.6366 146.9825 145.1436 145.8679 149.6766 148.3947
 [57] 156.1056 152.6936 151.4451 148.3983 150.1896 145.8903 144.6277
 [64] 146.6376 154.3656 149.2795 151.6863 152.2306 153.3180 148.1821
 [71] 150.8419 155.4791 149.8087 155.3558 149.6408 149.4098 154.0923
 [78] 148.6606 153.0398 150.0385 151.4564 149.2033 150.5751 145.5390
 [85] 145.2656 145.1572 155.5233 151.4097 146.9386 152.2166 147.6251
 [92] 152.2420 148.2120 143.4210 147.7971 148.4928 155.3153 153.3922
 [99] 148.7496 155.1808
ggplot()+
 aes(g)+
 geom_histogram(binwidth=1, colour="#413839", fill="white")+
 labs(title="Mean values histogram", x = " Mean values in rp", y = "Count" )+
theme(plot.title = element_text(hjust = 0.5))
```

Mean values histogram



28- Create a vector X with 10 values and calculate the cumulative sums for this vector using a for loop.

```
X <- sample(100, 10)
X

[1] 78 15 92 8 50 83 71 30 10 19

for (i in c(2:length(X))) {
   X[i] <- X[i] + X[i - 1]
}
X</pre>
```

[1] 78 93 185 193 243 326 397 427 437 456

29- Create two vectors, Z1 and Z2. Z1 is a vector of 20 elements filled with 20 random numbers from a standard normal distribution. Z2 is a string of 20 zeros. Design a for loop that counts from 1 to 20. For each value, it has to evaluate if the value is greater than 0. For all those values, it must write a 1 in the same position of the vector Z2. For lower than 0 values it must write a -1. Is it possible to do the same thing using which()? How would you do it?

With the for loop

```
Z1 <- rnorm(20)
Z2 <- rep(0, 20)
for (i in c(1:20)) {
   if (Z1[i] > 0) {
        Z2[i] <- 1
   } else{
        Z2[i] <- -1
   }
}</pre>
```

With which()

```
Z2 <- rep(0,20)
Z2[which(Z1 > 0)] <- 1
Z2[which(Z1 < 0)] <- -1
```

30- Now we are going to import a data file:plants.csv and use read.table()function to store the new table in an object called plants

```
plants <- read.table("Data/plants2017_10_13D19_4_42 (1).csv", sep = ",")
```

31- How do you find the rows and columns of the variable plants? And the size in bytes?

As we can see below, there is a large number of rows:

```
nrow(plants)
[1] 5166
ncol(plants)
```

[1] 10

A small subset of the row names will be displayed. All the column names will be displayed

```
rownames(plants)[1:10]
 [1] "1" "2"
               "3"
                                               "9"
colnames(plants)
 [1] "Scientific_Name"
                                                      "Active_Growth_Period"
                              "Duration"
                                                      "pH_Max"
 [4] "Foliage_Color"
                              "pH_Min"
 [7] "Precip_Min"
                              "Precip_Max"
                                                      "Shade_Tolerance"
[10] "Temp_Min_F"
The size in bytes:
object.size(plants)
```

933520 bytes

32- How would you see the first rows of the experiment?

head(plants)

	Scientific_Name			Duration		Active_Growth_Period	
1		Abe:	lmoschus	3	<na></na>		<na></na>
2	Abelmoso	hus es	culentus	Annual, Pe	erennial		<na></na>
3			Abies	3	<na></na>		<na></na>
4		Abies 1	balsamea	n Pe	erennial	Spring and	Summer
5	Abies balsamea	a var. 1	balsamea	n Pe	erennial		<na></na>
6			Abutilon	ı	<na></na>		<na></na>
	Foliage_Color	pH_Min	pH_Max	Precip_Min	Precip_Max	Shade_Tole	cance
1	<na></na>	NA	NA	NA	NA		<na></na>
2	<na></na>	NA	NA	NA	NA		<na></na>
3	<na></na>	NA	NA	NA	NA		<na></na>
4	Green	4	6	13	60	Tole	erant
5	<na></na>	NA	NA	NA	NA		<na></na>
6	<na></na>	NA	NA	NA	NA		<na></na>
	Temp_Min_F						
1	NA						
2	NA						
3	NA						
4	-43						
5	NA						
6	NA						

33- What information is summary() providing when applied to the experiment variable? What NA plants\$Precip_Minmeans? What information is str() providing?

summary() shows basic statistical values of the vector. In this case, I have assumed that one of the experiment variables is pH_Min.

summary(plants\$pH_Min)

```
Min. 1st Qu. Median Mean 3rd Qu. Max. NA's 3.000 4.500 5.000 4.997 5.500 7.000 4327
```

NA states fot Not Available (it is missing data)

str() provides the type of variable and the elements that can be found inside it. As an example, we can see that str is a datagfarme and therefore it can contain different types of values.

```
str(plants, strict.width="cut")
'data.frame':
               5166 obs. of 10 variables:
$ Scientific Name
                      : Factor w/ 5166 levels "Abelmoschus",..: 1 2 3 4 ...
$ Duration
                       : Factor w/ 8 levels "Annual", "Annual, Biennial",...
 $ Active_Growth_Period: Factor w/ 8 levels "Fall, Winter and Spring",.....
                       : Factor w/ 6 levels "Dark Green", "Gray-Green", .....
 $ Foliage Color
 $ pH Min
                       : num NA NA NA 4 NA NA NA 7 NA ...
 $ pH_Max
                       : num NA NA NA 6 NA NA NA NA 8.5 NA ...
 $ Precip Min
                       : int NA NA NA 13 NA NA NA NA 4 NA ...
                       : int NA NA NA 60 NA NA NA NA 20 NA ...
 $ Precip_Max
 $ Shade_Tolerance
                       : Factor w/ 3 levels "Intermediate",..: NA NA NA 3..
 $ Temp_Min_F
                       : int NA NA NA -43 NA NA NA NA -13 NA ...
```

34- Create a function to calculate the minimum $Temp_Min_F$ and the average $Precip_Min$ of the table plants

There are already functions to calculate the minimum and average values of a vector, I have assumed that the function has to retrieve both at the same time, from the columns specified, when a datafarme is provided.

```
Calculate_plants <- function(plants){
  minimum <- min(plants$Temp_Min_F, na.rm = TRUE)
  average <- mean(plants$Precip_Min, na.rm = TRUE)
  return(c(minimum, average))
}</pre>
Calculate_plants(plants)
```

```
[1] -79.00000 25.56884
```

To be evaluated:

Create a function that:

- Creates a 20 by 20 matrix of 0 values
- Places in a random position inside the matrix one vector of size 6 and represents it with six consecutive "1" values. This vector will be our ship
- Receives two vectors of six values as inputs. X and Y. Both vectors store six values between 1 and 20 and represent coordinates in the matrix
- The function returns a vector with six values depending if the coordinates have hit or miss our ship. Example=("hit", "miss", "miss", "miss", "hit")

Make the number of ships in the matrix a parameter given by the user and export the matrix to a text file.

The ships can be vertical or horizontal, but they can't overlap.

```
Battleship <- function(X, Y, ships) {
  # Create the empty matrix
  m1 <- matrix(0, 20, 20)
  # Iterate over ships
  for (s in c(1:ships)) {</pre>
```

```
# We avoid solapping ships
    done <- F
    while (done == F) {
      # Place in a random position, and random direction
      variablenum \leftarrow c(1:6) + sample(c(1:14), 1)
      fixnum \leftarrow sample(c(1:20), 1)
      random <- sample(c(1:2))</pre>
      order <- list()
      order[[random[1]]] <- variablenum</pre>
      order[[random[2]]] <- fixnum</pre>
      if (sum(m1[order[[1]], order[[2]]]) == 0) {
        m1[order[[1]], order[[2]]] <- c(rep(1, 6))
        done <- T
    }
  }
  # Creates result
  result <- as.factor(diag(m1[X, Y]))
  levels(result) <- c('miss', 'hit')</pre>
  # Export matrix and return result
  write.table(m1, 'matrix.txt', col.names = F,row.names = F,quote = F)
  return(as.character(result))
}
```

Here there is an example of the result of the function:

```
Battleship(c(1, 4, 15, 6, 17, 11), c(10, 14, 16, 2, 7, 20), 3)
```

[1] "miss" "miss" "miss" "miss" "miss" "miss"

The generated file looks like this (I am using engine = 'bash'):

```
cat matrix.txt
```

```
 \  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  \, 0\  
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