

# Iris: A Modular Foundation for Higher-Order Concurrent Separation Logic<sup>1</sup>

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January 8, 2018 @ POPL Tutorials, Los Angeles

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## Preparation for this tutorial

- ▶ Download the tutorial lecture material  
`http://iris-project.org/tutorial`
- ▶ Follow README to install Iris **3.1**

## Iris Proof Mode (IPM)

Many recent program logics come with mechanized soundness proofs, but how to reason in these logics?

**Goal of IPM:** reasoning in Iris in the same style as reasoning in Coq

# Iris Proof Mode (IPM)

Many recent program logics come with mechanized soundness proofs, but how to reason in these logics?

**Goal of IPM:** reasoning in Iris in the same style as reasoning in Coq

**Features of IPM:**

- ▶ Extends Coq with (spatial and non-spatial) named proof contexts for Iris
- ▶ Tactics for introduction and elimination of all connectives of Iris
- ▶ Entirely implemented using reflection, type classes and Ltac (no OCaml plugin needed)



# Iris Proof Mode (IPM) demo

**Lemma** `and_exist_sep {A} P R (Ψ: A → iProp) :`

`P * (∃ a, Ψ a) * R -* ∃ a, Ψ a * P.`

**Proof.**

1 subgoal

`M : ucmraT`

`A : Type`

`P, R : iProp`

`Ψ : A → iProp`

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`P * (∃ a : A, Ψ a) * R -* ∃ a : A, Ψ a * P`

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`iIntros "[HP [HΨ HR]]".`

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\_\_\_\_\_ (1/1)

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**Lemma** `and_exist_sep {A} P R ( $\Psi$ :  $A \rightarrow \text{iProp}$ ) :`

`P * ( $\exists a, \Psi a$ ) * R  $\multimap$   $\exists a, \Psi a$  * P.`

**Proof.**

`iIntros "[HP [H $\Psi$  HR]]".`

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`M : ucmraT`

`A : Type`

`P, R : iProp`

`$\Psi$  :  $A \rightarrow \text{iProp}$`

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`"HP" : P`

`"H $\Psi$ " :  $\exists a : A, \Psi a$`

`"HR" : R`

\*

`$\exists a : A, \Psi a$  * P`

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**Proof.**

`iIntros "[HP [H $\Psi$  HR]]".`

`iDestruct "H $\Psi$ " as (x) "H $\Psi$ ".`

1 subgoal

`M : ucmraT`

`A : Type`

`P, R : iProp`

`$\Psi$  : A  $\rightarrow$  iProp`

---

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`"HP" : P`

`"H $\Psi$ " :  $\exists$  a : A,  $\Psi$  a`

`"HR" : R`

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\*

`$\exists$  a : A,  $\Psi$  a * P`



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`P, R : iProp`

`$\Psi$  : A  $\rightarrow$  iProp`

`x : A`

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`"H $\Psi$ " :  $\Psi$  x`

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**Proof.**

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iIntros "[HP [H $\Psi$  HR]]".  
iDestruct "H $\Psi$ " as (x) "H $\Psi$ ".  
iExists x.
```

```
1 subgoal  
M : ucmraT  
A : Type  
P, R : iProp  
 $\Psi$  :  $A \rightarrow \text{iProp}$   
x : A
```

---

```
"HP" : P  
"H $\Psi$ " :  $\Psi$  x  
"HR" : R
```

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\*

```
 $\exists a : A, \Psi a$  * P
```

# Iris Proof Mode (IPM) demo

**Lemma** `and_exist_sep {A} P R ( $\Psi$ : A  $\rightarrow$  iProp) :`  
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```

```
1 subgoal  
M : ucmraT  
A : Type  
P, R : iProp  
 $\Psi$  : A  $\rightarrow$  iProp  
x : A
```

---

```
"HP" : P  
"H $\Psi$ " :  $\Psi$  x  
"HR" : R
```

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```
 $\Psi$  x * P
```

\*

# Iris Proof Mode (IPM) demo

**Lemma** `and_exist_sep {A} P R ( $\Psi$ : A  $\rightarrow$  iProp) :`  
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**Proof.**

```
iIntros "[HP [H $\Psi$  HR]]".
iDestruct "H $\Psi$ " as (x) "H $\Psi$ ".
iExists x.
iSplitL "H $\Psi$ ".
```

```
1 subgoal
M : ucmraT
A : Type
P, R : iProp
 $\Psi$  : A  $\rightarrow$  iProp
x : A
```

---

```
"HP" : P
"H $\Psi$ " :  $\Psi$  x
"HR" : R
```

---

$\Psi$  x \* P

# Iris Proof Mode (IPM) demo

**Lemma** `and_exist_sep {A} P R ( $\Psi$ : A  $\rightarrow$  iProp) :`  
`P * ( $\exists$  a,  $\Psi$  a) * R  $\multimap$   $\exists$  a,  $\Psi$  a * P.`

**Proof.**

```
iIntros "[HP [H $\Psi$  HR]]".
iDestruct "H $\Psi$ " as (x) "H $\Psi$ ".
iExists x.
iSplitL "H $\Psi$ ".
```

2 subgoals

`M : ucmraT`

`A : Type`

`P, R : iProp`

`$\Psi$  : A  $\rightarrow$  iProp`

`x : A`

---

(1/2)

`"H $\Psi$ " :  $\Psi$  x`

---

\*

`$\Psi$  x`

---

(2/2)

`"HP" : P`

`"HR" : R`

---

\*

`P`

# Iris Proof Mode (IPM) demo

**Lemma** `and_exist_sep {A} P R ( $\Psi$ : A  $\rightarrow$  iProp) :`  
`P * ( $\exists$  a,  $\Psi$  a) * R  $\multimap$   $\exists$  a,  $\Psi$  a * P.`

**Proof.**

```
iIntros "[HP [H $\Psi$  HR]]".  
iDestruct "H $\Psi$ " as (x) "H $\Psi$ ".  
iExists x.  
iSplitL "H $\Psi$ ".  
-
```

```
1 subgoal  
M : ucmraT  
A : Type  
P, R : iProp  
 $\Psi$  : A  $\rightarrow$  iProp  
x : A
```

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"H $\Psi$ " :  $\Psi$  x

---

\*

$\Psi$  x

# Iris Proof Mode (IPM) demo

**Lemma** `and_exist_sep {A} P R ( $\Psi$ : A  $\rightarrow$  iProp) :`  
`P * ( $\exists$  a,  $\Psi$  a) * R  $\multimap$   $\exists$  a,  $\Psi$  a * P.`

**Proof.**

```
iIntros "[HP [H $\Psi$  HR]]".  
iDestruct "H $\Psi$ " as (x) "H $\Psi$ ".  
iExists x.  
iSplitL "H $\Psi$ ".  
- iAssumption.
```

```
1 subgoal  
M : ucmraT  
A : Type  
P, R : iProp  
 $\Psi$  : A  $\rightarrow$  iProp  
x : A
```

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"H $\Psi$ " :  $\Psi$  x

---

\*

$\Psi$  x

# Iris Proof Mode (IPM) demo

**Lemma** `and_exist_sep {A} P R ( $\Psi$ :  $A \rightarrow \text{iProp}$ ) :`  
`P * ( $\exists a, \Psi a$ ) * R  $\multimap$   $\exists a, \Psi a$  * P.`

**Proof.**

```
iIntros "[HP [HΨ HR]]".  
iDestruct "HΨ" as (x) "HΨ".  
iExists x.  
iSplitL "HΨ".  
- iAssumption.
```

This subproof is complete, but there are some unfocused goals:

```
_____(1/1)  
"HP" : P  
"HR" : R  
_____*  
P
```



# Iris Proof Mode (IPM) demo

**Lemma** `and_exist_sep {A} P R ( $\Psi$ : A  $\rightarrow$  iProp) :`  
`P * ( $\exists$  a,  $\Psi$  a) * R  $\multimap$   $\exists$  a,  $\Psi$  a * P.`

**Proof.**

```
iIntros "[HP [H $\Psi$  HR]]".
iDestruct "H $\Psi$ " as (x) "H $\Psi$ ".
iExists x.
iSplitL "H $\Psi$ ".
- iAssumption.
-
```

```
1 subgoal
M : ucmraT
A : Type
P, R : iProp
 $\Psi$  : A  $\rightarrow$  iProp
x : A
```

---

```
"HP" : P
"HR" : R
```

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\*

P

# Iris Proof Mode (IPM) demo

**Lemma** `and_exist_sep {A} P R ( $\Psi$ : A  $\rightarrow$  iProp) :`  
`P * ( $\exists$  a,  $\Psi$  a) * R  $\multimap$   $\exists$  a,  $\Psi$  a * P.`

**Proof.**

```
iIntros "[HP [H $\Psi$  HR]]".
iDestruct "H $\Psi$ " as (x) "H $\Psi$ ".
iExists x.
iSplitL "H $\Psi$ ".
- iAssumption.
- iAssumption.
```

```
1 subgoal
M : ucmraT
A : Type
P, R : iProp
 $\Psi$  : A  $\rightarrow$  iProp
x : A
```

---

```
"HP" : P
"HR" : R
```

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\*

P

# Iris Proof Mode (IPM) demo

**Lemma** `and_exist_sep {A} P R ( $\Psi$ :  $A \rightarrow \text{iProp}$ ) :`      No more subgoals.

`P * ( $\exists a, \Psi a$ ) * R  $\multimap \exists a, \Psi a$  * P.`

**Proof.**

`iIntros "[HP [H $\Psi$  HR]]".`

`iDestruct "H $\Psi$ " as (x) "H $\Psi$ ".`

`iExists x.`

`iSplitL "H $\Psi$ ".`

`- iAssumption.`

`- iAssumption.`

# Iris Proof Mode (IPM) demo

**Lemma** `and_exist_sep {A} P R ( $\Psi$ :  $A \rightarrow \text{iProp}$ ) :`      No more subgoals.

`P * ( $\exists a, \Psi a$ ) * R  $\multimap$   $\exists a, \Psi a$  * P.`

**Proof.**

`iIntros "[HP [H $\Psi$  HR]]".`

`iDestruct "H $\Psi$ " as (x) "H $\Psi$ ".`

`iExists x.`

`iSplitL "H $\Psi$ ".`

`- iAssumption.`

`- iAssumption.`

**Qed.**

# Iris Proof Mode (IPM) demo

**Lemma** `and_exist_sep {A} P R ( $\Psi$ : A  $\rightarrow$  iProp) :`

`P * ( $\exists$  a,  $\Psi$  a) * R  $\rightarrow$   $\exists$  a,  $\Psi$  a * P.`

**Proof.**

`iIntros "[HP [H $\Psi$  HR]]".`

`iDest` Logical notations overridden in scope for Iris

`iExists x.`

`iSplitL "H $\Psi$ ".`

`- iAssumption.`

`- iAssumption.`

**Qed.**

# Iris Proof Mode (IPM) demo

**Lemma** `and_exist_sep {A} P R (Ψ: A → iProp) :`  
`P * (∃ a, Ψ a) * R →* ∃ a, Ψ a * P.`

**Proof.**

`iIntros "[HP [HΨ HR]]".`

1 subgoal

`M : ucmraT`

`A : Type`

`P, R : iProp`

`Ψ : A → iProp`

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`"HP" : P`

`"HΨ" : ∃ a : A, Ψ a`

`"HR" : R`

Notation for deeply embedded context

\*

`∃ a : A, Ψ a * P`

# Iris Proof Mode (IPM) demo

**Lemma** `and_exist_sep {A} P R (Ψ: A → iProp) :`  
`P * (∃ a, Ψ a) * R →* ∃ a, Ψ a * P.`

**Proof.**

`iIntros "[HP [HΨ HR]]".`

`Unset Printing Notations.`

1 subgoal

`M : ucmraT`

`A : Type`

`P, R : iProp`

`Ψ : A → iProp`

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`"HP" : P`

`"HΨ" : ∃ a : A, Ψ a`

`"HR" : R`

Notation for deeply embedded context

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`∃ a : A, Ψ a * P`

# Iris Proof Mode (IPM) demo

**Lemma** `and_exist_sep {A} P R ( $\Psi$ : A  $\rightarrow$  iProp) :`

`P * ( $\exists$  a,  $\Psi$  a) * R  $\multimap$   $\exists$  a,  $\Psi$  a * P.`

**Proof.**

`iIntros "[HP [H $\Psi$  HR]]".`

`Unset Printing Notations.`

`1 subgoal`

`M : ucmraT`

`A : Type@{Top.105}`

`P, R : uPred M`

`$\Psi$  : forall _ : A, uPred M`

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`@uPred_entails M`

`(@of_envs M`

`(@Envs M (@Enil (uPred M))`

`(@Esnoc (uPred M)`

`(@Esnoc (uPred M)`

`(@Esnoc (uPred M) (@Enil (uPred M))`

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`(Ascii false false false true false`

`false true`

`false)`

`(String`

`(Ascii false false false false true`

`false true`

`false) EmptyString)) P)`

`(String`



## Why should we care about interactive proofs? Why not automate everything?

Infeasible to automate everything, for example:

- ▶ The Rust type system (Jung, Jourdan, Krebbers, Dreyer)
- ▶ Logical relations (Krogh-Jespersen, Svendsen, Timany, Birkedal, Krebbers)
- ▶ Termination-preserving refinement (Tassarotti, Jung, Harper)
- ▶ Weak memory concurrency (Kaiser, Dang, Dreyer, Lahav, Vafeiadis)
- ▶ Object capability patterns (Swasey, Garg, Dreyer)
- ▶ Logical atomicity (Jung, Swasey, Krogh-Jespersen, Zhang, Dreyer, Birkedal)
- ▶ Defining Iris (Krebbers, Jung, Jourdan, Bizjak, Dreyer, Birkedal)

Most of these projects are formalized in IPM

## Coq demo

