

Interval of interest

Description



Motivation

A sequence of integers are given: i_1, i_2, \dots, i_n . Define the interval of interest (IOI) with respect to x , parameterized by $[l, r]$ subjected to: $\gcd(i_l, i_{l+1}, \dots, i_r) = x$, where $1 \leq l \leq r \leq n$.

Gcd here means the greatest common divisor.

Goal

Count all possible intervals with respect to $x = x_1, x_2, \dots, x_q$ for the given sequence i_1, i_2, \dots, i_n .

Interval of interest w.r.t 4				
	$l=2, r=4$		$x=4$	
15,	12,	24,	64,	12
i_1	i_2	i_3	i_4	i_5
	$l=2, r=5$		$x=4$	
15,	12,	24,	64,	12
	$l=3, r=5$		$x=4$	
15,	12	24,	64,	12
	$l=4, r=5$		$x=4$	
15,	12,	24,	64,	12
	$l=2, r=3$		$x=12$	
15,	12,	24,	64,	12
				$\Sigma=4$ w.r.t. $x=4$

Input

- The first line: an integer n , ($1 \leq n \leq 10^5$), indicating the length of the given sequence.
- Next line: n integers separated by space: i_1, i_2, \dots, i_n ($1 \leq i_j \leq 10^9$).
- The third line: an integer q , ($1 \leq q \leq 3 \cdot 10^5$), indicating the number of x s
- The forth line: q integers separated by space: x_1, x_2, \dots, x_q , ($1 \leq x_j \leq 10^9$).

Output

For each x , output the number of possible IOIs with respect to x_1, x_2, \dots

Sample Input 1

```
5
15 12 24 64 12
2
4 12
```

Sample Output 1

```
4 3
```

Hint

Observation1: $\gcd(a, b, c) = \gcd(\gcd(a, b), c)$

Observation2: for the sequence i_1, \dots, i_n , define the sequence $k_1=i_1, k_j=\gcd(k_{j-1}, i_j)$ for $2 \leq j \leq n$. The number of distinct values in k sequence is no more than $1 + \log_2\{i_1\}$.

Hint1: Divide & conquer may be useful:

- count IOIs at left half (by recursion)
- count IOIs at right half (by recursion)
- merge and conut intervals that start from the left half and end at right half (how to count efficiently?, hint: observation 2)

Hint2: try to set a AVL tree / hash, count gcd for all x in one time.

Hint3: the solution of $n \log n$ is possible

Problems

Announcements

Submissions

Rankings

View Contest

Information

ID	401
Time Limit	1000MS
Memory Limit	128MB
IO Mode	Standard IO
Created By	root
Level	High
Score	100
Tags	Show

Statistic

Details

