

Team Contest Reference

Universität zu Lübeck

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1 Mathematische Algorithmen

1.1 Primzahlen

1.1.1 Sieb des Eratosthenes

```
1 static boolean[] sieve(int until) {  
2     boolean[] a = new boolean[until + 1];  
3     Arrays.fill(a, true);  
4     for (int i = 2; i < Math.sqrt(a.length); i++) {  
5         if (a[i]) {  
6             for (int j = i * i; j < a.length; j += i) a[j] = false;  
7         }  
8     }  
9     return a; // a[i] == true, iff. i is prime. a[0] is ignored  
10 }
```

2 Mathematisch Formeln und Gesetze

2.1 Catalan

$$C_n = \frac{1}{n+1} \binom{2n}{n} = \prod_{k=2}^n (n+k)/k$$

2.2 kgV und ggT

$$ggT(n, m) \cdot kgV(m, n) = |m \cdot n|$$

2.3 Kreuzprodukt

$$\vec{a} \times \vec{b} = \begin{pmatrix} a_1 \\ a_2 \\ a_3 \end{pmatrix} \times \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix} = \begin{pmatrix} a_2 b_3 - a_3 b_2 \\ a_3 b_1 - a_1 b_3 \\ a_1 b_2 - a_2 b_1 \end{pmatrix}$$

2.4 Orthogonale Projektion

r_0 : Ortsvektor; u : Richtungsvektor; n : Normalenvektor

$$P_g(\vec{x}) = \vec{r}_0 + \frac{(\vec{x} - \vec{r}_0) \cdot \vec{u}}{\vec{u} \cdot \vec{u}} \vec{u}$$

$$P_g(\vec{x}) = \vec{x} - \frac{(\vec{x} - \vec{r}_0) \cdot \vec{n}}{\vec{n} \cdot \vec{n}} \vec{n} \text{ (nur 2D bzw. 3D auf Ebene)}$$

3 Datenstrukturen

3.1 Fenwick Tree (Binary Indexed Tree)

```
1 class FenwickTree {
2     private int[] values;
3     private int n;
4     public FenwickTree(int n) {
5         this.n = n;
6         values = new int[n];
7     }
8     public int get(int i) { //get value of i
9         int x = values[0];
10        while (i > 0) {
11            x += values[i];
12            i -= i & -i; }
13        return x;
14    }
15    public void add(int i, int x) { // add x to interval [i,n]
16        if (i == 0) values[0] += x;
17        else {
18            while (i < n) {
19                values[i] += x;
20                i += i & -i; }
21        }
22    }
23 }
```

4 Graphenalgorithmen

4.1 Topologische Sortierung

```
1 static List<Integer> topoSort(Map<Integer, List<Integer>> edges,
2     Map<Integer, List<Integer>> revedges) {
3     Queue<Integer> q = new LinkedList<Integer>();
4     List<Integer> ret = new LinkedList<Integer>();
5     Map<Integer, Integer> indeg = new HashMap<Integer, Integer>();
6     for (int v : revedges.keySet()) {
7         indeg.put(v, revedges.get(v).size());
8         if (revedges.get(v).size() == 0)
9             q.add(v);
10    }
11    while (!q.isEmpty()) {
12        int tmp = q.poll();
13        ret.add(tmp);
14        for (int dest : edges.get(tmp)) {
15            indeg.put(dest, indeg.get(dest) - 1);
16            if (indeg.get(dest) == 0)
17                q.add(dest);
18        }
19    }
20    return ret;
21 }
```

4.2 Prim (Minimum Spanning Tree)

```
1 #define WHITE 0
2 #define BLACK 1
3 #define INF INT_MAX
4
```

```

5 int baum( int **matrix, int N){
6     int i, sum = 0;
7
8     int color[N];
9     int dist[N];
10
11     // markiere alle Knoten ausser 0 als unbesucht
12     color[0] = BLACK;
13     for( i=1; i<N; i++){
14         color[i] = WHITE;
15         dist[i] = INF;
16     }
17
18     // berechne den Rand
19     for( i=1; i<N; i++){
20         if( dist[i] > matrix[i][nextIndex]){
21             dist[i] = matrix[i][nextIndex];
22         }
23     }
24
25     while( 1){
26         int nextDist = INF, nextIndex = -1;
27
28         /* Den naechsten Knoten waehlen */
29         for(i=0; i<N; i++){
30             if( color[i] != WHITE) continue;
31
32             if( dist[i] < nextDist){
33                 nextDist = dist[i];
34                 nextIndex = i;
35             }
36         }
37
38         /* Abbruchbedingung*/
39         if( nextIndex == -1) break;
40
41         /* Knoten in MST aufnehmen */
42         color[nextIndex] = RED;
43         sum += nextDist;
44
45         /* naechste kuerzeste Distanzen berechnen */
46         for( i=0; i<N; i++){
47             if( i == nextIndex || color[i] == BLACK ) continue;
48
49             if( dist[i] > matrix[i][nextIndex]){
50                 dist[i] = matrix[i][nextIndex];
51             }
52         }
53     }
54
55     return sum;
56 }

```

5 Geometrische Algorithmen

5.1 Graham Scan (Convex Hull)

```

1 static List<P> graham(List<P> l) {
2     if (l.size() < 3)
3         return l;
4     P temp = l.get(0);

```

```

5  for (P p : l)
6      if (temp.y > p.y || temp.y == p.y && temp.x > p.x)
7          temp = p;
8  final P start = temp; // min y (then leftmost)
9
10 Collections.sort(l, new Comparator<P>() {
11     public int compare(P o1, P o2) {
12         if (new Double(Math.atan2(o1.y - start.y, o1.x - start.x)) // same angle
13             .compareTo(Math.atan2(o2.y - start.y, o2.x - start.x)) == 0)
14             return new Double(Math.sqrt((o1.x - start.x)
15                 * (o1.x - start.x) + (o1.y - start.y)
16                 * (o1.y - start.y))).compareTo((o2.x - start.x)
17                 * (o2.x - start.x) + (o2.y - start.y)
18                 * (o2.y - start.y)); // use distance
19             return new Double(Math.atan2(o1.y - start.y, o1.x - start.x))
20                 .compareTo(Math.atan2(o2.y - start.y, o2.x - start.x));
21     }
22 });
23 Stack<P> s = new Stack<P>();
24 s.add(start);
25 s.add(l.get(1));
26 for (int i = 2; i < l.size(); i++) {
27     while (s.size() >= 2
28         && ccw(s.get(s.size() - 2), s.get(s.size() - 1), l.get(i)) <= 0)
29         s.pop();
30     s.push(l.get(i));
31 }
32 return s;
33 }
34
35 // turn is counter-clockwise if > 0; collinear if = 0; clockwise else
36 static double ccw(P p1, P p2, P p3) {
37     return (p2.x - p1.x) * (p3.y - p1.y) - (p2.y - p1.y) * (p3.x - p1.x);
38 }
39
40 public static class P {
41     double x, y;
42
43     P(double x, double y) {
44         this.x = x;
45         this.y = y;
46     }
47     // polar coordinates (not used)
48     // double r() { return Math.sqrt(x * x + y * y); }
49     // double d() { return Math.atan2(y, x); }
50 }

```

6 Verschiedenes

6.1 Potenzmenge

```

1 static <T> Iterator<List<T>> powerSet(final List<T> l) {
2     return new Iterator<List<T>>() {
3         int i; // careful: i becomes 2^l.size()
4         public boolean hasNext() {
5             return i < (1 << l.size());
6         }
7         public List<T> next() {
8             Vector<T> temp = new Vector<T>();
9             for (int j = 0; j < l.size(); j++)
10                 if (((i >>> j) & 1) == 1)

```

```

11         temp.add(l.get(j));
12         i++;
13         return temp;
14     }
15     public void remove() {}
16 };
17 }

```

6.2 LongestCommonSubsequence

```

1  #include <iostream>
2  #include <vector>
3  #include <string>
4  #include <sstream>
5  #include <algorithm>
6  #include <iterator>
7  using namespace std;
8
9  #define MAX(a,b) (a > b) ? a : b
10
11 string X,Y;
12 vector< vector<int> > c(101, vector<int>(101,0));
13 int m,n,ctr;
14
15 int LCS()
16 {
17     m = X.length(),n=Y.length();
18
19     c.resize(m+1);
20     for(int i = 0; i<n+1; i++) {
21         c[i].resize(n+1);
22         c[i][0] = 0;
23     }
24
25     int i,j;
26
27     for (i=0;i<=m;i++)
28         for (j=0;j<=n;j++)
29             c[i][j]=0;
30
31     for (i=1;i<=m;i++)
32         for (j=1;j<=n;j++)
33         {
34             if (X[i-1]==Y[j-1])
35                 c[i][j]=c[i-1][j-1]+1;
36             else
37                 c[i][j]=max(c[i][j-1],c[i-1][j]);
38         }
39     return c[m][n];
40 }
41 /** Print a songle LCS */
42 void printLCS(int i,int j)
43 {
44     if (i==0 || j==0)
45         return;
46     if (X[i-1]==Y[j-1])
47     {
48         printLCS(i-1,j-1);
49         cout<<X[i-1];
50     }
51     else if (c[i][j]==c[i-1][j])
52         printLCS(i-1,j);

```

```

53     else
54         printLCS(i,j-1);
55 }
56
57 int main()
58 {
59     while(cin>>X>>Y)
60     {
61         cout << "Length:_" << LCS() << endl;
62         printLCS(m,n);
63         cout<<endl ;
64     }
65 }

```

6.3 LongestCommonSubstring

6.4 Permutation & Sequenzen

```

1  import java.util.Scanner;
2
3  public class PermsAndSequ {
4      public static void main(String[] args) {
5          Scanner sc = new Scanner(System.in);
6          int n;
7          while ((n = sc.nextInt()) != 0) {
8              int k = sc.nextInt();
9              Sequences(n, k);
10             Permutations(n);
11         }
12
13     }
14
15     public static void Sequences(int n, int k) {
16         int[] x = new int[k];
17         for (int i = 0; i < k; i++)
18             x[i] = 1;
19         Print(x);
20         while (true) {
21             boolean lastX = true;
22             for (int i = 0; i < k; i++)
23                 if (x[i] != n) {
24                     lastX = false;
25                     break;
26                 }
27             if (lastX)
28                 break;
29             int p = k - 1;
30             while (!(x[p] < n))
31                 p--;
32             x[p] = x[p] + 1;
33             for (int i = p + 1; i < k; i++)
34                 x[i] = 1;
35             Print(x);
36         }
37     }
38
39     public static void Permutations(int n) {
40         int[] x = new int[n];
41         for (int i = 0; i < n; i++)
42             x[i] = i + 1;
43         Print(x);
44         while (true) {

```

```

45     boolean lastX = true;
46     for (int i = 0; i < n - 1; i++)
47         if (x[i] < x[i + 1]) {
48             lastX = false;
49             break;
50         }
51     if (lastX)
52         break;
53     int k = n - 1 - 1;
54
55     while (x[k] > x[k + 1])
56         k--;
57     int t = k + 1;
58
59     while (t < (n - 1) && x[t + 1] > x[k])
60         t++;
61
62     int tmp = x[k];
63     x[k] = x[t];
64     x[t] = tmp;
65     // reverse x[k+1] ... x[n-1]
66
67     for (int i = 0; i <= ((n - 1) - (k + 1)) / 2; i++) {
68         tmp = x[k + 1 + i];
69         x[k + 1 + i] = x[n - 1 - i];
70         x[n - 1 - i] = tmp;
71     }
72     Print(x);
73 }
74 }
75
76
77 public static void Print(int[] x) {
78     for (int i = 0; i < x.length; i++)
79         System.out.print(x[i] + " ");
80     System.out.println("");
81 }
82
83 }

```