Team Contest Reference

Universität zu Lübeck

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1 Mathematische Algorithmen

1.1 Primzahlen

1.1.1 Sieb des Eratosthenes

```
static boolean[] sieve(int until) {
  boolean[] a = new boolean[until + 1];
  Arrays.fill(a, true);
  for (int i = 2; i < Math.sqrt(a.length); i++) {
    if (a[i]) {
      for (int j = i * i; j < a.length; j += i) a[j] = false;
    }
  }
  return a; // a[i] == true, iff. i is prime. a[0] is ignored
}
```

1.1.2 Primzahlentest

```
static boolean isPrim(int p) {
  if (p < 2 || p > 2 && p % 2 == 0) return false;
  for (int i = 3; i <= Math.sqrt(p); i += 2)
    if (p % i == 0) return false;
  return true;
}
```

1.2 Binomial Koeffizient

```
static int[][] mem = new int[MAX_N][(MAX_N + 1) / 2];
static int binoCo(int n, int k) {
  if (k < 0 || k > n) return 0;
  if (2 * k > n) binoCo(n, n - k);
  if (mem[n][k] > 0) return mem[n][k];
  int ret = 1;
  for (int i = 1; i <= k; i++) {
    ret *= n - k + i;
    ret /= i;
    mem[n][i] = ret;
  }
  return ret;
}
```

2 Datenstukturen

2.1 Fenwick Tree (Binary Indexed Tree)

```
class FenwickTree {
  private int[] values;
  private int n;
  public FenwickTree(int n) {
    this.n = n;
    values = new int[n];
  }
  public int get(int i) { //get value of i
    int x = values[0];
    while (i > 0) {
      x += values[i];
      i -= i & -i; }
    return x;
  }
  public void add(int i, int x) { // add x to interval [i,n]
    if (i == 0) values[0] += x;
    else {
      while (i < n) {
        values[i] += x;
        i += i & -i; }
    }
  }
}
```

3 Graphenalgorithmen

3.1 Topologische Sortierung

```
static List<Integer> topoSort(Map<Integer, List<Integer>> edges,
    Map<Integer, List<Integer>> revedges) {
  Queue<Integer> q = new LinkedList<Integer>();
  List<Integer> ret = new LinkedList<Integer>();
  Map<Integer, Integer> indeg = new HashMap<Integer, Integer>();
  for (int v : revedges.keySet()) {
    indeg.put(v, revedges.get(v).size());
    if (revedges.get(v).size() == 0)
      q.add(v);
  }
  while (!q.isEmpty()) {
    int tmp = q.poll();
    ret.add(tmp);
    for (int dest : edges.get(tmp)) {
      indeg.put(dest, indeg.get(dest) - 1);
      if (indeg.get(dest) == 0)
        q.add(dest);
    }
  }
  return ret;
}
```

3.2 Prim (Minimum Spanning Tree)

```
#define WHITE 0
#define BLACK 1
#define INF INT_MAX

int baum( int **matrix, int N){
  int i, sum = 0;

  int color[N];
  int dist[N];
```

```
10
11      // markiere alle Knoten ausser 0 als unbesucht
12    color[0] = BLACK;
13    for( i=1; i<N; i++){
14      color[i] = WHITE;
15      dist[i] = INF;
16    }
17
18      // berechne den Rand
19    for( i=1; i<N; i++){
20          if( dist[i] > matrix[i][nextIndex]){
21              dist[i] = matrix[i][nextIndex];
22          }
23      }
24
25    while( 1){
26      int nextDist = INF, nextIndex = -1;
27
28      /* Den naechsten Knoten waehlen */
29      for(i=0; i<N; i++){
30        if( color[i] != WHITE) continue;
31
32        if( dist[i] < nextDist){
33          nextDist = dist[i];
34          nextIndex = i;
35        }
36      }
37
38      /* Abbruchbedingung*/
39      if( nextIndex == -1) break;
40
41      /* Knoten in MST aufnehmen */
42      color[nextIndex] = RED;
43      sum += nextDist;
44
45      /* naechste kuerzeste Distanzen berechnen */
46      for( i=0; i<N; i++){
47              if( i == nextIndex || color[i] == BLACK ) continue;
48
49              if( dist[i] > matrix[i][nextIndex]){
50                  dist[i] = matrix[i][nextIndex];
51              }
52      }
53    }
54
55    return sum;
56  }
```

4 Geometrische Algorithmen

4.1 Graham Scan (Convex Hull)

```
1  static List<P> graham(List<P> l) {
2    if (l.size() < 3)
3      return l;
4    P temp = l.get(0);
5    for (P p : l)
6      if (temp.y > p.y || temp.y == p.y && temp.x > p.x)
7        temp = p;
8    final P start = temp; // min y (then leftmost)
9
```

```
  Collections.sort(l, new Comparator<P>() {
    public int compare(P o1, P o2) {
      if (new Double(Math.atan2(o1.y - start.y, o1.x - start.x)) // same angle
          .compareTo(Math.atan2(o2.y - start.y, o2.x - start.x)) == 0)
        return new Double(Math.sqrt((o1.x - start.x)
            * (o1.x - start.x) + (o1.y - start.y)
            * (o1.y - start.y))).compareTo((o2.x - start.x)
            * (o2.x - start.x) + (o2.y - start.y)
            * (o2.y - start.y)); // use distance
      return new Double(Math.atan2(o1.y - start.y, o1.x - start.x))
          .compareTo(Math.atan2(o2.y - start.y, o2.x - start.x));
    }
  });
  Stack<P> s = new Stack<P>();
  s.add(start);
  s.add(l.get(1));
  for (int i = 2; i < l.size(); i++) {
    while (s.size() >= 2
        && ccw(s.get(s.size() - 2), s.get(s.size() - 1), l.get(i)) <= 0)
      s.pop();
    s.push(l.get(i));
  }
  return s;
}

// turn is counter-clockwise if > 0; collinear if = 0; clockwise else
static double ccw(P p1, P p2, P p3) {
  return (p2.x - p1.x) * (p3.y - p1.y) - (p2.y - p1.y) * (p3.x - p1.x);
}

public static class P {
  double x, y;

  P(double x, double y) {
    this.x = x;
    this.y = y;
  }
  // polar coordinates (not used)
  // double r() { return Math.sqrt(x * x + y * y); }
  // double d() { return Math.atan2(y, x); }
}
```

5 Verschiedenes

5.1 Potenzmenge

```
static <T> Iterator<List<T>> powerSet(final List<T> l) {
  return new Iterator<List<T>>() {
    int i; // careful: i becomes 2^l.size()
    public boolean hasNext() {
      return i < (1 << l.size());
    }
    public List<T> next() {
      Vector<T> temp = new Vector<T>();
      for (int j = 0; j < l.size(); j++)
        if (((i >>> j) & 1) == 1)
          temp.add(l.get(j));
      i++;
      return temp;
    }
    public void remove() {}
```

```
16          };
17      }
```