SDM4 in R: Multiple Regression (Chapter 28)

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Introduction and background

This document is intended to help describe how to undertake analyses introduced as examples in the Fourth Edition of *Stats: Data and Models* (2014) by De Veaux, Velleman, and Bock. More information about the book can be found at http://wps.aw.com/aw_deveaux_stats_series. This file as well as the associated R Markdown reproducible analysis source file used to create it can be found at http://www.amherst.edu/~nhorton/sdm4.

This work leverages initiatives undertaken by Project MOSAIC (http://www.mosaic-web.org), an NSF-funded effort to improve the teaching of statistics, calculus, science and computing in the undergraduate curriculum. In particular, we utilize the mosaic package, which was written to simplify the use of R for introductory statistics courses. A short summary of the R needed to teach introductory statistics can be found in the mosaic package vignettes (http://cran.r-project.org/web/packages/mosaic).

Chapter 28: Multiple Regression

Section 28.1: What is multiple regression?

The table on page 818 displays the results from the multiple regression model.

```
library(mosaic); library(readr)
options(digits=3)
BodyFat <- read_csv("http://www.amherst.edu/~nhorton/sdm4/data/Body_fat_complete.csv")
BodyFatmod <- lm(PctBF ~ waist + Height, data=BodyFat)
msummary(BodyFatmod)</pre>
```

```
##
               Estimate Std. Error t value Pr(>|t|)
               -3.1009
                            7.6861
                                     -0.40
## (Intercept)
                                               0.69
## waist
                 1.7731
                            0.0716
                                     24.77 < 2e-16 ***
## Height
                -0.6015
                            0.1099
                                     -5.47 1.1e-07 ***
##
## Residual standard error: 4.46 on 247 degrees of freedom
## Multiple R-squared: 0.713, Adjusted R-squared: 0.711
## F-statistic: 307 on 2 and 247 DF, p-value: <2e-16
```

Section 28.2: Interpreting multiple regression coefficients

Figure 28.1 on page 819 displays the scatterplot of percent body fat against height.

```
xyplot(PctBF ~ Height, type=c("p", "r"), data=BodyFat)
```

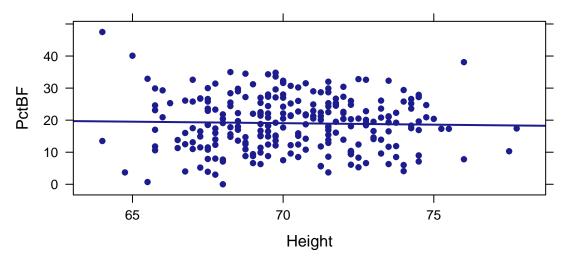
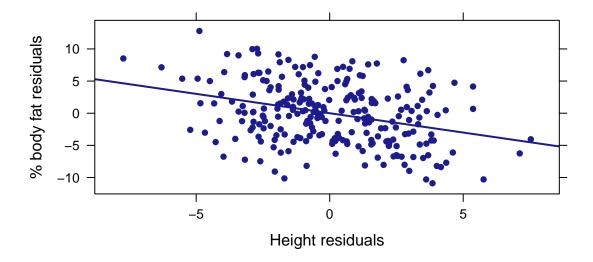


Figure 28.2 (page 820) displays the scatterplot for a subset of the data (men with waist sizes between 36 and 38 inches).

Figure 28.3 (page 820) displays the partial regression plot for weight.

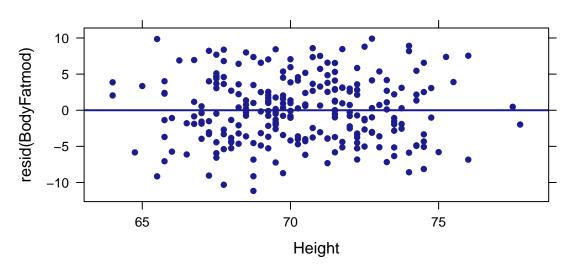
Height



Section 28.3: The multiple regression model (assumptions and conditions)

Figure 28.4 (page 822) displays scatterplots of residuals vs. height and waist, respectively.





xyplot(resid(BodyFatmod) ~ waist, type=c("p", "r"), data=BodyFat)

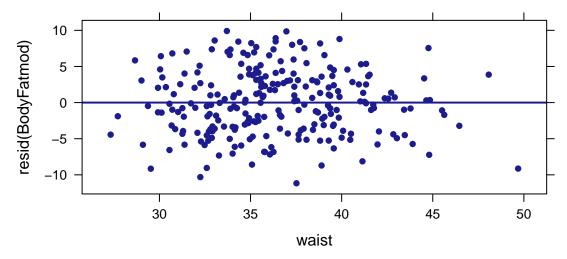
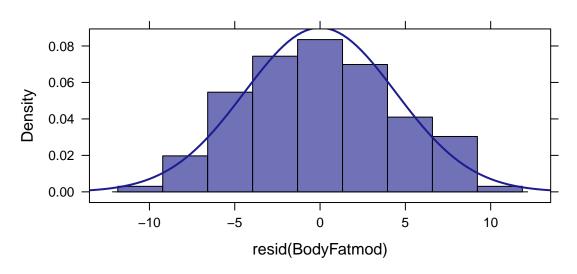
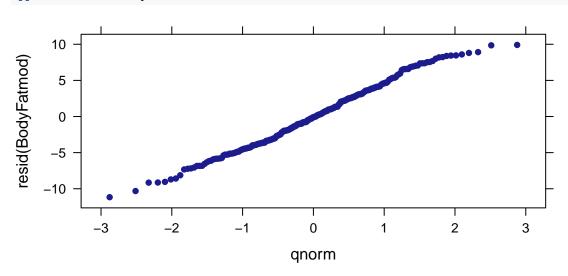


Figure 28.5 (page 823) displays histogram and qq plot of the residuals.

histogram(~ resid(BodyFatmod), fit="normal")



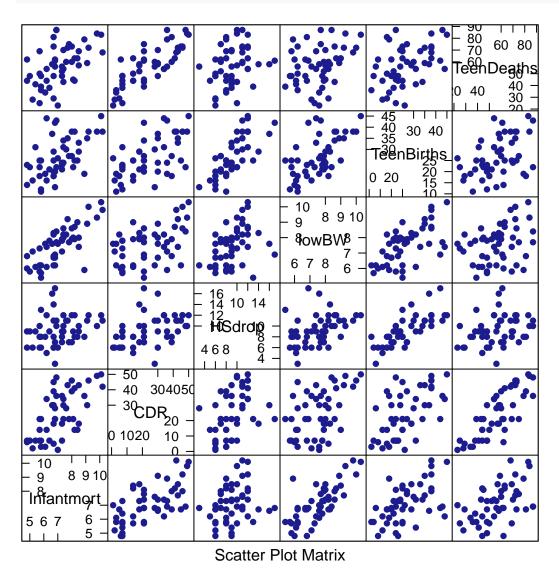
qqmath(~ resid(BodyFatmod))



Section 28.4: Multiple regression inference

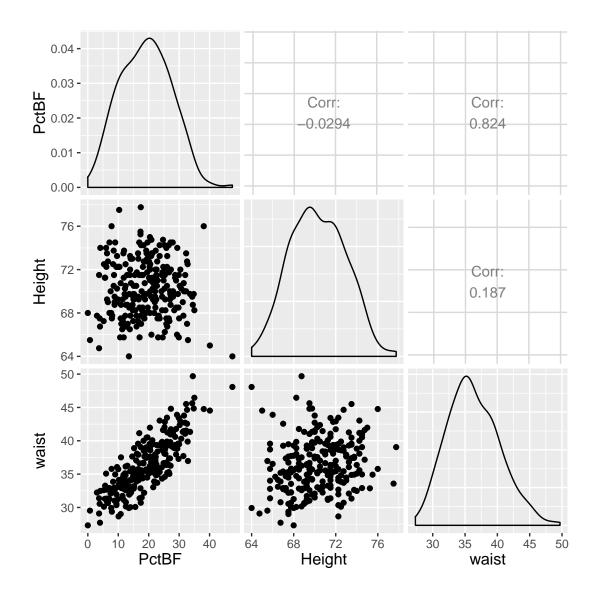
Figure 28.6 (page 829) displays the scatterplot matrix infant mortality data.

InfantMortality <- read_csv("http://www.amherst.edu/~nhorton/sdm4/data/Infant_Mortality.csv")
splom(select(InfantMortality, -State))</pre>



In addition, we display a scatterplot matrix for the motivating example from the chapter (BodyFat) using the GGally package.

```
subsetBodyFat <- select(BodyFat, PctBF, Height, waist)
library(GGally)
ggpairs(subsetBodyFat)</pre>
```



Section 28.5: Comparing multiple regression models

We may want to compare which of our models provides the most parsimonious fit to these data.

msummary(BodyFatheight)

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 65.8864    1.4848    44.37    <2e-16 ***
## waist    0.1216    0.0406    2.99    0.003 **
##
## Residual standard error: 2.58 on 248 degrees of freedom
## Multiple R-squared: 0.0349, Adjusted R-squared: 0.031
## F-statistic: 8.96 on 1 and 248 DF, p-value: 0.00305</pre>
```

msummary(BodyFatwaist)

##

Estimate Std. Error t value Pr(>|t|)

```
## (Intercept) -42.7341     2.7165   -15.7     <2e-16 ***
## waist     1.7000     0.0743     22.9     <2e-16 ***
##
## Residual standard error: 4.71 on 248 degrees of freedom
## Multiple R-squared: 0.678, Adjusted R-squared: 0.677
## F-statistic: 523 on 1 and 248 DF, p-value: <2e-16</pre>
```

msummary(BodyFatmod)

```
Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -3.1009
                           7.6861
                                    -0.40
                                              0.69
                1.7731
                           0.0716
                                    24.77 < 2e-16 ***
## waist
## Height
               -0.6015
                           0.1099
                                    -5.47 1.1e-07 ***
##
## Residual standard error: 4.46 on 247 degrees of freedom
## Multiple R-squared: 0.713, Adjusted R-squared: 0.711
## F-statistic: 307 on 2 and 247 DF, p-value: <2e-16
```

The adjusted R-squared value of 0.711 is considerably higher for the model with both predictors (though the model with just waist has an adjusted R-squared value of 0.677).