

Data Structure & Algorithms 1

CHAPTER 2: CONTROL STRUCTURE

Sep – Dec 2023

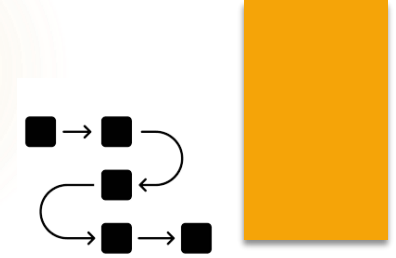
Algorithm: Control Structure

1. Sequencing 

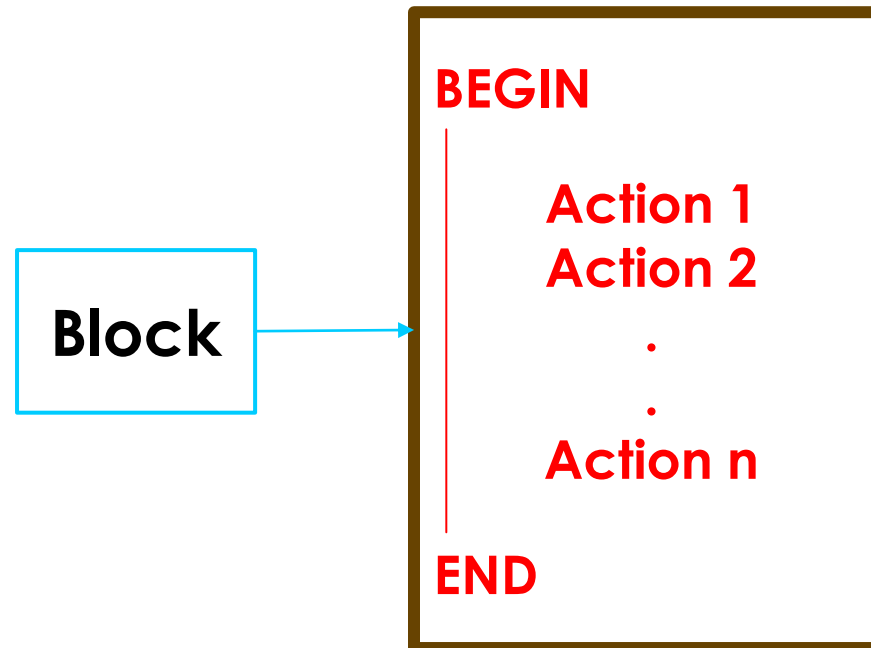
2. Conditional and Alternative 

3. Repetitive 

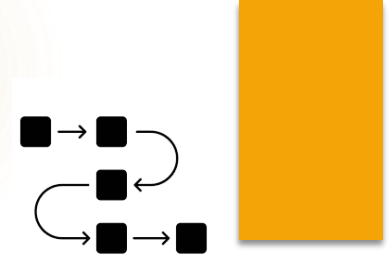
Algorithm: Control Structure



1. **Sequencing:** Primitive actions are executed **in the order in which they appear** in the algorithm.



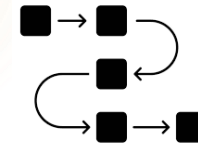
Algorithm: Control Structure



Sequencing Example

- ▶ Create an algorithm that, based on an amount excluding taxes (MontHT), displays the amount to be paid including all taxes (MontTTC), considering that a tax (VAT) is applied to the amount excluding taxes.
- ▶ To calculate the total amount including taxes (what the customer will pay) based on an amount excluding taxes: **$\text{MontTTC} = \text{MontHT} * (1 + \text{VAT}/100)$**
- ▶ **Example** with a 20% VAT:
 - ▶ $\text{MontTTC} = \text{MontHT} * (1 + 20/100)$
 - ▶ $\text{MontTTC} = \text{MontHT} * 1.2$

Algorithm: Control Structure



Algorithm Calculate_Invoice

Constant VAT = 20

Variables Real NetAmount, GrossAmount

BEGIN

WRITE ('Enter the Net Amount: ')

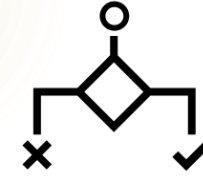
READ (NetAmount)

GrossAmount = NetAmount * (1 + VAT/100)

WRITE ('The Gross Amount is: ', GrossAmount)

END

Algorithm: Control Structure



1. **Conditional:** If the condition is met, execute the block; otherwise, continue sequentially.

IF Logical_expression **THEN**

Block

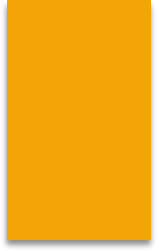
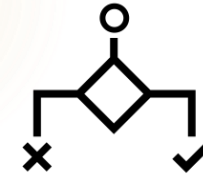
END IF

Next instruction

Evaluate the logical expression:

- **IF** the logical expression is **TRUE**, then the **Block** is executed.
- Otherwise, **IF** the logical expression is **FALSE**, we proceed sequentially (**Next Instruction**)

Algorithm: Control Structure



1. **Alternative:** If the condition is not met, execute the **else** block.

IF Logical_expression **THEN**

Block1

ELSE

Block2

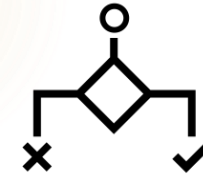
ENDIF

Next instruction

Evaluate the logical expression:

- **IF** the logical expression is **TRUE**, then the **Block1** is executed and then we proceed to **Next Instruction**
- **ELSE**, i.e., logical expression is **FALSE**, so execute **block2** and then **Next Instruction**

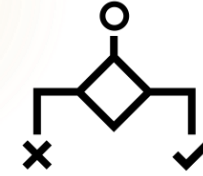
Algorithm: Control Structure



Remarks:

1. The conditional statement is a specific case of the alternative statement;
2. A block is a coherent set composed of 1 or more actions. Intended under the **IF** statement.

Algorithm: Control Structure



Example 1: Conditional and Alternative

.....

Go straight until the next intersection.

IF the right street is open to traffic **THEN**

 Turn right

 Continue forward

 Take the second left

ELSE

 Keep going until the next right street

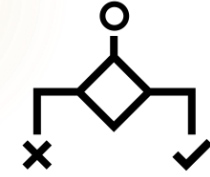
 Take that street

 Take the first right

ENDIF

.....

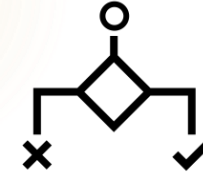
Algorithm: Control Structure



Example2: Conditional and Alternative

Write an algorithm that, given an **amount**, **displays** the **amount to be paid**, considering a 10% discount for any amount greater than or equal to 3500 DZD

Algorithm: Control Structure



Example2: First solution

Algorithm AmountToPay

Constant discount = 0.10

Variables Real InitAmount, AmountToPay

BEGIN

READ (InitAmount)

IF InitAmount >= 3500 **THEN**

AmountToPay = InitAmount * (1 - discount)

ELSE

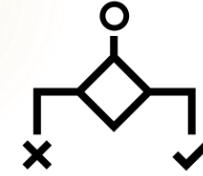
AmountToPay = InitAmount

ENDIF

WRITE (AmountToPay)

END

Algorithm: Control Structure



Example2: Second solution

Algorithm AmountToPay

Constant discount = 0.10

Variables Real InitAmount, AmountToPay

BEGIN

READ (InitAmount)

 AmountToPay = InitAmount

IF InitAmount >= 3500 **THEN**

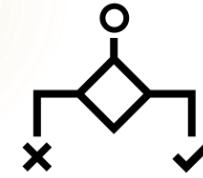
 AmountToPay = InitAmount * (1 - discount)

ENDIF

WRITE (AmountToPay)

END

Algorithm: Control Structure



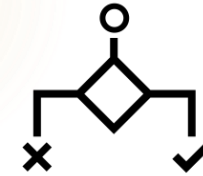
Example3:

IF... ELSE statement opens **two** paths, corresponding to **two** different processes.

However, there are many situations where **two** paths are **not sufficient**.

For example, a program that needs to determine the state of water based on its temperature should be able to choose from **three** possible responses (solid, liquid, or gaseous).

Algorithm: Control Structure



Example3:

ANALYSIS: First Solution

- ▶ Let Temp be the water temperature.
- ▶ Start by reading the temperature, Temp.
- ▶ Check if Temp is less than or equal to 0; if true, display that it is ice.
- ▶ Check if (Temp is greater than 0 and Temp is less than or equal to 100); if true, display that it is liquid.
- ▶ Check if Temp is greater than 100; if true, display that it is vapor.

Algorithm TempV1

Variables Integer Temp

BEGIN

WRITE ('Provide the temperature: ')

READ (Temp)

IF temp <= 0 THEN

WRITE ('Ice')

ENDIF

IF (temp > 0) AND (Temp <=100) THEN

WRITE ('Liquid')

ENDIF

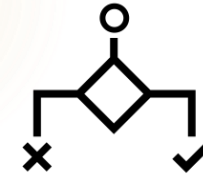
IF temp > 100 THEN

WRITE ('Vapor')

ENDIF

END

Algorithm: Control Structure



Example3:

Remarks about the first solution

You will notice that this is a bit cumbersome. The conditions are somewhat similar, and most importantly, we force the machine to examine three successive tests, all of which concern the same thing: the water temperature (the value of the variable Temp).

- It would be much more rational to **nest** the tests in this way,

Algorithm TempV1

Variables Integer Temp

BEGIN

WRITE ('Provide the temperature: ')

READ (Temp)

IF temp <= 0 THEN

WRITE ('Ice')

ELSE

IF Temp <=100 THEN

WRITE ('Liquid')

ELSE

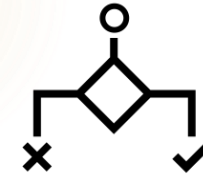
WRITE ('Vapor')

ENDIF

ENDIF

END

Algorithm: Control Structure



Example3:

Remarks about the second solution

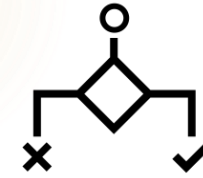
We have made savings: instead of having to type *three* conditions, one of which is compound, we now have only *two* simple conditions. But more importantly, we have *saved* on the computer's **execution time**.

If the temperature is below zero, it writes "It's ice" and goes directly to the end without being slowed down by the examination of other possibilities (which are necessarily false).

This second version is not only simpler to write and more readable but also more efficient in execution.

Nested testing structures are therefore an indispensable tool for simplifying and optimizing algorithms.

Algorithm: Control Structure

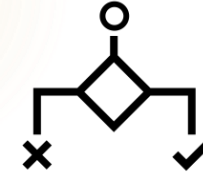


Example4:

It is about reading 3 integers **A, B, C** and **sorting** them in **ascending** order, which means putting the smallest value in A and the largest value in C.

► **Two** different solutions with two different analyses.

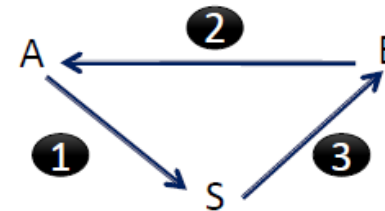
Algorithm: Control Structure



Example4:

ANALYSIS: First Solution

- ▶ Let A, B, and C be three integers.
- ▶ We compare A and B, and if they are out of order, we swap A and B.
- ▶ Next, we compare B and C, and if they are out of order, we swap B and C.
- ▶ Finally, we compare A and B again, and if they are out of order, we swap A and B.
- ▶ To swap two variables, we use a third variable S to temporarily store the value of one and perform the swap.



Algorithm Sorting

Variables Integer A, B, C, S

BEGIN

READ (A, B, C)

IF A > B **THEN**

S = A

A = B

B = S

ENDIF

IF B > C **THEN**

S = C

B = C

C = S

ENDIF

IF A > B **THEN**

S = A

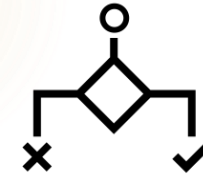
A = B

B = S

ENDIF

END

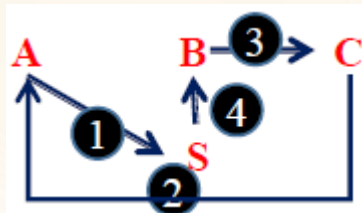
Algorithm: Control Structure



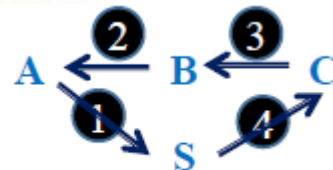
Example4:

ANALYSIS: Second Solution

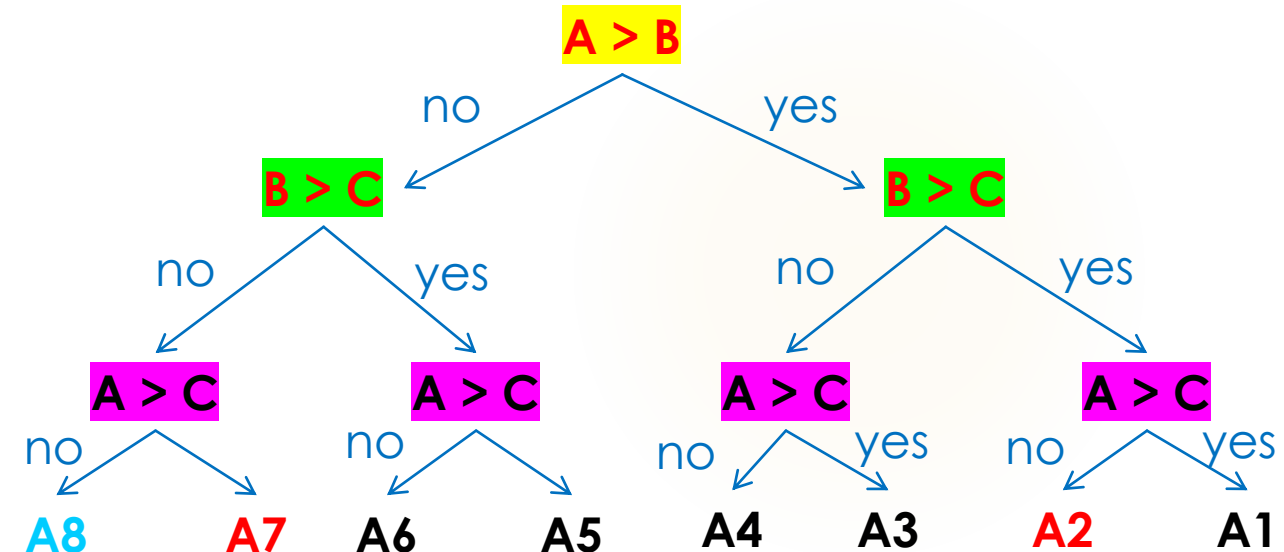
- ▶ Let A, B, and C be three integers.
- ▶ We compare **A and B**, then **B and C**, then **A and C**.
- ▶ Next, we decide about the action to take once **all** the comparisons are done.



Right circular swapping



Left circular swapping



A1 : 8 5 4 - Swap A and C

A2 : impossible

A3 : 8 5 6 – Left circular swapping

A4 : 8 5 9 - Swap A and B

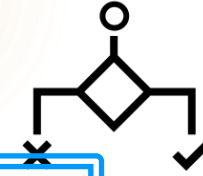
A5 : 5 8 4 – Right circular swapping

A6 : 5 8 6 – Swap B and C

A7 : impossible

A8 : 5 6 8 Do nothing

Algorithm: Control Structure



Example4:

A1 : 8 5 4 - Swap A and C

A2 : impossible

A3 : 8 5 6 – Left circular swapping

A4 : 8 5 9 - Swap A and B

A5 : 5 8 4 – Right circular swapping

A6 : 5 8 6 – Swap B and C

A7 : impossible

A8 : 5 6 8 Do nothing

Algorithm Sorting

Variables Integer A, B, C, S

BEGIN

READ (A, B, C)

IF A > B **THEN**

IF B > C **THEN**

A1

S = A
A = C
C = S

ELSE

IF A > C **THEN**

A3

S = A
A = B
B = C
C = S

ELSE

A4

ENDIF

ENDIF

ELSE

IF B > C **THEN**

IF A > C **THEN**

A5

S = A
A = C
C = B
B = S

ELSE

A6

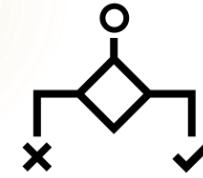
ENDIF

ENDIF

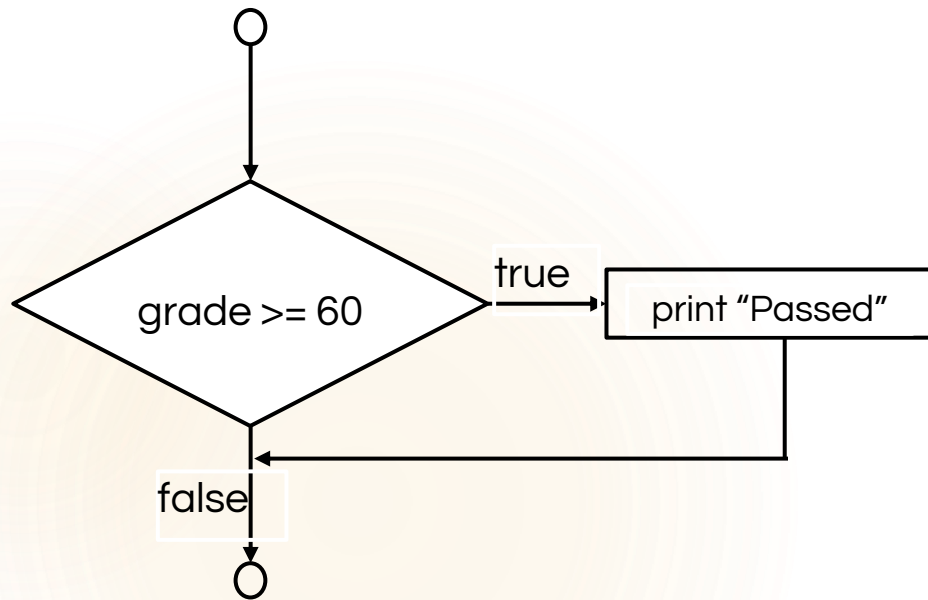
ENDIF

END

Algorithm: Control Structure



✚ Flowchart of pseudocode statement



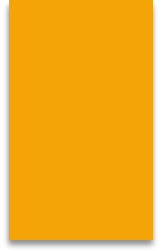
A decision can be made on any expression.

zero - false
nonzero - true

C++ code

```
if ( grade >= 60 )  
{  
    cout << "Passed";  
}  
else  
{  
    cout << "Failed";  
}
```

Algorithm: Control Structure



The repetitive structure: It often happens that we need to repeat an action or a set of actions (block) multiple times. To achieve this, we use a repetitive structure. There are three forms of repetitive structures:

1. The **FOR** form
2. The **WHILE** form
3. The **REPEAT** form

Algorithm: Control Structure



The **FOR** form:

FORMAT:

```
FOR Control_variable FROM Start_value TO End_value DO
```

```
    Block
```

```
END FOR
```

Remark: This structure is used when the number of repetitions is known in advance

Algorithm: Control Structure



The **FOR** form:

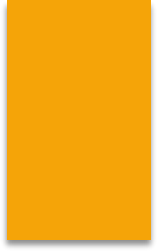
OPERATION:

- a) Initialization of the control variable
- b) Incrementation at each iteration
- c) End test

For each value of the control variable, which ranges from the initial value to the final value with a step of **1**, the block will be executed. Each execution of the block is called an iteration (or loop).

- ▶ The block is repeated $(\text{final value} - \text{initial value} + 1)$ times

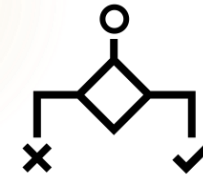
Algorithm: Control Structure



The **FOR** form:

Note: The FOR form is well-suited for cases where you **can predict** the number of block executions, i.e., the number of iterations, and where it is possible to determine the **initial** and **final** values of the control variable.

Algorithm: Control Structure



The **FOR** form: **EXAMPLE**

```
A = 5
FOR I FROM 1 TO 6 DO
    K = A * I
    A = K
END FOR
```

A	I	K
5	1	5
5	2	10
10	3	30
30	4	120
120	5	600
600	6	3600
3600	7	

Algorithm: Control Structure



The **WHILE** form:

FORMAT:

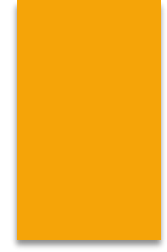
```
WHILE Condition (logical expression) DO
```

```
    Block
```

```
END WHILE
```

Remark: The number of times to repeat is **not known** in advance. The number of iterations depends on the value of the **logical expression**.

Algorithm: Control Structure



The **WHILE** form:

OPERATION:

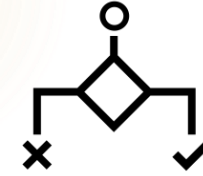
The block is repeated as long as the logical expression is **TRUE**.

At the beginning of each iteration, the logical expression is evaluated. **IF** the value is **TRUE**, then the block is executed; **ELSE**, it proceeds sequentially.

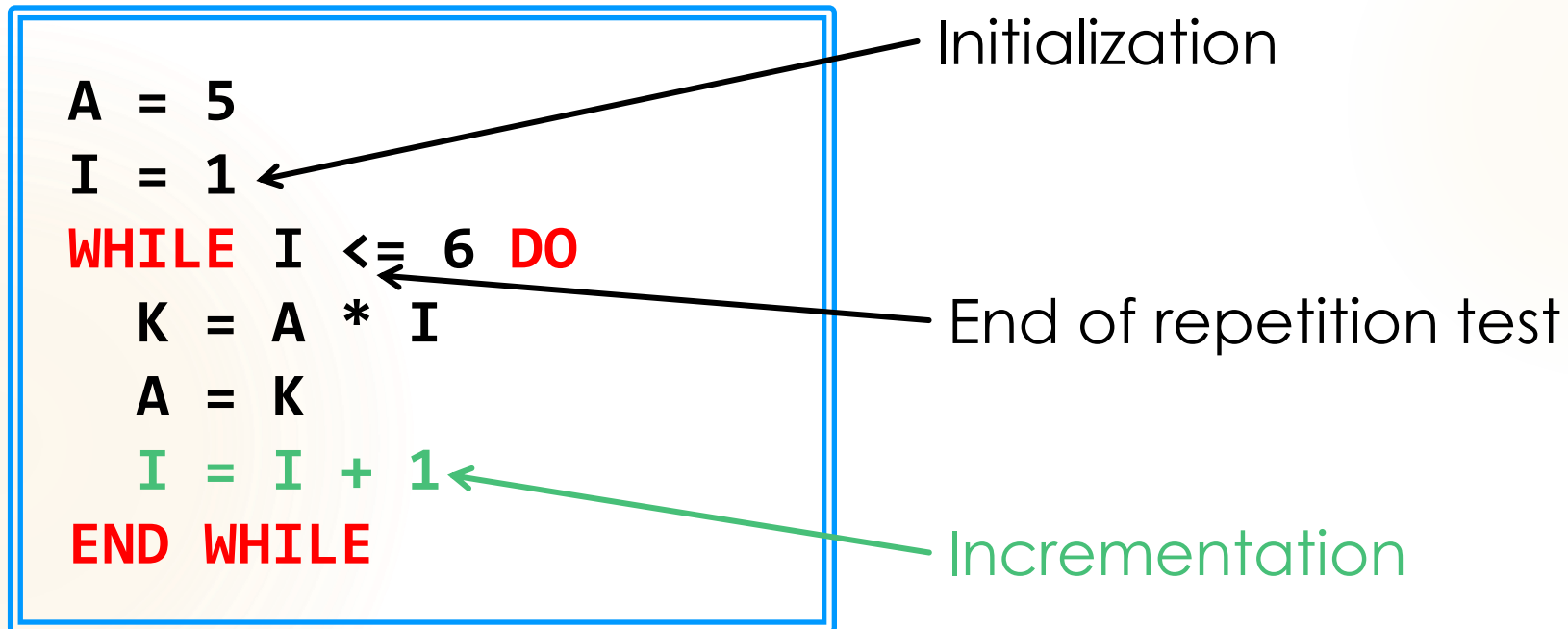
The repetition stops when the condition is no longer satisfied.

Remark: The block may not be executed at all (logical expression is FALSE from the start). In this case, the WHILE structure is a 0, N structure.

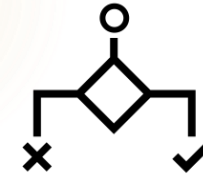
Algorithm: Control Structure



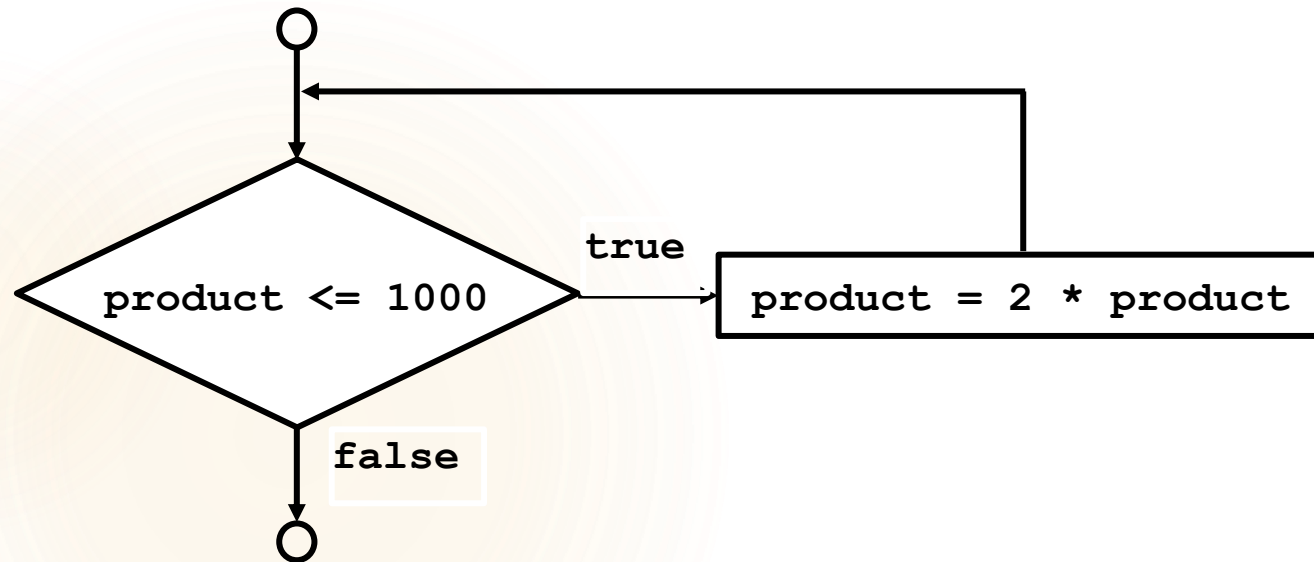
The **WHILE** form: **EXAMPLE**



Algorithm: Control Structure



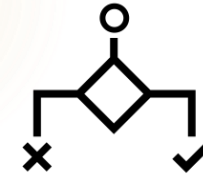
The **WHILE** form: Flowchart



C++ code

```
while (product <= 1000)
{
    product = 2 * product
}
```

Algorithm: Control Structure

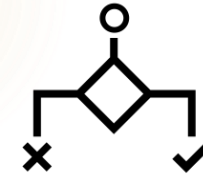


The **WHILE** form: **EXAMPLE**

Write the algorithm that allows you to determine if an integer N, read from the keyboard, is **prime** or **not**.

Reminder: the twenty-five prime numbers less than 100 are:
2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61,
67, 71, 73, 79, 83, 89, and 97.

Algorithm: Control Structure



The **WHILE** form: EXAMPLE

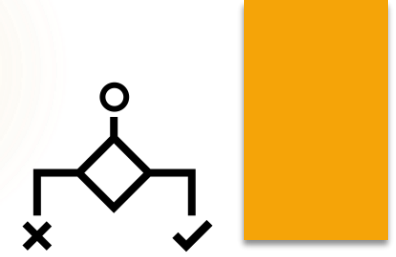
Idea:

Simply look for a divisor of N in the interval $[2, N \text{ Div } 2]$.

As soon as such a divisor is found, the number N is not prime.

Therefore, we will use the **WHILE** structure, which allows us to **stop** the search as soon as a divisor is found.

Algorithm: Control Structure

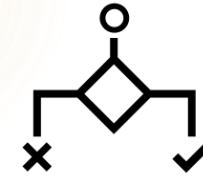


The **WHILE** form: **EXAMPLE**

Analysis:

- ▶ Let N be an integer.
- ▶ Create an intermediate variable N_{div2} , which corresponds to $(N \text{ DIV } 2)$.
- ▶ We divide N by divisors d generated from 2 up to N_{div2} at most.
- ▶ This process stops either when d divides N or when d exceeds N_{div2} .
- ▶ At the end of the process, to determine if N is prime or not, we examine how the previous process concluded. IF $(N \text{ MOD } d > (N \text{ Div } 2))$, then N is prime; OTHERWISE, it is not.

Algorithm: Control Structure



The **WHILE** form: EXAMPLE

Algorithm PrimeNumber

Variables Integer N, d, Ndiv2

BEGIN

READ (N)

 d = 2

 Ndiv2 = N DIV 2

WHILE (N MOD d <> 0) AND (d <= Ndiv2) **DO**
 d = d + 1

END WHILE

IF (d > Ndiv2) **THEN**
 WRITE (N, ' is a Prime number')
 ELSE
 WRITE (N, ' is NOT a Prime number')
 ENDIF

END

```
include <iostream>
using namespace std;
int main() {
    int N, d, Ndiv2;
    cout << "Enter an integer N: ";
    cin >> N;
    d = 2;
    Ndiv2 = N / 2;
    while (N % d != 0 && d <= Ndiv2) {
        d = d + 1;
    }
    if (d > Ndiv2) {
        cout << N << " is a Prime #" << endl;
    } else {
        cout << N << " is not a Prime #" << endl;
    }
    return 0;
}
```

Algorithm: Control Structure



The **REPEAT** form:

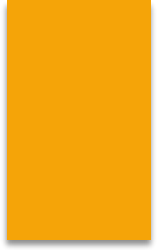
FORMAT:

REPEAT

Block

UNTIL Condition (Logical expression)

Algorithm: Control Structure



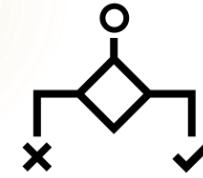
The **REPEAT** form:

OPERATION:

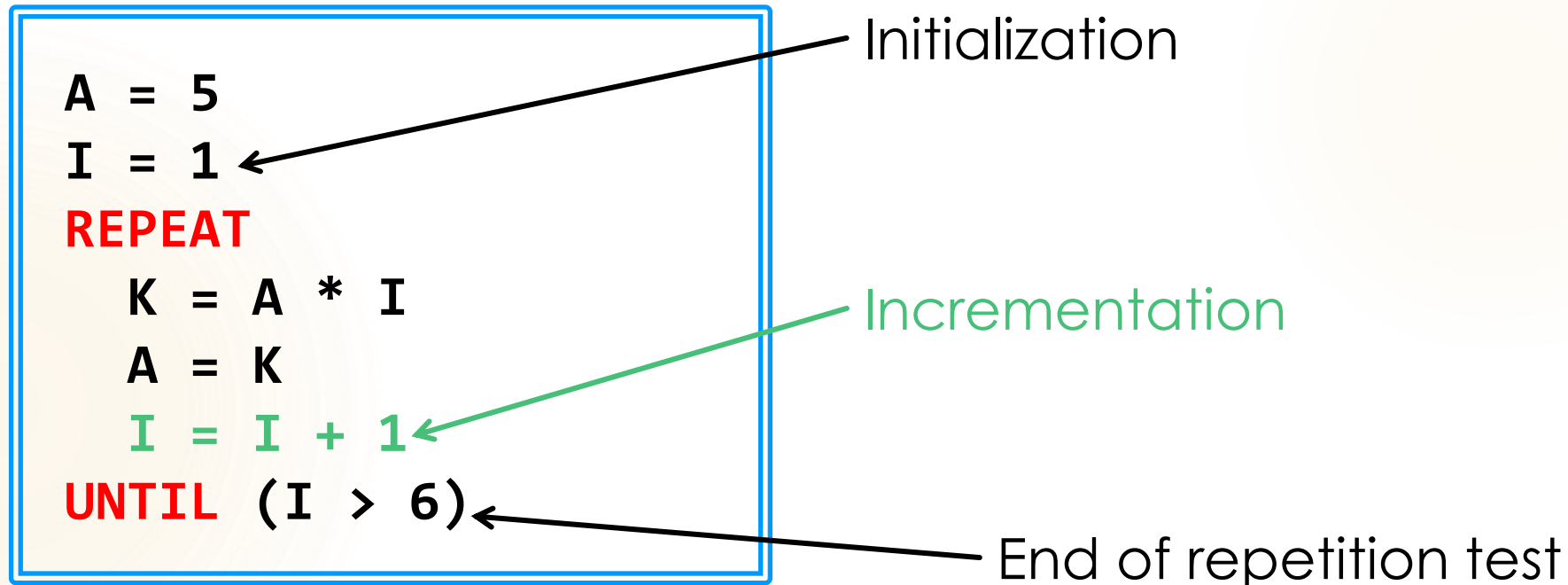
The actions located between the keywords **REPEAT** and **UNTIL** are repeated until the logical expression becomes TRUE. At the end of each iteration, the logical expression is evaluated. If the value is FALSE, the actions are executed; otherwise, the program continues in sequence.

Remark: The actions are executed **at least once** because the logical expression is evaluated only when we reach the UNTIL keyword. This is why the REPEAT structure is referred to as a 1, N structure.

Algorithm: Control Structure

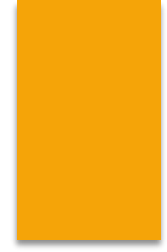


The **REPEAT** form: **EXAMPLE**



Total number of iteration is **6**

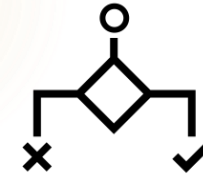
Algorithm: Control Structure



Additional Notes:

- ▶ The WHILE and REPEAT forms are used when the number of loops (iterations) is **unknown**. However, it is always at least 1 for REPEAT, whereas it can be equal to 0 in the WHILE form. This difference often influences the choice between these two forms.
- ❑ Be cautious of design errors that can lead to an "**infinite loop**," where the condition always remains true.

Algorithm: Control Structure



Infinite Loop Example

```
A = 5
```

```
REPEAT
```

```
    X = A * 2
```

```
    Y = 100 - X
```

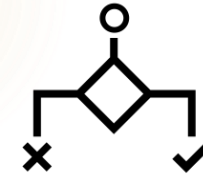
```
    A = A - 2
```

```
UNTIL (A == 0)
```

```
WRITE (X, Y)
```

Indeed, if we unfold this portion of the algorithm, we can see that A will never be equal to zero. This would result in an **infinite** loop.

Algorithm: Control Structure



Choice of the loop (FOR, WHILE, REPEAT)

The rule is simple:

- If the number of iterations is known in advance, then we use a **FOR** loop.
- Otherwise: we use a **REPEAT** loop (when there is always at least one iteration),
- or a **WHILE** loop (when the number of iterations can be zero).