

Data Structure & Algorithms 1

CHAPTER 3: MODULAR PROGRAMMING

Sep – Dec 2023

Fundamental Concepts of Modularity

- ▶ In a program, you may often find that a particular sequence of actions is **repeated** multiple times. In such cases, it's wise to write this sequence only once and reuse it as needed.
- ▶ Furthermore, you may notice that certain groups of actions relate to **different tasks**. It's advisable to represent each of these tasks separately in a subroutine, improving the clarity and readability of the program (or algorithm).

→ As a result, a program can be seen as a **main program** along with a collection of **subroutines**, enhancing organization and efficiency.

Fundamental Concepts of Modularity

Modularity, the cornerstone of structured programming, is simply the act of **breaking down** a problem into a set of **reusable modules**. It serves two fundamental objectives:

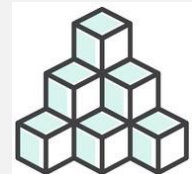


- ▶ **Decomposing Complexity:** It transforms a complex problem into "n" simpler problems that can be resolved independently.
- ▶ **Solution Reusability:** The idea is to find a solution for a problem just once. Once a module, designed for a specific task, is constructed, tested, and documented, it becomes a reusable asset.

Fundamental Concepts of Modularity

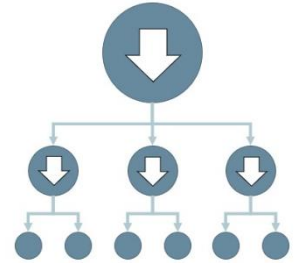
In summary, to save time and write **shorter, well-structured** algorithms, we group one or more blocks performing **specific tasks** into a **MODULE**. We assign a **NAME** to this module, and subsequently, we can "**call**" it whenever needed, simply by referencing its name. There's no need to reconstruct it.

The advantages of modularity make it not just interesting but highly **recommended** to systematically employ modular design in constructing our solutions.



Fundamental Concepts of Modularity

- ▶ Algorithm design naturally follows the top-down approach through progressive refinement:
 1. We start by breaking down our problem into logically coherent modules.
 2. Next, we separately construct each module, whether they are caller modules (calling other modules) or callee modules (called by other modules), along with the main algorithm. We treat them as if they were **independent** problems. As mentioned earlier, these modules may even be assigned to different developers.



Fundamental Concepts of Modularity

- ▶ When using a module, **we no longer need to know** how it is constructed **but** only what it does.
- ▶ The role you assign to each module is crucial, because if it is inadequately defined, ambiguous, or incomplete, your module becomes entirely unusable and, as a result, **USELESS**.

Fundamental Concepts of Modularity

Advantages

- ▶ Improved readability
- ▶ Reduced risk of errors
- ▶ Selective testing possibilities
- ▶ Reuse of existing modules
- ▶ Ease of modification
- ▶ Promote collaborative work
- ▶



Fundamental Concepts of Modularity

Algorithm Algo_1

BEGIN

Bloc A

Bloc B

Bloc C

Bloc A

Bloc B

Bloc C

END

MODULE A

MODULE B

MODULE C

Algorithm Algo_1

Modules A, B, C

BEGIN

Call Module A

Call Module B

Call Module C

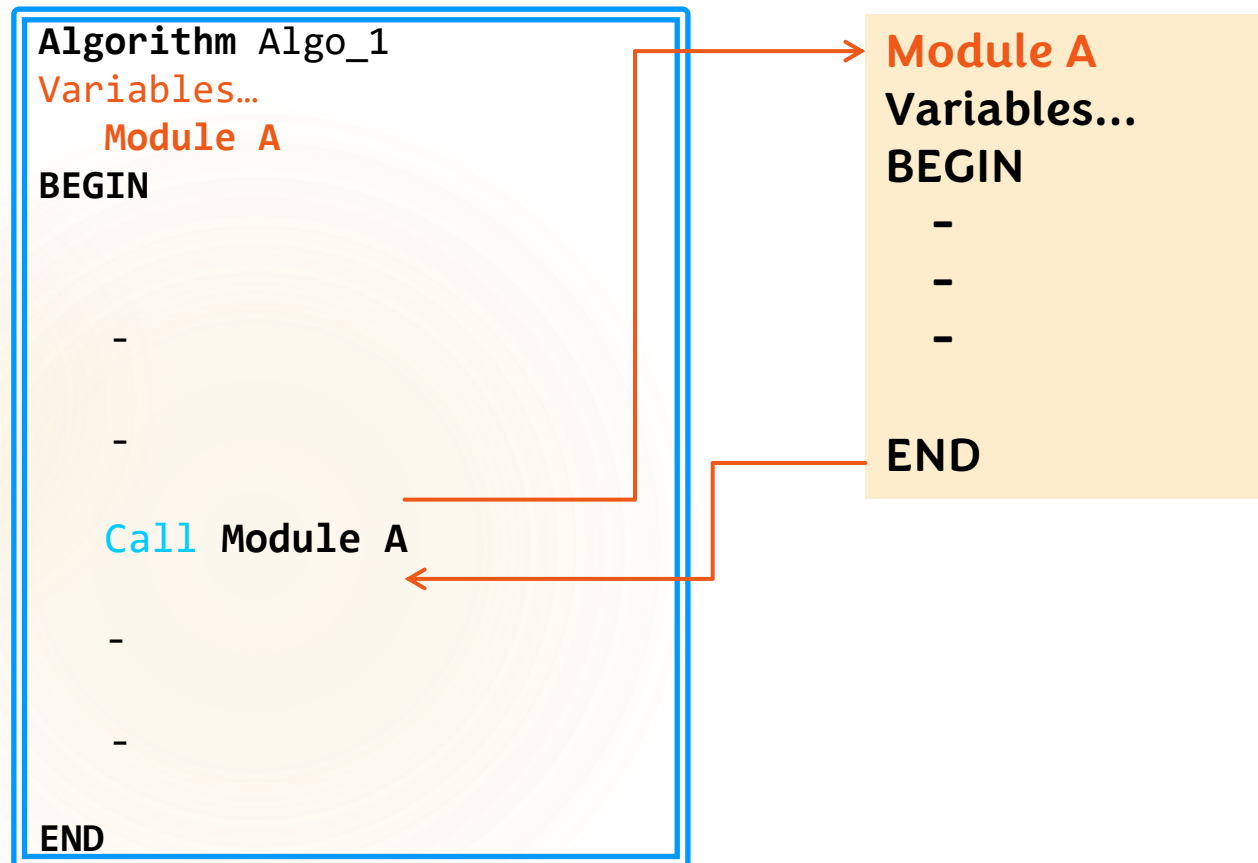
Call Module A

Call Module B

Call Module C

END

Fundamental Concepts of Modularity (calling a module)

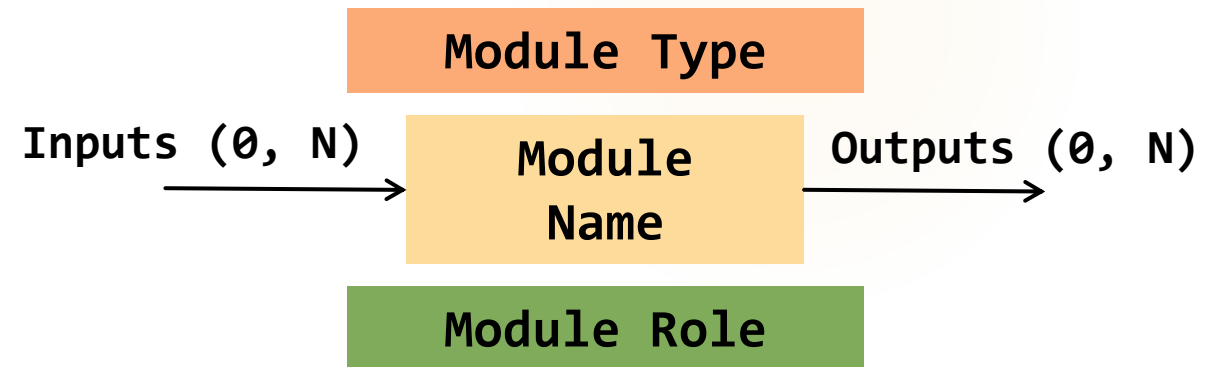


When a module **call** is encountered, the execution of the calling module is **suspended** until the called module is entirely executed, and then the execution of the calling module **resumes** immediately after the call.

Fundamental Concepts of Modularity (calling a module)

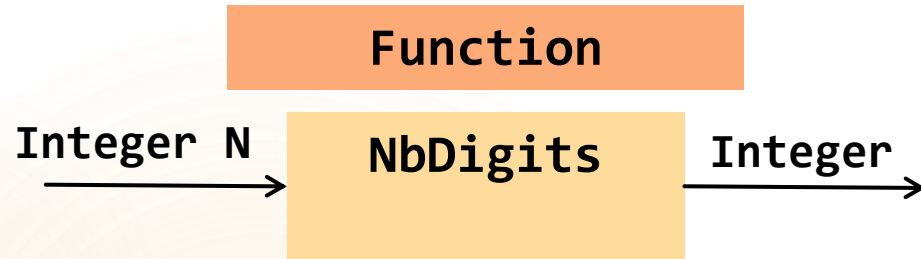
A module is considered as a black box that performs a specific task.

From a syntax perspective, a module follows the same structure as an algorithm. It is defined by **its name, its role, its type, and its interfaces** which means the data it receives as input and the data it returns to the caller.



Fundamental Concepts of Modularity (calling a module)

The interface consists of the inputs / outputs of the module; it is what allows establishing the **link** between the **module** and its **environment**.



Role: return the # digits in N

Algorithm Example_1

Variable Integer N, NbD

Integer Function NbDigits (Integer N)

The body of NbDigits function...

BEGIN

READ(N)

NbD = NbDigits(N)

WRITE (NbD)

END

Integer Function NbDigits (Integer N)

Variable Integer i

BEGIN

i = 0

WHILE (N > 0) DO

i = i + 1

N = N DIV 10

END WHILE

NbDigits = i

END

Modular Approach and Formalism

How to proceed?

First step: understanding the problem

Second step: problem analysis and design

1. break down the problem.
2. construct the modules.

Third step: implementation

Modular Approach and Formalism

Dividing the Problem

- ▶ Identify the modules to be built. Some modules are evident and can be quickly detected, while others may not be apparent at first.
- ▶ Don't waste your time and energy trying to list all the necessary modules.
- ▶ Start with the obvious modules and expand your division as you see fit.
- ▶ Sometimes the division is implicit, meaning that a careful reading of the problem will help you identify the modules to build, while in other cases, it may require analysis and creativity.

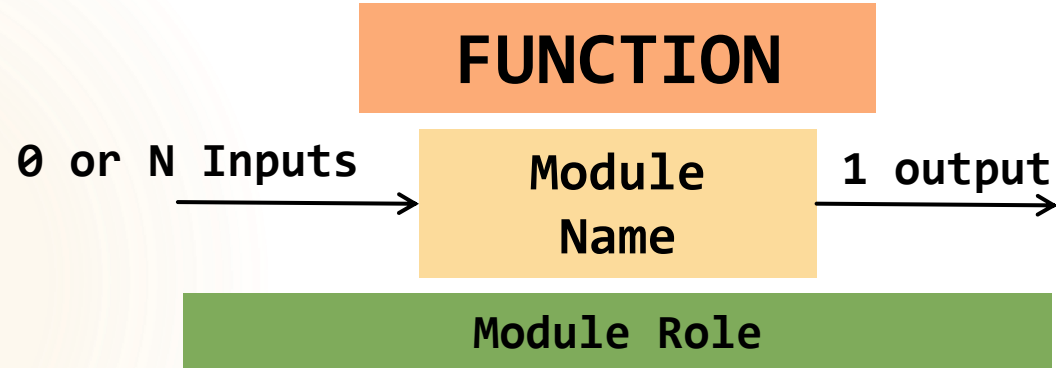
Modular Approach and Formalism

Module Quality

- ▶ **Reusability:** Always aim to make your modules as general as possible for later reuse.
- ▶ **Independence:** Avoid using read or write operations in a module, and the use of global variables. (best way to prevent side effects)
- ▶ **Simplicity:** A module should have a **SINGLE** clear task to perform.

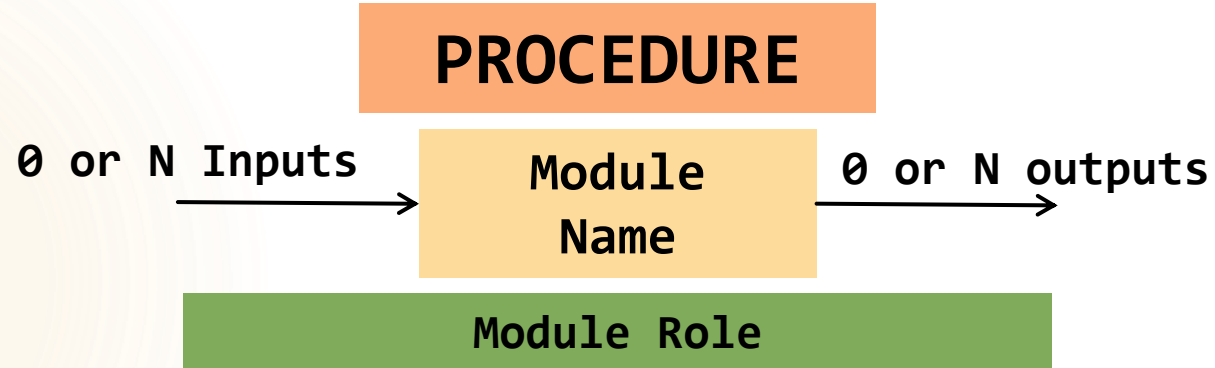
Modular Approach and Formalism

When a module has only one output, and it's a basic data element, it's called a **FUNCTION**. Otherwise, it's a PROCEDURE, meaning it can have zero to many outputs of any type.



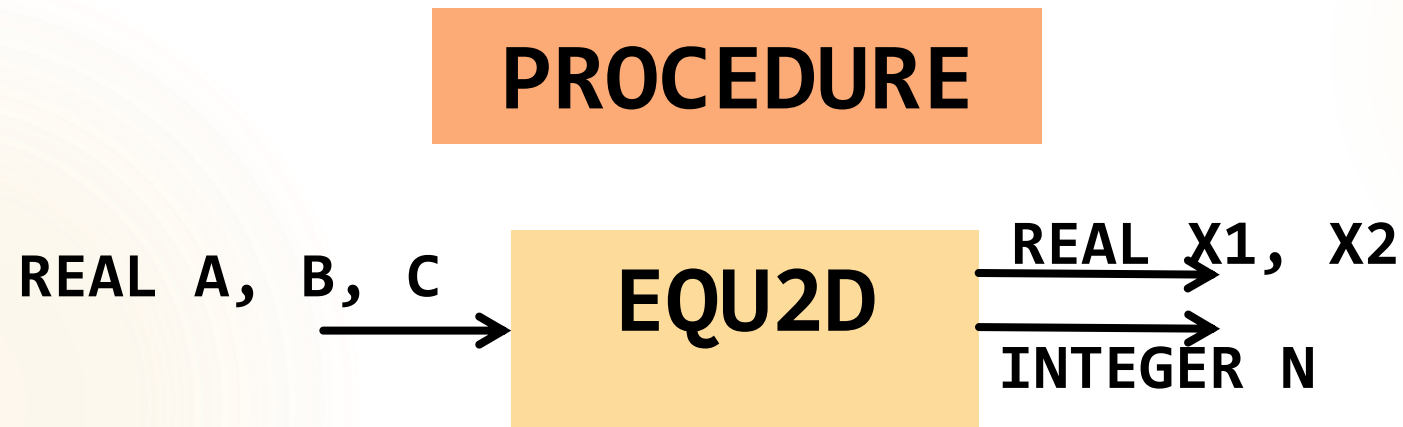
Modular Approach and Formalism

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Modular Approach and Formalism

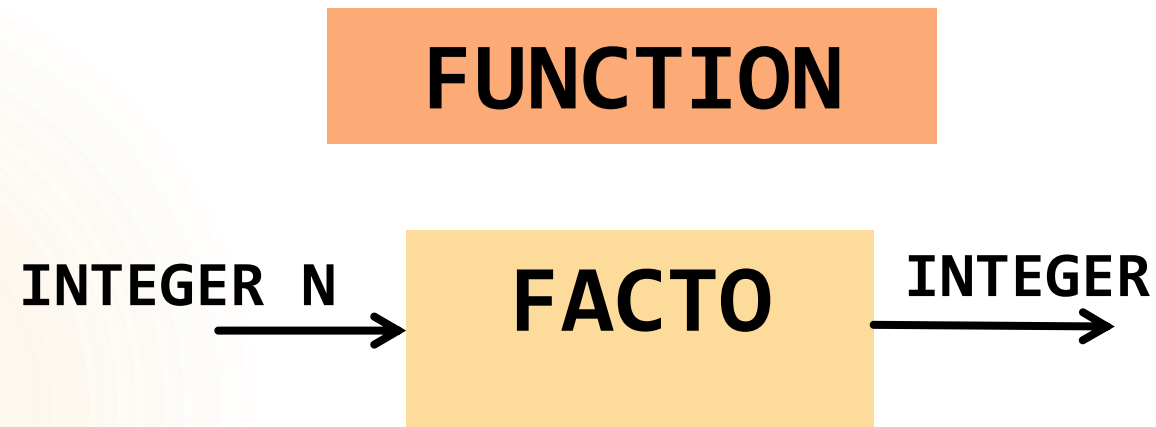
EXAMPLE 1:



Role: Find the number of solutions (**N**) and the roots (**X1** and **X2**) of a quadratic equation with coefficients **A**, **B**, and **C**.

Modular Approach and Formalism

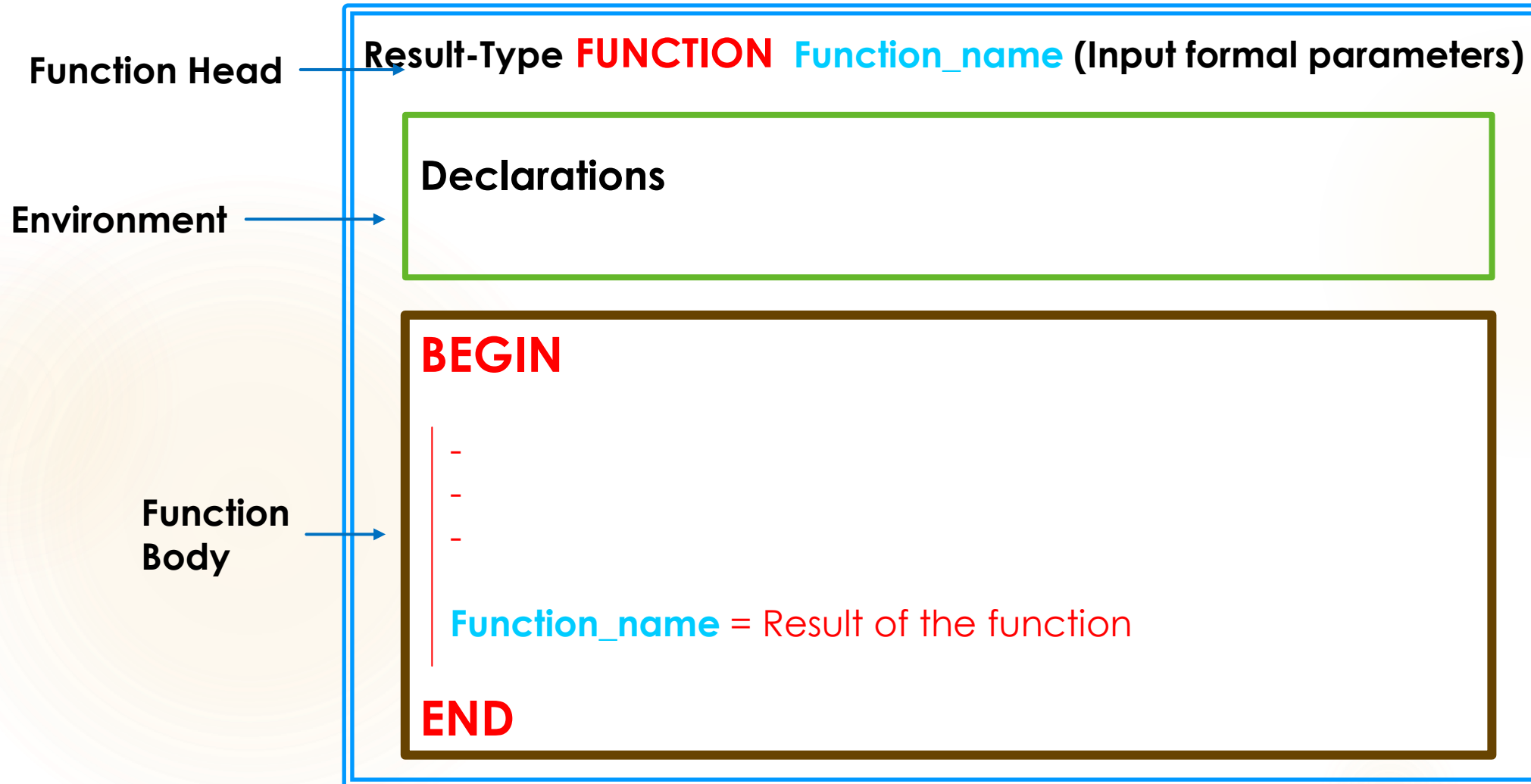
EXAMPLE 2:



Role: Calculte the factorial of an integer N

Modular Approach and Formalism

FUNCTION STRUCTURE



Modular Approach and Formalism

FUNCTION STRUCTURE

- The body of the function can contain all the declarations and algorithmic structures.
- The **result** must always be **transmitted** in the **name of the function**, and this assignment is typically the final action of the function.
- The list of formal parameters describes the objects provided to the function, including their types and their passing mode (this concept is discussed later)."

Modular Approach and Formalism

FUNCTION Call

The call to a function is made by referencing its name to the right of the assignment symbol in a condition or in a procedure or function call.

```
Algorithm Example_Prime
Variable Integer N
      Boolean Res
Boolean Function PRIME (Integer N)
  The body of PRIME function...
BEGIN
  READ(N)
  Res = PRIME(N)
  IF Res == True Then
    WRITE (N, ' is Prime')
  ELSE
    WRITE (N, ' is not Prime')
  END IF
END
```

```
Boolean Function PRIME (Integer N)
Variable Integer i
BEGIN
  i = 2
  WHILE (N MOD i <> 0) AND (i <= N DIV 2) DO
    i = i + 1
  END WHILE
  PRIME = ((N == 2) OR (i > N DIV 2))
END
```

Modular Approach and Formalism

Functions in C++



- **Local variables**
 - Known only in the function in which they are defined
 - All variables declared in function definitions are local variables
- **Parameters**
 - Local variables passed to function when called
 - Provide outside information

Modular Approach and Formalism

Functions in C++



- Function prototype
 - Tells compiler argument type and return type of function
 - **int square(int);**
 - Function takes an **int** and returns an **int**
 - Explained in more detail later
- Calling/invoking a function
 - **square(x);**
 - Parentheses an operator used to call function
 - Pass argument x
 - Function gets its own copy of arguments
 - After finished, passes back result

Modular Approach and Formalism

Functions in C++



- Format for function definition

```
return-value-type function-name( parameter-list )  
{  
    declarations and statements  
}
```

- Parameter list
 - Comma separated list of arguments
 - Data type needed for each argument
 - If no arguments, use **void** or leave blank
- Return-value-type
 - Data type of result returned (use **void** if nothing returned)

Modular Approach and Formalism

Functions in C++



- Example function

```
int square( int y )  
{  
    return y * y;  
}
```

- **return** keyword
 - Returns data, and control goes to function's caller
 - If no data to return, use **return;**
 - Function ends when reaches right brace
 - Control goes to caller
- Functions cannot be defined inside other functions

Modular Approach and Formalism

Functions in C++



EXAMPLE

```
1 // Finding the maximum of three floating-point numbers.
2 //
3     #include <iostream>
4
5     using std::cout;
6     using std::cin;
7     using std::endl;
8
9     double maximum( double, double, double ); // function prototype
10
11 int main()
12 {
13     double number1;
14     double number2;
15     double number3;
16
17     cout << "Enter three floating-point numbers: ";
18     cin >> number1 >> number2 >> number3;
19
20     // number1, number2 and number3 are arguments to
21     // the maximum function call
22     cout << "Maximum is: "
23         << maximum( number1, number2, number3 ) << endl;
24
25     return 0; // indicates successful termination
```

Modular Approach and Formalism

Functions in C++



EXAMPLE

```
26
27     } // end main
28
29     // function maximum definition;
30     // x, y and z are parameters
31     double maximum( double x, double y, double z )
32     {
33         double max = x;    // assume x is largest
34
35         if ( y > max )      // if y is larger,
36             max = y;        // assign y to max
37
38         if ( z > max )      // if z is larger,
39             max = z;        // assign z to max
40
41         return max;        // max is largest value
42
43     } // end function maximum
```

Enter three floating-point numbers: 99.32 37.3 27.1928
Maximum is: 99.32

Enter three floating-point numbers: 1.1 3.333 2.22
Maximum is: 3.333

Enter three floating-point numbers: 27.9 14.31 88.99
Maximum is: 88.99

Function declaration and use

Result type =
Function type

- ▶ Integer FUNCTION LeastCommonMultiple (Integer A, B)
- ▶ Integer FUNCTION Factorial (Integer N)
- ▶ Boolean FUNCTION Prime (Integer N)

Formal
parameters

Functions call:

- ▶ WRITE ('The LCM of ' i ' and ', j, ' is: ', LeastCommonMultiple(i, j))
- ▶ WRITE ('The Factorial of ' N, ' is: ', Factorial(N))
- ▶ IF Prime (i * j + 25) THEN ...

Function
call

Actual
parameters

Function declaration and use

CAUTION

- ▶ The number of actual parameters must be equal to that of formal parameters.
- ▶ The order of actual parameters must match the order of formal parameters.
- ▶ There must be type compatibility between formal and actual parameters.

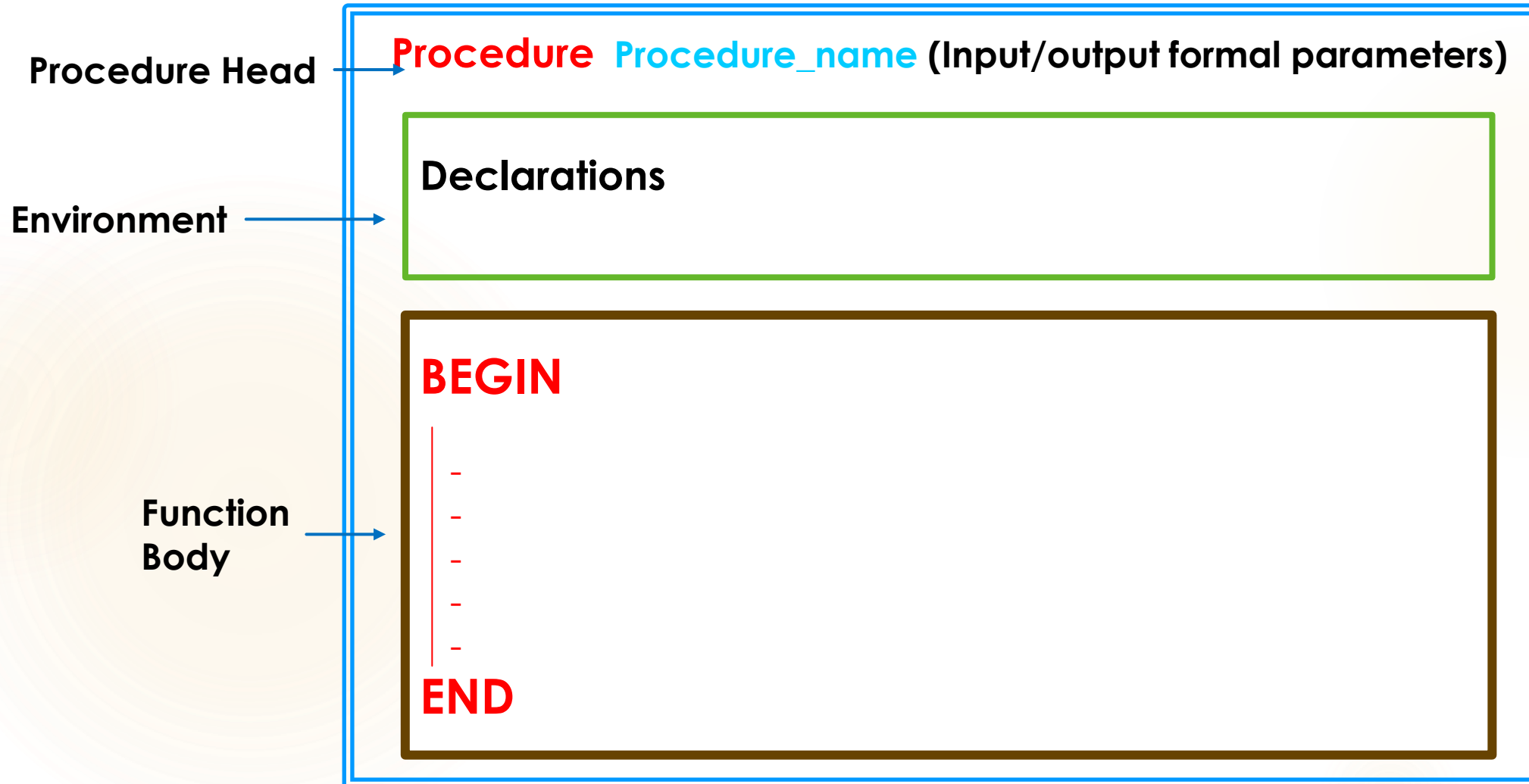
```
Integer FUNCTION LeastCommonMultiple (Integer A, B)
```

```
    READ (i, j)                                // i, j and Res must be of type Integer
    Res = LeastCommonMultiple(i, j)
    WRITE ('The LCM of ' i ' and ', j, ' is: ', Res)
```

PROCEDURE

Modular Approach and Formalism

PROCEDURE STRUCTURE



Modular Approach and Formalism

PROCEDURE STRUCTURE

- The body of the procedure can contain all the declarations and algorithmic structures.
- The list of formal parameters describes the input **and output** parameters including their types and their passing mode
- The parameter passing is identical to that of functions, but **ALL** output parameters must be defined with a **pass-by-variable** method.

Modular Approach and Formalism

PROCEDURE Call

Calling a procedure is done by stating its name followed by the list of actual parameters, just like an **instruction**.

The calling of a procedure is, in fact, a primitive action, consisting of the procedure name followed by the list of actual input and output parameters enclosed in parentheses, separated by commas.

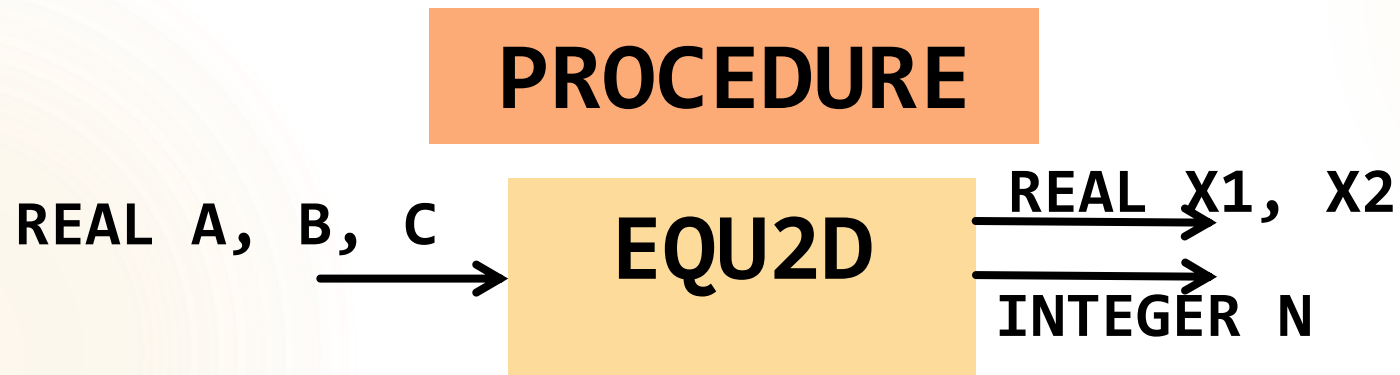
Just like with functions, the number, order, and type of actual parameters **must match** those of the formal parameters.

Call Example: EQU2D(e, f, g, Nr, S1, S2)

Modular Approach and Formalism

Procedure Declaration (Example):

Write an algorithm that solves a second-degree equation with coefficients A, B, and C read from the keyboard.



Role: Find the number of solutions (N) and the roots (X1 and X2) of a quadratic equation with coefficients A, B, and C.

Modular Approach and Formalism

Procedure Declaration (Example):

Analysis:

- Calculation of $\Delta = B^2 - 4AC$
- IF ($\Delta < 0$) THEN
 $N = 0$
- ELSE
 - IF ($\Delta == 0$) THEN
 $N = 1$
 $X1 = -B / (2*A)$
 $X2 = X1$
 - ELSE
 $Ns = 2$
 $X1 = (-B - \text{SQRT}(\Delta)) / (2*A)$
 $X2 = (-B + \text{SQRT}(\Delta)) / (2*A)$
 - END IF
- END IF

Modular Approach and Formalism

Procedure Declaration (Example):

```
PROCEDURE EQU2D(Real A, B, C; Var Integer N; Var Real X1, X2)
Variable Real Delta
BEGIN
    Delta = B*B - 4*A*C
    IF (Delta > 0) THEN
        X1 = (-B - SQRT(Delta)) / (2*A)
        X2 = (-B + SQRT(Delta)) / (2*A)
        N = 2
    ELSE
        IF (Delta == 0) THEN
            X1 = -B / (2*A)
            x2 = X1
            N = 1
        ELSE
            N = 0
        END IF
    END IF
END
```

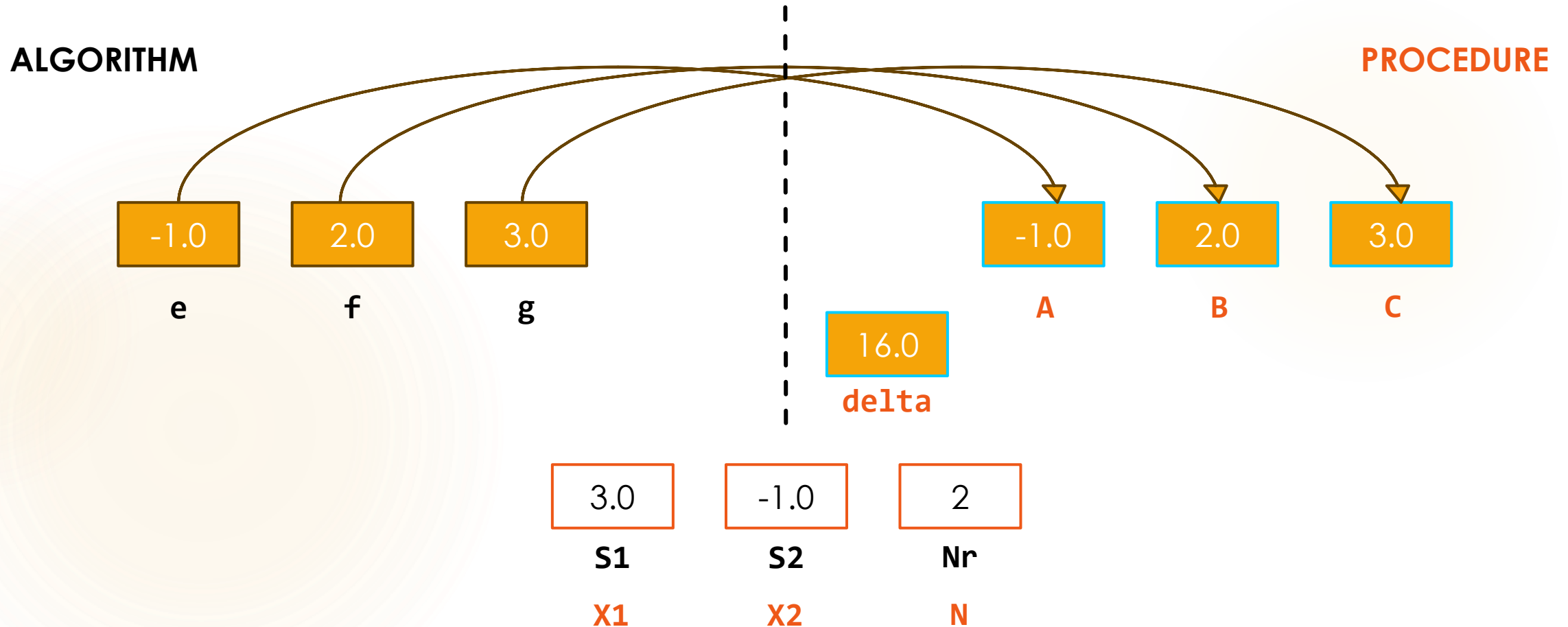
Modular Approach and Formalism

Procedure Declaration (Example):

```
Algorithm Example_Procedure
Variable Real e, f, g, S1, S2
          Integer Nr
          //Procedure declaration
Procedure EQU2D(Real A, B, C; Var Integer N; Var Real X1, X2)
  ... The body of EQU2D procedure here ...
BEGIN
  WRITE ('Give the parameters: A, B and C: ')
  READ(e, f, g)
  EQU2D(e, f, g, Nr, S1, S2)
  CASE OF Nr
    0: WRITE ('No Solution')
    1: WRITE ('One double root X1 = X2 = ', S1)
    2: WRITE ('Two distinct roots, X1 = ', S1, 'X2 = ', S2)
  ENDCASE
END
```

Modular Approach and Formalism

Procedure Declaration (Example):



MODULAR DECOMPOSITION EXAMPLE

Modular Decomposition:

Example

Consider the sequence: 1, 11, 21, 1112, 3112, ...

What is the next element? You've found it!

Now, let's build an analysis to obtain an element from the previous one.

Justification:

We observe that each element is derived from the previous one. It consists of the number of **1s** followed by **1** and then the number of **2s** followed by **2**. These elements are concatenated as we progress.

1, 11, 21, 1112, 3112, 211213 ...

This sequence is formed by concatenating the counts of 1s and 2s to the previous element.

Modular Decomposition: Example

ANALYSIS

- ▶ Let N be an integer representing an element of the sequence.
- ▶ For each digit C (from 1 to 9):
 - ❑ **Count** the number of times (NB) the digit C appears in N .
 - ❑ **Compose** the desired number $N2$.
- ▶ Display $N2$.
- ▶ Additional instructions may be required.

We will need two modules:

- ▶ A module that calculates the number of occurrences of a given digit in a number (**FREQDG**).
- ▶ A module that concatenates two numbers (**CONCAT**).

Modular Decomposition: Example

Algorithm Sequence

Variable Integer N, C, N2, N3, Nb

Integer Function FREQDG (Integer N , C)

... //Function Body here

Integer Function CONCAT (Integer A , B)

... //Function Body here

BEGIN

 READ(N)

 N2 = 0

 FOR C FROM 1 TO 9 DO

 Nb = FREQDG(N,C)

 IF (Nb <> 0) THEN

 N3 = CONCAT(Nb, C)

 N2 = CONCAT(N2, N3)

 END IF

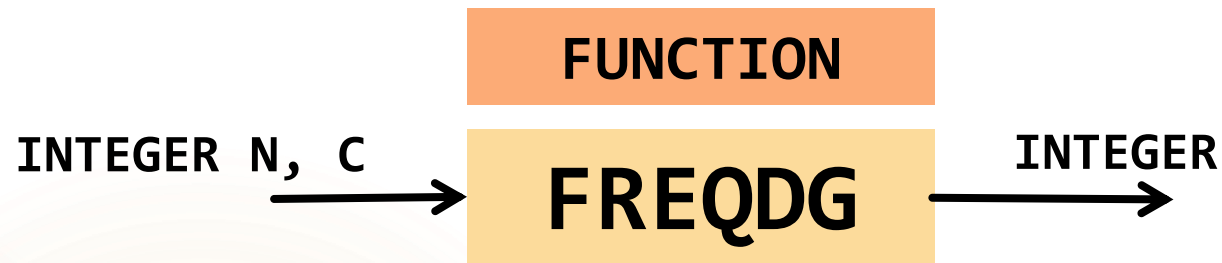
 END FOR

 WRITE(N2)

 N = N2

END

Modular Decomposition: Example



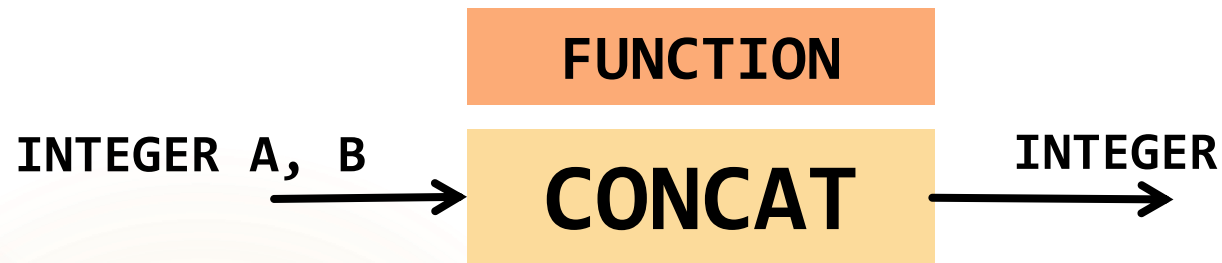
Role: Provide the number of times the digit C appears in N

ANALYSIS:

The algorithm decomposes N digit by digit until a quotient of 0 is obtained. For each digit obtained ($N \text{ Mod } 10$), if it is equal to C, it is counted.

```
Integer Function FREQDG (Integer N , C)
Variable Integer Cpt, ND, i
BEGIN
    Cpt = 0
    ND = NbDigit(N)
    FOR i FROM 1 TO ND DO
        IF (N Mod 10 == C) THEN
            Cpt = Cpt + 1
        END IF
        N = N Div 10
    END FOR
    FREQDG = Cpt
END
```

Modular Decomposition: Example



Role: Concatenate integer A with integer B

$$\begin{array}{r} 1230000 \\ + \quad 4567 \\ \hline = 1234567 \end{array}$$

ANALYSIS:

When you want to concatenate N1 (123) and N2 (4567), you can achieve this by adding **4 zeros** to N1 and then adding N2 (**4** is the number of positions in N2).

Result = $N1 * 10^{Np} + N2 = N1 * N3 + N2$, where $N3 = 10^{Np}$.

In this context, Np represents the number of positions in N2 that determine how many zeros need to be added to N1 for concatenation.

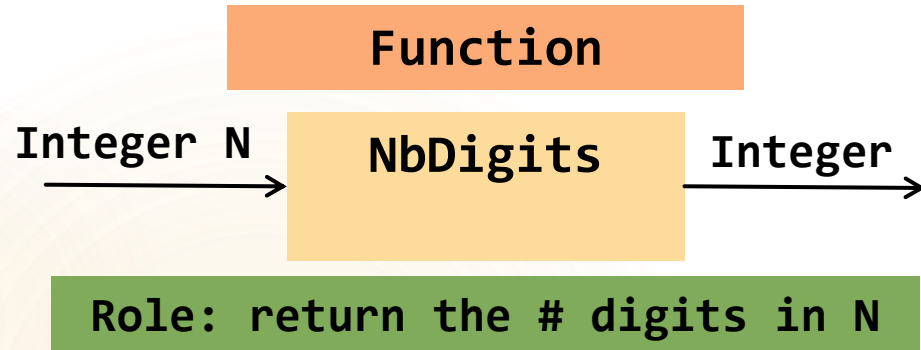
From the analysis we need to construct the following 2 modules: **CONCAT, NbDigits**

Modular Decomposition: Example

```
Integer Function NbDigits(Integer N)  
  //.... Function Body
```

```
Integer Function CONCAT(Integer A, B)  
Variables Integer NP, P1  
BEGIN  
  NP = NbDigits (B)  
  P1 = 10 ** NP  
  CONCAT = A* P1 + B  
END
```

Modular Decomposition: Example



```
Integer Function NbDigits (Integer N)
Variable Integer i
BEGIN
    i = 0
    WHILE (N > 0) DO
        i = i + 1
        N = N DIV 10
    END WHILE
    NbDigits = i
END
```

PRAMETER PASSING



Parameter Passing

Parameter passing is a concept that needs to be **mastered**; otherwise, there is a risk of losing control over the functioning of modules, especially in terms of the **flow** of our algorithms.

There are two modes of parameter passing:

1. **Value passing mode**
2. **Reference or variable passing mode**

Parameter Passing

- ▶ When a parameter is provided to a module, and we want the module to return the same value that the parameter had at the input, we will perform a **value passing** of parameters.
- ▶ But when a parameter is modified during the execution of a module, and we want to have the modified content of the parameter at the output of the module, we will perform a **variable (or reference) passing**. In this case, the formal parameter must be preceded by the word "**VAR.**"

Parameter Passing

In general

It is necessary to use:

- ▶ Variable passing for ALL output parameters of a procedure-type module.
- ▶ Value passing for input parameters of a function.

Parameter Passing

```
PROCEDURE EQU2D(Real A, B, C; Var Integer N; Var Real X1, X2)
```

The **absence** of "VAR" indicates that the parameter passing mode is a **value passing** mode.

6 Formal parameters

"VAR" indicates that the parameter passing mode is a **variable passing** mode.

Procedure Call:

```
EQU2D (i, j, k, Nr, r1, r2)
```

```
EQU2D (-2.0, 3.0, 1, Nr, r1, r2)
```

6 Actual parameters

Parameter Passing in C++



Call by value

- Copy of data passed to function
- Changes to copy do not change original

Call by reference

- Function can directly access data
- Changes affect original

Parameter Passing in C++



- Reference parameter
 - Alias for argument in function call
 - Passes parameter by reference
 - Use **&** after data type in prototype
 - **void myFunction(int &data)**
 - Read “**data** is a reference to an **int**”
 - Function call format the same
 - However, original can now be changed

- Function call with omitted parameters
 - If not enough parameters, rightmost go to their defaults
 - Default values
 - Can be constants, global variables, or function calls
- Set defaults in function prototype

```
int myFunction( int x = 1, int y = 2, int z = 3 );
```

 - **myFunction(3)**
 - **x = 3**, **y** and **z** get defaults (rightmost)
 - **myFunction(3, 5)**
 - **x = 3**, **y = 5** and **z** gets default

Math Library in C++



Method	Description	Example
ceil(x)	rounds x to the smallest integer not less than x	ceil(9.2) is 10.0 ceil(-9.8) is -9.0
cos(x)	trigonometric cosine of x (x in radians)	cos(0.0) is 1.0
exp(x)	exponential function e^x	exp(1.0) is 2.71828 exp(2.0) is 7.38906
fabs(x)	absolute value of x	fabs(5.1) is 5.1 fabs(0.0) is 0.0 fabs(-8.76) is 8.76
floor(x)	rounds x to the largest integer not greater than x	floor(9.2) is 9.0 floor(-9.8) is -10.0
fmod(x, y)	remainder of x/y as a floating-point number	fmod(13.657, 2.333) is 1.992
log(x)	natural logarithm of x (base e)	log(2.718282) is 1.0 log(7.389056) is 2.0
log10(x)	logarithm of x (base 10)	log10(10.0) is 1.0 log10(100.0) is 2.0
pow(x, y)	x raised to power y (x^y)	pow(2, 7) is 128 pow(9, .5) is 3
sin(x)	trigonometric sine of x (x in radians)	sin(0.0) is 0
sqrt(x)	square root of x	sqrt(900.0) is 30.0 sqrt(9.0) is 3.0
tan(x)	trigonometric tangent of x (x in radians)	tan(0.0) is 0

LOCAL & GLOBAL OBJECT

Local and Global Objects

A **block** corresponds to a **region** of a program.
In a program, blocks can be nested within each other.
This structure, known as the block structure, defines levels of blocks:

- ▶ The **main** program forms block **level 0**.
- ▶ **Procedures** and **functions** declared directly within the main program each form a block of **level 1**.
- ▶ **Procedures** and **functions** declared within level 1 procedures or functions each form a block of **level 2**.

Level 0 Main Program

|

Level 1 Procedures Functions in Main Program

|

Level 2 Procedures Functions in Level 1

|

...

Local and Global Objects

- ▶ Procedures and functions declared within procedures or functions of level N each form a block of level $N+1$.
- ▶ The level number is referred to as the depth of the level. A block of level 5 is deeper than a block of level 2.

Local and Global Objects

Scope of an object

An object is known and usable:

- ▶ In its defining block as soon as the object has been declared.
- ▶ In **all blocks at deeper levels** if they are declared **within and after** its defining block.

The **region** of a program where an object **can be used** is called the **object's scope**.

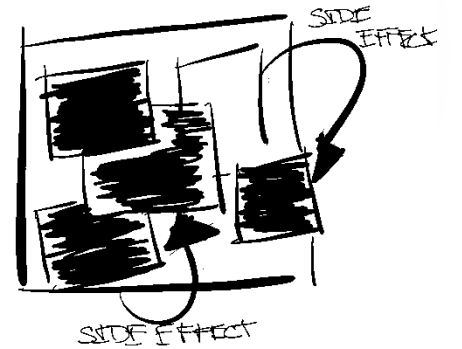
Local and Global Objects

Scope of an object

An object is known and usable:

- ▶ An object is **local** to a block if it is declared in the declarative part of the block.
- ▶ An object is **global** to a block if it is declared outside the block, and the block is within the scope of that identifier.

SIDE EFFECT



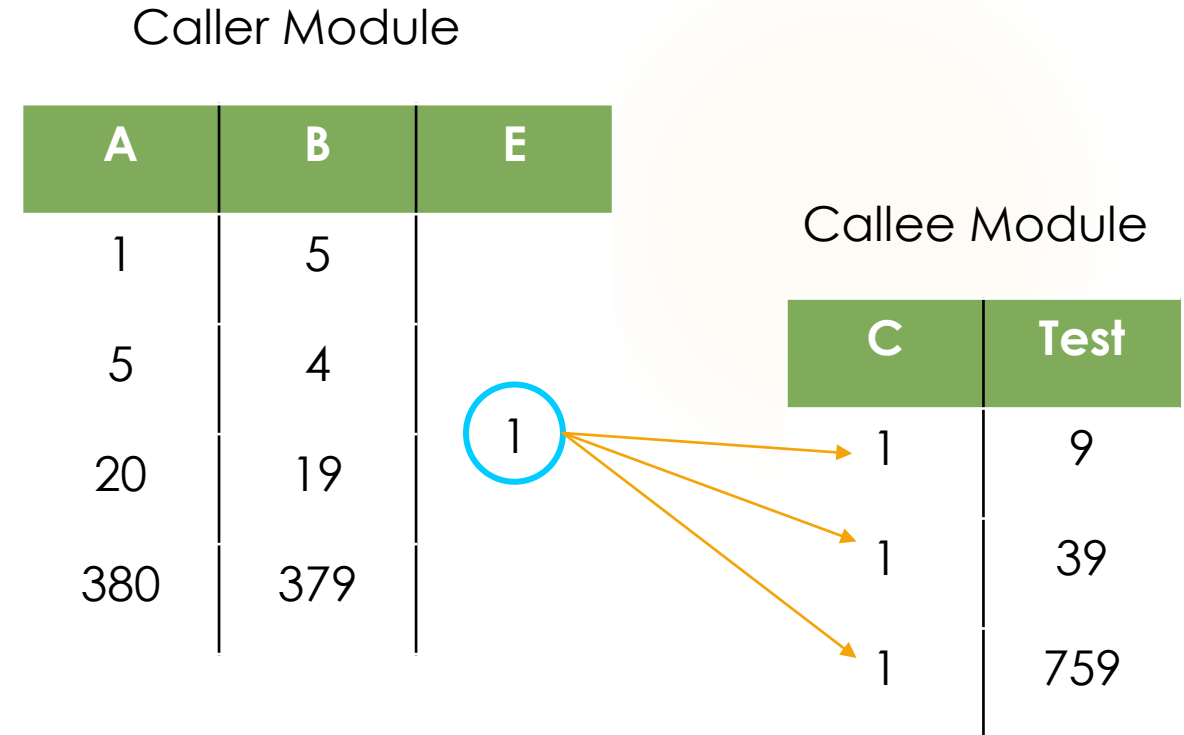
Side Effects

A side effect is when a function relies on, or **modifies**, something **outside** its parameters to do something.

For example, a function which reads or writes from a variable outside its own arguments, a database, a file, or the console can be described as having side effects.

Side Effects

```
Algorithm Side_Effect
Variable Integer A, B, E
Integer Function Test(Integer C)
  BEGIN
    A = A * B
    B = A - C
    Test = A + B
  END
BEGIN
  A = 1
  B = 5
  E = 1
  WRITE (Test(E))
  WRITE (Test(E))
  WRITE (Test(E))
END
```



Side Effects

To avoid side effects, simply follow the following rule:

- ▶ Whenever possible, do not use global variables within a module. Otherwise, only modify local objects.