

# Сюжеты, возникающие при обучении больших моделей

Даня Меркулов

```
RuntimeError: cuda runtime error (2) : out of memory at /data/users/soumith/miniconda2/cond
```

how can i solve this error?



**apaszke** commented on Mar 8, 2017

Member + ...

You're running out of memory on the GPU. It's not a bug.

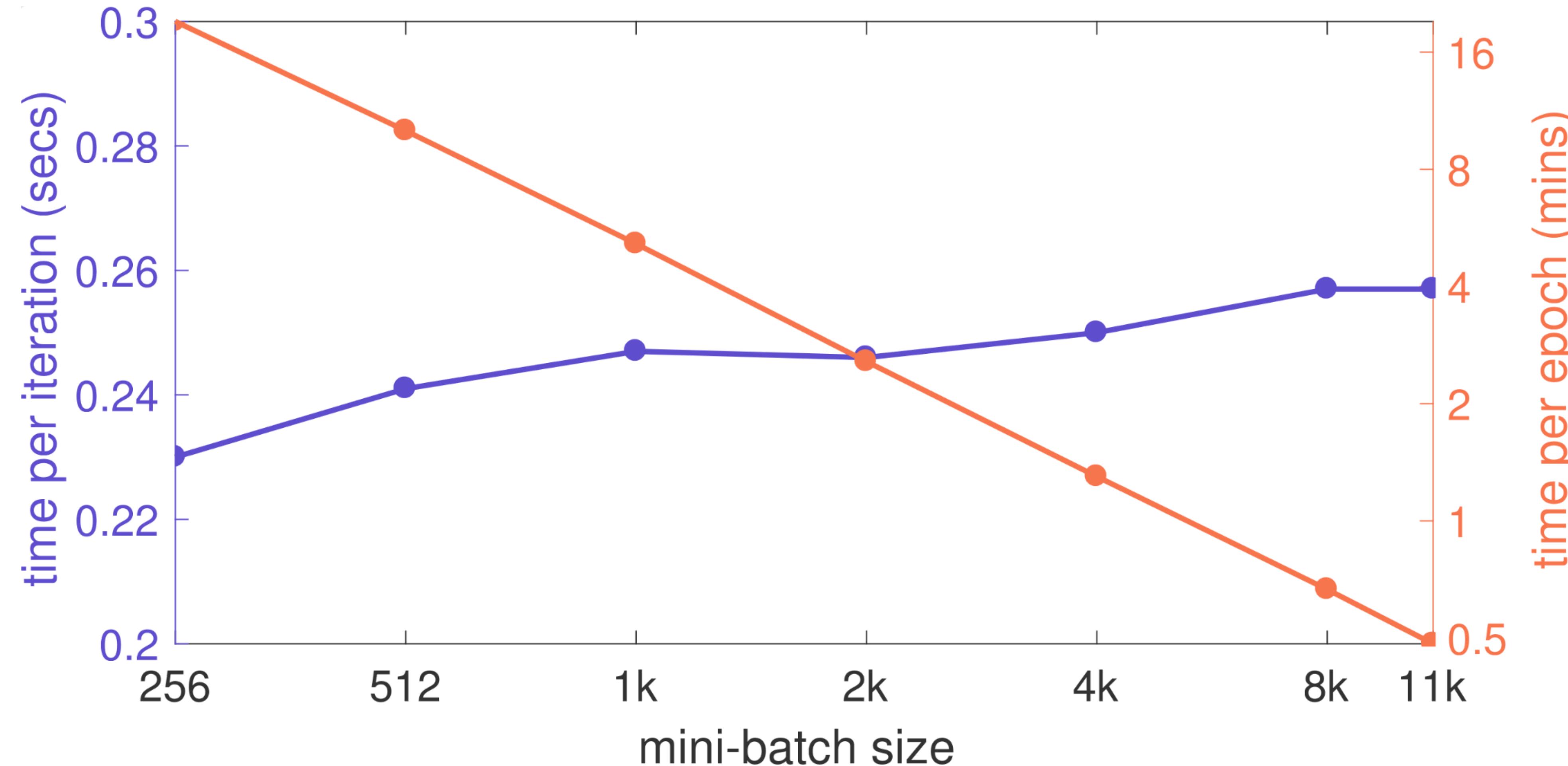


16



3

# Размер батча и время эпохи



При наличии достаточной памяти GPU, увеличение размера батча позволяет утилизировать ресурсы параллельных вычислений.

# Просто так увеличить размер батча не выйдет

Обучение ResNet-50 на датасете ImageNet с разными вариантами увеличения размера батча.

$kn$	$\eta$	top-1 error (%)
256	0.05	$23.92 \pm 0.10$
256	0.10	$23.60 \pm 0.12$
256	0.20	$23.68 \pm 0.09$
8k	$0.05 \cdot 32$	$24.27 \pm 0.08$
8k	$0.10 \cdot 32$	$23.74 \pm 0.09$
8k	$0.20 \cdot 32$	$24.05 \pm 0.18$
8k	0.10	$41.67 \pm 0.10$
8k	$0.10 \cdot \sqrt{32}$	$26.22 \pm 0.03$

(a) **Comparison of learning rate scaling rules.** A reference learning rate of  $\eta = 0.1$  works best for  $kn = 256$  (23.68% error). The linear scaling rule suggests  $\eta = 0.1 \cdot 32$  when  $kn = 8k$ , which again gives best performance (23.74% error). Other ways of scaling  $\eta$  give worse results.

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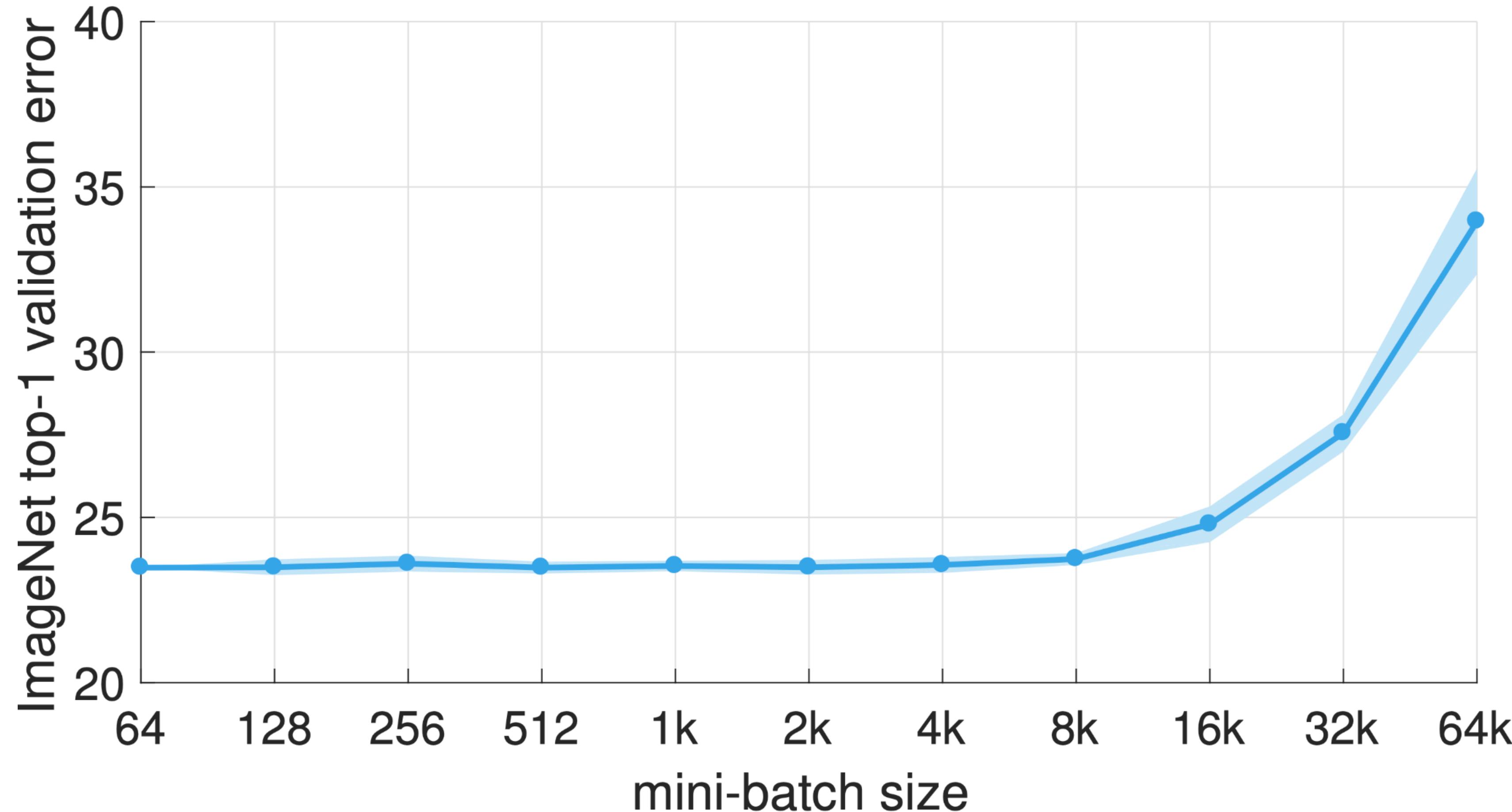
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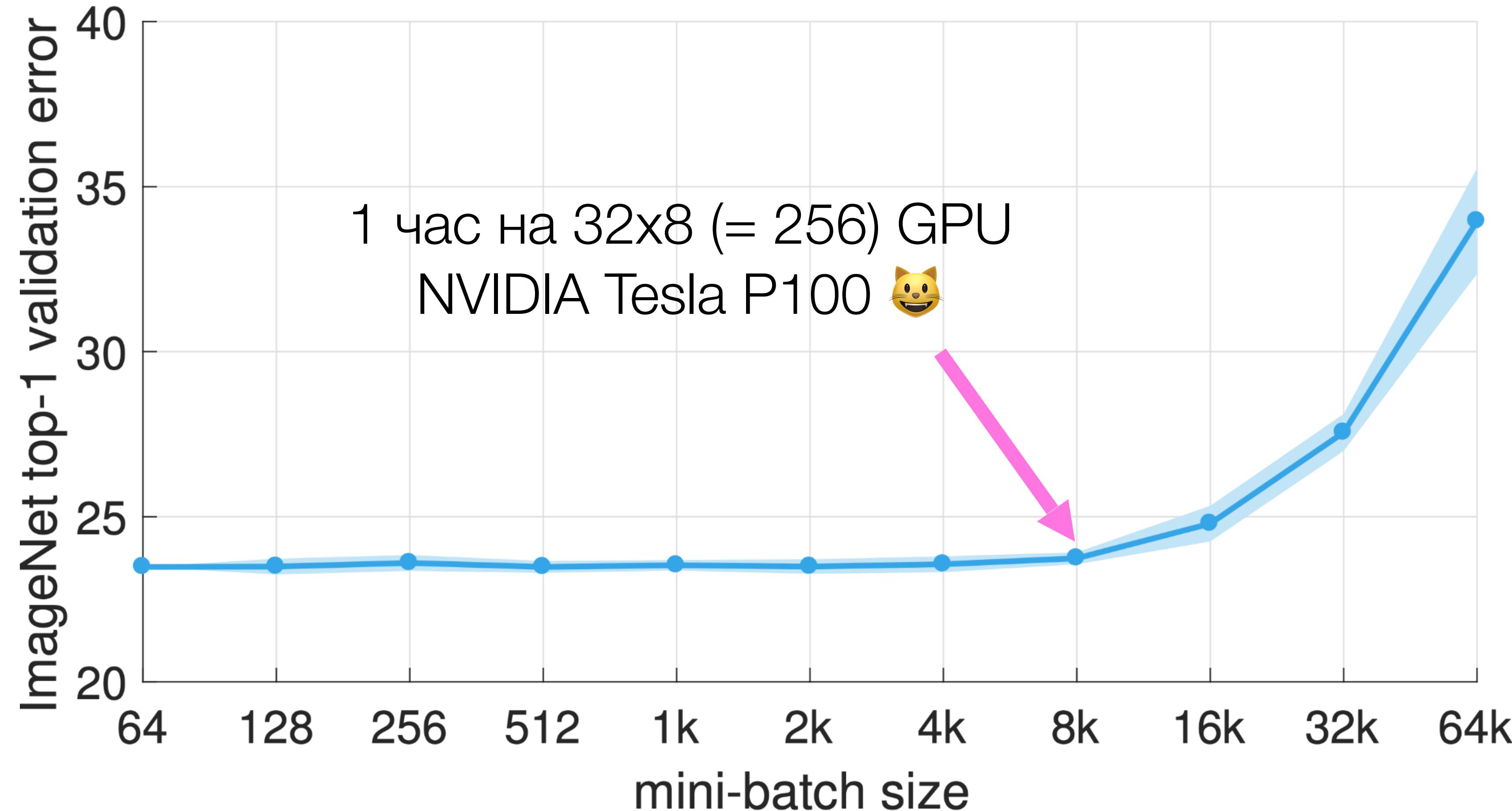
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# Как увеличивать размер батча?

## 1. Linear scaling rule.

При увеличении размера батча в  $k$  раз, learning rate увеличивать тоже в  $k$  раз:

## 2. Gradual warmup.

На первых эпохах (итерациях) learning rate увеличивать постепенно от начального до целевого.

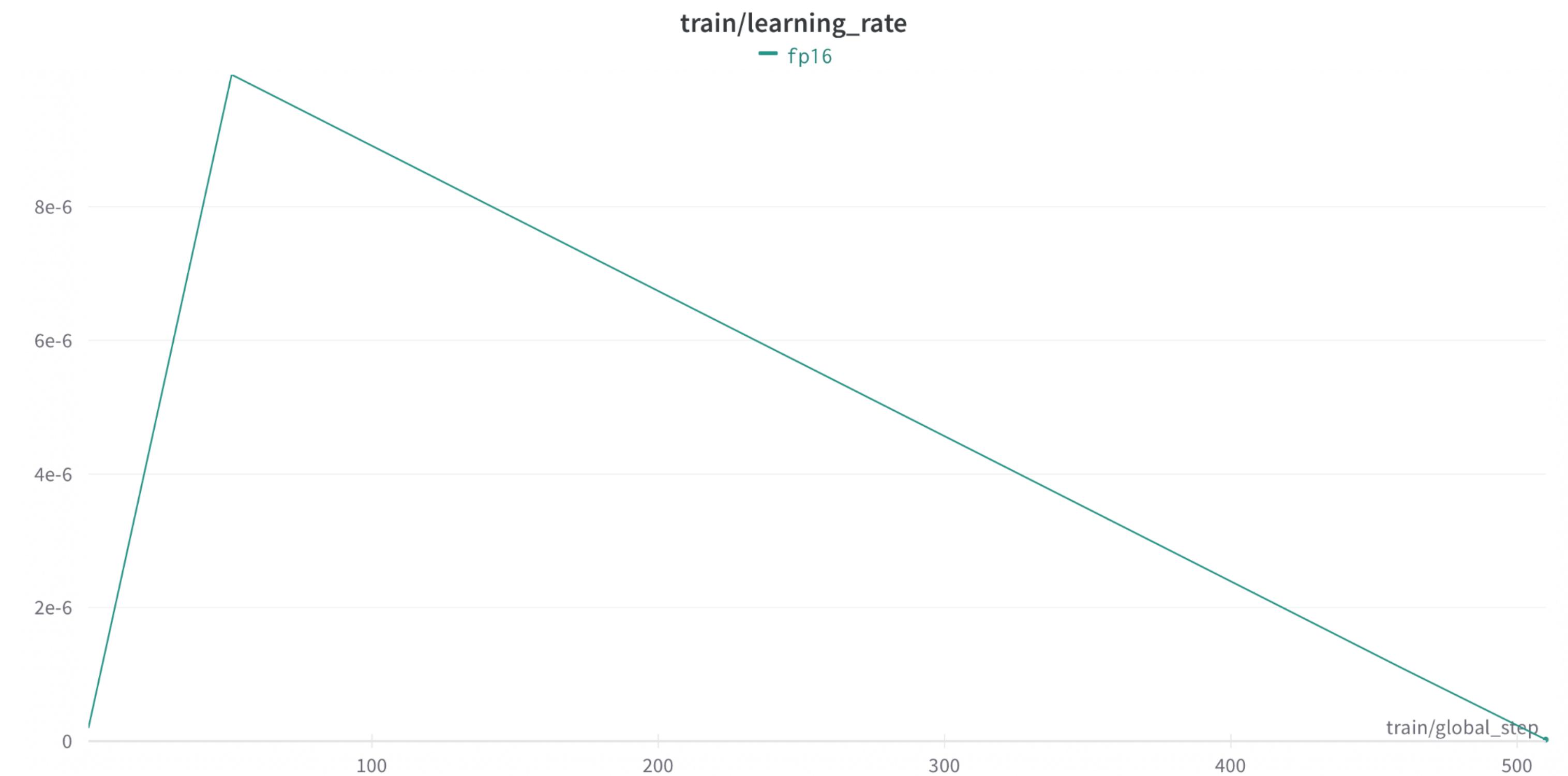
## 3. Square root scaling rule

SGD

$$\hat{\alpha} = k \cdot \alpha$$

Adaptive algorithms  
(Adam, RMSProp and etc.)

$$\hat{\alpha} = \sqrt{k} \cdot \alpha$$



# Как ещё увеличивать размер батча?

LARS (Layer-wise Adaptive Rate Scaling):

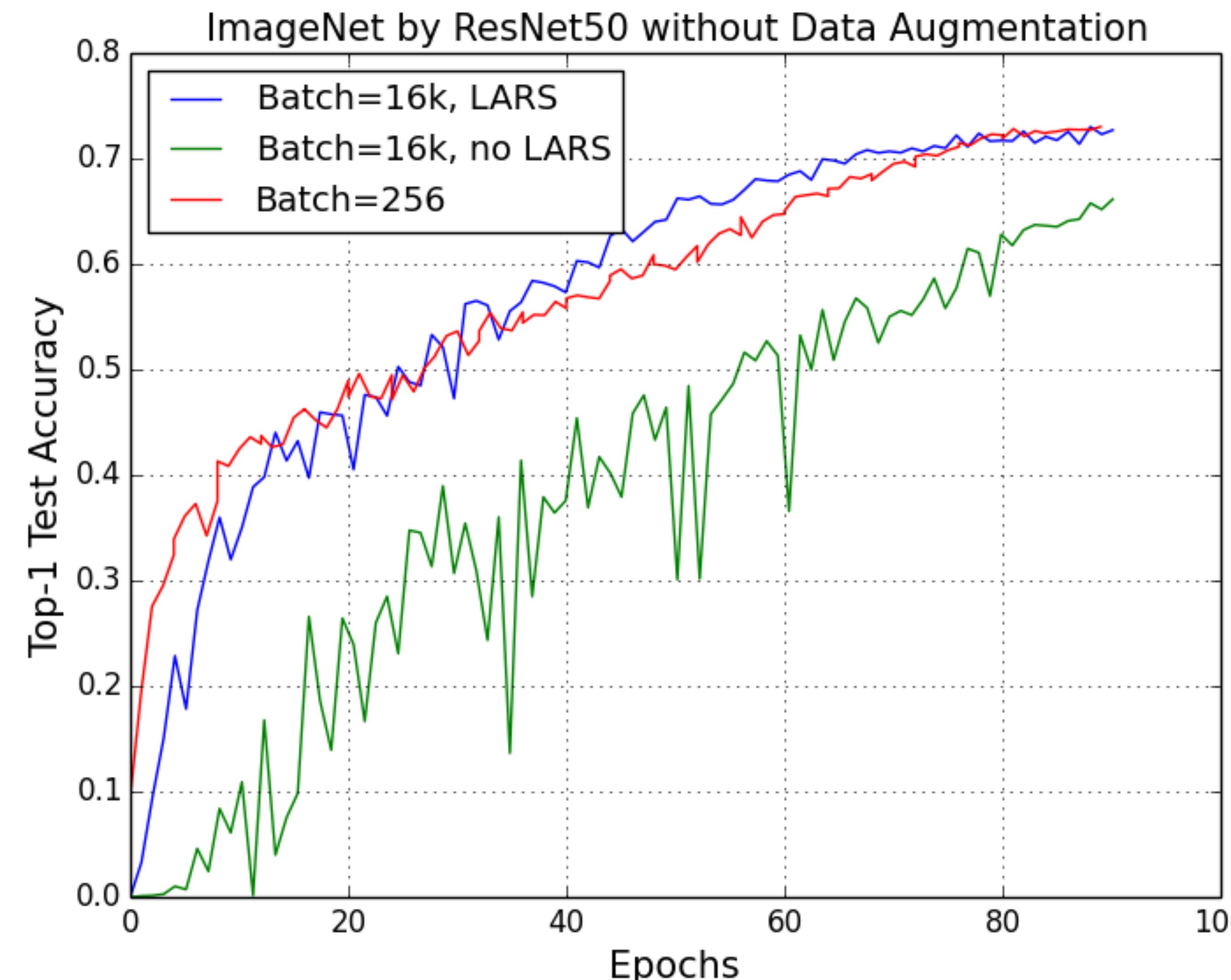
Linear scaling rule + для каждого слоя свой learning rate, который шкалируется на норму весов этого слоя.

$$\hat{\alpha}_l = k\alpha_l \frac{\|w_l\|}{\|\nabla_{w_l} L\|}$$
$$l = 1, \dots, N_{layers}$$

$w_l$  - веса l-ого слоя  
 $\nabla_{w_l} L$  - градиент по l-ому слою

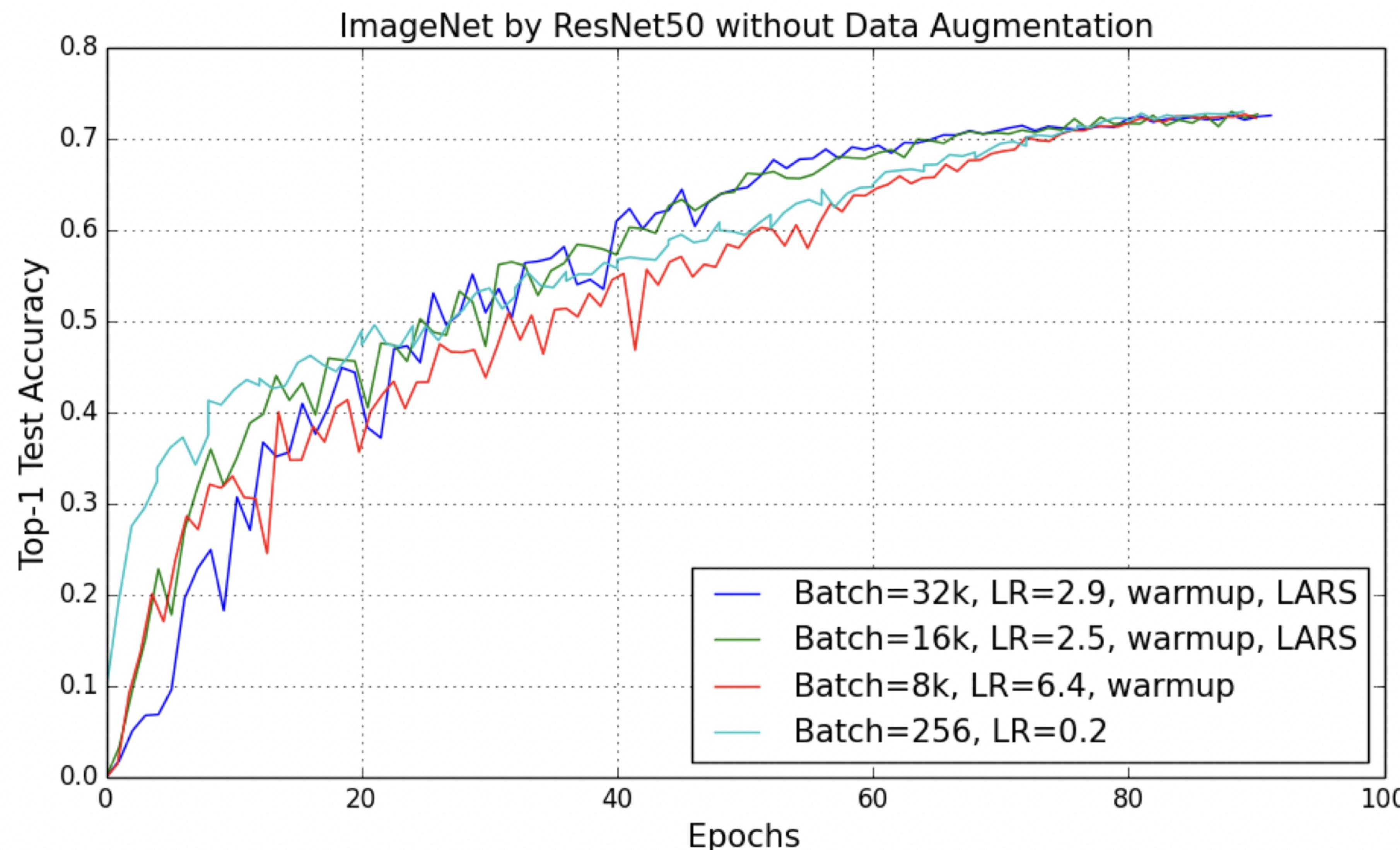
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LARS



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LARS



# Как ещё увеличивать размер батча?

LAMB = LARS + Adam



---

## Algorithm 1 LARS

---

**Input:**  $x_1 \in \mathbb{R}^d$ , learning rate  $\{\eta_t\}_{t=1}^T$ , parameter  $0 < \beta_1 < 1$ , scaling function  $\phi$ ,  $\epsilon > 0$

Set  $m_0 = 0$

**for**  $t = 1$  **to**  $T$  **do**

    Draw b samples  $S_t$  from  $\mathbb{P}$

    Compute  $g_t = \frac{1}{|S_t|} \sum_{s_t \in S_t} \nabla \ell(x_t, s_t)$

$m_t = \beta_1 m_{t-1} + (1 - \beta_1)(g_t + \lambda x_t)$

$x_{t+1}^{(i)} = x_t^{(i)} - \eta_t \frac{\phi(\|x_t^{(i)}\|)}{\|m_t^{(i)}\|} m_t^{(i)}$  for all  $i \in [h]$

**end for**

---

---

## Algorithm 2 LAMB

---

**Input:**  $x_1 \in \mathbb{R}^d$ , learning rate  $\{\eta_t\}_{t=1}^T$ , parameters  $0 < \beta_1, \beta_2 < 1$ , scaling function  $\phi$ ,  $\epsilon > 0$

Set  $m_0 = 0$ ,  $v_0 = 0$

**for**  $t = 1$  **to**  $T$  **do**

    Draw b samples  $S_t$  from  $\mathbb{P}$ .

    Compute  $g_t = \frac{1}{|S_t|} \sum_{s_t \in S_t} \nabla \ell(x_t, s_t)$ .

$m_t = \beta_1 m_{t-1} + (1 - \beta_1)g_t$

$v_t = \beta_2 v_{t-1} + (1 - \beta_2)g_t^2$

$m_t = m_t / (1 - \beta_1^t)$

$v_t = v_t / (1 - \beta_2^t)$

    Compute ratio  $r_t = \frac{m_t}{\sqrt{v_t} + \epsilon}$

$x_{t+1}^{(i)} = x_t^{(i)} - \eta_t \frac{\phi(\|x_t^{(i)}\|)}{\|r_t^{(i)} + \lambda x_t^{(i)}\|} (r_t^{(i)} + \lambda x_t^{(i)})$

**end for**

---

# Как ещё увеличивать размер батча?

LAMB

Solver	batch size	steps	F1 score on dev set	TPUs	Time
Baseline	512	1000k	90.395	16	81.4h
LAMB	512	1000k	91.752	16	82.8h
LAMB	1k	500k	91.761	32	43.2h
LAMB	2k	250k	91.946	64	21.4h
LAMB	4k	125k	91.137	128	693.6m
LAMB	8k	62500	91.263	256	390.5m
LAMB	16k	31250	91.345	512	200.0m
LAMB	32k	15625	91.475	1024	101.2m
LAMB	64k/32k	8599	90.584	1024	76.19m

# Как ещё увеличивать размер батча?

## LAMB

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LAMB	64k/32k	8599	90.584	1024	76.19m

76 минут на 1024 TPU 😊

# Аккумуляция градиентов



БЫЛО:

```
# loop through batches
for (inputs, labels) in data_loader:

    # extract inputs and labels
    inputs = inputs.to(device)
    labels = labels.to(device)

    # passes and weights update
    with torch.set_grad_enabled(True):

        # forward pass
        preds = model(inputs)
        loss = criterion(preds, labels)

        # backward pass
        loss.backward()

        # weights update
        optimizer.step()
        optimizer.zero_grad()
```



СТАЛО:

```
# batch accumulation parameter
accum_iter = 4

# loop through enumaretad batches
for batch_idx, (inputs, labels) in enumerate(data_loader):

    # extract inputs and labels
    inputs = inputs.to(device)
    labels = labels.to(device)

    # passes and weights update
    with torch.set_grad_enabled(True):

        # forward pass
        preds = model(inputs)
        loss = criterion(preds, labels)

        # normalize loss to account for batch accumulation
        loss = loss / accum_iter

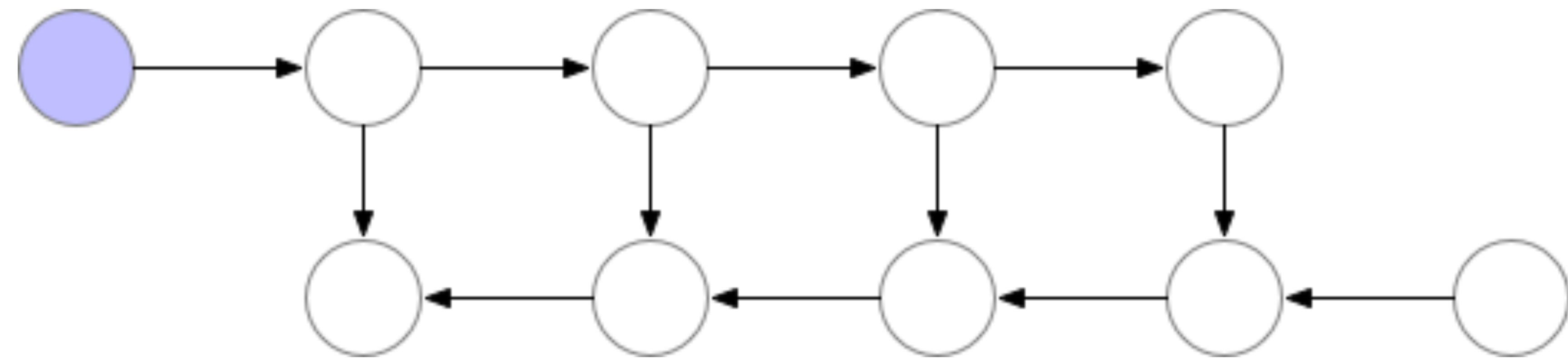
        # backward pass
        loss.backward()

        # weights update
        if ((batch_idx + 1) % accum_iter == 0) or (batch_idx + 1 == len(data_loader)):
            optimizer.step()
            optimizer.zero_grad()
```

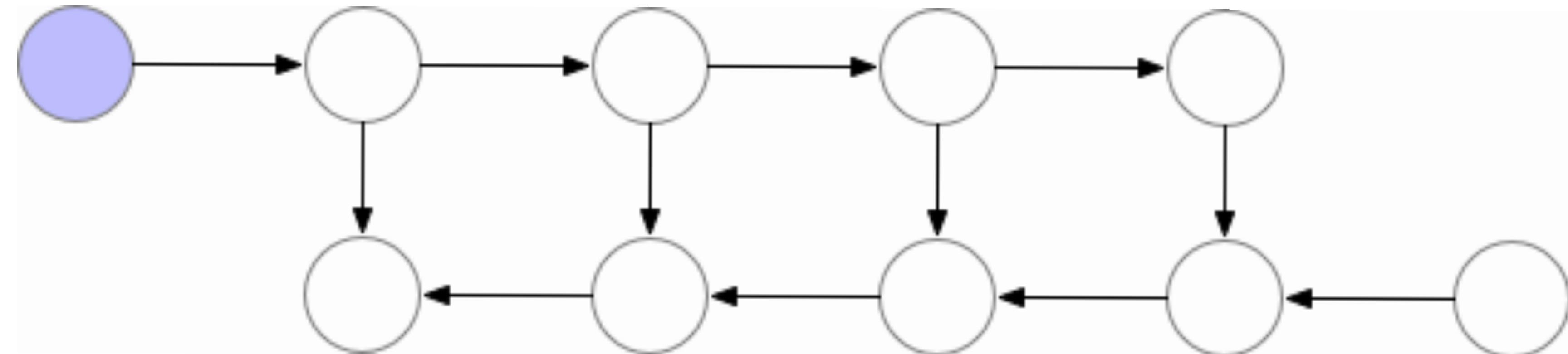
# Gradient checkpointing

## Идея

Обычные Forward и Backward проходы.

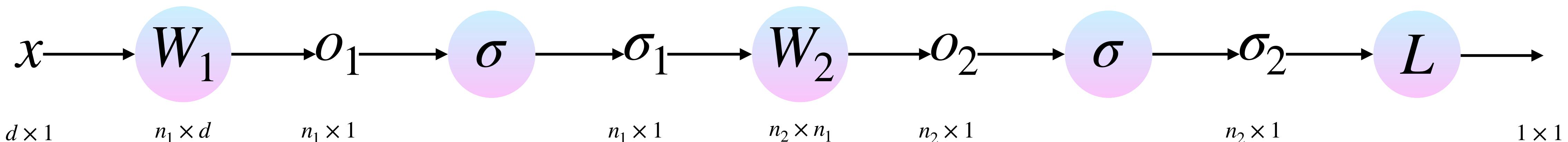


Экономный вариант Forward и Backward проходов. Для вычисления градиентов нужны значения активаций с предыдущих шагов. Вместо их хранения, они пересчитываются заново.



# Gradient checkpointing

## Идея



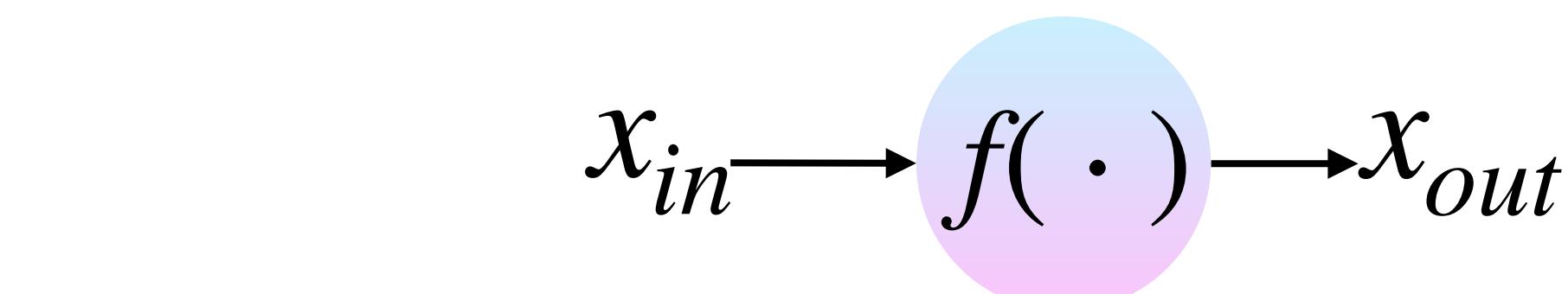
Знаем:

производную  $\frac{\partial L}{\partial x_{out}}$  и

якобиан преобразования  $J$

вычислить:

производную  $\frac{\partial L}{\partial x_{in}}$

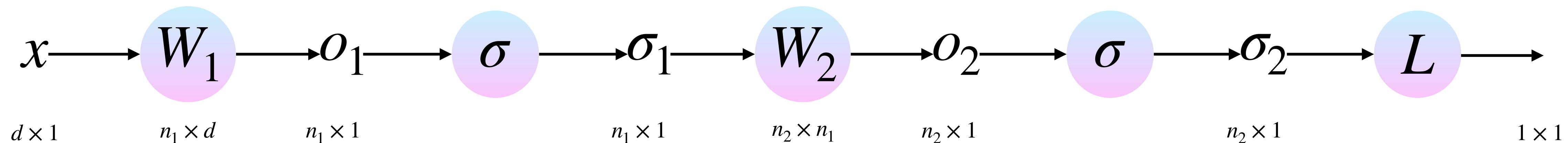


$$\frac{\partial L}{\partial x_{in}} = J \frac{\partial L}{\partial x_{out}}$$

$$\left( \frac{\partial L}{\partial x_{in}} \right)^T = \left( \frac{\partial L}{\partial x_{out}} \right)^T J^T$$

# Gradient checkpointing

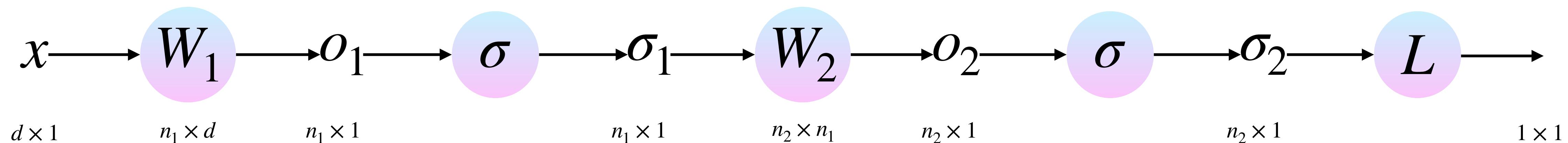
Идея



$$L = \frac{1}{2} \|\sigma_2 - y\|^2$$

# Gradient checkpointing

Идея

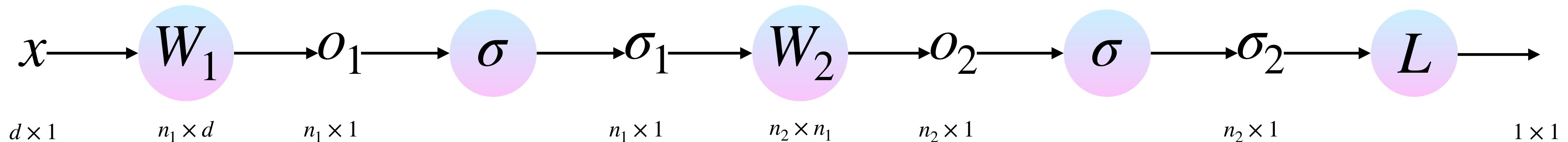


$$L = \frac{1}{2} \|\sigma_2 - y\|^2$$

$$\frac{\partial L}{\partial \sigma_2} = \sigma_2 - y$$

# Gradient checkpointing

Идея

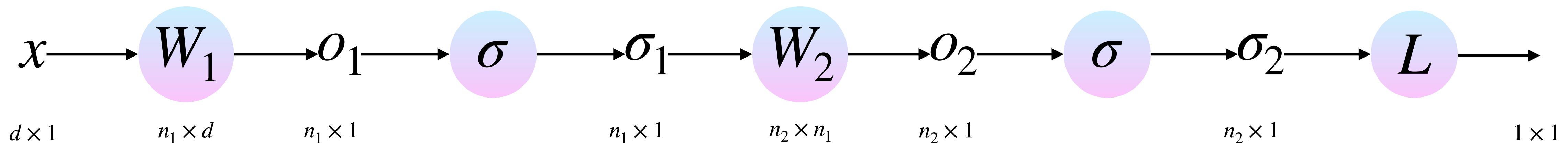


$$L = \frac{1}{2} \|\sigma_2 - y\|^2$$

$$\frac{\partial L}{\partial \sigma_2} = \sigma_2 - y \quad \frac{\partial L}{\partial o_2} = J_\sigma \frac{\partial L}{\partial \sigma_2}$$

# Gradient checkpointing

Идея



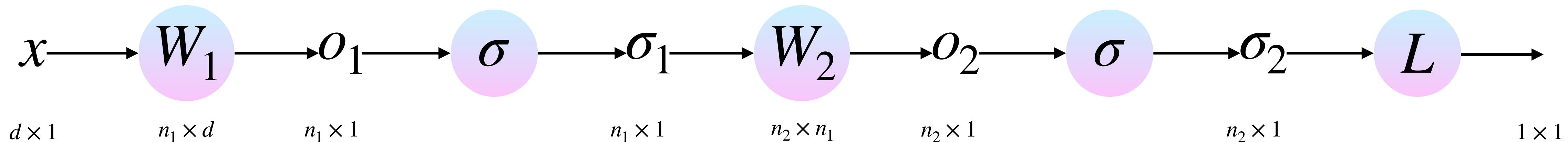
$$L = \frac{1}{2} \|\sigma_2 - y\|^2$$

$$J_\sigma = \text{diag} (\sigma(o_2)(1 - \sigma(o_2))) = \text{diag} (\sigma_2(1 - \sigma_2))$$

$$\frac{\partial L}{\partial \sigma_2} = \sigma_2 - y \quad \frac{\partial L}{\partial o_2} = J_\sigma \frac{\partial L}{\partial \sigma_2}$$

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Идея



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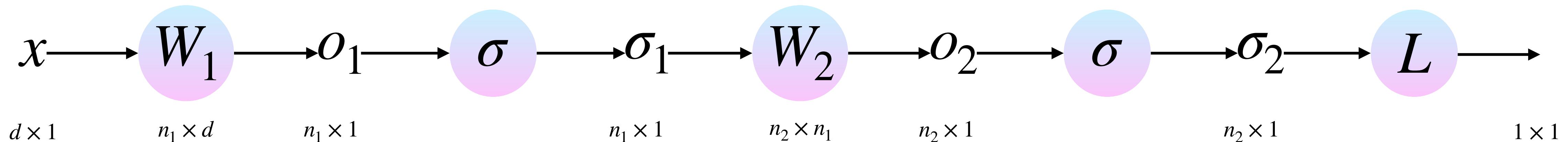
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$$\frac{\partial L}{\partial o_2} = J_\sigma \frac{\partial L}{\partial \sigma_2} = \text{diag} (\sigma_2(1 - \sigma_2))(\sigma_2 - y) = \sigma_2 \odot (1 - \sigma_2) \odot (\sigma_2 - y)$$

# Gradient checkpointing

Идея



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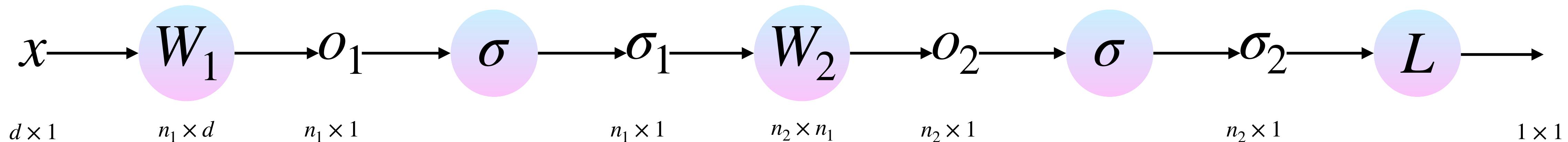
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$$\frac{\partial L}{\partial W_2} = J_{W_2}(W_2) \frac{\partial L}{\partial o_2}$$

$n_1 n_2 \times 1 \quad n_1 n_2 \times n_2 \quad n_2 \times 1$   
 $n_2 \times n_1 \quad (n_2 \times n_1) \times n_2$

# Gradient checkpointing

Идея



$$L = \frac{1}{2} \|\sigma_2 - y\|^2$$

$$J_\sigma = \text{diag} (\sigma(o_2)(1 - \sigma(o_2))) = \text{diag} (\sigma_2(1 - \sigma_2))$$

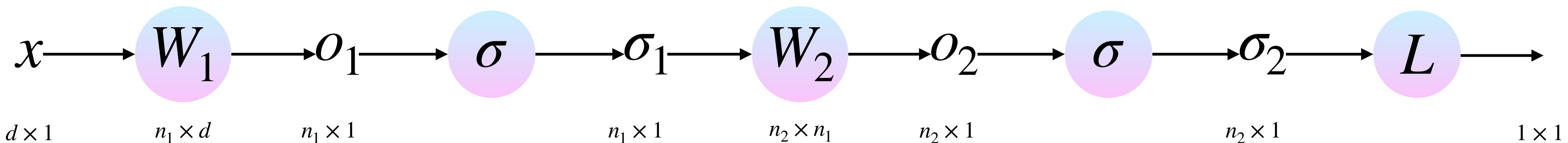
$$\frac{\partial L}{\partial \sigma_2} = \sigma_2 - y \quad \frac{\partial L}{\partial o_2} = J_\sigma \frac{\partial L}{\partial \sigma_2} = \text{diag} (\sigma_2(1 - \sigma_2))(\sigma_2 - y) = \sigma_2 \odot (1 - \sigma_2) \odot (\sigma_2 - y)$$

$$\frac{\partial L}{\partial W_2} = J_{W_2}(W_2) \frac{\partial L}{\partial o_2} = \sigma_2 \odot (1 - \sigma_2) \odot (\sigma_2 - y) \sigma_1^\top$$

$n_2 \times n_1 \qquad \qquad \qquad 1 \times n_1$

# Gradient checkpointing

Идея



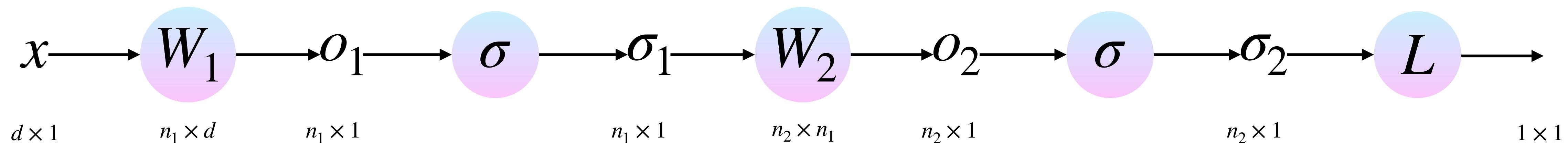
$$\frac{\partial L}{\partial o_2} = \sigma_2 \odot (1 - \sigma_2) \odot (\sigma_2 - y) \quad J_{W_2}(\sigma_1) = W_2^\top$$

$$\frac{\partial L}{\partial \sigma_1} = J_{W_2}(\sigma_1) \frac{\partial L}{\partial o_2} \quad \frac{\partial L}{\partial \sigma_1} = W_2^\top \sigma_2 \odot (1 - \sigma_2) \odot (\sigma_2 - y)$$

$$\frac{\partial L}{\partial o_1} = \sigma_1 \odot (1 - \sigma_1) \odot \frac{\partial L}{\partial \sigma_1} = \sigma_1 \odot (1 - \sigma_1) \odot W_2^\top \sigma_2 \odot (1 - \sigma_2) \odot (\sigma_2 - y)$$

# Gradient checkpointing

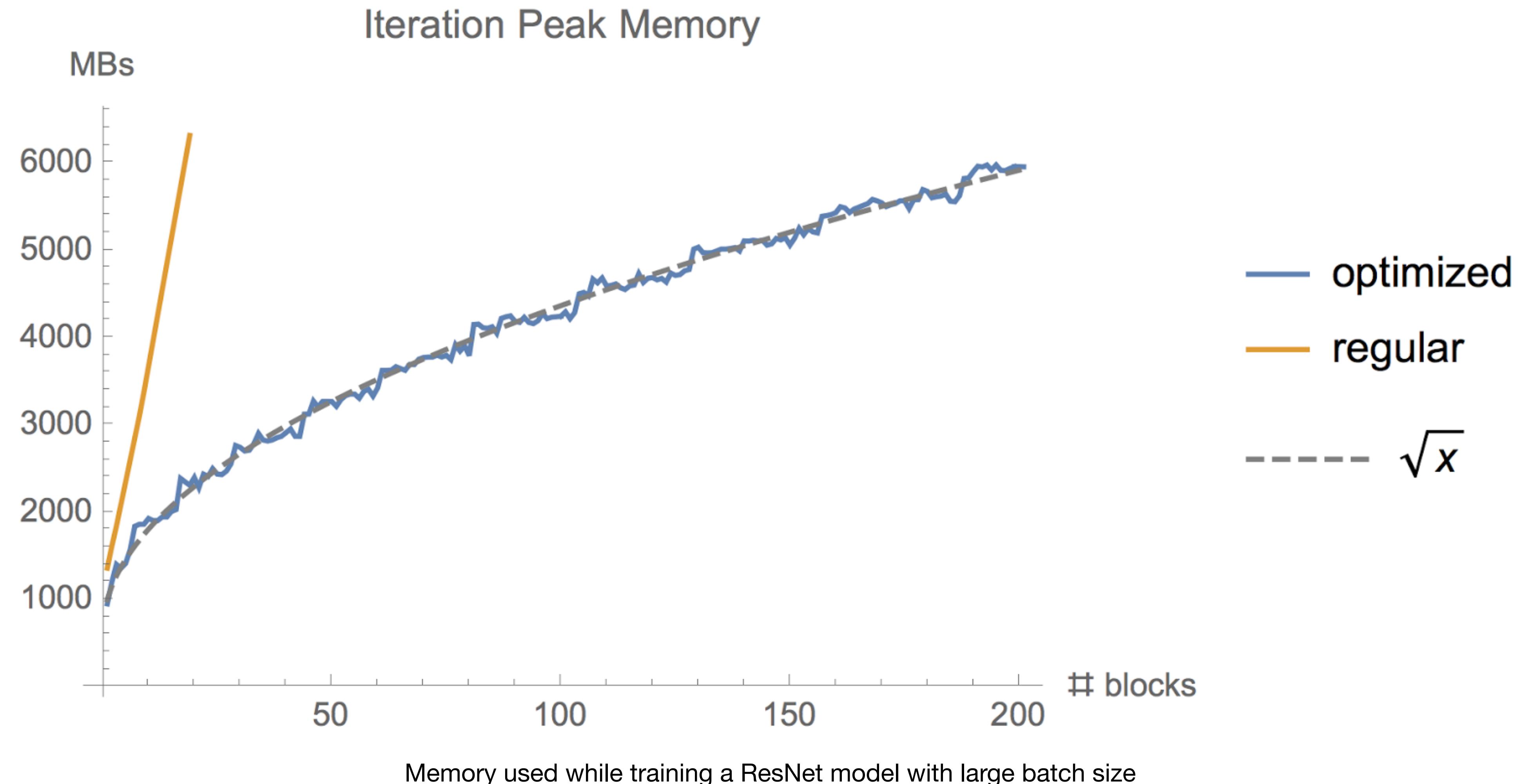
Идея



$$\frac{\partial L}{\partial W_1} = J_{W_1}(W_1) \frac{\partial L}{\partial o_1} = \sigma_1 \odot (1 - \sigma_1) \odot W_2^\top \sigma_2 \odot (1 - \sigma_2) \odot (\sigma_2 - y) x^\top$$

# Gradient checkpointing

Идея



# Gradient checkpointing

## Примеры

	Batch Size	Memory	T4	V100
✗	64	9.42 GB	47m 30s	18m 51s
✓	64	3.71 GB	1h 0m 34s	23m 48s

```
training_args = TrainingArguments(  
    per_device_train_batch_size=1, gradient_accumulation_steps=4, gradient_checkpointing=True,  
)
```

**GPT3small\_Puskin without checkpointing (batch = 8, sec\_len = 512)**

Aa index	# used_mem	# delta_mem	# delta_time	+ ...
begin	5804	0	0	
forward	13006	7202	0.04	
backward	14576	8772	1.2	
optim_step	14576	8772	0.02	
end	5840	36	0.13	
total	15109.75	0	1.396	

**GPT3small\_Puskin with checkpointing (batch = 8, sec\_len = 512) ...**

Aa index	# used_mem	# delta_mem	# delta_time	+ ...
begin	4828	0	0	
forward	6398	1570	0.45	
backward	7968	3140	1.14	
optim_step	7968	3140	0.05	
end	4828	0	0.01	
total	15109.75	0	1.655	

# Activation quantization

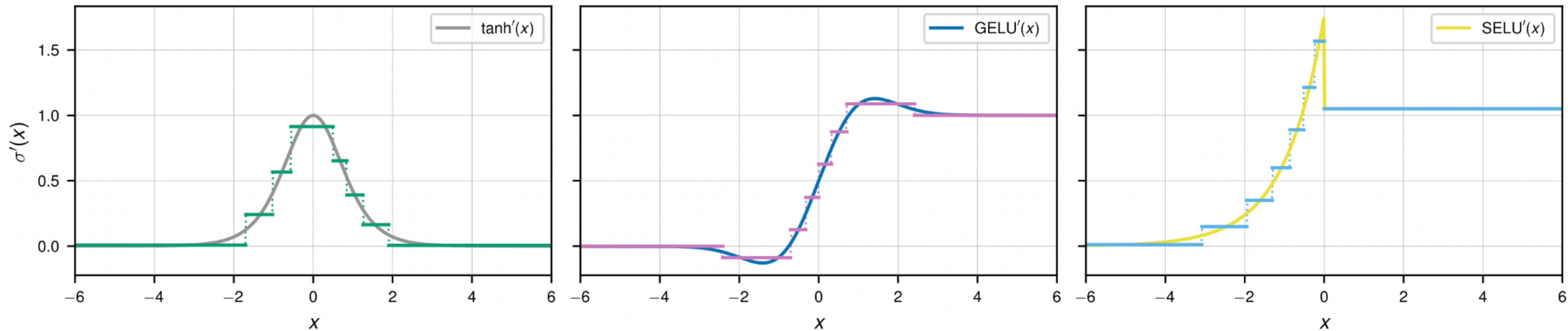


Figure 1. Optimized 3-bit piecewise-constant approximations of the derivatives of activation functions.

	Task	Batch Size	GELU	Linear Layer	Peak Memory, GiB	Saving, %
1	MRPC	128	Vanilla	Vanilla	11.30	0.0
2	MRPC	128	3-bit	Vanilla	9.75	13.8
3	MRPC	128	Vanilla	Randomized	9.20	18.6
4	MRPC	128	3-bit	Randomized	7.60	32.7

# Automatic Mixed Precision training

Fine-tuning **32-bit** model for 215 iterations.

Time: **01:32**

Peak GPU memory consumption:

**8325 MB**

Loss: 2.7370730377906978

Fine-tuning **16-bit** model for 215 iterations.

Time: 01:01

Peak GPU memory consumption:

**6691 MB**

Loss: 2.737271473019622

- B : Baseline (FP32)
- AMP : Automatic Mixed Precision Training (AMP)

Algorithm	Test Accuracy	GPU Memory	Total Training Time
B - 1080 Ti	94.13	10737MB	64.9m
B - 2080 Ti	94.17	10855MB	54.3m
AMP - 1080 Ti	94.07	6615MB	64.7m
AMP - 2080 Ti	94.23	7799MB	37.3m

# LION optimizer

## Symbolic Discovery of Optimization Algorithms

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### Algorithm 1 AdamW Optimizer

---

```
given  $\beta_1, \beta_2, \epsilon, \lambda, \eta, f$ 
initialize  $\theta_0, m_0 \leftarrow 0, v_0 \leftarrow 0, t \leftarrow 0$ 
while  $\theta_t$  not converged do
     $t \leftarrow t + 1$ 
     $g_t \leftarrow \nabla_{\theta} f(\theta_{t-1})$ 
    update EMA of  $g_t$  and  $g_t^2$ 
     $m_t \leftarrow \beta_1 m_{t-1} + (1 - \beta_1) g_t$ 
     $v_t \leftarrow \beta_2 v_{t-1} + (1 - \beta_2) g_t^2$ 
    bias correction
     $\hat{m}_t \leftarrow m_t / (1 - \beta_1^t)$ 
     $\hat{v}_t \leftarrow v_t / (1 - \beta_2^t)$ 
    update model parameters
     $\theta_t \leftarrow \theta_{t-1} - \eta_t (\hat{m}_t / (\sqrt{\hat{v}_t} + \epsilon) + \lambda \theta_{t-1})$ 
end while
return  $\theta_t$ 
```

---

---

### Algorithm 2 Lion Optimizer (ours)

---

```
given  $\beta_1, \beta_2, \lambda, \eta, f$ 
initialize  $\theta_0, m_0 \leftarrow 0$ 
while  $\theta_t$  not converged do
     $g_t \leftarrow \nabla_{\theta} f(\theta_{t-1})$ 
    update model parameters
     $c_t \leftarrow \beta_1 m_{t-1} + (1 - \beta_1) g_t$ 
     $\theta_t \leftarrow \theta_{t-1} - \eta_t (\text{sign}(c_t) + \lambda \theta_{t-1})$ 
    update EMA of  $g_t$ 
     $m_t \leftarrow \beta_2 m_{t-1} + (1 - \beta_2) g_t$ 
end while
return  $\theta_t$ 
```

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