Think It Through

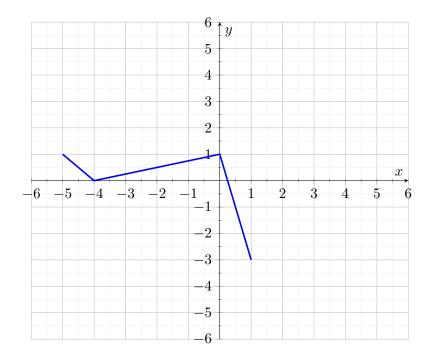
November 16

1. Let $f(x) = x^2$, $g(x) = x^2 + 1$ and $h(x) = \sqrt{x}$. Determine each of the following.

- (a) $(f \circ g)(x)$
- (b) $(g \circ f)(x)$
- (c) $(g \circ f \times h)(x)$
- (d) (g+h)(x)
- (e) (g h)(x)

2. Let g(x) = af(b(x-h) + k) be the function obtained by applying transformations the the graph of f(x). Write down what transformations the parameters represent. (parameters are a, b, h, and k.

3. Consider the function f(x) below.



Draw g(x) in each of the following circumstances and determine its new domain and range.

- (a) g(x) = 2f(x+1)
- (b) g(x) = -f(2x+2)
- (c) $g(x) = -\frac{1}{2}f(-3x+6) 1$

(d) The relation that is acquired after each of the following transformations are applied to f(x)

- \bullet Reflection in the x-axis
- Stretch by a factor of 2 in the y-axis
- Reflection in the line y = x
- Vertical translation 3 units down

- 4. Let f(x) = |x + 3|, x > 0. Each of the following transformations are applied to f(x) to arrive at g(x).
 - Shifted 3 units up
 - translated 4 units right
 - Reflection in y-axis
 - Shifted 2 units down
 - Stretch by a factor of a in the x-axis

Find a so that g(-20) = 4

- 5. Let $f(x) = \sqrt{x}$. Each of the following transformations are applied to f(x) to arrive at g(x)
 - reflection in the line y = x
 - stretch by a factor of 2 about the y-axis
 - Shift 3 units up
 - Stretch by a factor of 2 in the x-axis

Write the function g(x) in terms of x.

- 6. Let $f(x) = \frac{1}{x}$. Write the function g(x) = 2f(-3(x+1)) + 1 in terms of x and describe what transformations occurred in what order.
- 7. Let $f(x) = \frac{1}{2}(3(x+1))^2$ and $g(x) = 3x^2 + 2$. Describe the transformations that occur to transform f(x) to g(x) (be sure to include order).
- 8. \bigstar Let $f(x) = \sqrt{x} + 1$. each of the following transformations are applied to f(x) to arrive at the function g(x)
 - Stretch by a factor of $\frac{1}{3}$ about the line x=1
 - Reflection in the line y = x
 - Stretch by a factor of a about the line y = -2

Find a so that g(3) = 4