

# Extra Practice: Prime Factors, Applications, Rational/Irrational, Number Systems & Radicals

Math 10 · Mr. Merrick

## Prime Factors

- State *all* positive divisors of the following.
  - 84
  - 75
  - 96
  - 105
- In each case, determine the *number* of factors of the given whole number.
  - 96
  - 131
  - 225
  - 256
  - 374
- From the list in Question 2, state which numbers are prime and which are composite.
- Classify each whole number as prime or composite.  
(a) 47   (b) 91   (c) 101   (d) 143   (e) 221   (f) 257
- Twin primes are consecutive odd primes (e.g. 5, 7). List seven other twin-prime pairs  $< 120$ .
- State the factors of 48.
  - State the *prime* factors of 48.
  - Express 72 as a product of prime factors.
- State the *prime factors* of:
  - 18
  - 40
  - 63
  - 90
- Explain why the numbers 0 and 1 have no prime factors.
- Use a *division table* to determine the prime factorization of:
  - 252
  - 378
  - 2025
  - 2926
- Use a *factor tree* to determine the prime factorization of:
  - 784
  - 960
  - 4725
  - 8400
- In each case, write the number as a product of prime factors.
  - 3315
  - 8085
  - 9990
  - 7980
- Which of the following numbers is *not* a prime factor of 2079?  
**A. 3   B. 7   C. 11   D. 13**
- How many numbers in the list 2, 3, 9, 13 are *not* prime factors of 2592?
- The sum of all *distinct* prime factors of 462 462 is \_\_\_\_\_.
- There is only one set of *prime triplets* (three consecutive odd primes). If the triplets are  $a, b, c$ , find  $abc$ .
- The number 375 can be expressed as  $p \times q^r$  in primes. Find  $p + q + r$ .

## Applications of Prime Factors

1. State the greatest common factor (GCF) of:
  - a) 18 and 27
  - b) 32 and 56
  - c) 36, 48, 90
2. Use prime factorization to determine the GCF of:
  - a) 180 and 420
  - b) 294 and 385
  - c) 252 and 756
3. Use prime factorization to determine the GCF of each pair.
  - a) 528 and 780
  - b) 616 and 840
  - c) 1870 and 2210
  - d) 714 and 1050
  - e) 128 and 320
  - f) 735 and 980
4. Determine the GCF of:
  - a) 84, 420, 1008
  - b) 128, 984, 1496, 3080
5. State the lowest common multiple (LCM) of:
  - a) 8 and 12
  - b) 7 and 9
  - c) 12 and 20
  - d) 15 and 18
6. Use prime factorization to determine the LCM of:
  - a) 18 and 24
  - b) 45 and 84
  - c) 96 and 144
  - d) 55 and 143
  - e) 72 and 252
7. Determine the LCM of:
  - a) 8, 12, 18
  - b) 6, 14, 35
  - c) 9, 10, 25
  - d) 12, 30, 105
8. In each case, decide whether the number is a perfect square (give the root if so).
  - a) 9801
  - b) 7776
  - c) 4900
  - d) 1089
9. Consider 103 823.
  - a) Evaluate  $\sqrt[3]{103\,823}$ .
  - b) Explain why 103 823 is a perfect cube.
10. Use prime factorization to test for perfect cubes (give the cube root if so).
  - a) 2744
  - b) 110 592
  - c) 35 937
  - d) 421 875
11. Explain how to tell if a number is *both* a perfect square and cube.
12. The greatest common factor of 425 and 595 is **A. 5   B. 7   C. 17   D. 85**
13. Two whole numbers  $x, y$  have  $\gcd(x, y) = 14$ . Which statement must be false?  
**A.**  $x, y$  both even   **B.**  $xy$  divisible by 98  
**C.**  $x, y$  both multiples of 7   **D.** Neither  $x$  nor  $y$  can be prime
14. The LCM of 36, 231, 275 is \_\_\_\_\_.
15. An encyclopedia has 840 pages. Page 12 and every 12th page is green; page 21 and every 21st is orange. How many pages are both?

## Rational and Irrational Numbers

- For each, state repeating/non-repeating and terminating/non-terminating.
  - $\frac{7}{20}$
  - $0.742742742\dots$
  - $\frac{19}{22}$
  - $\sqrt{\frac{196}{400}}$
  - $-\sqrt{31}$
  - $\sqrt{0.36}$
  - $-4\frac{5}{11}$
  - $\pi$
- True/False.
  - Every terminating decimal is rational.
  - A repeating decimal cannot be written as a fraction.
  - Only terminating decimals are rational.
  - Every rational decimal is either terminating or repeating.
  - A decimal cannot be both repeating and non-repeating.
  - $\pi$  is irrational.
- Rational or irrational? Briefly justify.
  - $-\frac{17}{8}$
  - $0.605$
  - $\sqrt{196}$
  - $0.305305305\dots$
- Order on a number line:  
 $\sqrt{14}$ ,  $\sqrt{\pi}$ ,  $\sqrt{0.2}$ ,  $\sqrt{98}$ ,  $2\sqrt{11}$ ,  $3\sqrt{5}$ .
- Identify as rational or irrational; if rational, simplest fraction.
  - $0.92$
  - $\sqrt{\frac{9}{121}}$
  - $\sqrt{0.0121}$
  - $-\sqrt{97}$
  - $-0.\bar{8}$
  - $-\sqrt{\frac{49}{81}}$
  - $4.612612\dots$
  - $\sqrt{\frac{361}{529}}$
  - $5.\bar{0}$
- Convert to improper fraction (simplest form).
  - $0.\bar{7}$
  - $0.1\bar{6}$
  - $1.2\bar{3}$
  - $0.\overline{204}$
  - $-2.45\overline{45}$
- Convert the repeating decimal to a fraction (algebraic method).
  - $0.\bar{3}$
  - $0.7\bar{2}$
  - $0.009\overline{81}$
- Convert each terminating decimal to an improper fraction (lowest terms).
  - $3.007$
  - $-2.125$
  - $4.0625$
- The decimal for  $\frac{7}{12}$  is
  - terminating & repeating
  - terminating & non-repeating
  - non-terminating & repeating
  - non-terminating & non-repeating
- Which is irrational?
 

**A.**  $\sqrt{256}$    **B.**  $\sqrt{0.09}$    **C.**  $\frac{25}{6}$    **D.**  $\sqrt{50}$
- $9.\bar{9}$  is equal to
 

**A.**  $\frac{99}{10}$    **B.**  $\frac{999}{100}$    **C.** 10   **D.** 9
- Write  $0.\overline{27} = \frac{a}{b}$  in lowest terms and compute  $b - a$ .

## Number Systems

- Place each into the appropriate nested sets ( $N \subset W \subset \mathbb{Z} \subset \mathbb{Q} \subset \mathbb{R}$  and  $\mathbb{R} \setminus \mathbb{Q}$ ):  $-3$ ,  $\sqrt{81}$ ,  $\frac{29}{11}$ ,  $\sqrt{2}$ ,  $0$ ,  $\pi$ .
- List all sets (largest  $\rightarrow$  smallest) each belongs to.
  - $-8$
  - $\sqrt{64}$
  - $3.2727\dots$
  - $-\frac{12}{7}$
  - $0$
  - $\sqrt{11}$
  - non-repeating  $-2.1345218\dots$
  - $\pi$
- Why does  $-7$  belong to more sets than  $-\frac{7}{2}$ ?
- Indicate membership in  $N, W, \mathbb{Z}, \mathbb{Q}, \overline{\mathbb{Q}}$  (irrationals), and  $\mathbb{R}$  for each.
  - $\frac{1}{5}$
  - $123987$
  - $-4$
  - $7.534$
  - $9.5$
  - $\sqrt{75}$
  - $-\pi$
  - $-\frac{355}{113}$
  - $-\sqrt{49}$
  - $0.000005$
  - non-repeating  $2.232425\dots$
- Find a number that satisfies each condition.
  - Integer but not whole.
  - Rational but not integer.
  - Real but not rational.
  - Whole but not natural.
- Fill with *always/sometimes/never*.
  - A whole number is \_\_\_\_\_ a natural number.
  - The quotient of two integers is \_\_\_\_\_ an integer.
  - A whole number is \_\_\_\_\_ a rational number.
  - The difference between two integers is \_\_\_\_\_ an integer.
  - The square root of a number is \_\_\_\_\_ irrational.
  - A negative number is \_\_\_\_\_ in  $W$ .
  - A number in  $N$  is \_\_\_\_\_ in  $\mathbb{R}$ .
- True/False.
  - All natural numbers are integers.
  - Real numbers consist of rationals and irrationals.
  - Integers are nested within rationals.
  - All integers are rational.
  - All irrationals are real.
  - $\mathbb{R}$  is contained in  $N$ .
  - $\mathbb{Q}$  is contained in  $W$ .
  - Exactly one element of  $W$  is not in  $N$ .
- More about roots (True/False).
  - Every positive number has two square roots but one cube root.
  - Every negative number has one real cube root but no real square roots.
- Short explanations (estimation).
  - $\sqrt{8} + \sqrt{17} \neq \sqrt{25}$
  - $\sqrt{2} + \sqrt{3} + \sqrt{4} \neq \sqrt{9}$
- Determine true or false.
  - $\sqrt{9} + \sqrt{4} = \sqrt{9+4}$ .
  - $\sqrt{9} - \sqrt{4} = \sqrt{9-4}$ .
  - $\sqrt{9} \cdot \sqrt{4} = \sqrt{36}$ .
  - $\sqrt{9} + \sqrt{4} = \sqrt{9} + 4$ .

11. For each, (i) estimate mentally; (ii) use a calculator (nearest tenth) and judge the estimate.
- $\sqrt{21}$
  - $\sqrt{27.4}$
  - $4\sqrt{48} - 3\sqrt{63}$
  - $\frac{3}{4}\sqrt{14.2} + \frac{1}{2}\sqrt{5}$
  - $\sqrt{123}$
  - $\sqrt{\sqrt{90}}$
  - $\sqrt{10} + \sqrt{24.5}$
  - $\sqrt{\sqrt{2601}}$
12. Estimate to one significant digit.
- $\sqrt{507.1}$
  - $\sqrt{7991}$
  - $\sqrt{10\,389}$
  - $\sqrt{823\,775}$
  - $\sqrt{0.501}$
  - $\sqrt{0.0501}$
  - $\sqrt{0.0876}$
  - $\sqrt{0.000\,397\,2}$
13. (i) estimate; (ii) calculator (nearest tenth).
- $\sqrt[3]{25}$
  - $\sqrt[3]{2}$
  - $\sqrt[3]{202}$
  - $\sqrt[3]{999.9}$
  - $2\sqrt[3]{58.7} - 3\sqrt[3]{7.62}$
  - $\frac{2}{3}\sqrt{40} - \frac{1}{2}\sqrt{60}$
  - $\sqrt[3]{3\sqrt{10}}$
14. Order on the number line:  
 $\sqrt{50}$ ,  $\sqrt[3]{50}$ ,  $5\sqrt{10}$ ,  $\sqrt[3]{10^3}$ ,  $10\sqrt{5}$ ,  $10\sqrt[3]{5}$ .
15. Which nesting statement is *false*?
- Integers  $\subset$  rationals
  - Wholes  $\subset$  naturals
  - Irrationals  $\subset$  reals
  - Reals  $\subset$  naturals
16. How many of  $-\sqrt{6}$ ,  $\sqrt[3]{-6}$ ,  $-\sqrt[3]{6}$ ,  $\sqrt{-6}$  are not real?
17. How many of  $\sqrt{49}$ ,  $\sqrt{49/100}$ ,  $\sqrt{0.49}$ ,  $\sqrt{\frac{4}{9}}$  can be written as  $\frac{a}{b}$  with  $a, b \in \mathbb{N}$ ?
18. To the nearest hundredth, evaluate  $5\sqrt[3]{7}$ .
19. Evaluate the absolute values.
- $|-4|$
  - $|13|$
  - $|3 - 9|$
  - $||3| - |9||$
  - $|\sqrt[3]{27}|$
  - $|\sqrt[3]{-27}|$
20. Decide whether the statement is true or false.
- $|x| = x$  if  $x > 0$ .
  - $|x| = -x$  if  $x < 0$ .
21. Sketch solution sets on a number line.
- $|x| < 5$
  - $|a| \geq 3$

## Radicals

- Mentally evaluate where possible (real numbers).
  - $\sqrt{81}$
  - $\sqrt[4]{81}$
  - $5\sqrt[3]{27}$
  - $\sqrt[5]{100\,000}$
  - $\sqrt{\frac{16}{25}}$
  - $\sqrt[4]{\frac{1}{16}}$
  - $4\sqrt[4]{\frac{1}{16}}$
  - $-\sqrt{1}$
  - $\sqrt{-1}$
  - $\sqrt[5]{-1}$
  - $7\sqrt[3]{-125}$
  - $-\sqrt[4]{\frac{1}{16}}$
  - $3\sqrt{144}$
  - $\frac{5}{2}\sqrt[5]{32}$
  - $-\sqrt[11]{-1}$
  - $\sqrt[3]{\frac{8}{27}}$
- True/False.
  - The square roots of 25 are  $\pm 5$ .
  - $\sqrt{25} = \pm 5$ .
  - If  $x^2 = 25$  and  $x \in \mathbb{R}$ , then  $x = \pm 5$ .
- Use a calculator to evaluate (state sign first, then value as needed).
  - $\sqrt[4]{4096}$
  - $\sqrt[5]{-243}$
  - $-\sqrt[4]{2401}$
  - $-\sqrt[3]{729}$
  - $\sqrt[3]{-729}$
  - $-8\sqrt[4]{\frac{1}{256}}$
  - $\sqrt[6]{0.015625}$
  - $\sqrt[4]{-6561}$
  - $\frac{3}{2}\sqrt[4]{\frac{16}{81}}$
- Evaluate to the nearest hundredth.
  - $\sqrt[4]{10}$
  - $\sqrt[8]{29}$
  - $\frac{3}{2}\sqrt[3]{-527}$
- Evaluate to the nearest tenth.
  - $\sqrt[5]{-25}$
  - $-5\sqrt[4]{169}$
  - $\frac{1}{2}\sqrt[3]{-81}$
- Identify the *index* and the *radicand* in each radical.
  - $\sqrt[3]{42}$   
index: \_\_\_\_\_  
radicand: \_\_\_\_\_
  - $\sqrt[4]{36}$   
index: \_\_\_\_\_  
radicand: \_\_\_\_\_
  - $5\sqrt{17}$   
index: \_\_\_\_\_  
radicand: \_\_\_\_\_
- Explain the meaning of the index 4 in the radical  $\sqrt[4]{36}$ .
- Determine whether each statement is **true** or **false**.
  - $\sqrt{30} = \sqrt{5}\sqrt{6}$
  - $\sqrt{6-4} = \sqrt{6} - \sqrt{4}$
  - $\sqrt{3} = \frac{\sqrt{45}}{\sqrt{15}}$
  - $\frac{\sqrt{20}}{\sqrt{10}} = \sqrt{10}$
  - $\sqrt{2} + \sqrt{2} = \sqrt{4}$
  - $\sqrt{2} \times \sqrt{2} = \sqrt{4}$
  - $\sqrt{\frac{1}{2} \cdot 30} = \sqrt{15}$
  - $\frac{1}{2}\sqrt{30} = \sqrt{15}$

9. Write as a *single* radical in the form  $\sqrt{x}$  (simplify  $x$ ).
- $\sqrt{5}\sqrt{7}$
  - $\sqrt{14}\sqrt{2}$
  - $\sqrt{3} \cdot \sqrt{8}$
  - $\sqrt{6} \cdot \sqrt{11}$
  - $\frac{\sqrt{20}}{\sqrt{10}}$
  - $\frac{\sqrt{25}}{\sqrt{5}}$
  - $\frac{\sqrt{10}\sqrt{6}}{\sqrt{2}}$
  - $\frac{\sqrt{81}}{\sqrt{9}}$
10. Express each as a product of radicals (split into two square roots).
- $\sqrt{35}$
  - $\sqrt{33}$
  - $\sqrt{65}$
  - $\sqrt{49}$
11. Consider the statements:
- The cube root of  $-27$  (over the reals) is  $\pm 3$ .
  - The fourth roots of  $81$  (over the reals) are  $\pm 3$ .
  - $-\sqrt[3]{1000} = \sqrt[3]{-1000}$ .
  - $-\sqrt[4]{16} = \sqrt[4]{-16}$ .
- Which are true?
- II and III only
  - I, II, and III only
  - I, II, III, and IV
  - Some other combination
12. In the radical  $\sqrt[4]{18}$ , the index and radicand are
- index 2, radicand  $\sqrt{18}$
  - index 1, radicand 1
  - index 18, radicand 1
  - index 4, radicand 18
13. To the nearest hundredth, evaluate  $\sqrt{\frac{7}{8}} + 2\sqrt[4]{\frac{7}{8}}$ .
- \_\_\_\_\_

## Entire Radicals and Mixed Radicals — Part One

- Without a calculator, arrange in order from *greatest to least*:  
 $3\sqrt{5}$ ,  $5\sqrt{3}$ ,  $\sqrt{15}$ ,  $2\sqrt{8}$ ,  $8\sqrt{2}$ .
  - Compute each to the nearest hundredth.
  - Which is more accurate?
  - Exact mixed radical.
- Two students find the hypotenuse  $PQ$  of a right triangle with legs  $\sqrt{34}$  and  $\sqrt{38}$ . Louis rounds each leg; Asia simplifies radicals first.
  - Compute each to the nearest hundredth.
  - Which is more accurate?
  - Exact mixed radical.
- Convert each to a *mixed radical* (simplest form).
  - $\sqrt{96}$
  - $\sqrt{242}$
  - $\frac{2}{3}\sqrt{180}$
  - $\frac{1}{8}\sqrt{320}$
  - $\sqrt{245}$
  - $4\sqrt{338}$
  - $\sqrt{1250}$
  - $\sqrt{66}$
  - $-\frac{5}{6}\sqrt{304}$
  - $\sqrt{980}$
  - $4\sqrt{272}$
  - $-3\sqrt{288}$
  - $2\sqrt{369}$
  - $\sqrt{364}$
  - $\frac{2}{5}\sqrt{450}$
  - $\frac{7}{11}\sqrt{341}$
- Convert to a *mixed radical* where the radicand is a whole number.
  - $\sqrt{\frac{2}{9}}$
  - $\sqrt{\frac{5}{4}}$
  - $\sqrt{\frac{18}{25}}$
  - $7\sqrt{\frac{20}{49}}$
- Convert to *entire radical* form.
  - $2\sqrt{6}$
  - $3\sqrt{7}$
  - $5\sqrt{15}$
  - $12\sqrt{2}$
  - $3\sqrt{25}$
  - $-8\sqrt{3}$
  - $9\sqrt{10}$
  - $-4\sqrt{5}$
- Convert the following to *entire radical* form.
  - $\frac{1}{3}\sqrt{27}$
  - 15
  - $\frac{3}{2}\sqrt{8}$
  - $3^2\sqrt{21}$
- Given  $\sqrt{6} \approx 2.45$  and  $\sqrt{60} \approx 7.75$ , approximate:
  - $\sqrt{600}$
  - $\sqrt{6000}$
  - $\sqrt{600\,000}$
  - $\sqrt{0.06}$
  - $\sqrt{0.6}$
  - $\sqrt{24}$
  - $\sqrt{540}$
  - $\sqrt{\frac{6}{25}}$
- Arrange from *greatest to least*:  
 $3\sqrt{7}$ ,  $5\sqrt{3}$ ,  $\sqrt{60}$ ,  $2\sqrt{11}$ ,  $\frac{1}{2}\sqrt{200}$ .
  - entire radical
  - mixed radical
  - decimal (nearest hundredth)
- In right  $\triangle XYZ$  with legs 19 cm and 5 cm, find hypotenuse  $XY$ :
  - entire radical
  - mixed radical
  - decimal (nearest hundredth)
- Find the missing side in simplest mixed radical form.
  - legs 4, 8; hypotenuse  $x$
  - legs 5, 6; hypotenuse  $x$
  - hypotenuse 8, leg 6; other leg  $x$
- The length of  $\overline{KL}$  for legs  $\sqrt{6}$  and  $\sqrt{24}$  is  
**A.**  $\sqrt{540}$  **B.**  $3\sqrt{2}$  **C.**  $\sqrt{30}$  **D.**  $9\sqrt{2}$
- Without a calculator, which radical is *not* equal to the others?  
**A.**  $12\sqrt{2}$  **B.**  $\sqrt{288}$  **C.**  $6\sqrt{8}$  **D.**  $4\sqrt{72}$



13. On a clear day,  $d = \sqrt{13h}$  (km), where  $h$  metres is eye level above ground. From a 698.2 m building with eye level 1.8 m above the roof, write  $d = a\sqrt{b}$  and find  $a + b$ .
14. Using Heron's formula, a triangle with sides 14, 15, 25 has area  $A = p\sqrt{26}$ . Find  $p$ .
15. A square of side 8 cm is inscribed in a larger square by joining midpoints. If larger side is  $p\sqrt{q}$ , find  $pq$ .

## Entire Radicals and Mixed Radicals — Part Two

- Convert the following radicals to mixed radicals in simplest form.
  - $\sqrt[3]{48}$
  - $\sqrt[3]{128}$
  - $\sqrt[3]{2000}$
  - $5\sqrt[3]{-81}$
  - $\frac{5}{6}\sqrt[3]{108}$
  - $5\sqrt[4]{162}$
  - $5\sqrt{192}$
  - $-2\sqrt[3]{625}$
- Convert the following mixed radicals to entire radicals.
  - $2\sqrt[5]{2}$
  - $3\sqrt[3]{4}$
  - $-3\sqrt[4]{3}$
  - $-10\sqrt[3]{5}$
  - $2\sqrt[5]{6}$
  - $\frac{1}{2}\sqrt[3]{16}$
  - $\frac{3}{10}\sqrt[4]{100000}$
  - $-5\sqrt[3]{9}$
- Arrange, least to greatest (no calculator):  $7\sqrt[6]{1}$ ,  $-3\sqrt[3]{-27}$ ,  $\frac{5}{2}\sqrt[4]{16}$ ,  $3\sqrt[3]{64}$ .
- Consider  $2\sqrt[3]{11}$ ,  $3\sqrt[3]{3}$ ,  $4\sqrt[3]{2}$ ,  $2\sqrt[3]{6}$ .
  - Explain how to compare without a calculator.
  - Order least to greatest.
- $\sqrt[3]{240}$  is equivalent to  
**A.**  $2\sqrt[3]{40}$    **B.**  $4\sqrt[3]{15}$    **C.**  $2\sqrt[3]{30}$    **D.**  $8\sqrt[3]{30}$
- Consider the statements:
  - $-3\sqrt[4]{8} = 3\sqrt[4]{-8}$ ,
  - $-2\sqrt[3]{7} = 2\sqrt[3]{-7}$ .**A.** Both true   **B.** Both false   **C.** 1 true, 2 false  
**D.** 1 false, 2 true
- The mixed radical  $\frac{1}{12}\sqrt[3]{128}$  equals  $a\sqrt[3]{b}$  in simplest form. Find  $a + b$  (nearest tenth).
- $\sqrt{3x} \cdot \sqrt{2x}$  is equivalent to  
**A.**  $\sqrt{6x}$    **B.**  $\sqrt{36x^2}$    **C.**  $6\sqrt{x}$    **D.**  $x\sqrt{6}$
- Express as an *entire* radical.
  - $6\sqrt{y}$
  - $8\sqrt{c^2}$
  - $10\sqrt{2yz^3}$
  - $-3\sqrt[3]{x^2}$
  - $c\sqrt{c}$
  - $x\sqrt{3y^3}$
  - $11c^2\sqrt{c^2d}$
  - $5a^3b\sqrt{3a^2b}$
- Express as a mixed radical in simplest form.
  - $\sqrt{a^5}$
  - $\sqrt{t^3}$
  - $\sqrt{x^{11}}$
  - $\sqrt[3]{x^4}$
  - $\sqrt[3]{b^8}$
  - $\sqrt[4]{x^6}$
- Express as a mixed radical.
  - $\sqrt{8y^2}$
  - $\sqrt{16p^3}$
  - $\sqrt{75y^3z^4}$
  - $\sqrt{300a^9w^7}$
  - $5\sqrt{28c^4d^3}$
  - $-6\sqrt{29a^4b^8}$

## Quick Check

- Which is not a prime factor of 14014?  
A. 7 B. 11 C. 13 D. 17
- How many numbers in the list 7, 11, 17, 21 are prime factors of 3234?  
A. 1 B. 2 C. 3 D. 4
- The sum of prime factors of 160797 is \_\_\_\_.
- The GCF of 6699 and 8265 is \_\_\_\_.
- LCM of 14 and 105 equals GCF of  $P, Q$ . Which must be false?  
A.  $P$  multiple of 7  
B.  $Q$  multiple of 21  
C.  $P < 200$   
D.  $Q > 2000$
- If  $x$  is a perfect square, minimum value of  $d$  (in the given factor tree) is  
A. 2 B. 3 C. 6 D. 9
- If  $x$  is a perfect cube, the minimum value of  $x$  is \_\_\_\_.
- $\otimes$  is irrational. Its decimal representation is  
A. terminating & repeating  
B. terminating & non-repeating  
C. non-terminating & repeating  
D. non-terminating & non-repeating
- Which are rational? (I) 1.0100100001... (non-repeating), (II)  $\sqrt[3]{\frac{8}{27}}$ , (III) 0.04, (IV) 0.29  
A. III, IV  
B. II, III, IV  
C. I, II, III, IV  
D. Other
- The rational number  $1.\overline{54}$  as  $\frac{c}{d}$ ; the value of  $c$  is  
A. 17 B. 11 C. 6 D. 4
- $M, N$  irrationals with  $30 < M < 40, 3 < N < 4$ . The value of  $\sqrt{M} + \sqrt{N}$  is best represented by  
A. P B. Q C. R D. S
- Largest among  $\sqrt[3]{67}, \sqrt[4]{98}, \sqrt{19}, \sqrt[5]{201}$  is  
A.  $\sqrt{19}$  B.  $\sqrt[4]{98}$  C.  $\sqrt[3]{67}$  D.  $\sqrt[5]{201}$
- The length  $12\sqrt[4]{4000}$  m has index and radicand  
A. 4 and 4000  
B. 12 and 4000  
C. 4 and 12  
D. 4000 and 4
- When  $7\sqrt[3]{6}$  is written as an entire radical, the radicand is \_\_\_\_.
- Which statements are true? 1)  $35 = 7\sqrt{5}$  2)  $\sqrt{28} = 2\sqrt{7}$  3)  $4\sqrt{3} = 48$   
A. 1 only  
B. 2 only  
C. 1 and 2 only  
D. 2 and 3 only
- Three students rewrote  $\sqrt{4050}$ . Who is correct?  
A. I only  
B. II and III  
C. All three  
D. Other
- Circle area: if area  $120\pi$  cm<sup>2</sup>, radius is  
A. 60 B.  $12\sqrt{10}$  C.  $2\sqrt{30}$  D.  $2\sqrt{15}$
- A cube with volume 720 mm<sup>3</sup> has edge length  $a\sqrt[3]{b}$  mm. Find  $a + b$ .
- Consider  $4\sqrt[3]{3}, 5\sqrt{x}, 16\sqrt{y}$ . Which is correct?  
A.  $x < y < z$   
B.  $z < x < y$   
C.  $y < z < x$   
D.  $z < y < x$