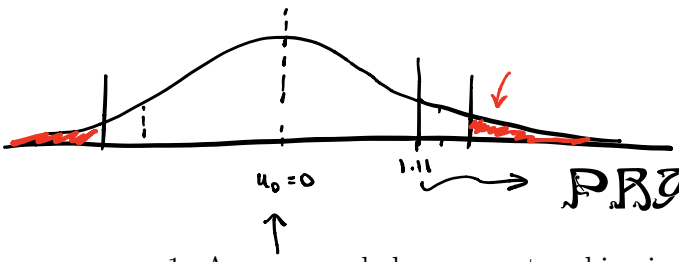
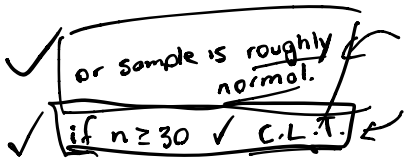


PRACTICE II



1. A company bakes computer chips in two ovens, oven A and oven B. The chips are randomly assigned to an oven and hundreds of chips are baked each hour. The percentage of defective chips coming from these ovens for each hour of production throughout a day is shown below.

	Hour	Oven A	Oven B
d_1	1	45	36
d_2	2	32	37
d_3	3	34	33
d_4	4	31	34
d_5	5	35	33
d_6	6	37	32
d_7	7	31	33
d_8	8	30	30
d_9	9	27	24

1. Will conduct a Paired-t-test for the mean of the differences, μ_d.

$H_0: \mu_d = 0$ ←

$H_a: \mu_d \neq 0$

2. For a t-test we require:

Independent: observations are independent note 9 ovens 'n' is very small in relation to all ovens. 'N'

normality: Sample size is to small for C.L.T to apply, however the diffrences appear to be normaly distributed from normal q-q plot.

3. Carry out the test

$$t = \frac{\mu_d - (0)}{\frac{s_d}{\sqrt{n}}} = \frac{1.11 - (0)}{\left(\frac{4.28}{\sqrt{9}}\right)} = \frac{1.11}{\left(\frac{4.28}{3}\right)} = 0.78$$

$P\text{-value} = 2 \cdot P(t_8 > 0.78)$

$= 0.46$

4. Results

The differences in the mean percentages in the samples of defective chips produced by ovens A and B is not statistically significant as our p-value of 0.46 is more than $\alpha = 0.05$.

If there was no difference in the percentages, the absolut difference of 1.11 or greater would happen 46% of the time with random sampling.

The percentage of defective chips produced each hour by oven A has a mean of 33.56 and a standard deviation of 5.20. The percentage of defective chips produced each hour by oven B has a mean of 32.44 and a standard deviation of 3.78. The hourly differences in percentages for oven A minus oven B have a mean of 1.11 and a standard deviation of 4.28.

Does there appear to be a difference in between oven A and oven B with respect to the mean percentages of defective chips produced? Give appropriate statistical evidence to support your answer.

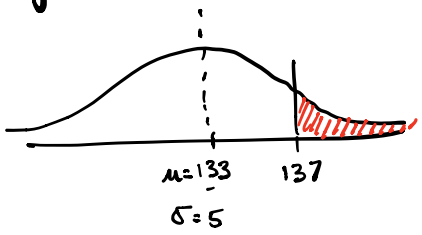
2. A grocery store purchases melons from two distributors, J and K. Distributor J provides melons from organic farms. The distribution of the diameters of the melons from Distributor J is approximately normal with mean 133 millimeters (mm) and standard deviation 5 mm.

(a) For a melon selected at random from Distributor J, what is the probability that the melon will have a diameter greater than 137 mm? Distributor K provides melons from nonorganic farms. The probability is 0.8413 that a melon selected at random from Distributor K will have a diameter greater than 137 mm. For all the melons at the grocery store, 70 percent of the melons are provided by Distributor J and 30 percent are provided by Distributor K

Let X denote the diameter of a randomly selected melon from distributer J.

$X \sim \text{normal}(\mu = 133, \sigma = 5)$

$$\text{Z-score} = \frac{x - \mu}{\sigma} = \frac{137 - 133}{5} = \frac{4}{5} = 0.8$$



So, $P(X > 137) = P(Z > 0.8) = 0.21185$

normalcdf(lb = 0.8, ub = 100000, μ = 0, σ = 1)

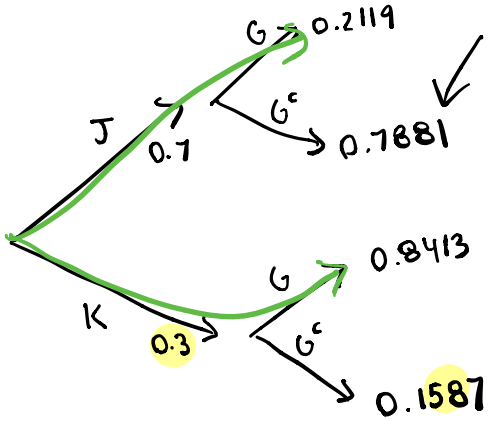
normalcdf(lb = 137, ub = 10000000, μ = 133, σ = 5)

≈ 21.2% of melons will have a diameter greater than 137 mm.

(b) For a melon selected at random from the grocery store, what is the probability that the melon will have a diameter greater than 137 mm?

30% come from K

70% come from J



$$P(G) = P(G|J)\cdot P(J) + P(G|K)\cdot P(K)$$

$P(G \text{ and } J)$ $\quad$ $P(G \text{ and } K)$

$$= 0.7(0.2119) + 0.3(8413)$$

$$= 0.4007$$

There is a 40.1% chance a melon has a diameter greater than 137.

$$P(A|B) = \frac{P(B|A)\cdot P(A)}{P(B)}$$

(c) Given that a melon selected at random from the grocery store has a diameter greater than 137 mm, what is the probability that the melon will be from Distributor J?

$$P(J|G) = \frac{P(G|J)\,P(J)}{P(G)} = \frac{P(J \text{ and } G)}{P(G)}$$

$$= \frac{0.7(0.2119)}{0.4007} = 0.371$$

37.1% of the time the melon will be from distribution J, given its diameter is > 137 mm.

3. A laboratory test for the detection of a certain disease gives a positive result 5 percent of the time for people who do not have the disease. The test gives a negative result 0.3 percent of the time for people who have the disease. Large-scale studies have shown that the disease occurs in about 2 percent of the population.

   (a) What is the probability that a person selected at random would test positive for this disease? Show your work.

   (b) What is the probability that a person selected at random who tests positive for the disease does not have the disease? Show your work.