



# **İzmir Institute of Technology**

Numerical Methods in Engineering

CE301

## **Assignment #1**

### **Section B**

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Mechanical Engineering

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To compare for error, the value of the integral that is accurate to more decimal places than are required is obtained via WolframAlpha:

$$\int_{\pi/6}^{\pi/2} \frac{\cos(x)(e^x + x)}{x^2 - \ln(x)} dx = 1.6724695$$

The MATLAB code (see Appendix A.1) output is as follows:

```
1 The number of sub-intervals needed for :  
2  
3 ----> Compound mid-point: 172  
4 ----> Compound trapezoid: 243  
5 ----> Simpson's rule: 16
```

The code can be further deliberated upon at instructors' request.

# Appendix

## A.1 Computer Code

```
1 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% Mert Emrem - 250203015 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% CE301 - Assignment #1 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
3
4 clc; clear all;
5
6 [a, b, err_goal, h_n] = deal(pi/6, pi/2, 1e-5, 1);
7
8 err = err_goal + 1;
9
10 true_int = 1.6724695;
11
12 f = @(x)(cos(x)*(exp(x)+x))/(x^2-log(x));
13
14 %%%% Compound mid-point:
15
16 while err > err_goal
17
18     h = (b-a)/h_n;
19     sum = 0;
20
21     for k = 1:h_n
22
23         z_i = a + ((k-1)*h) + (h/2);
24         nth_section = h*f(z_i);
25         sum = sum + nth_section;
26
27     end
28
29     err = abs(sum - true_int);
30     h_n = h_n + 1;
31
32 end
33
34 comp_mp_h = h_n - 1;
35
36 %%%% Reset starting conditions
37
```

```

38 h_n = 1;
39 err = err_goal + 1;
40
41
42 %%%% Compound trapezoid:
43
44 %      (a+h*(k-1))+(a+h*k)
45 % h * -----
46 %           2
47
48 while err > err_goal
49
50     h = (b-a)/h_n;
51     sum = 0;
52
53     for k = 1:h_n
54
55         x_alpha = a + h*(k-1);
56         x_beta = a + h*k;
57         nth_section = h * (f(x_alpha)+f(x_beta))/2;
58         sum = sum + nth_section;
59
60     end
61
62     err = abs(sum - true_int);
63     h_n = h_n + 1;
64
65 end
66
67 comp_trap_h = h_n - 1;
68
69 %%%% Reset starting conditions
70
71 h_n = 1;
72 err = err_goal + 1;
73
74
75 %%%% Simpson's rule:
76
77 % (h/3)(A + B + C + D), where A & D are f(x_1), f(x_n)
78
79
80 A = f(a);
81 D = f(b);
82
83
84 while err > err_goal

```

```

85
86     h = (b-a)/h_n;
87     sum = 0;
88
89     B = 0;
90     C = 0;
91
92     for k = 1:2:(h_n-1)
93
94         B_section = 4*f(a+h*k);
95         B = B + B_section;
96
97     end
98
99
100    for k = 2:2:(h_n-1)
101
102        C_section = 2*f(a+h*k);
103        C = C + C_section;
104
105    end
106
107    sum = (h/3)*(A + B + C + D);
108
109    err = abs(sum - true_int);
110    h_n = h_n + 1;
111
112 end
113
114 simpson_h = h_n - 1;
115
116
117
118 disp("The number of sub-intervals needed for:");
119
120 line_1 = ['----> Compound mid-point: ', num2str(comp_mp_h)];
121 line_2 = ['----> Compound trapezoid: ', num2str(comp_trap_h)];
122 line_3 = ['----> Simpson''s rule:      ', num2str(simpson_h)];
123
124 disp(" ");
125 disp(line_1);
126 disp(line_2);
127 disp(line_3);

```