

**GIT Department of Computer Engineering
CSE 222/505 - Spring 2022
Homework #7 Report**

**Mert Gürşimşir
1901042646**

PART 1

THEORETICAL RUN TIME COMPLEXITY ANALYSIS OF QUESTION 1

Java sort uses quick sort so it is $\rightarrow \theta(n \log n)$ on average

Recursive method:

$$T(n) = 2T(n/2) + \theta(1)$$

$$T(n) = 2(2T(n/4) + \theta(1)) + \theta(1) = 2^2T(n/4) + 3\theta(1)$$

$$T(n) = 2^2[2T(n/8) + \theta(1)] + 3\theta(1) = 2^3T(n/8) + 7\theta(1)$$

$$T(n) = 2^3[2T(n/16) + \theta(1)] + 7\theta(1) = 2^4T(n/2^4) + 2^3\theta(1) + 2^2\theta(1) + 2^1\theta(1) + 2^0\theta(1)$$

$$T(n) = 2^5T(n/2^5) + 2^4\theta(1) + 2^3\theta(1) + 2^2\theta(1) + 2^1\theta(1) + 2^0\theta(1)$$

...

$$T(n) = 2^kT(n/2^k) + 2^{k-1}\theta(1) + 2^{k-2}\theta(1) + \dots + 2^0\theta(1)$$

$$2^k = n, \quad k = \log_2 n :$$

$$T(n) = nT(1) + (2^k - 1)\theta(1) = nT(1) + (n - 1)\theta(1) \quad (T(1) = \theta(1))$$

$$T(n) = n + n - 1 = 2n - 1$$

$$T(n) = \theta(n) \rightarrow \text{on average}$$

Or shortly we can say if there are n nodes, there are $2n+1$ calls for the traversal algorithms:

$$T(n) = \theta(n)$$

Adding elements of binary tree to binary search tree (createBST method):

$$T(n) = 2T(n/2) + n$$

$$T(n) = 2^2[T(n/2^2)] + n + n$$

$$T(n) = 2^3[T(n/2^3)] + 3n$$

...

$$T(n) = 2^k(T(n/2^k)) + kn$$

$$2^k = n, \quad k = \log_2 n :$$

$$T(n) = 2^kT(1) + kn$$

$$T(n) = n + n \log n = O(n \log n)$$

IT IS NOT θ BECAUSE WORST CASE FOR ADDING TO BST IS LINEAR

All in all, this program runs in $T(n) = \theta(n \log n)$ time.

THEORETICAL RUN TIME COMPLEXITY ANALYSIS OF QUESTION 2

Rotate to right and left (rotateRight() and rotateLeft()) runs in constant time. $\rightarrow \theta(1)$

convertAVL(node):

$$T(n) = 2T(n/2) + n$$

$$T(n) = 2^2[T(n/2^2)] + n + n$$

$$T(n) = 2^3[T(n/2^3)] + 3n$$

...

$$T(n) = 2^k(T(n/2^k)) + kn$$

$$2^k = n, \quad k = \log_2 n :$$

$$T(n) = 2^k T(1) + kn$$

$$T(n) = n + n \log n = \theta(n \log n)$$

height():

$$T(n) = 2T(n/2) + \theta(1)$$

$$T(n) = 2(2T(n/4) + \theta(1)) + \theta(1) = 2^2 T(n/4) + 3\theta(1)$$

$$T(n) = 2^2[2T(n/8) + \theta(1)] + 3\theta(1) = 2^3 T(n/8) + 7\theta(1)$$

$$T(n) = 2^3[2T(n/16) + \theta(1)] + 7\theta(1) = 2^4 T(n/2^4) + 2^3\theta(1) + 2^2\theta(1) + 2^1\theta(1) + 2^0\theta(1)$$

$$T(n) = 2^5 T(n/2^5) + 2^4\theta(1) + 2^3\theta(1) + 2^2\theta(1) + 2^1\theta(1) + 2^0\theta(1)$$

...

$$T(n) = 2^k T(n/2^k) + 2^{k-1}\theta(1) + 2^{k-2}\theta(1) + \dots + 2^0\theta(1)$$

$$2^k = n, \quad k = \log_2 n :$$

$$T(n) = nT(1) + (2^k - 1)\theta(1) = nT(1) + (n - 1)\theta(1) \quad (T(1) = \theta(1))$$

$$T(n) = n + n - 1 = 2n - 1$$

$$T(n) = \theta(n) \rightarrow \text{on average}$$

balance():

$$T(n) = \theta(n) \rightarrow \text{on average}$$

All in all, this program runs in $T(n) = \theta(n \log n)$ time.

PART 2

1. SYSTEM REQUIREMENTS

Environment

Editor: Sublime Text

OS: Ubuntu

Javac Version: 11.0.15

Q1

To create binary search tree from the elements in the given array and from the structure of given binary tree you can simply use static method convert from the class convertToBST:

```
BinarySearchTree<Integer> bst = convertToBST.convert(root, array);
```

root: binary tree

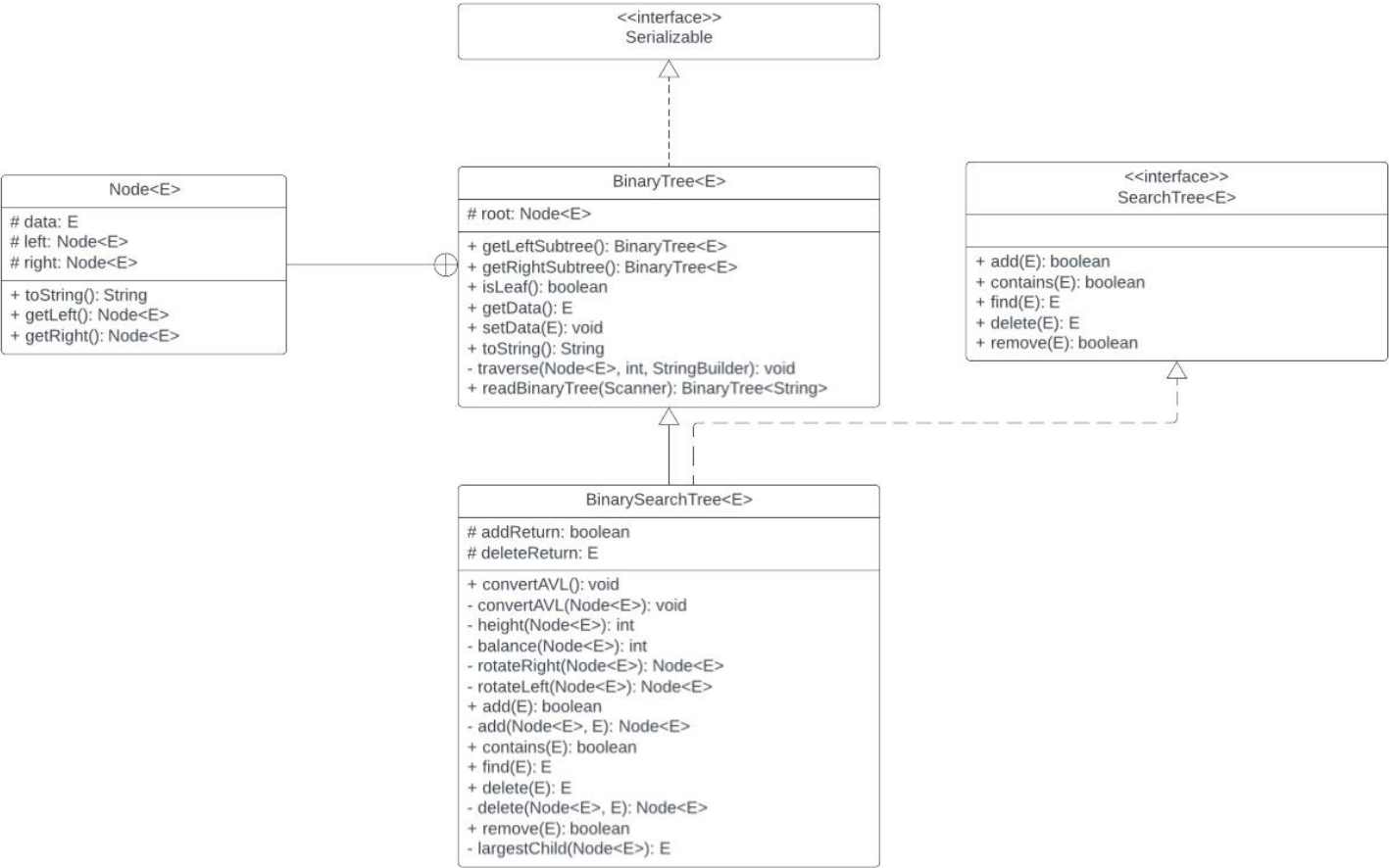
array: array

Q2

To convert binary search tree to AVLTree using rotation operations, you should have a binary search tree (bst1), then you can simply use convertAVL() method:

```
bst1.convertAVL();
```

2. CLASS DIAGRAMS



3. PROBLEM SOLUTION APPROACH

Q1

Firstly, I have thought about the design a little bit. After trying different strategies, I have decided this one: Firstly, to make things easier, I have sorted the array by quick sort. Then I have tried to solve the problem recursively. This is the best solution in tree structures as far as I am concerned. I began to fill the binary tree structure with the elements of array in the ascending order starting from bottom-left of the tree. After placing the elements to the binary tree with this approach, all I do is convert this binary tree to binary search tree by adding elements one by one properly.

Q2

Firstly, design process was a bit hard to consider because I couldn't access the node structure outside the class. After some instructions of the teacher, I have written the method inside the BinarySearchTree class. Then I traverse through the nodes. While traversal, if any unbalanced node is seen, I immediately applied the proper rotation. These rotations provides balanced binary search tree which is AVLTree.

4. TEST CASES

Q1

```
/******TEST FOR CONVERSION FROM BINARY TREE TO BINARY SEARCH TREE******/
System.out.println("*****TEST FOR CONVERSION FROM BINARY TREE TO BINARY SEARCH TREE*****");
System.out.println("TEST 1\n-----");
Integer[] array = {10, 2, 8, 4, 7};
System.out.printf("Array of elements: ");
for (int i = 0; i < array.length; ++i) System.out.printf("%d ", array[i]);
System.out.println("\n=====");

BinaryTree<Integer> node1 = new BinaryTree(0, null, null);
BinaryTree<Integer> node2 = new BinaryTree(0, null, null);
BinaryTree<Integer> node3 = new BinaryTree(0, node1, node2);
BinaryTree<Integer> node4 = new BinaryTree(0, null, null);
BinaryTree<Integer> root = new BinaryTree(0, node3, node4);
System.out.println("STRUCTURE OF THE BINARY TREE");
System.out.println("-----");
System.out.println(root);
System.out.println("=====");

System.out.println("BINARY SEARCH TREE");
System.out.println("-----");
BinarySearchTree<Integer> bst = convertToBST.convert(root, array);
System.out.println(bst);
```

```
System.out.println("\n\n\nTEST 2\n-----");
Integer[] array2 = {10, 9, 8, 7, 6, 5, 4, 3, 2, 1};
System.out.printf("Array of elements: ");
for (int i = 0; i < array2.length; ++i) System.out.printf("%d ", array2[i]);
System.out.println("\n=====");

node1 = new BinaryTree(0, null, null);
node2 = new BinaryTree(0, null, node1);
node3 = new BinaryTree(0, null, node2);
node4 = new BinaryTree(0, null, node3);
BinaryTree<Integer> node5 = new BinaryTree(0, null, node4);
BinaryTree<Integer> node6 = new BinaryTree(0, null, node5);
BinaryTree<Integer> node7 = new BinaryTree(0, null, node6);
BinaryTree<Integer> node8 = new BinaryTree(0, null, node7);
BinaryTree<Integer> node9 = new BinaryTree(0, null, node8);
root = new BinaryTree(0, null, node9);
System.out.println("STRUCTURE OF THE BINARY TREE");
System.out.println("-----");
System.out.println(root);
System.out.println("=====");

System.out.println("BINARY SEARCH TREE");
System.out.println("-----");
bst = convertToBST.convert(root, array2);
System.out.println(bst);
```

```
System.out.println("\n\n\nTEST 3\n-----");
Integer[] array3 = {42};
System.out.printf("Array of elements: ");
for (int i = 0; i < array3.length; ++i) System.out.printf("%d ", array3[i]);
System.out.println("\n=====");

root = new BinaryTree(0, null, null);
System.out.println("STRUCTURE OF THE BINARY TREE");
System.out.println("-----");
System.out.println(root);
System.out.println("=====");

System.out.println("BINARY SEARCH TREE");
System.out.println("-----");
bst = convertToBST.convert(root, array3);
System.out.println(bst);
```

Q2

```

/*****TEST FOR CONVERSION FROM BINARY SEARCH TREE TO AVL TREE*****/
System.out.println("\n\n\n*****TEST FOR CONVERSION FROM BINARY SEARCH TREE TO AVL TREE*****");
System.out.println("TEST 1\n-----");
BinarySearchTree<Integer> bst1 = new BinarySearchTree();
bst1.add(33); bst1.add(53); bst1.add(61);
bst1.add(13); bst1.add(21); bst1.add(11);
bst1.add(8); bst1.add(9);

System.out.println("BINARY SEARCH TREE\n-----\n" + bst1);
System.out.println("=====");

bst1.convertAVL();
System.out.println("AVL TREE\n-----\n" + bst1);
System.out.println("=====");

System.out.println("\n\n\nTEST 2\n-----");
BinarySearchTree<Integer> bst2 = new BinarySearchTree();
bst2.add(4); bst2.add(3); bst2.add(2);
bst2.add(1); bst2.add(5); bst2.add(6);
bst2.add(7);

System.out.println("BINARY SEARCH TREE\n-----\n" + bst2);
System.out.println("=====");

bst2.convertAVL();
System.out.println("AVL TREE\n-----\n" + bst2);
System.out.println("=====");

System.out.println("\n\n\nTEST 3\n-----");
BinarySearchTree<Integer> bst3 = new BinarySearchTree();
bst3.add(1); bst3.add(2); bst3.add(3);
bst3.add(4); bst3.add(5); bst3.add(6);

System.out.println("BINARY SEARCH TREE\n-----\n" + bst3);
System.out.println("=====");

bst3.convertAVL();
System.out.println("AVL TREE\n-----\n" + bst3);
System.out.println("=====");

```


5. RUNNING AND RESULTS

```
*****TEST FOR CONVERSION FROM BINARY TREE TO BINARY SEARCH TREE*****
```

```
TEST 1
```

```
-----
```

```
Array of elements: 10 2 8 4 7
```

```
=====
```

```
STRUCTURE OF THE BINARY TREE
```

```
-----
```

```
0
```

```
0
  0
    null
    null
  0
    null
    null
0
  null
  null
```

```
=====
```

```
BINARY SEARCH TREE
```

```
-----
```

```
8
```

```
4
  2
    null
    null
  7
    null
    null
10
  null
  null
```

```
TEST 2
```

```
-----
```

```
Array of elements: 10 9 8 7 6 5 4 3 2 1
```

```
=====
```

```
STRUCTURE OF THE BINARY TREE
```

```
-----
```

```
0
```

```
null
0
  null
  0
    null
    0
      null
      0
        null
        0
          null
          0
            null
            0
              null
              0
                null
                0
                  null
                  null
                  null
```

```
=====
BINARY SEARCH TREE
-----
1
  null
2
  null
3
  null
4
  null
5
  null
6
  null
7
  null
8
  null
9
  null
10
  null
  null
```

```
TEST 3
-----
Array of elements: 42
=====
STRUCTURE OF THE BINARY TREE
-----
0
  null
  null
```

```
=====
BINARY SEARCH TREE
-----
42
  null
  null
```

*****TEST FOR CONVERSION FROM BINARY SEARCH TREE TO AVL TREE*****

TEST 1

BINARY SEARCH TREE

33

```
  13
   11
    8
     null
     9
      null
      null
   null
  21
   null
   null
53
 null
61
 null
 null
```

=====

AVL TREE

11

```
  8
   null
   9
    null
    null
33
 13
   null
   21
    null
    null
53
 null
61
 null
 null
```

=====

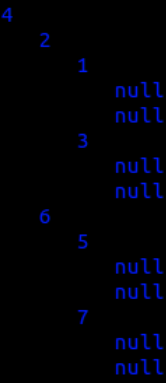
TEST 2

BINARY SEARCH TREE



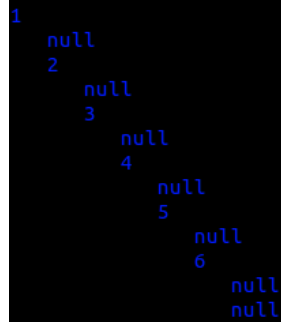
=====

AVL TREE



TEST 3

BINARY SEARCH TREE



=====

AVL TREE

