

1. Compute the weakest preconditions for the following statements. All variables are of integer type.

a. `if i=j then i=i-j else i=j; {i=0}`

b. `x=x+1; y=y*z; {y=z*x}`

c. `a=3*(2*b+a) ; b = 2*a-1; {b>5}`

2. Prove that the following grammar is ambiguous.  $\langle S \rangle$  is the starting symbol.

$\langle S \rangle \rightarrow \langle A \rangle \langle B \rangle \mid aa \langle B \rangle$

$\langle A \rangle \rightarrow a \mid \langle A \rangle a$

$\langle B \rangle \rightarrow b$

3. Consider the following grammar:

$Y \rightarrow pYrQ \mid P \mid q$

$P \rightarrow rP \mid r$

$Q \rightarrow s \mid P$

Which of the following strings are generated by the above context free grammar?

a. p q r s

b. p r s

c. p r r r q r r r

4. Write an attribute grammar whose BNF and language (static semantics) rules are as follows:

BNF:

$\langle \text{assign} \rangle \rightarrow \langle \text{var} \rangle = \langle \text{expr} \rangle$

$\langle \text{expr} \rangle \rightarrow \langle \text{var} \rangle + \langle \text{var} \rangle \mid \langle \text{var} \rangle$

$\langle \text{var} \rangle \rightarrow A \mid B \mid C$

Static semantics rules: Data types cannot be mixed in expressions, but assignment statements need not have the same types on both sides of the assignment operator.