

# When the Stream meets the Bump...

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**NHOM-Brest: Workshop on Non-Hydrostatic Ocean Modeling**

*Bridging the gap between sub-mesoscales and boundary layer turbulence*

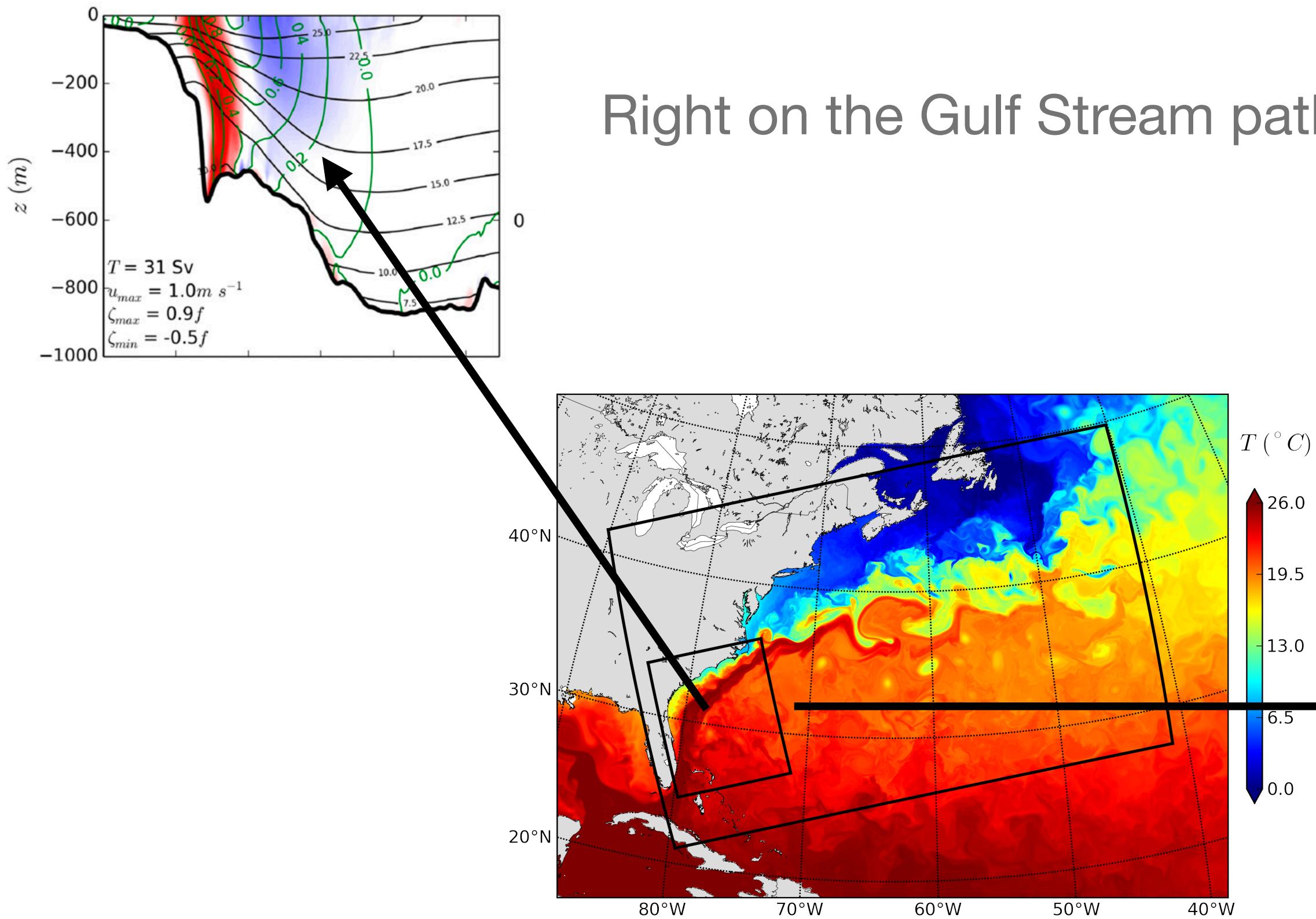
15-17 Oct 2018, Brest (France)

Jonathan Gula, Charly De Marez, Noé Lahaye (LOPS)  
Tanya Blacic (MSU) & Robert Todd (WHOI)

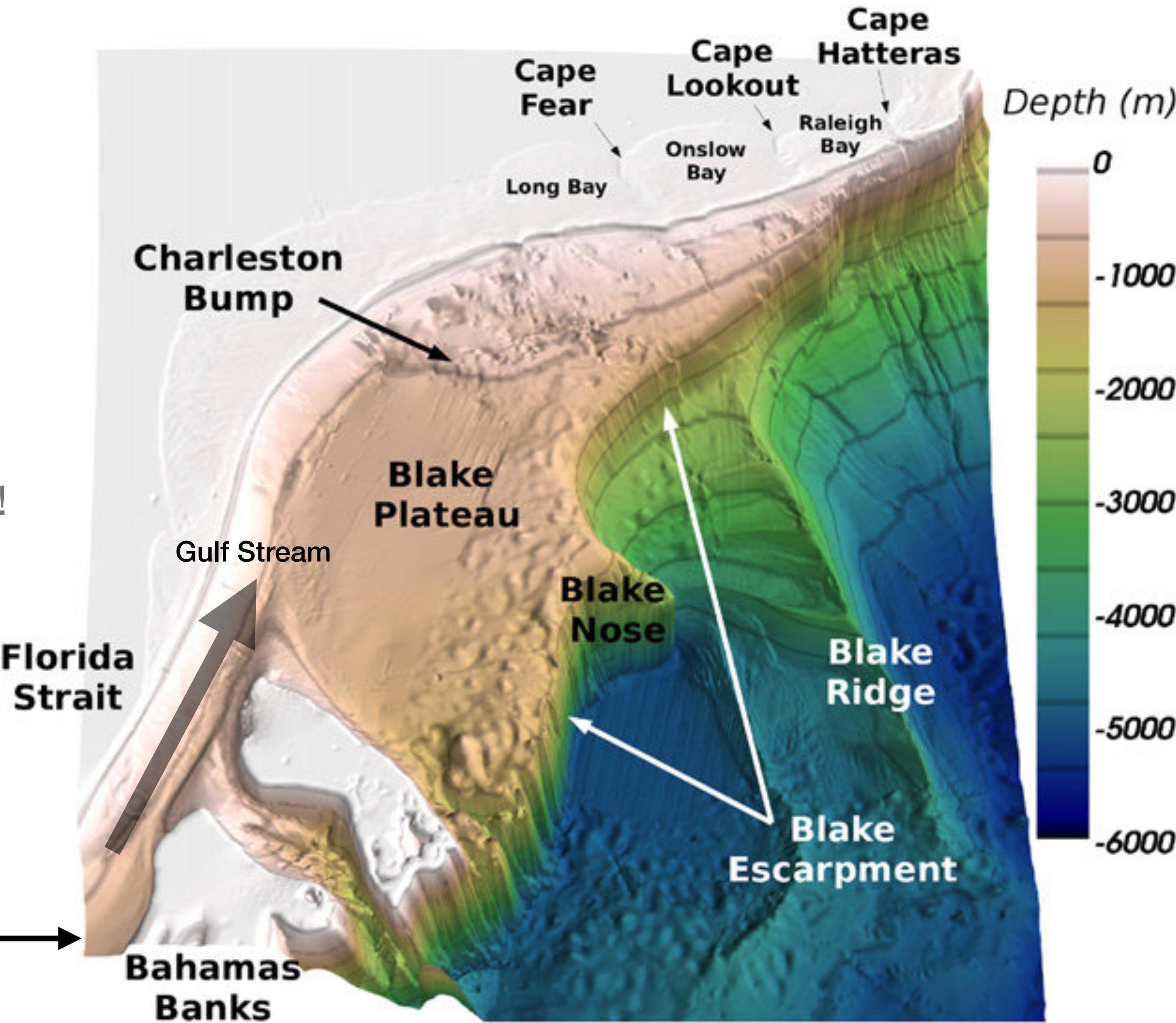


# What is the Charleston Bump?

- The Charleston Bump is a prominent topographic feature along the U.S. eastern seaboard (100 km x 200 km)

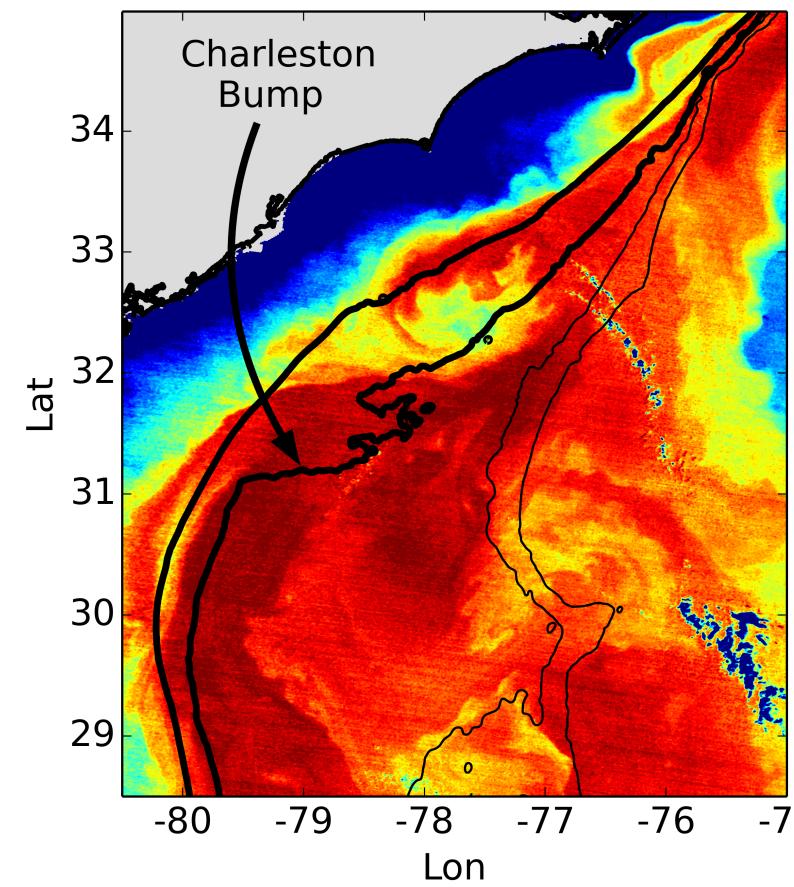


Right on the Gulf Stream path!

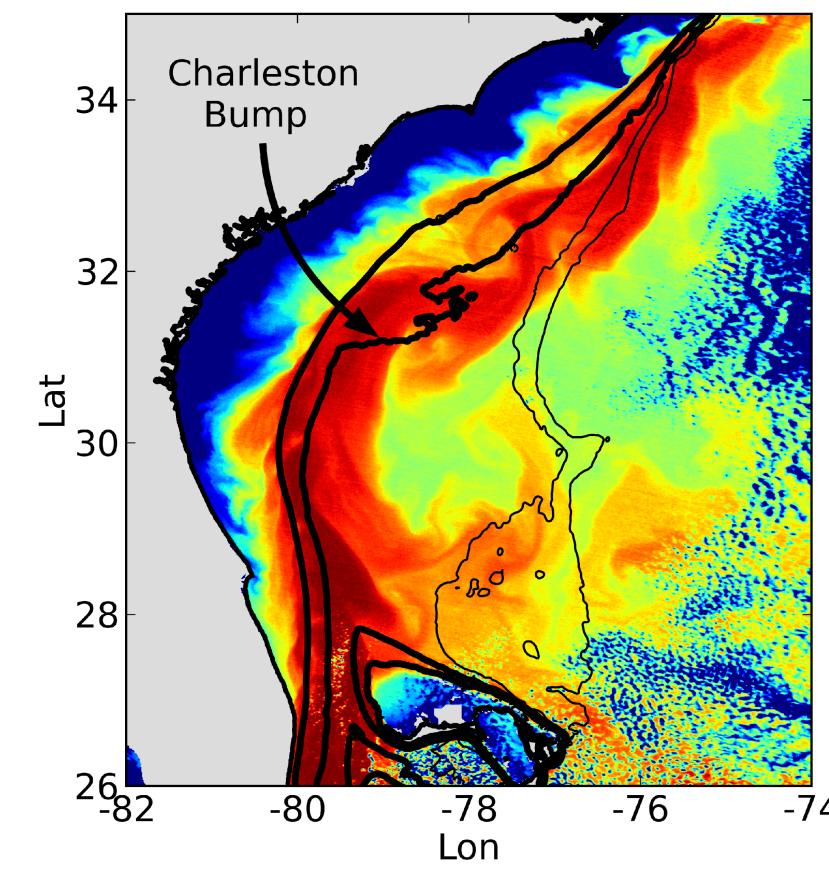


# Generation of frontal eddies

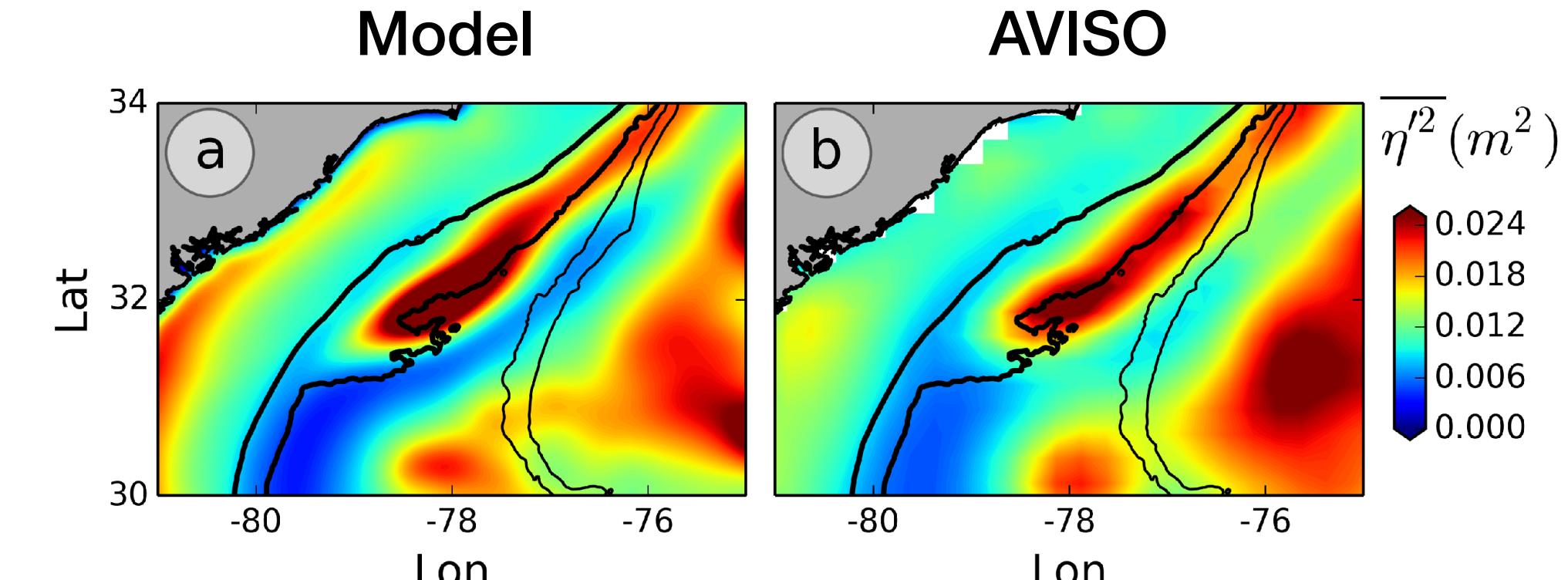
- Mesoscale frontal eddies are commonly observed in the lee of the Bump
- It is a region of strong amplification for meanders and frontal eddies through mixed barotropic/baroclinic energy conversion.



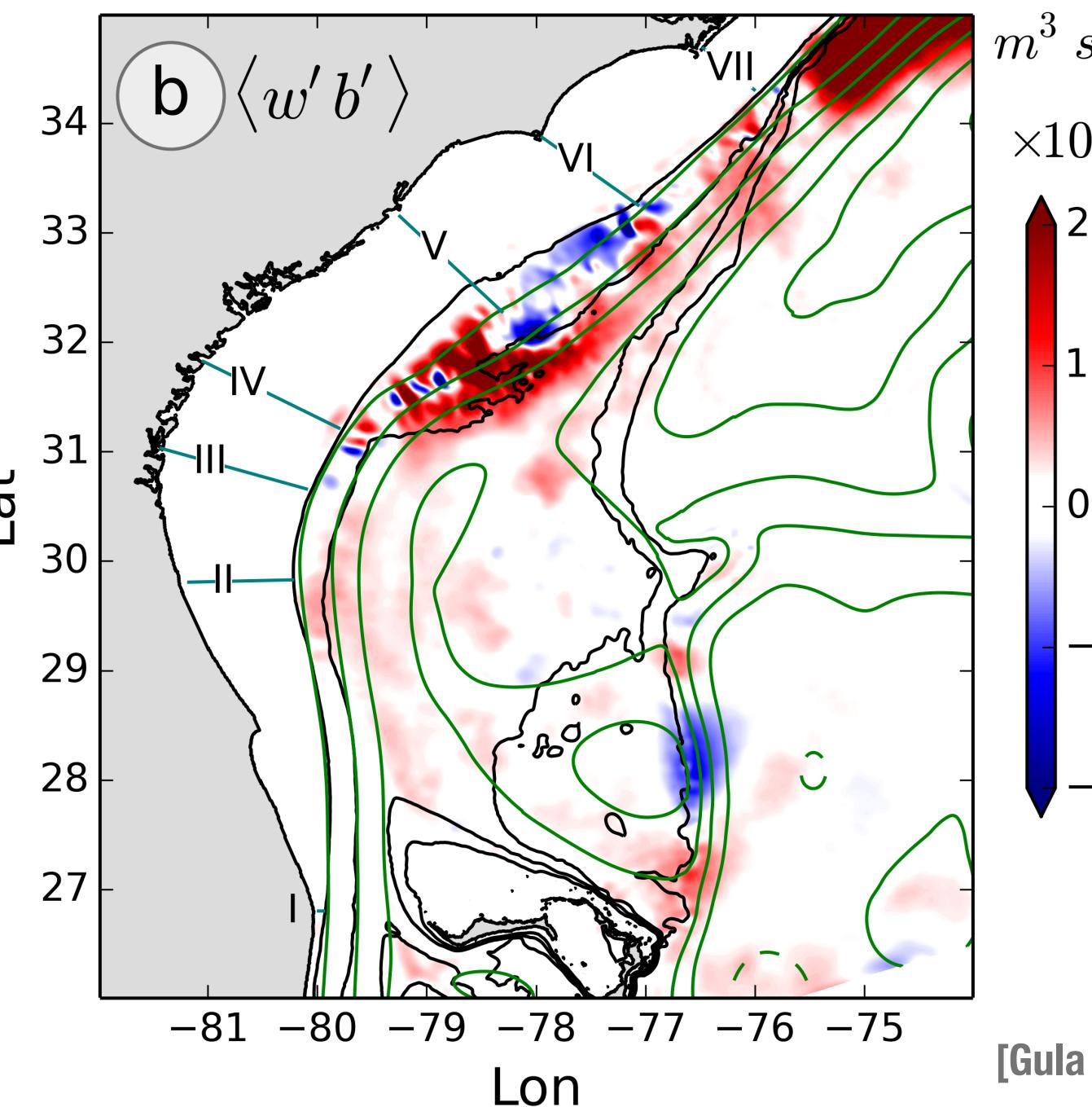
Observed Sea Surface Temperature (SST) of the Gulf Stream. Data from MODIS-AQUA.



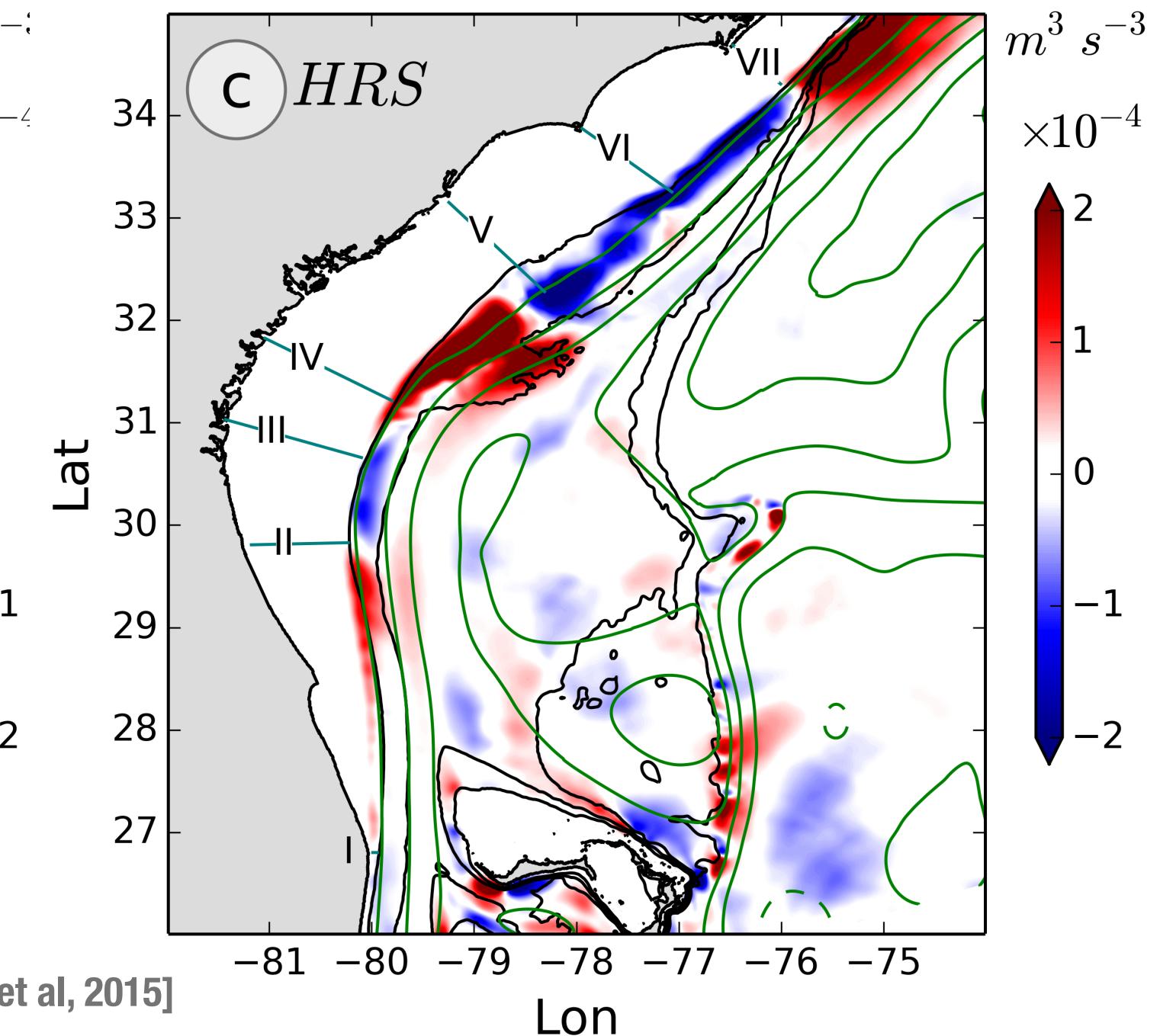
Conversion from eddy potential to eddy kinetic energy (Baroclinic instability)



SSH variability from model and AVISO



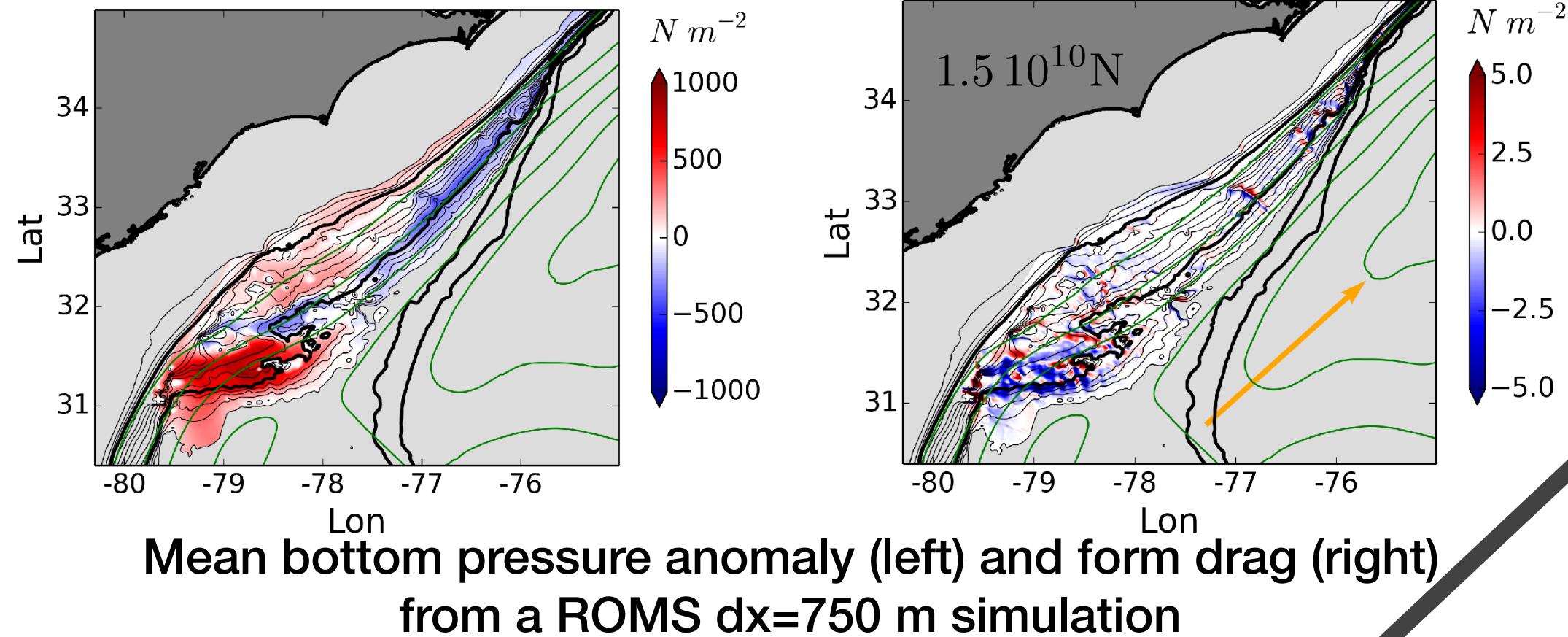
[Gula et al, 2015]



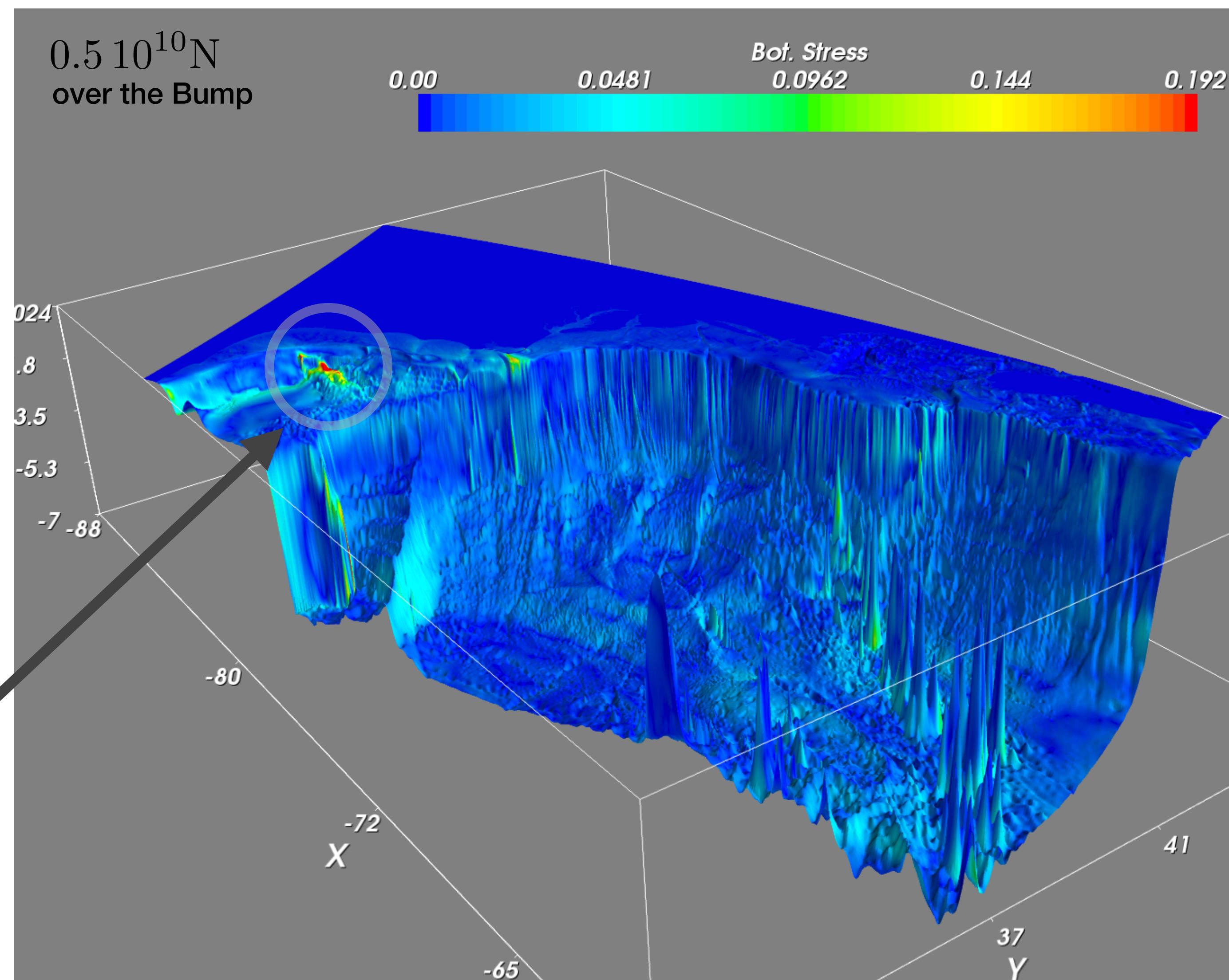
Conversion from mean kinetic to eddy kinetic energy (Barotropic instability)

# Flow topography interactions

- Significant local pressure anomalies and topographic form drag exerted by the Bump that retard the mean flow and steer the mean current pathway seaward.

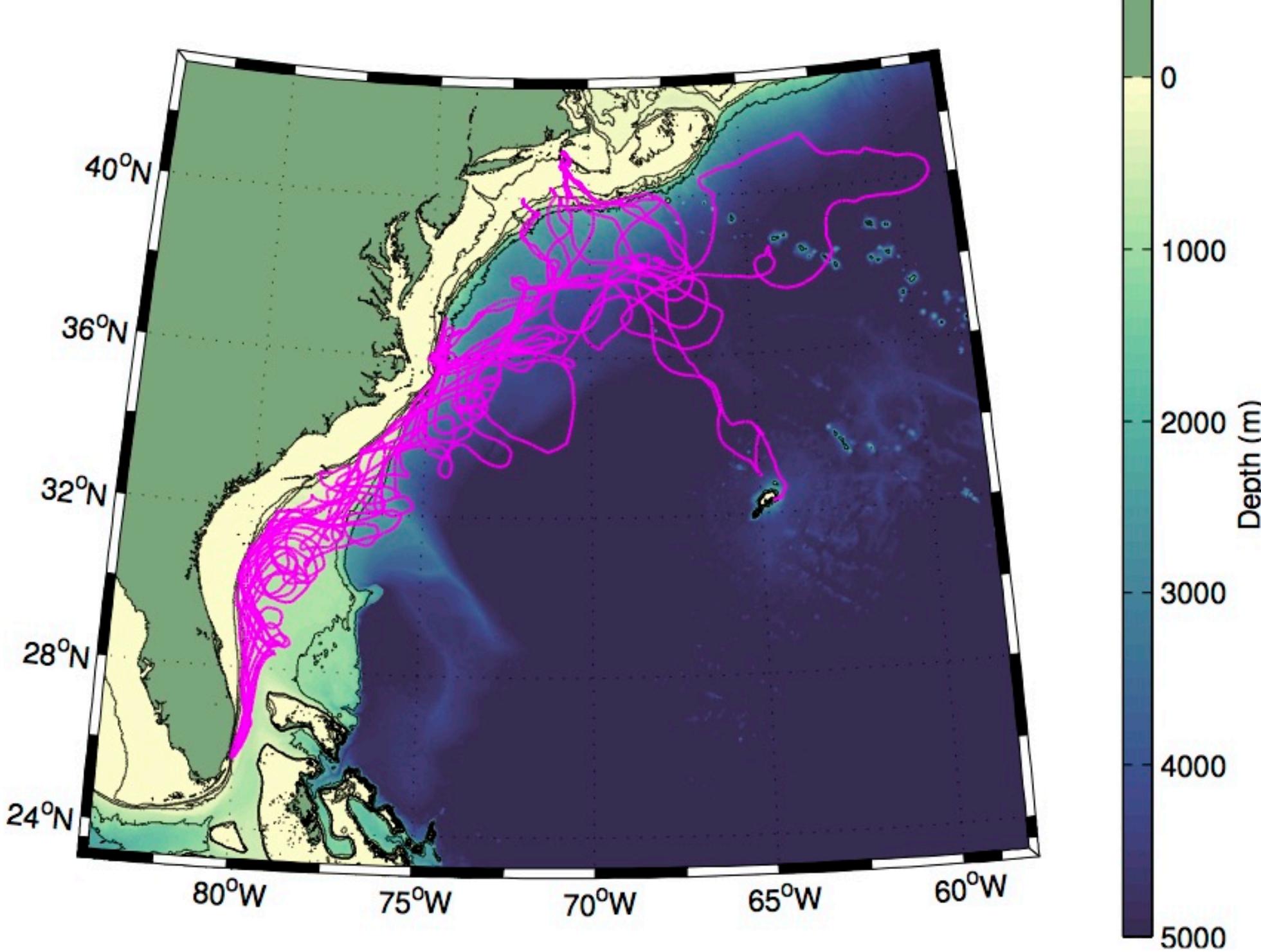
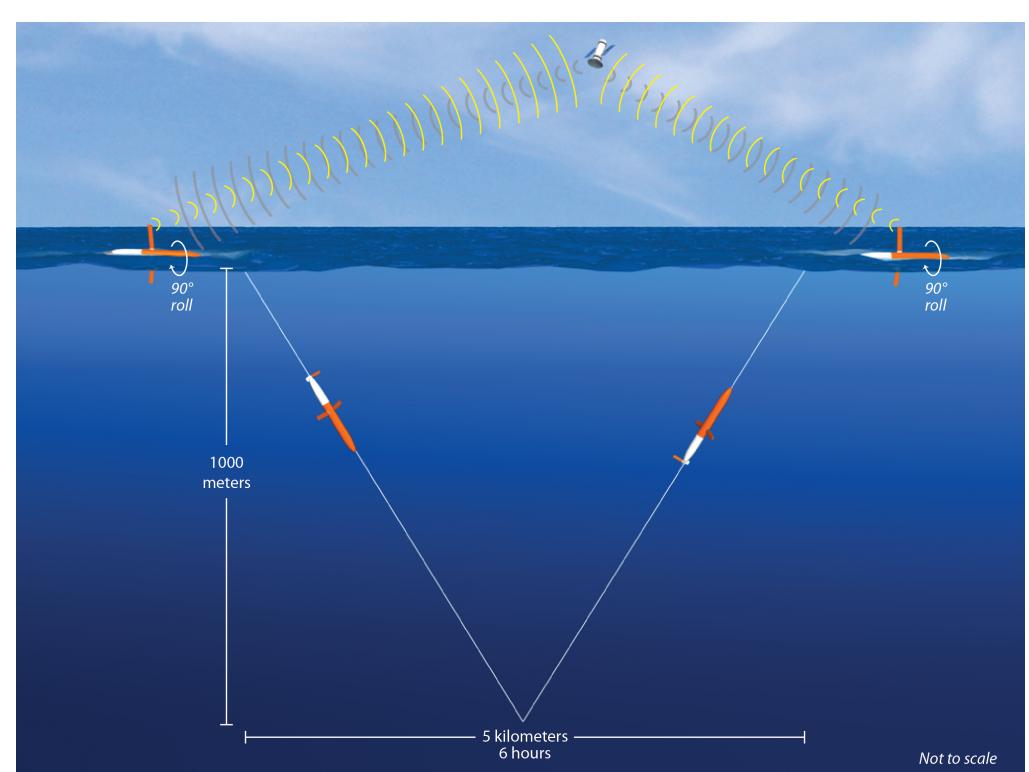
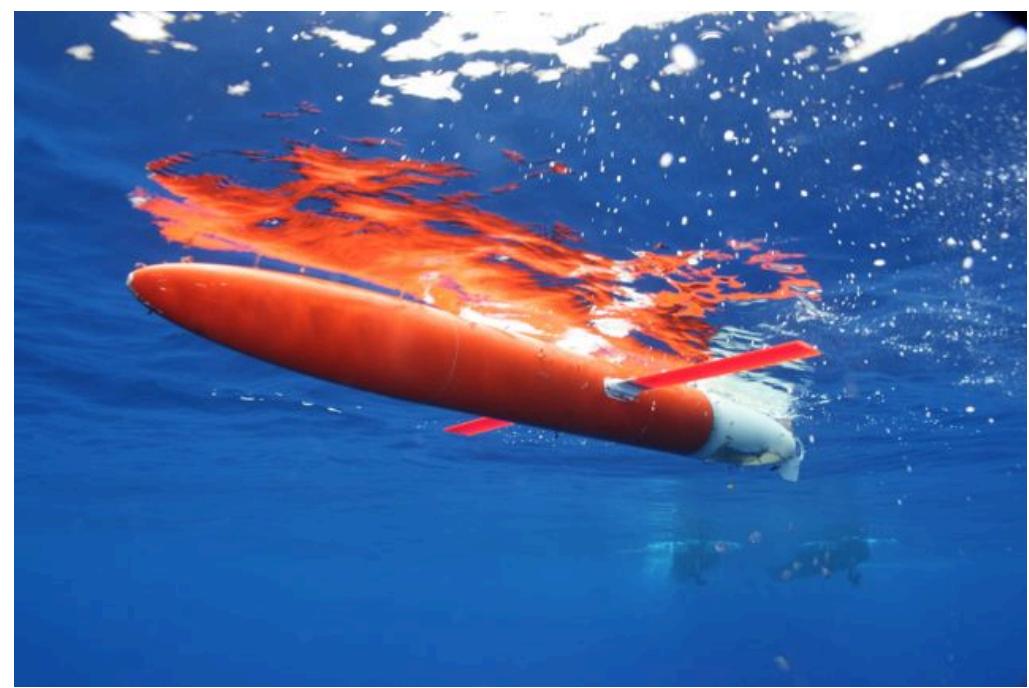


- Hot spot for the viscous drag



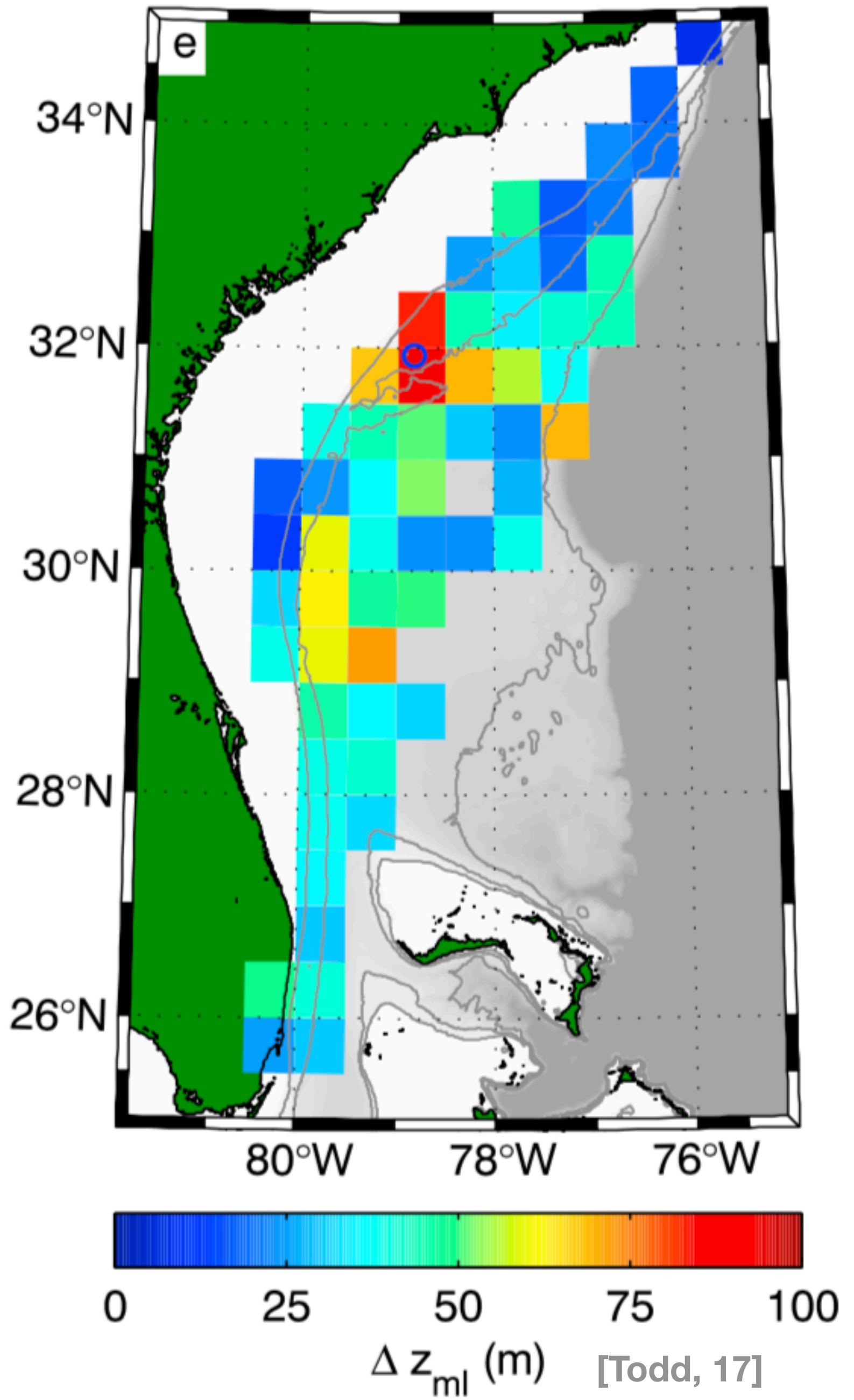
# Bottom boundary layer

- Thick  $O(100\text{ m})$  bottom mixed layers are generated in the lee of topography, likely due to enhanced turbulence generated by  $O(1\text{ m s}^{-1})$  near-bottom flows.



Glider Data [Todd & Owens, 16]

publicly available: <https://spraydata.ucsd.edu/projects/GS>

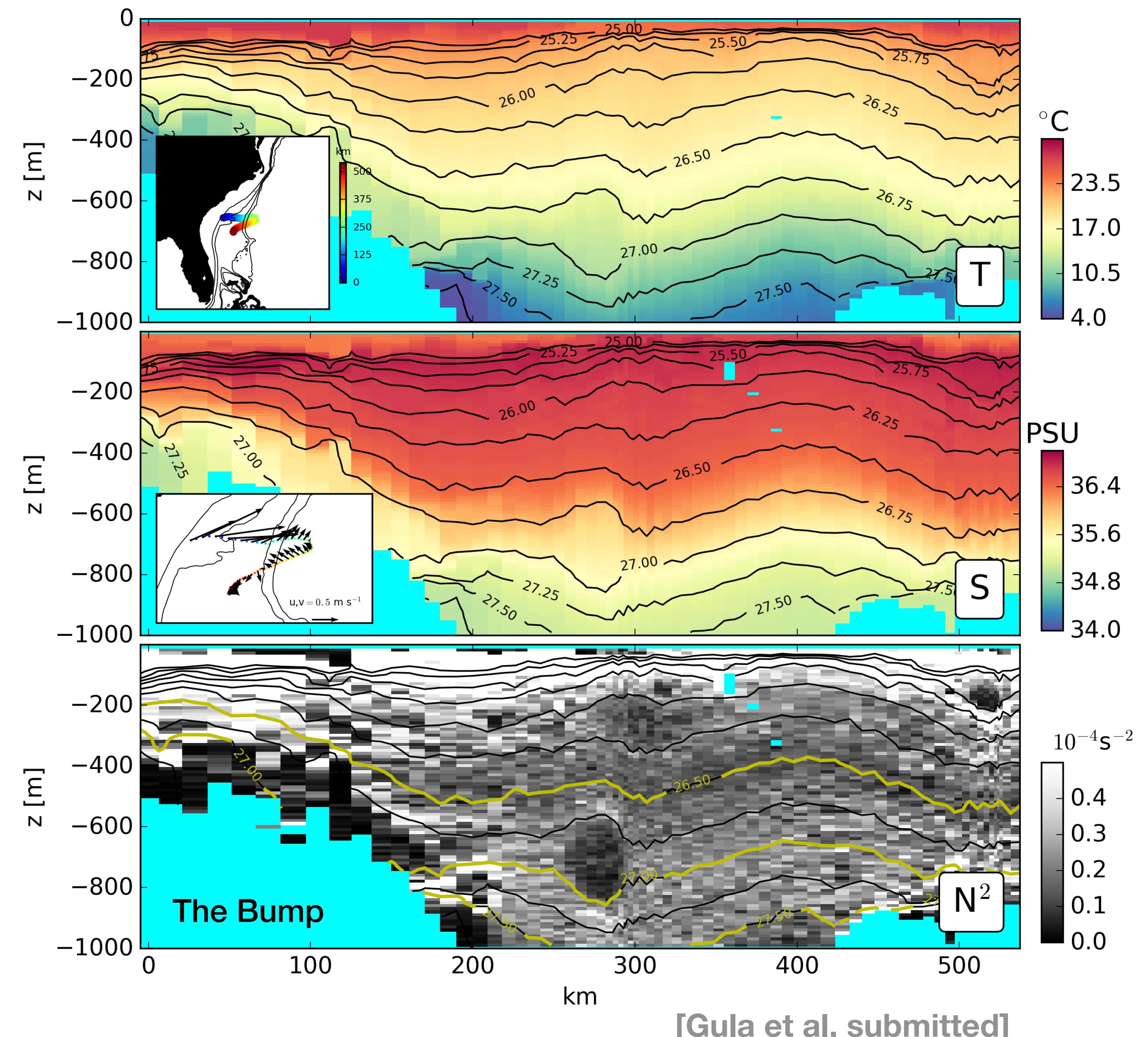


# Generation of submesoscale coherent vortices (SCVs)

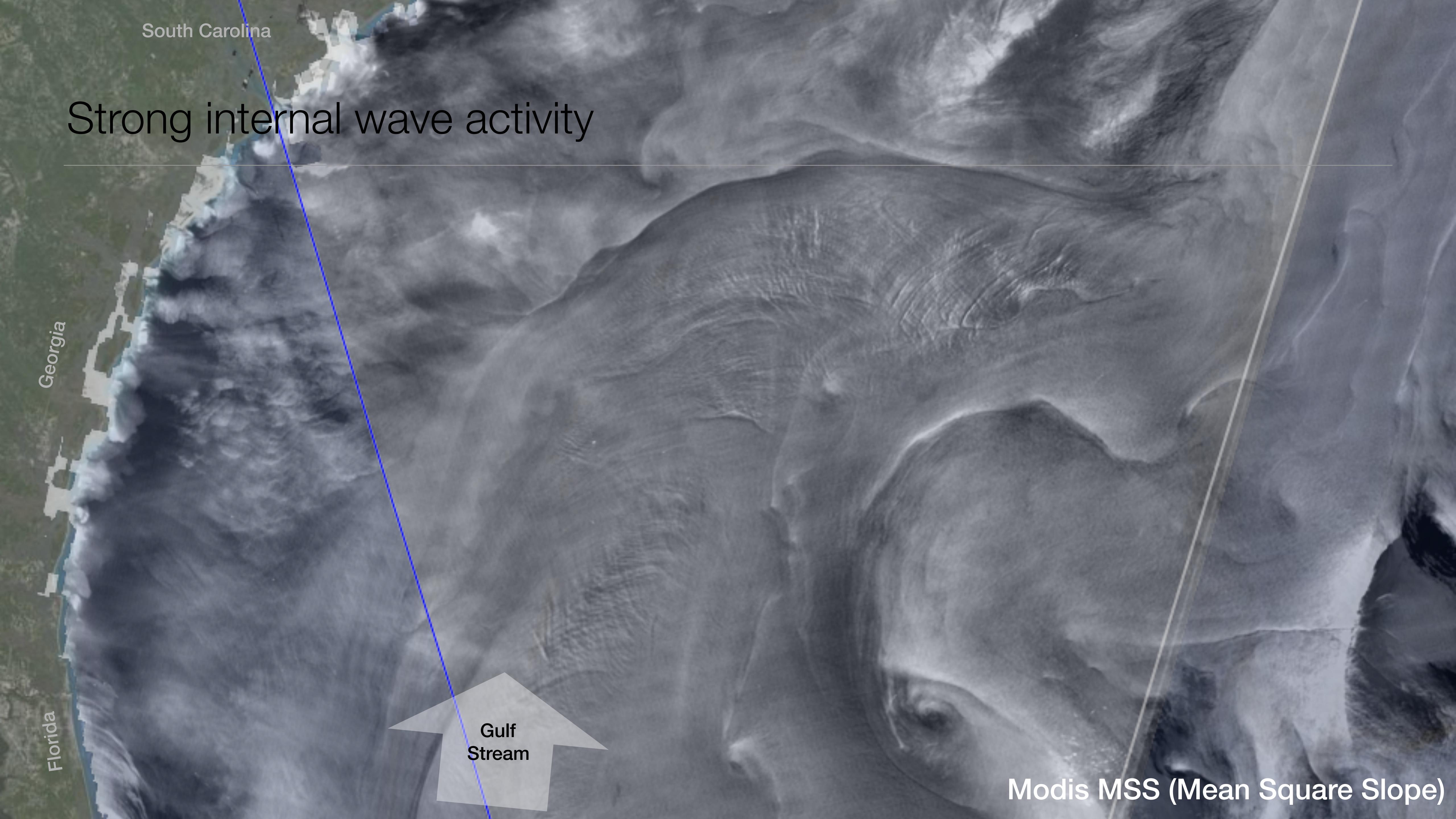
Glider data

- Submesoscale lenses of well-mixed water are observed in glider sections of the Gulf Stream in the lee of the Bump

Part 1 of this talk



[Gula et al, submitted]

A satellite image of the southeastern coast of North America, specifically the Carolinas, Georgia, and Florida. The image shows a complex pattern of ocean surface textures and currents. A prominent feature is the Gulf Stream, which is visible as a bright, textured band flowing from the south towards the north. The surrounding waters exhibit various shades of gray and white, indicating different levels of internal wave activity and current intensity. The coastline is clearly visible along the left edge.

South Carolina

Strong internal wave activity

Georgia

Florida

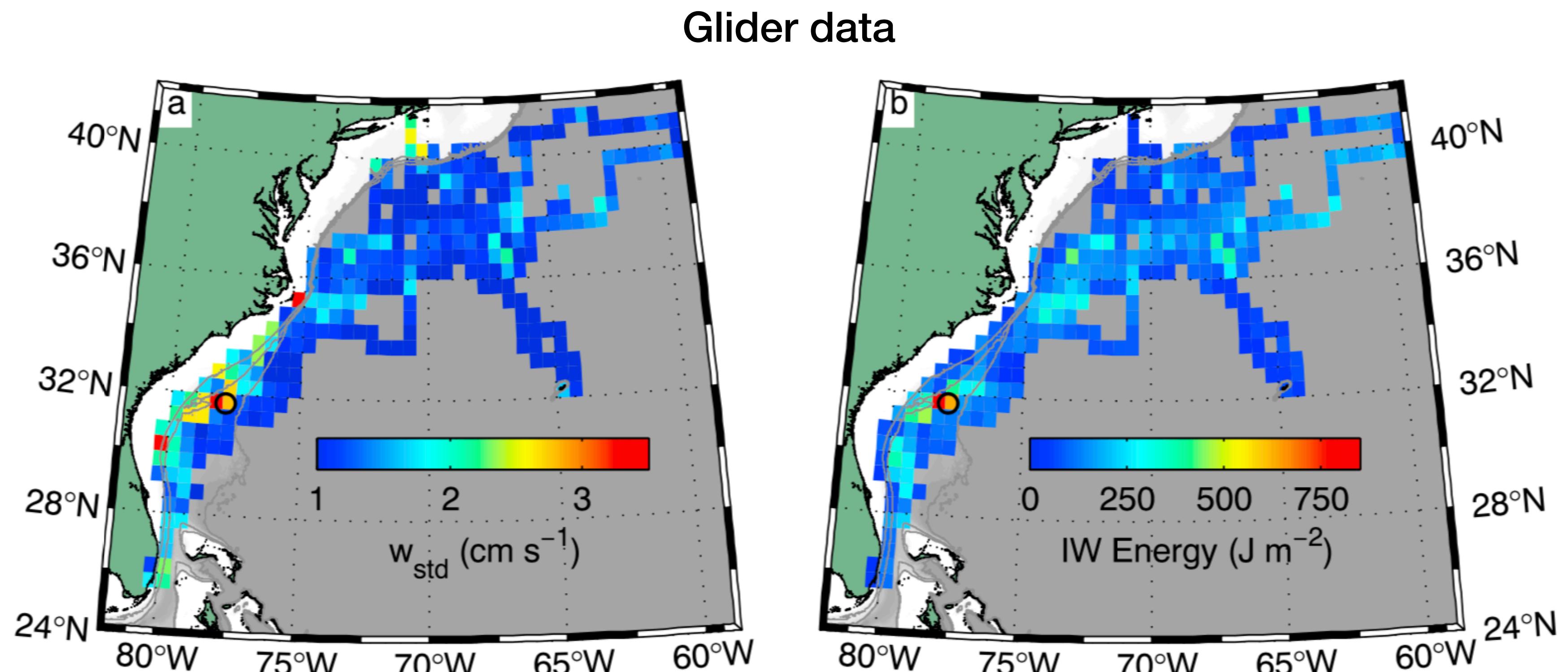
Gulf  
Stream

Modis MSS (Mean Square Slope)

# Strong internal wave activity

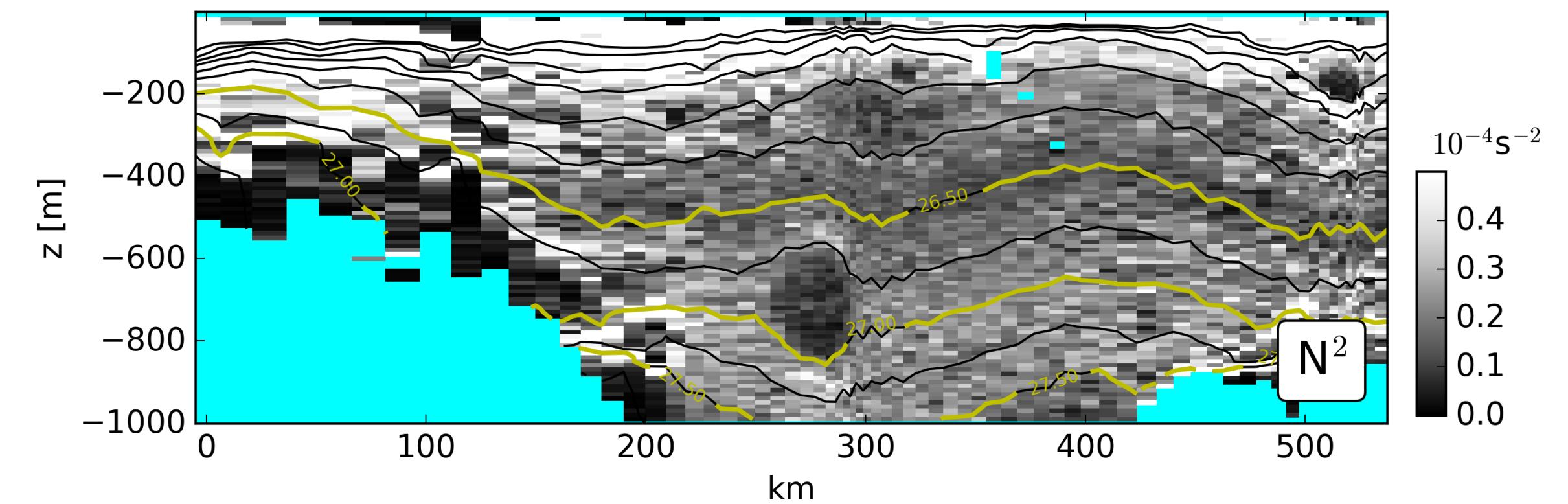
- Internal waves with vertical velocities exceeding  $0.1 \text{ m s}^{-1}$  are found over the Charleston Bump.

Part 2 of this talk

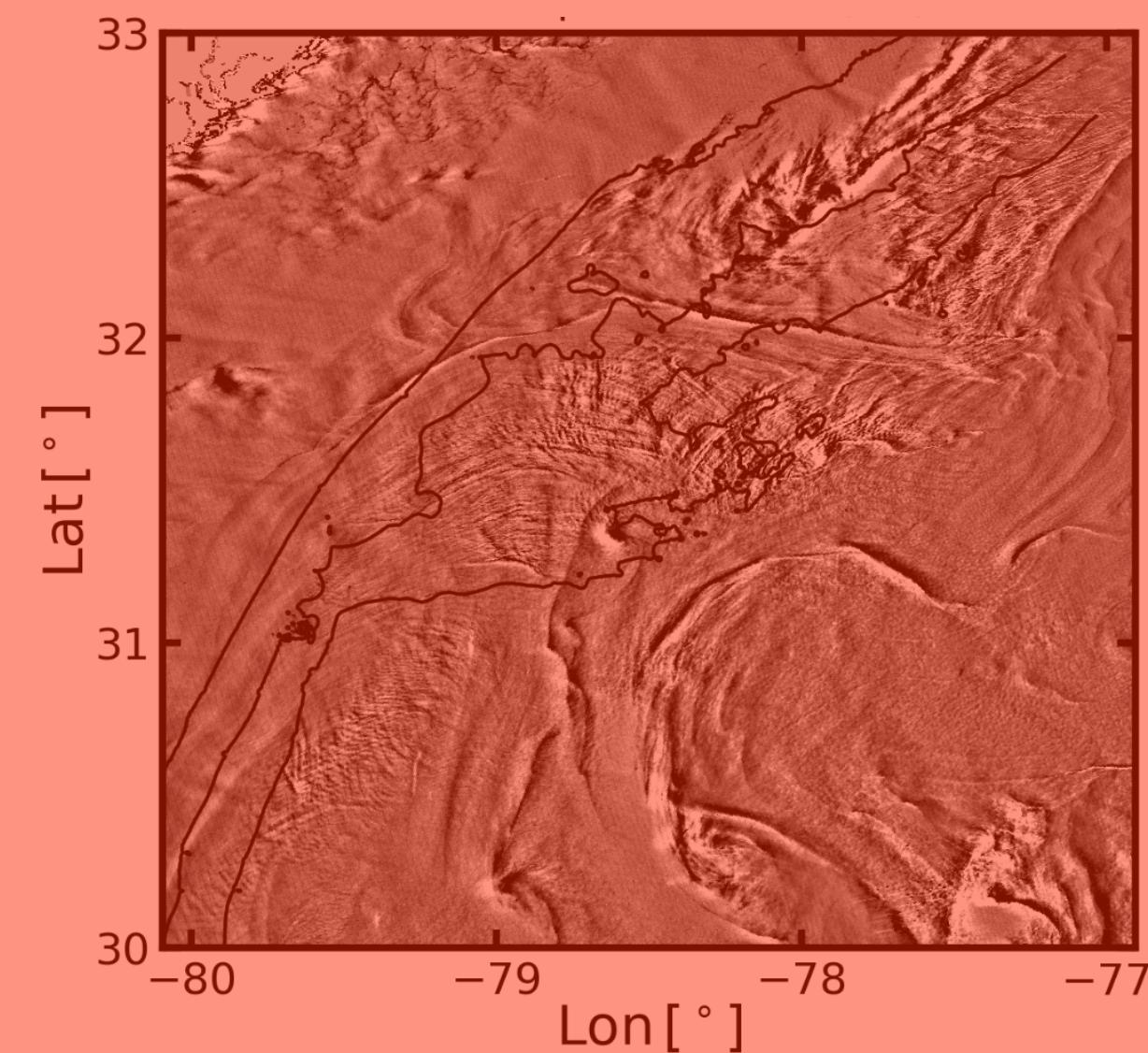


# OUTLINE

1. Generation of Submesoscale coherent vortices in the lee of the Bump

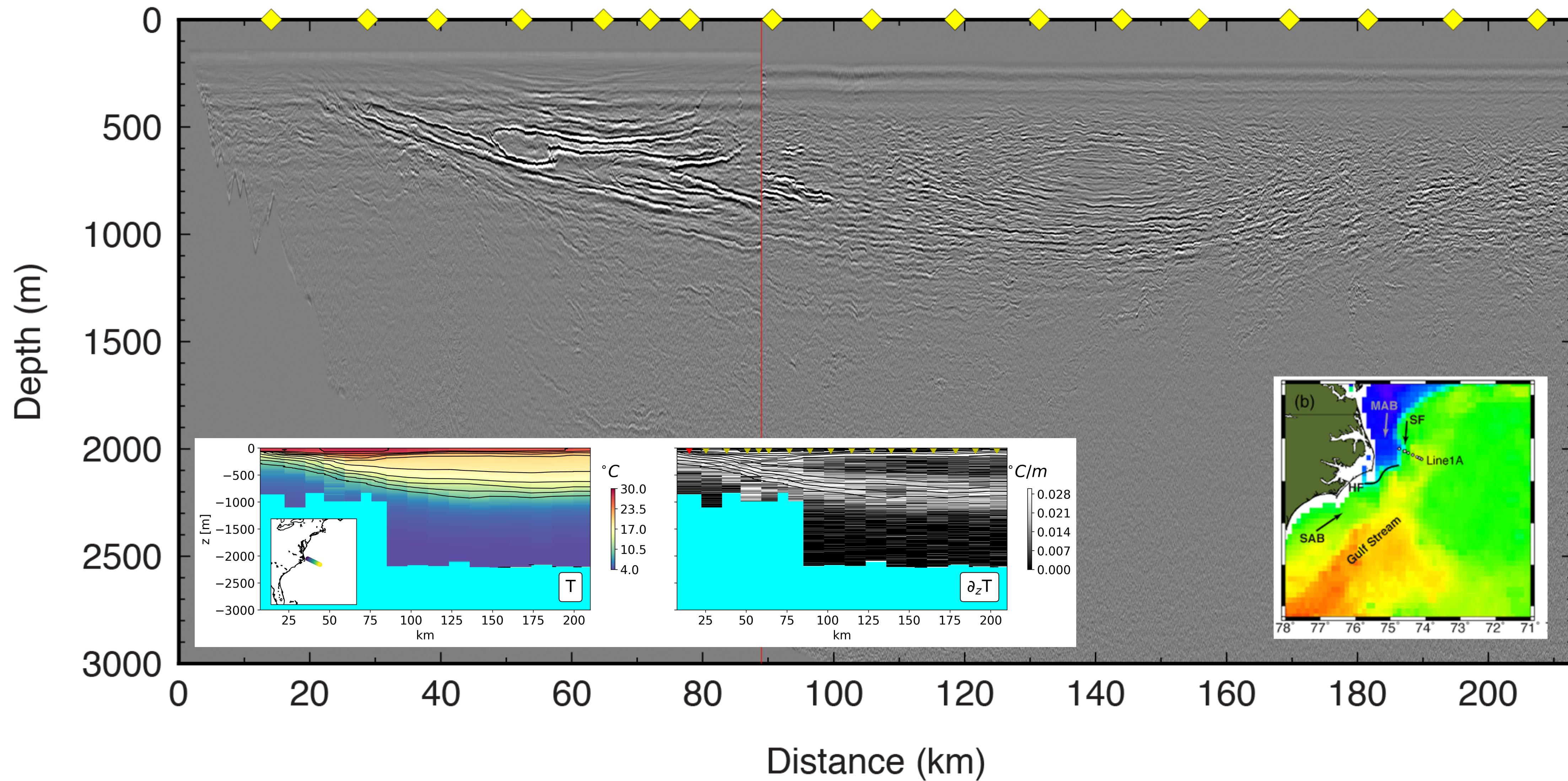


2. Generation of Lee waves over the Charleston Bump



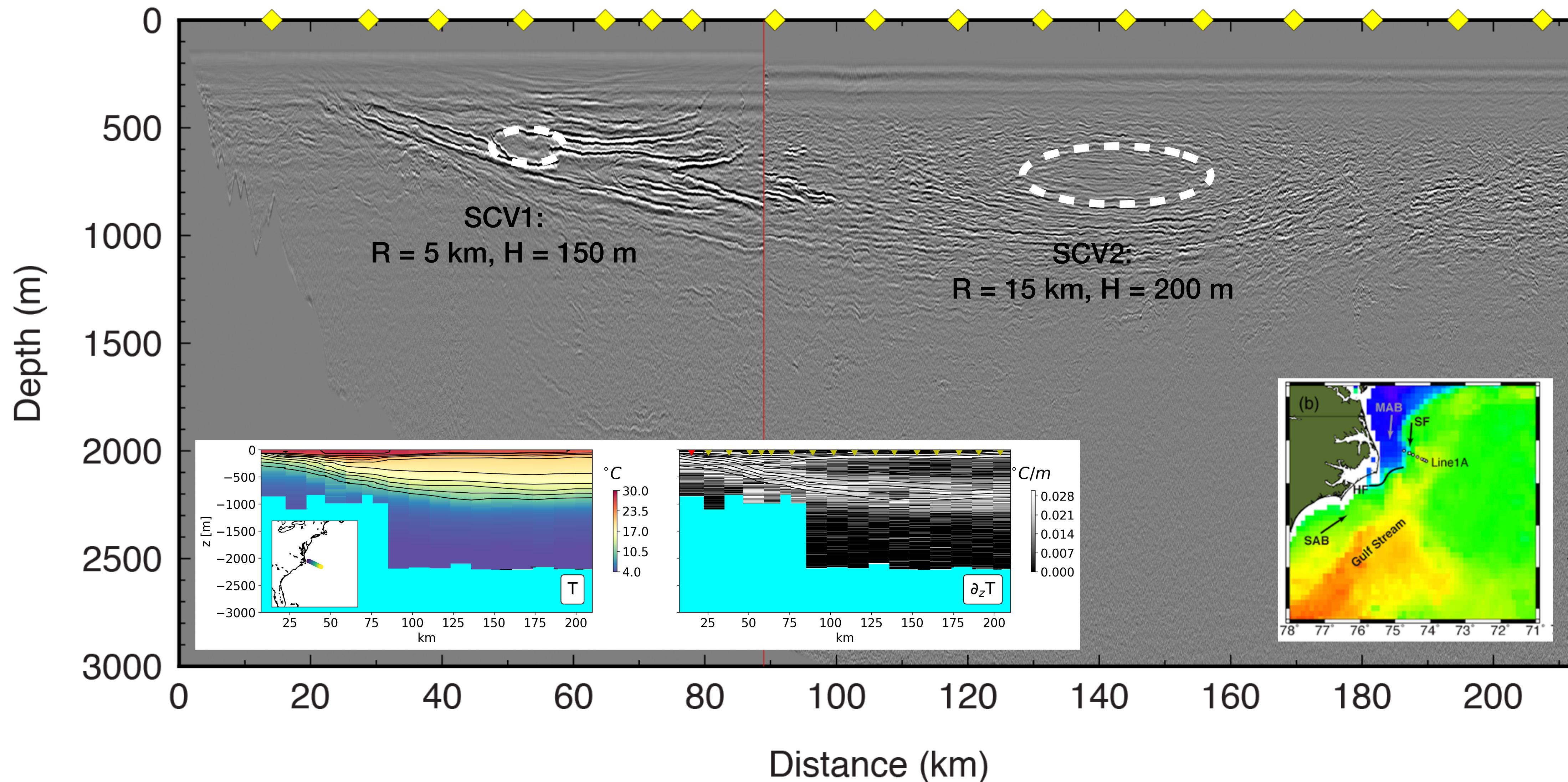
# Observations of SCVs in the Gulf Stream

Seismic Data from the Eastern  
North America Margin  
Community Seismic Experiment  
in Sep. 2014



# Observations of SCVs in the Gulf Stream

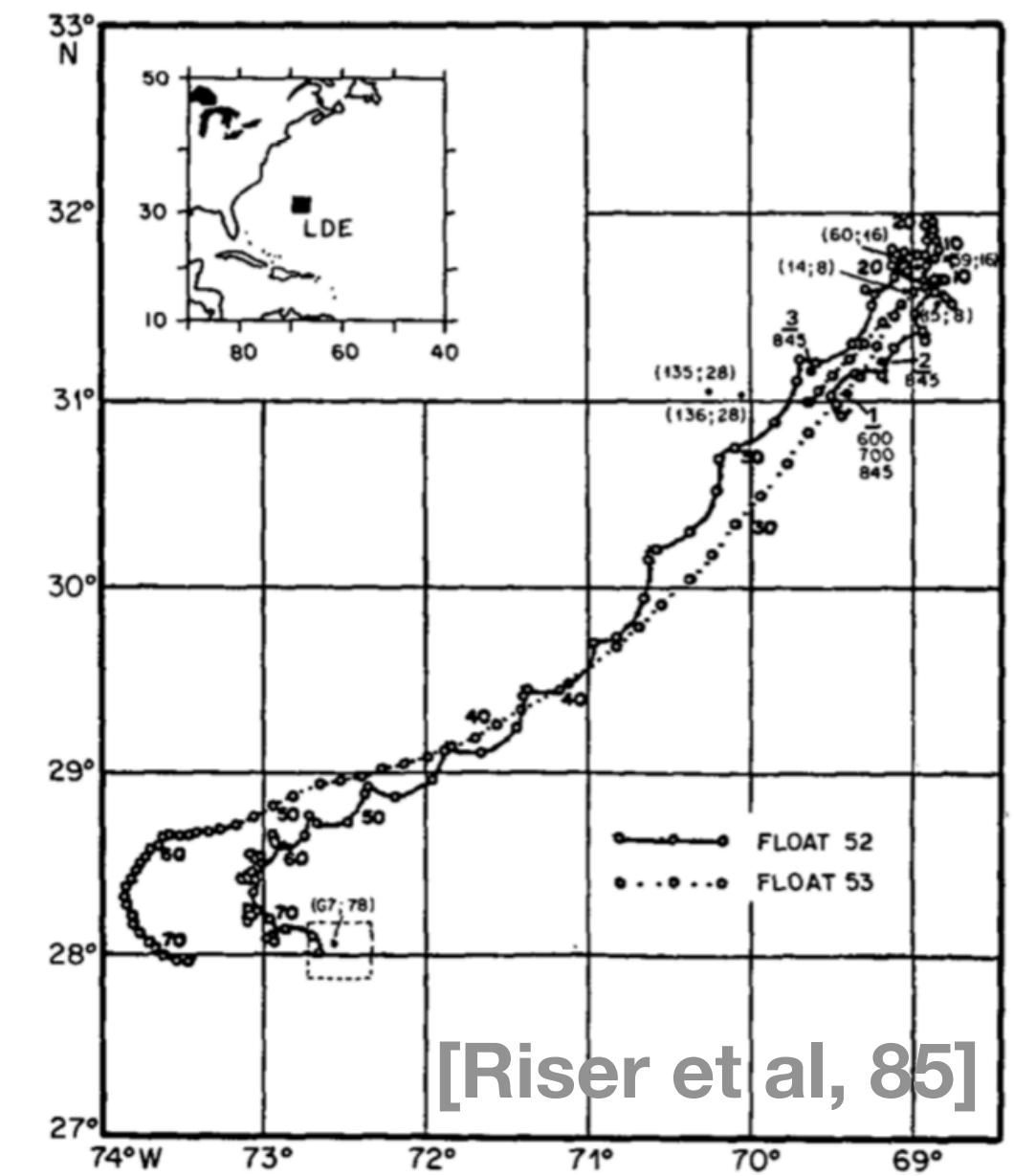
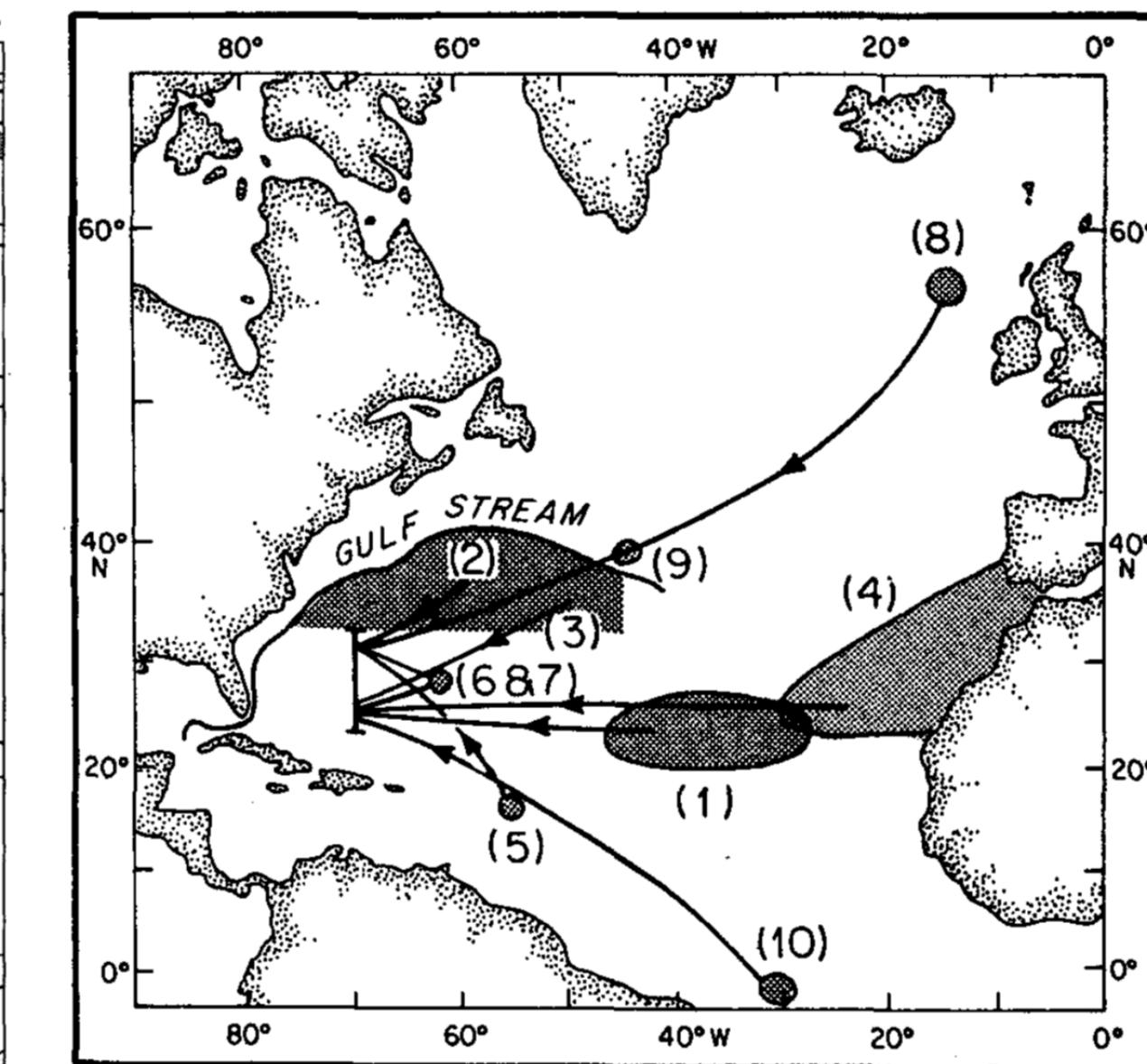
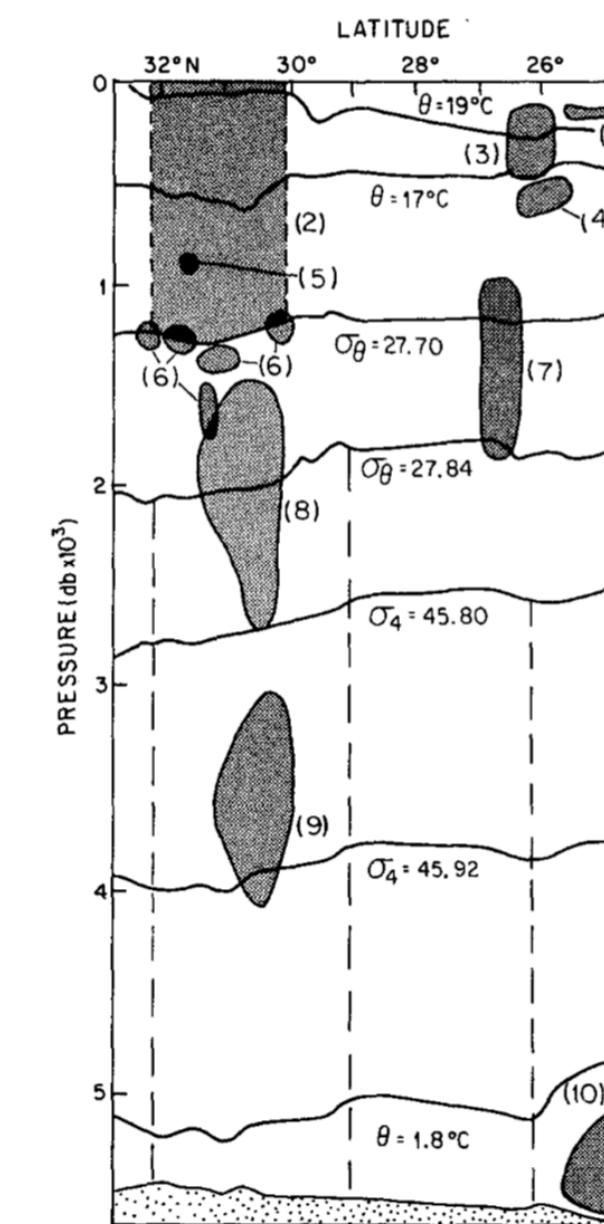
# Seismic Data from the Eastern North America Margin Community Seismic Experiment in Sep. 2014



# Observations of SCVs in the Subtropical gyre

Historical observations

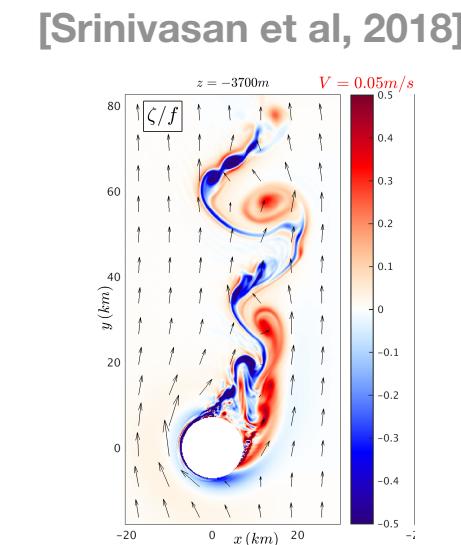
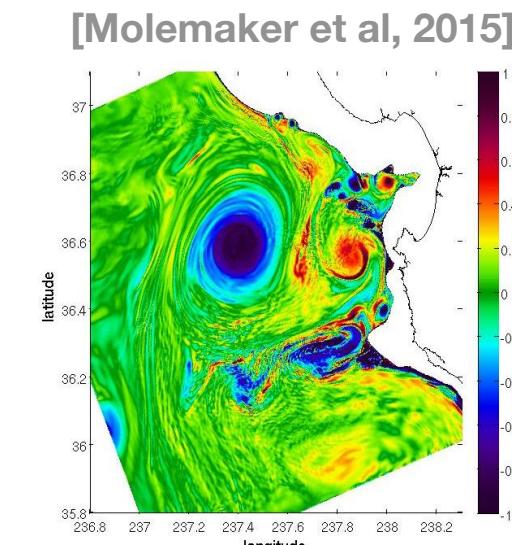
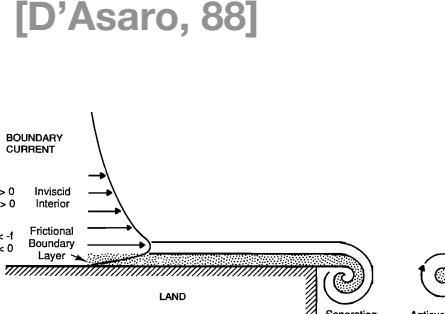
- A number of moorings and hydrographic sections in the Sargasso Sea highlighted presence of SCVs [Dugan et al, 82, McWilliams, 85, Lindstrom & Taft, 85, McDowell, 86, Bane et al, 89, Kostianoy & Belkin, 89, etc.]. About 1 SCV per 100 km.<sup>2</sup>
- Several SCVs with very similar properties than the one observed in seismic data [e.g. Riser et al, 86].
- Origins of SCVs can be tracked using water-mass properties and oxygen [e.g. Ebbesmeyer et al, 86]



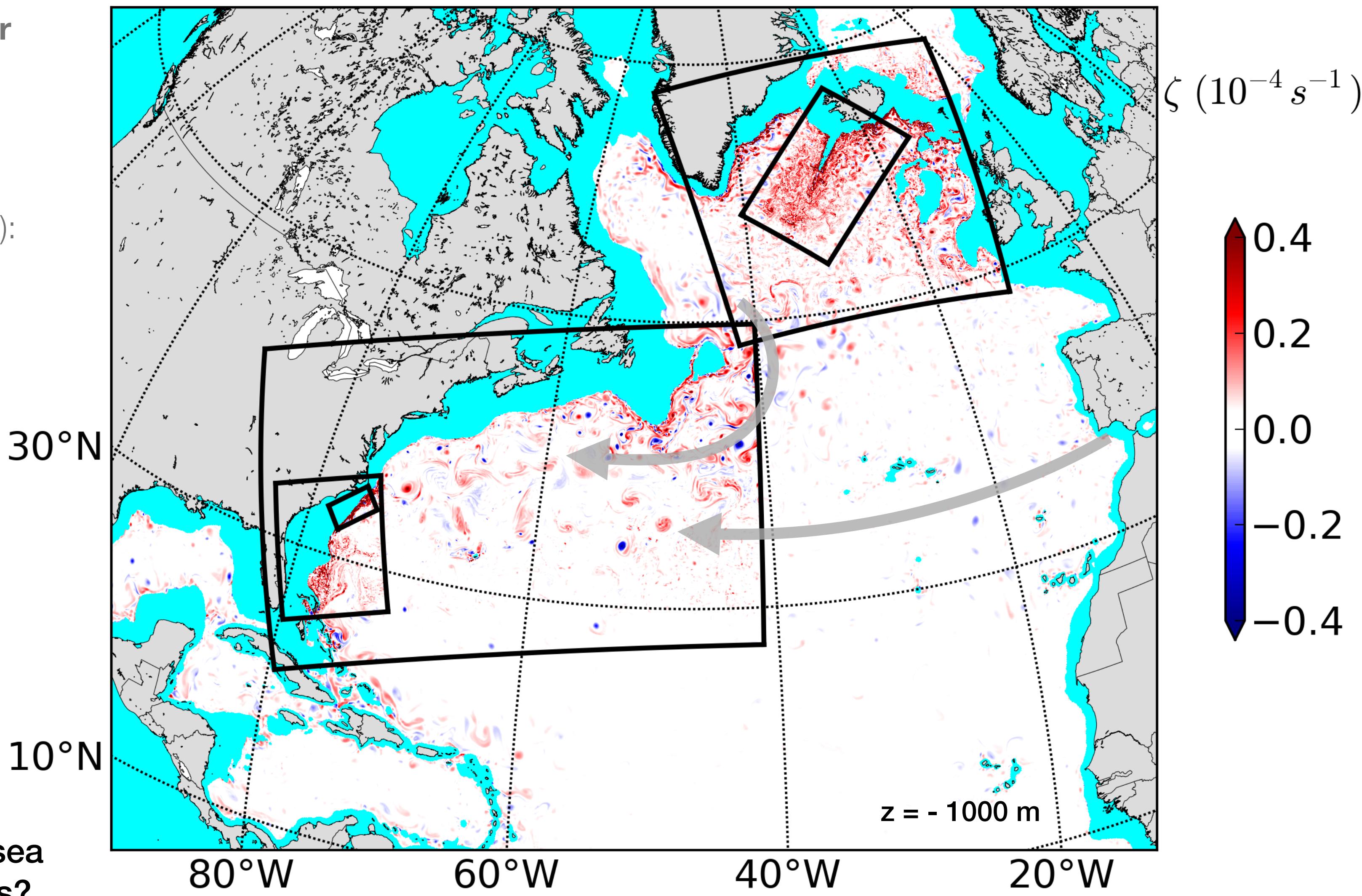
[Riser et al, 85]

# Generation mechanisms of SCVs in the Subtropical gyre

- Surface diabatic effects (deep convection): **Labrador Sea, Greenland Sea, Mediterranean Sea**
- Frictional effects (wind over fronts): Everywhere
- Diabatic effects at the bottom (hydrothermal forcings): **Juan de Fuca Ridge**
- Boundary Current instabilities/Frictional effects along topography: **Mediterranean outflow, Red Sea, Persian Gulf, Beaufort Gyre, California Undercurrent, Peru-Chile Undercurrent, West African upwelling, DWBC, etc.**

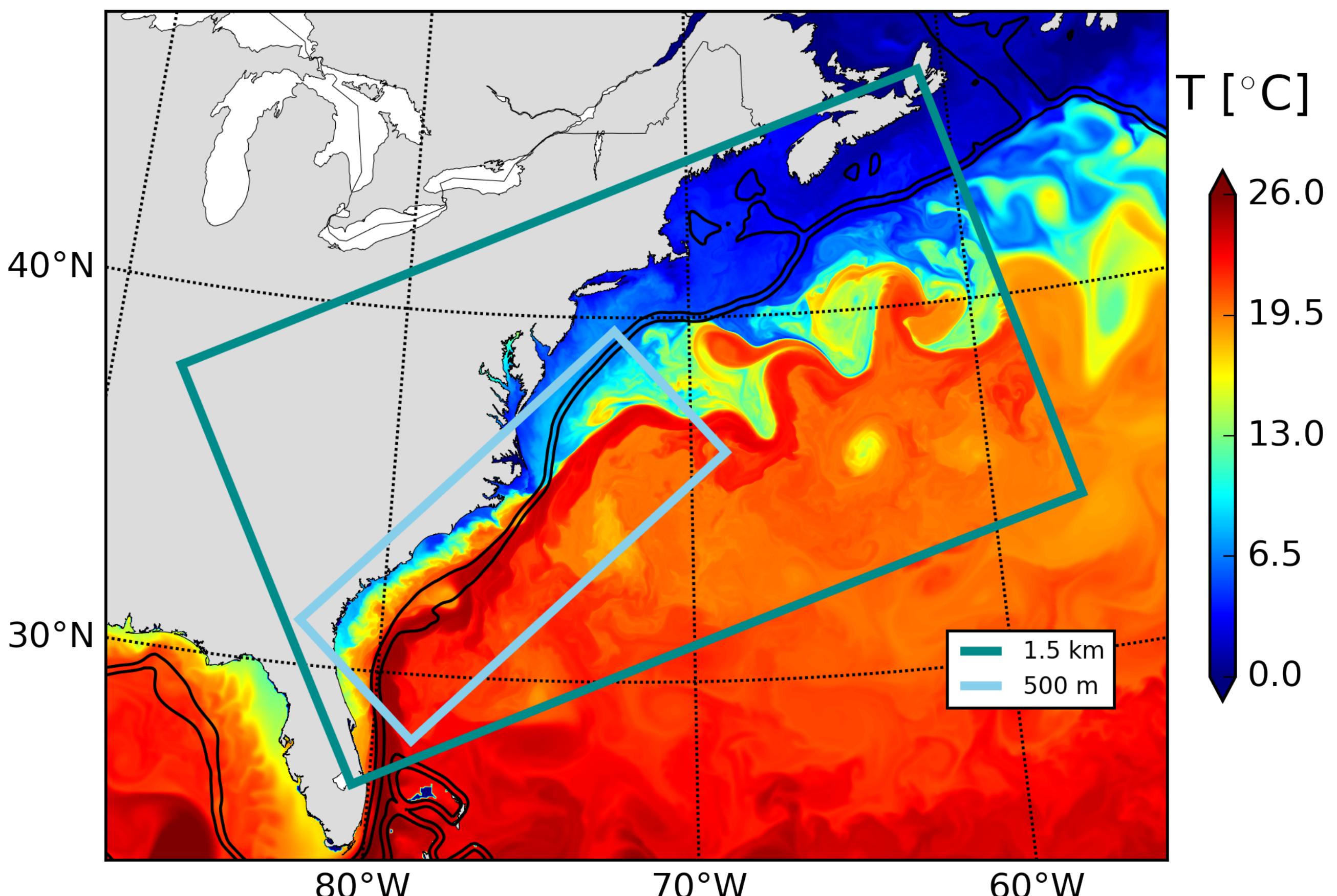


SCV1 and SCV2 do not match Labrador or Med sea water. How are they generated? Local processes?



# Realistic modelling with ROMS/CROCO

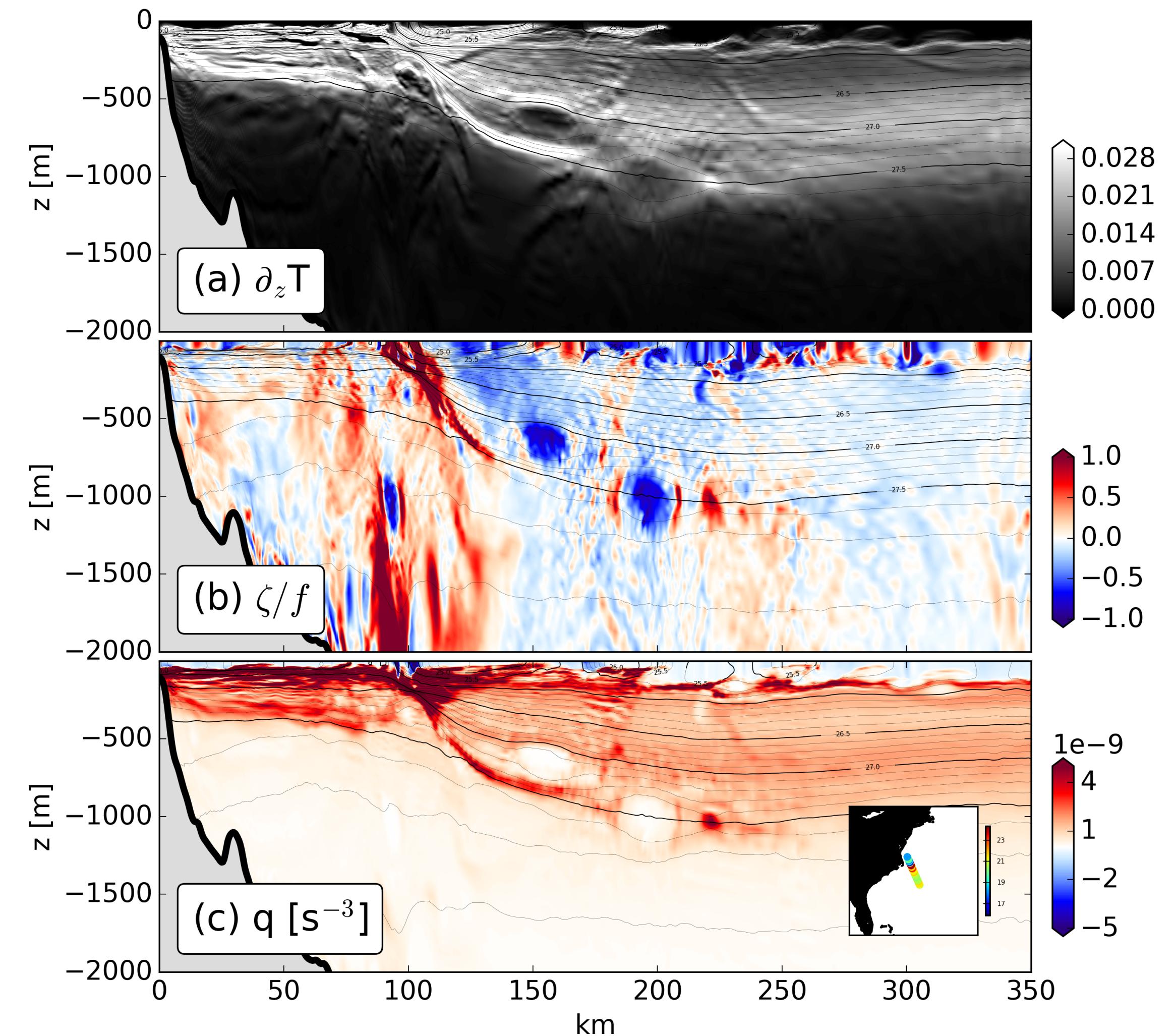
- Successive down-scale nested grids with the ROMS/CROCO model, from Atlantic ( $dx = 6 \text{ km}$ ) to local subdomains ( $dx = 500 \text{ m}$ , 100 lev.).
- $N_x \times N_y \times N_z = 2800 \times 1600 \times 100$
- Climatological forcings (daily winds, no tides)



# SCV's in the Gulf Stream

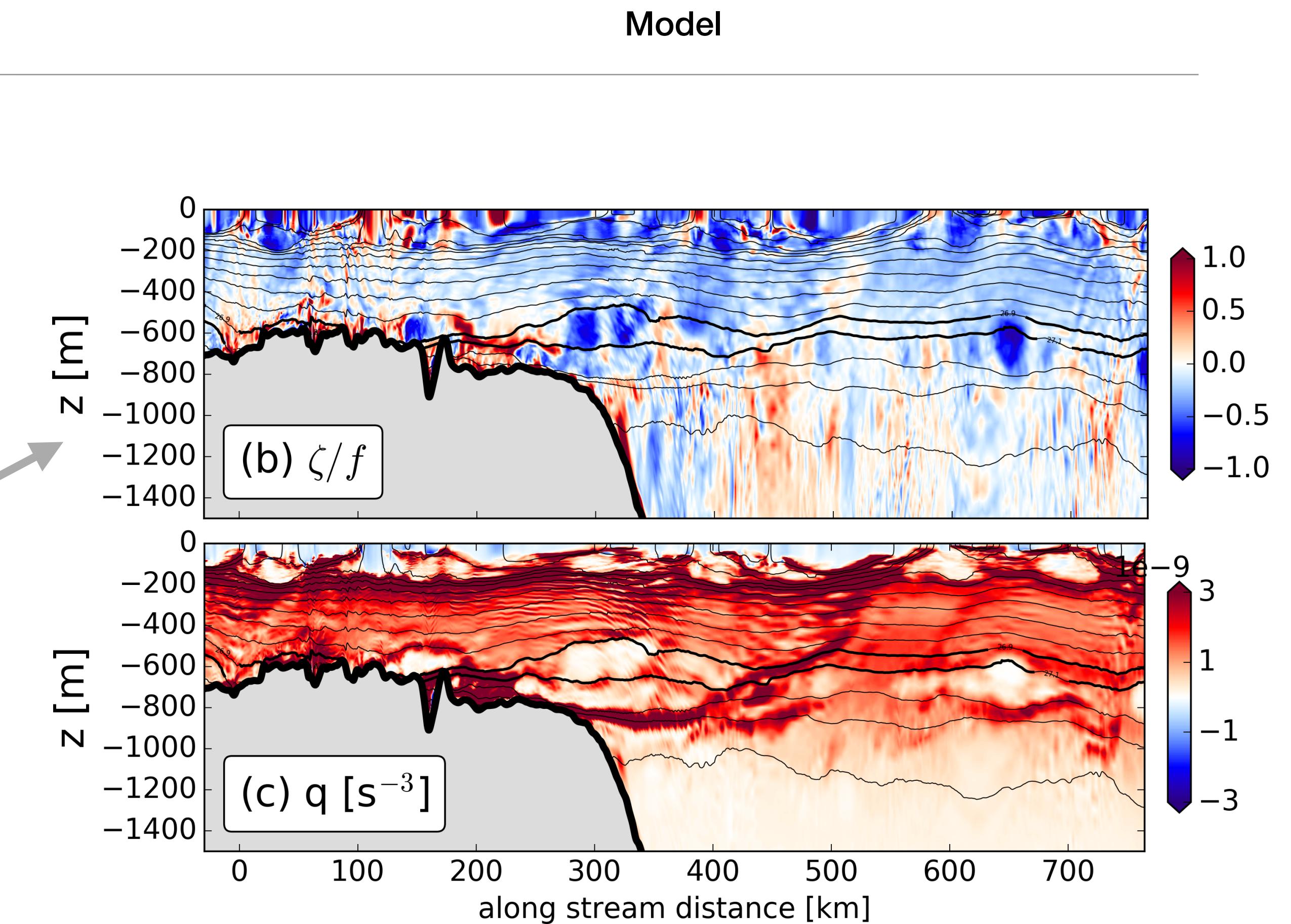
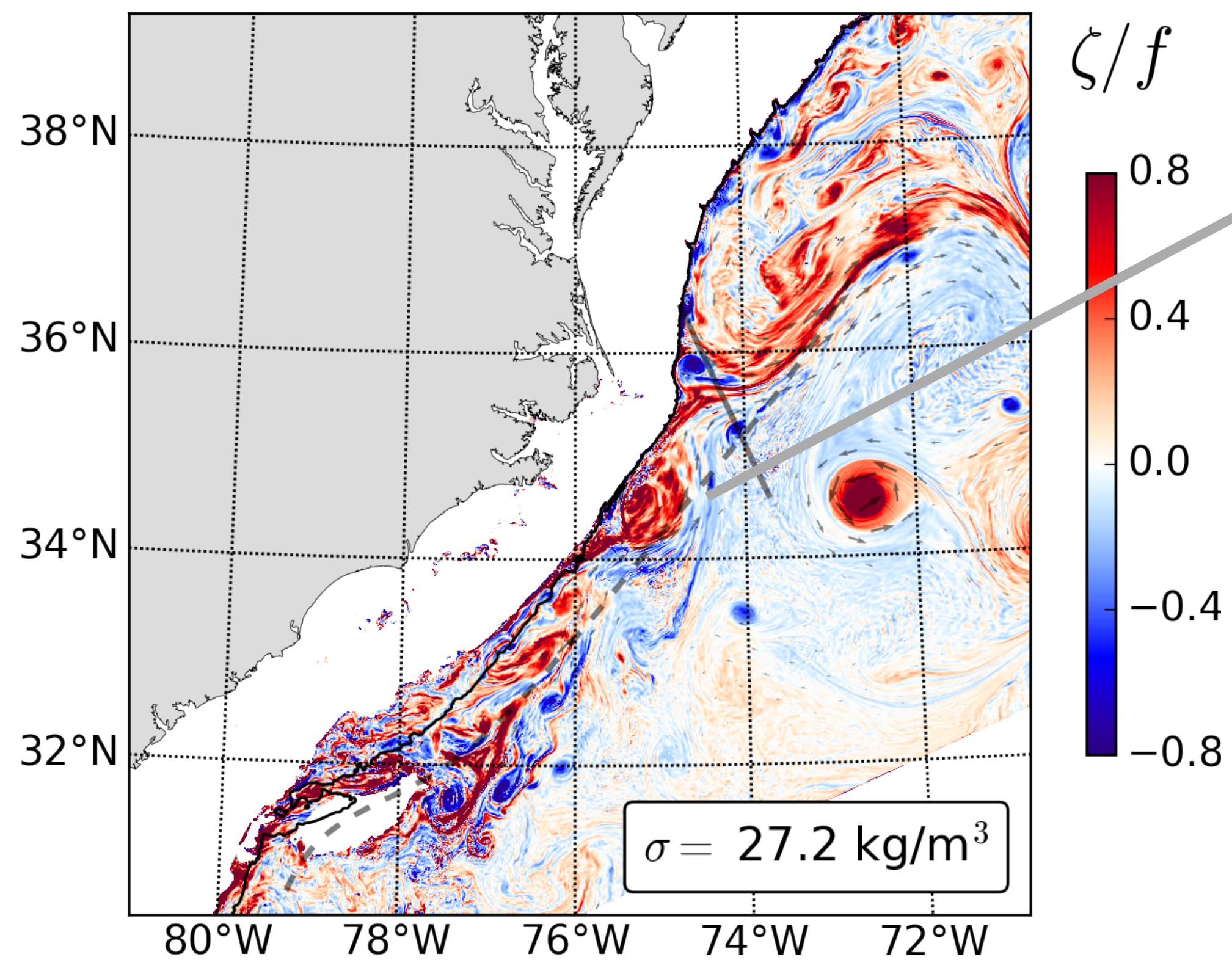
- The model typically exhibit a few SCVs at the location of the seismic data. They are located at similar depths and have similar radius and thickness.

Model ( $\Delta x = 500$  m)



# SCV's in the Gulf Stream

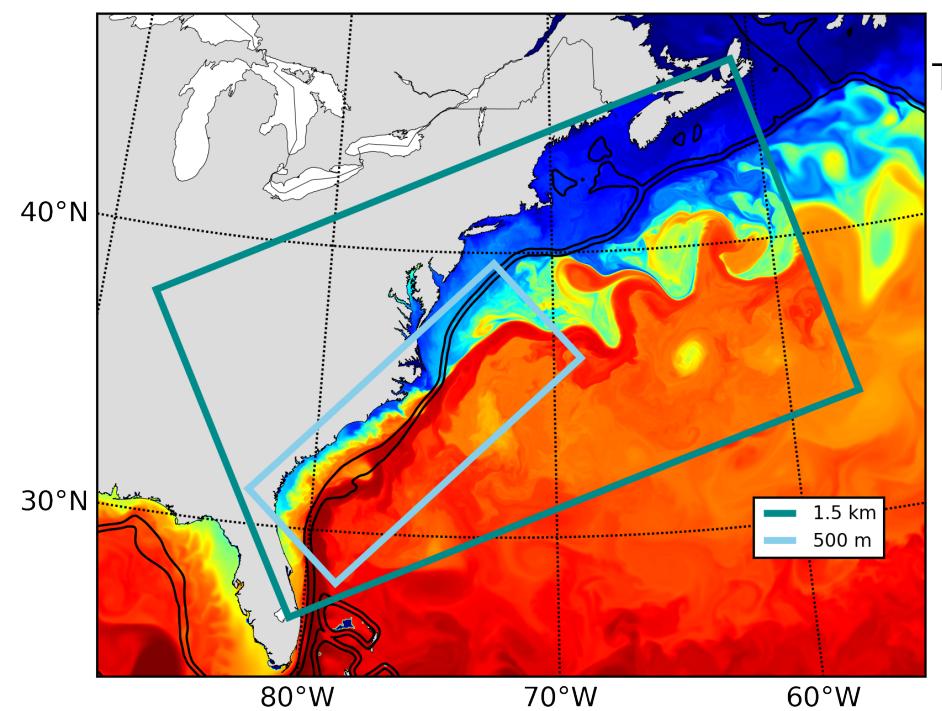
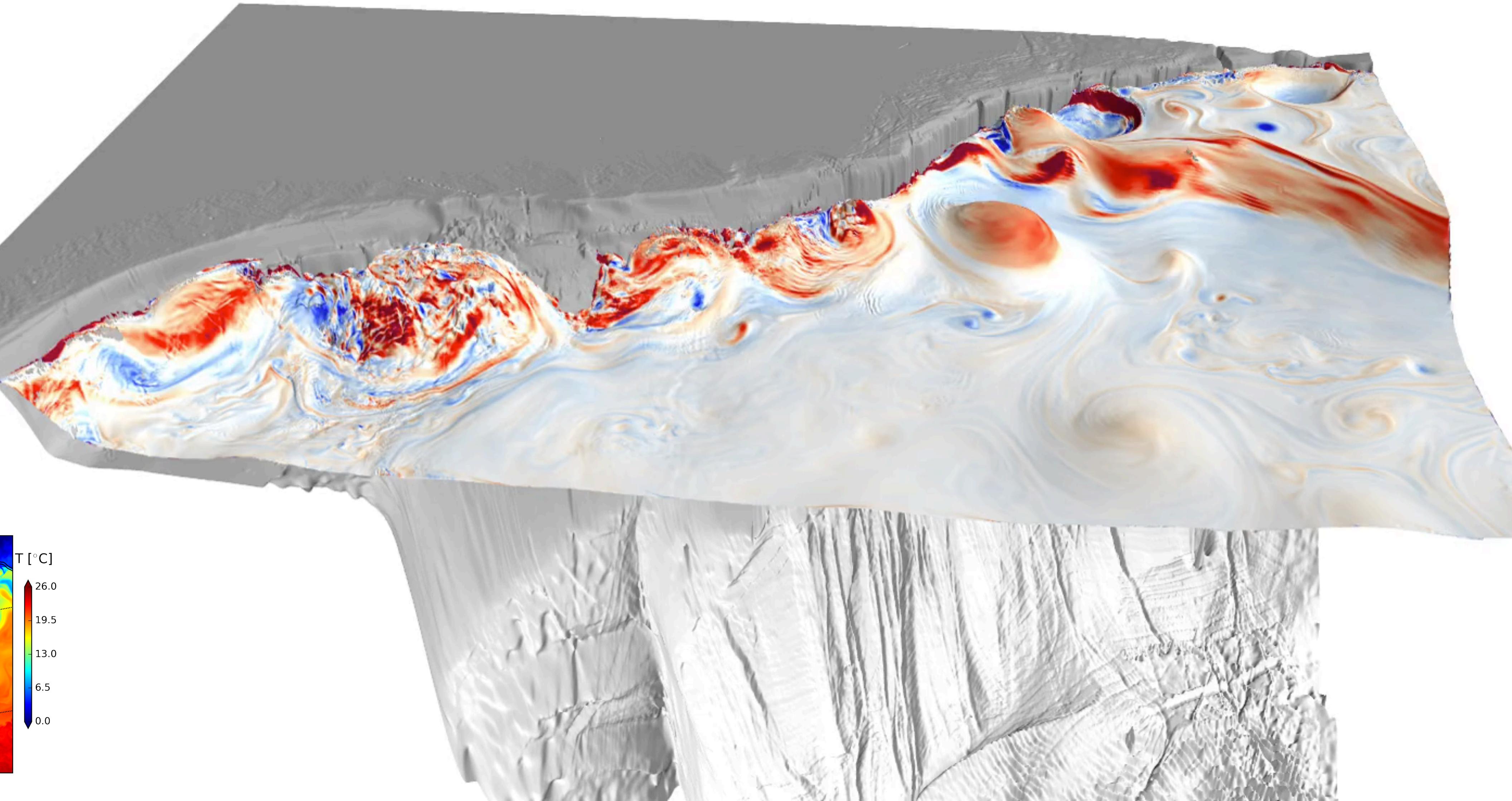
- The SCVs originate from the Charleston Bump, where there is a strong generation of vorticity due to frictional effects



# SCV's in the Gulf Stream

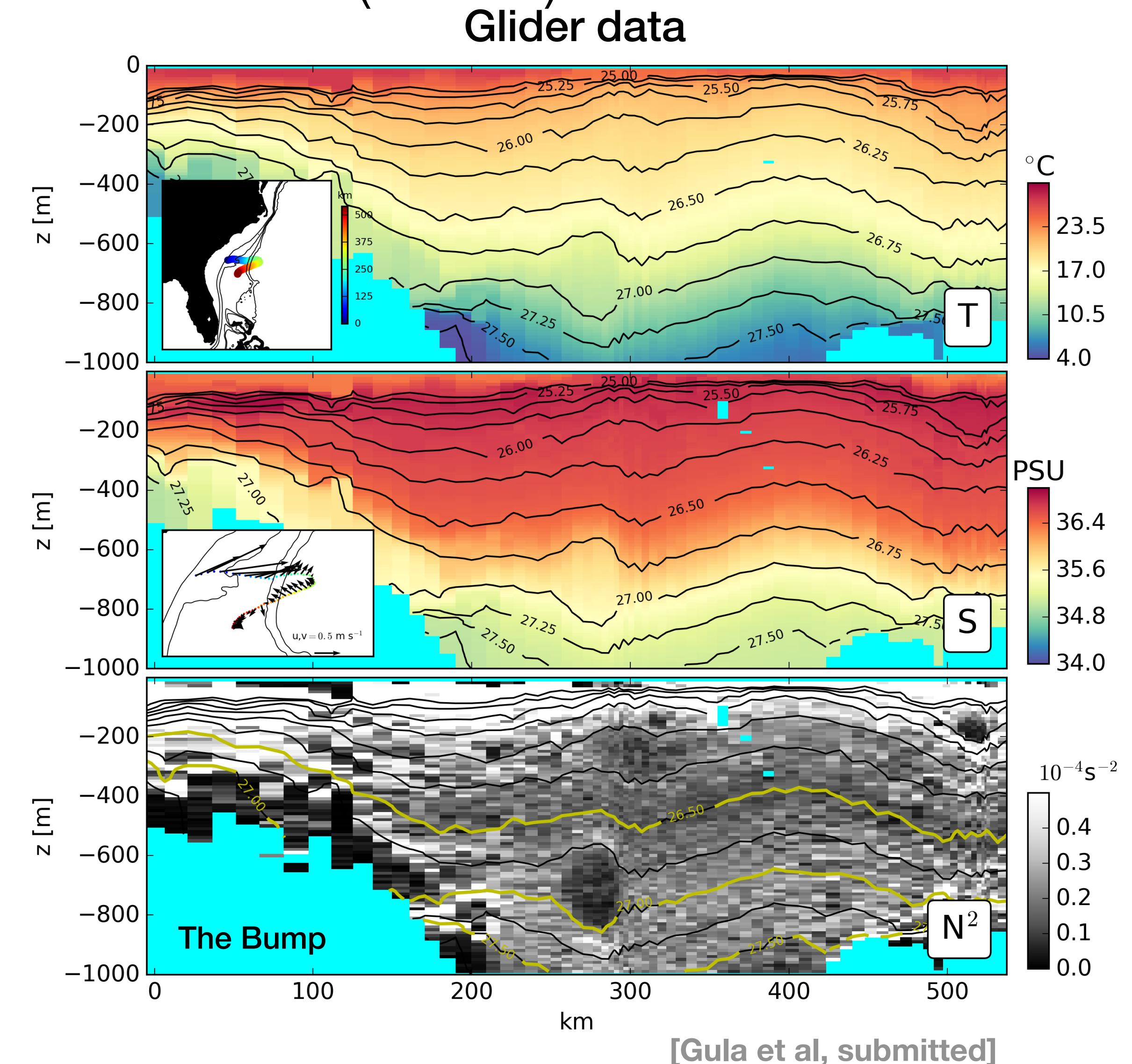
Relative vorticity on  
the isopycnal

$$\sigma = 27 \text{ kg m}^{-3}$$



# Generation of submesoscale coherent vortices (SCVs)

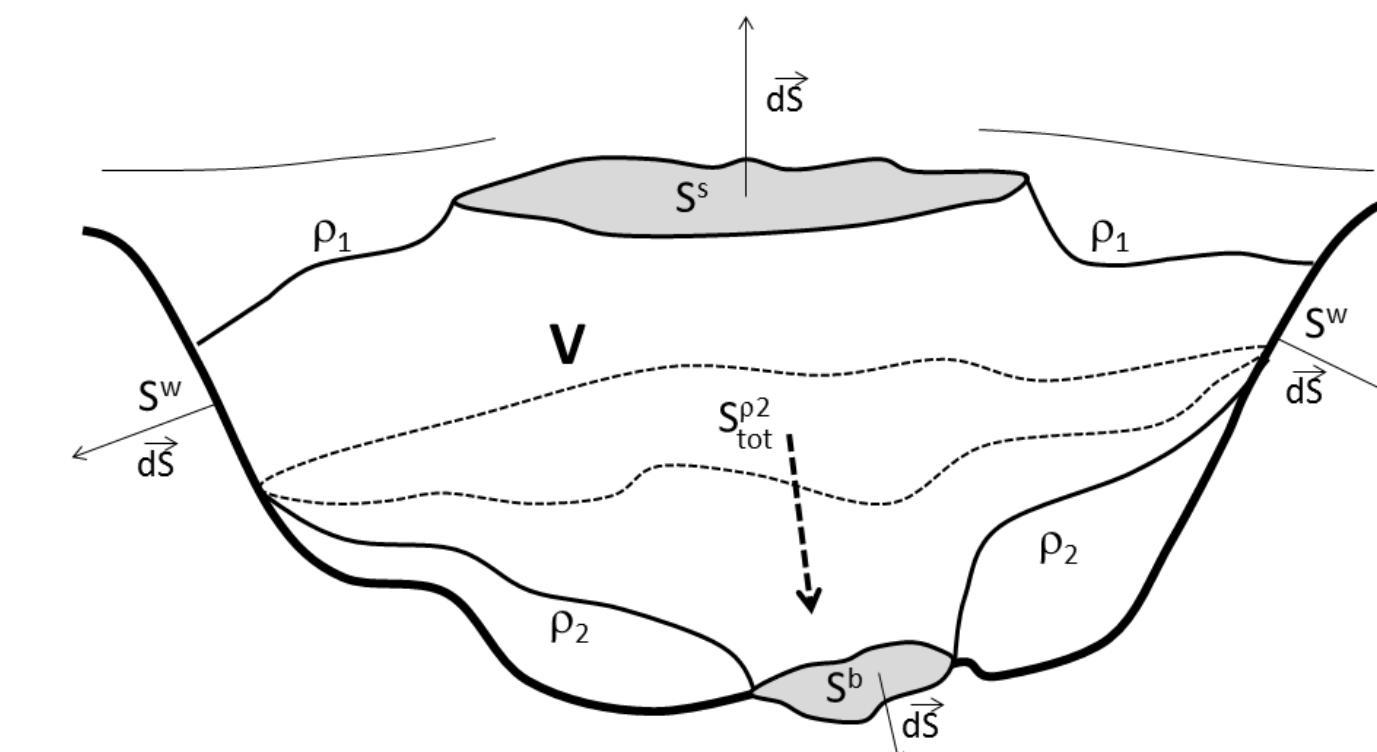
- Anticyclonic submesoscale lenses of well-mixed water are observed in glider sections of the Gulf Stream in the lee of the Bump
- Generation process is confirmed by Glider measurements.



# Bottom flux of PV

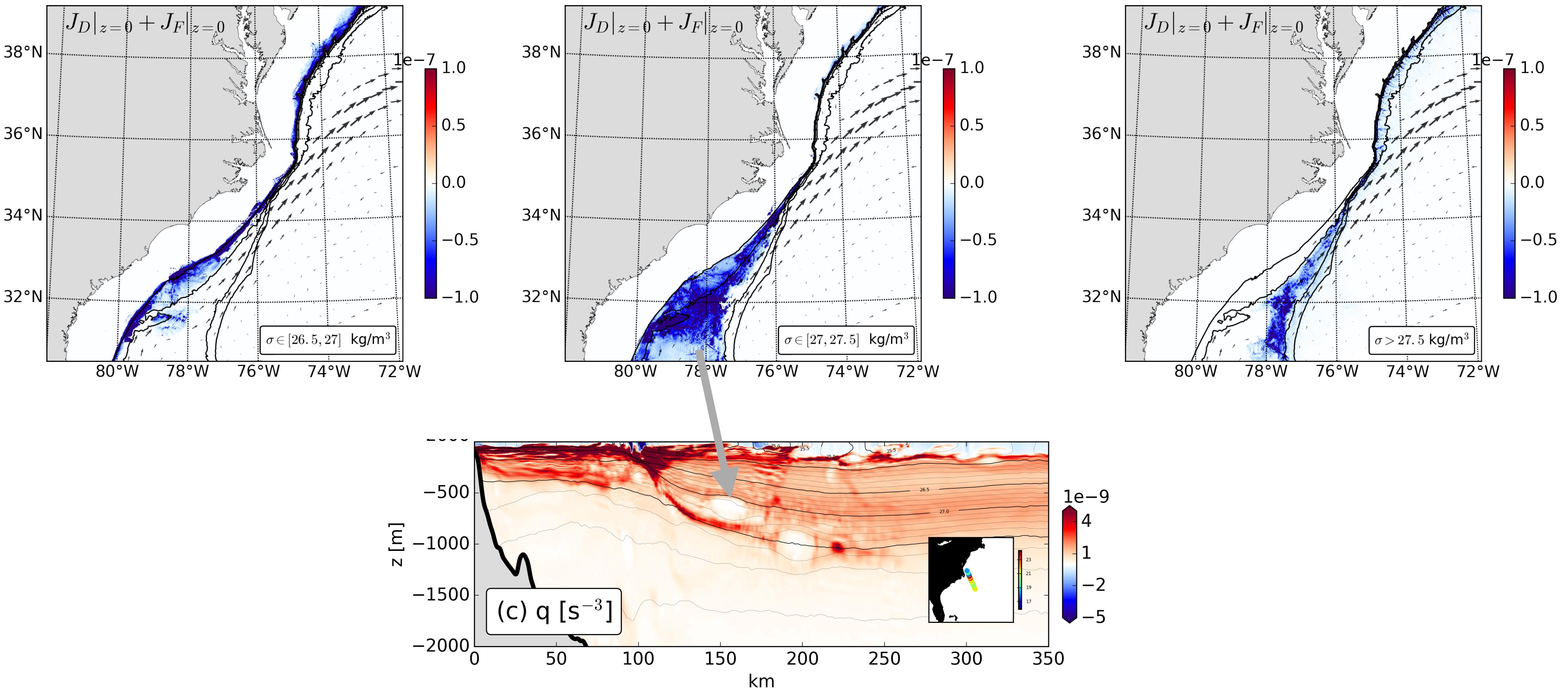
- The mechanisms of SCV formation must account for the creation of the low PV anomalies in their cores. They need to provide a source of low PV in a spatially intermittent fashion.
- PV is defined as.  $q = \omega_{\mathbf{a}} \cdot \nabla b$  with  $\omega_{\mathbf{a}} = f\mathbf{z} + \nabla \times \mathbf{u}$  and  $b = -g \frac{\rho}{\rho_0}$
- PV fluxes can be written: 
$$\frac{\partial q}{\partial t} + \nabla \cdot [ \underbrace{q\mathbf{u}}_{J_A} - \underbrace{\omega_{\mathbf{a}} \frac{Db}{Dt}}_{J_D} + \underbrace{\nabla b \times \mathbf{F}}_{J_F} ] = 0,$$
- For a volume of water between 2 isopycnals, the potential vorticity impermeability theorem [Haynes & McIntyre, 87, Haynes & McIntyre, 90], states that PV changes can only be due to frictional or diabatic effects in outcropping regions:

$$\frac{\partial}{\partial t} \int q dV = - \int (J_D|_{z=0} + J_F|_{z=0}) dA,$$



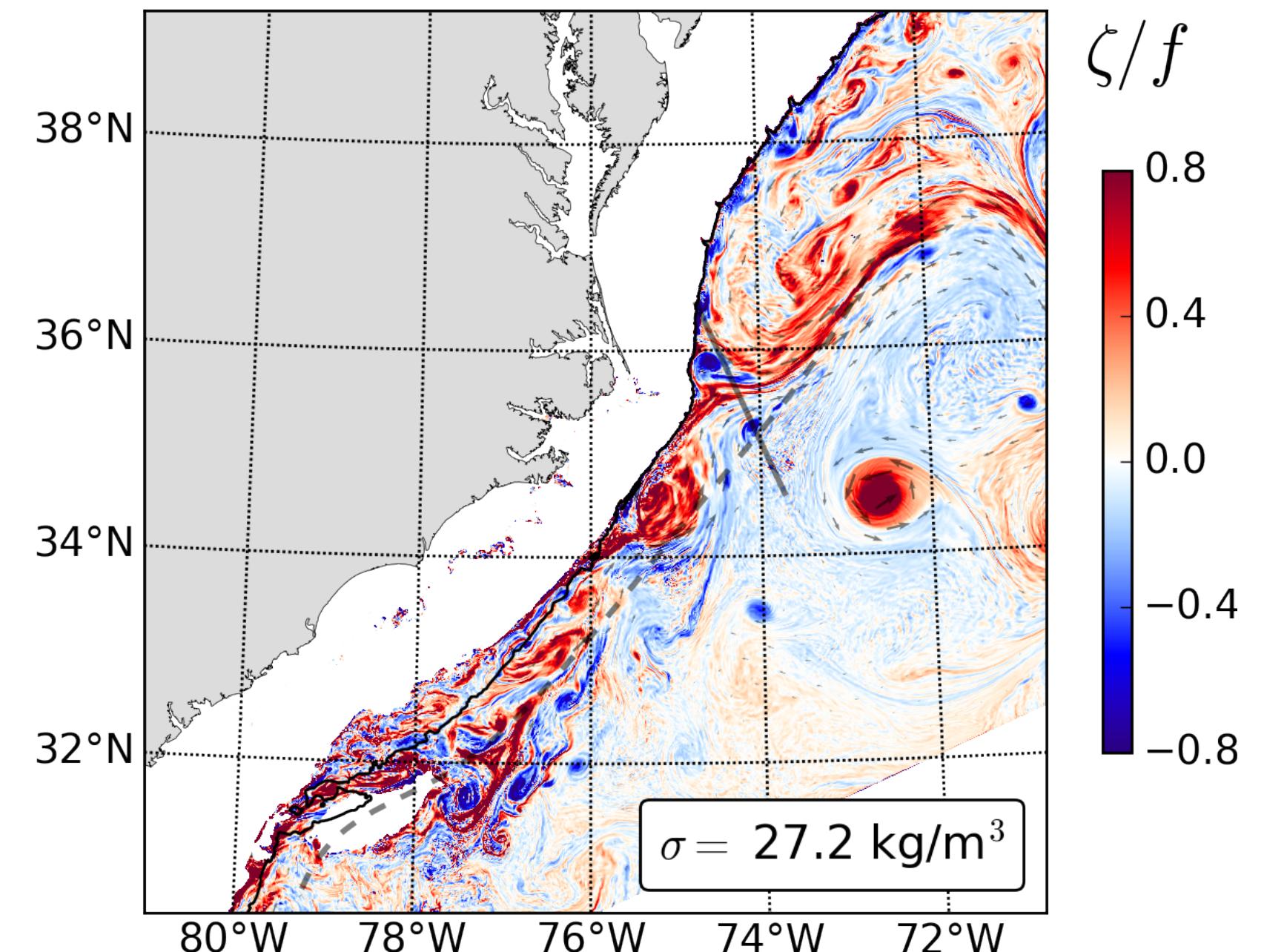
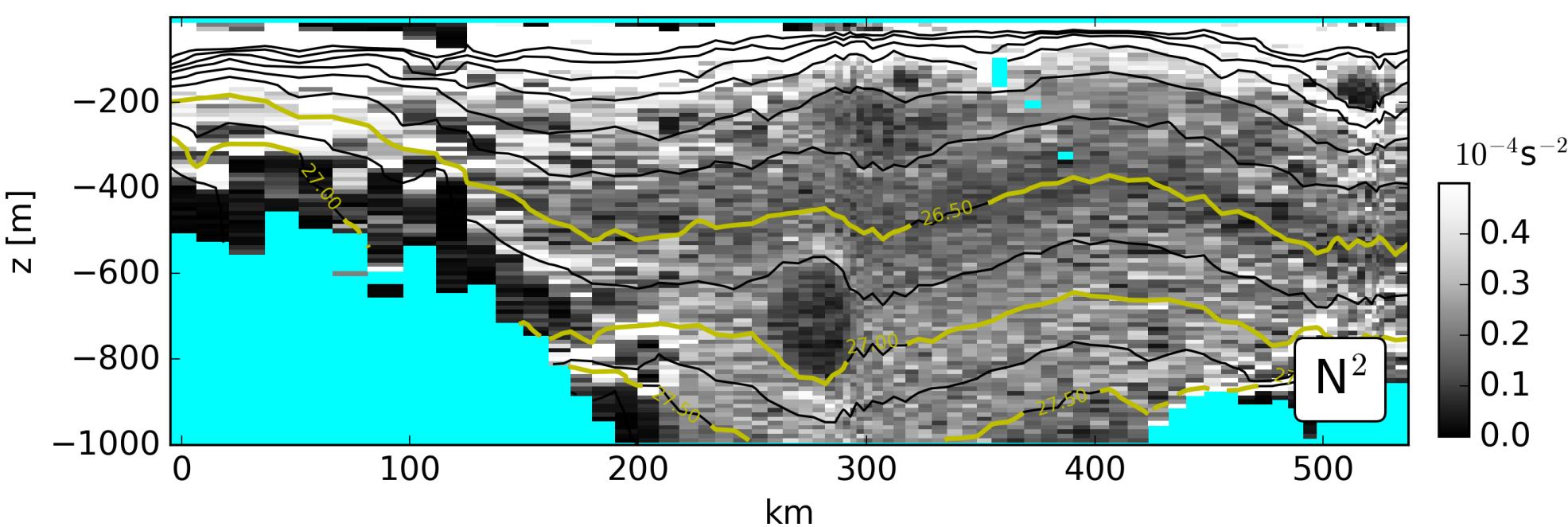
# Bottom flux of PV

- Injection of negative PV within different isopycnal ranges:



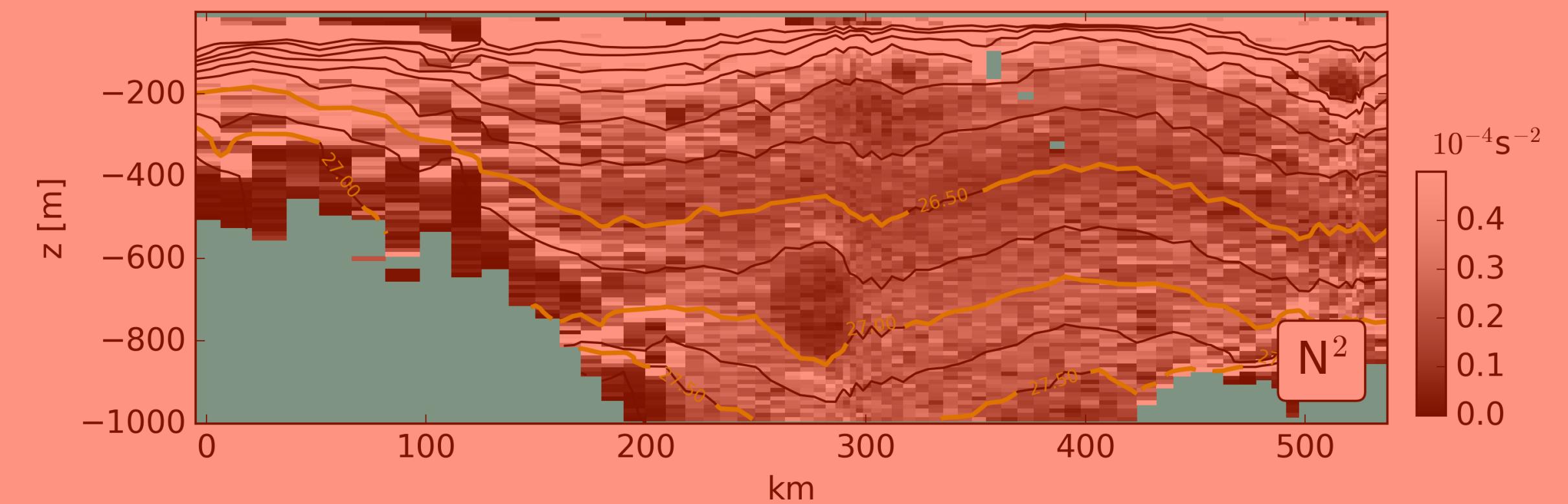
# Partial Summary

1. Submesoscale lenses of well-mixed water are observed in seismic reflection images and glider sections of the Gulf Stream
2. They are reproduced by a submesoscale resolving realistic simulation and identified as anticyclonic submesoscale coherent vortices
3. Submesoscale coherent vortices are generated by flow topography interactions in the lee of the Charleston Bump

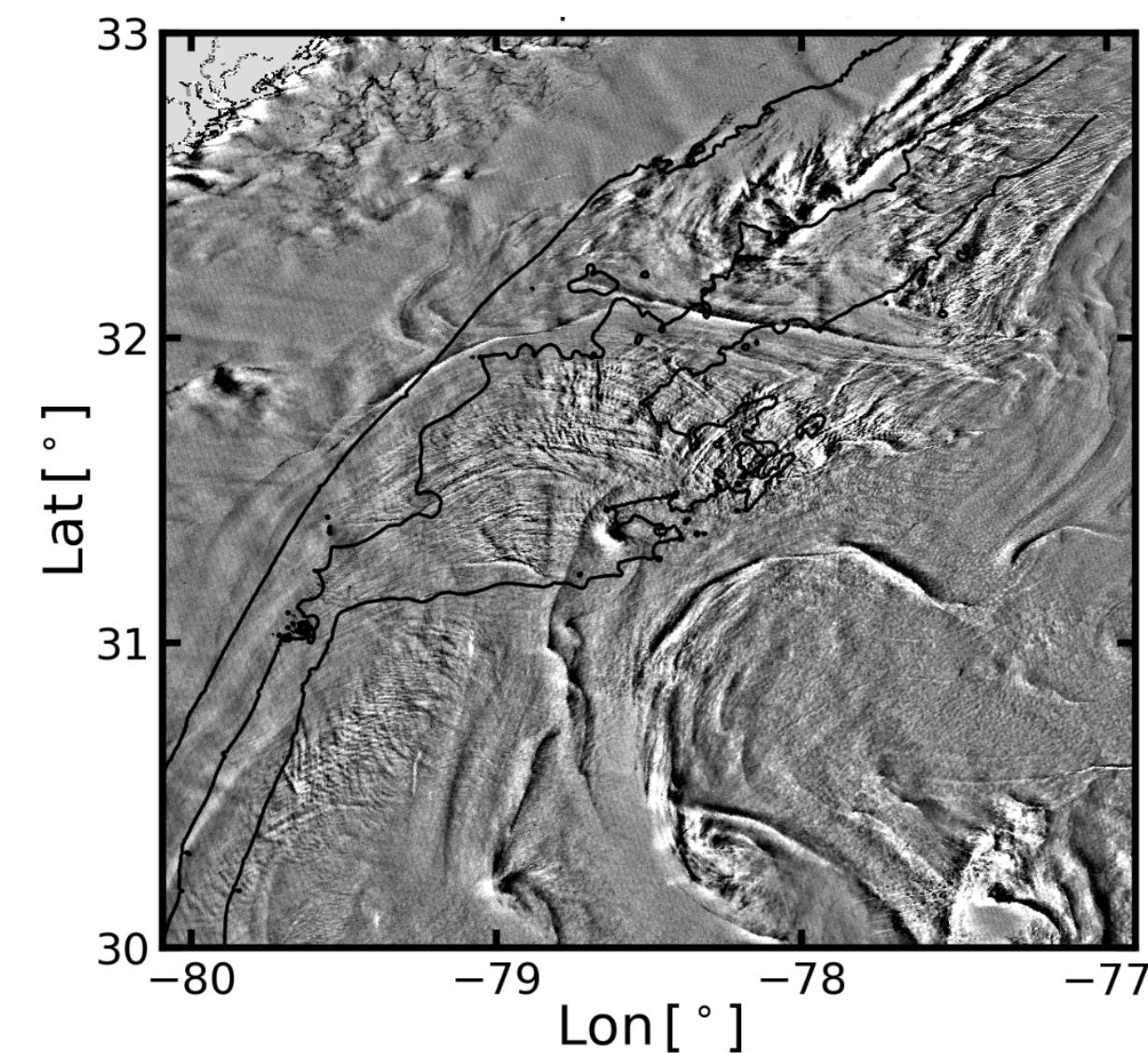


# OUTLINE

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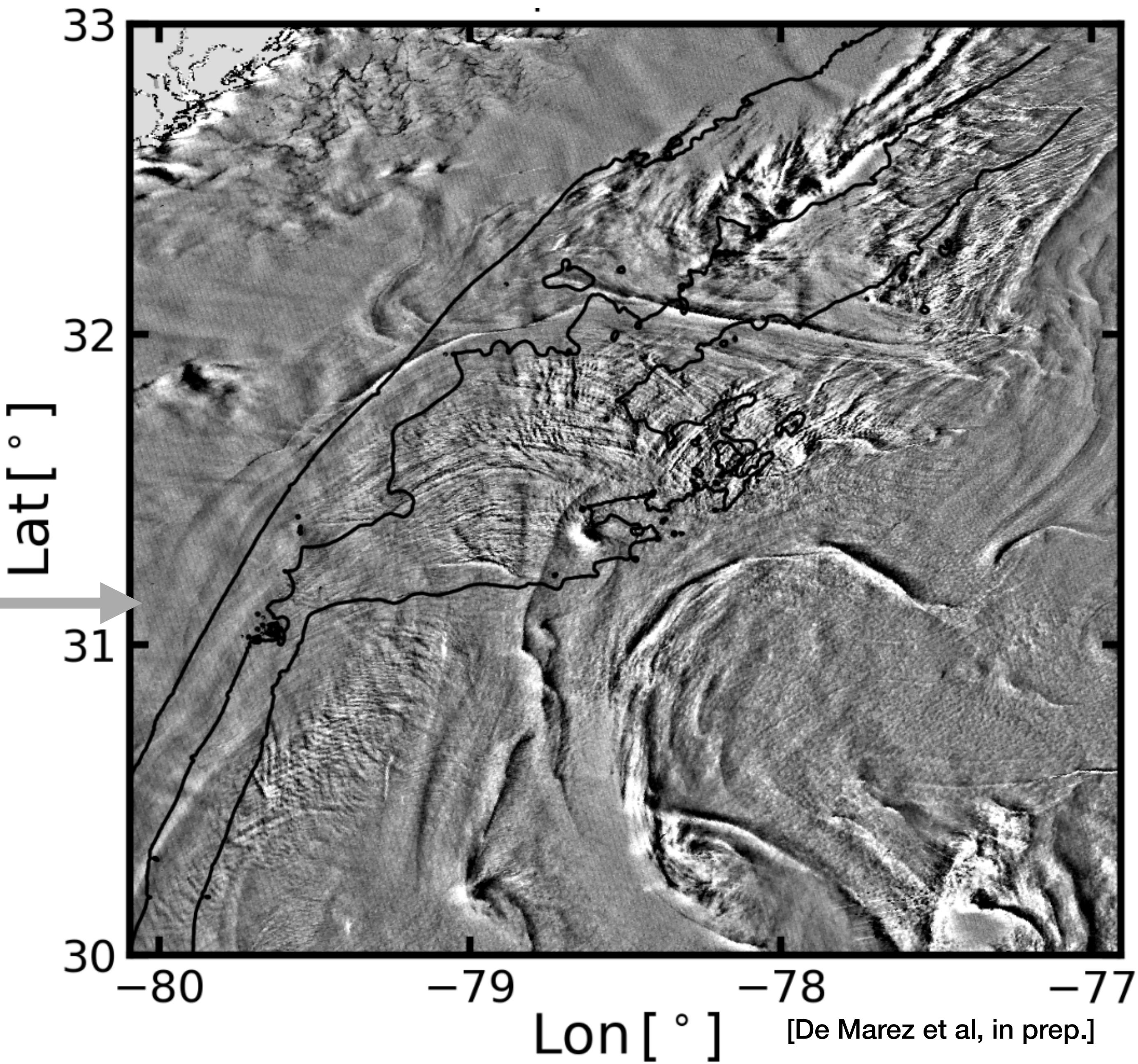
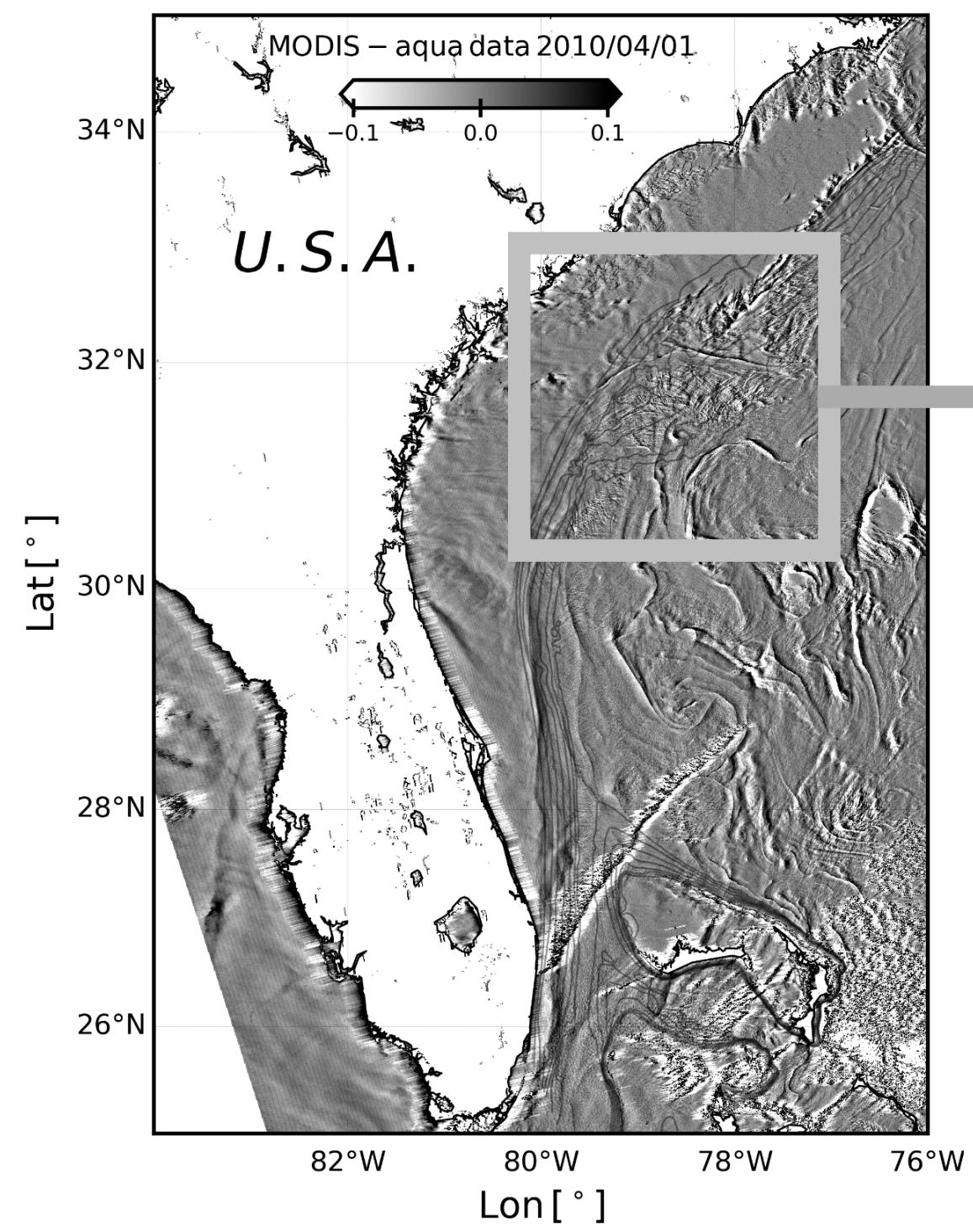


2. Generation of Lee waves over the Charleston Bump



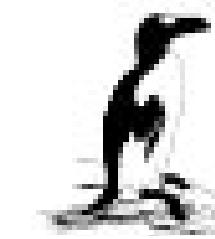
# Observations of Lee Waves in the Gulf Stream

- Internal waves can be observed using synthetic aperture radars (SAR) or Sun-glitter images through their surface roughness signature.



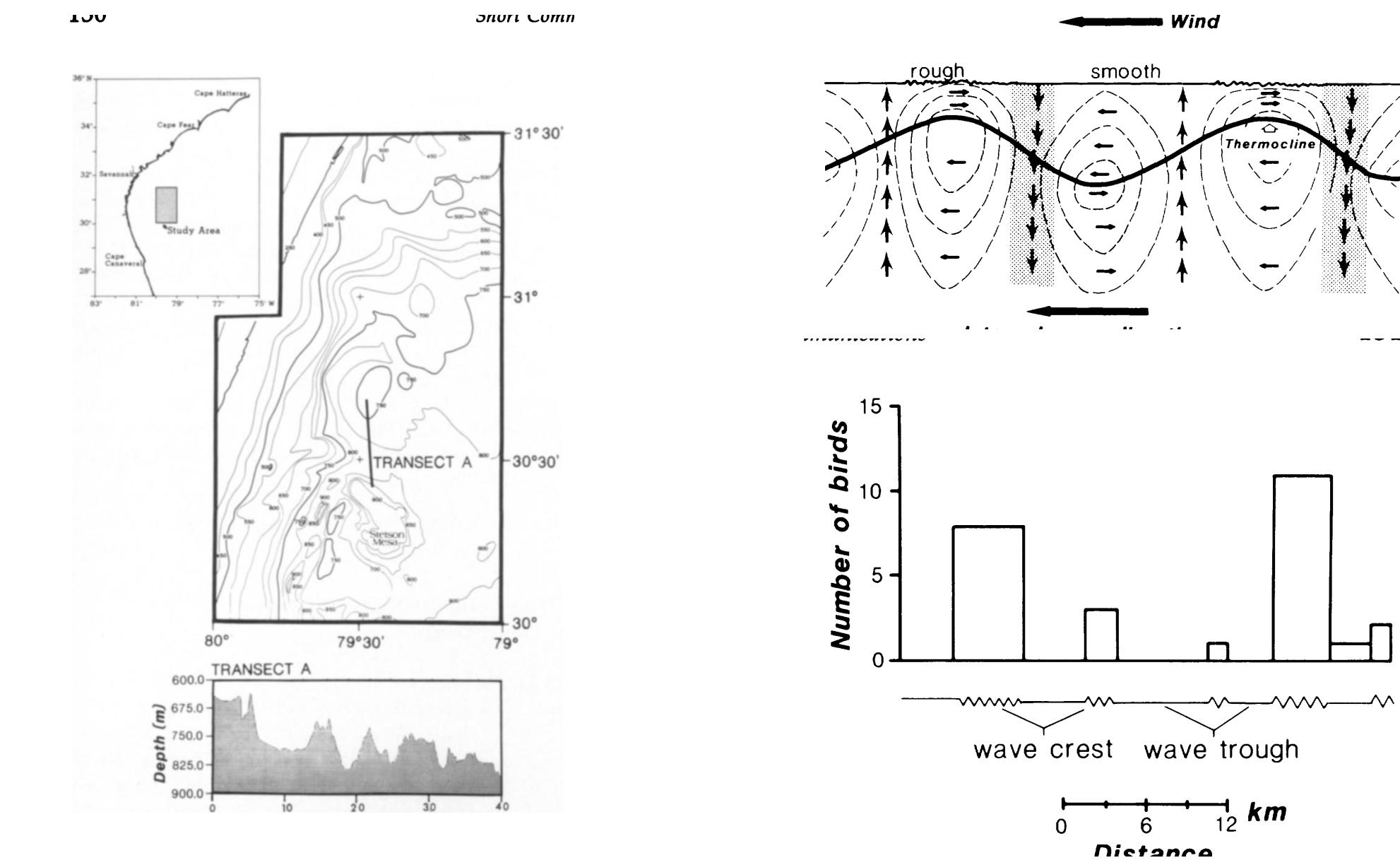
# Observations of Lee Waves in the Gulf Stream

- They were also previously inferred from patchiness in sea-birds distribution:



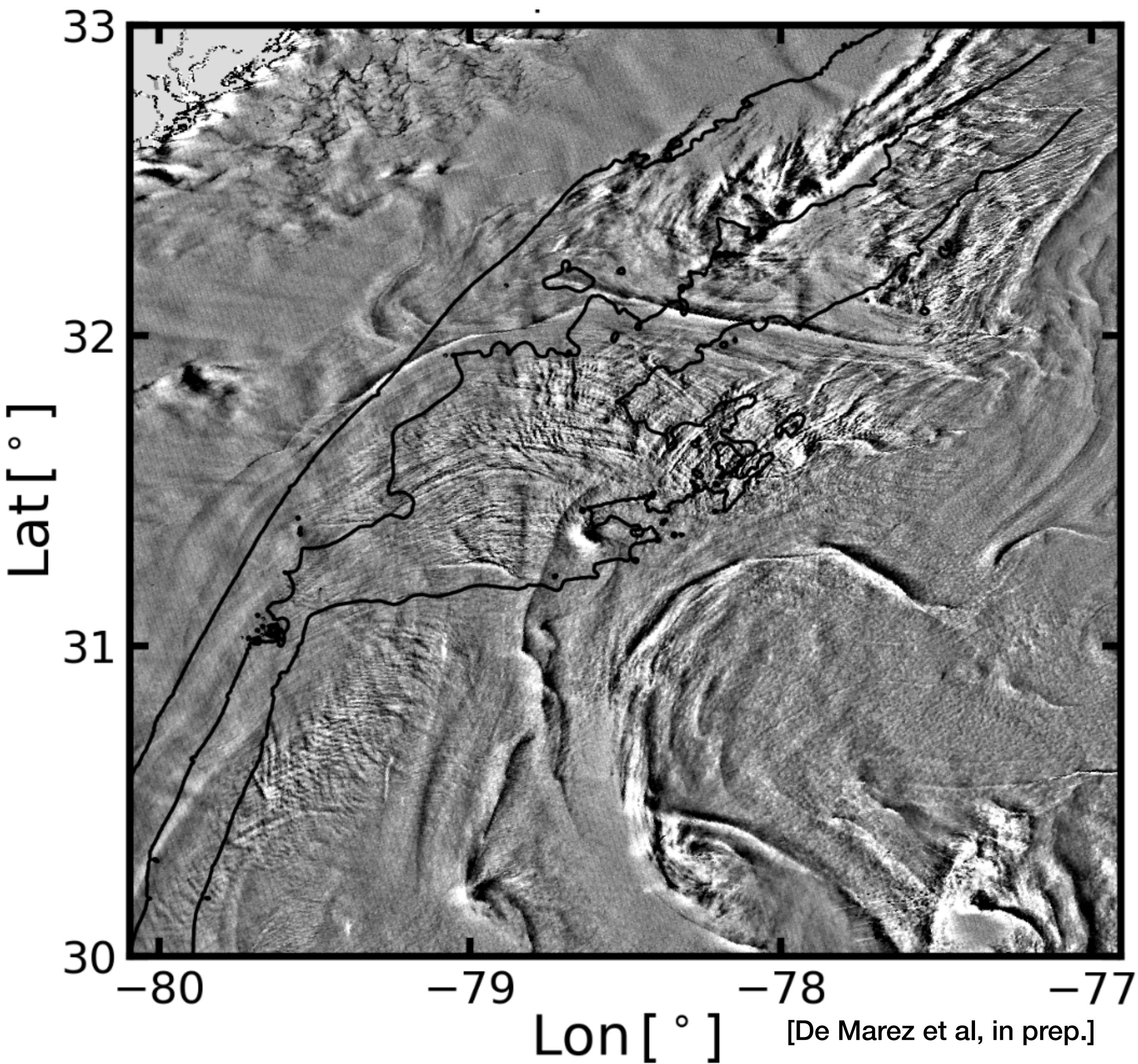
The American  
Ornithologists' Union

Haney, 1986: “Ocean Internal Waves as Sources of Small-Scale Patchiness in Seabird Distribution on the Blake Plateau”.



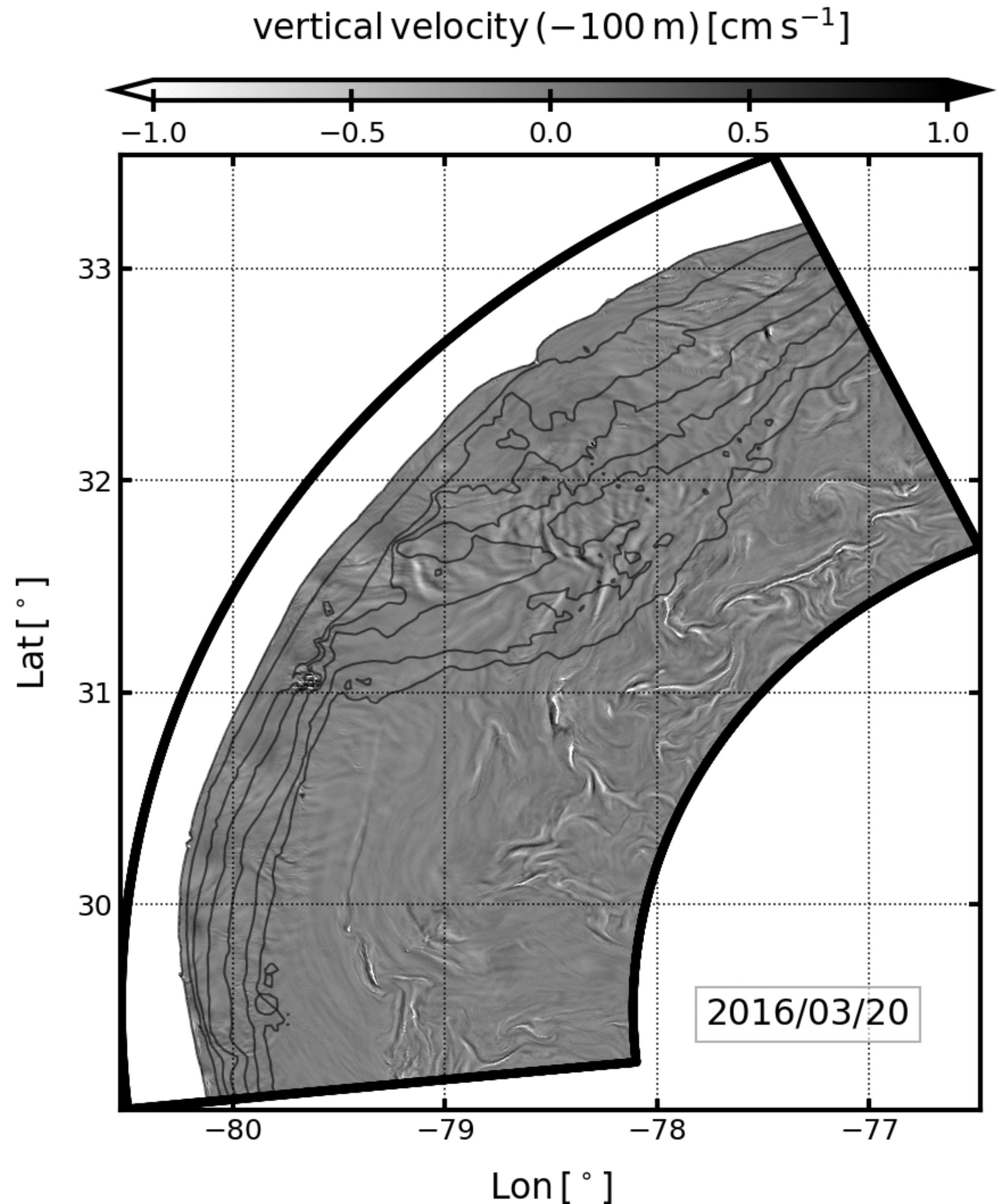
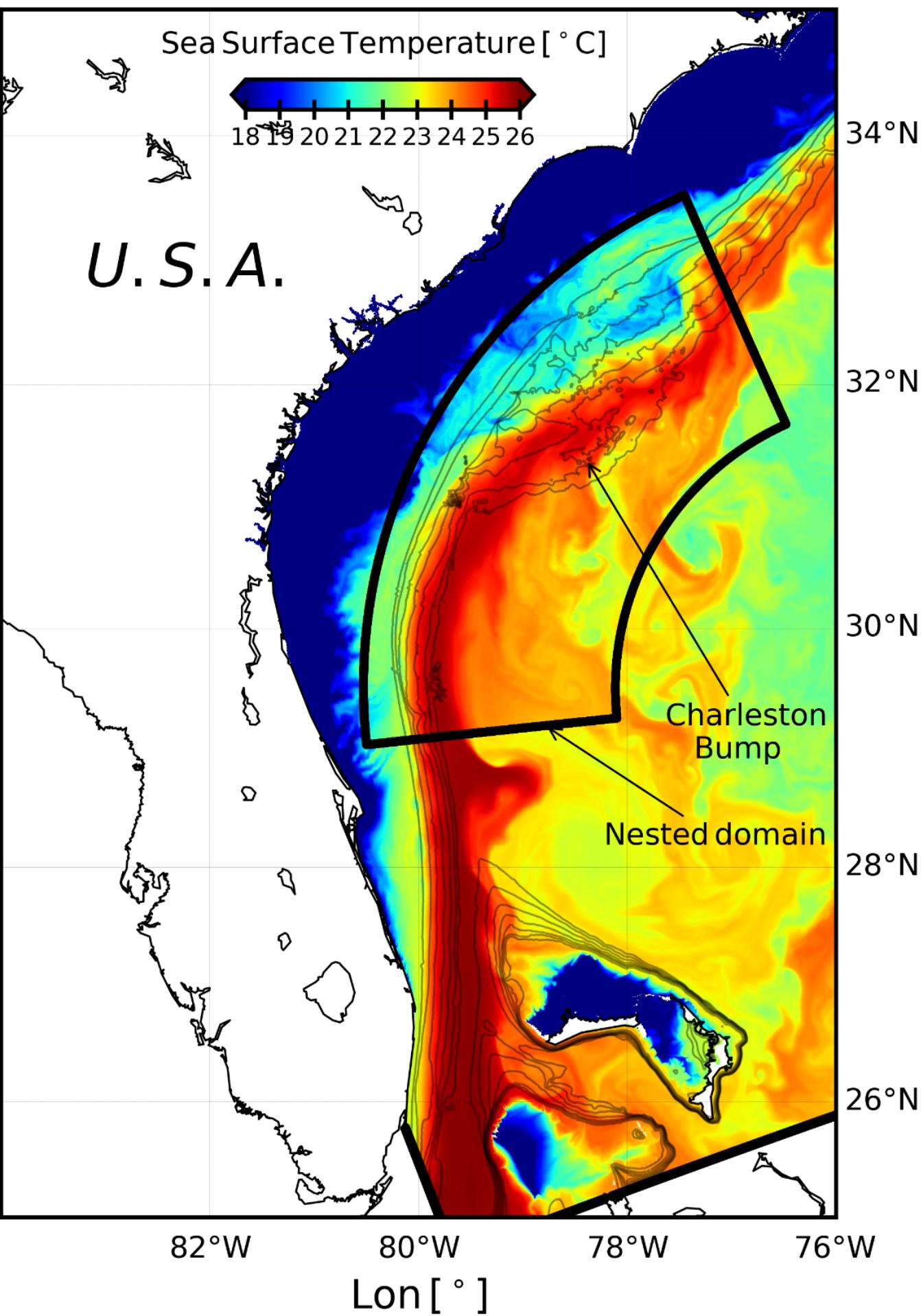
# Questions about Lee Waves

- Formally identify the internal waves signature, are all of these signatures of Lee waves?
- Characterize Lee waves dynamics. Are they linear, hydrostatic?
- Do they impact energy dissipation and mixing?



# Simulation of the Gulf Stream

- We performed a ROMS/CROCO nest  $\text{dx} = 200 \text{ m}$ ,
- $\text{Nx} \times \text{Ny} \times \text{Nz} = 1024 \times 2048 \times 128$
- Climatological forcings (monthly winds, no tides)
- 



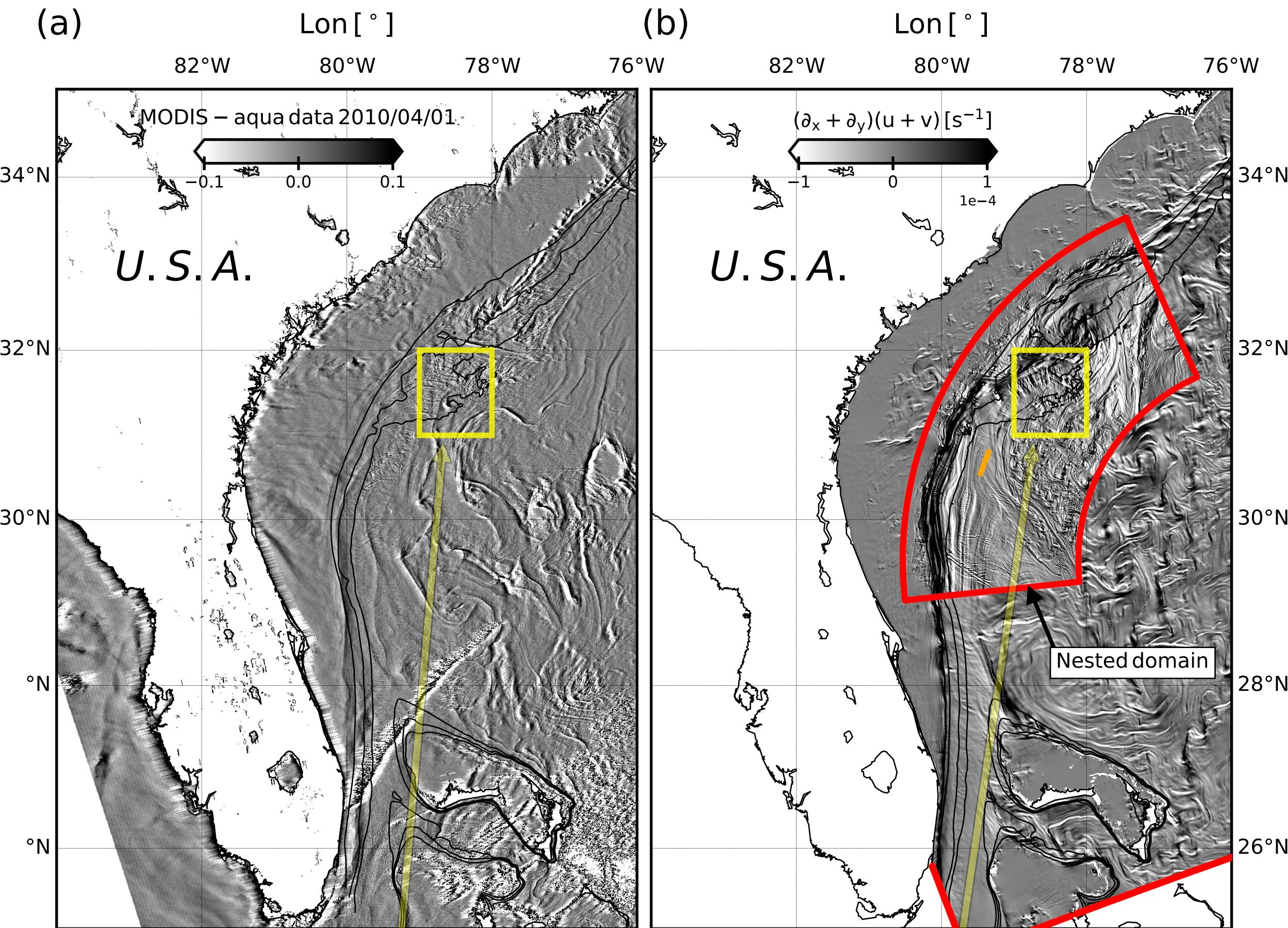
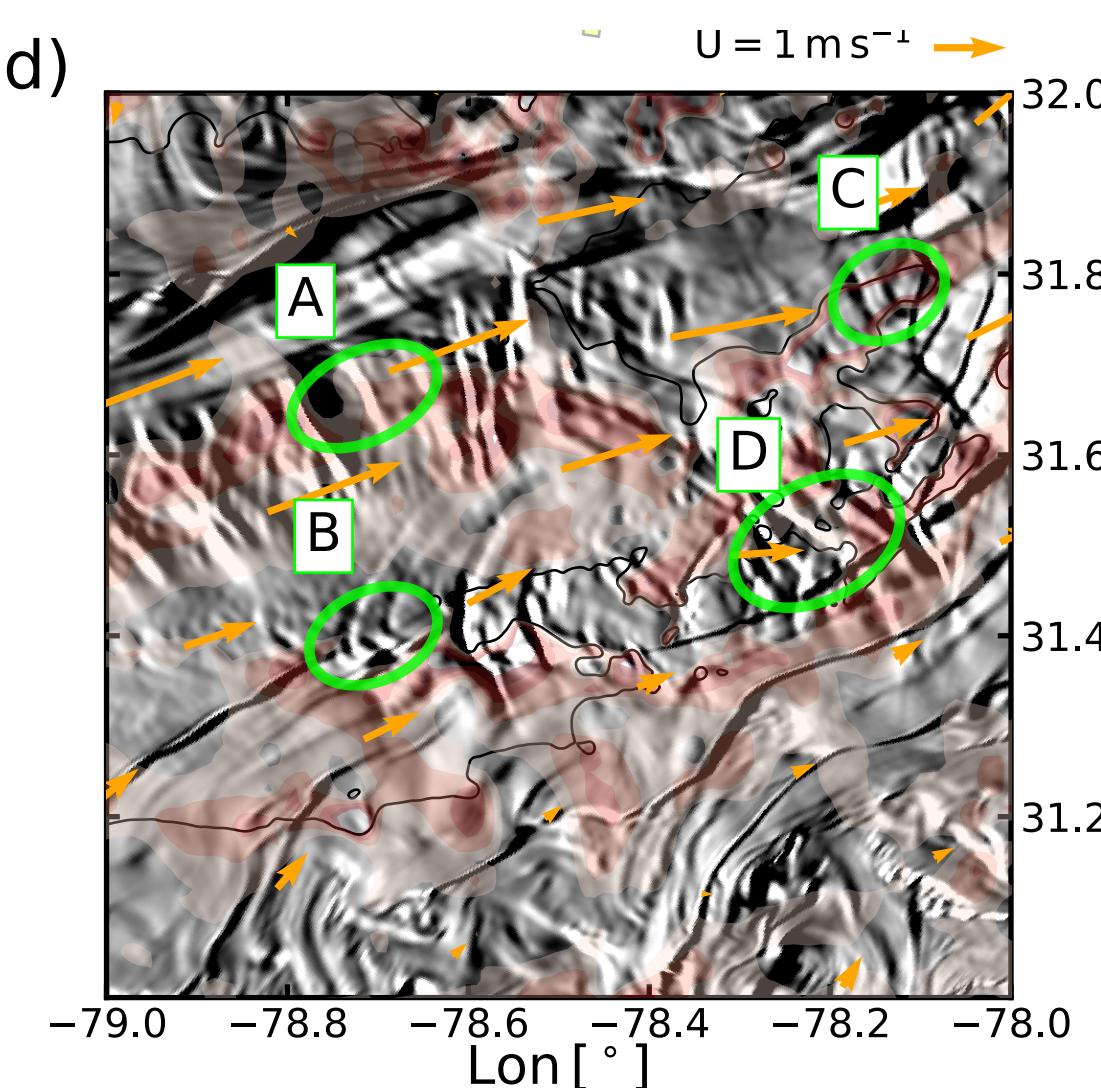
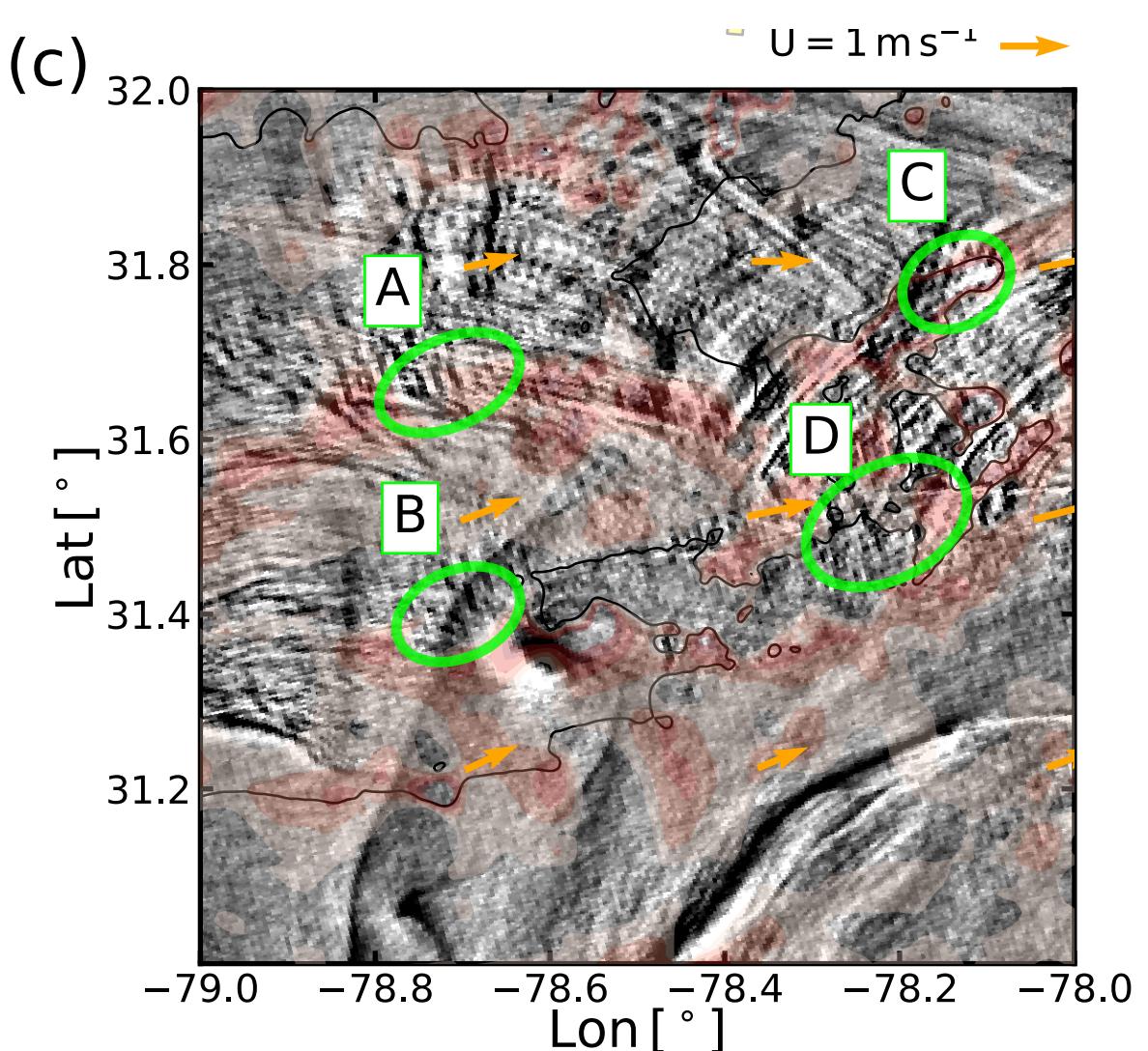
# Lee Waves in the Gulf Stream

The surface roughness can be interpreted as:

$$\text{roughness} \sim \alpha \partial_x u + \beta \partial_y u + \gamma \partial_x v + \delta \partial_y v,$$

where the coefficients  $\alpha$ ,  $\beta$ ,  $\gamma$  and  $\delta$  are functions of (1) the wind direction and (2) the position of the measuring device with respect to the position of the sun. So we compute, as a first approximation:

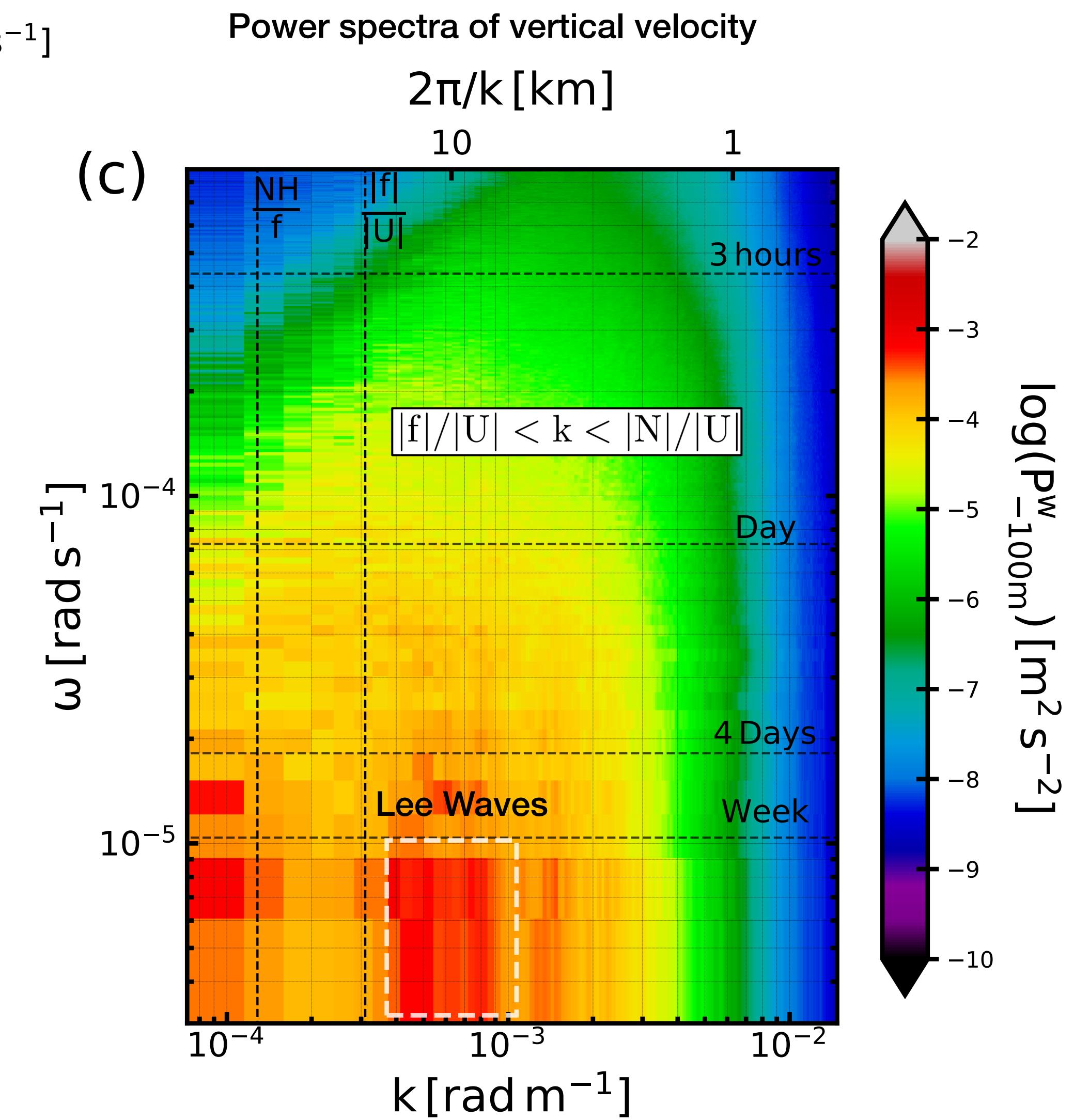
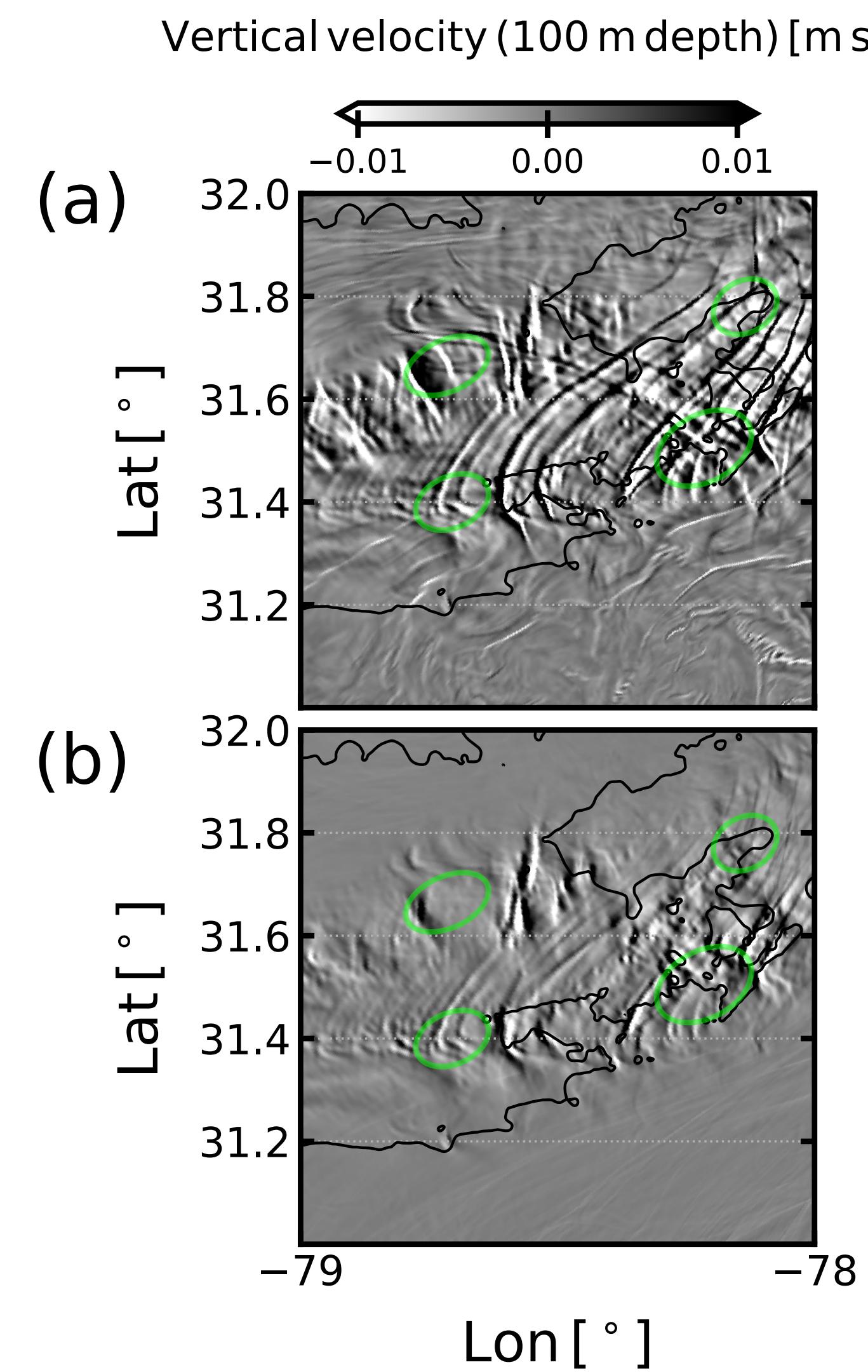
$$(\partial_x + \partial_y)(u + v)$$



**Qualitatively similar wave patterns in the simulation – Point to point comparison limited by accuracy of topographic data (here SRTM30)!**

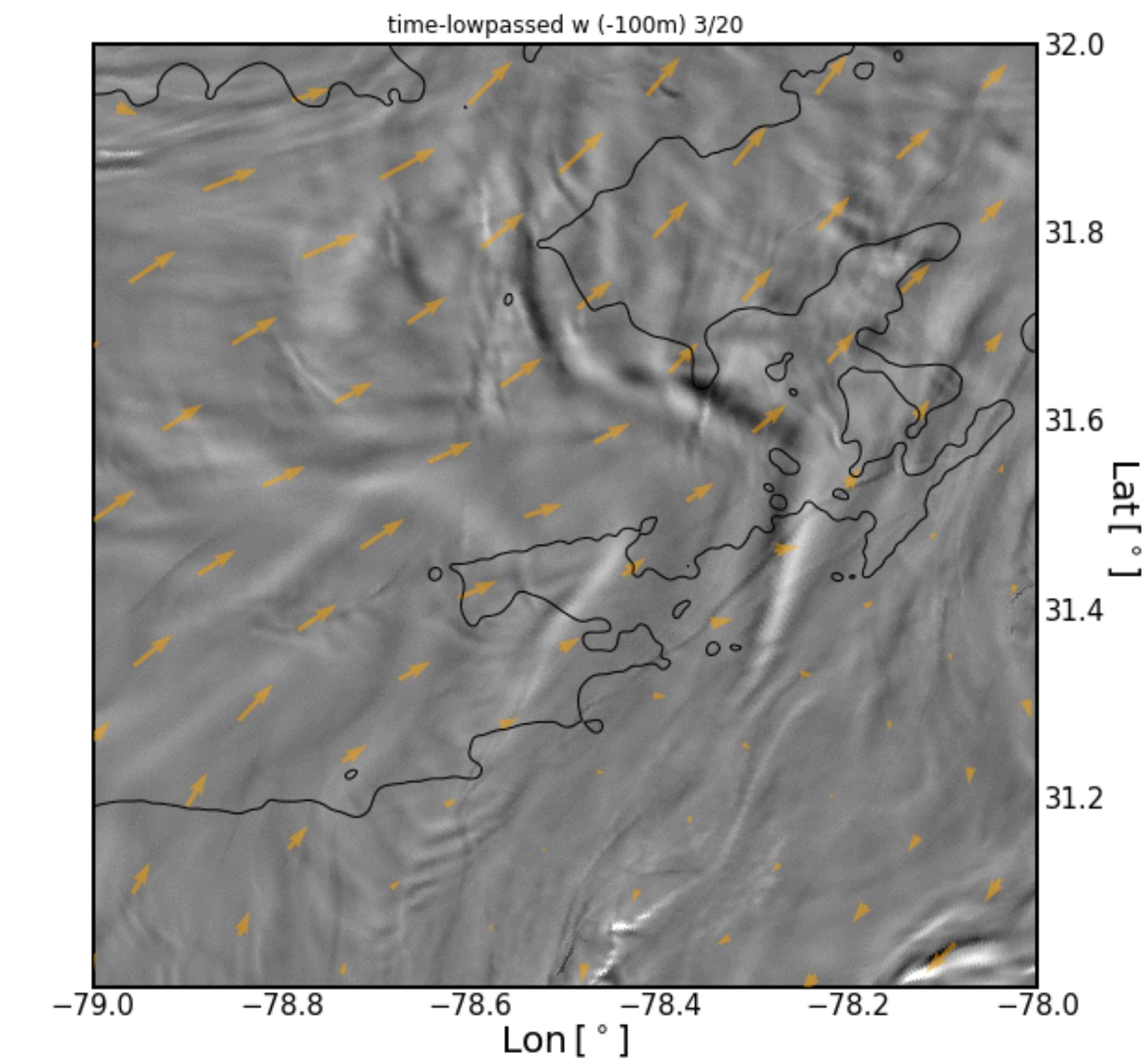
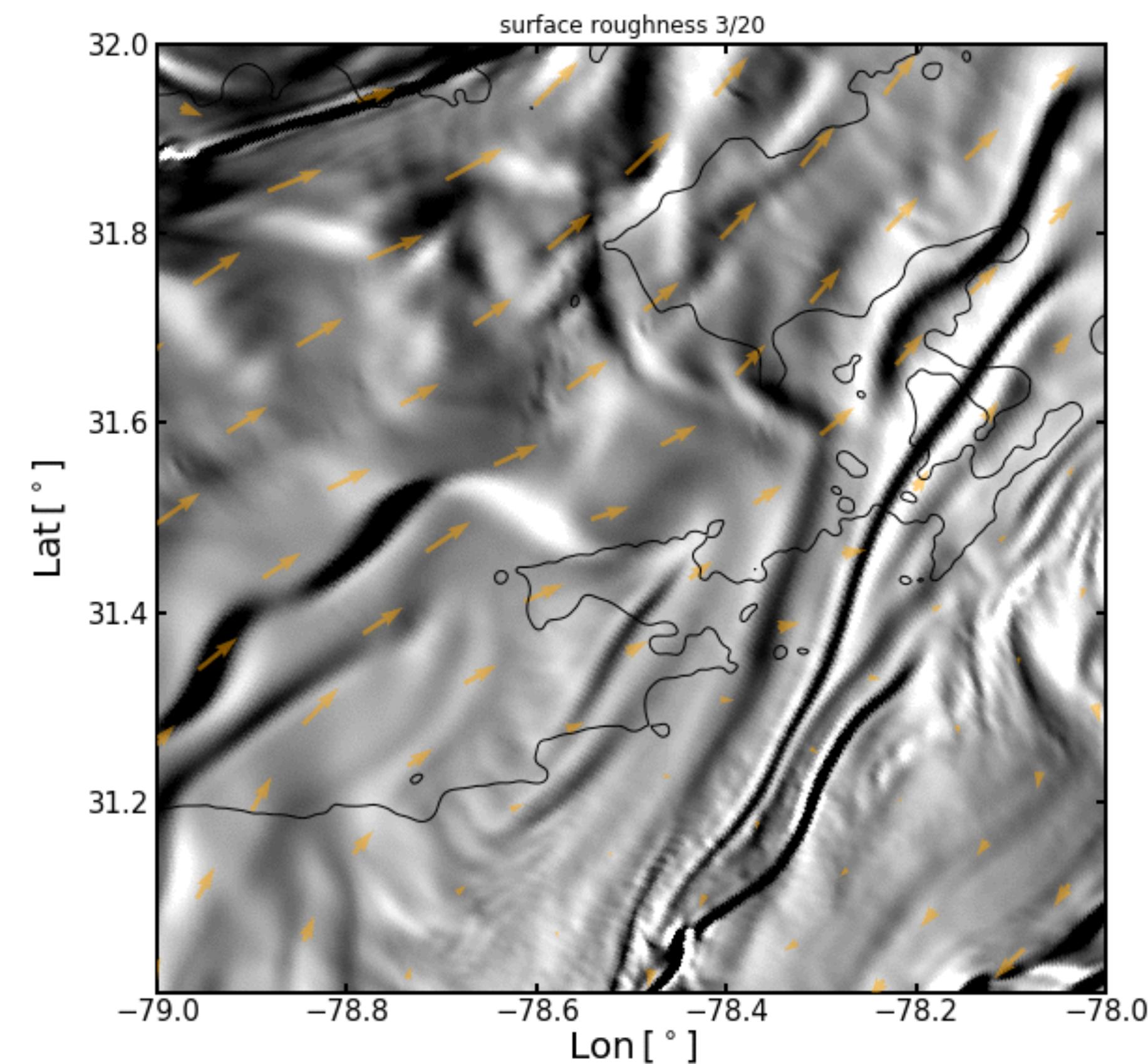
# Lee Waves in the Gulf Stream

- We can isolate patterns related to Lee Waves by looking at time-low passed vertical velocities below the thermocline:



# Lee Waves in the Gulf Stream

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# Comparison of Lee Waves with linear theory

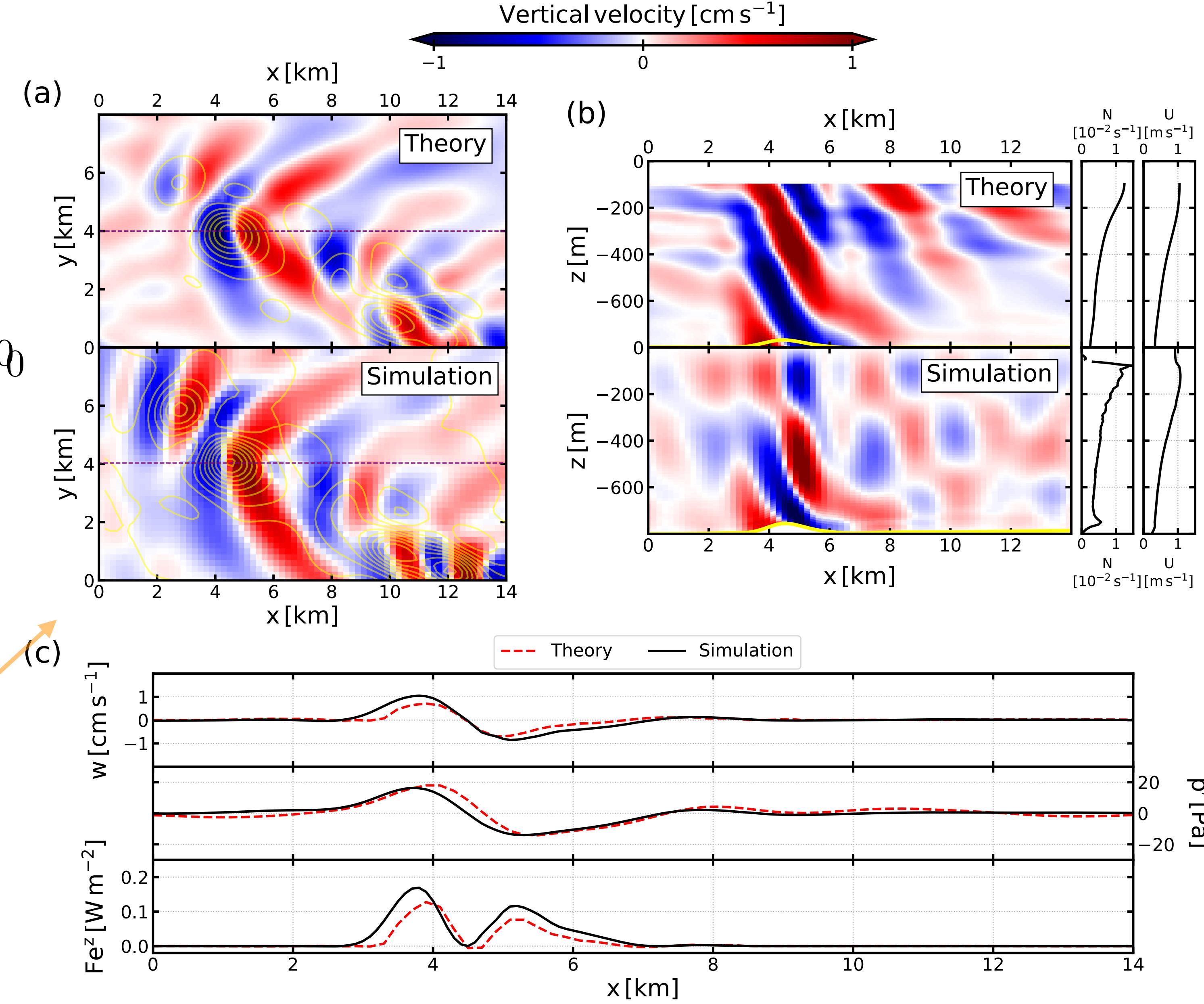
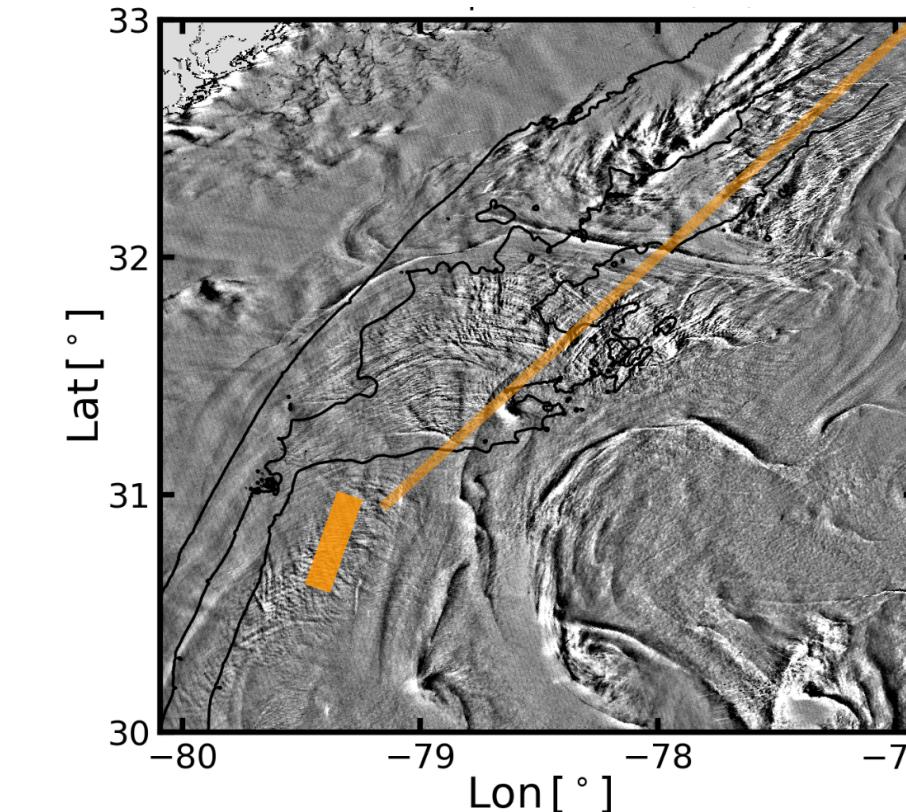
3D theoretical prediction of hydrostatic lee waves is obtained by numerically solving:

$$\partial_{zz} \tilde{\eta}(k, m, z) + n^2 \tilde{\eta}(k, m, z) = 0$$

under the WKBJ approximation with the dispersion relation:

$$n^2(k, m, z) = k^{-2} (k^2 + m^2) \left( \frac{N^2}{U^2} + \frac{\partial_{zz} U}{U} \right)$$

and radiation condition at the top of the domain and a Dirichlet condition at the bottom.



# Comparison of Lee Waves with linear theory

Condition for a hydrostatic flow:

$$\varepsilon = \frac{U}{NL} \ll 1 \rightarrow \text{Hydrostatic}$$

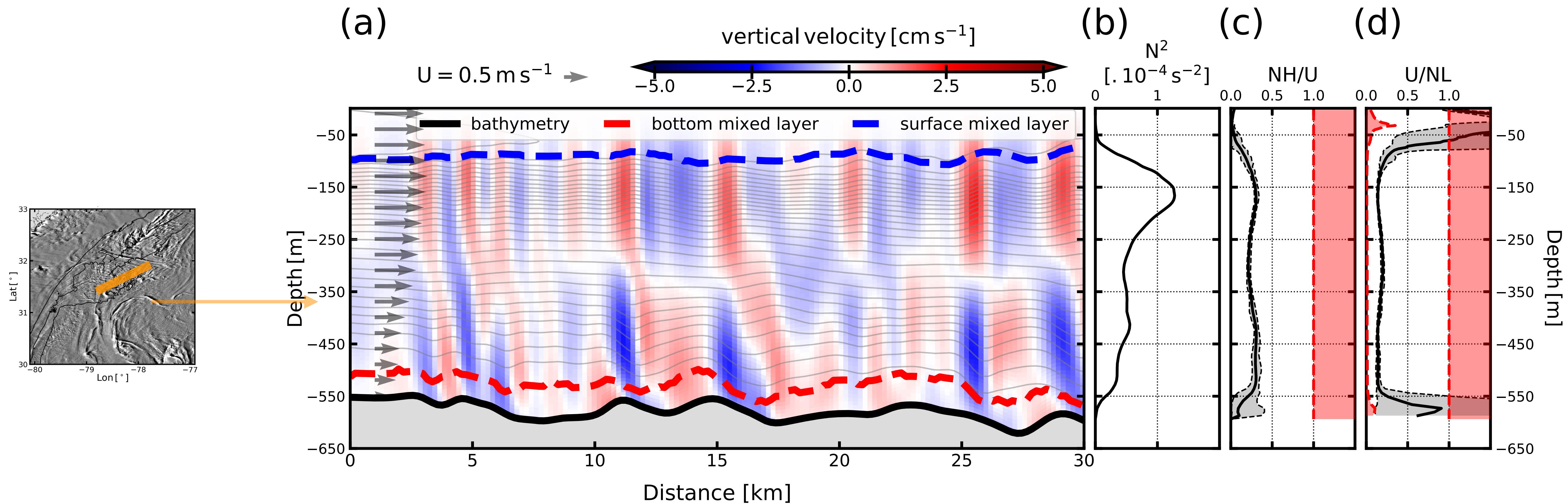
And for linear waves:

[Mayer and Fringer, 2017]

$$Fr_{\text{lee}} = \frac{NH}{U} = \frac{\text{vertical velocity within the lee wave}}{\text{group velocity of the lee wave}}$$

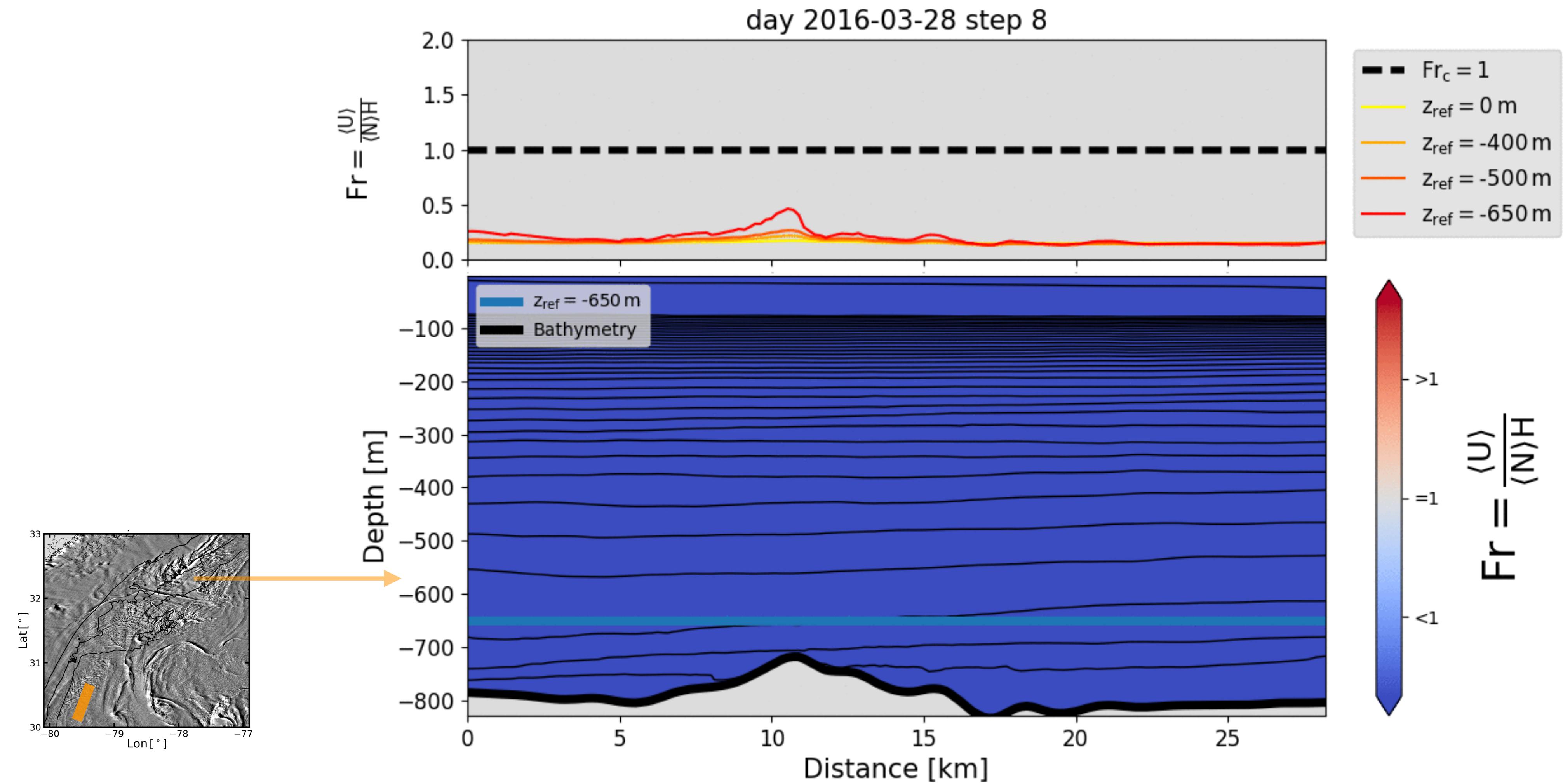
$Fr_{\text{lee}} < 1 \rightarrow \text{linear propagation of the waves}$

$Fr_{\text{lee}} \gtrsim 1 \rightarrow \text{non - linearity of the waves.}$



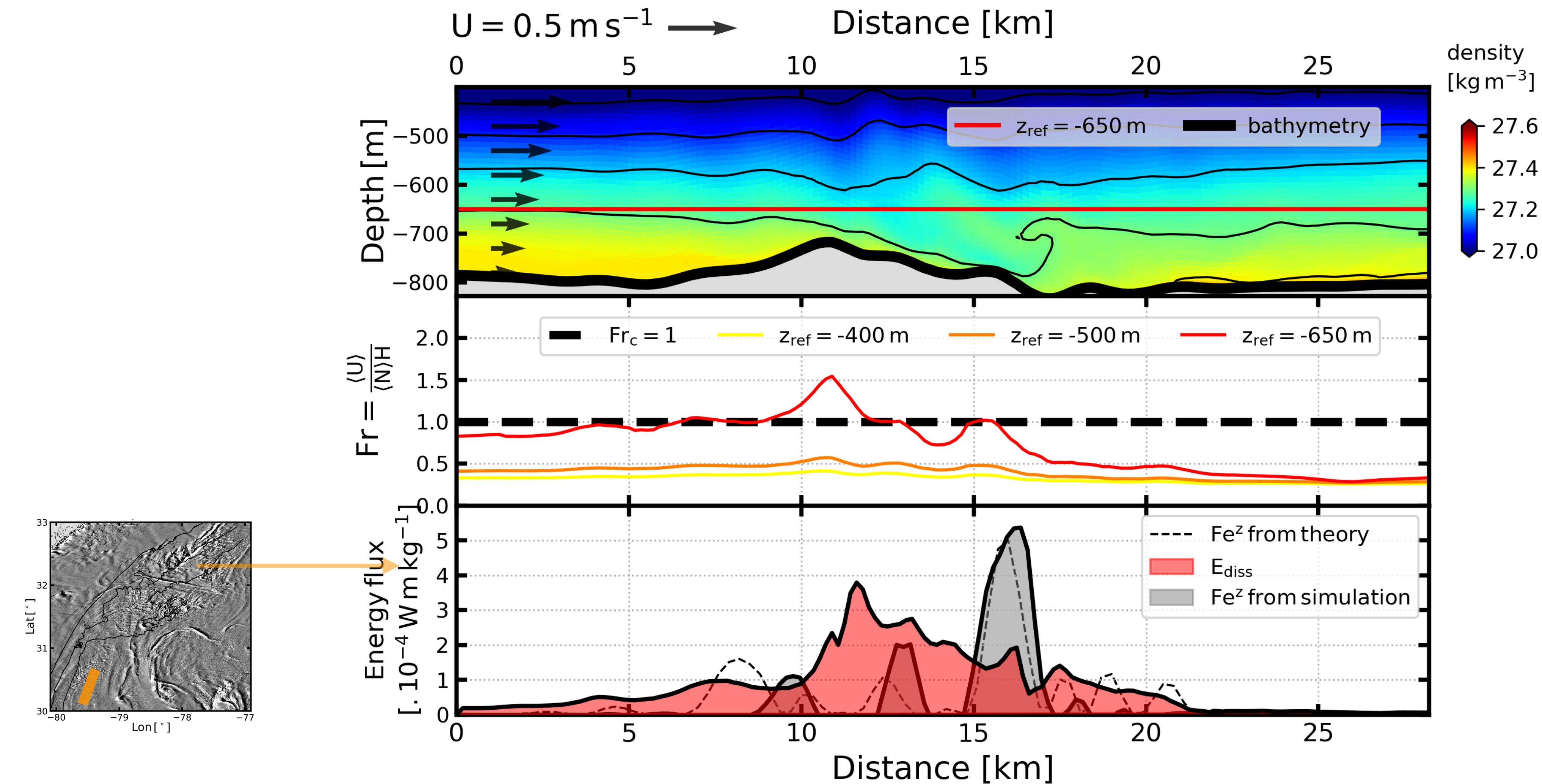
# Non-linearities at the bottom

Examples of hydraulic jumps:



# Non-linearities at the bottom

Examples of hydraulic jumps:



# Energy dissipation due to Lee Waves

A significant amount of energy ( $O(1)$  GW) is being dissipated in the interior of the fluid by the lee waves, including at locations where these waves may exhibit nonlinearities.

The lee wave energy flux ( $F_{\text{e}^z} = p'w$ ) computed using analytical formulation of Nikurashin and Ferrari (2011):

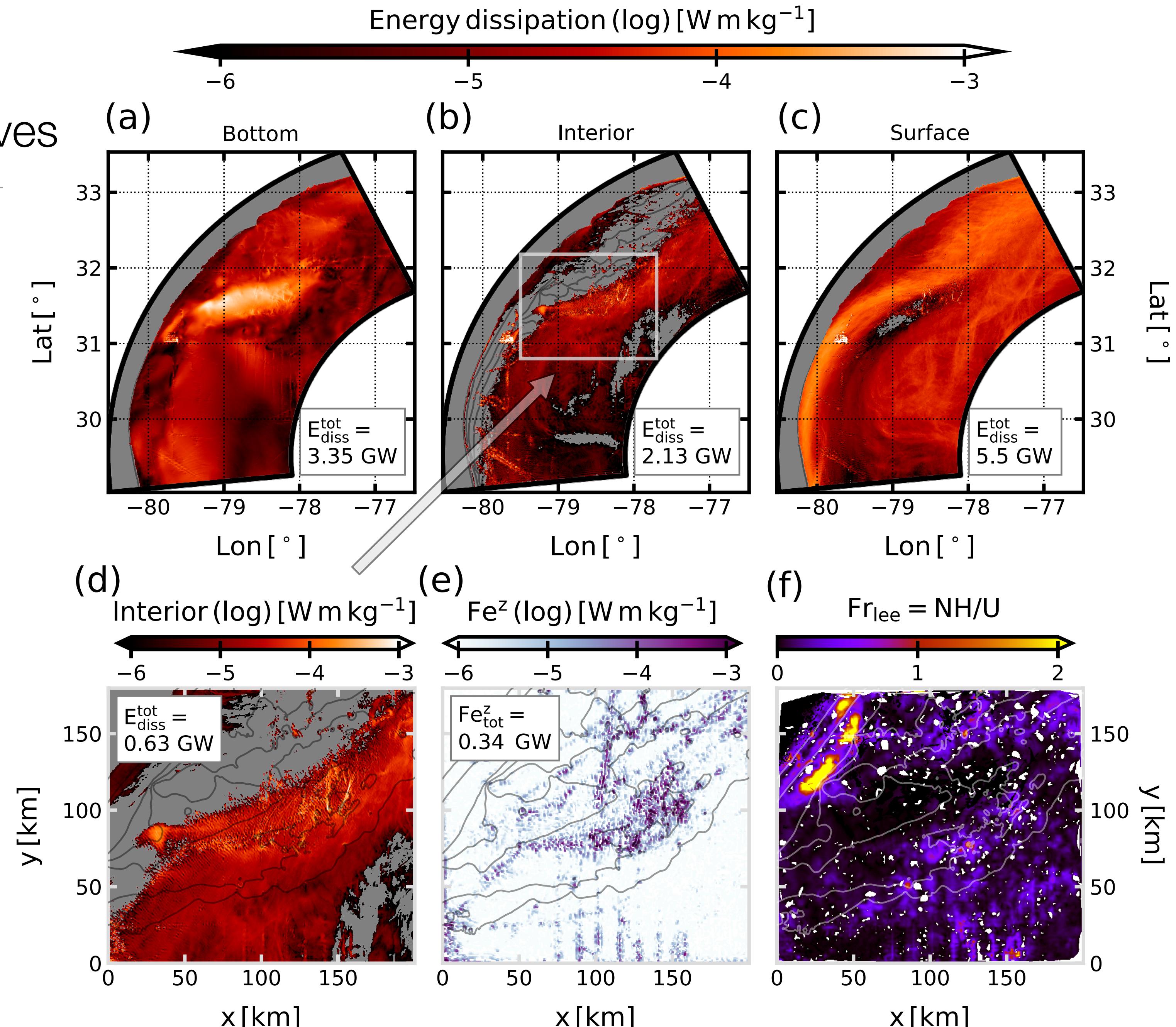
$$E = \frac{\rho_0 |\mathbf{U}|}{2\pi} \int_{|f|/|\mathbf{U}|}^{N/|\mathbf{U}|} P_*(k) \sqrt{N^2 - |\mathbf{U}|^2 k^2} \sqrt{|\mathbf{U}|^2 k^2 - f^2} dk,$$

yields a total conversion of  $O(0.3)$  GW.

The wave drag can be computed as:

$$\text{Form Drag} = \rho_0 \sqrt{(u'w)^2 + (v'w)^2}$$

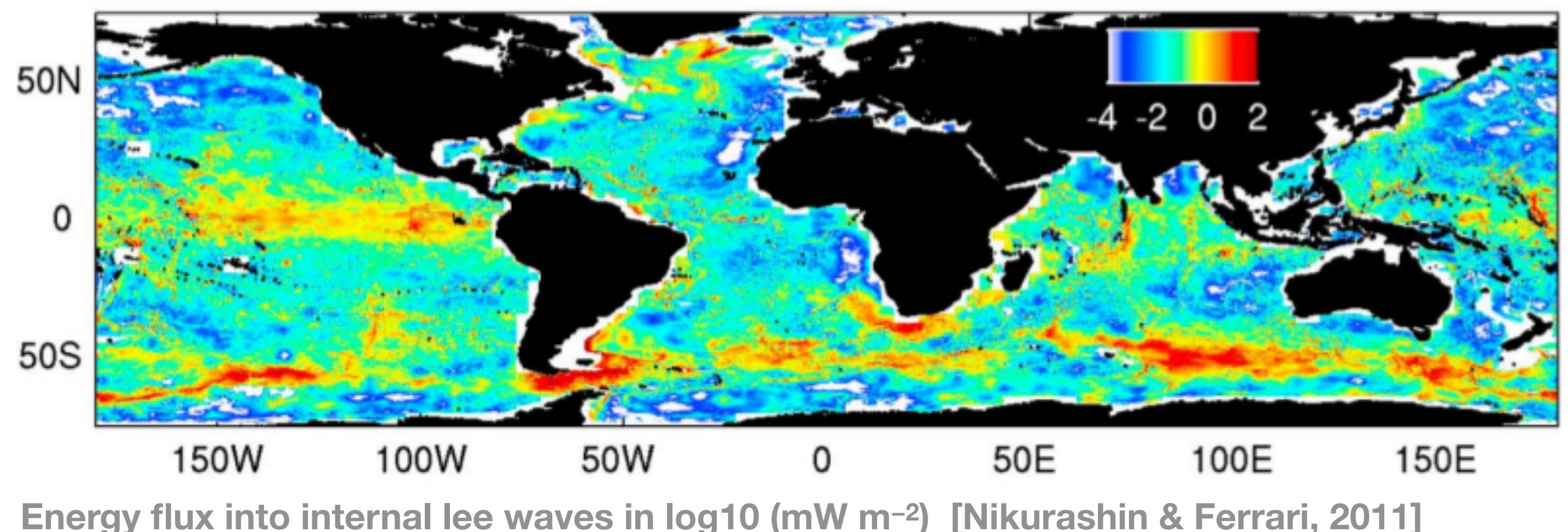
It amounts to  $O(1)$  GN and represents about 20% of the form drag exerted by the whole Charleston Bump.



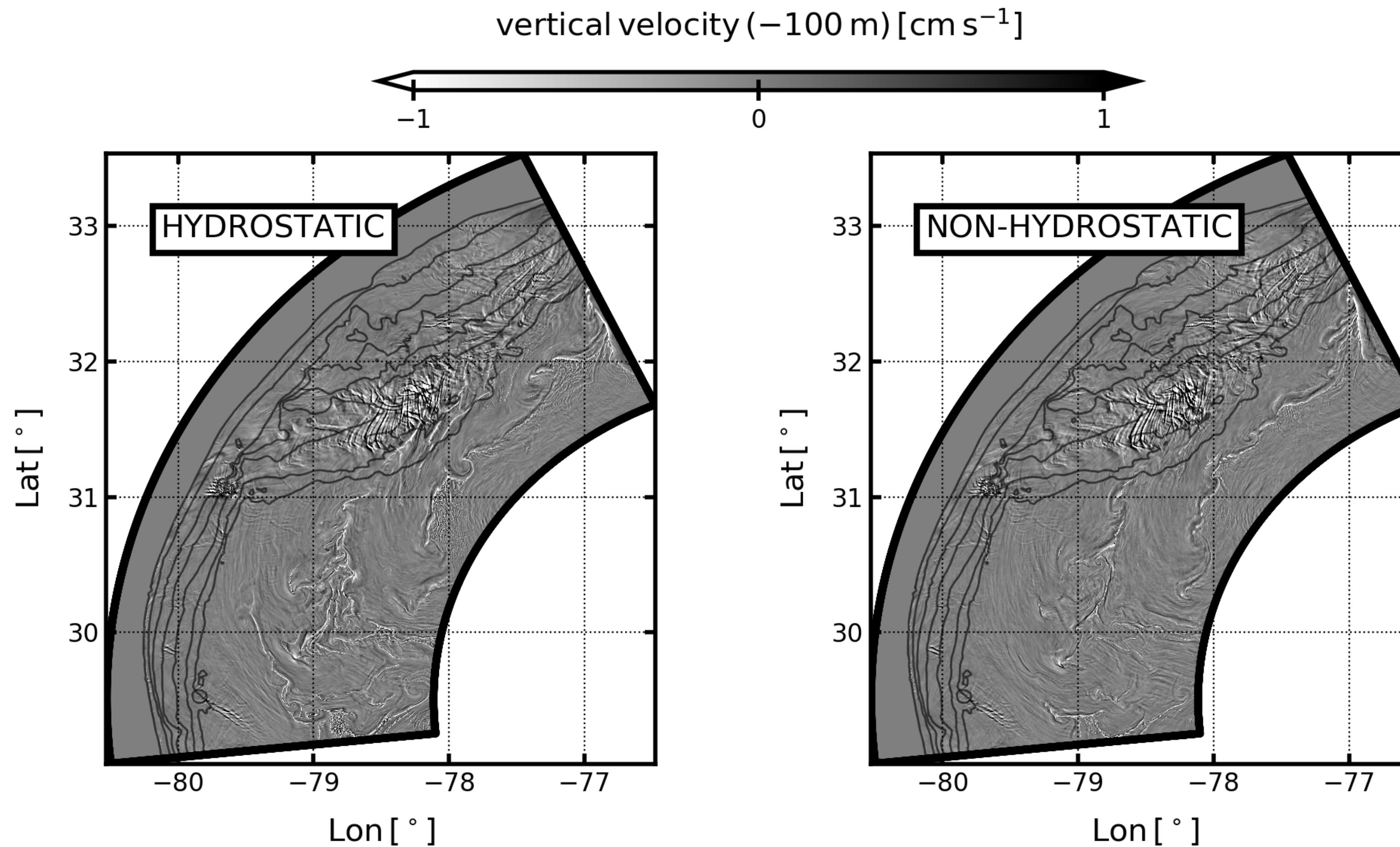
# Another Summary

1. Signature of lee waves are observed over the Gulf Stream in satellite sun-glitter images and reproduced using a realistic simulation.
2. Linear theory accurately reflects the generation properties of lee waves over most of the domain.
3. The breaking of lee waves above the Charleston Bump provides a significant mechanism for the dissipation of energy :  $O(1 \text{ GW})$

Total energy dissipated by lee waves: 0,2TW - 0.8TW

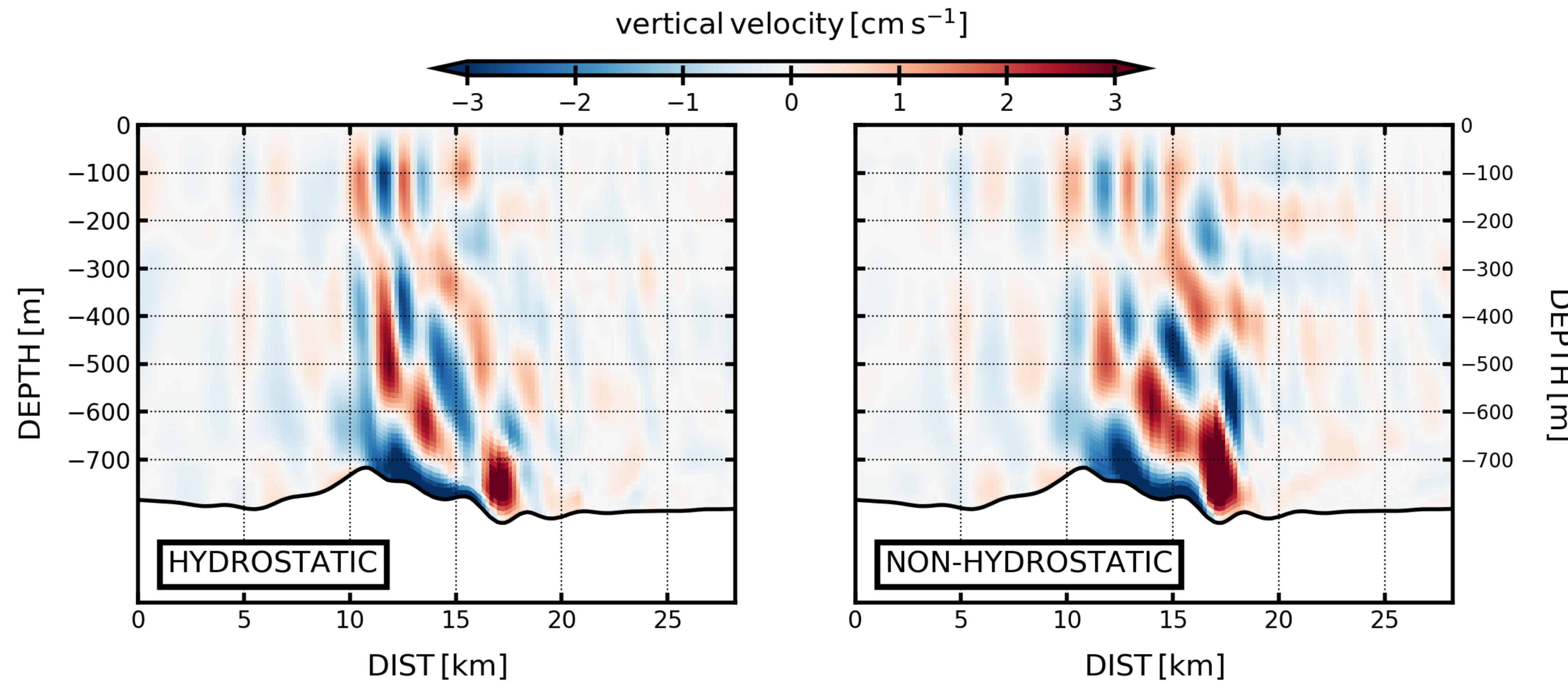


# Some extras: Differences with the non-hydrostatic code?

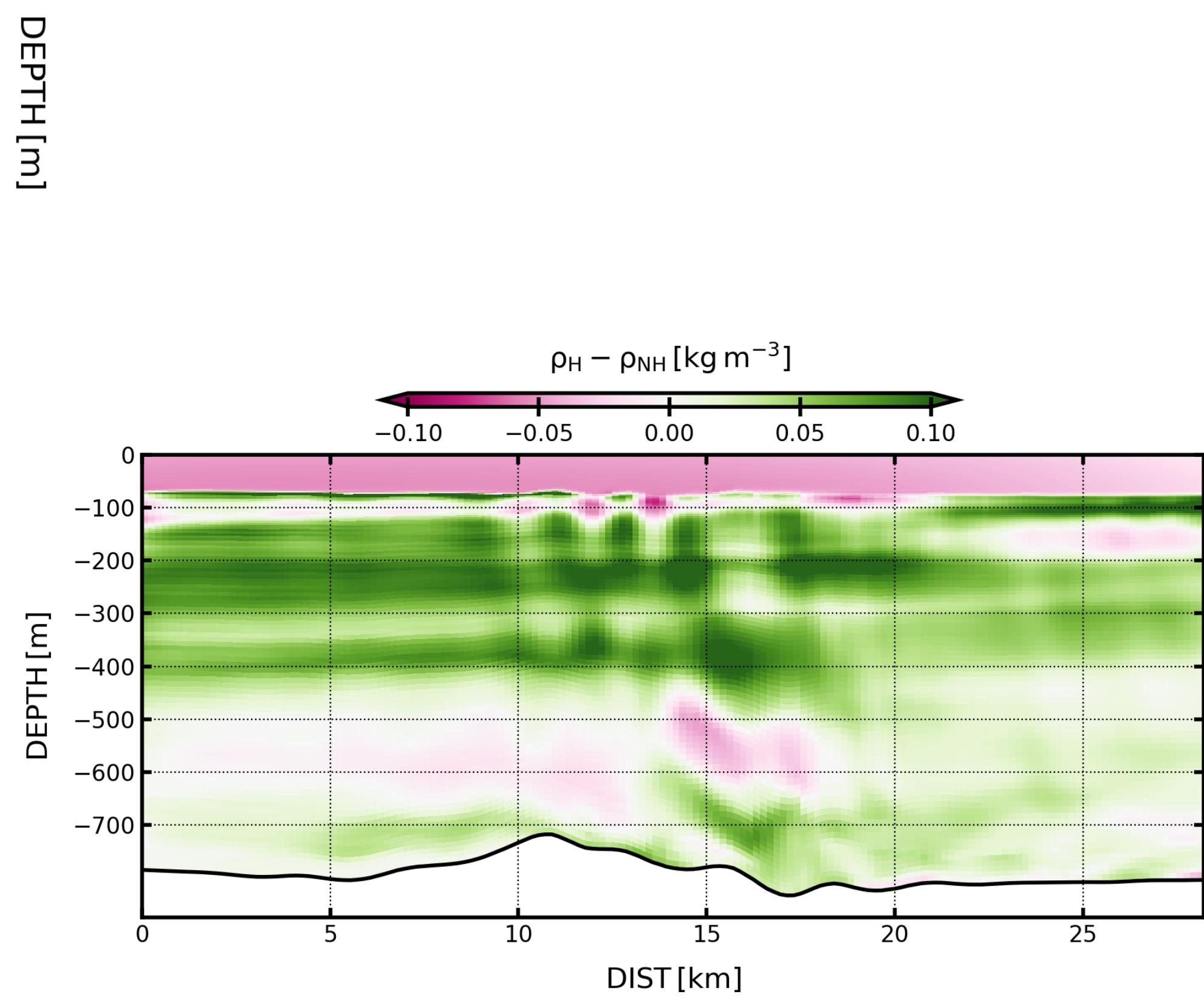
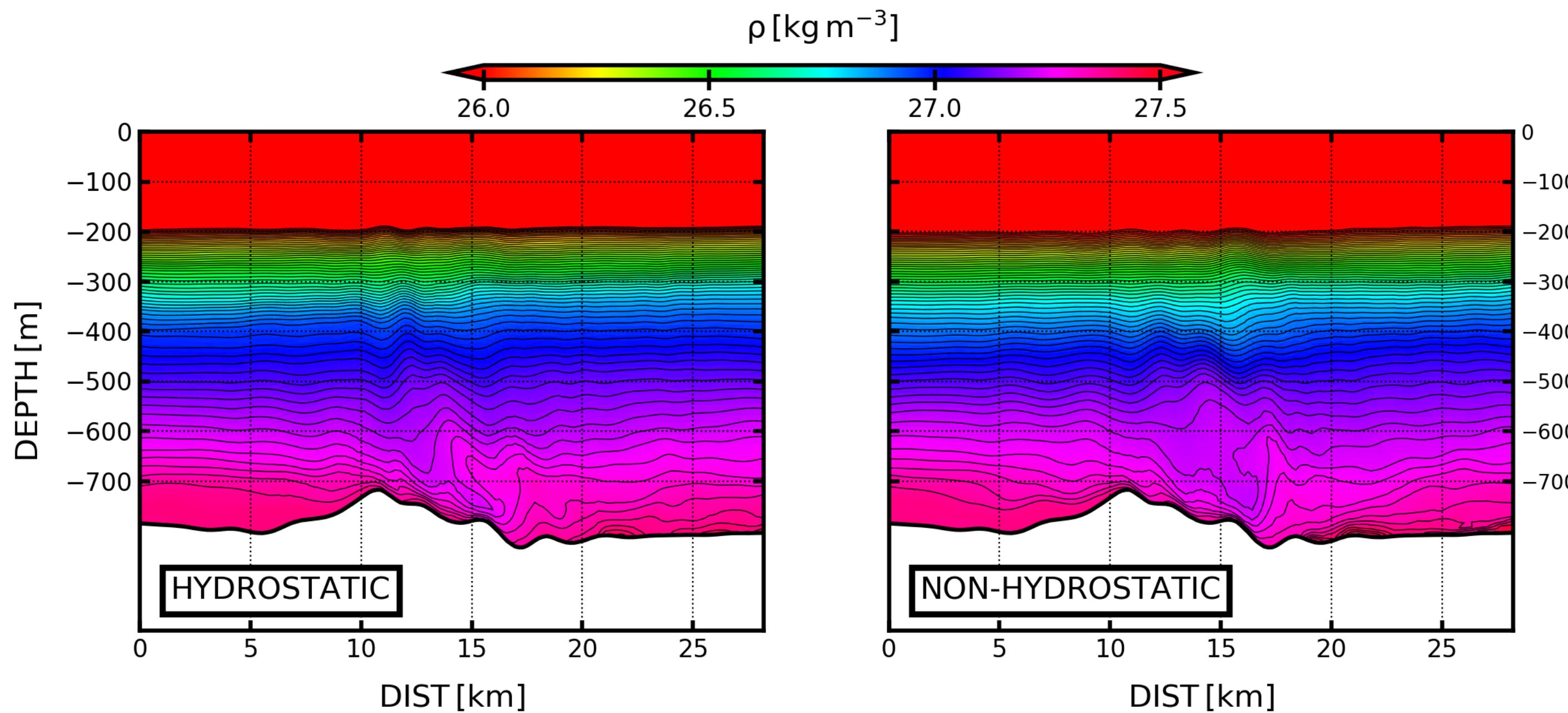


- Identical simulation with:
- # define NHMG
- # define NONRAD\_COR
- Identical time-step
- Overhead = 215 %

# Some extras: Differences with the non-hydrostatic code?



# Some extras: Differences with the non-hydrostatic code?

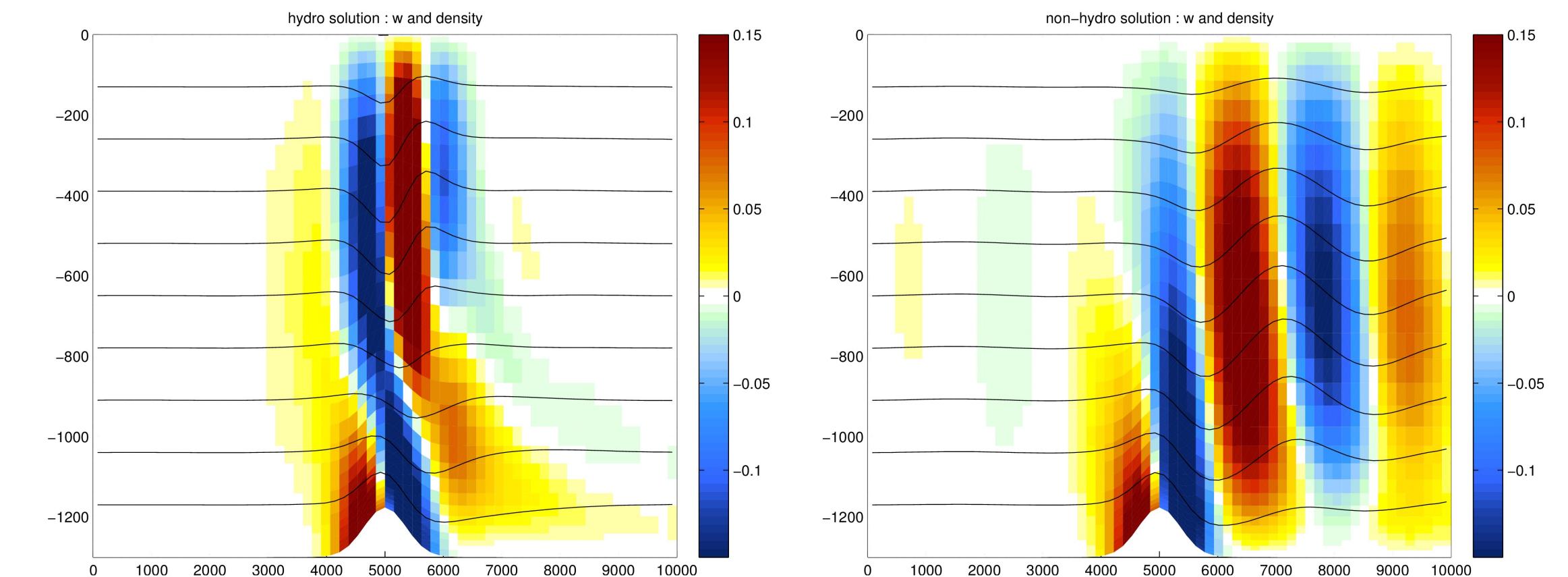
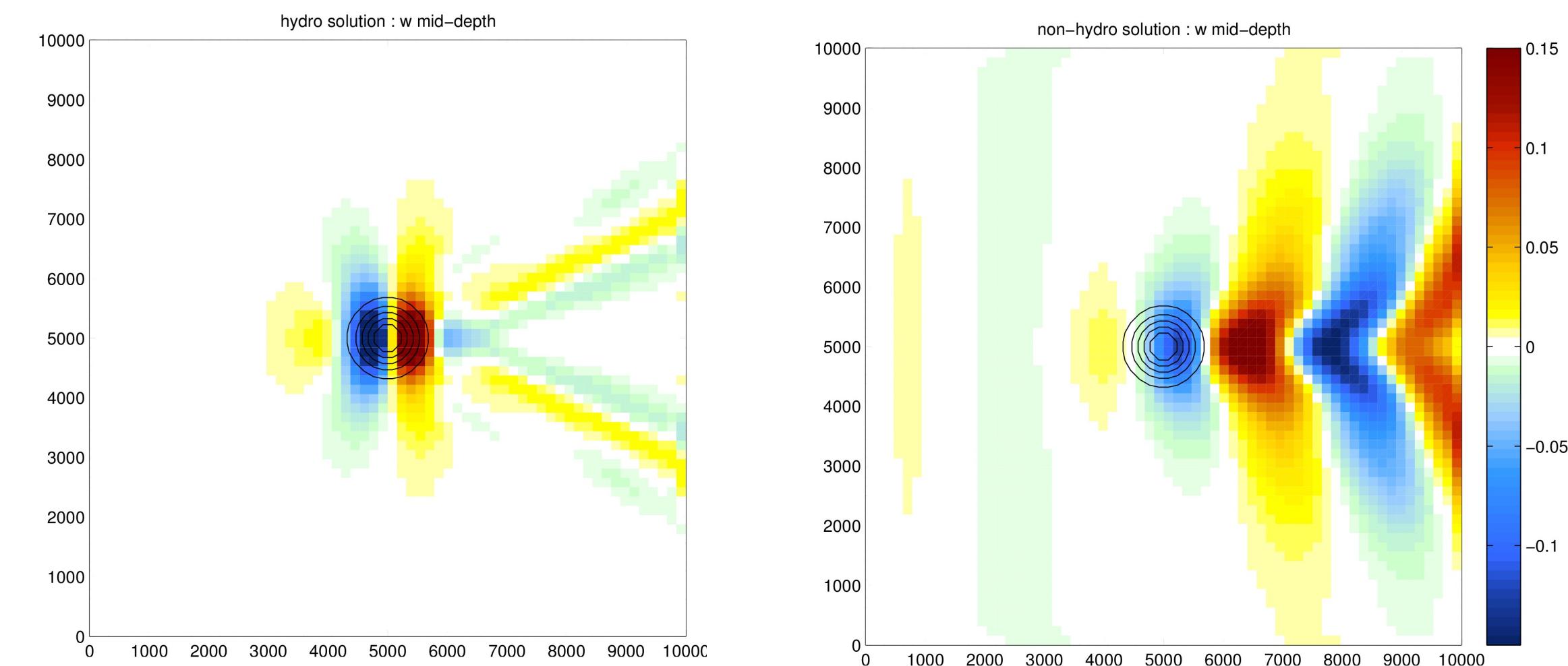


Thanks for your attention

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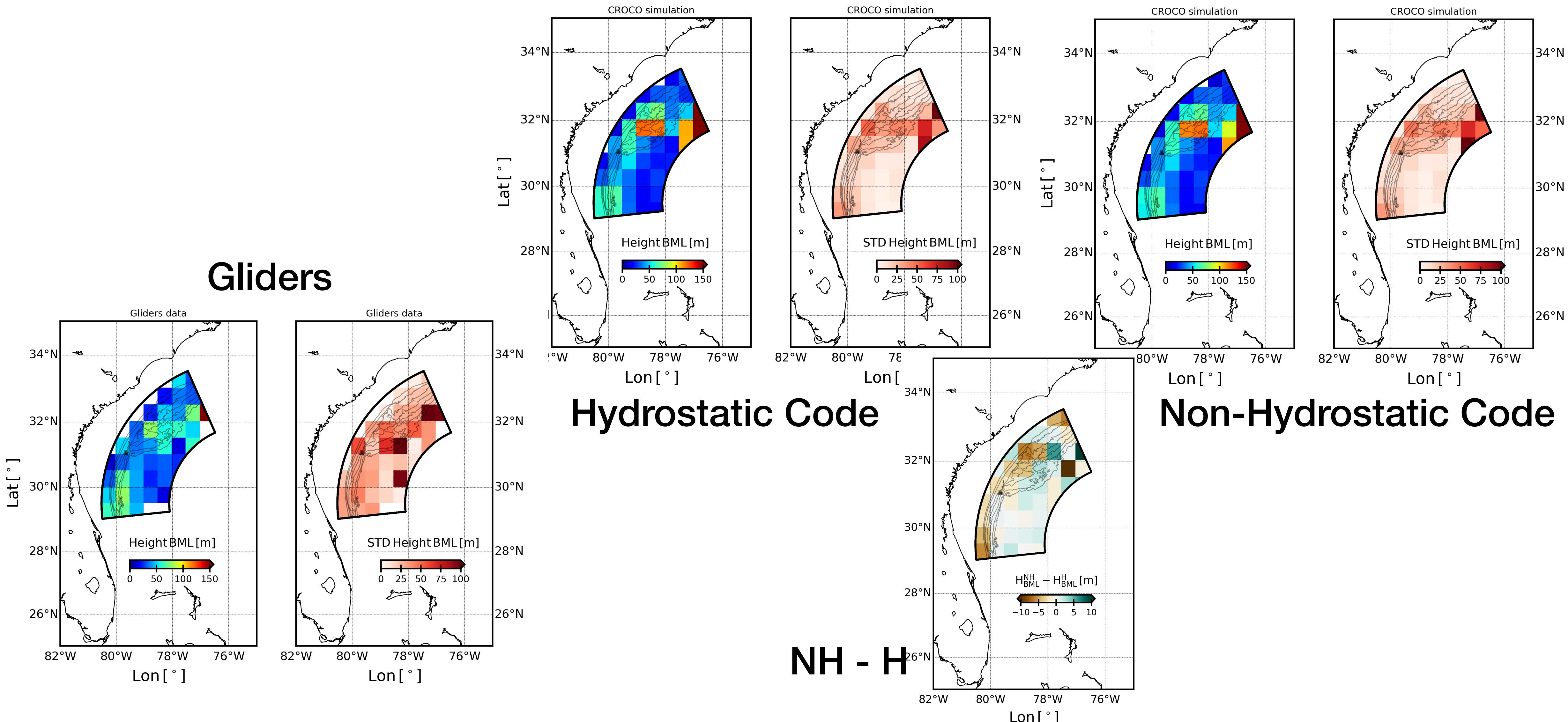
# Some extras: Differences with the non-hydrostatic code?

- With  $U \sim 1.2 \text{ m s}^{-1}$  and  $N \sim 3e-3 \text{ s}^{-1}$ ,
- $U/N \sim 400 \text{ m}$  and  $L \sim 500 \text{ m}$

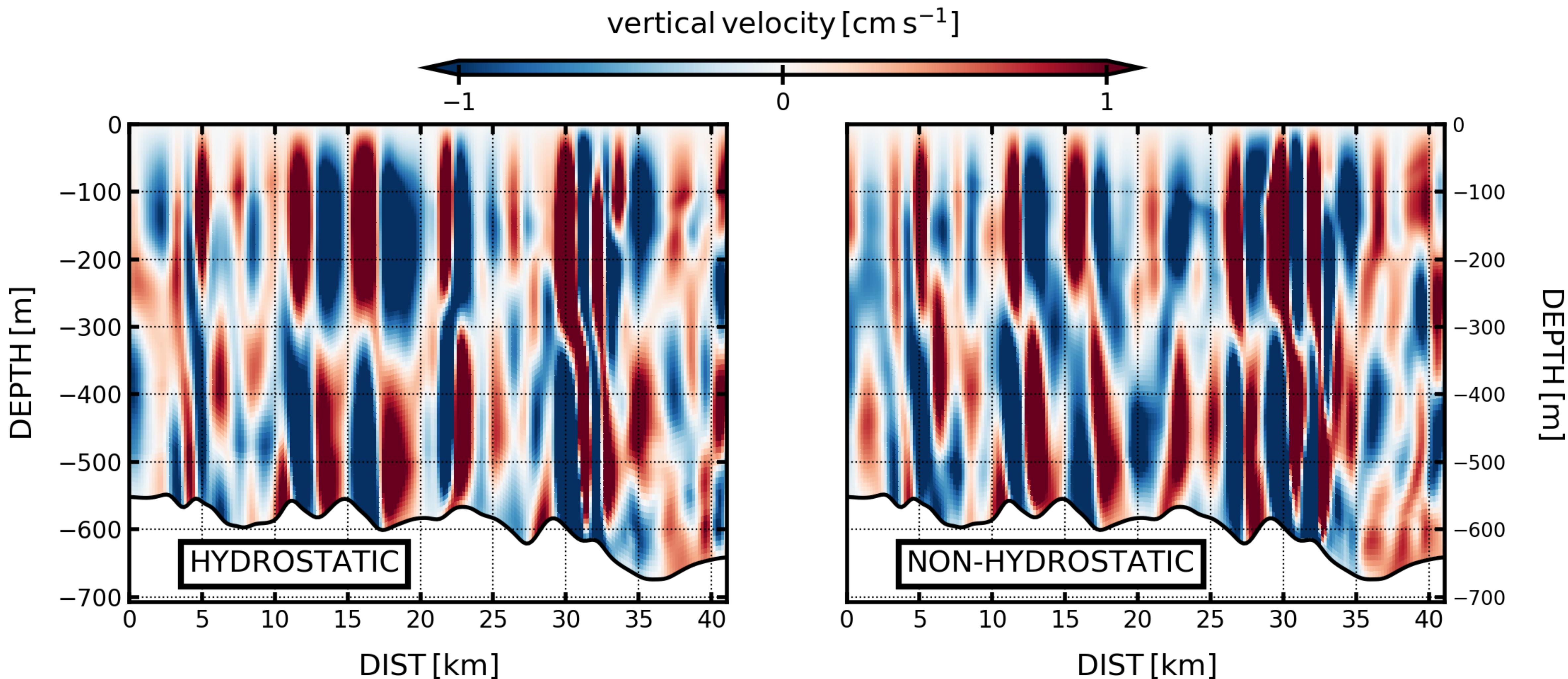


From N. Ducousso

# Some extras: Differences with the non-hydrostatic code?

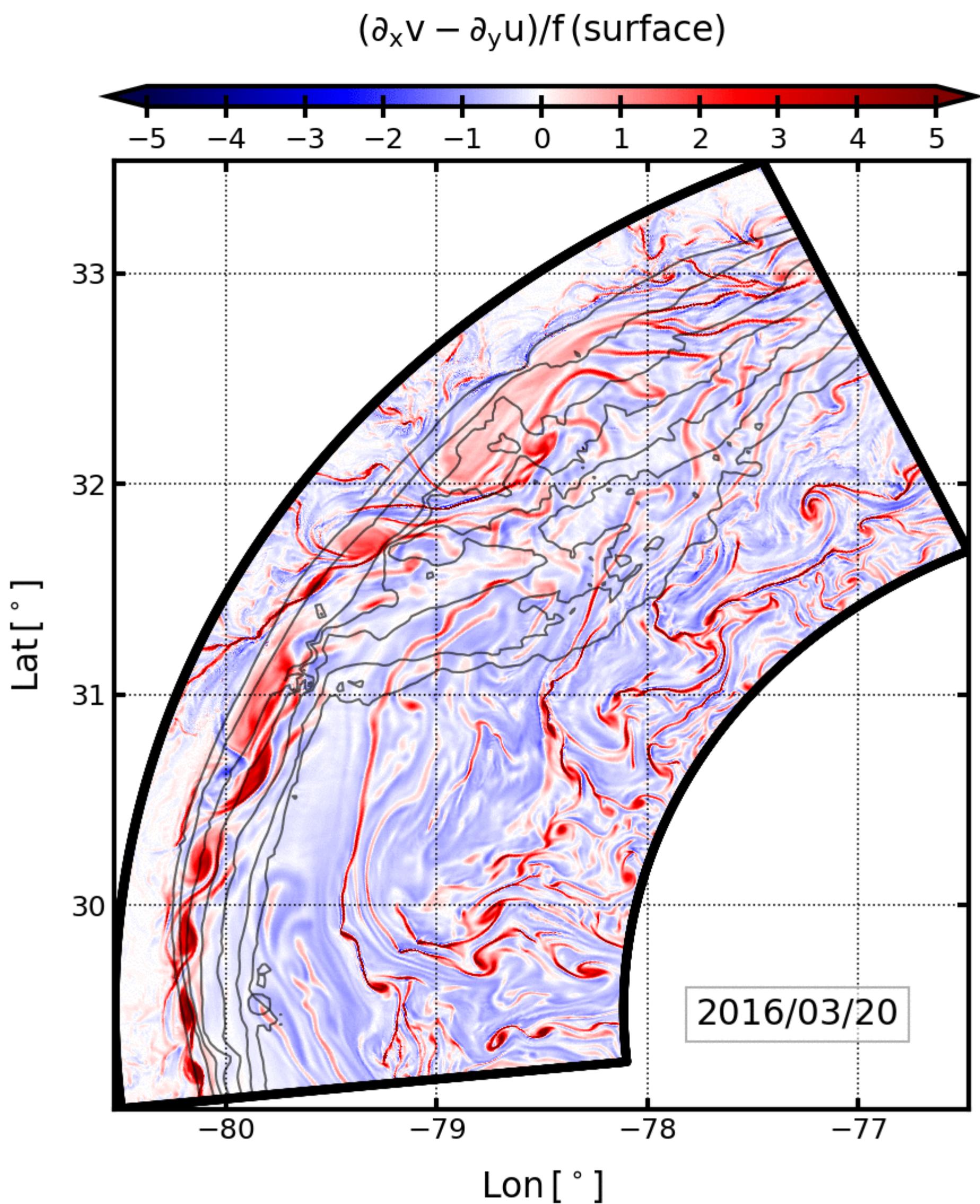
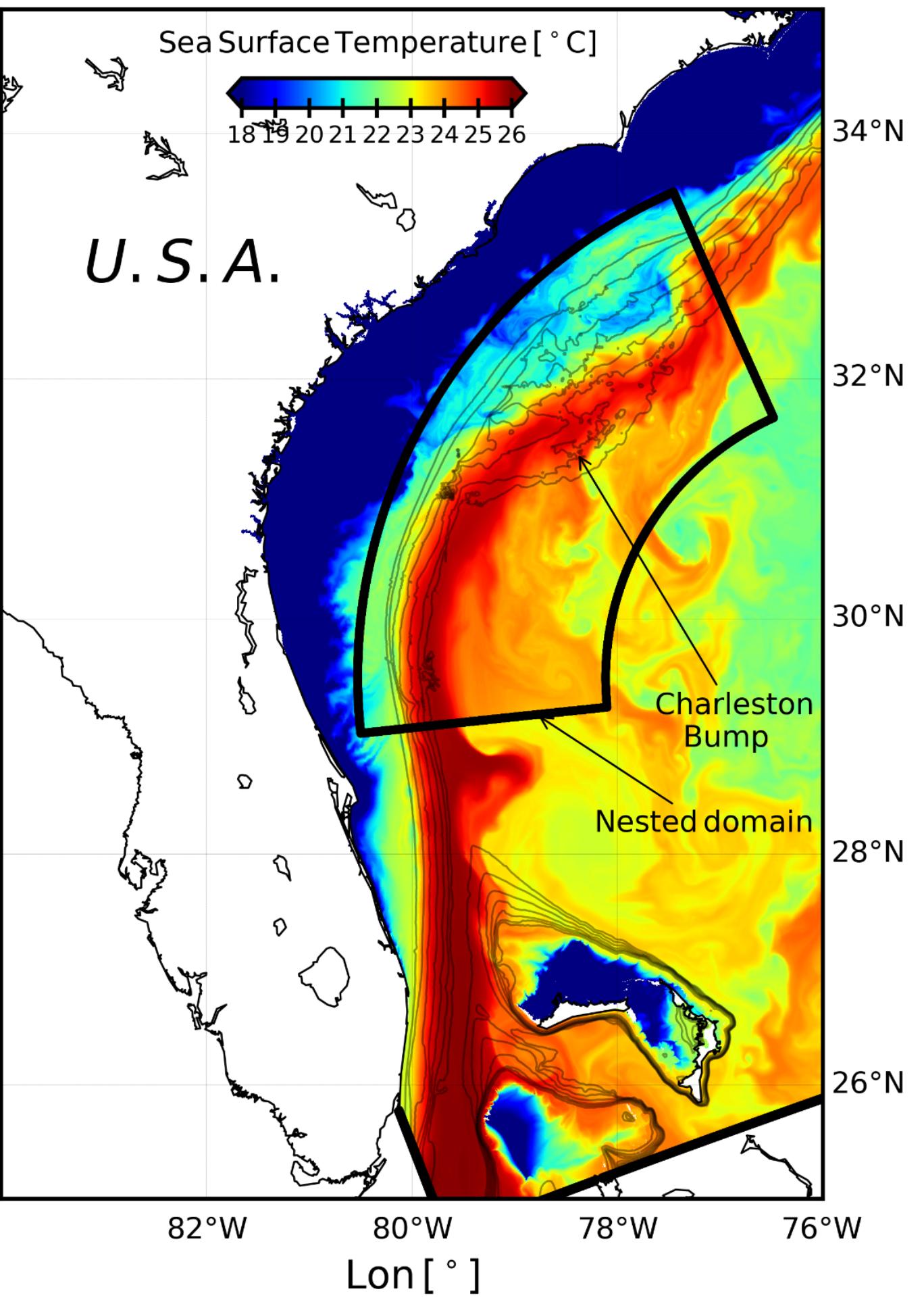


# Some extras: Differences with the non-hydrostatic code?



# Simulation of the Gulf Stream

- We performed a ROMS/CROCO nest  **$dx = 200 \text{ m}$** , **128 lev.**
- Climatological forcings (monthly winds, no tides)



# Impact for biology and fisheries

- The frontal eddies have strong implications for the biological production in the South Atlantic Bight. The upwelling pumps nutrient-rich bottom waters toward the surface, resulting in high levels of ocean productivity.
- The Bump provides a unique habitat for pelagic and demersal fishes, nursery habitats for early life history stages, and a “stepping stone” in the migratory route of several highly migratory pelagic fishes.
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