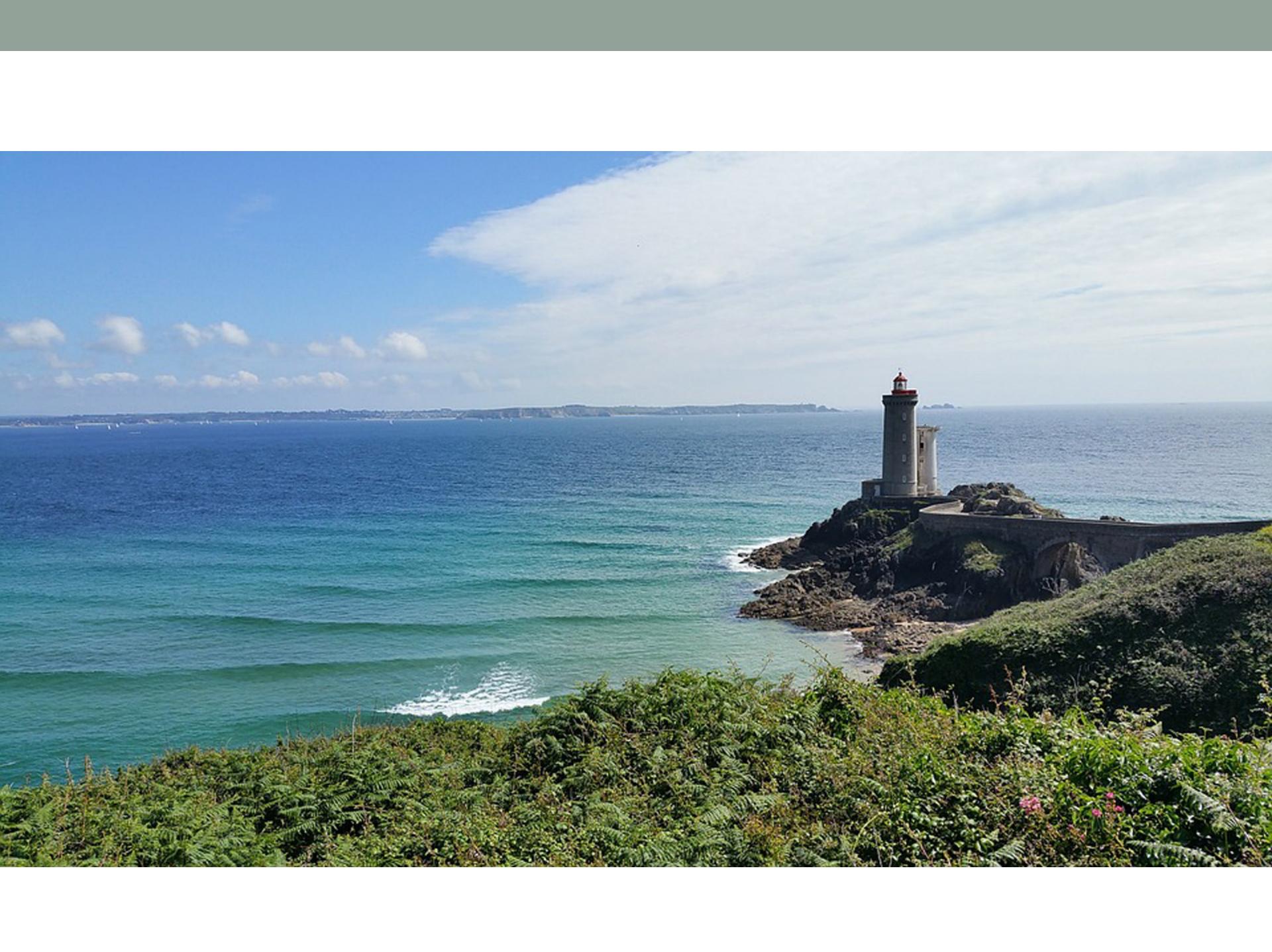


FLUIDS 2

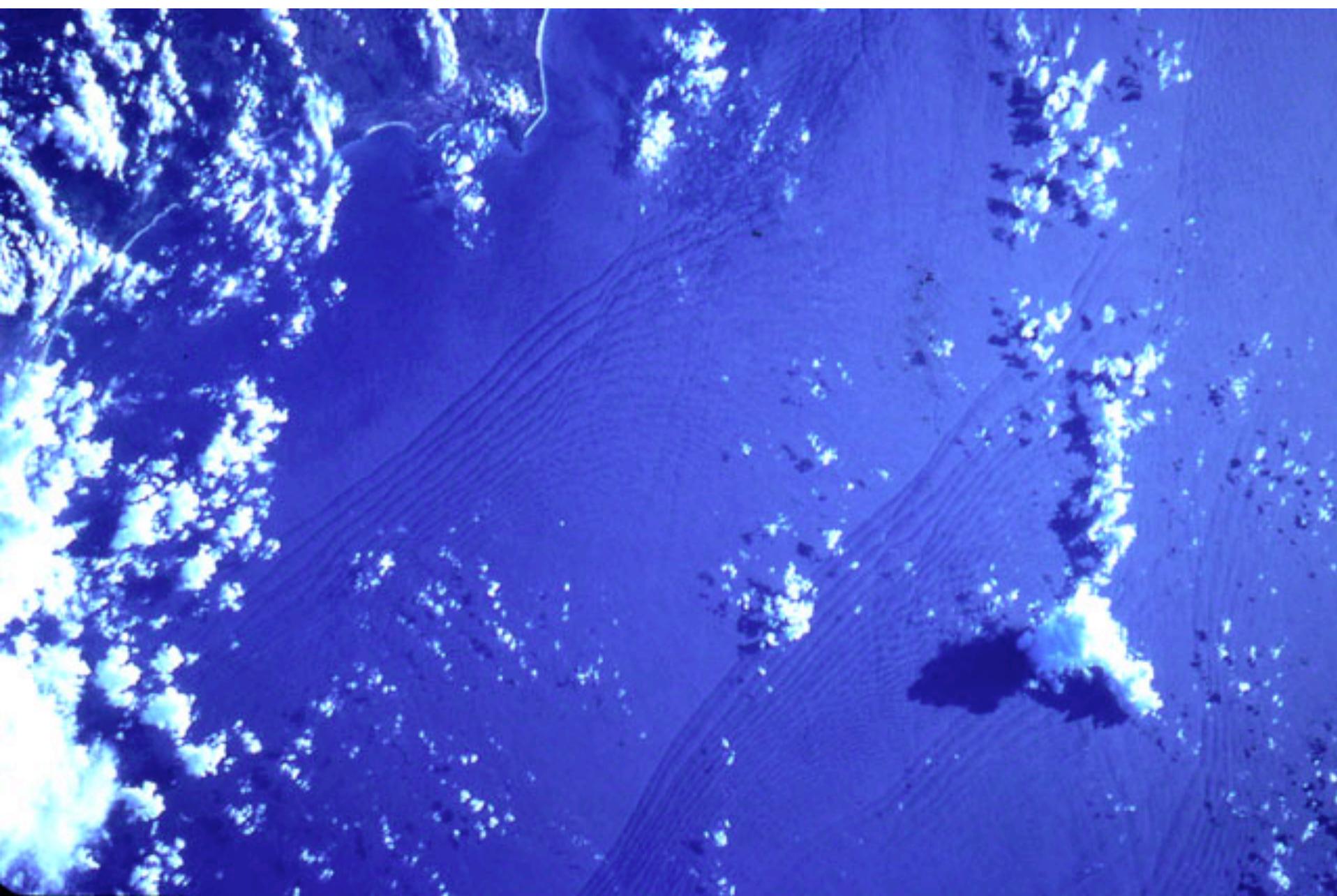
Jonathan GULA
gula@univ-brest.fr



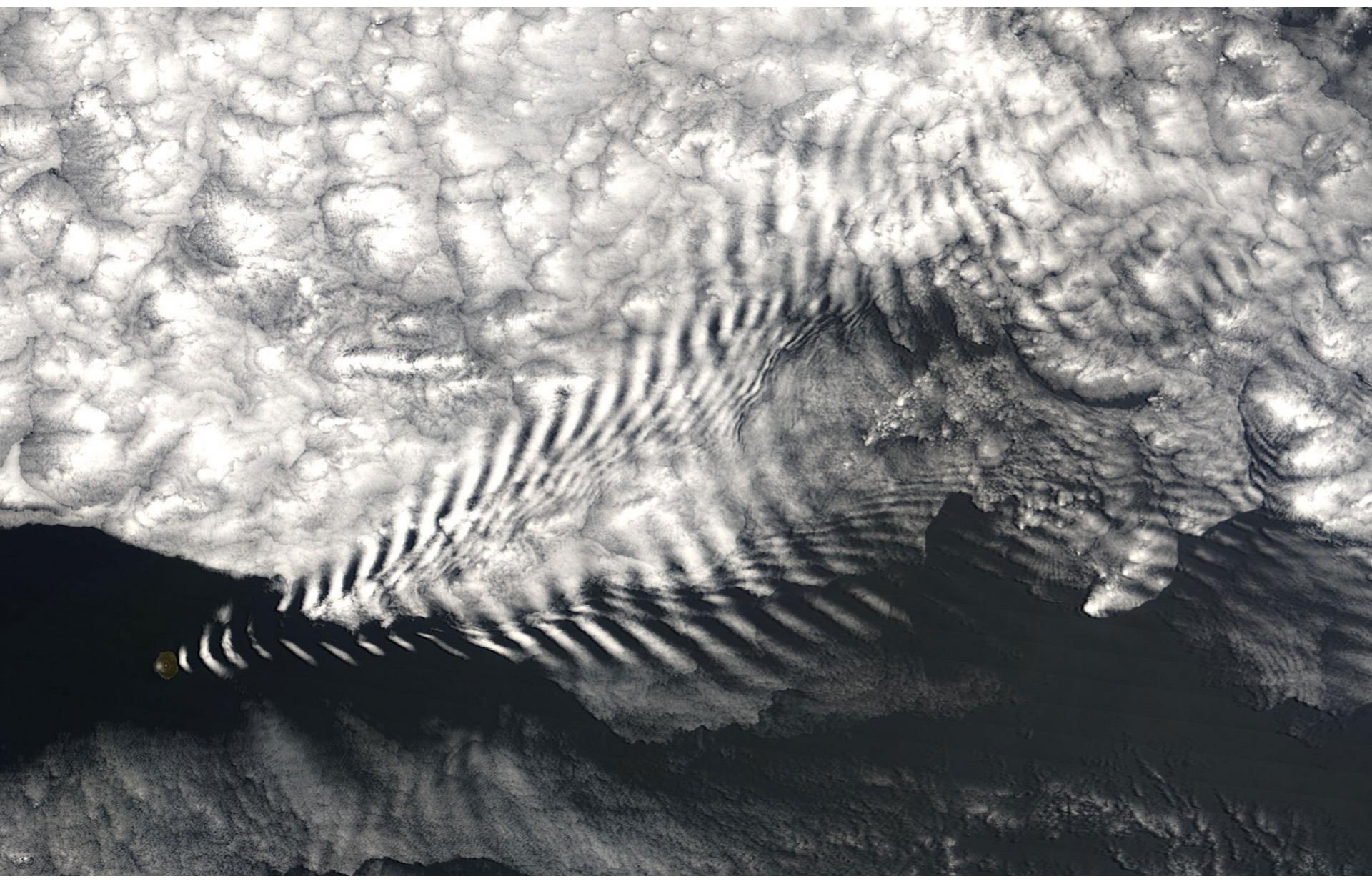






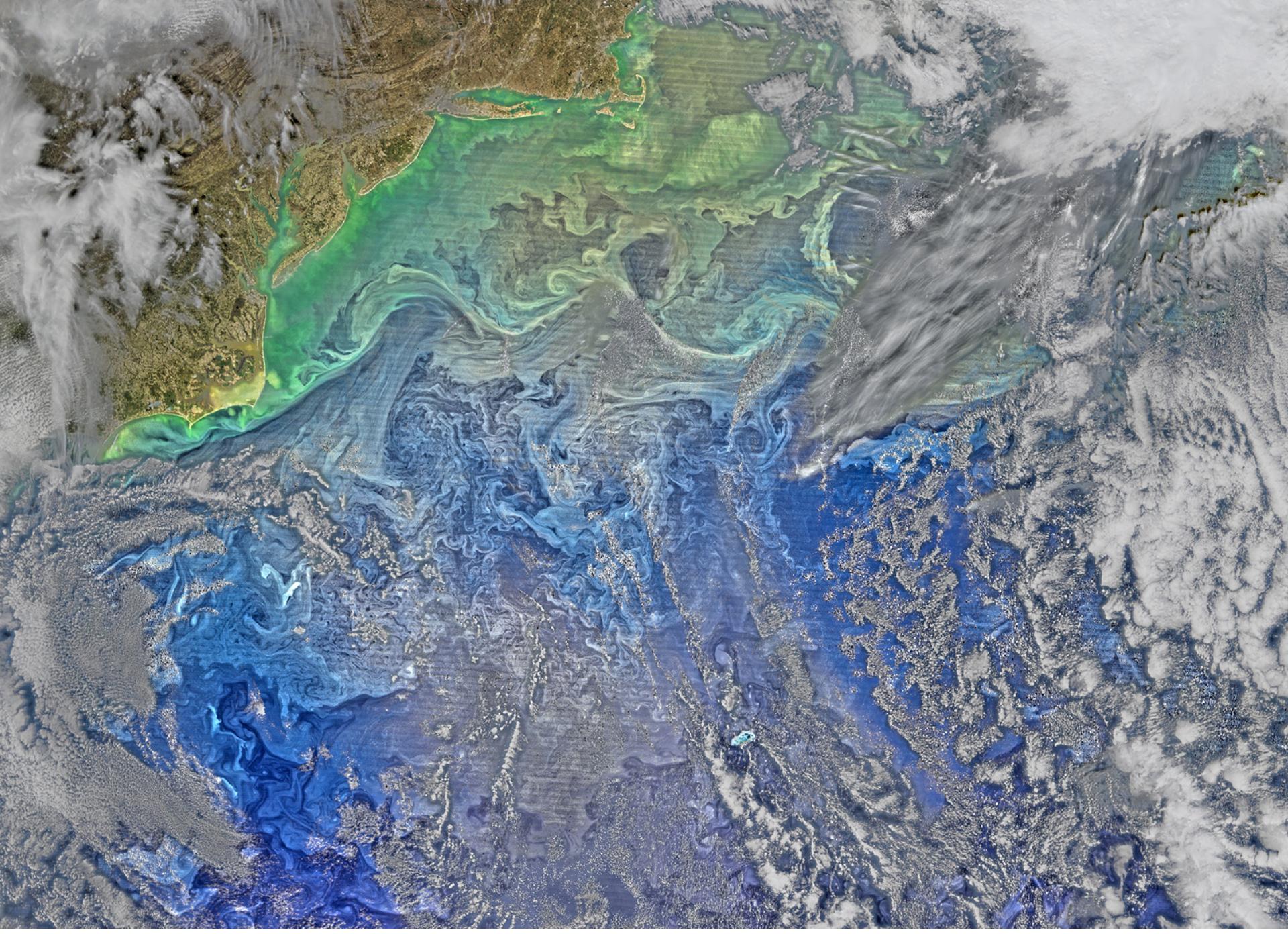


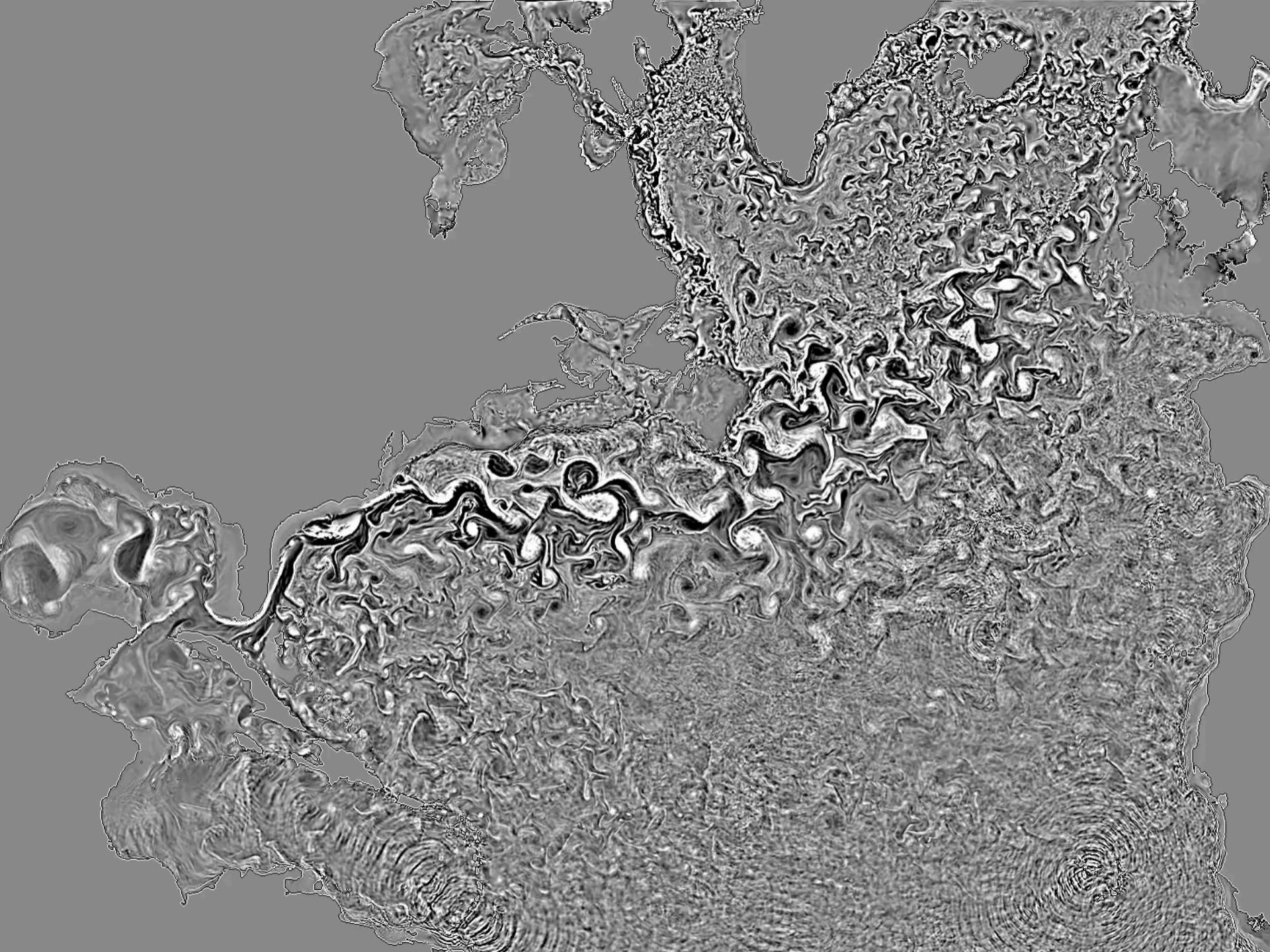






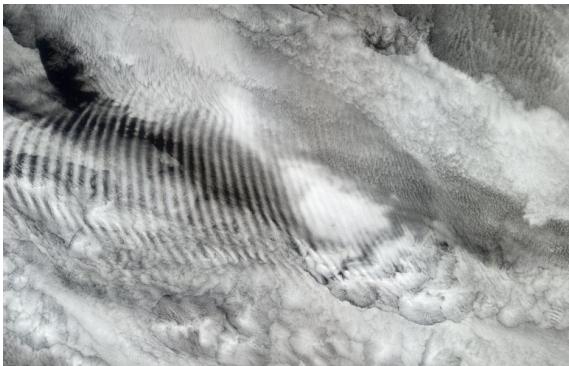
©morissoftgarden



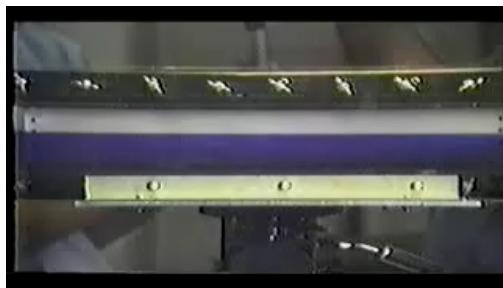


FLUIDS 2

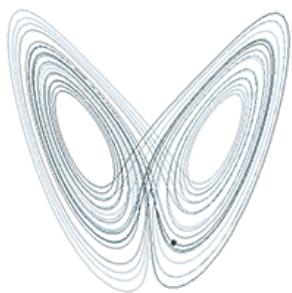
1. Waves



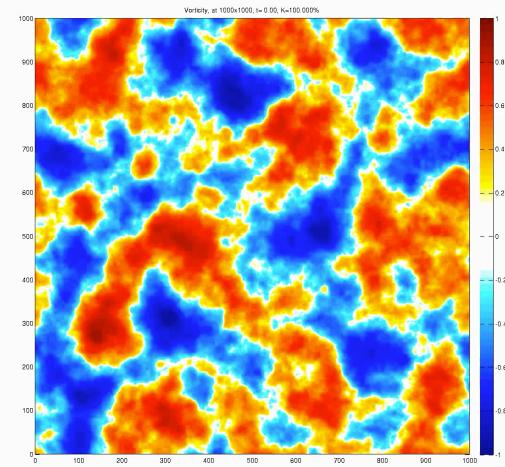
2. Instabilities



3. Chaos



4. Turbulence



I. WAVES

Jonathan GULA
gula@univ-brest.fr

I. WAVES

I.1. Introduction

I.2. General properties of Waves

I.3. Different type of ocean waves

I.3.1 Surface Gravity Waves

I.3.2 Internal Waves

I.3.3 Acoustic Waves

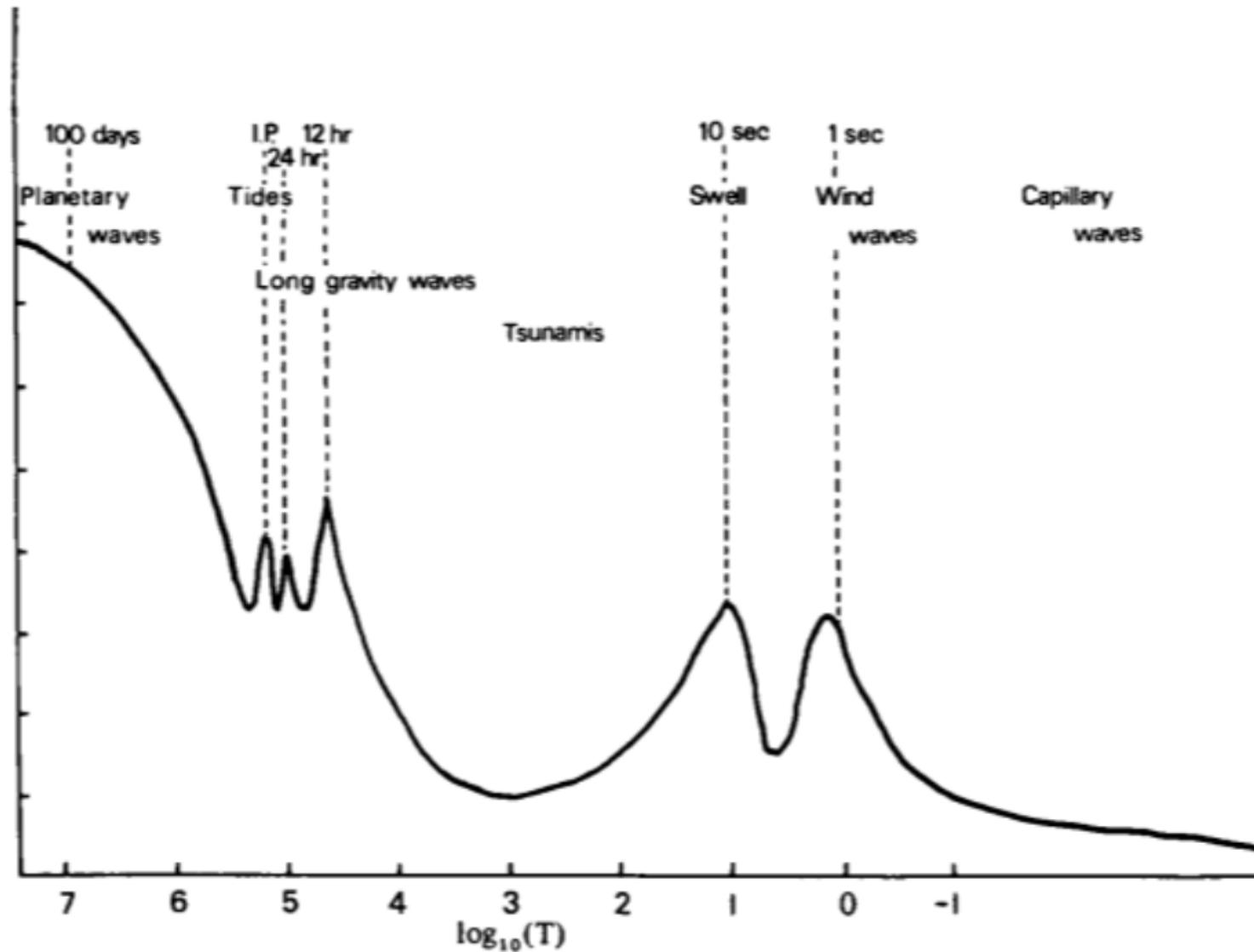
I.4. Ray Theory

Bibliography

- Whitham (1974) : *Linear and nonlinear waves*
- Leblond-Mysak (1977) : *Waves in the ocean*
-

I.1. Introduction

Ocean Waves



Schematic energy spectrum of ocean variability [Leblond & Mysak]

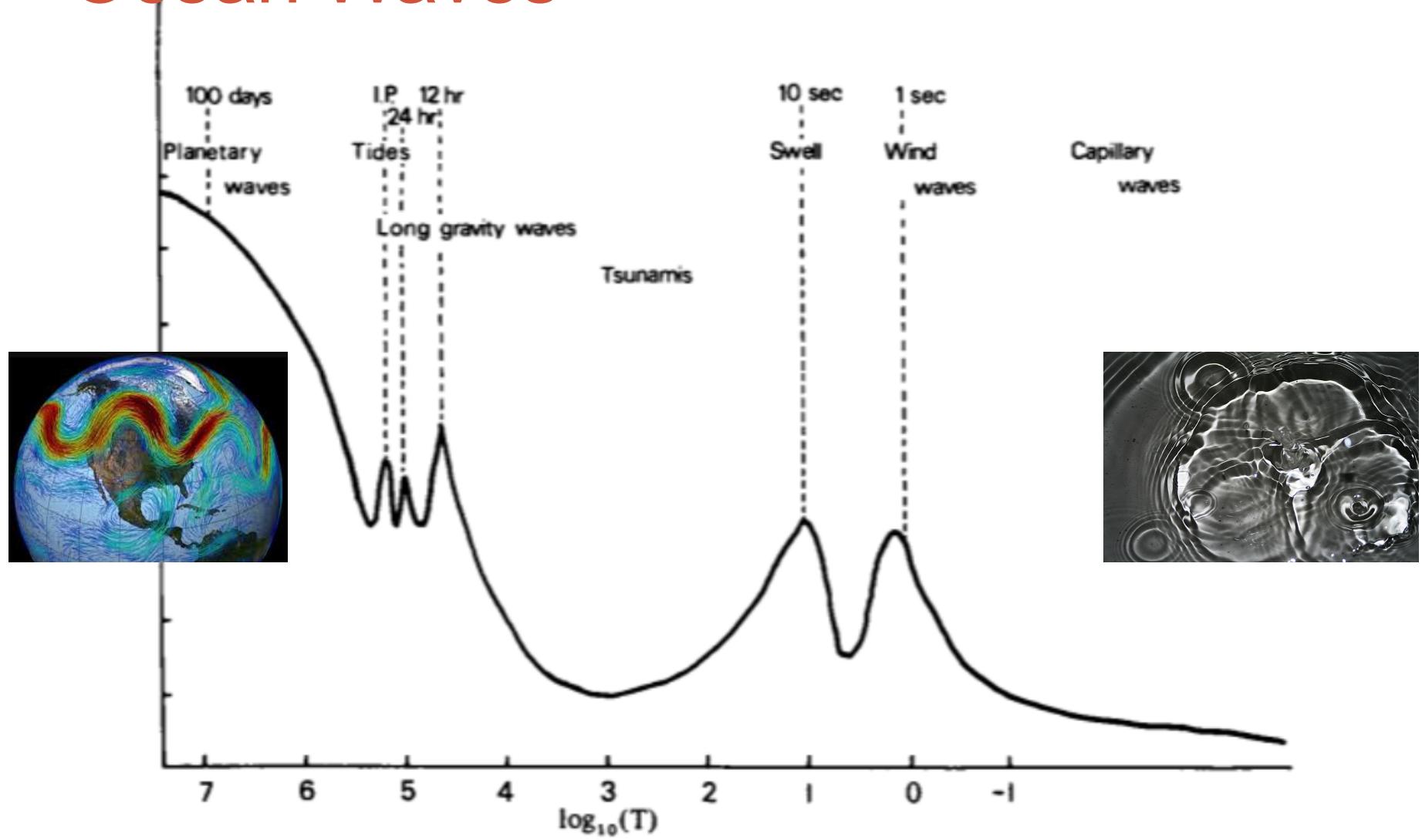
Ocean Waves

Different type of waves are classified on the basis of:

- Disturbing force
- Restoring force
- Wavelength
- Free wave Vs forced wave

I.1. Introduction

Ocean Waves



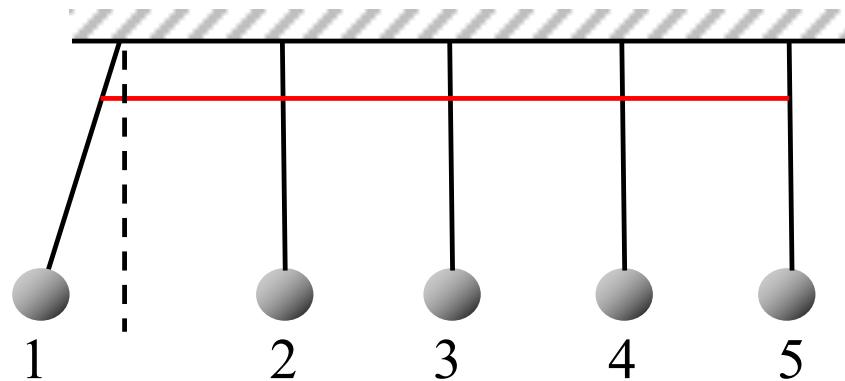
Schematic energy spectrum of ocean variability [Leblond & Mysak]

Definition of a wave:

- A wave is a recognizable signal that is transferred from one part of the medium to another with a recognizable velocity of propagation. The signal may be any feature of the disturbance, such as a maximum or an abrupt change in some quantity, provided that it can be clearly recognized and its location at any time can be determined. [Whitham: « Linear and nonlinear waves »]
-

Definition of a wave:

- Restoring force and a continuous medium to transport oscillation



Definition of a wave:

- Restoring force and a continuous medium to transport oscillation



<http://hal.elte.hu/fij/wave/pmwiki.php?n>Main.Model>

I.2. General properties

I.2.1 Simple Wave example

I.2. General properties

- Mathematically two main classes of waves:

Hyperbolic waves and dispersive waves

Hyperbolic waves

1. **Hyperbolic waves** are formulated in terms of hyperbolic partial differential equations, for example:

$$\eta_t + c\nabla\eta = 0$$

$$\eta_{tt} - c^2\nabla^2\eta = 0$$

Hyperbolic waves

1. **Hyperbolic waves** are formulated in terms of hyperbolic partial differential equations, for example:

$$\eta_t + c\nabla\eta = 0$$

$$\eta_{tt} - c^2\nabla^2\eta = 0$$

- Activity: Write the general solution of

$$\eta_{tt} - c^2\nabla^2\eta = 0$$

With Initial Conditions:

$$\eta(x, 0) = f(x) \quad \eta_t(x, 0) = 0$$

Hyperbolic waves

1. **Hyperbolic waves** are formulated in terms of hyperbolic partial differential equations, for example:

$$\eta_t + c\nabla\eta = 0$$

$$\eta_{tt} - c^2\nabla^2\eta = 0$$

- With general solutions in the form:

$$\eta = f(x - ct)$$

$$\eta = f(x - ct) + g(x + ct)$$

- Very frequent in acoustics, elasticity, electromagnetism, etc.

I.2. General properties

Hyperbolic waves

1. Examples of **Hyperbolic waves**

- Flood wave, tidal bores



- Shock wave



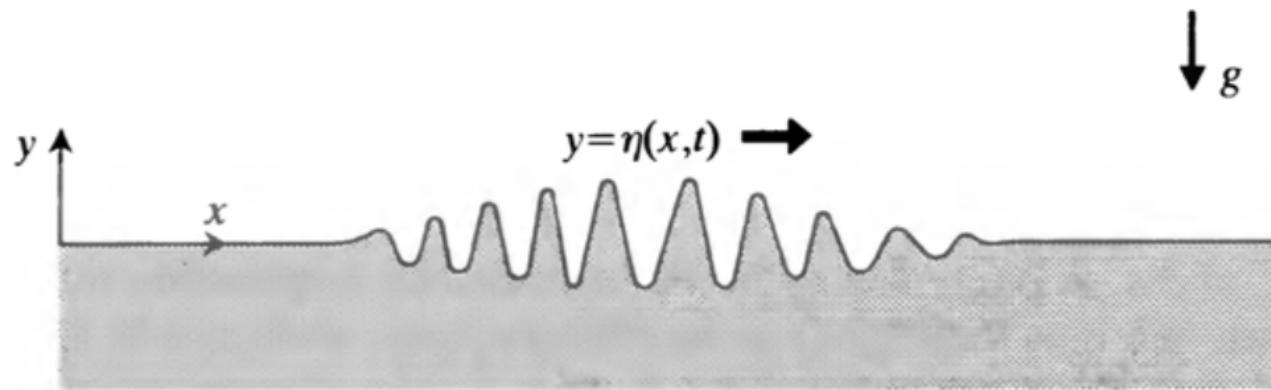
Dispersive waves

2. Dispersive waves come from a variety of partial differential equations, they are characterized principally by their dispersion relation:

$$\omega = f(k)$$

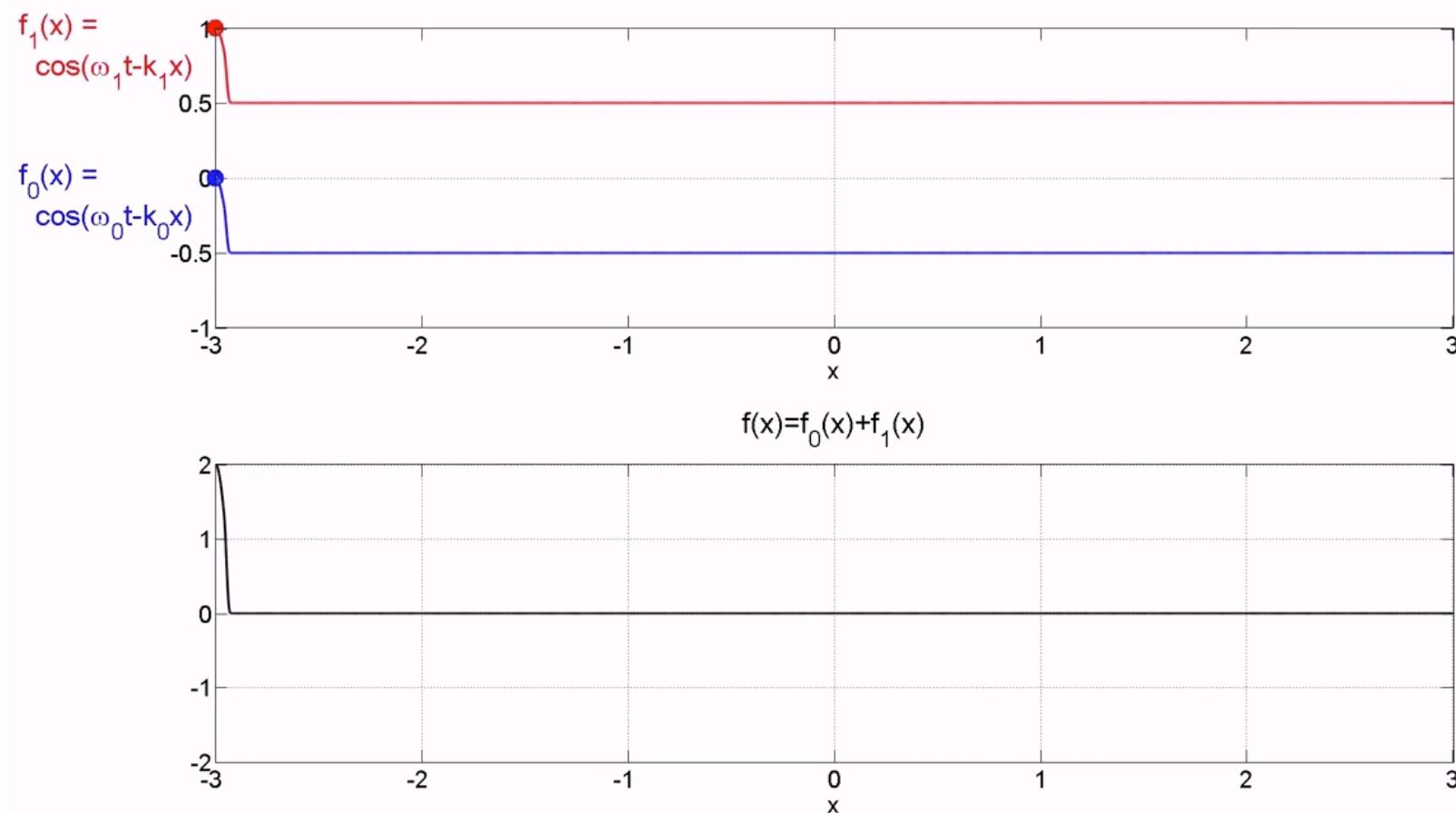
Connecting the frequency and the wave number.

They are visualized as a group of waves where the different Fourier components propagate at different speeds



I.2. General properties

Dispersive waves



Source: https://www.youtube.com/watch?v=uui9clp_DSg

I. WAVES

I.1. Introduction

I.2. General properties of Waves

I.3. Different type of ocean waves

I.3.1 Surface Gravity Waves

I.3.2 Internal Waves

I.3.3 Acoustic Waves

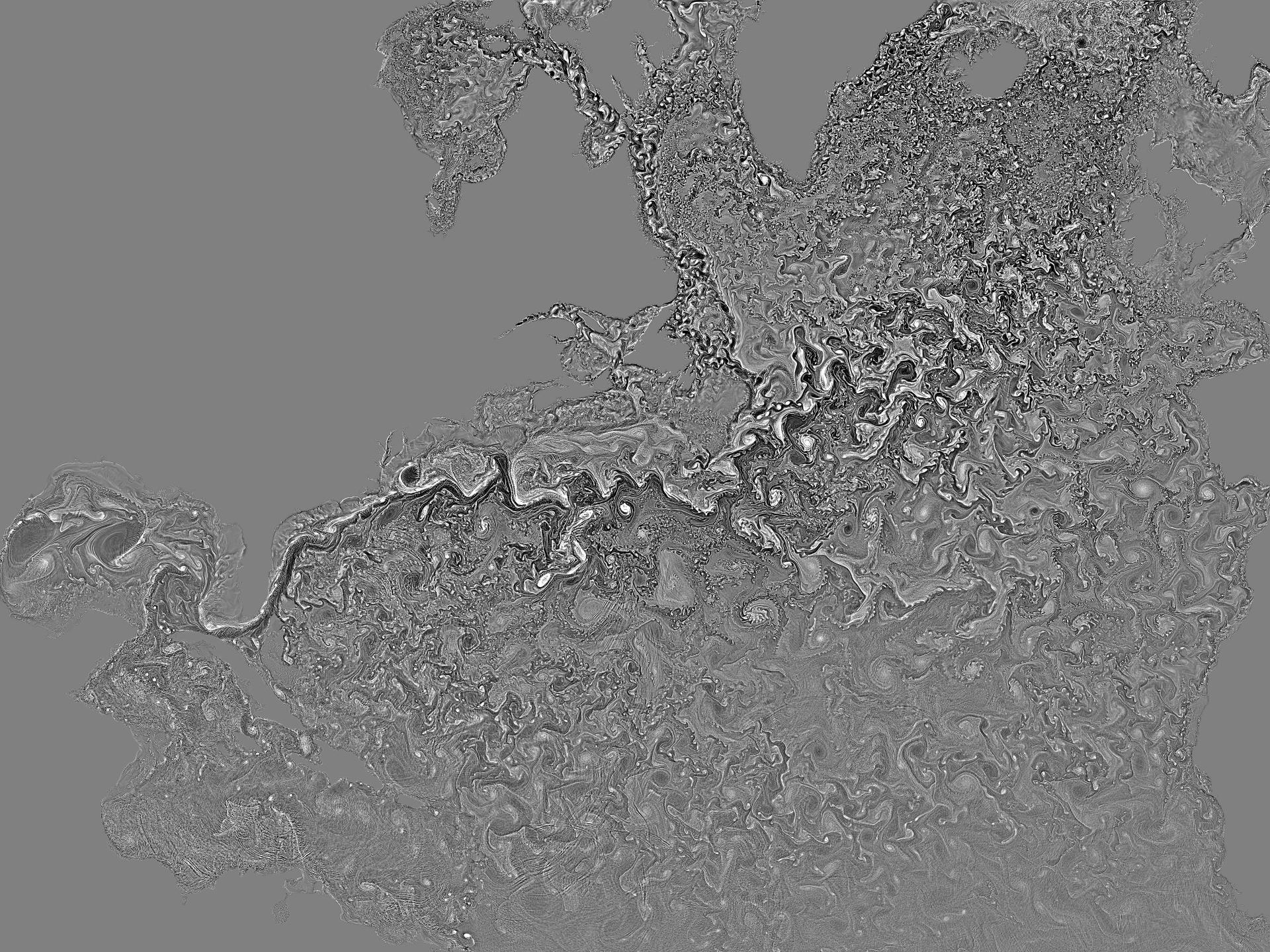
I.4. Ray Theory

I.2. General properties

I.2.2 Planar Wave example

I.2. General properties





I.3. Different type of ocean waves

I.3.1 Surface gravity waves

I.3.1.1 Long waves

I.3.1.2 Short waves

I.3.1.3 The general case

I.3. Different type of ocean waves



I.3. Different type of ocean waves

I.3.1 Surface gravity waves

I.3.1.1 Long waves

I.3.1.2 Short waves

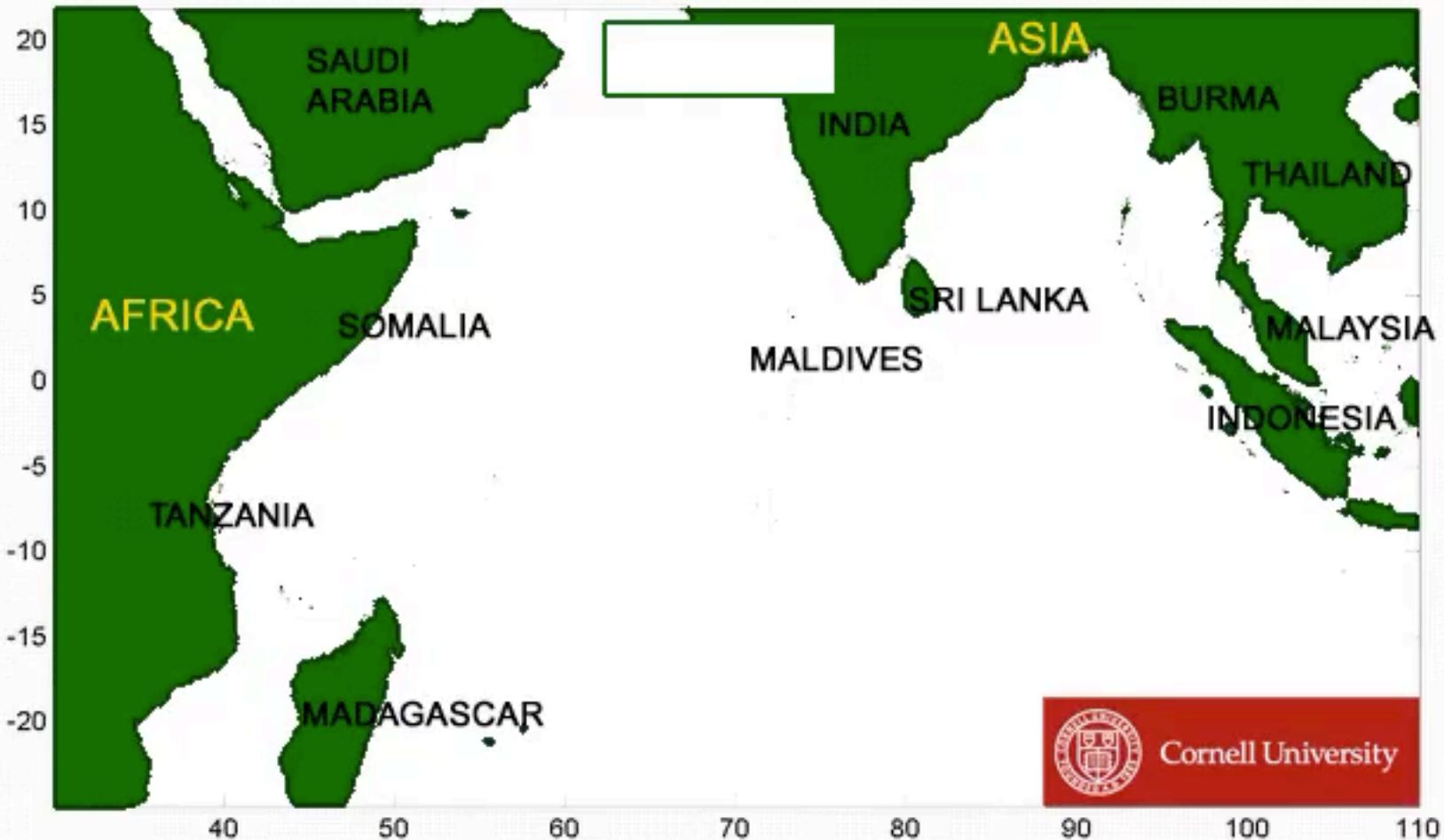
I.3.1.3 The general case

I.3.1.1 Long waves

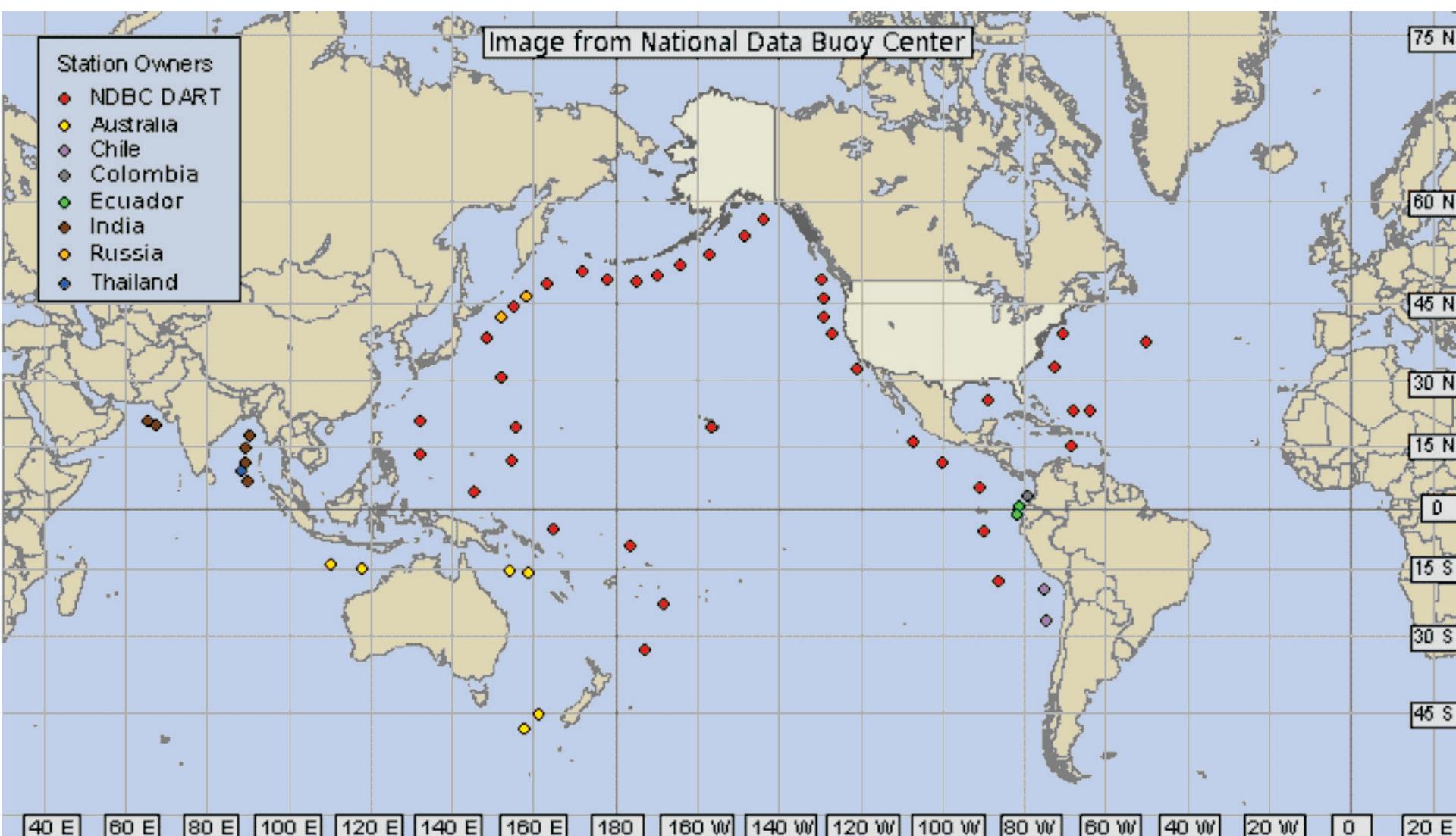
Example of long waves:

- **Tsunamis**
- **Tidal bores**

I.3.1.1 Long waves



I.3.1.1 Long waves



Tsunami detection buoys have been placed around many tectonically active locations. Map is from NOAA Tsunami Detection website <http://www.ndbc.noaa.gov/dart.shtml>

I.3.1.1 Long waves

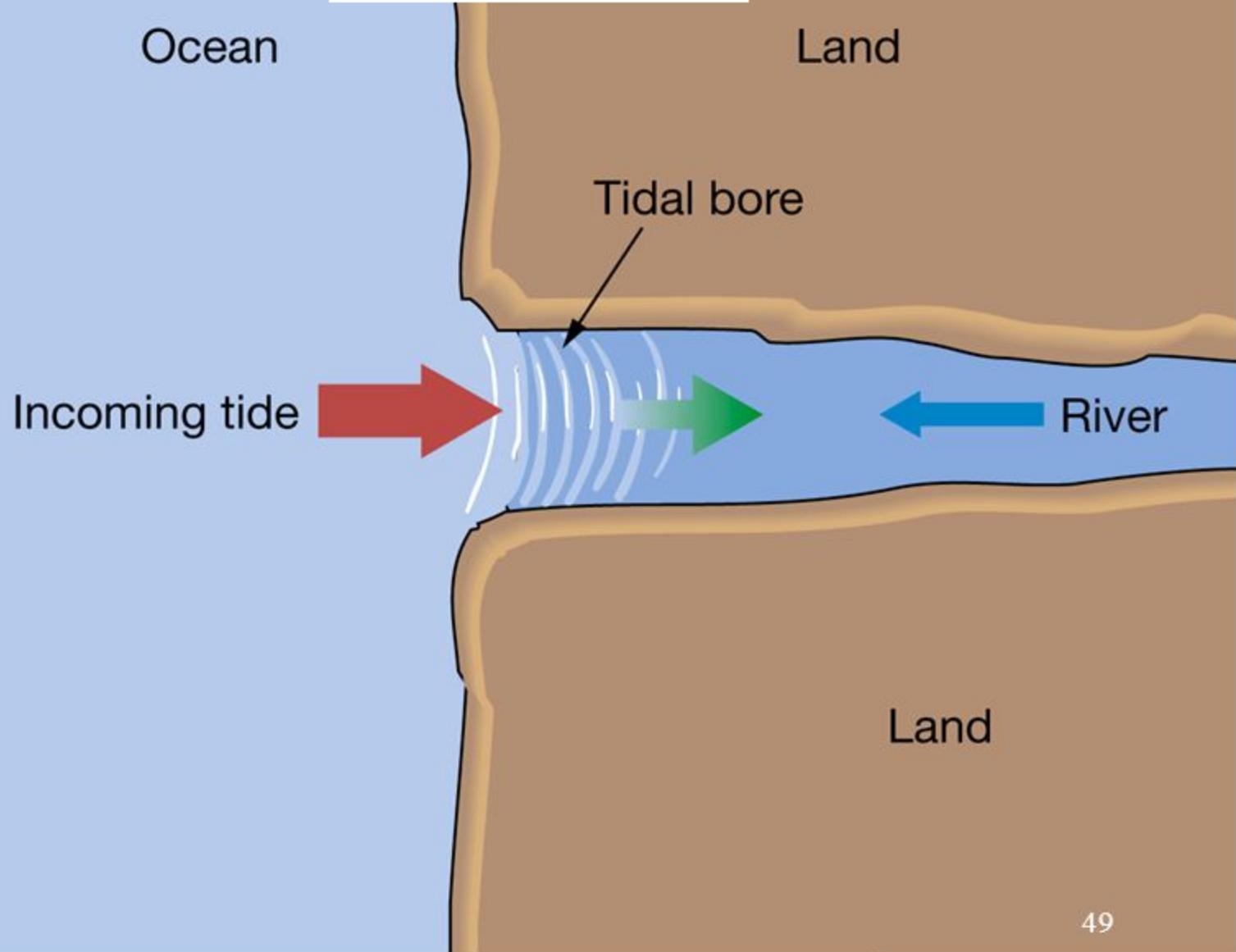
I.3.1.1 Long waves

Example of long waves:

- **Tsunamis**
- **Tidal bores**

Tidal Bore

A tidal bore is a wall of water that surges upriver with the advancing high tide.



I.3.1.1 Long waves



I.3.1.1 Long waves

I.3. Different type of ocean waves

I.3.1 Surface gravity waves

I.3.1.1 Long waves

I.3.1.2 Short waves

I.3.1.3 The general case

I.3. Different type of ocean waves

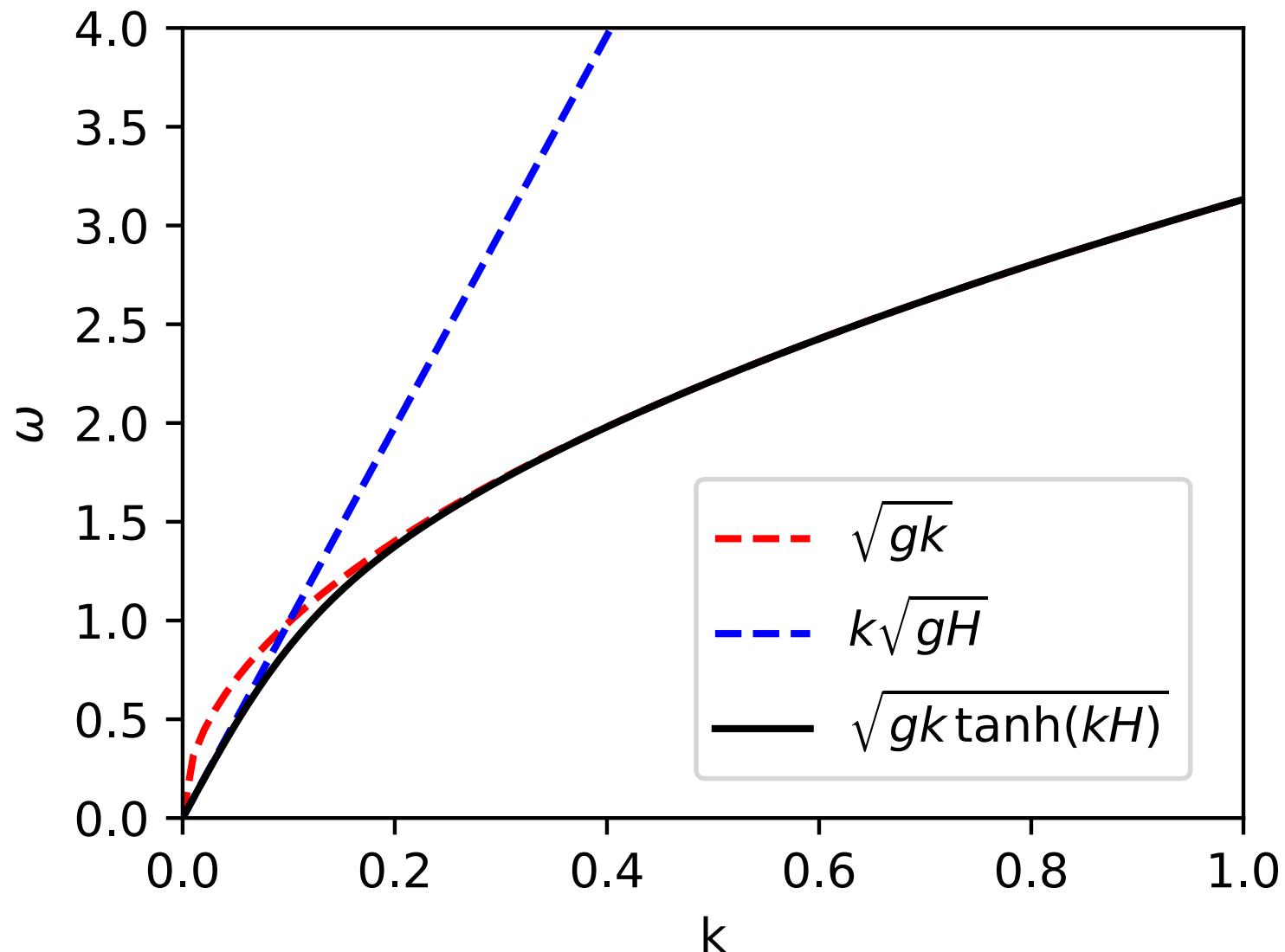
I.3.1 Surface gravity waves

I.3.1.1 Long waves

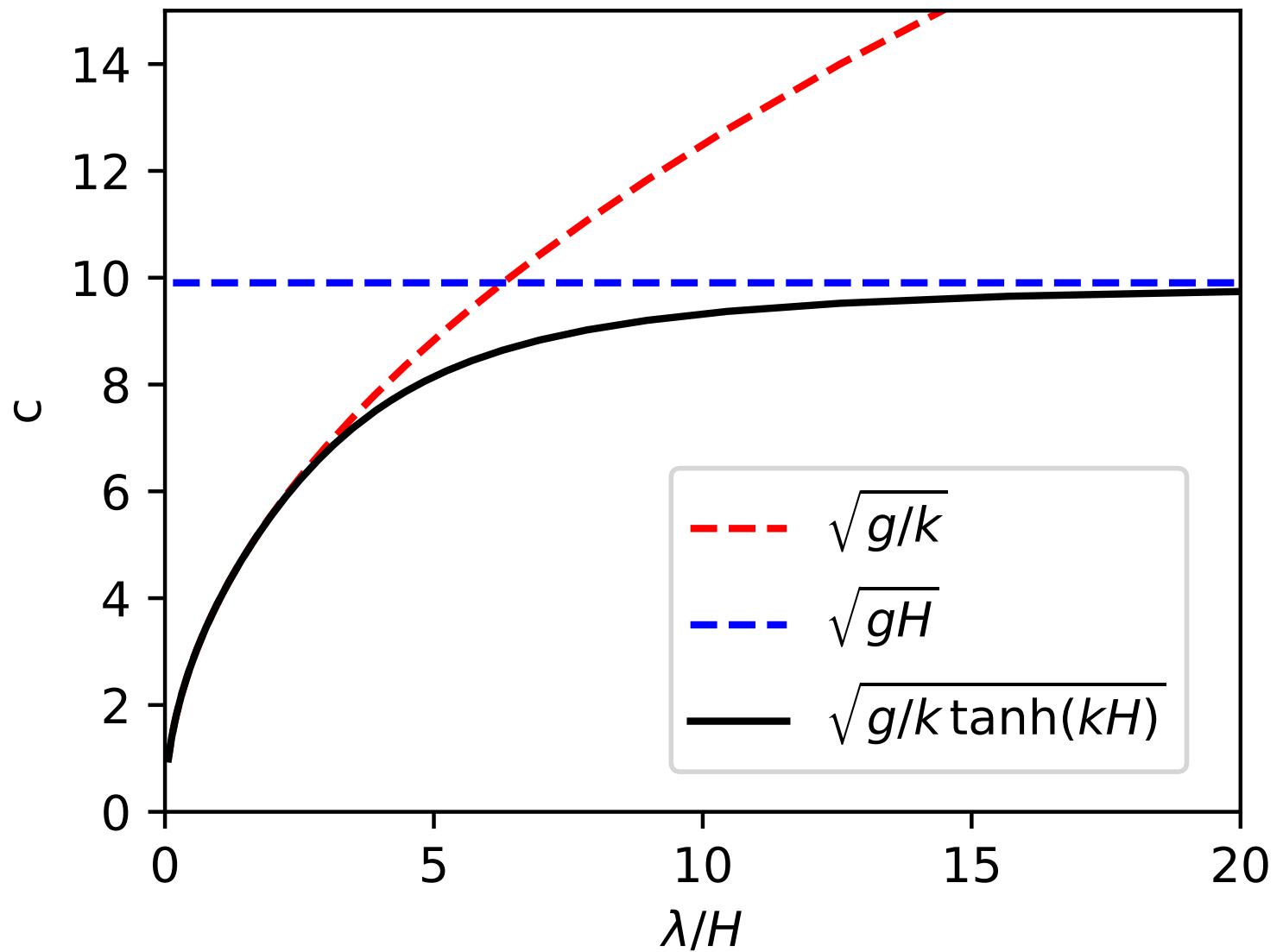
I.3.1.2 Short waves

I.3.1.3 The general case

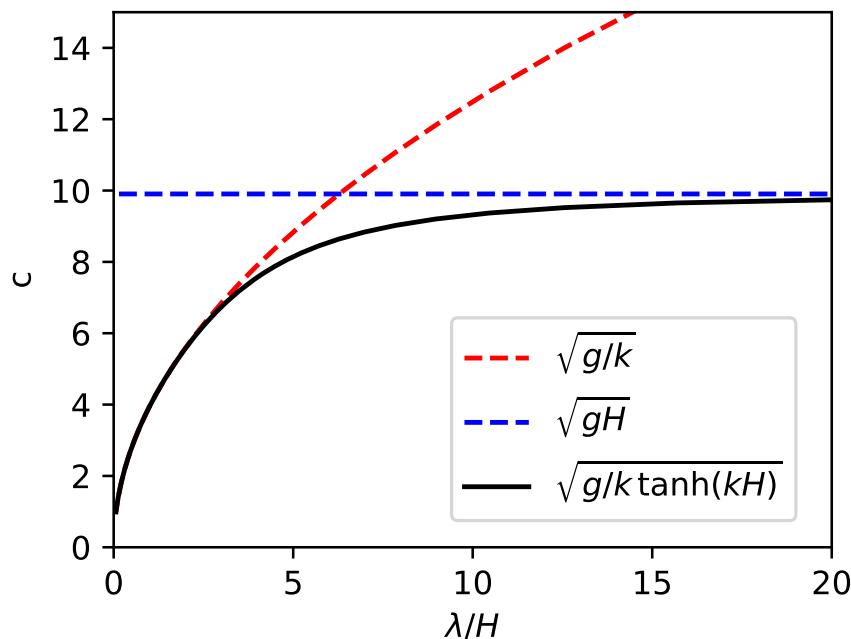
I.3.1.3 The general case



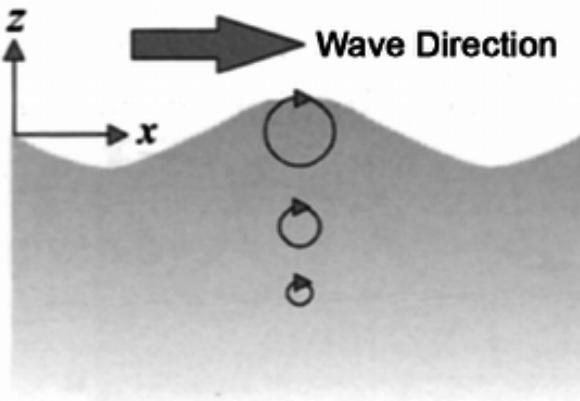
I.3.1.3 The general case



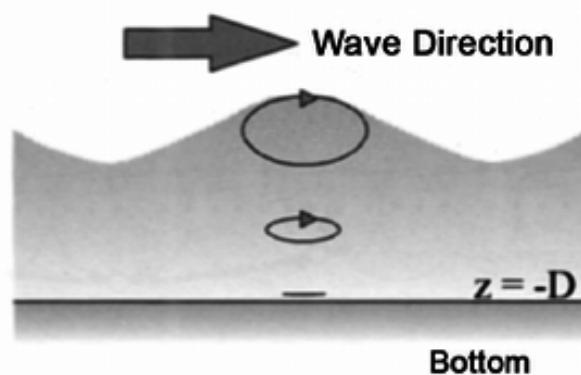
I.3.1.3 The general case



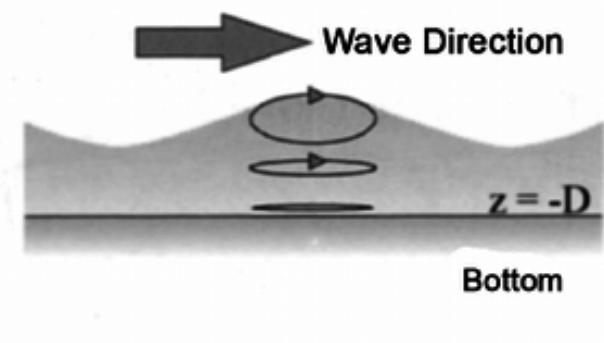
Deep Water



Intermediate Depth



Very Shallow Water



I.3.1.3 The general case

