Numerical Modelling

Jonathan GULA
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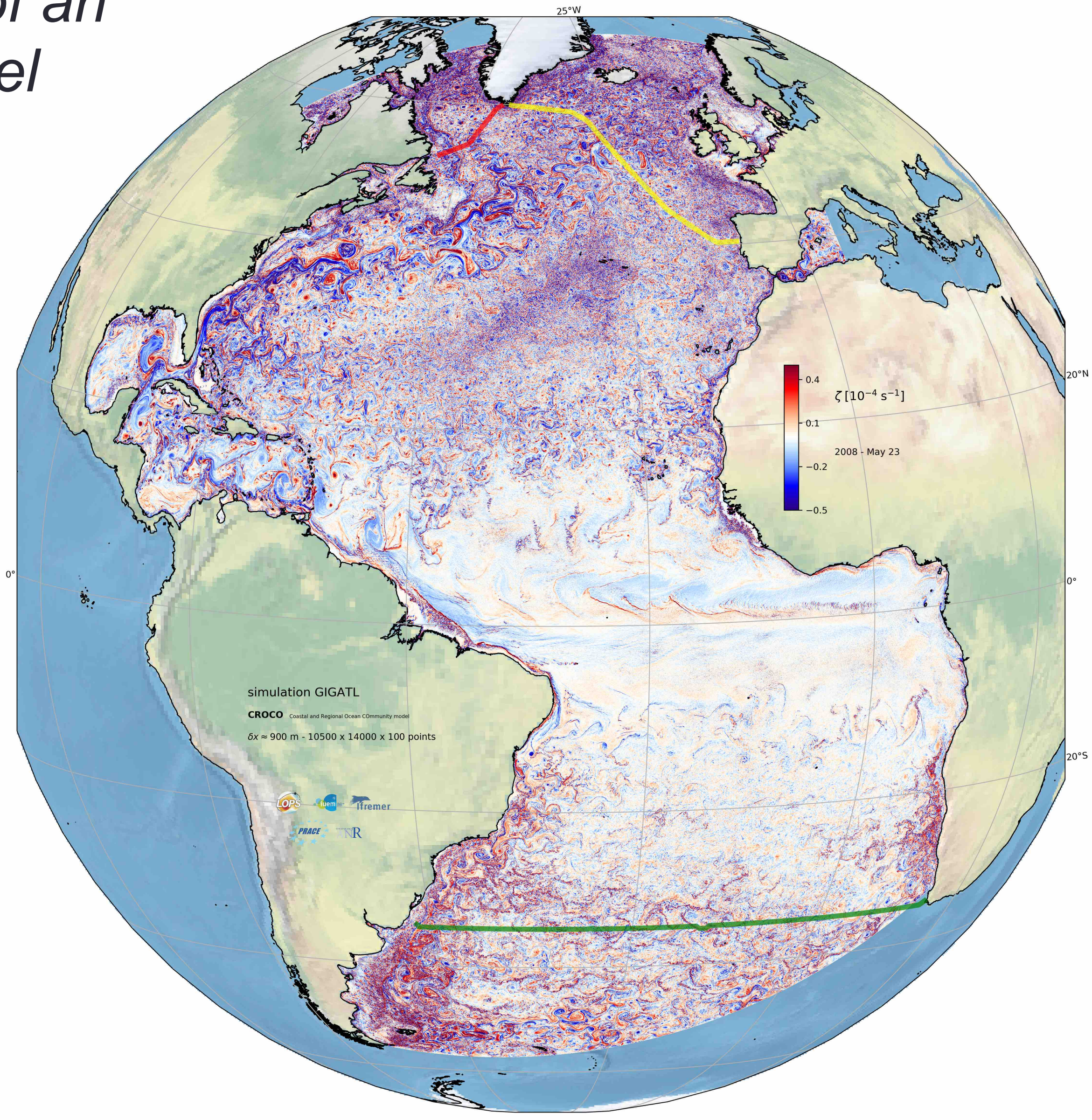
the anatomy of an ocean model



- **Lesson 1 :**
  - Introduction
  - Equations of motions
  - *Activity 1 [run an ocean model]*

- **Lesson 2 :** [B 012]
  - Horizontal Discretization
  - *Activity 2 [Dynamics of an ocean gyre]*

- **Lesson 3 :** [D109]
  - Numerical schemes
  - *Activity 3 [Impacts of numerics]*

- **Lesson 4 :** [D109]
  - Vertical coordinates
  - Model parameterizations
  - *Activity 4 [Impact of topography]*

- **Lesson 5 :** [D109]
  - Boundary Forcings
  - Presentation of the model CROCO
  - *Activity 4 [Design a realistic simulation]*

- **Lesson 6 :** [D109]
  - Diagnostics and validation
  - *Activity 5 [Analyze a realistic simulation]*

- **Lesson 7 :** [D109]
  - *Work on your projet*

Presentations and material will be available at :

jgula.fr/ModNum/

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Evaluation

- The evaluation is based on a project, which consists in setting up a realistic configuration of the region of your choice, run the experiment and perform some analysis.

- Written Report **due for Feb. 04**

Useful references

Extensive courses:

- MIT: https://ocw.mit.edu/courses/earth-atmospheric-and-planetary-sciences/12-950-atmospheric-and-oceanic-modeling-spring-2004/lecture-notes/
- Princeton: https://stephengriffies.github.io/assets/pdfs/GFM_lectures.pdf

Overview on ocean modelling and current challenges:

- Griffies et al., 2000, Developments in ocean climate modelling, Ocean Modelling.http://jgula.fr/ModNum/Griffiesetal00.pdf
- Griffies, 2006, "Some Ocean Model Fundamentals", In "Ocean Weather Forecasting: An Integrated View of Oceanography", 2006, Springer Netherlands. http://jgula.fr/ModNum/Griffies_Chapter.pdf
- Fox-Kemper et al, 19, "Challenges and Prospects in Ocean Circulation Models" http://jgula.fr/ModNum/FoxKemperetal19.pdf

ROMS/CROCO:

- https://www.croco-ocean.org/documentation/
- Shchepetkin, A., and J. McWilliams, 2005: The Regional Oceanic Modeling System (ROMS): A split-explicit, free-surface, topography-following- coordinate ocean model. Ocean Modell. http://jgula.fr/ModNum/ShchepetkinMcWilliams05.pdf

Introduction

Master's degree 2^{nd} year Marine Physics

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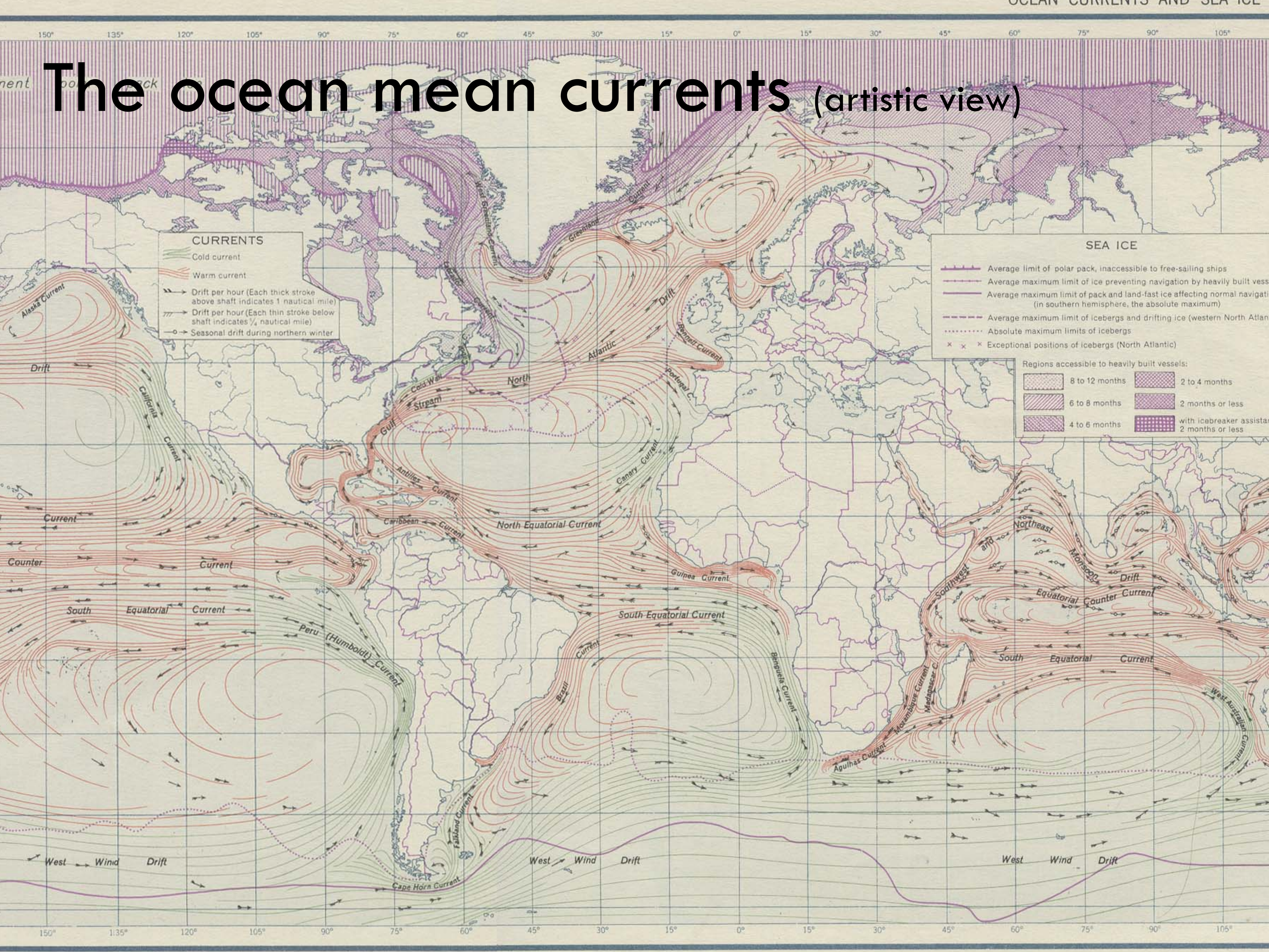
The ocean mean currents (artistic view)



Can be understood using theory and simplified models

THE WESTWARD INTENSIFICATION OF WIND-DRIVEN OCEAN CURRENTS

Henry Stommel

(Contribution No. 408, Woods Hole Oceanographic Institution)

Abstract--A study is made of the wind-driven circulation in a homogeneous rectangular ocean under the influence of surface wind stress, linearised bottom friction, horizontal pressure gradients caused by a variable surface height, and Coriolis force.

An intense crowding of streamlines toward the western border of the ocean is discovered to be caused by variation of the Coriolis parameter with latitude. It is suggested that this process is the main reason for the formation of the intense currents (Gulf stream and others) observed in the actual oceans.

JOURNAL OF METEOROLOGY

ON THE WIND-DRIVEN OCEAN CIRCULATION

By *Walter H. Munk*

Institute of Geophysics and Scripps Institution of Oceanography, University of California[1]

(Manuscript received 24 September 1949)

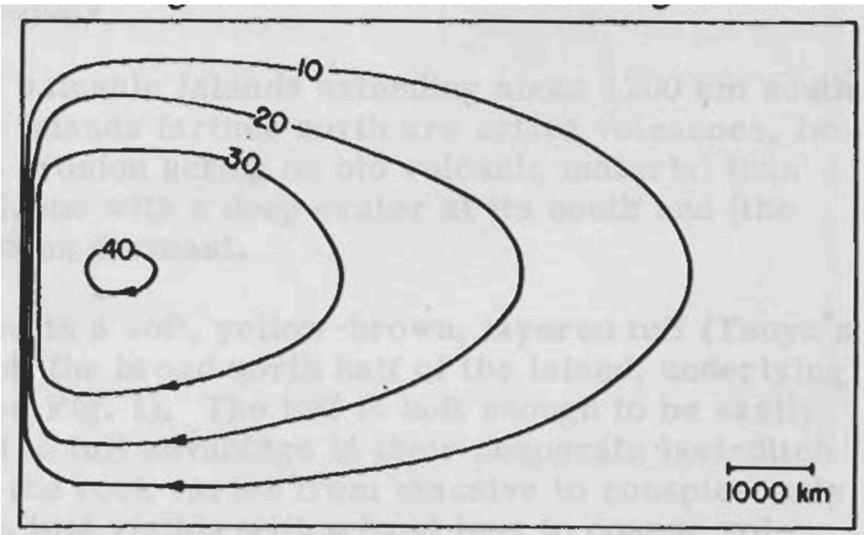


Fig. 5--Streamlines for the case where the Coriolis force is a linear function of latitude

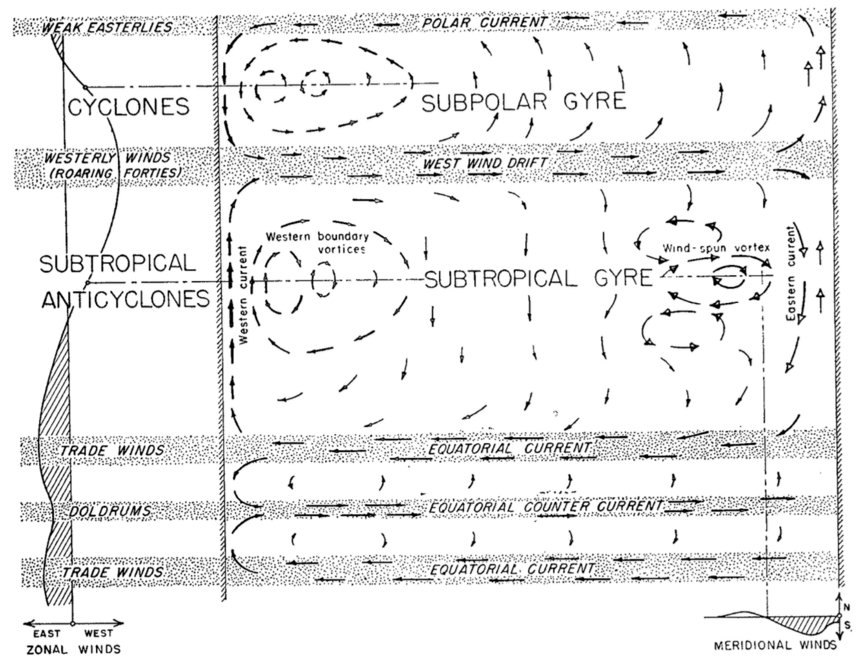
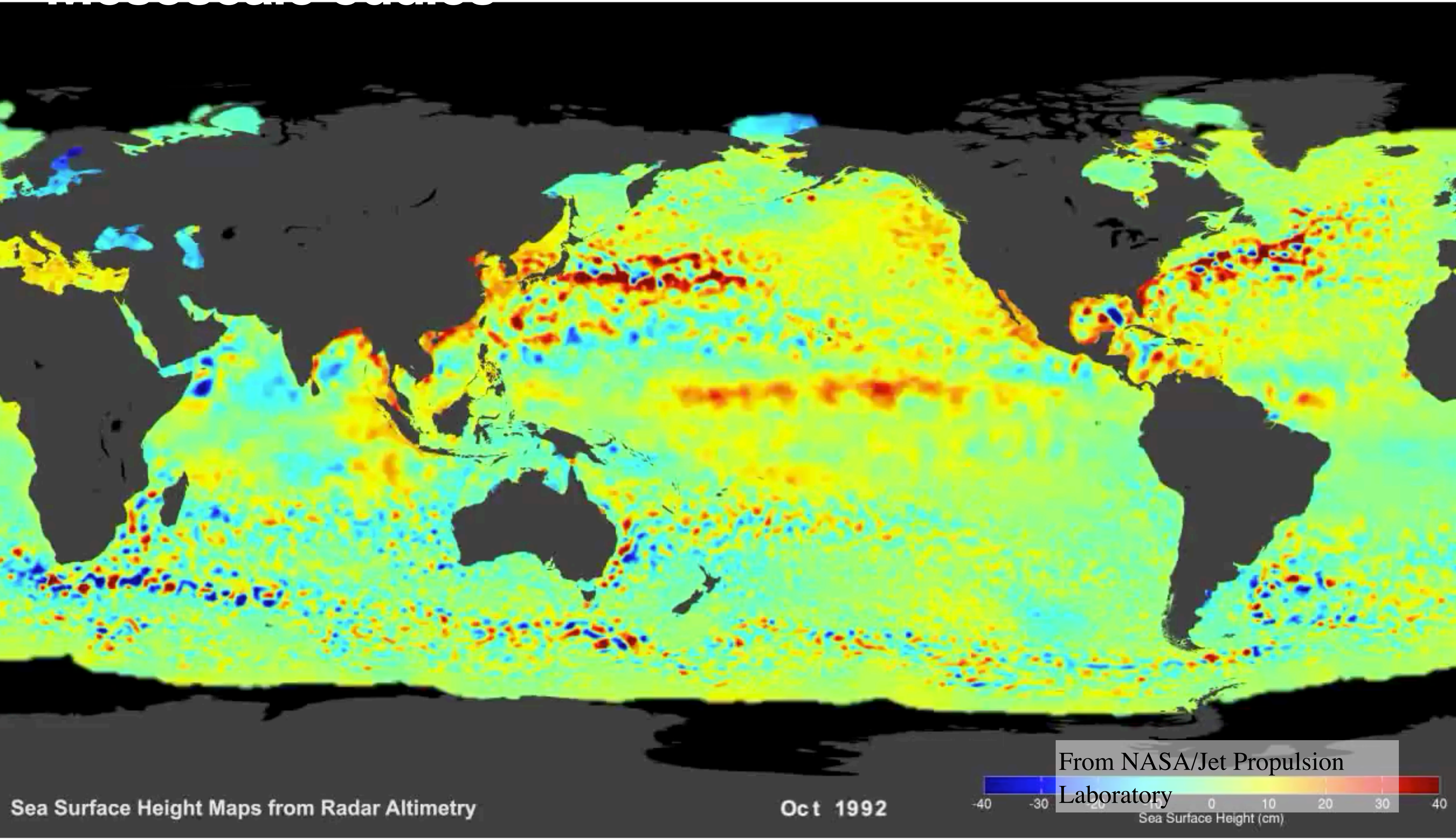


FIG. 8. Schematic presentation of circulation in a rectangular ocean resulting from zonal winds (filled arrowheads), meridional winds (open arrowheads), or both (half-filled arrowheads). The width of the arrows is an indication of the strength of the currents. The nomenclature applies to either hemisphere, but in the Southern Hemisphere the subpolar gyre is replaced largely by the Antarctic Circumpolar Current (west wind drift) flowing around the world. Geographic names of the currents in various oceans are summarized in table 3.

https://www.jgula.fr/ModNum/Stommel48.pdf

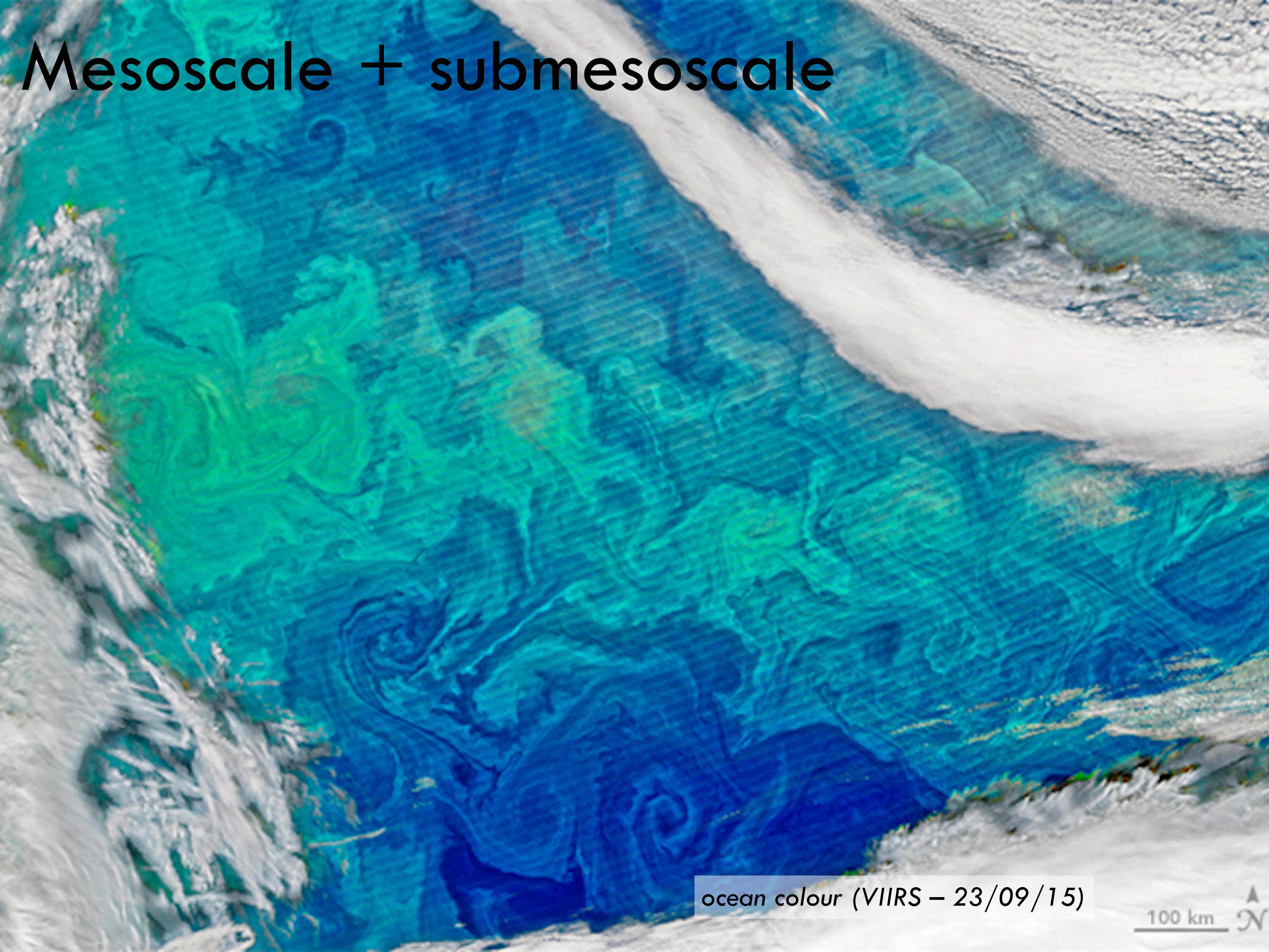
https://www.jgula.fr/ModNum/Munk50.pdf

But reality is much more turbulent:

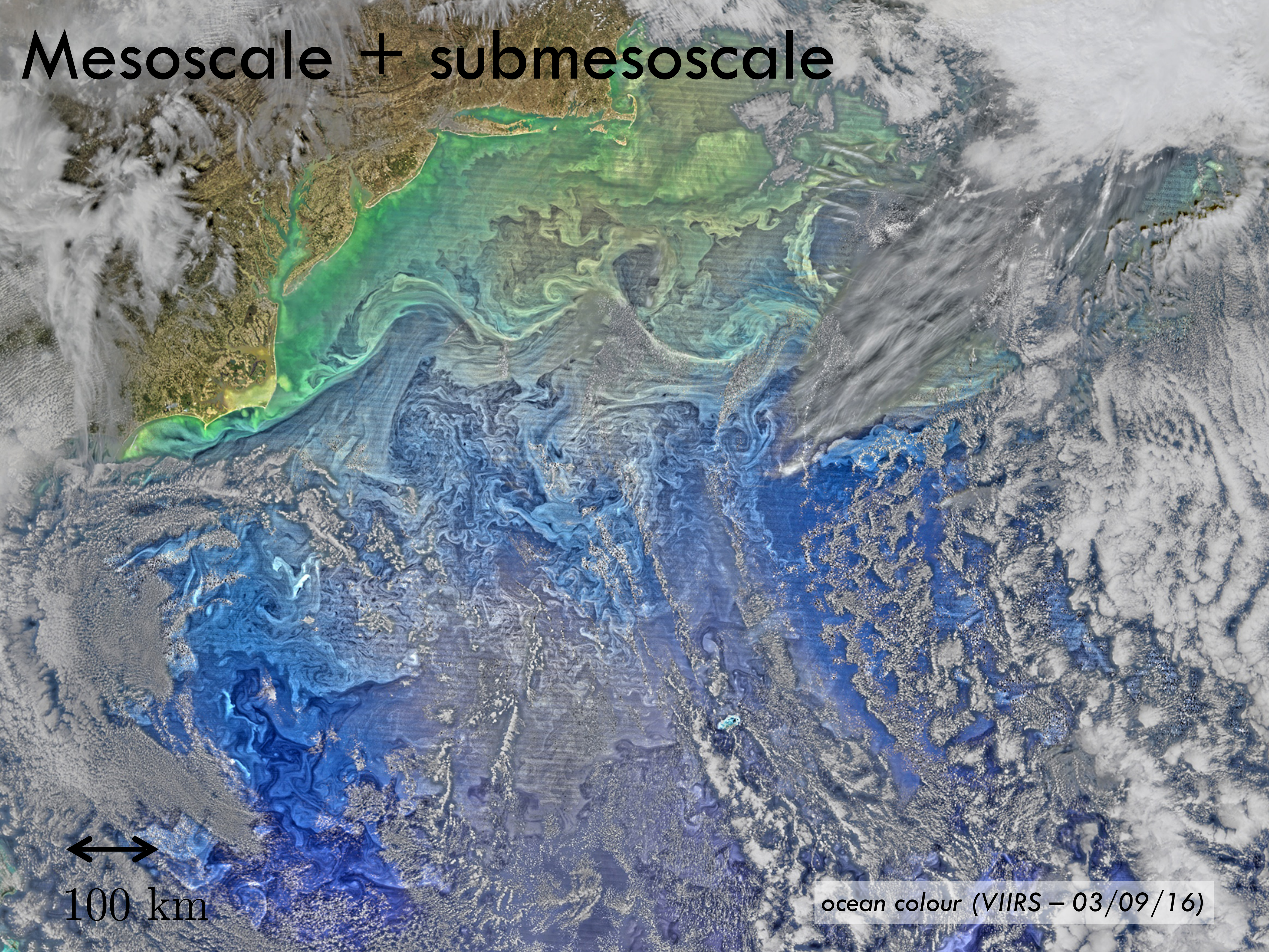


From NASA/Jet Propulsion Laboratory

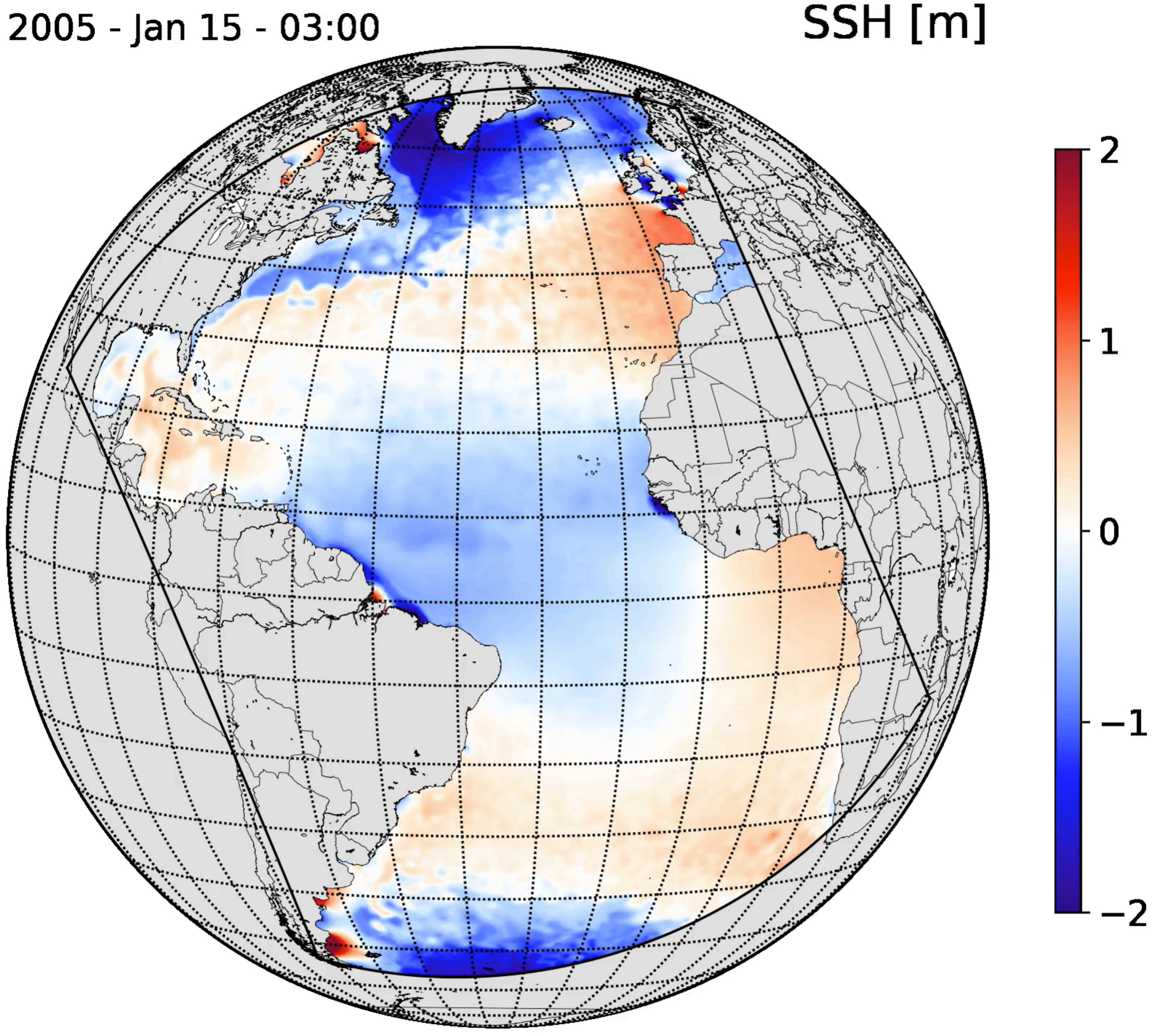
Mesoscale + submesoscale



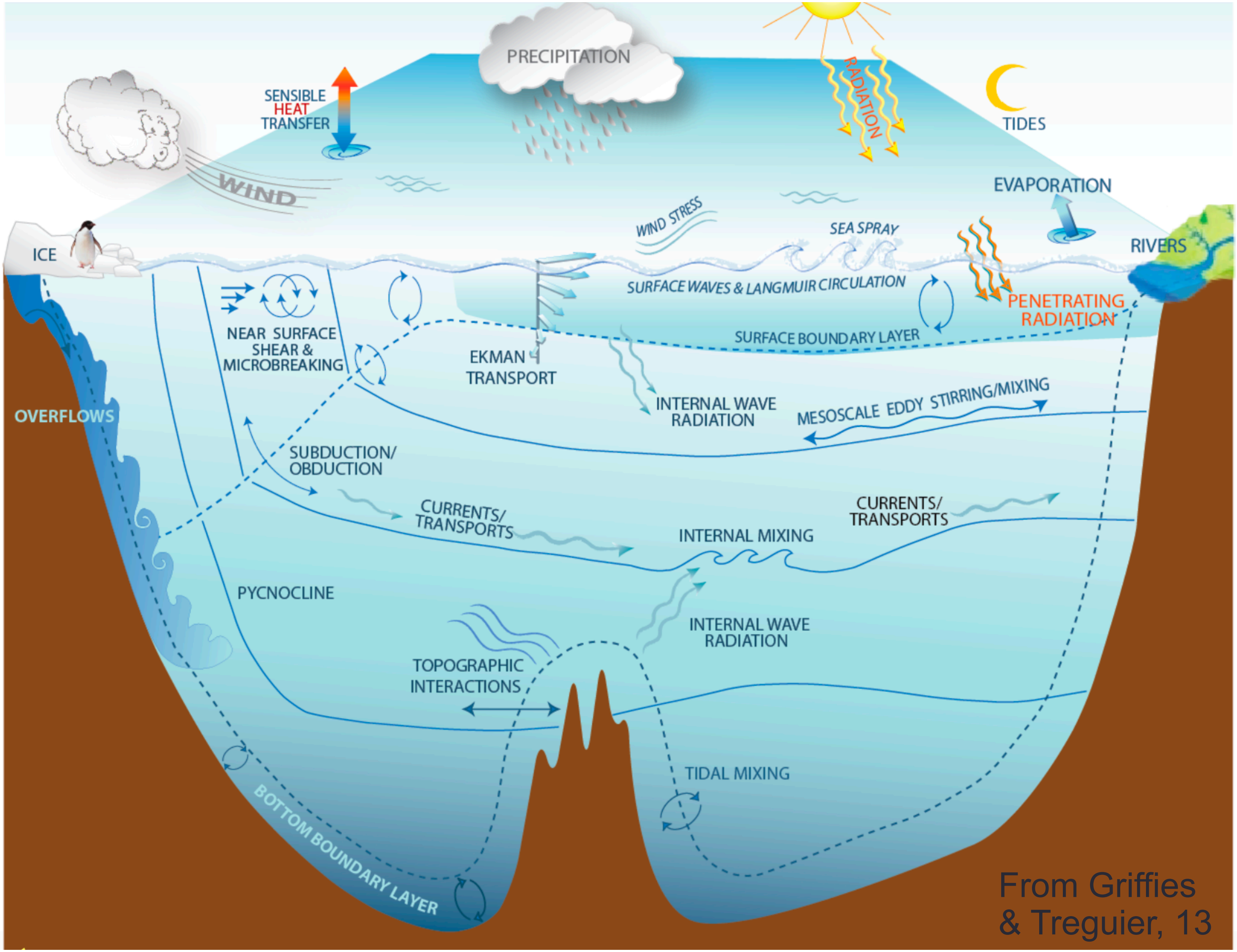
ocean colour (VIIRS – 23/09/15)


Mesoscale + submesoscale
100 km
ocean colour (VIIRS – 03/09/16)

And HF motions like tides:

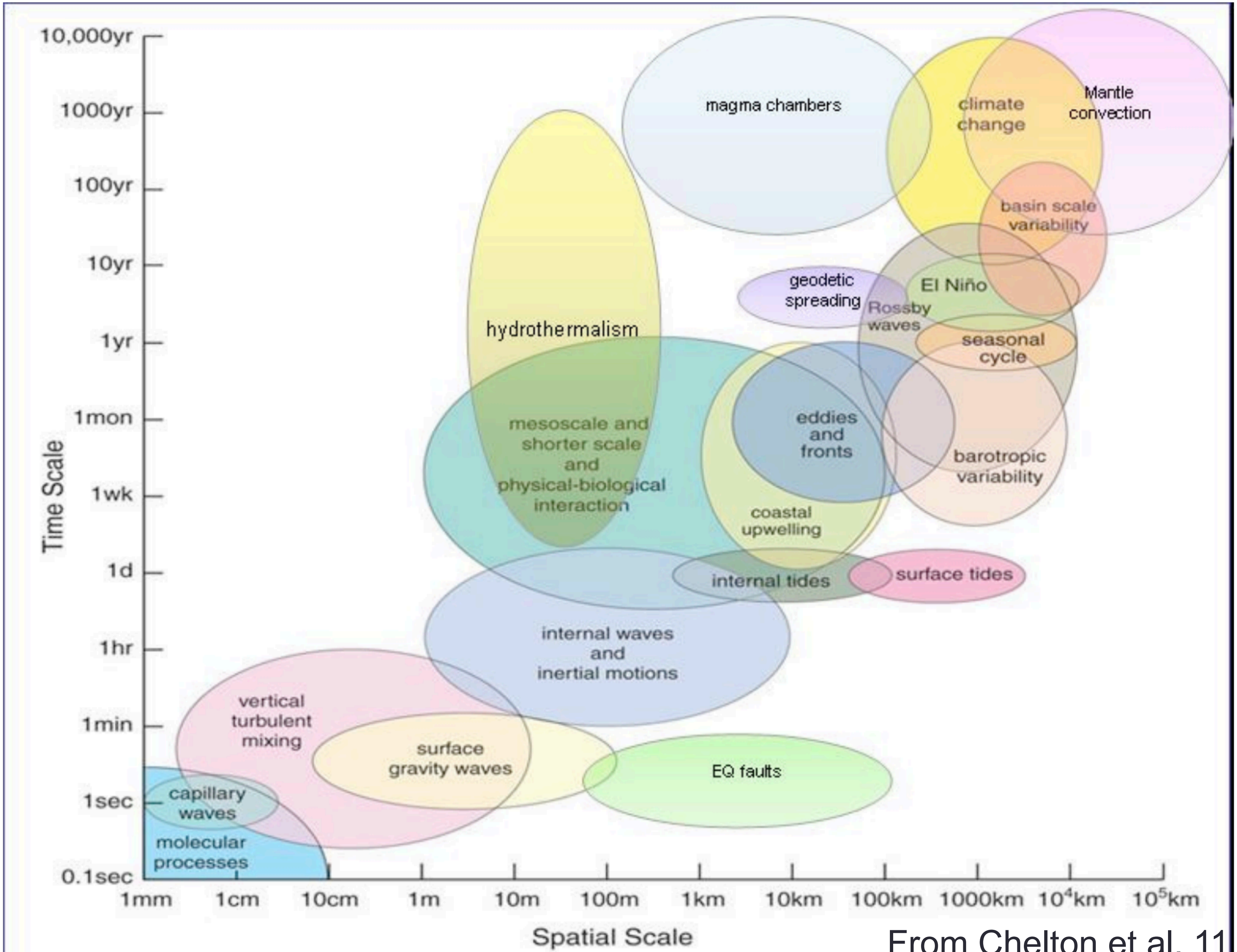


A zoo of processes and scales



From Griffies & Treguier, 13

Temporal and spatial scales in the ocean



From Chelton et al, 11

We know the equations:

Navier-Stokes
[Momentum equations]

$$\frac{\partial \vec{u}}{\partial t} + \vec{u} \cdot \vec{\nabla} \vec{u} + 2\vec{\Omega} \times \vec{u} + g\vec{k} = -\frac{\vec{\nabla} P}{\rho} + \vec{\mathcal{F}}$$

Conservation of mass

$$\frac{\partial \rho}{\partial t} + \vec{\nabla} \cdot \rho \vec{u} = 0$$

Conservation of heat

$$\frac{DT}{Dt} = \mathcal{S}_T$$

Conservation of salinity

$$\frac{DS}{Dt} = \mathcal{S}_S$$

Equation of state

$$\rho = \rho(T, S, p)$$

We know the equations:

Navier-Stokes
[Momentum equations]

$$\frac{\partial \vec{u}}{\partial t} + \vec{u} \cdot \vec{\nabla} \vec{u} + 2\vec{\Omega} \times \vec{u} + g\vec{k} = -\frac{\vec{\nabla} P}{\rho} + \vec{\mathcal{F}}$$

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Conservation of salinity

$$\frac{DS}{Dt} = \mathcal{S}_S$$

Equation of state

$$\rho = \rho(T, S, p)$$

But we don't know the solutions…

We know the equations:

Millennium Prize problems

Navier–Stokes existence and smoothness

The Clay Mathematics Institute in May 2000 made this problem one of its seven Millennium Prize problems in mathematics. It offered a US $1,000,000 prize to the first person providing a solution for a specific statement of the problem:[1]

Prove or give a counter-example of the following statement:

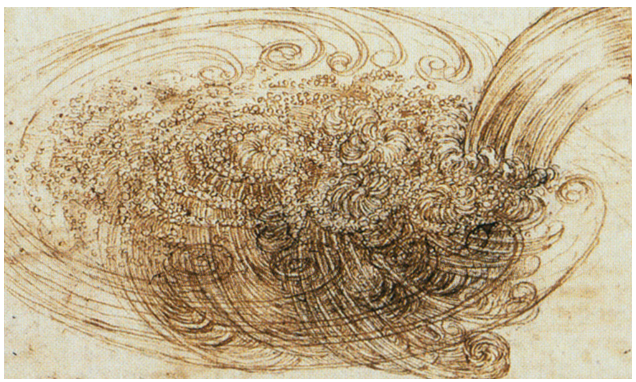
In three space dimensions and time, given an initial velocity field, there exists a vector velocity and a scalar pressure field, which are both smooth and globally defined, that solve the Navier–Stokes equations.

We know the equations:

Navier-Stokes
[Momentum equations]

$$\frac{\partial \vec{u}}{\partial t} + \boxed{\vec{u} \cdot \vec{\nabla} \vec{u}} + 2\vec{\Omega} \times \vec{u} + g\vec{k} = -\frac{\vec{\nabla} P}{\rho} + \vec{\mathcal{F}}$$

Non-linear terms = Turbulence



turbolenza by da Vinci [1507]

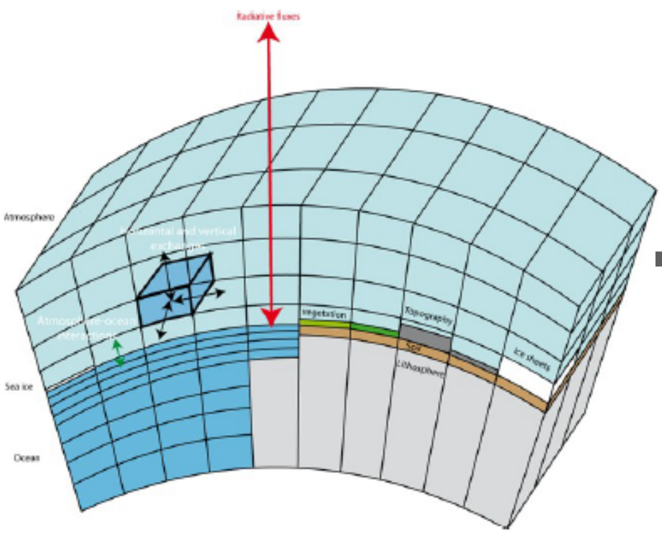
Big whorls have little whorls,
which feed on their velocity;
And little whorls have lesser whorls,
And so on to viscosity.
L.F. Richardson [1922]

Turbulent water jet (Re = 2300) [Van Dyke, 82]

$$\frac{\partial \vec{u}}{\partial t} + \vec{u} \cdot \vec{\nabla} \vec{u} + 2\vec{\Omega} \times \vec{u} + g\vec{k} = -\frac{\vec{\nabla} P}{\rho} + \vec{\mathcal{F}}$$

Navier Stokes equations

+



Grid Discretization

+

Supercomputer (Curie – CEA)

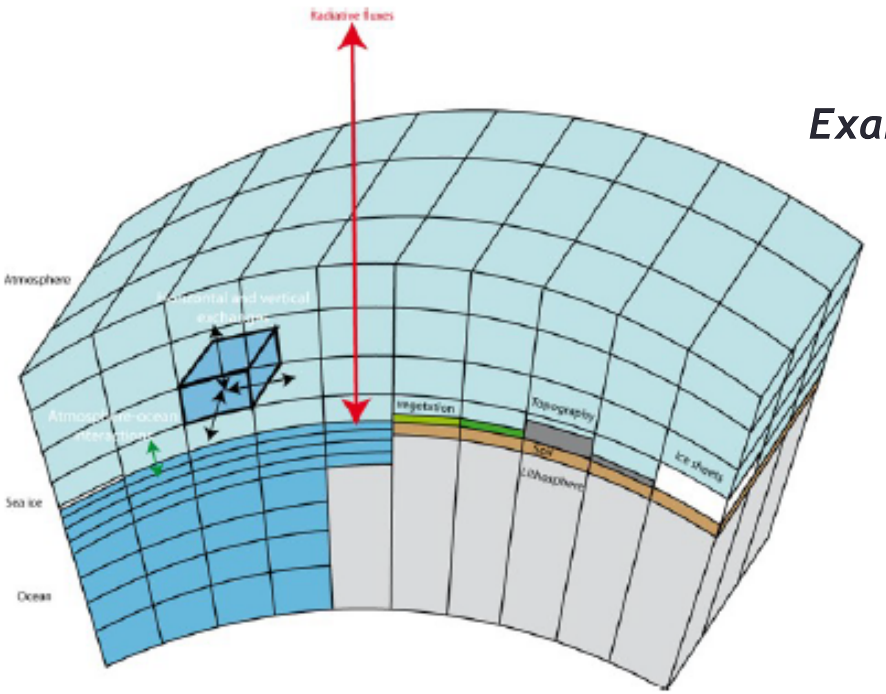
One way to solve them (approximately): **Numerical modelling**

Ocean modeling principle

An ocean model is simplified representation of physical processes that take place in the ocean.

The ocean is divided into boxes : **discretization**

The NS equations can be solved on the grid using **numerical methods**



Example of a finite difference grid

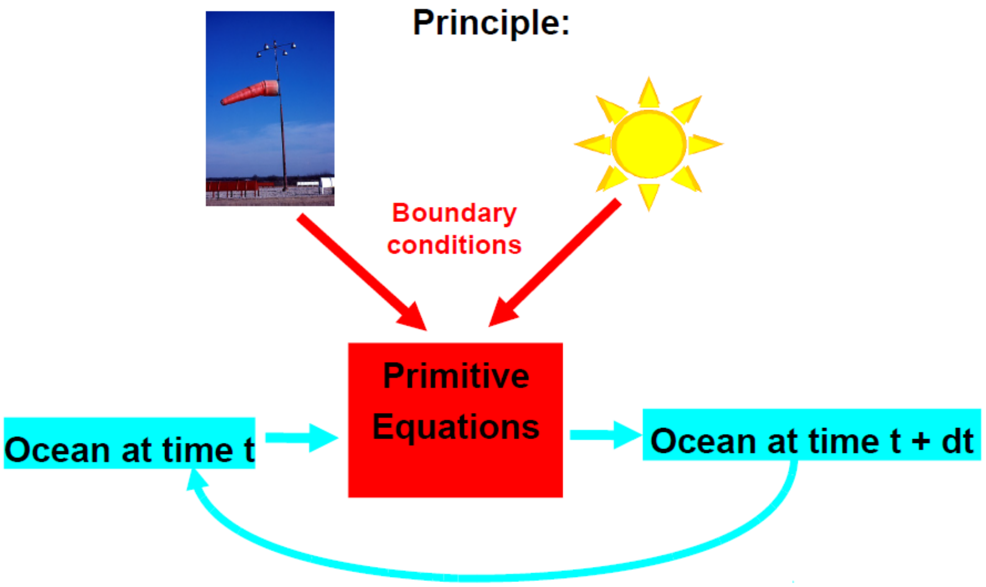
Ocean modeling principle

If we know:

- The **ocean state at time *t* :**

  u, v, w, T, S, …

- **Boundary conditions :**
  surface, bottom, lateral sides



→ We can **compute the ocean state at time** ***t+dt*** using **numerical approximations of fluid dynamics equations**

Ocean modeling principle

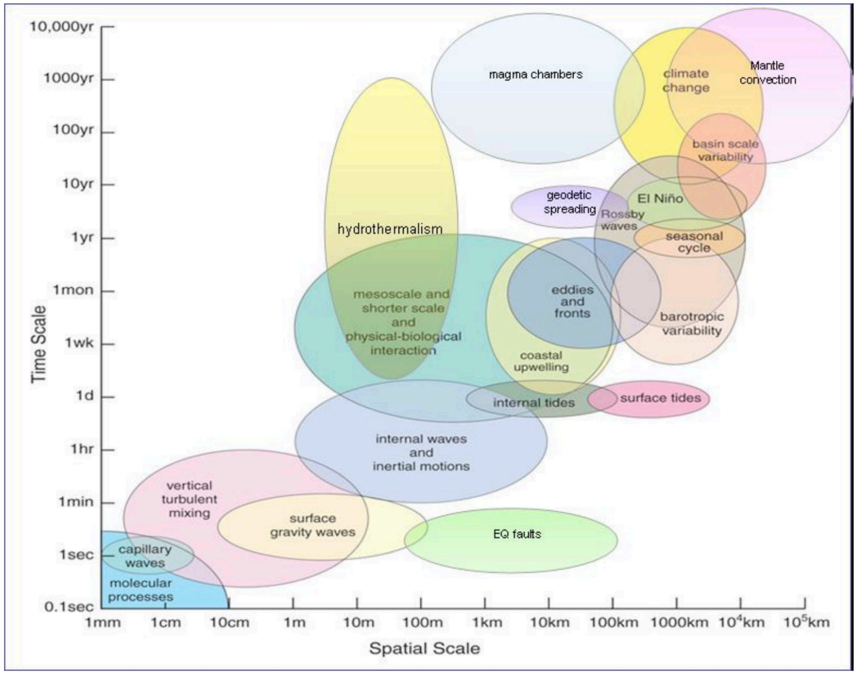
One major Problem:

Setting the model's grid scale to the Kolmogorov length (to resolve diffusive processes) $\Delta = 10^{-3}$m over a global ocean domain of volume 1.3×10^{18} m^3 requires 1.3×10^{27} discrete grid cells.

And Direct Numerical Simulation (DNS) of the global ocean climate requires 3×10^{10} time steps of one second (1000 years).

So we will be dust long before DNS of global ocean climate is possible:

In the meantime, we must use **subgrid scale parameterizations** to simulate the ocean.



Ocean Circulation Models

- ROMS ➔ CROCO https://www.croco-ocean.org/
- NEMO http://www.nemo-ocean.eu/
- MITgcm http://mitgcm.org/
- HYCOM http://hycom.org/
- POP http://www.cesm.ucar.edu/models/cesm1.0/pop2/
- OFES http://www.jamstec.go.jp/esc/ofes/eng/
- MOM http://www.gfdl.noaa.gov/ocean-model
- POM http://www.ccpo.odu.edu/POMWEB/
- etc

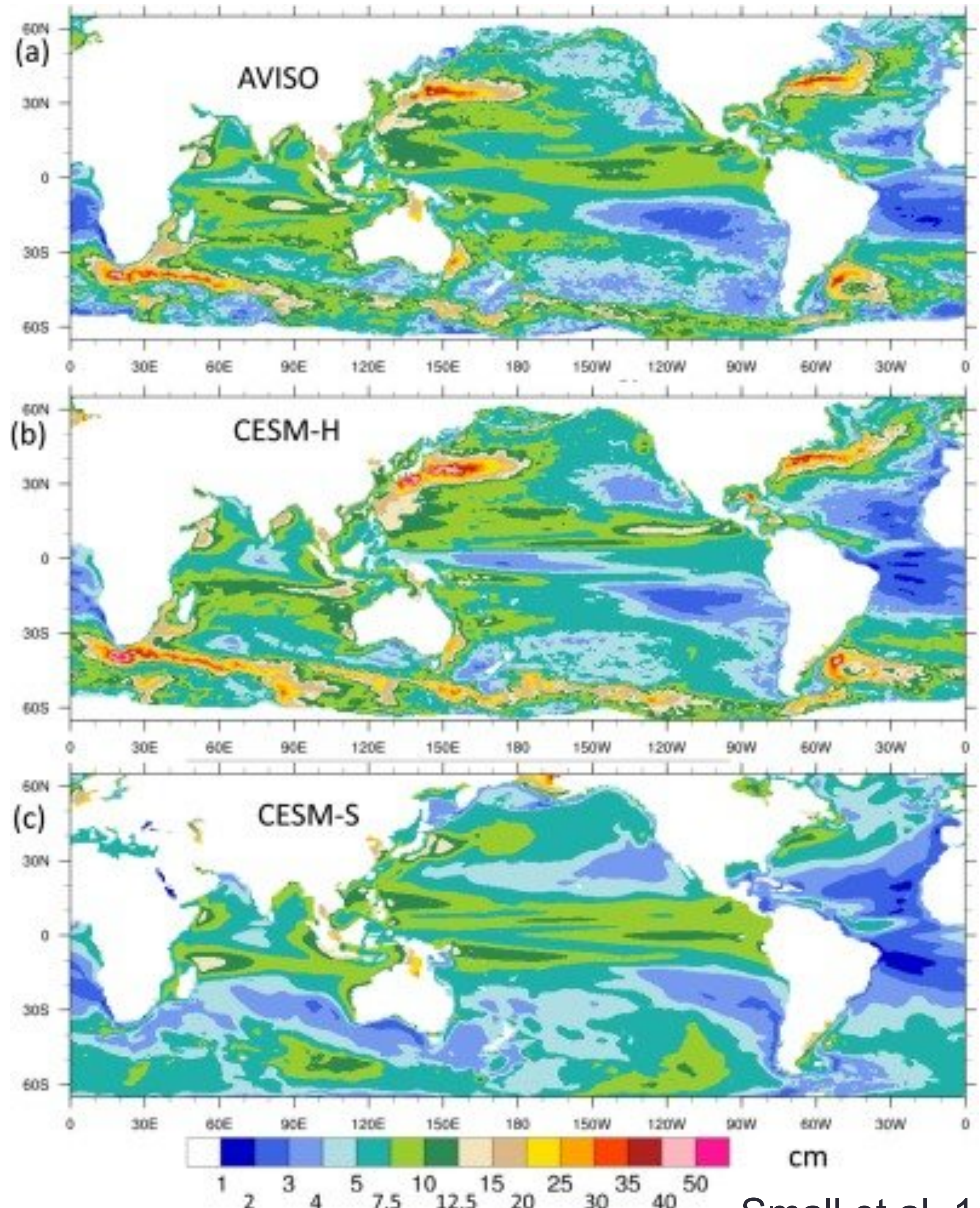
Ocean Circulation Models

- Mechanistic studies of ocean and climate processes:
  - Process studies using fine resolution (≤ 1 km) simulations (**MITgcm, SUNTANS, CROCO-NH**)
  - Mechanisms for coastal and shelf processes (≤ 10 km) (**ROMS/CROCO, MARS3D, HYCOM**)
  - Mechanisms for climate variability (basin to global) (**MOM6, NEMO**)
- Operational predictions and state estimation
  - Coastal forecasting India **INCOIS**
  - Coastal forecasting USA **NCEP**
  - Ocean state estimation **ECCO**
- Projections for future climate change
  - IPCC-class simulations with anthropogenic forcing (**CMIP**)

Ocean Modelling example:

IPCC global run

Typical length = 100 - 1000 years



0.1 deg

1 deg

Small et al, 14

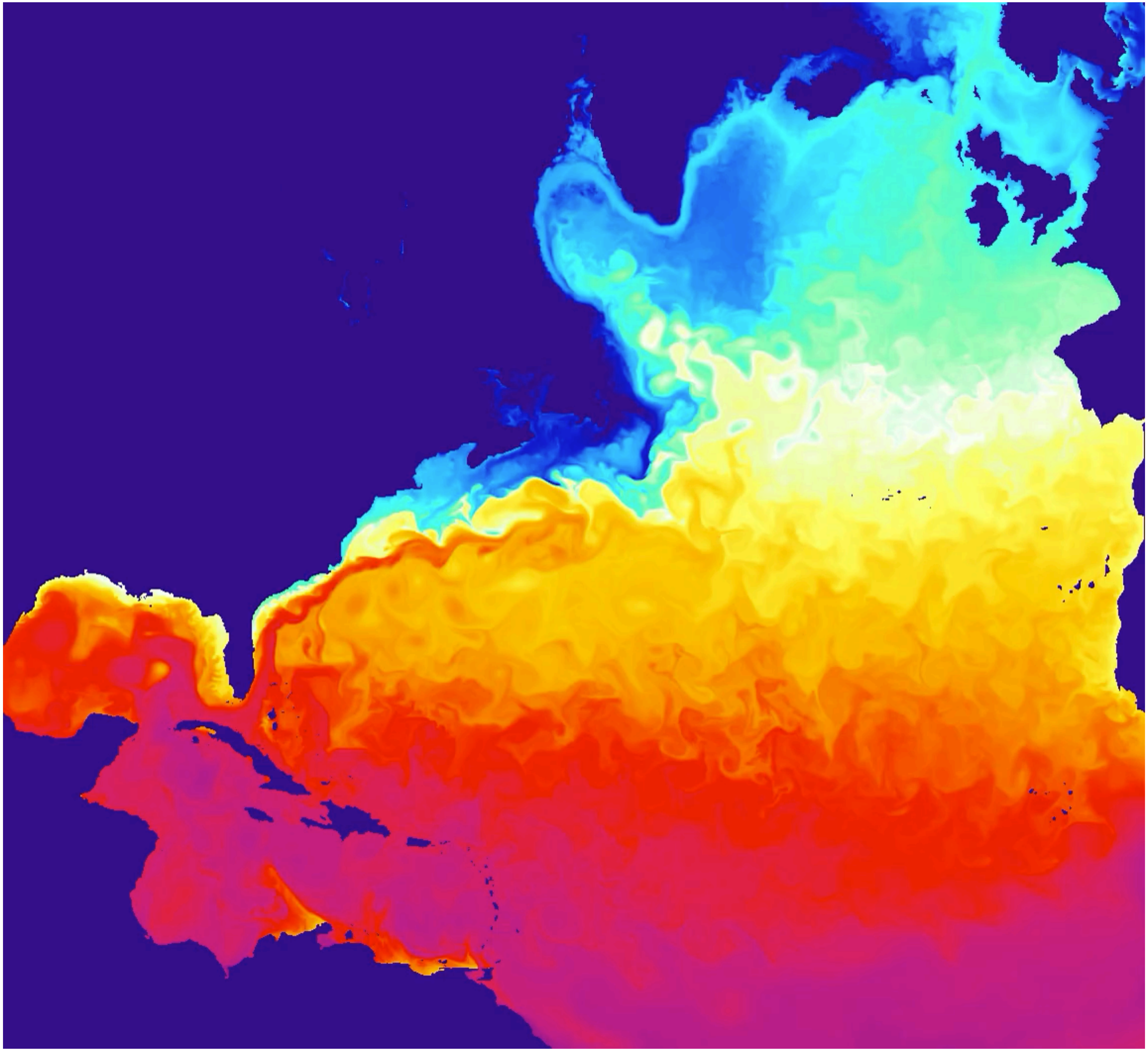
Ocean Modelling example:

Mesoscale-resolving basin-scale simulation

Typical length = 10 - 100 years

North-Atlantic coupled simulations:

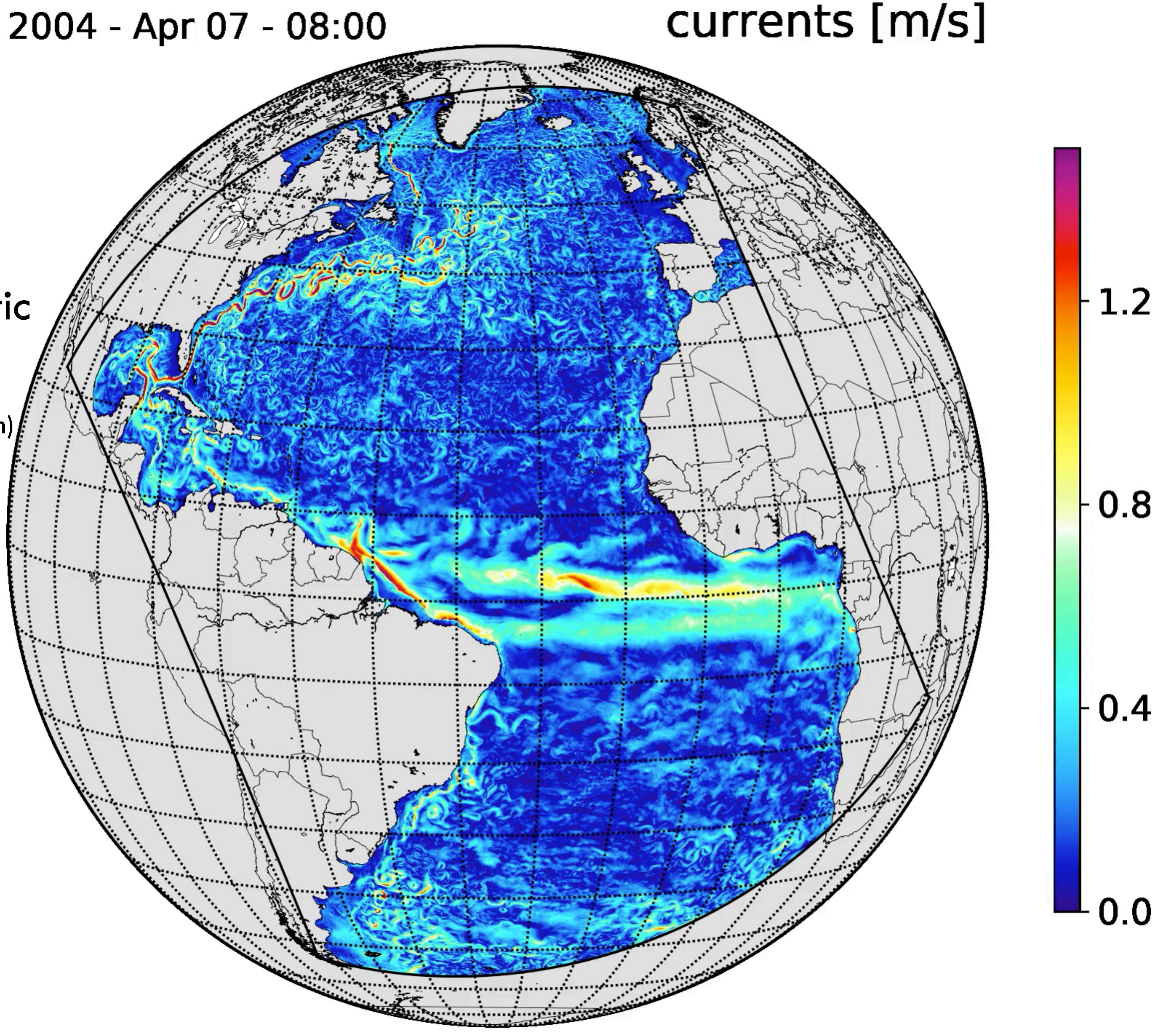
- oceanic model (6 km)
- atmospheric model (18 km)



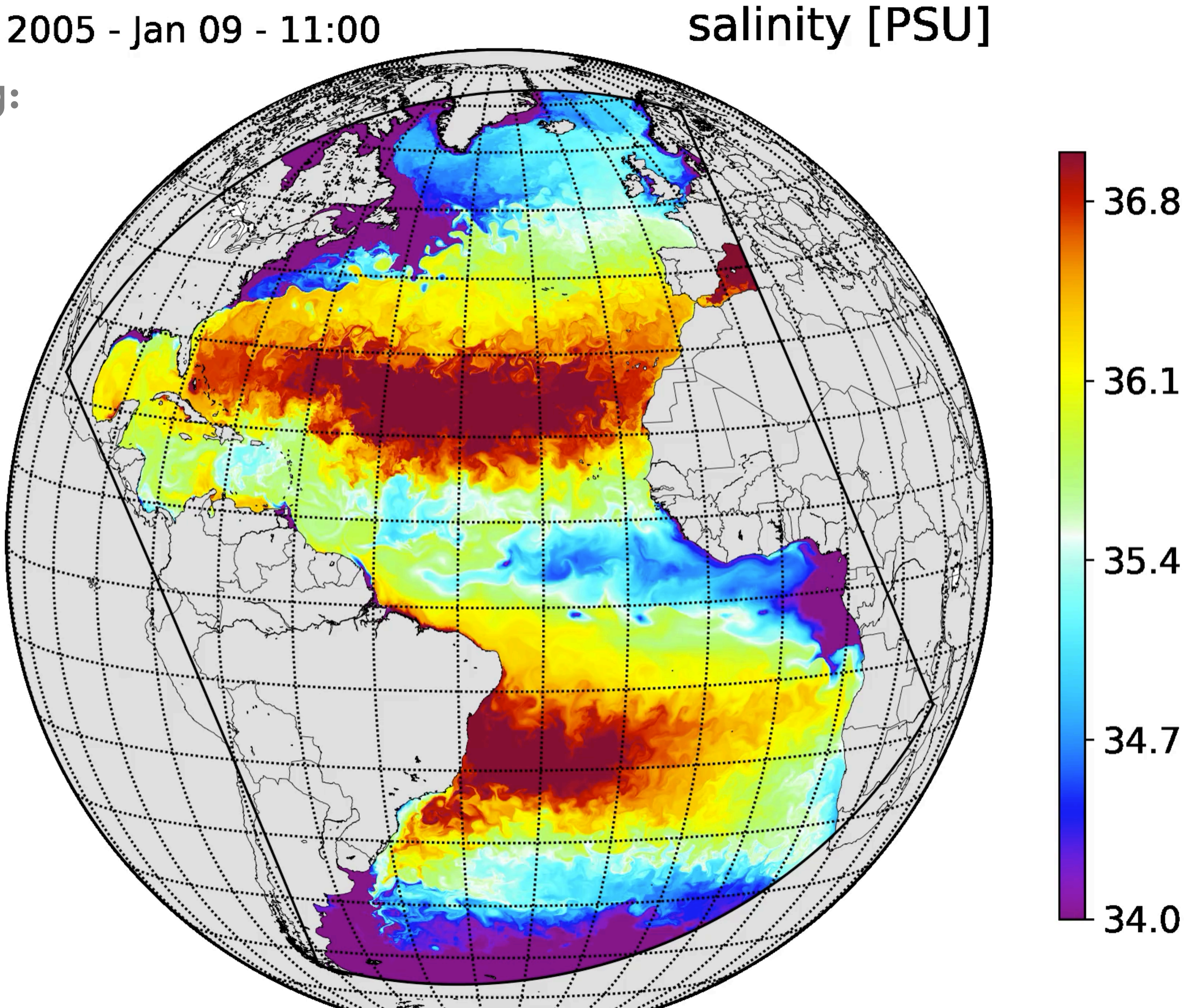
Realistic Modelling:

Forced Atlantic simulations:

- oceanic model (3 km)



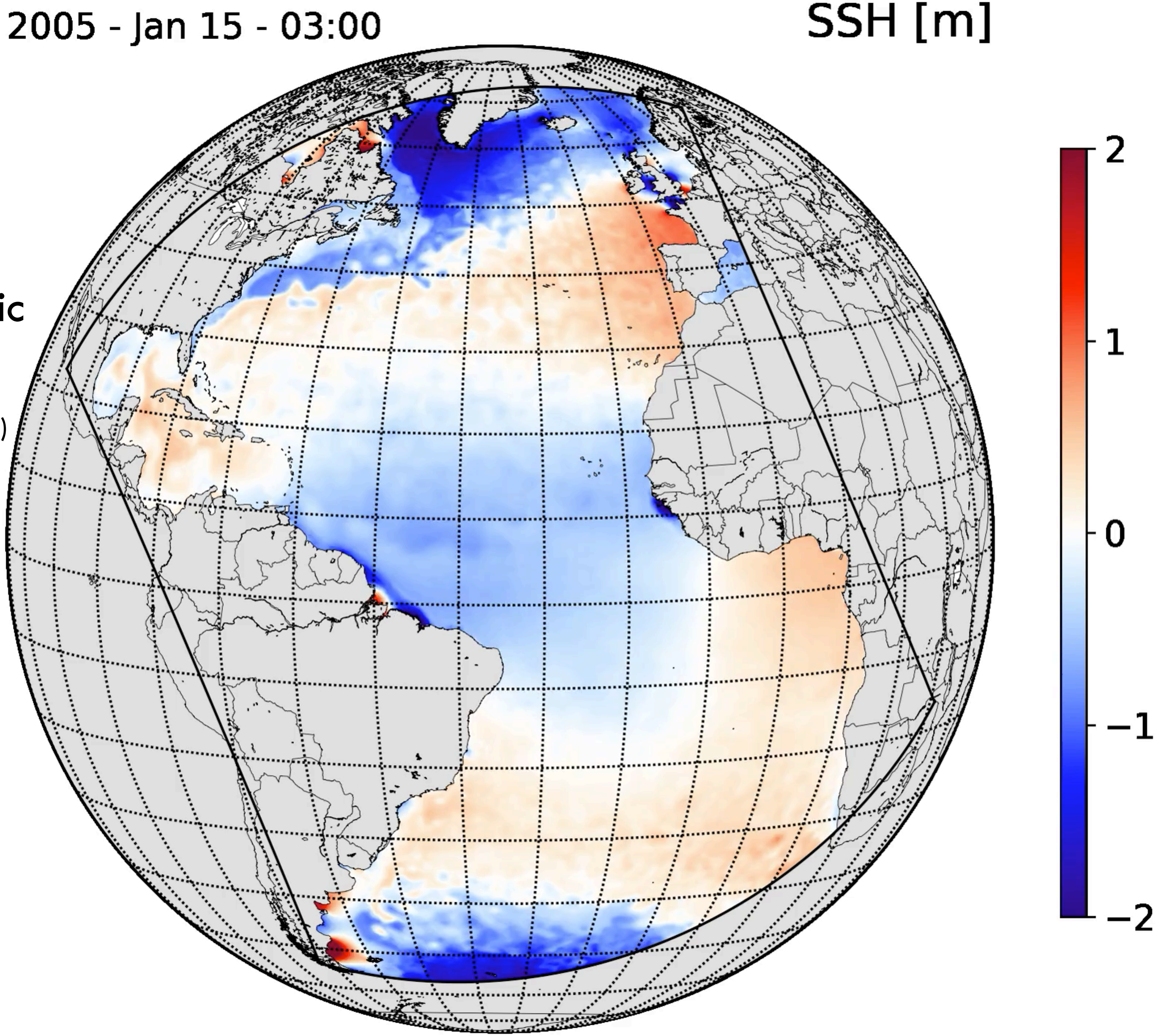
Realistic Modelling:



Realistic
Modelling:

Forced Atlantic
simulations:

- oceanic model (3 km)



Realistic Modelling:

Forced Atlantic simulations:

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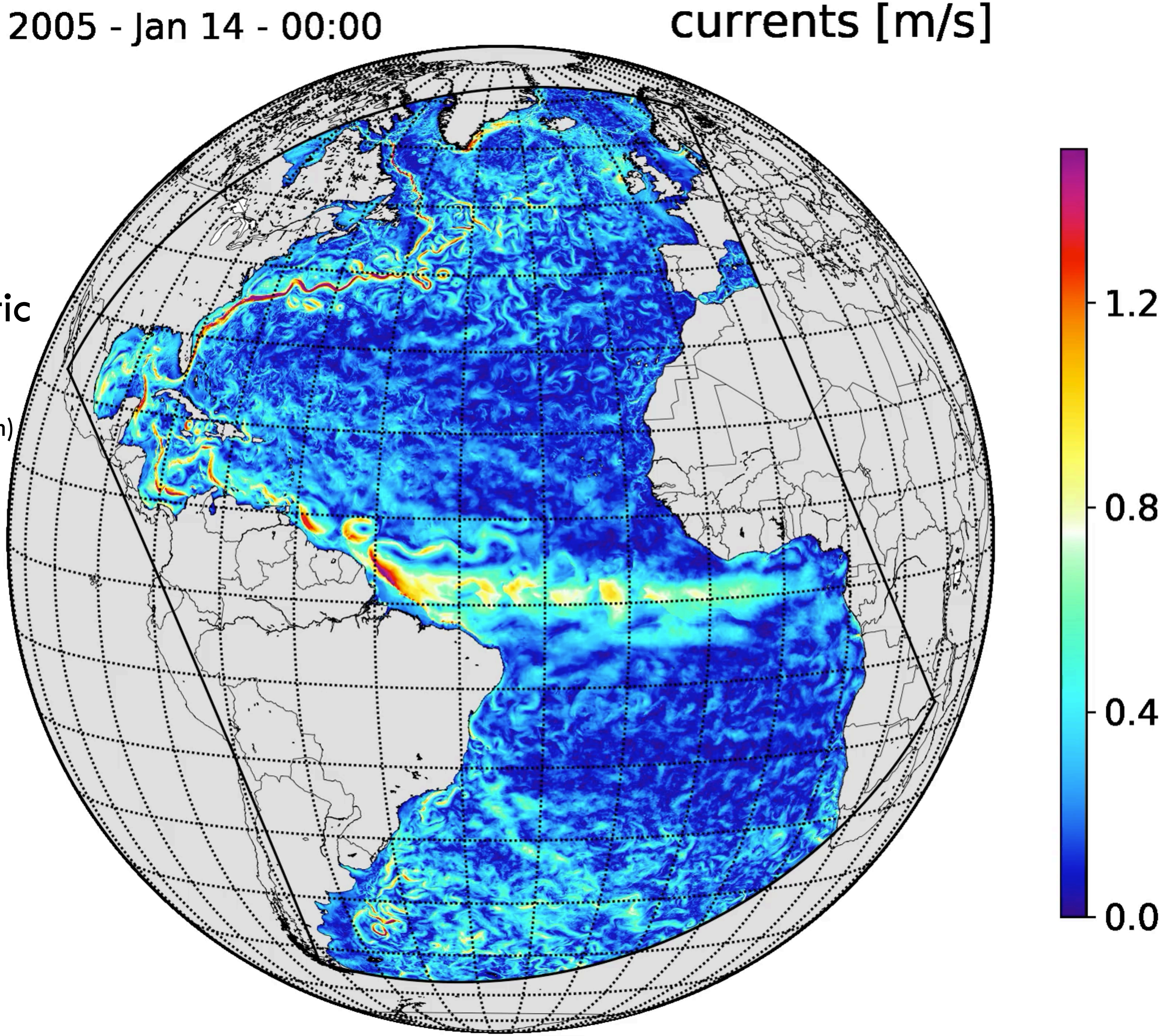


Basin-scale configuration **GIGATL**

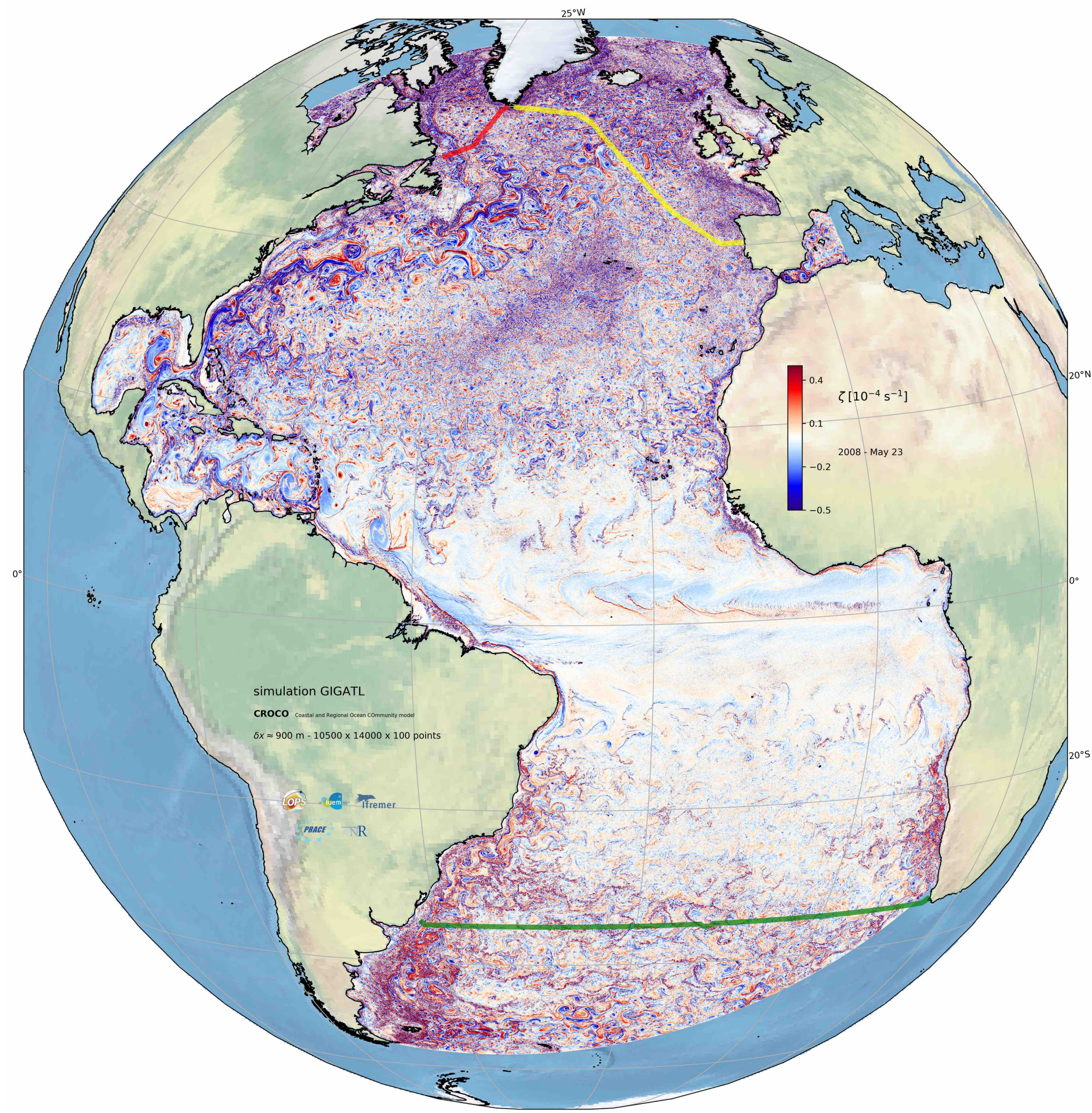
Submesoscale-permitting basin-scale simulation

Typical length = 1 year

Horizontal resolutions up to **0.75 - 1 km** with 100 topography following levels (refined at the bottom)
= 10500 x 14000 x 100 points

including **hourly surface forcings and tides**.

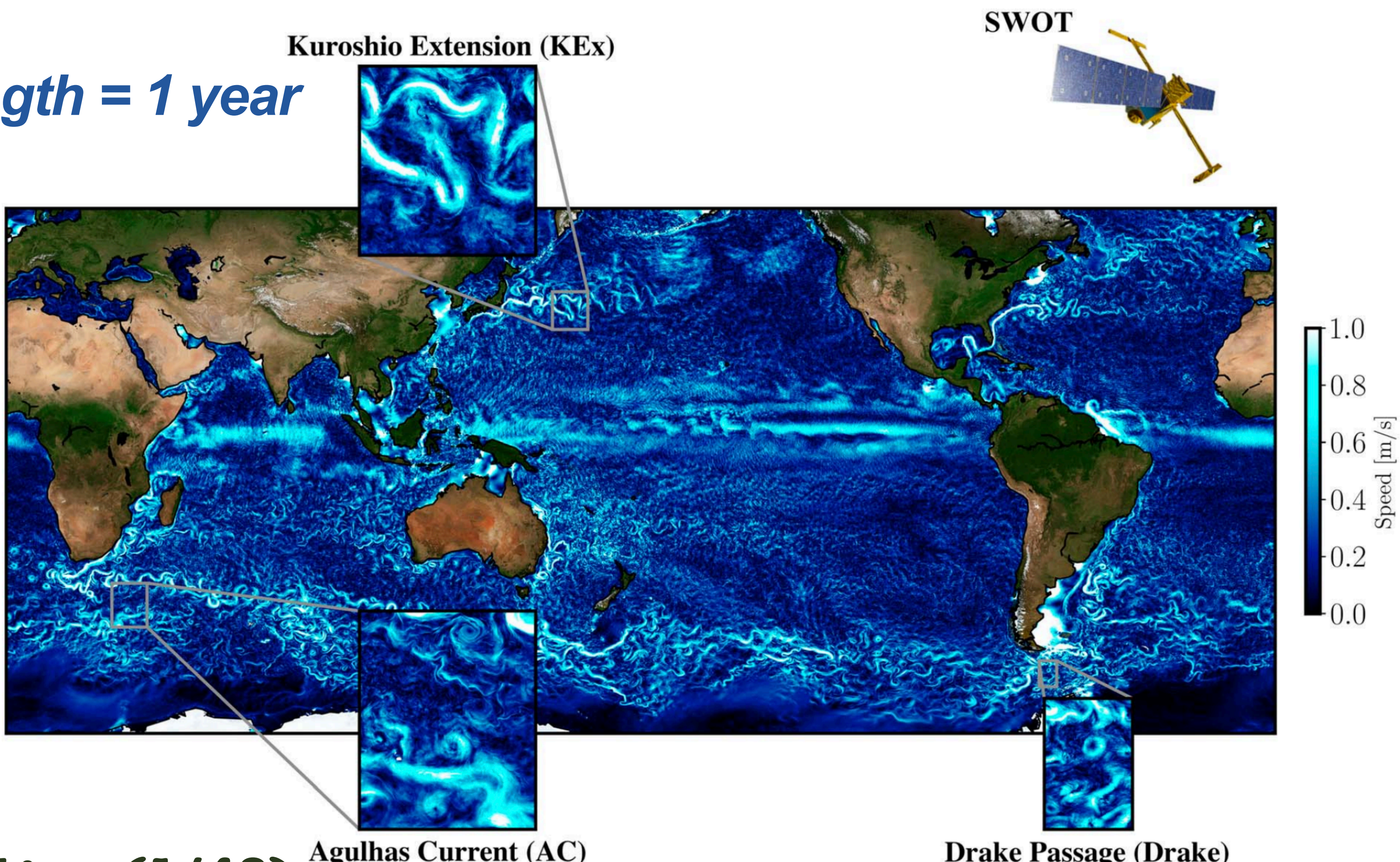
Run on 10000 processors - 40M cpu-hours - About 4PB of data



Global configuration LLC4320

Submesoscale-permitting global simulation

Typical length = 1 year

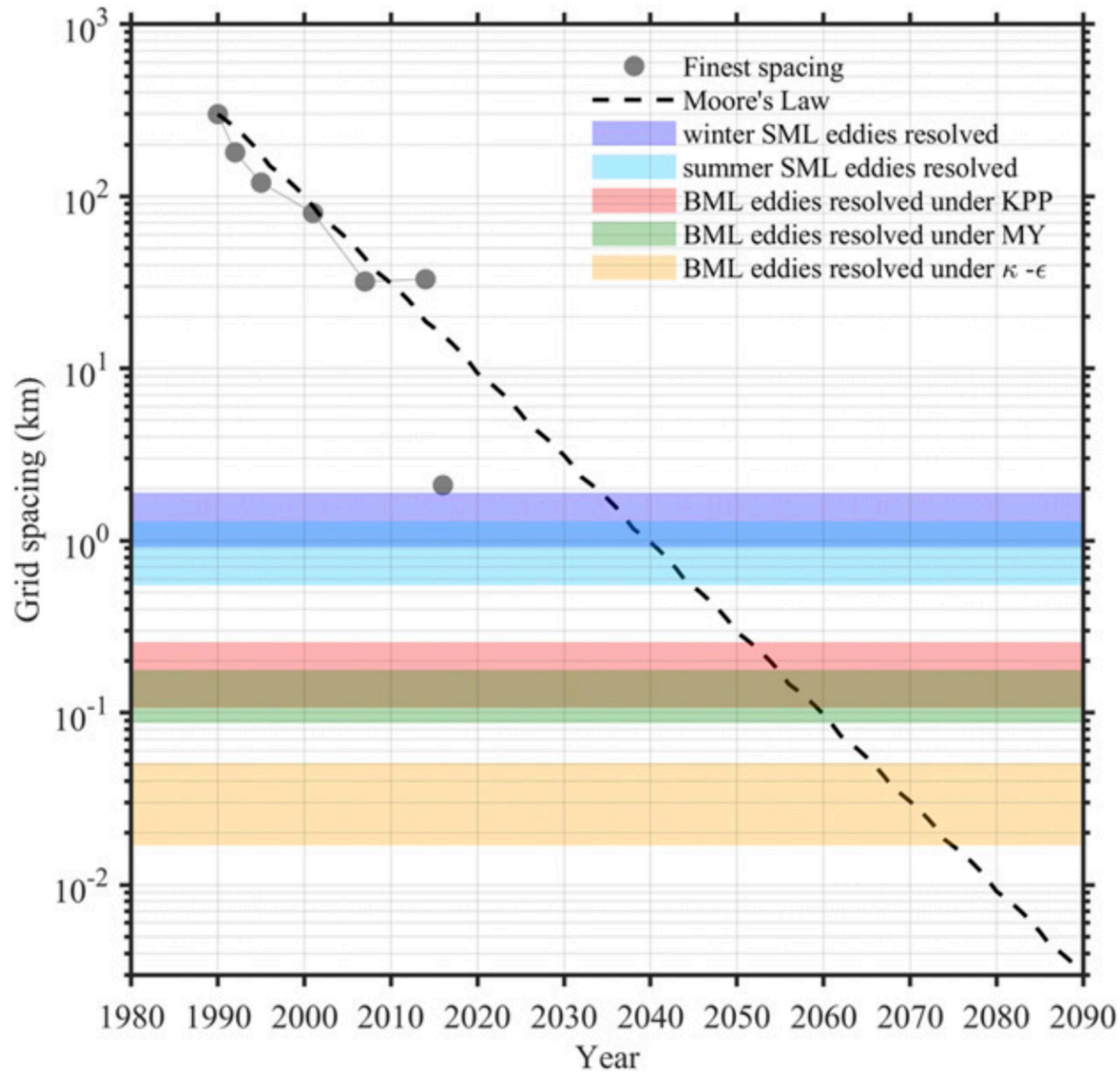


Model MITgcm (1/48)

[Torres et al, 19]

Estimate of horizontal grid spacings of the IPCC ocean models

- The gray dots denote the finest grid spacings reported by the IPCC reports by year of publication, except the latest one from the ECCO MITgcm LLC4320 simulation.
- The black line denotes the estimate predicted by Moore's Law, while the shaded regions denote the grid spacing intervals resolving 50% and 90% of surface mixed-layer eddies globally based on the observations and bottom mixed-layer eddies based on simulations.

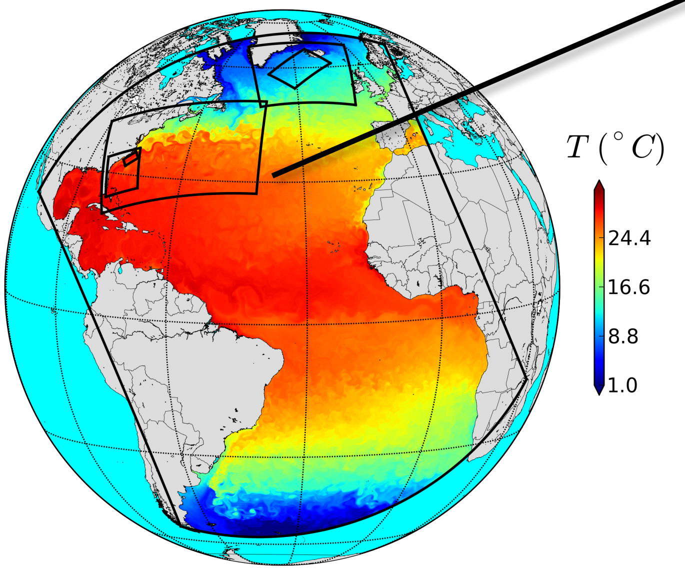


Dong et al. (2020)

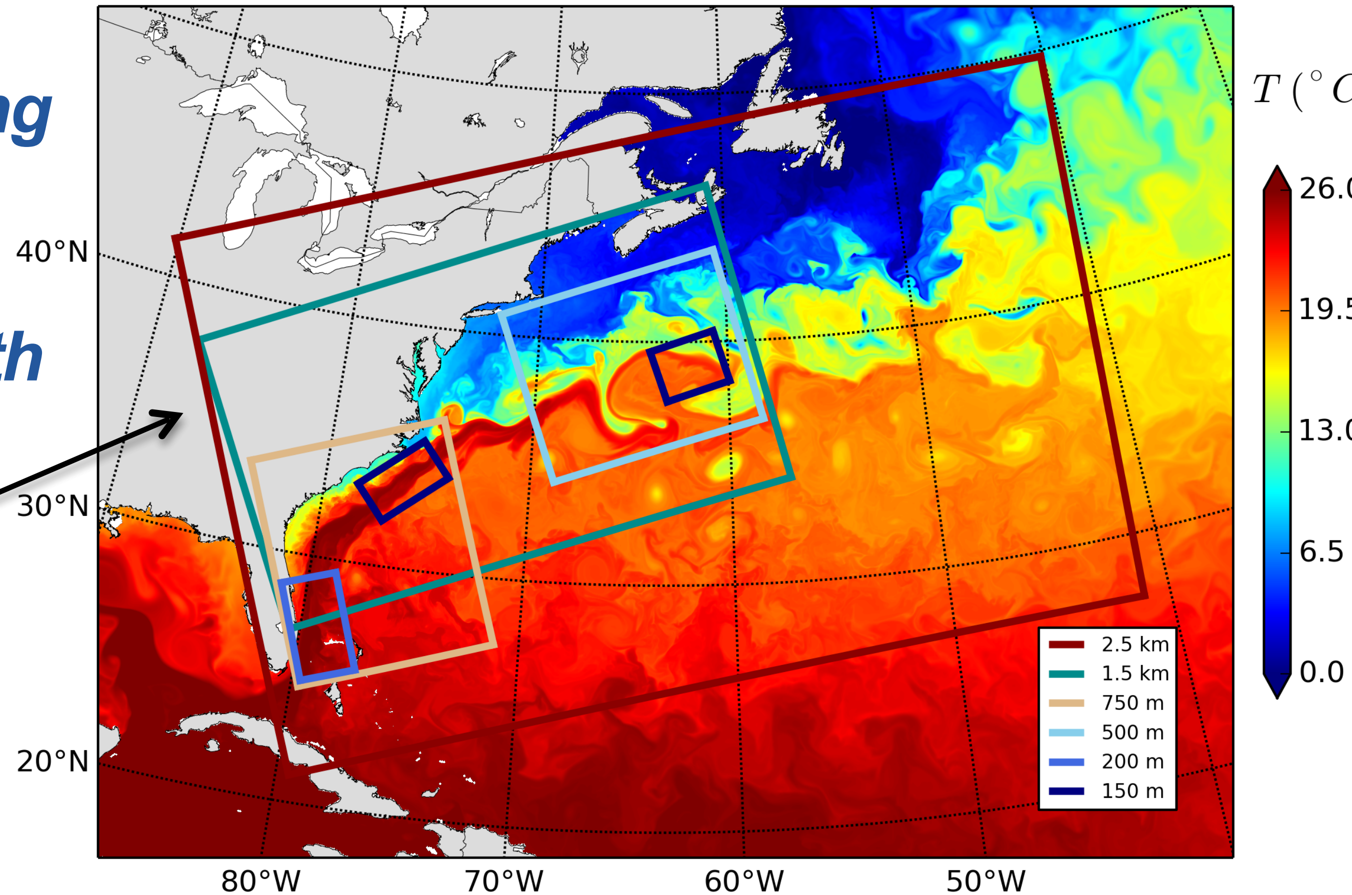
Ocean Modelling examples:

Submesoscale-resolving regional simulation

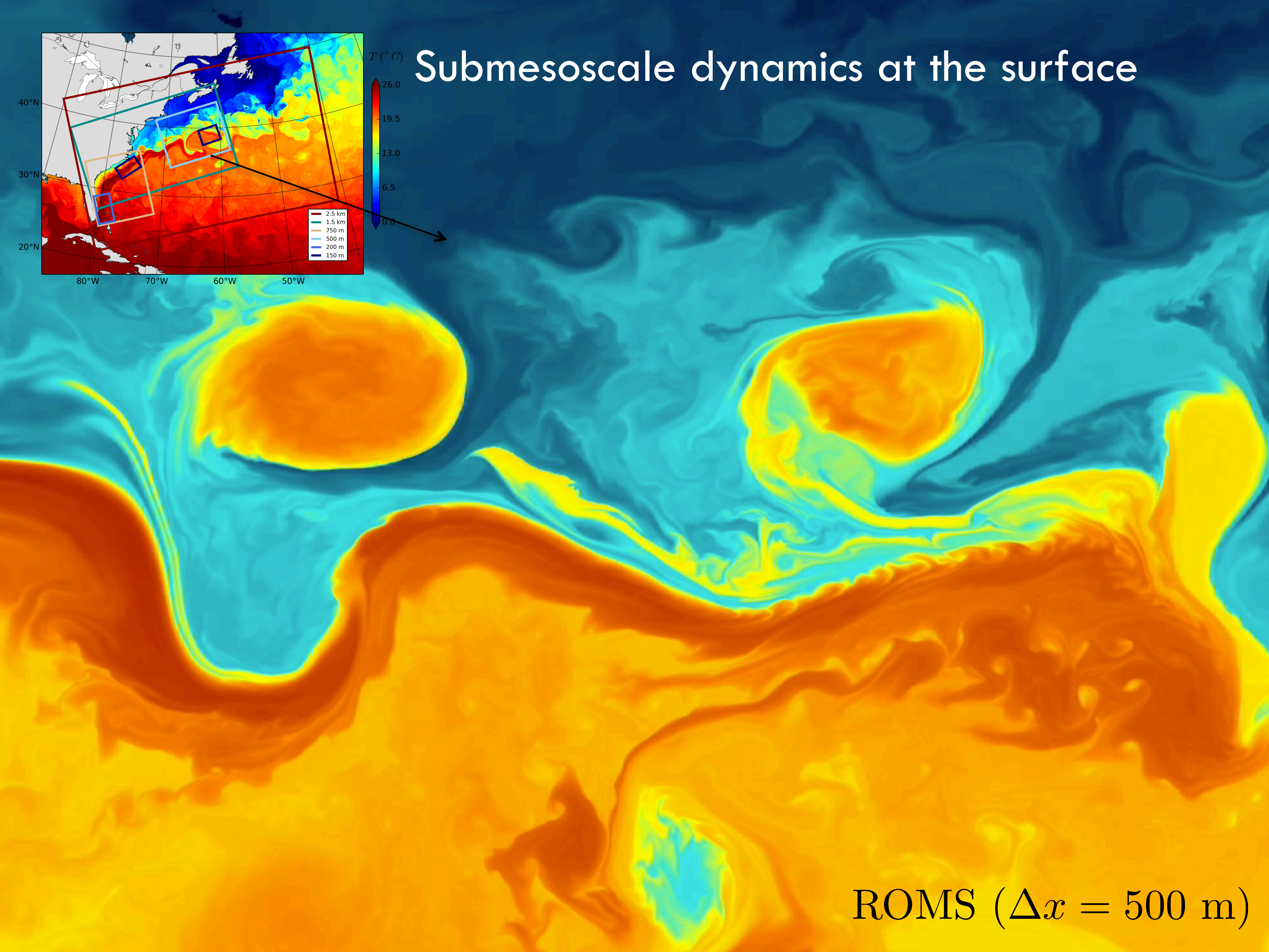
Typical length = 1 month 10 years

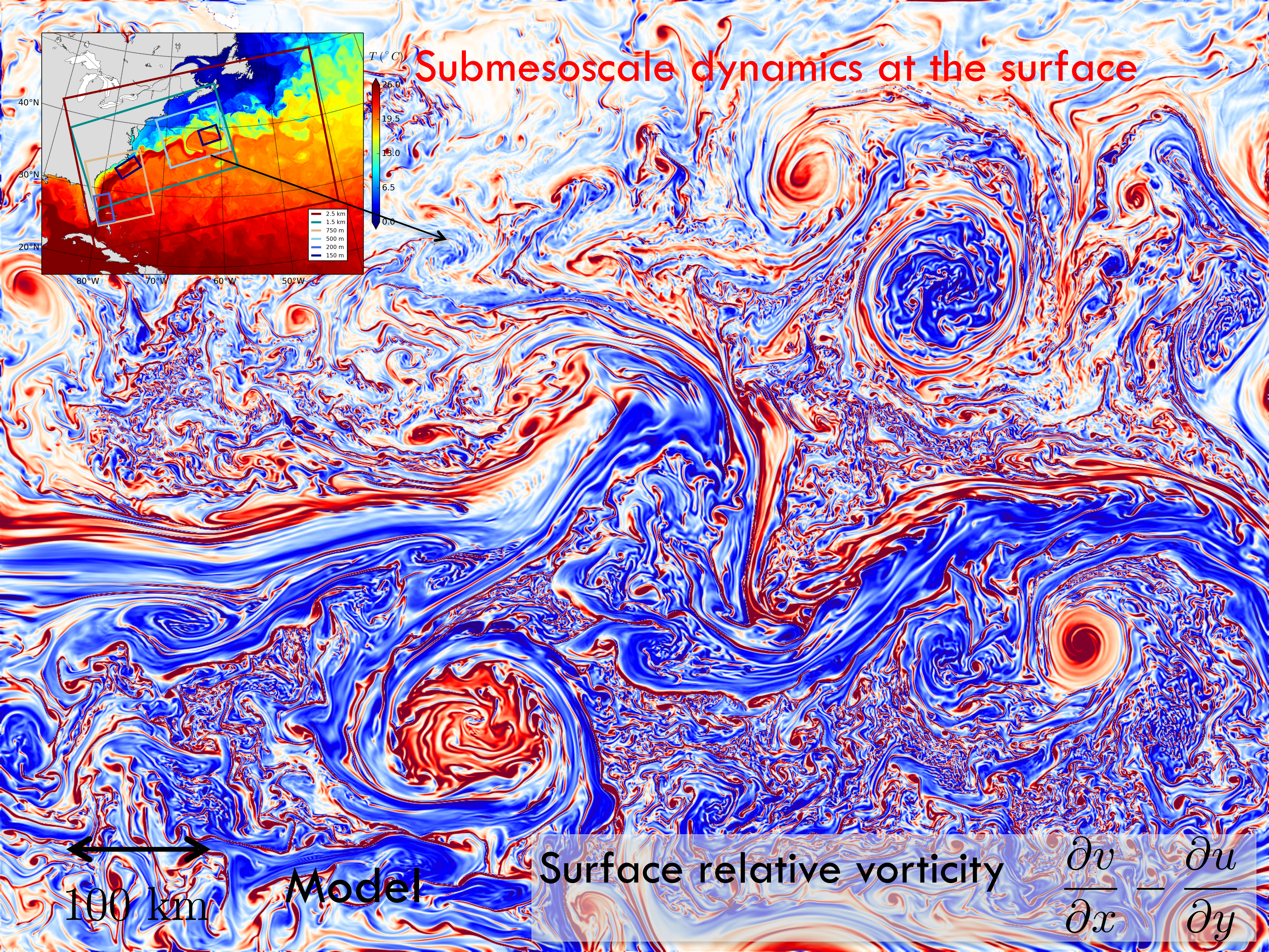


$$\Delta x = 6 \rightarrow 0.15 \text{ km}$$



A portion of the Atlantic domain showing mean SST and several (1-way) nested grids:


Submesoscale dynamics at the surface
$T\,(^{\circ}C)$
26.0
19.5
13.0
6.5
0.0
40°N
30°N
20°N
80°W
70°W
60°W
50°W
2.5 km
1.5 km
750 m
500 m
200 m
150 m
ROMS ($\Delta x = 500$ m)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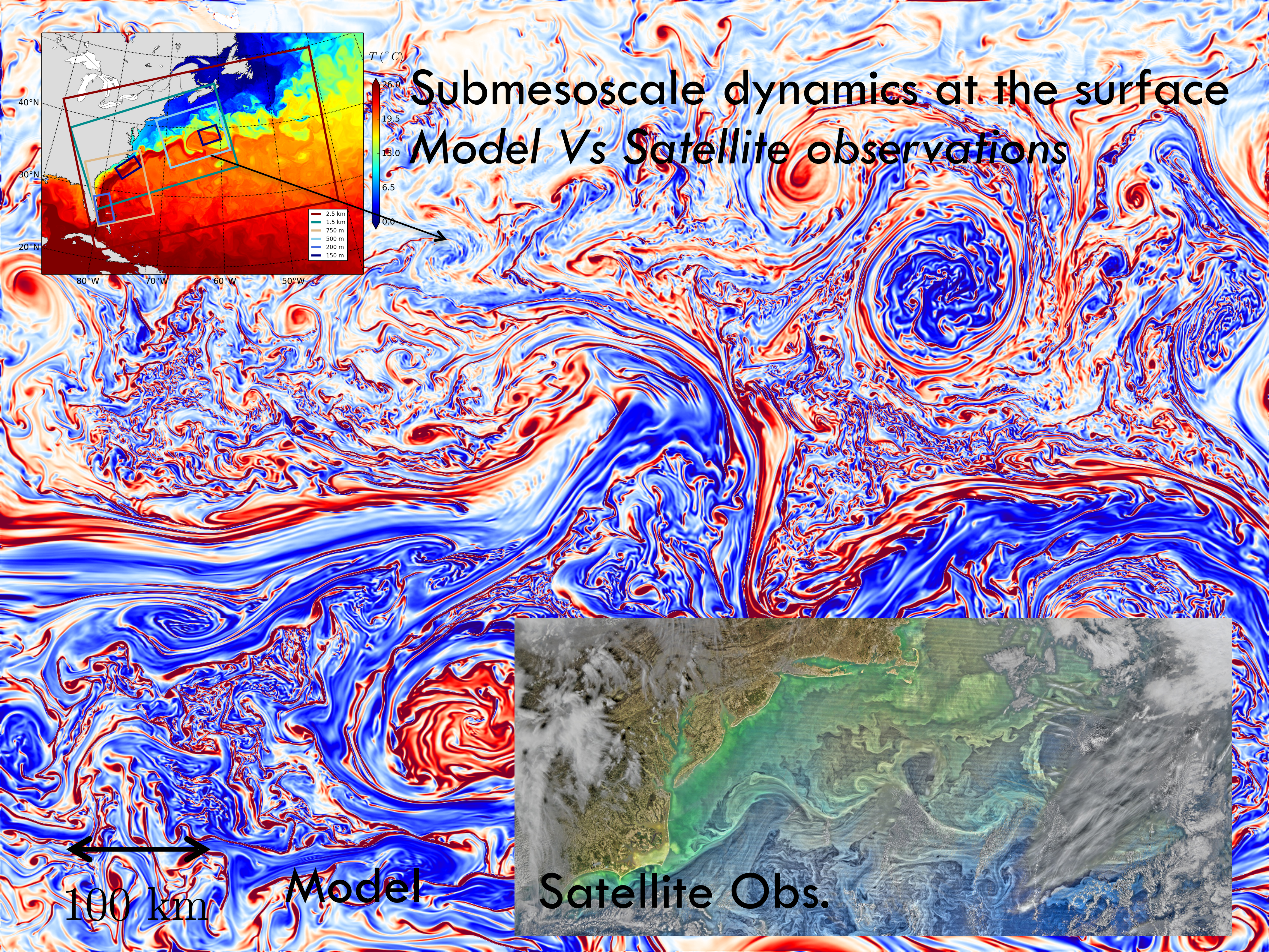
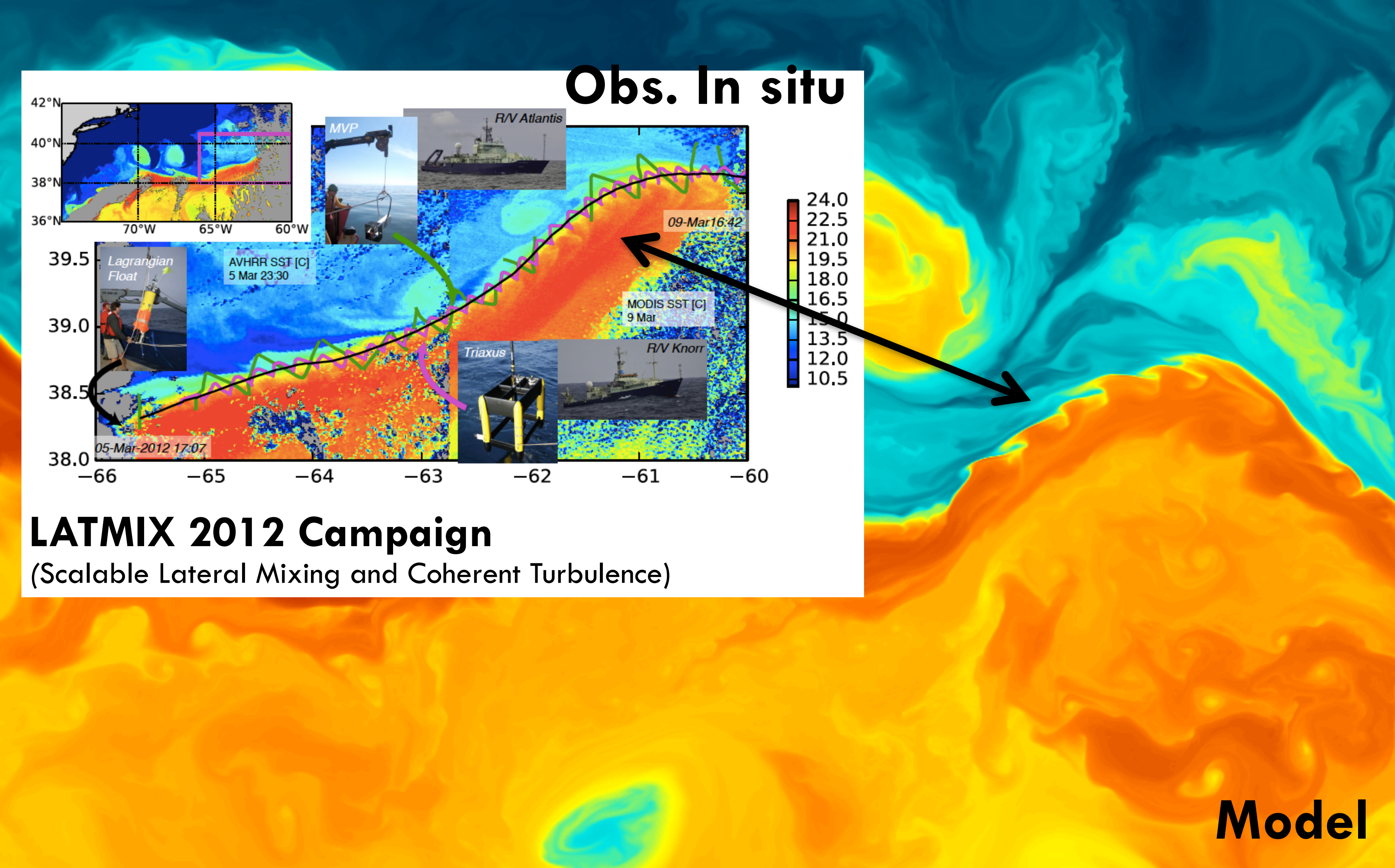
40°N
30°N
20°N
80°W
70°W
60°W
50°W
2.5 km
1.5 km
750 m
500 m
200 m
150 m
100 km
Model
Surface relative vorticity $\frac{\partial v}{\partial x} - \frac{\partial u}{\partial y}$



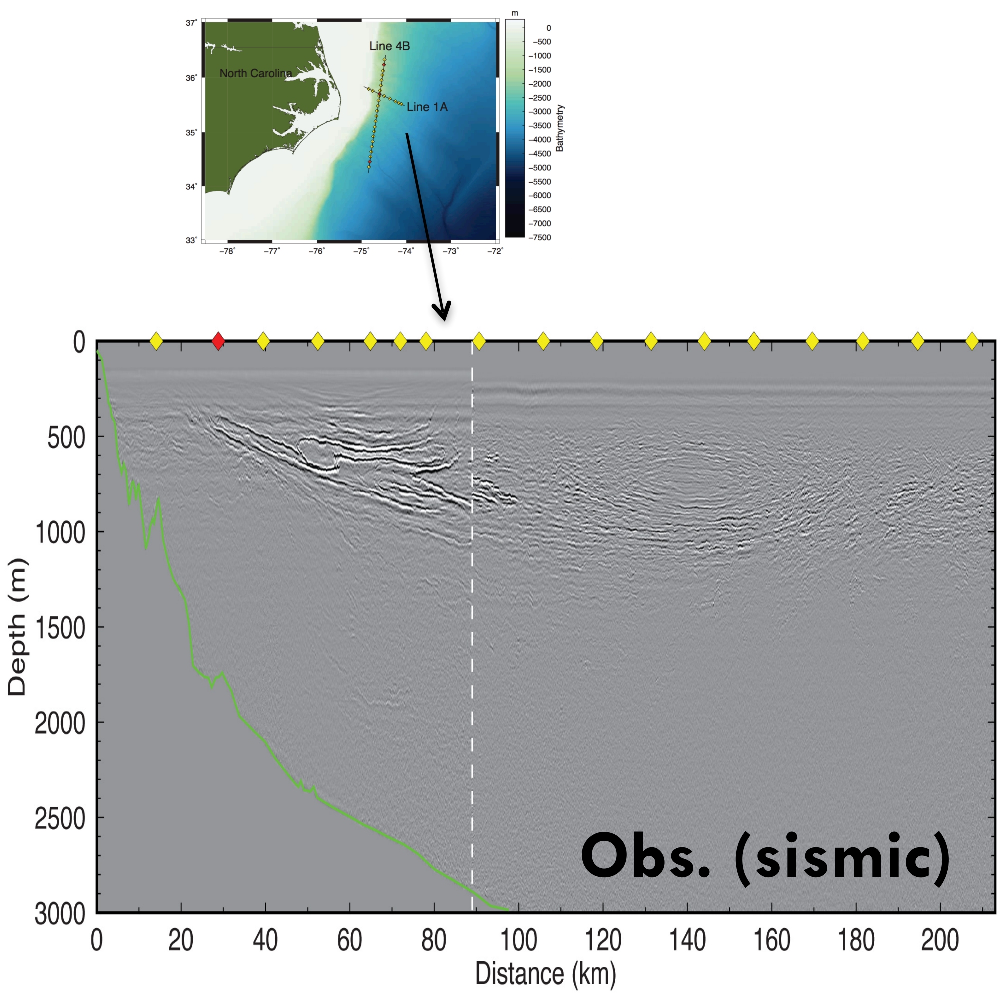
Submesoscale dynamics at the surface
Model Vs Satellite observations
T(°C)
26.0
19.5
13.0
6.5
0.0
40°N
30°N
20°N
80°W
70°W
60°W
50°W
2.5 km
1.5 km
750 m
500 m
200 m
150 m
100 km
Model
Satellite Obs.

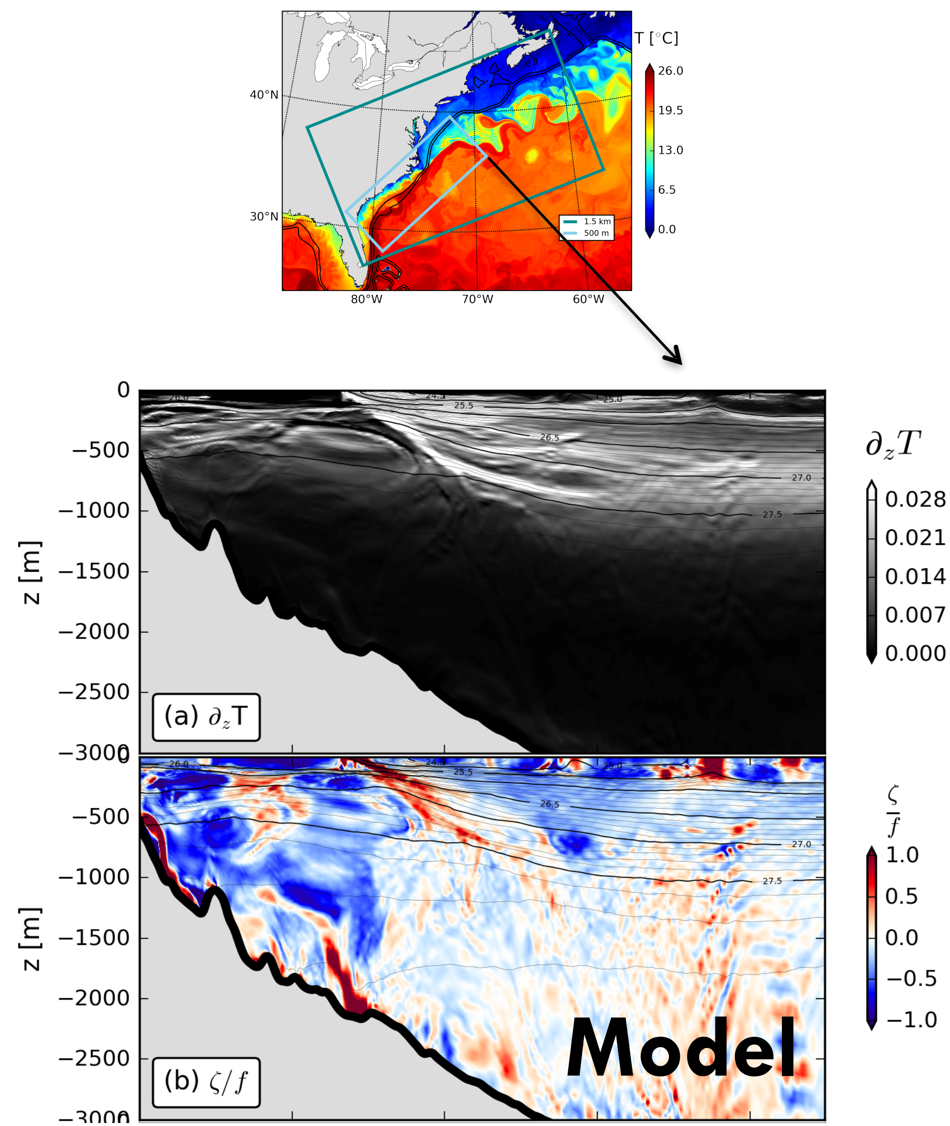
Submesoscale dynamics at the surface
Model Vs Satellite observations



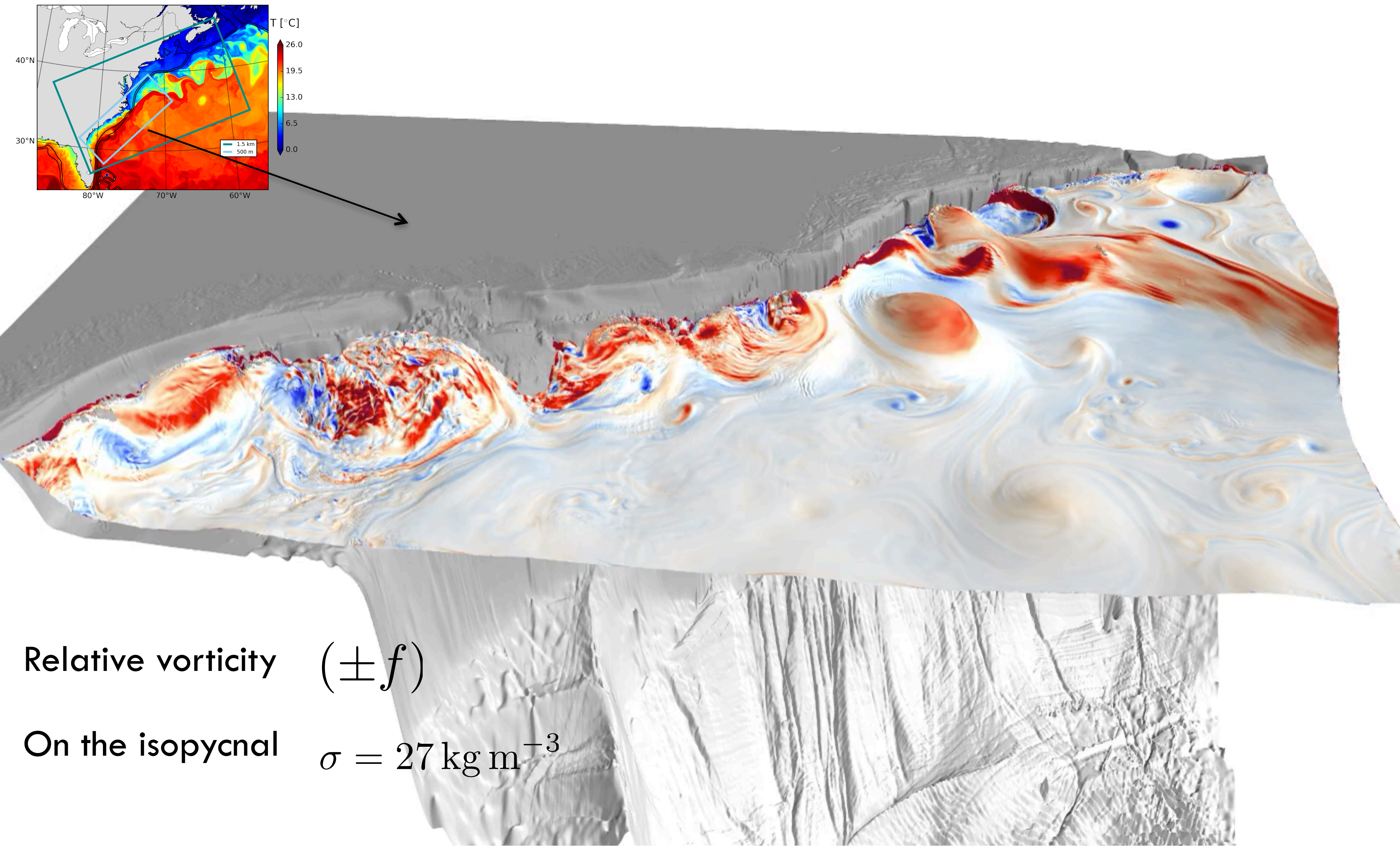
Submesoscale dynamics in the interior

- Generation of submesoscale coherent vortices:





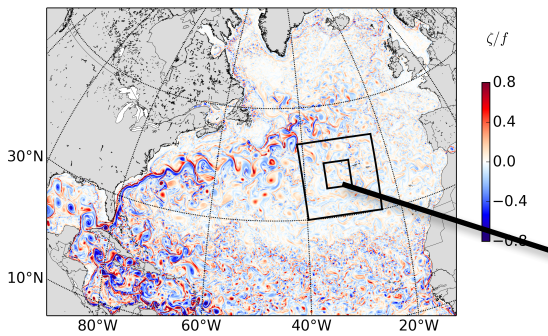
Submesoscale dynamics in the interior

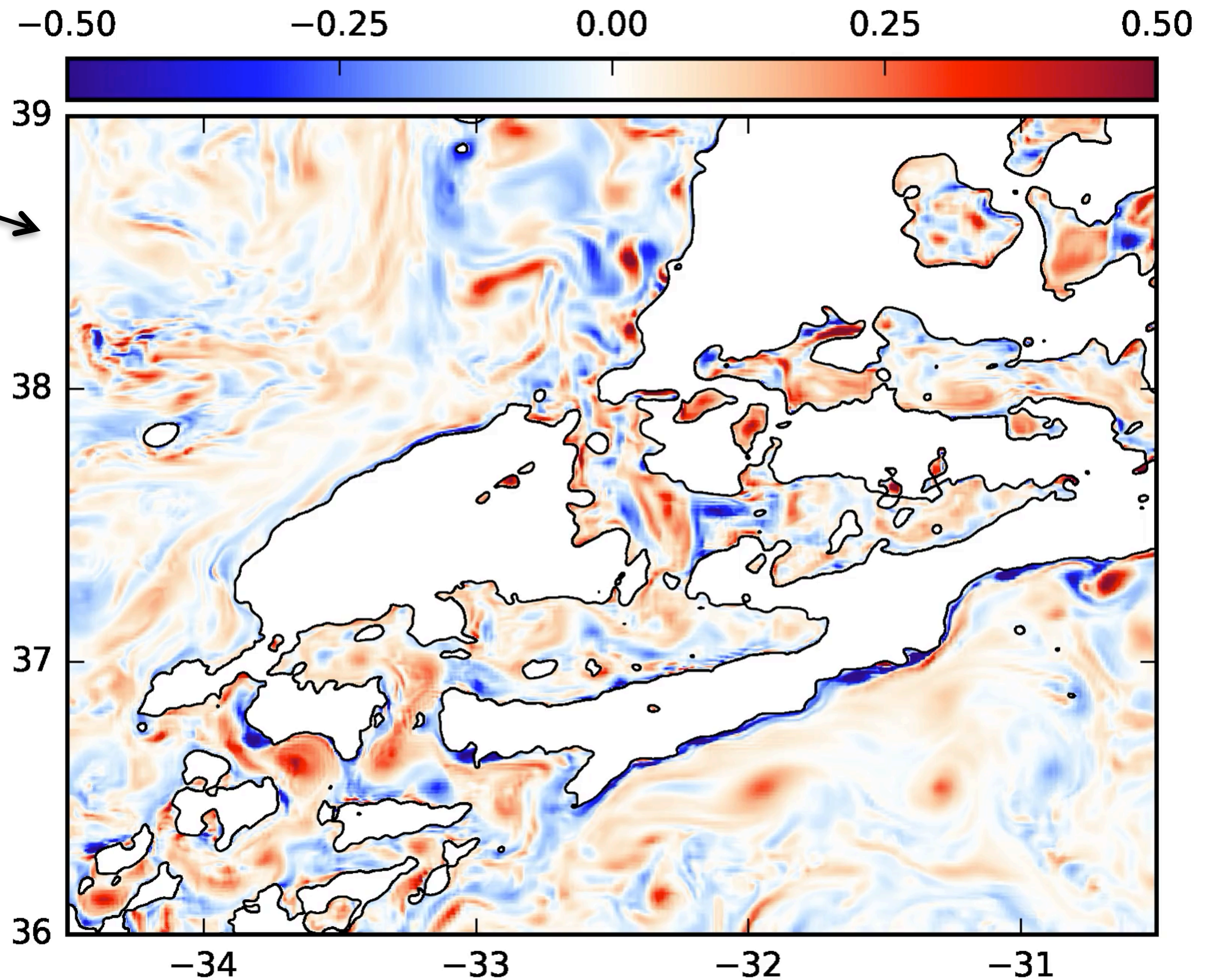


Relative vorticity $(\pm f)$

On the isopycnal $\sigma = 27\,\mathrm{kg\,m^{-3}}$

Submesoscale dynamics in the Abyss!



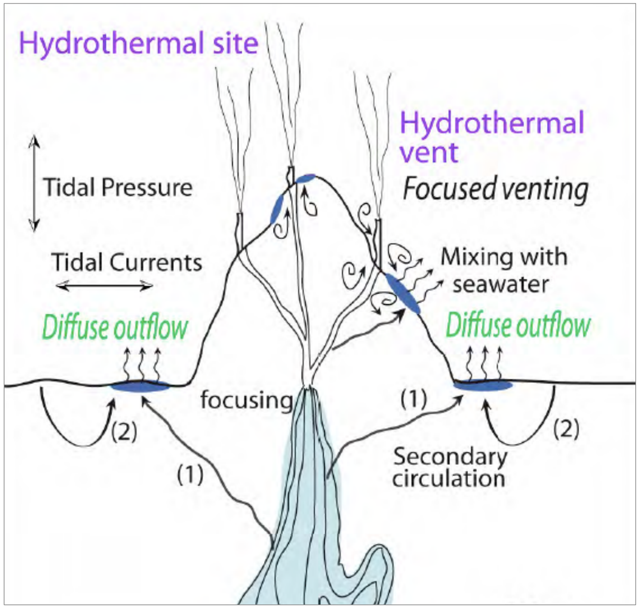


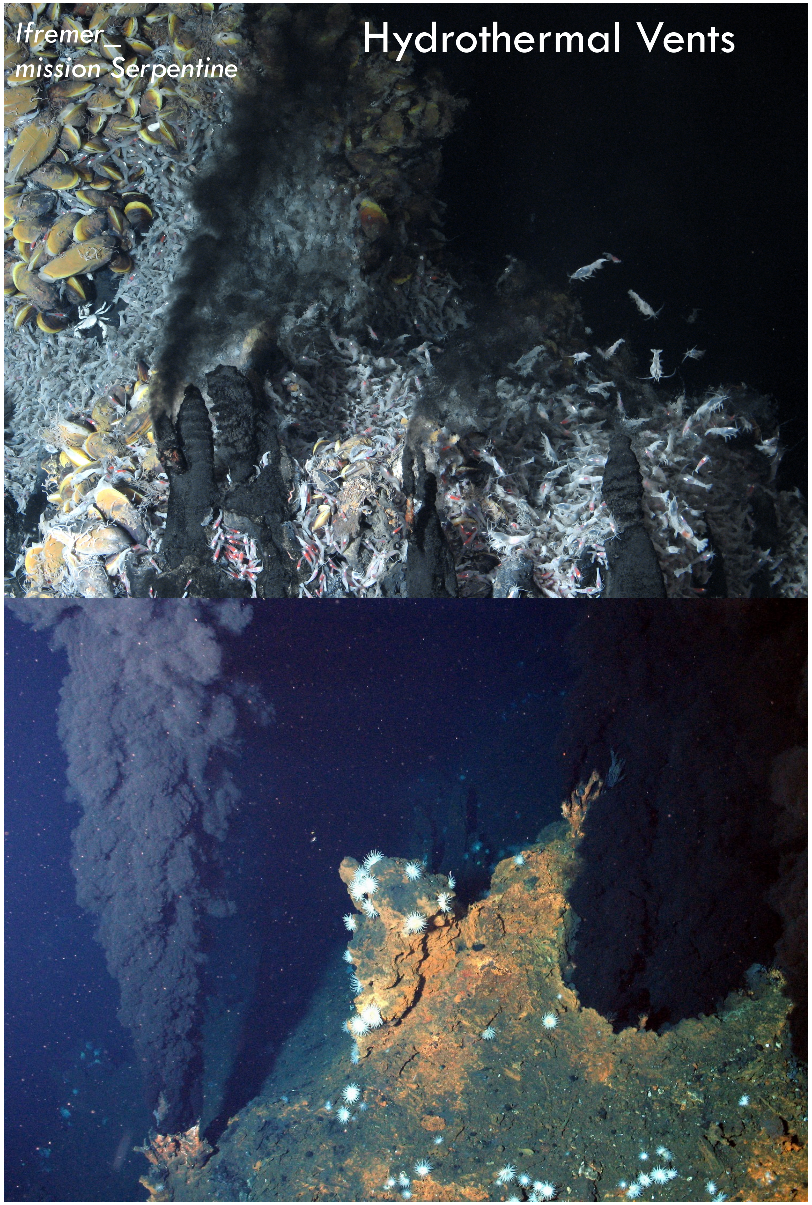
$$\Delta x = 500\,\mathrm{m}$$

relative vorticity at -1800 m

And the abyssal turbulence impacts a lot of things:

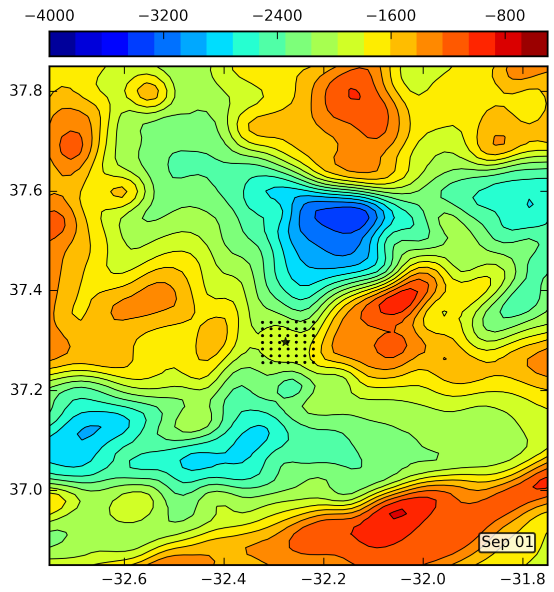
- *Dispersion of hydrothermal effluents*
- *Transport of biogeochemical tracers*
- *Connectivity between deep ecosystems*

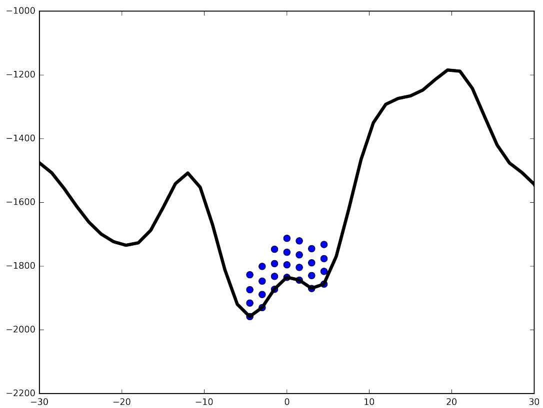


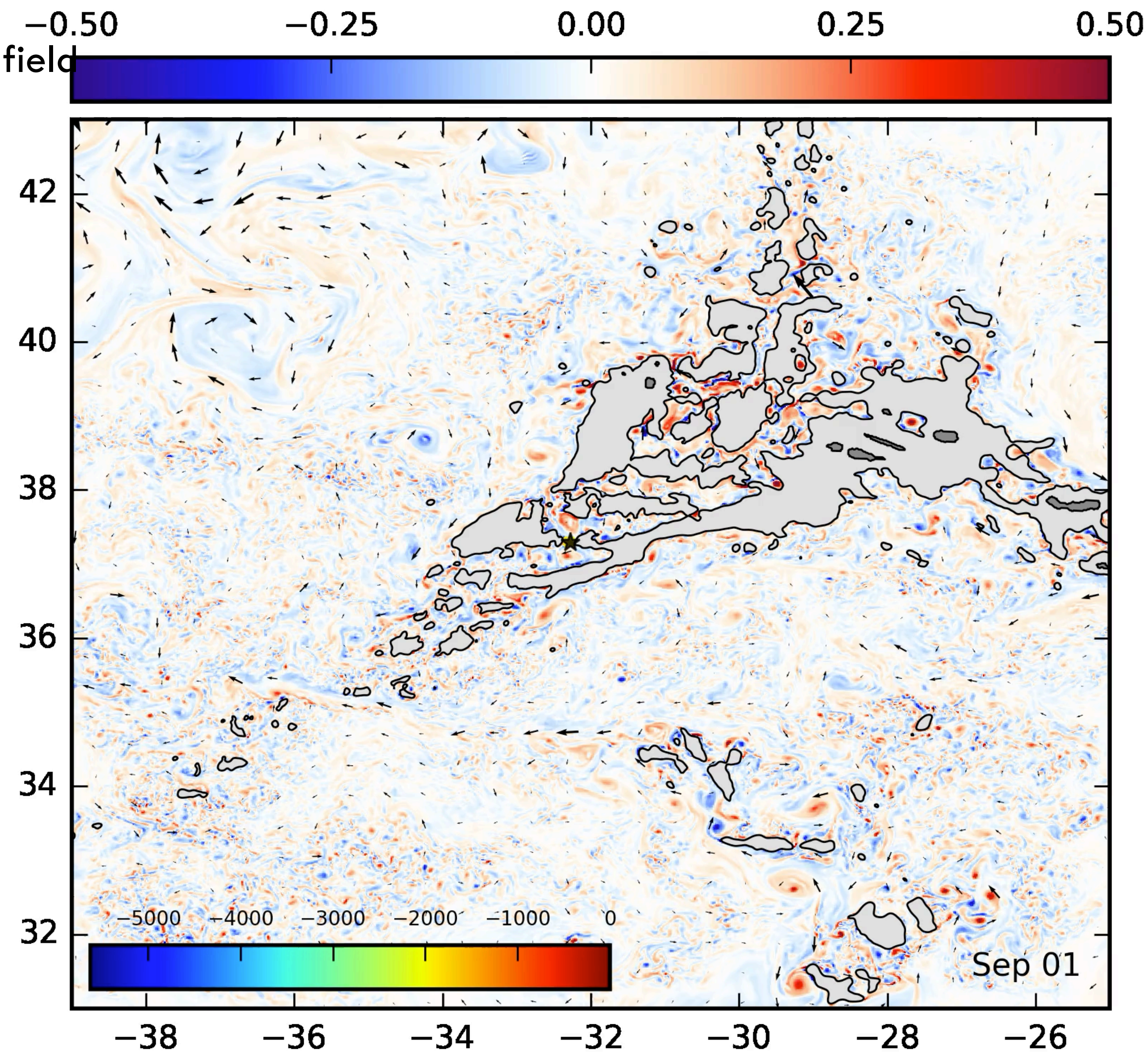


Dispersion of larvae by abyssal turbulence

Continuous release of Lagrangian particles near the Lucky Strike vent field (1.5 km res)





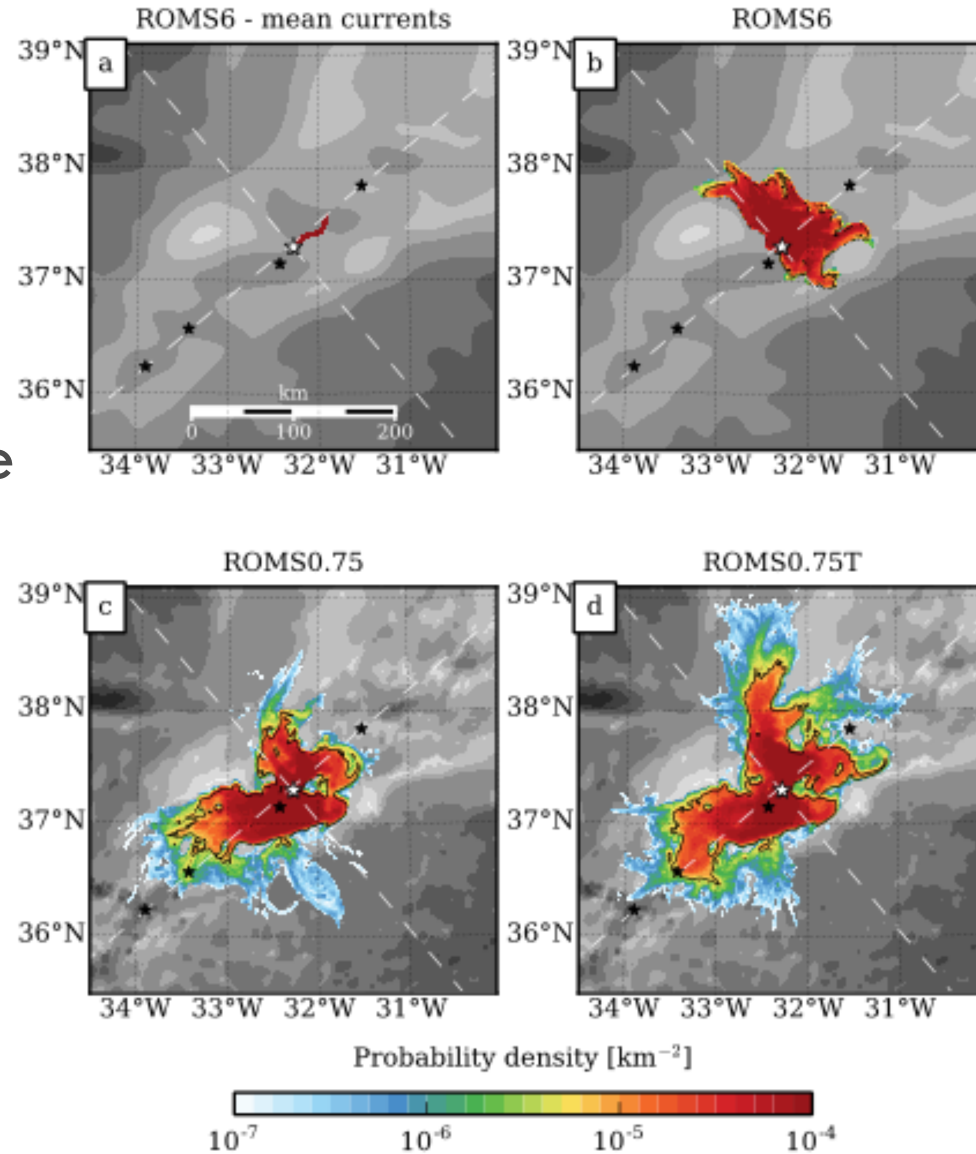


Dispersion of larvae by abyssal turbulence

Mean currents only

Mesoscale

Larvae dispersion from the Lucky Strike vent after 30 days.



Mesoscale + submesoscale

Mesoscale + submesoscale + tides

Dispersion of larvae by abyssal turbulence

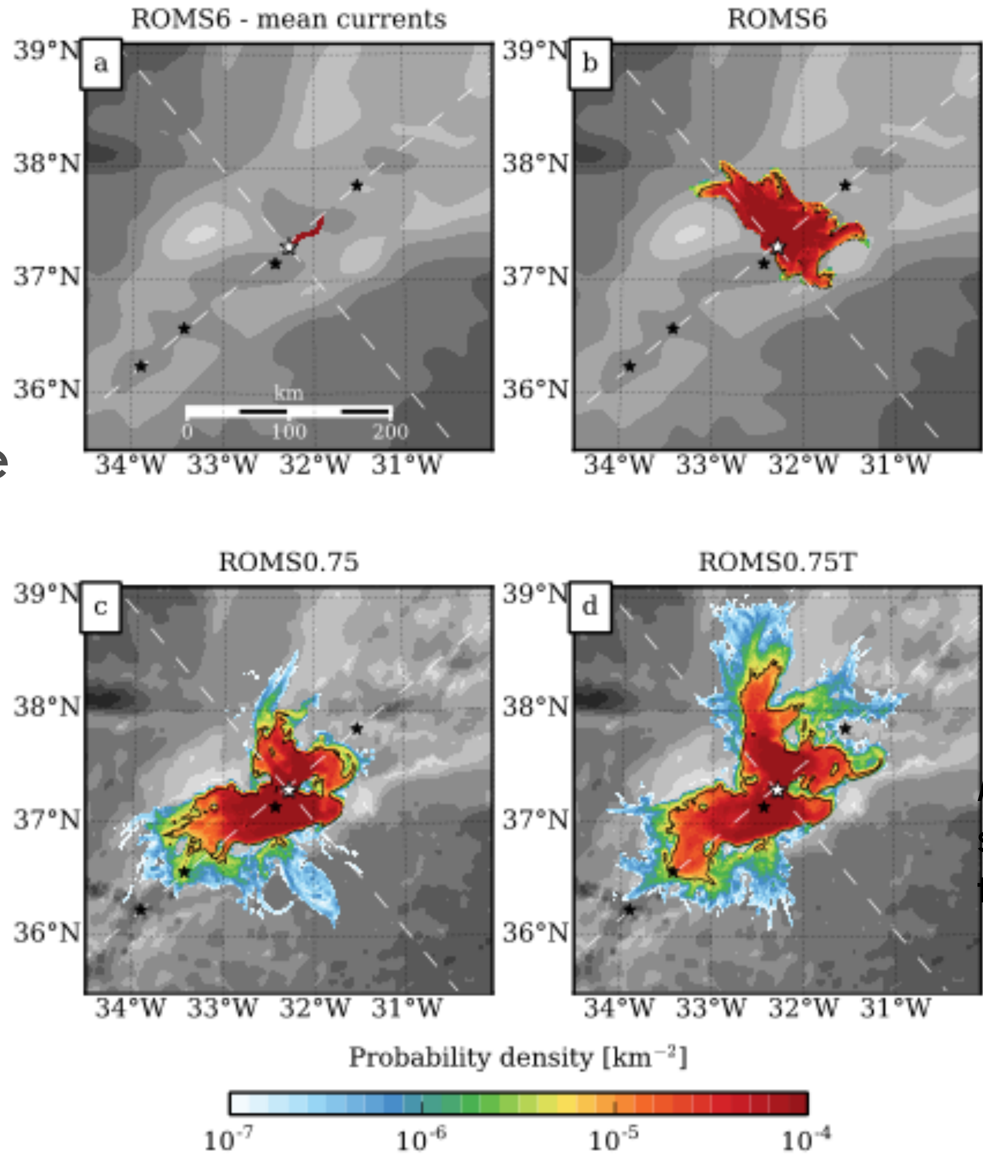
Larvae dispersion from the Lucky Strike vent after 30 days.

Mean currents only

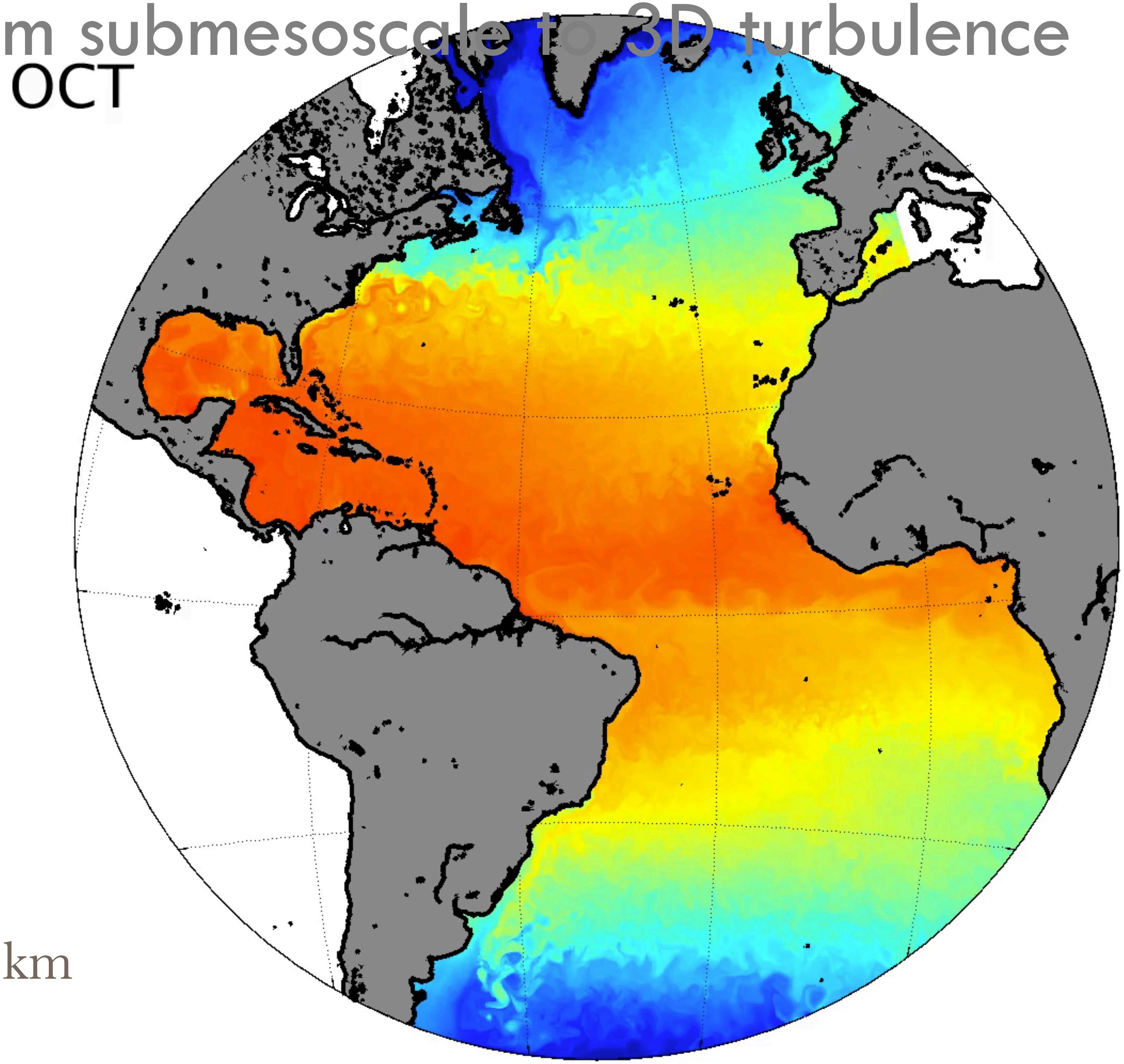
Mesoscale

Mesoscale + submesoscale

Mesoscale + submesoscale + tides



From submesoscale to 3D turbulence

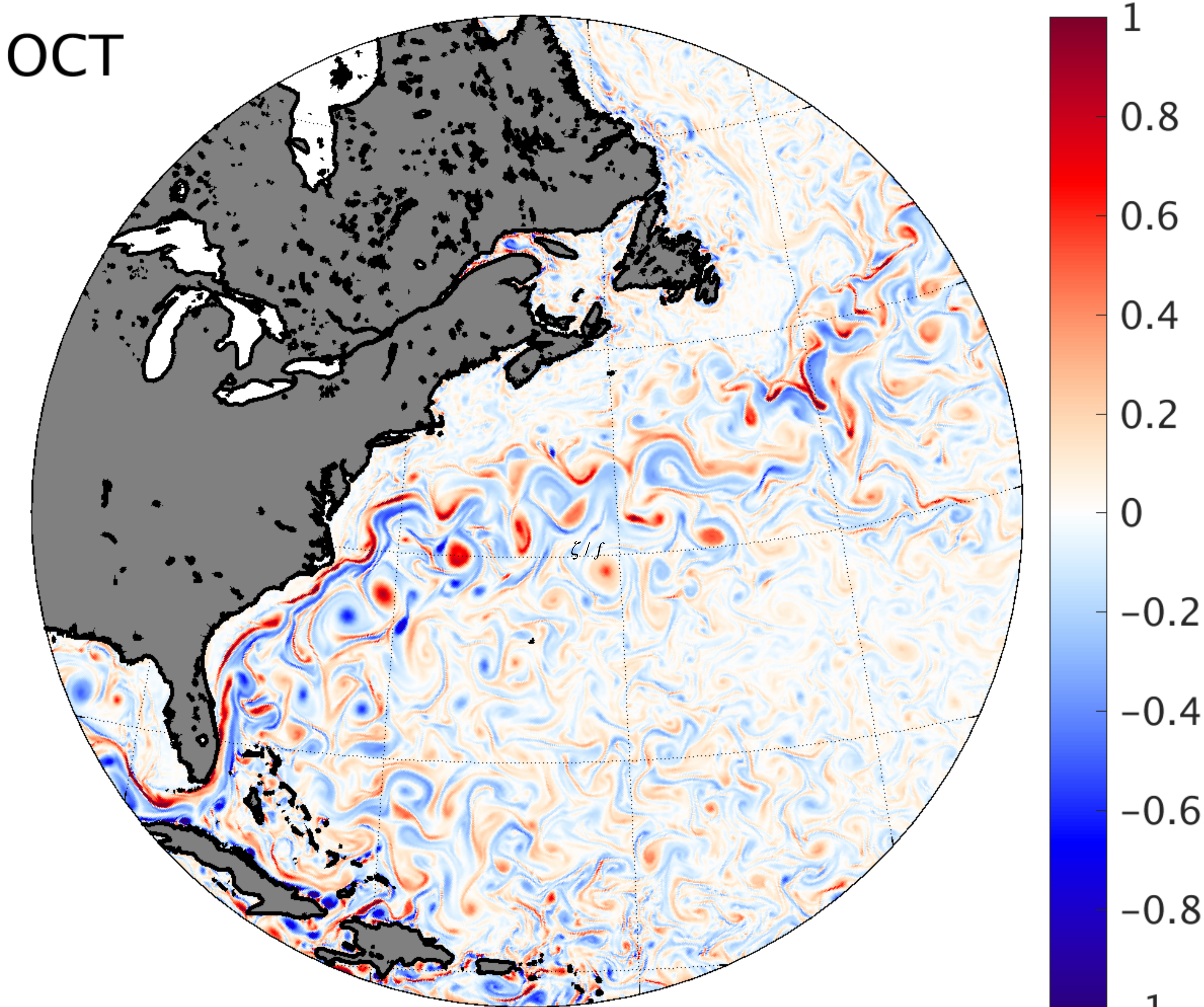


dx = 5-7 km

SST

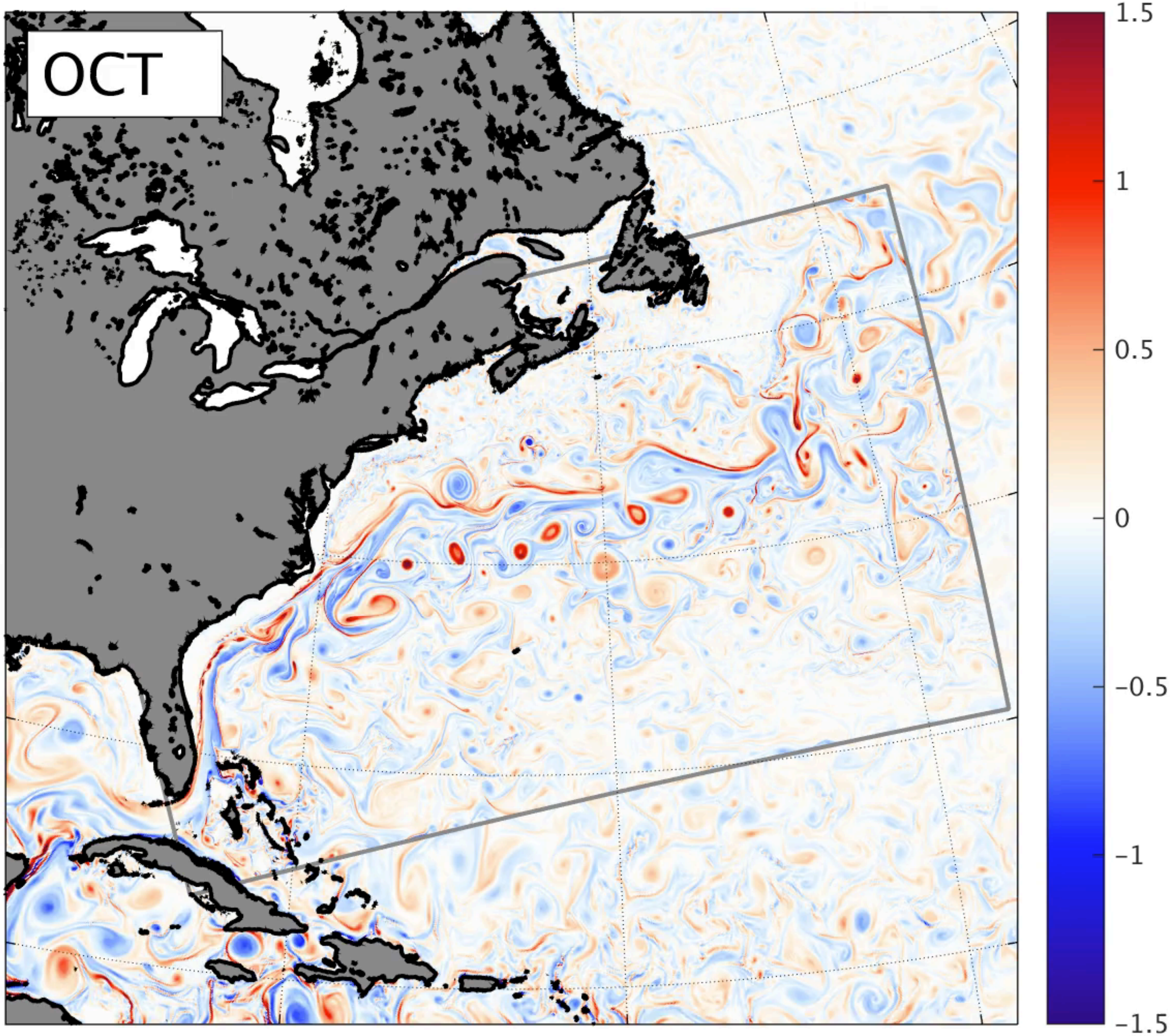
Simulations using ROMS: Regional is a relative concept

Animation from J. Molemaker

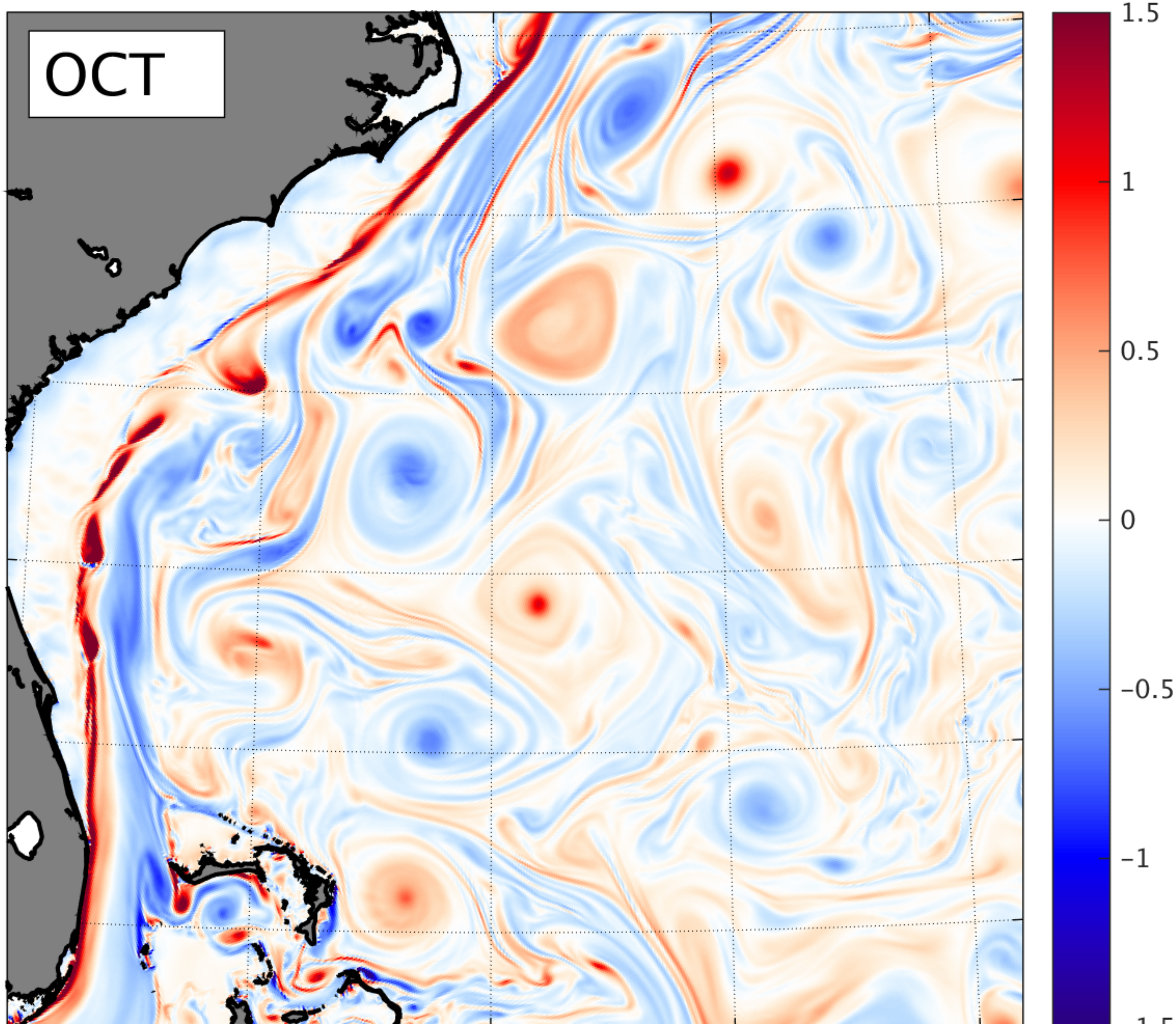


Normalized relative vorticity, or $Ro = \zeta / f$

ζ / f

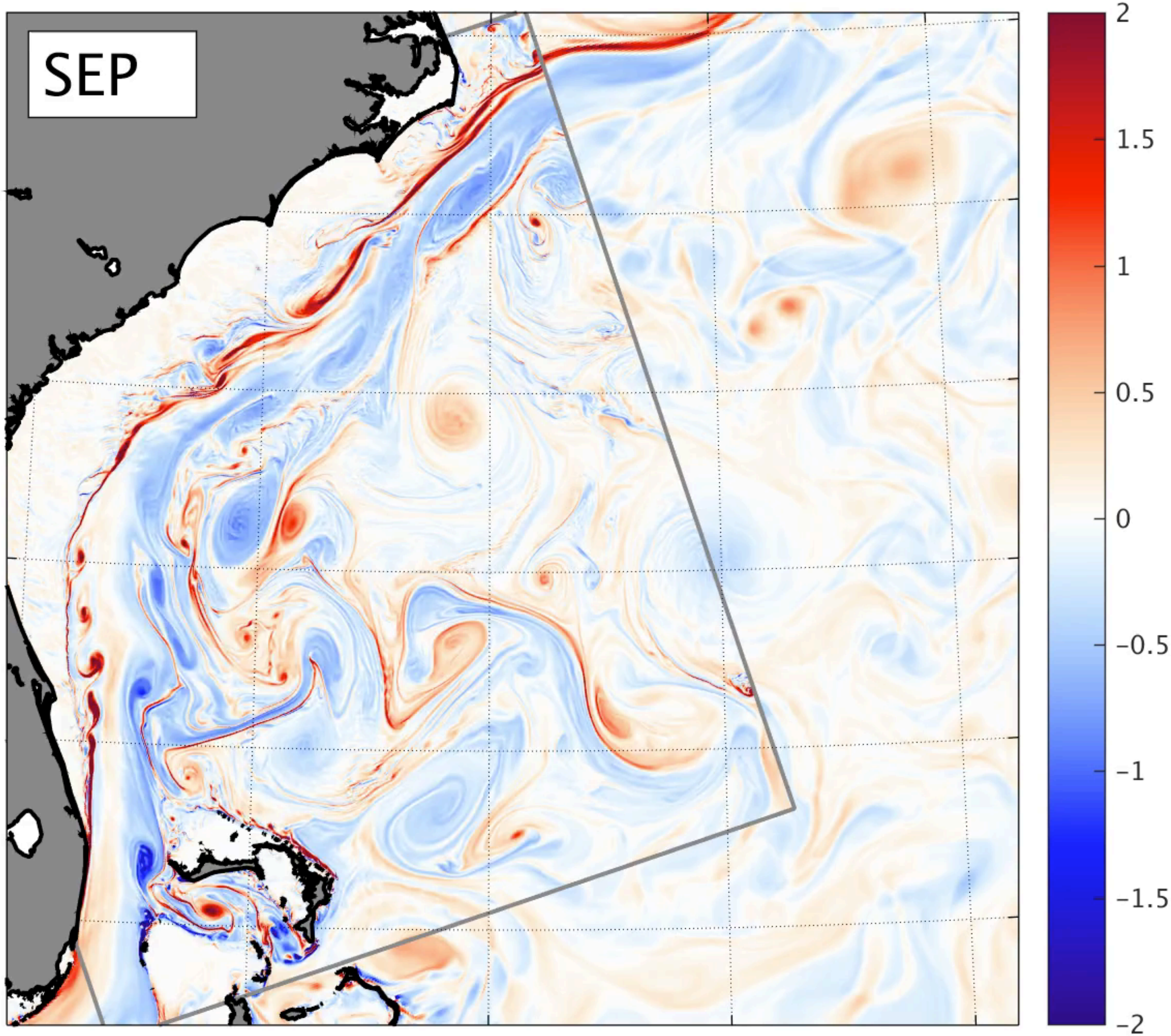


Nested domain with open boundaries with dx = 2.5 km

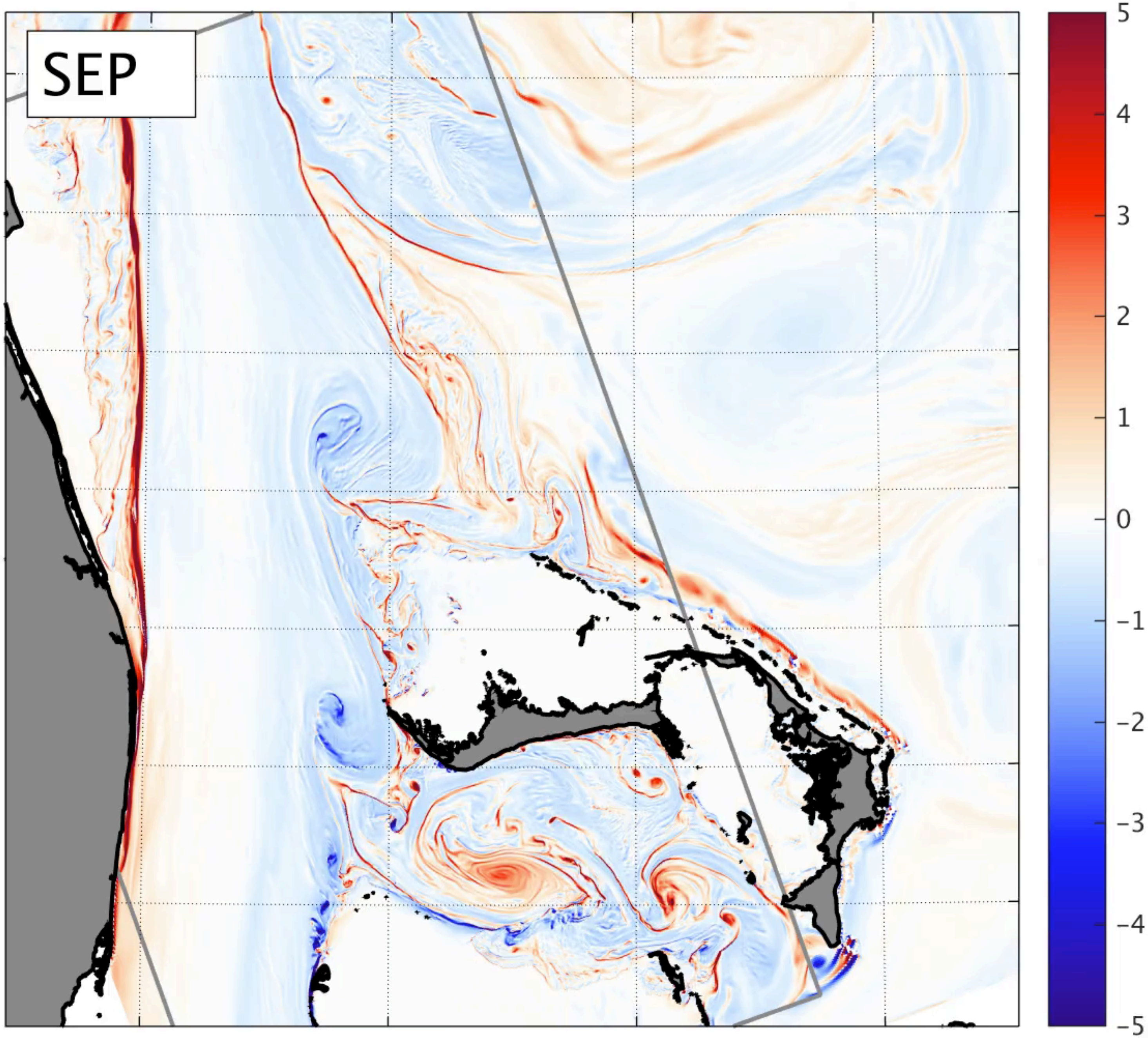


ζ / f

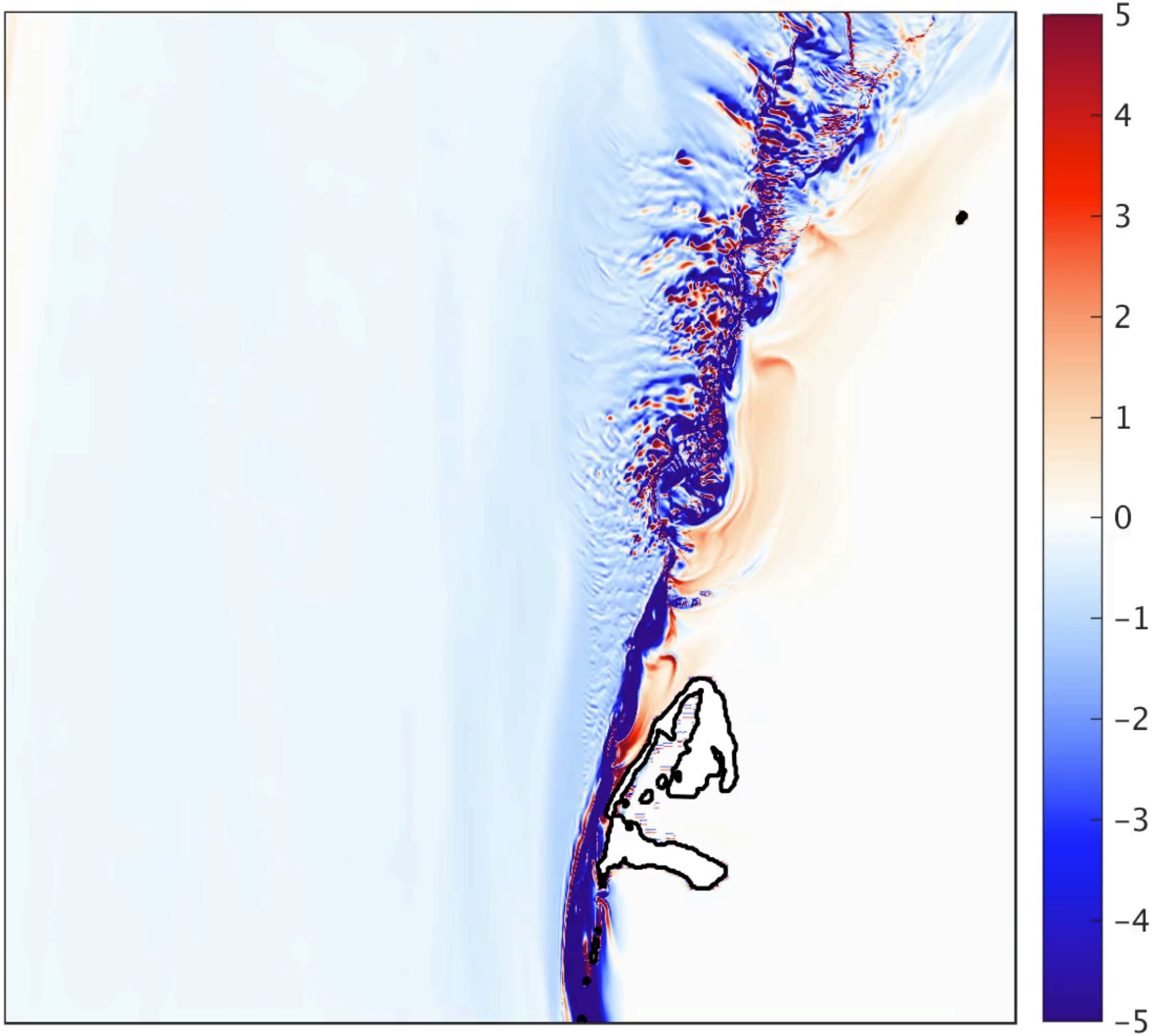
dx = 2.5 km



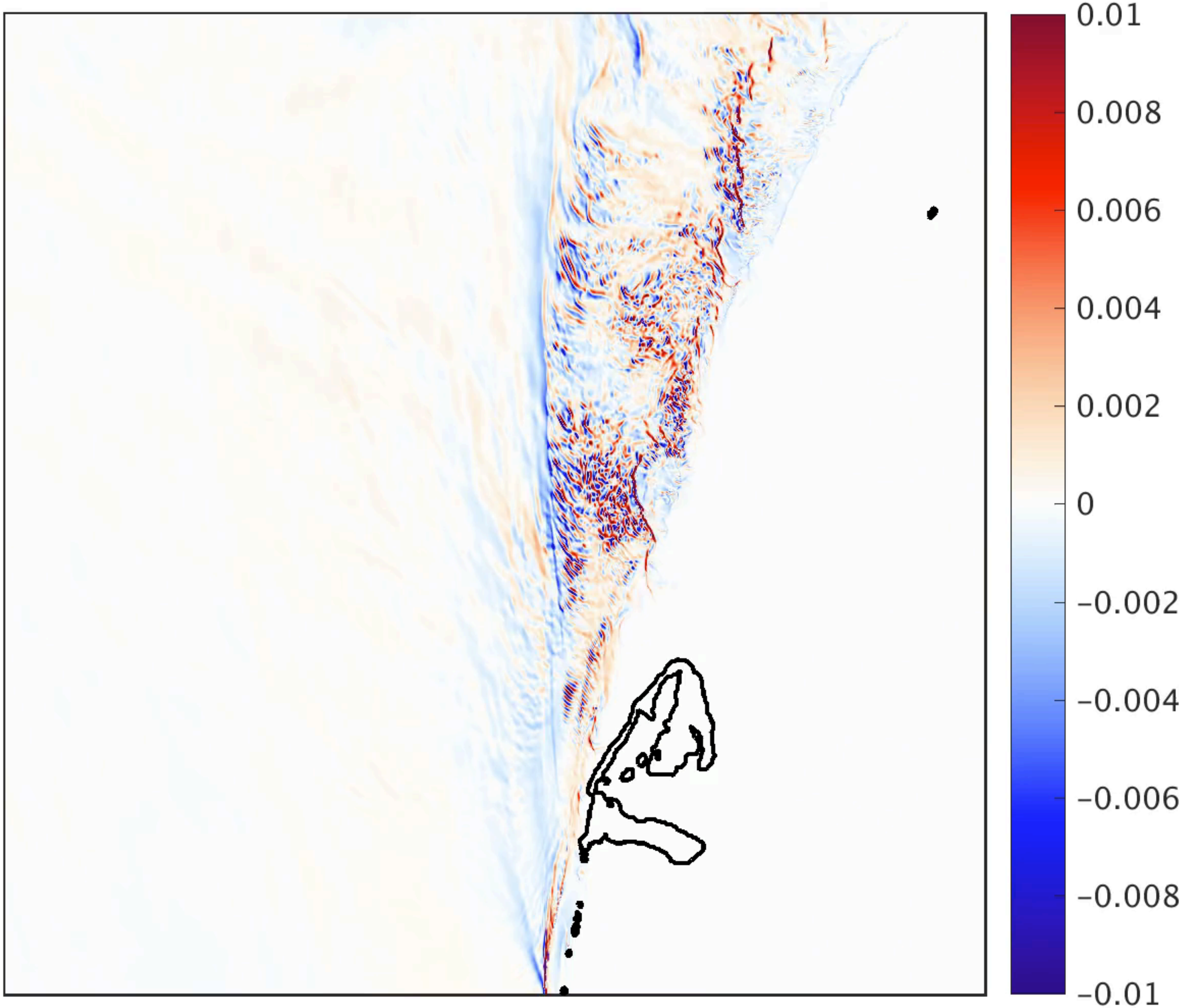
dx = 700 m



dx = 200 m

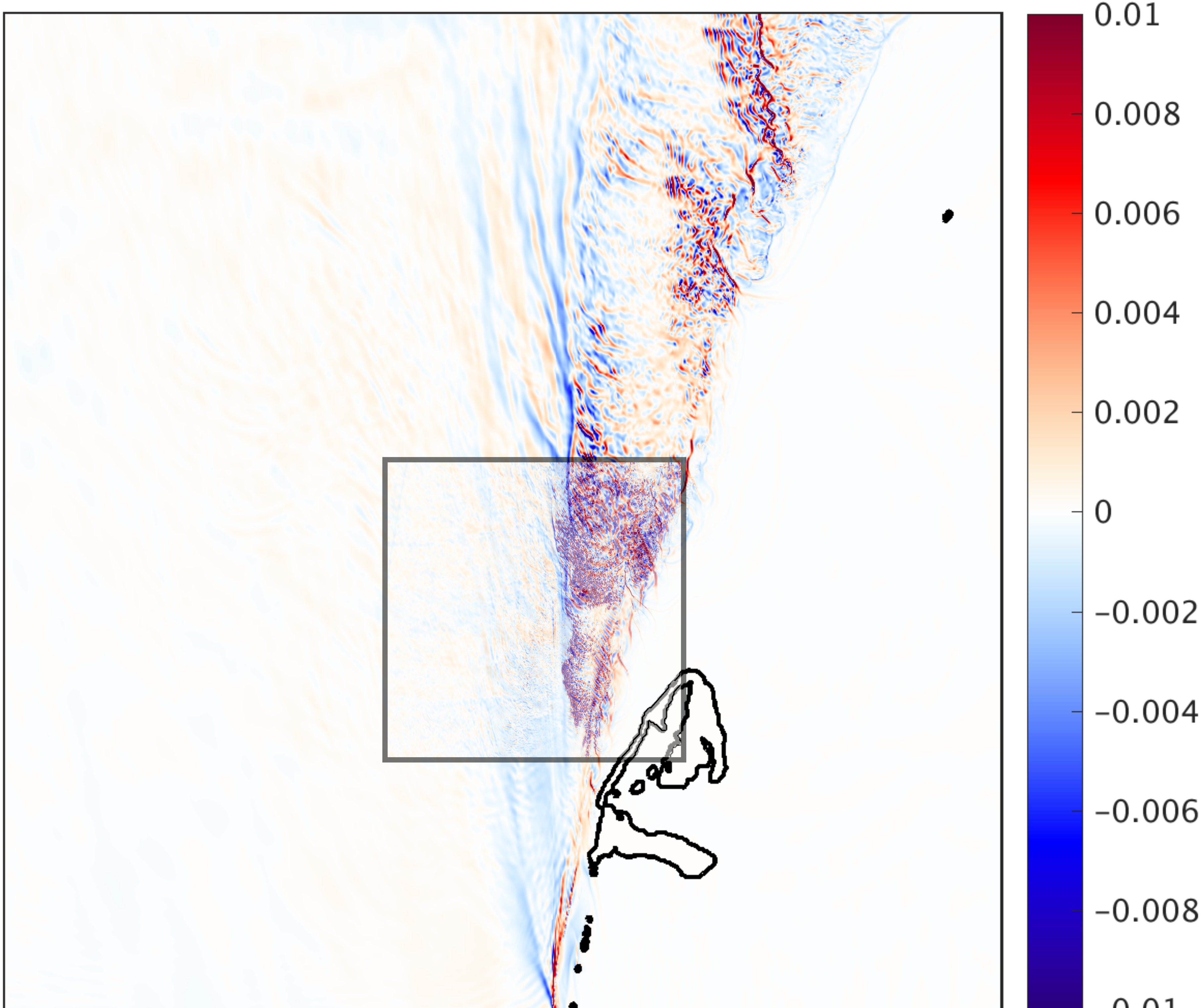


dx = 50 m, non-hydrostatic

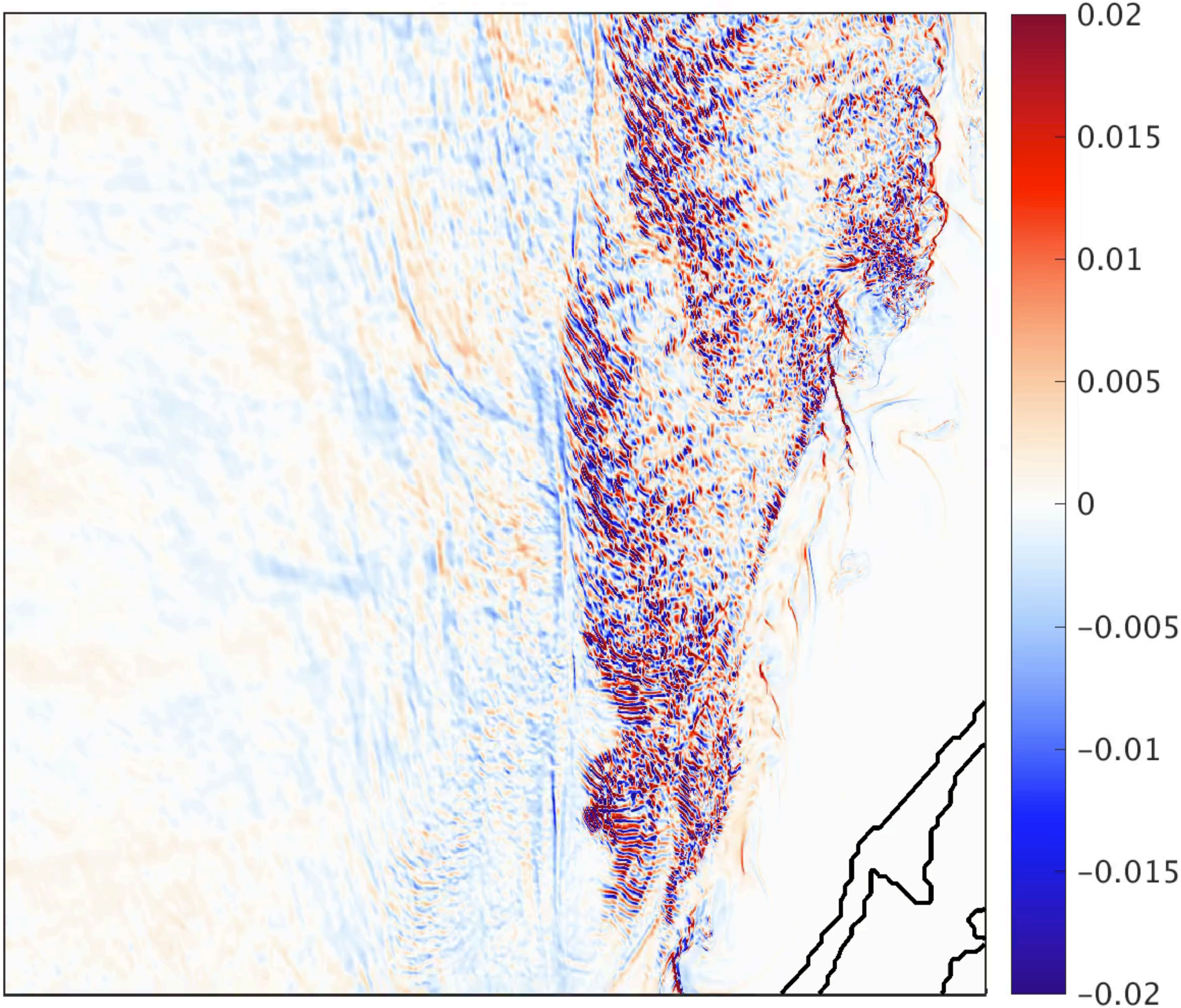


dx = 50 m, non-hydrostatic

Surface layer vertical velocity



0.01
0.008
0.006
0.004
0.002
0
−0.002
−0.004
−0.006
−0.008
−0.01

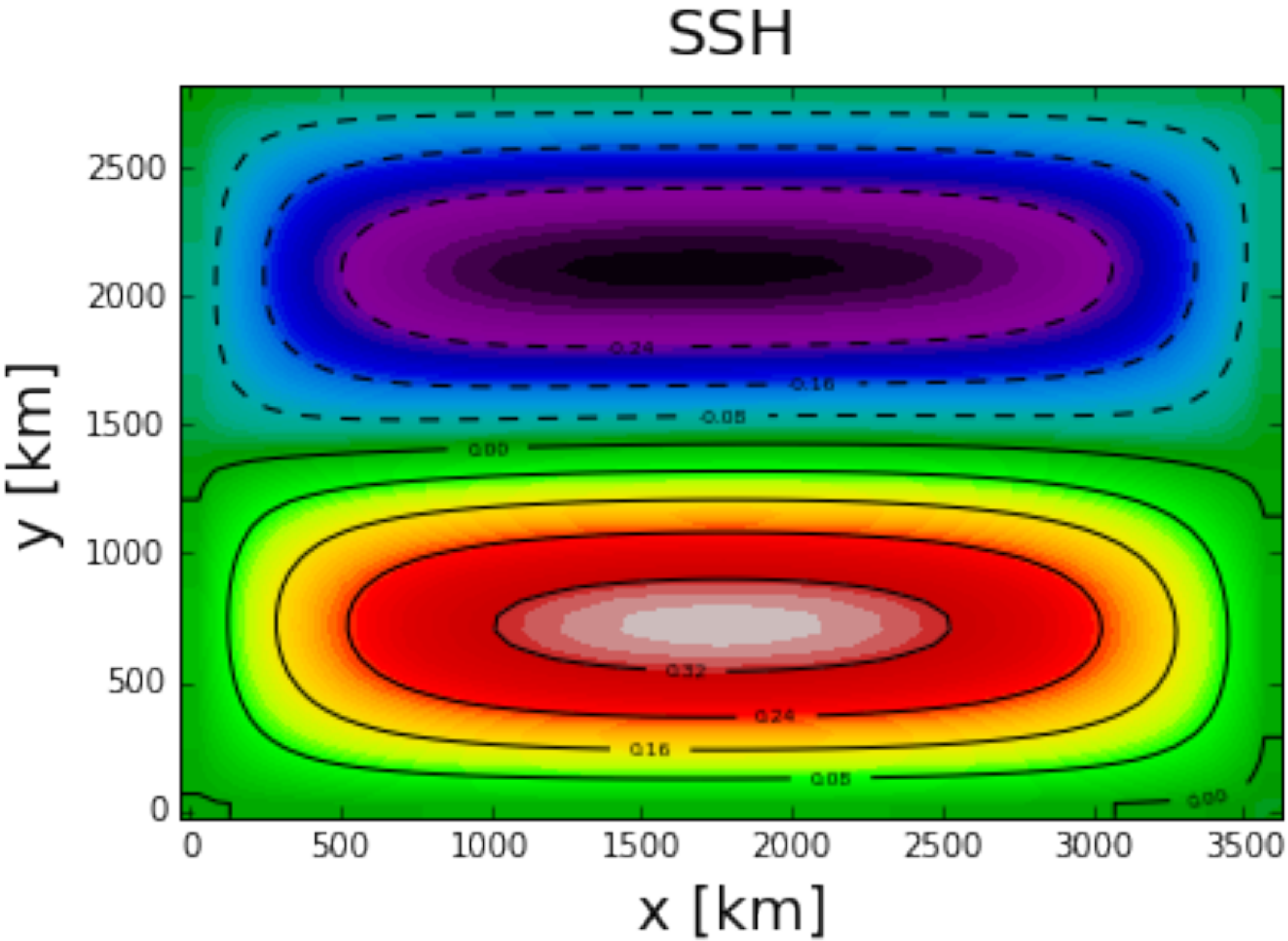


dx = 15 m (NH)

Surface layer vertical velocity


Visible light, (credit NASA)

Activity 1 – Run an idealized ocean basin



Activity 1 – Run an idealized ocean basin

- **Jobcomp** (compilation)
- **cppdefs.h** (Numerical/physical options)
- **param.h** (gris size/ parallelisation)
- **croco.in** (choice of variables, parameter values, etc.)

1) Preparing and compiling the model

For that use the the jobcomp bash file
./jobcomp

1. Set library path
2. Automatic selection of option accordingly the platform used
3. Use of makefile
   - C-preprocessing step : .F → .f using the CPP keys defintions (in cppdefs.h file, customization of the code)
   - Compilation step : .f → .o (object) using Fortran compiler
   - Linking step : link all the .o file and the librairy (Netcdf, MPI, AGRIF) --
   - --> produce the executable roms

1) Preparing and compiling the model

Edit the param.h and cppdefs.h file to set-up the model

param.h defines the size of the arrays in ROMS:

```
...
#elif defined REGIONAL
# if defined  BENGUELA
    parameter (LLm0=23, MMm0=31, N=32) <---- Southern Benguela test Model
# else
    parameter (LLm0=??,  MMm0=??,  N=??)
# endif
...
```

Given by running make_grid

Defined in romstools_param.m

cppdefs.h:

- Basic options
- More advanced options

- Define CPP keys used by the C-preprocessor when compiling the model.
- Reduce the code to its minimal size: fast compilation.
- Avoid FORTRAN logical statements: efficient coding.

1) Preparing and compiling the model

View cppdef.h file

```
!------------------------------------------------------------
!              BASIC OPTIONS
!------------------------------------------------------------
*/
/*                      Configuration Name */
# define BENGUELA
/*                      Parallelization */
# undef  OPENMP
# undef  MPI
/*                      Embedding */
# undef AGRIF
/*                      Open Boundary Conditions */
# undef  TIDES
# define OBC_EAST
# undef OBC_WEST
# define OBC_NORTH
# define OBC_SOUTH
*/                       Embedding conditions */
# ifdef AGRIF
#  undef AGRIF_OBC_EAST
#  define AGRIF_OBC_WEST
#  define AGRIF_OBC_NORTH
#  define AGRIF_OBC_SOUTH
# endif
/*                     Applications */
# undef  BIOLOGY
# undef  FLOATS
# undef  STATIONS
# undef  PASSIVE_TRACER
# undef  SEDIMENTS
# undef  BBL
```

```
!------------------------------------------------------------
!         MORE ADVANCED OPTIONS
!------------------------------------------------------------
*/
/*                      Model dynamics */
# define SOLVE3D
# define UV_COR
# define UV_ADV
# ifdef TIDES
#  define SSH_TIDES
#  define UV_TIDES
#  define TIDERAMP
# endif
/*                      Grid configuration */
# define CURVGRID
# define SPHERICAL
# define MASKING
/*                           Input/Output & Diagnostics */
# define AVERAGES
# define AVERAGES_K
# define  DIAGNOSTICS_TS
# define  DIAGNOSTICS_UV
/*                           Equation of State  */ ...
/*                           Surface Forcing */ ...
/*                           Lateral Forcing  */ ...
/*                           Input/Output & Diagnostics */ ...
*                            Bottom Forcing  */ ...
/*                           Point Sources - Rivers */ ...
/*                           Lateral Mixing  */ ...
/*                           Vertical Mixing */ ...
/*                           Open Boundary Conditions  */ ...
/*                           Embedding conditions  */ ...
```

2) Running the model

The namelist roms.in

roms.in provides the run time parameters for ROMS:

```
title:
      Southern Benguela
time_stepping: NTIMES   dt[sec]  NDTFAST  NINFO
           480     5400    60     1
S-coord: THETA_S,   THETA_B,    Hc (m)
        6.0d0     0.0d0     10.0d0
grid:  filename
                 ROMS_FILES/roms_grd.nc
forcing: filename
                 ROMS_FILES/roms_frc.nc
bulk_forcing: filename
                 ROMS_FILES/roms_blk.nc
climatology: filename
                 ROMS_FILES/roms_clm.nc
boundary: filename
                 ROMS_FILES/roms_bry.nc
initial: NRREC  filename
        1
                 ROMS_FILES/roms_ini.nc
restart:         NRST, NRPFRST / filename
           480   -1
                 ROMS_FILES/roms_rst.nc
```

Warning ! These should be identical to the ones in romstools_param.m

```
history: LDEFHIS, NWRT, NRPFHIS / filename
        T    480    0
                 ROMS_FILES/roms_his.nc
averages: NTSAVG, NAVG, NRPFAVG / filename
        1     48    0
                 ROMS_FILES/roms_avg.nc

primary_history_fields: zeta UBAR VBAR  U  V   wrtT(1:NT)
                 T    F   F   F  F    10*F
auxiliary_history_fields:   rho Omega  W  Akv  Akt  Aks  HBL  Bostr
                   F  F    F   F    F    F    F    F
primary_averages: zeta UBAR VBAR  U  V   wrtT(1:NT)
             T    T    T    T  T   10*T
auxiliary_averages: rho Omega  W  Akv  Akt  Aks  HBL  Bostr
              F  T    T  F    T   F    T    T
rho0:
    1025.d0
lateral_visc:   VISC2,    VISC4    [m^2/sec for all]
           0.      0.
tracer_diff2: TNU2(1:NT)          [m^2/sec for all]
          10*0.d0
bottom_drag:     RDRG [m/s],  RDRG2,  Zob [m],  Cdb_min, Cdb_max
           0.0d-04      0.d-3    1.d-2     1.d-4    1.d-1
gamma2:
           1.d0
sponge:         X_SPONGE [m],    V_SPONGE [m^2/sec]
             100.e3          800.

nudg_cof:    TauT_in, TauT_out, TauM_in, TauM_out  [days for all]
          1.       360.      10.      360.
```

Activity 1 – Run an idealized ocean basin

- **param.h**

```
      parameter (LLm0=60,   MMm0=50,   N=10)
```

- **cppdefs.h**

```
# define UV_COR
# define UV_VIS2
# define TS_DIF2

# define ANA_GRID
# define ANA_INITIAL
```

- **ana_grid.F**

```
f0=1.E-4
beta=0.
```

- **croco.in**

```
bottom_drag:     RDRG(m/s),      RDRG2, Zob [m],  Cdb_min, Cdb_max
                 3.e-4             0.      0.         0.      0.
gamma2:
                 1.
lin_EOS_cff:  R0 [kg/m3], T0 [Celsius], S0 [PSU], TCOEF [1/Celsius], SCOEF [1/PSU]
              30.         0.            0.        0.28               0.
lateral_visc:   VISC2     [m^2/sec ]
                 1000.  0.
tracer_diff2: TNU2          [m^2/sec]
                 1000. 0.
```

Homework

- For next time:
  - Read https://www.jgula.fr/ModNum/Stommel48.pdf
  - Read https://www.jgula.fr/ModNum/Munk50.pdf
  -