

**EE/CSCI 451**

**Fall 2020**

**Homework 8**

**Assigned: October 16, 2020**

**Due: October 22, 2020, AOE**

**Total Points: 100**

YOU DO NOT NEED TO SUBMIT THIS HOMEWORK.

## **1 [10 points]**

Explain the following terms:

- Task dependency graph
- Block distribution
- Master-slave model
- Owner-computes rule
- Critical path length

## 2 [10 points]

Perform a level-by-level ordering of the task dependency graph given in Figure 1 and show the level that each node (i.e., task) belongs to.

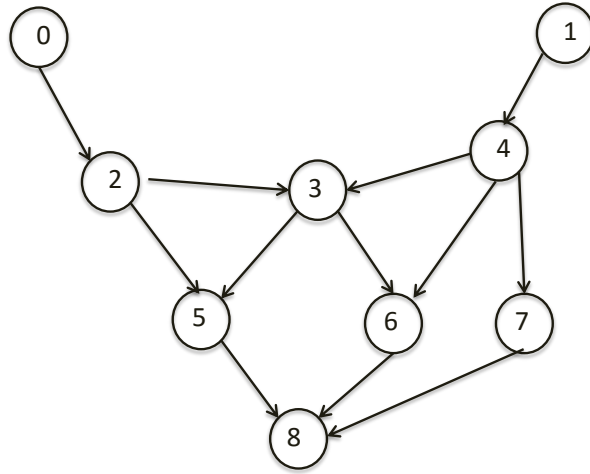


Figure 1: Problem 2

### 3 [12 points]

For the task dependency graphs shown in Figure 2, determine the following:

- Maximum degree of concurrency
- Critical path length
- Maximum achievable speedup over one process assuming that an arbitrarily large number of processes is available

Assume each task is of unit size.

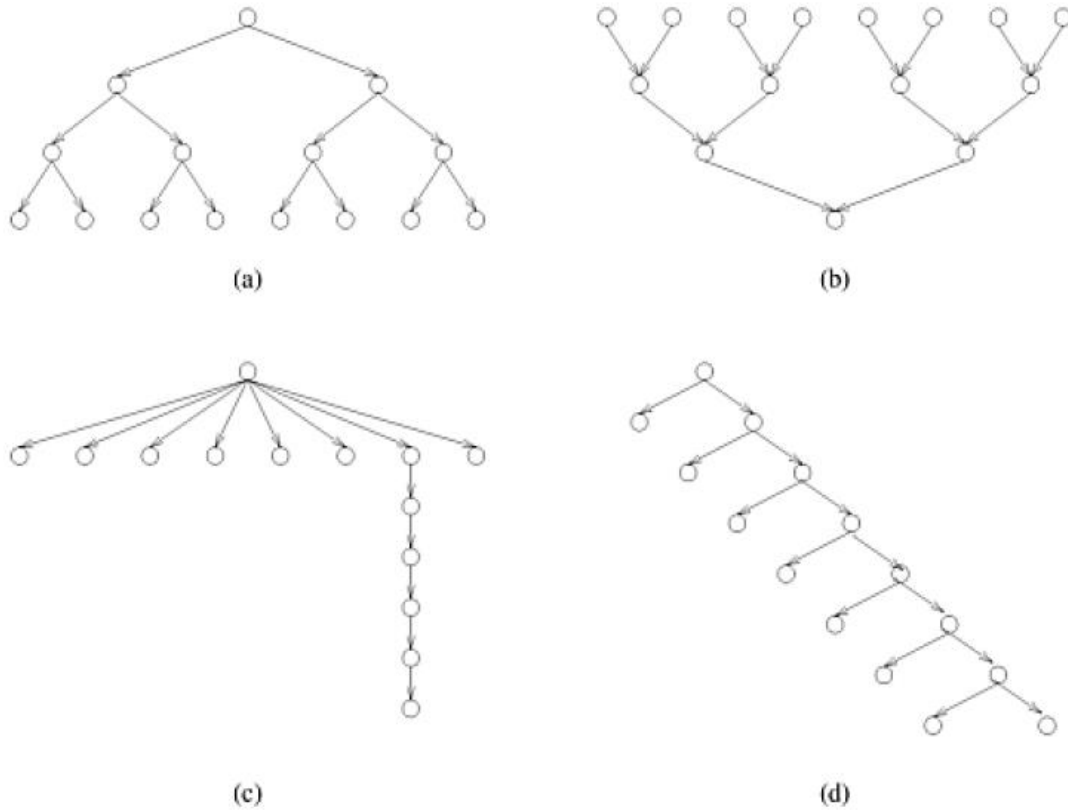


Figure 2: Problem 3

## 4 [18 points]

Suppose there are 4 processes and suppose that  $\mathbf{x}$  is a vector with  $n = 24$  elements.

- How would the elements of  $\mathbf{x}$  be distributed among the processes in a program that uses the block distribution?
- How would the elements of  $\mathbf{x}$  be distributed among the processes in a program that uses the cyclic distribution?
- How would the elements of  $\mathbf{x}$  be distributed among the processes in a program that uses a block-cyclic distribution with block size of 2?

## 5 [20 points]

Consider an array of  $n$  elements which is distributed among  $p$  processes using (i) block distribution and (ii) cyclic distribution. Assume  $n$  and  $p$  are powers of 2 and the amount of work performed on the  $i^{th}$  element,  $0 \leq i \leq n-1$ , of the array is  $i+1$  units.

- For  $n = 16$  and  $p = 4$ , calculate the total units of work done by each process using (i) block distribution and (ii) cyclic distribution.

	Block distribution	Cyclic distribution
Process 0		
Process 1		
Process 2		
Process 3		

- Derive exact expressions for the total work done by the  $j^{th}$  process ( $0 \leq j \leq p-1$ ) where the  $n$  elements are distributed using (i) block distribution and (ii) cyclic distribution ( $n$  and  $p$  are powers of 2).

## 6 [10 points]

Consider seven tasks with running times of 1, 2, 3, 4, 5, 5, and 10 units, respectively. Assuming that it does not take any time to assign work to a process, compute the best-case and worst-case speedup for a centralized scheme using dynamic mapping with two processes.