

### FUZZY C-MEANS ALGORITHM

Fuzzy Clustering

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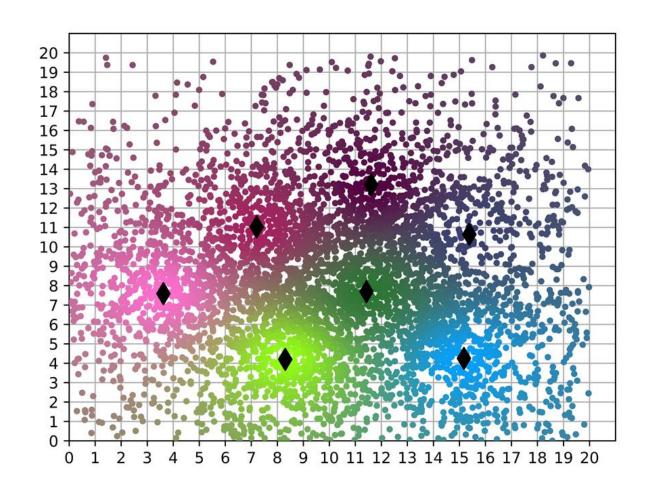


#### FUZZY C-MEANS **ALGORITHM**

The site will have relation to each center. Iterate the following two steps from randomly

$$c_{j} = \frac{\sum_{i=1}^{n} (\mu_{ij})^{m} s_{i}}{\sum_{i=1}^{n} (\mu_{ij})^{m}}, j = 1, 2, ..., k$$

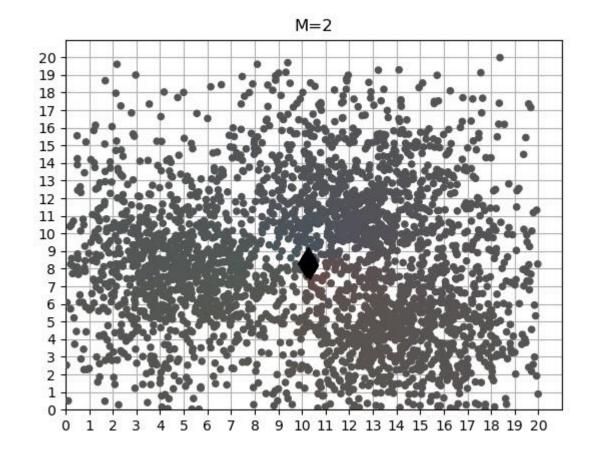
$$\begin{split} c_j &= \frac{\sum_{i=1}^n \left(\mu_{ij}\right)^m s_i}{\sum_{i=1}^n \left(\mu_{ij}\right)^m}, j=1,2,...,k \\ \mu_{ij} &= \left[\sum_{h=1}^k \left(\frac{\text{dist}(s_i,c_j)}{\text{dist}(s_i,c_h)}\right)^{\frac{2}{m-1}}\right]^{-1} \text{ for all } i \text{ and } j \end{split}$$



#### **FUZZY C-MEANS ALGORITHM**

#### Build the map:

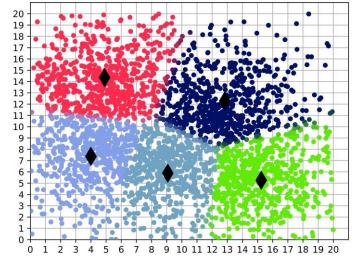
- Choice some points on the map and move them away from each other.
- •Use Monte-carlo sampling to generate the map.
- Initial the cluster
  - ullet Set all the  $\mu_{ij}$  be 1. And the center will in the same location.
- Clustering:
  - Iterate and update the cluster until it is convergence

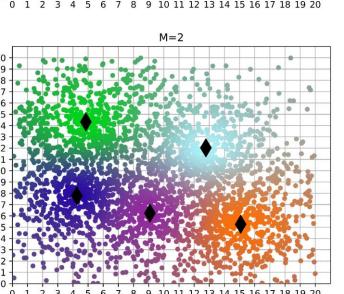


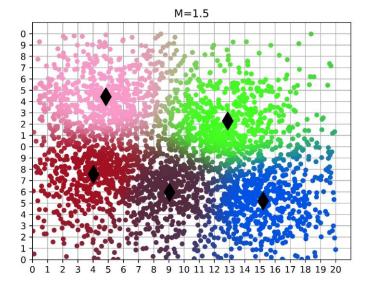
#### THE EFFECT OF M IN THE FUZZY C-MEANS

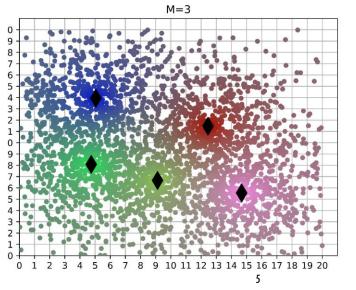
**ALGORITHM** 

When m increase, the boundary of the colors will be more "fuzzy"



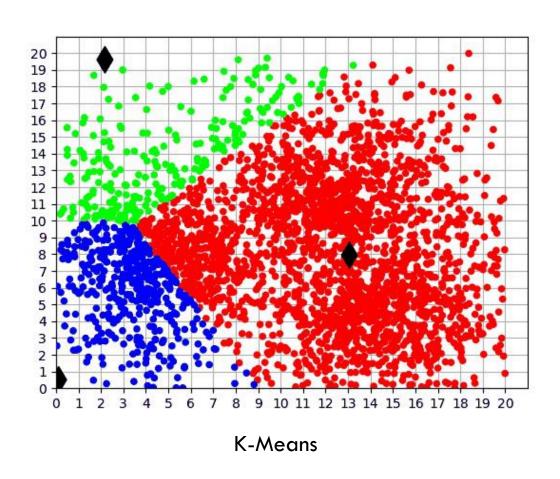


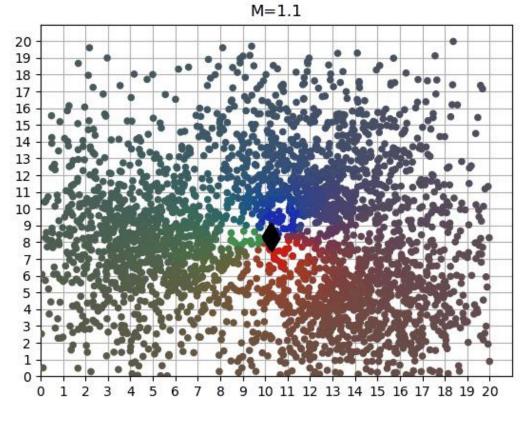


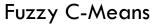




#### K-MEANS AND FUZZY C-MEANS ALGORITHM

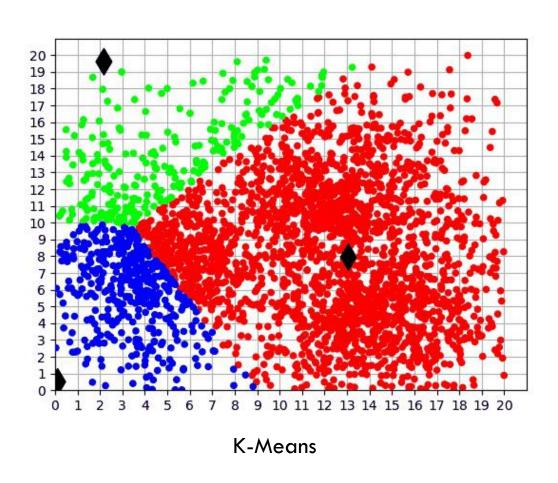


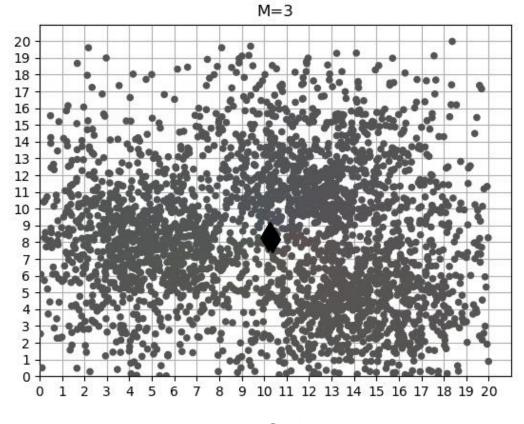






#### K-MEANS AND FUZZY C-MEANS ALGORITHM

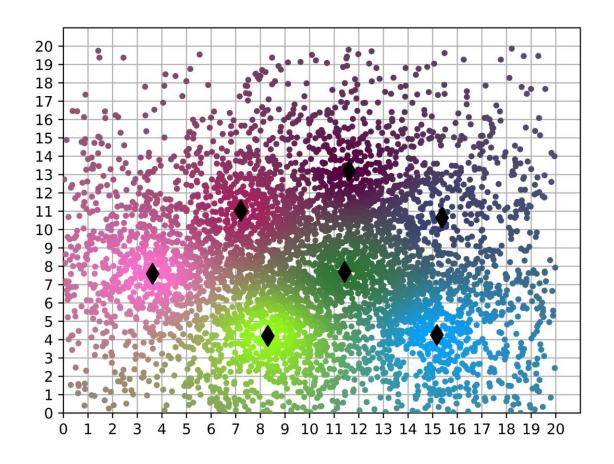




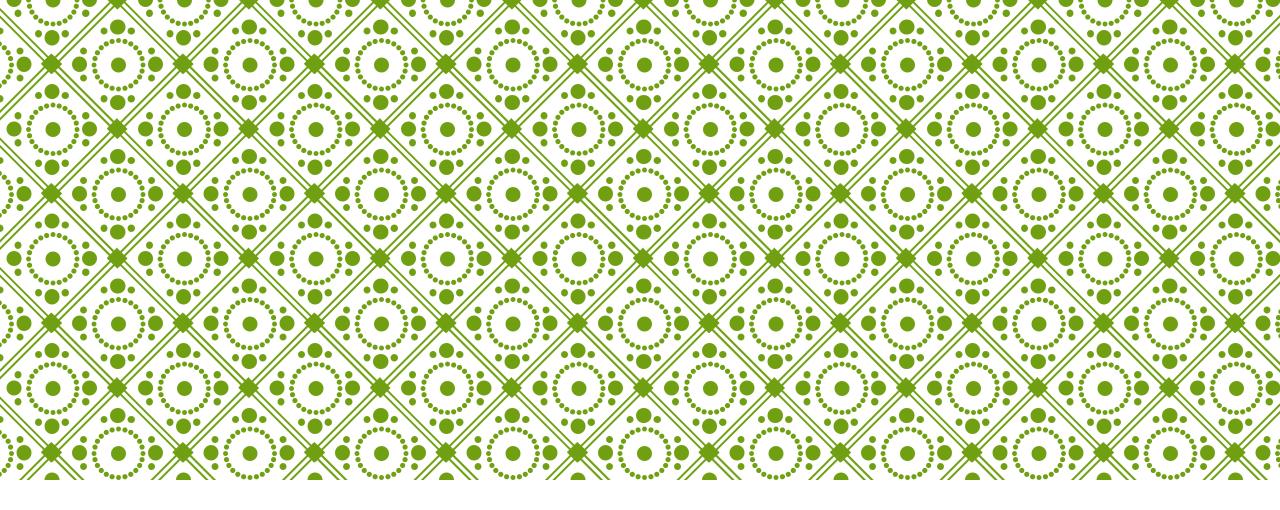


# K-MEANS AND FUZZY C-MEANS ALGORITHM

- K-Means: In the K-Means, each site only in one partition. it is only related to one center.
- Fuzzy C-Means: In the Fuzzy C-Means, a site have relations to all the centers, the distance is closer, the relation is stronger.







## THANK YOU! Q&A

