

1. (8 points) **Example:** Let  $T$  be the tetrahedron with vertices  $O(0, 0, 0)$ ,  $A(0, 0, 6)$ ,  $B(4, 0, 0)$ ,  $C(0, 4, 0)$  (*Note that the plane containing  $A, B, C$  has the equation  $3x + 3y + 2z = 12$ .*)

- (a) Express  $T$  as a solid region of type 1.
- (b) Express  $\iiint_T f(x, y, z) dV$  as an iterated integral.

2. (8 points) Change the order of integration in

$$\int_{x=0}^2 \int_{y=x}^2 \int_{z=0}^y (x + y + z) dz dy dx$$

so that the order becomes  $dz dx dy$ , and sketch the projection of the region on the  $xy$ -plane.

3. (8 points) Express  $\iiint_E (x + z) dV$  in cylindrical coordinates, where  $E$  lies *above* the cone  $z = \sqrt{x^2 + y^2}$  and *below* the plane  $z = 3$  in the first octant. **Do not evaluate.**

4. (8 points) Evaluate  $\iiint_E (x^2 + y^2) dV$ , where  $E$  is the solid under the paraboloid  $z = 4 - x^2 - y^2$  and above the  $xy$ –plane.

5. (6 points) Set up (but do not evaluate) a triple integral in cylindrical coordinates for the volume of the solid bounded by the cone  $z = \sqrt{x^2 + y^2}$  and the plane  $z = 2$ .

6. (8 points) Find the mass of the solid hemisphere  $x^2 + y^2 + z^2 \leq 9$ ,  $z \geq 0$ , with density  $\rho(x, y, z) = z$ .

7. (8 points) Express the volume of the region *inside* the sphere  $x^2 + y^2 + z^2 = 16$  but *outside* the cylinder  $x^2 + y^2 = 4$  as a triple integral in spherical coordinates. **Do not evaluate.**

8. (3 points) Let  $\mathbf{F}(x, y) = \langle 3x^2y - y^3, x^3 - 3xy^2 \rangle$ . Determine whether  $\mathbf{F}$  is conservative on  $\mathbb{R}^2$ .