

MATH 243 Worksheet 5: 2D integrals

Note: Problems 1-4 are leftover problems from slides. Problems 5-x are brand new.

1: Evaluate $\iint_R f(x, y) dA$ for these functions and regions:

- a. $f(x, y) = x \cos^2(y)$, $R = [0, 3] \times [0, \pi/2]$
- b. $f(x, y) = 2x - 4y^3$, $R = [4, 5] \times [0, 3]$
- c. $f(x, y) = xy + \cos(x) + \sin(y)$, $R = [0, 1] \times [0, 1]$

1: Evaluate $\iint_D f(x, y) dA$ for these functions and regions:

- a. $f(x, y) = 4xy - y^3$, D is region bound by $y = \sqrt{x}$ and $y = x^3$
- b. $f(x, y) = x^2 - 2y$, D is triangle with vertices $(0, 3)$, $(1, 1)$, $(5, 3)$
- c. $f(x, y) = e^{x/y}$, $D = \{(x, y) : 1 \leq y \leq 2, y \leq x \leq y^3\}$

3: Find the surface area of the portion of $z = xy$ in the cylinder given by $x^2 + y^2 = 1$

4: Find the center of mass of the following regions:

- a. Portion of the unit disk lying in the 1st quadrant
- b. Square $0 \leq x, y \leq \pi$ with weight function $f(x, y) = x \sin(x) y^3$