

# General 2D integrals

Lecture for 6/25

# General 2D integrals

We can find the integral for a general 2D region



# Switching Order of Integration

- We can switch order of integration



# Average Value

Average value of function  $f$  over region  $R$ :

- Equal to  $(1/A) \iint_R f(x, y) \, dx \, dy$  where  $A$  is area of  $R$

# Practice Problems

Evaluate  $\iint_D f(x, y) \, dA$  for these functions and regions:

- $f(x, y) = 4xy - y^3$ ,  $D$  is region bound by  $y = x^{1/2}$  and  $y = x^3$
- $f(x, y) = x^2 - 2y$ ,  $D$  is triangle with vertices  $(0, 3)$ ,  $(1, 1)$ ,  $(5, 3)$
- $f(x, y) = e^{x/y}$ ,  $D = \{(x, y): 1 \leq y \leq 2, y \leq x \leq y^3\}$

# Scratchwork







