## MATH 243 Worksheet 8: Stokes' and Divergence Theorems

- 1: Evaluate  $\iint_S \mathbf{F} \cdot d\mathbf{S}$  for the following functions and surfaces
- **a.**  $\mathbf{F} = (3x, 2y, 1 y^2)$ , S is the portion of  $z = 2 3y + x^2$  oriented downward and lying over triangle with vertices (0,0), (2,0), (2,-4)
- **b.**  $\mathbf{F} = (yz, x, 3y^2)$ , S is the surface of solid bounded by  $x^2 + y^2 = 4$ , z = x 3, z = x + 2 with negative orientation
- **c.**  $\mathbf{F} = \nabla \times G, G = (z^2 1, z + xy^3, 6), S$  is the portion of  $x = 6 4y^2 4z^2$  in front of x = -2 with orientation in the negative x-direction
- d. For extra computation practice, do part c without using Stokes' Theorem
- 2: Evaluate  $\int_C \mathbf{F} \cdot d\mathbf{r}$  for the following functions and curves
- **a.**  $\mathbf{F} = (-yz, 4y + 1, xy)$ , C is the circle of radius 3 centered at (0, 4, 0), perpendicular to y-axis, and oriented CW when looking above y > 4
- **b.**  $\mathbf{F} = (3yx^2 + z^3, y^2, 4yx^2)$ , C is the triangle with vertices (0,0,3), (0,2,0), (4,0,0) oriented CCW when looking above C towards origin
- 3: Evaluate  $\iint_S \mathbf{F} \cdot d\mathbf{S}$  for these with and without using divergence theorem
- **a.**  $\mathbf{F} = (\sin(\pi x), zy^3, z^2 + 4x)$ , S is the surface of box with -1 < x < 2, 0 < y < 1, 1 < z < 4 oriented pointing out of the box
- **b.**  $\mathbf{F} = (2xz, 1 4xy^2, 2z z^2)$ , S is the surface of the solid bounded by  $z = 6 2x^2 2y^2$  and z = 0, oriented pointing inside the solid
- 4: New problems to be continued