

1. (8 points) **Example:** Let T be the tetrahedron with vertices $O(0, 0, 0)$, $A(0, 0, 6)$, $B(4, 0, 0)$, $C(0, 4, 0)$ (Note that the plane containing A, B, C has the equation $3x + 3y + 2z = 12$.)

(a) Express T as a solid region of type 1.

(b) Express $\iiint_T f(x, y, z) dV$ as an iterated integral.

2. (8 points) Change the order of integration in

$$\int_{x=0}^2 \int_{y=x}^2 \int_{z=0}^y (x + y + z) dz dy dx$$

so that the order becomes $dz dx dy$, and sketch the projection of the region on the xy -plane.

3. (8 points) Express $\iiint_E (x + z) dV$ in cylindrical coordinates, where E lies *above* the cone $z = \sqrt{x^2 + y^2}$ and *below* the plane $z = 3$ in the first octant. **Do not evaluate.**

4. (8 points) Evaluate $\iiint_E (x^2 + y^2) dV$, where E is the solid under the paraboloid $z = 4 - x^2 - y^2$ and above the xy -plane.

5. (6 points) Set up (but do not evaluate) a triple integral in cylindrical coordinates for the volume of the solid bounded by the cone $z = \sqrt{x^2 + y^2}$ and the plane $z = 2$.

6. (8 points) Find the mass of the solid hemisphere $x^2 + y^2 + z^2 \leq 9$, $z \geq 0$, with density $\rho(x, y, z) = z$.

7. (8 points) Express the volume of the region *inside* the sphere $x^2 + y^2 + z^2 = 16$ but *outside* the cylinder $x^2 + y^2 = 4$ as a triple integral in spherical coordinates. **Do not evaluate.**

8. (3 points) Let $\mathbf{F}(x, y) = \langle 3x^2y - y^3, x^3 - 3xy^2 \rangle$. Determine whether \mathbf{F} is conservative on \mathbb{R}^2 .