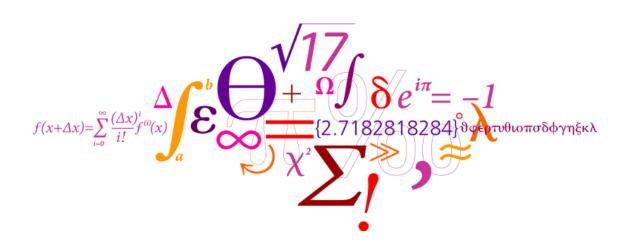
31310 Linear Control Design 2

Compulsory Assignment 2015: Loudspeaker control

by

KATLEEN BLANCHET S150798 TITOUAN BOULMIER S150810



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Technical University of Denmark Department of Electrical Engineering

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Part I

Exercise 1: Distortion Attenuation for Loudspeakers

Moving-coil Loudspeakers

1 Loudspeakers electrical equivalent circuit

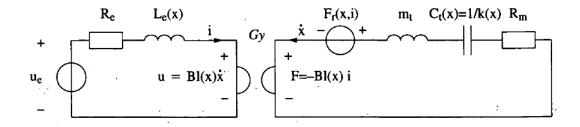


Figure 1: Electrical equivalent lumped element model of the voltage driven electrodynamic loudspeaker for low frequencies. The coupling between the electrical and mechanical domain is performed through the gyrator with gy- ration constant Bl(x).

$$u_e = R_e i + \frac{dL_e(x)}{dx} \frac{dx}{dt} i + L_e(x) \frac{di}{dt} + Bl(x) \frac{dx}{dt}$$
(1)

$$Bl(x)i = m_t \frac{d^2x}{dt^2} + R_m \frac{dx}{dt} + k(x)x - \frac{1}{2} \frac{dL_e(e)}{dx} i^2$$
 (2)

where

$$Bl(x) = Bl_0 + b_1 x + b_2 x^2 (3)$$

$$L_e(x) = L_{e0} + l_1 x + l_2 x^2 (4)$$

$$k(x) = k_0 + k_1 x + k_2 x^2 (5)$$

1.1 Problem 1

By means of Eqs 1, 2, 3, 4 and 5, we can identify 3 state variables x, \dot{x} and i. We can also identify the input u_e .

$$\mathbf{x} = \begin{pmatrix} x \\ \dot{x} \\ i \end{pmatrix}$$
 and $\mathbf{u} = (u_e)$

Then, we can derive the nonlinear dynamical state space model to obtain

$$\dot{x} = \dot{x} \tag{6}$$

$$\ddot{x} = \frac{(Bl_0 + b_1 x + b_2 x^2)i - R_m \dot{x} - (k_0 + k_1 x + k_2 x^2)x + \frac{1}{2}(l_1 + 2l_2 x)\dot{x}i^2}{m_t} \tag{7}$$

$$\ddot{x} = \frac{(Bl_0 + b_1 x + b_2 x^2)i - R_m \dot{x} - (k_0 + k_1 x + k_2 x^2)x + \frac{1}{2}(l_1 + 2l_2 x)\dot{x}i^2}{m_t}$$

$$\dot{i} = \frac{u_e - (R_e + (l_1 + 2l_2 x)\dot{x}^2)i - (Bl_0 + b_1 x + b_2 x^2)\dot{x}}{L_{e0} + l_1 x + l_2 x^2}$$
(8)

In matrix format, we have

$$\dot{\mathbf{x}} = f(\mathbf{x}) + g(\mathbf{x})\mathbf{u} \tag{9}$$

with

$$f(\mathbf{x}) = \begin{pmatrix} \mathbf{x}(2) \\ \frac{(Bl_0 + b_1 \mathbf{x}(1) + b_2 \mathbf{x}(1)^2) \mathbf{x}(3) - R_m \mathbf{x}(2) - (k_0 + k_1 \mathbf{x}(1) + k_2 \mathbf{x}(1)^2) \mathbf{x}(1) + \frac{1}{2}(l_1 + 2l_2 \mathbf{x}(1)) \mathbf{x}(2) \mathbf{x}(3)^2}{m_t} \\ \frac{-(R_e + (l_1 + 2l_2 \mathbf{x}(1)) \mathbf{x}(2)^2) \mathbf{x}(3) - (Bl_0 + b_1 \mathbf{x}(1) + b_2 \mathbf{x}(1)^2) \mathbf{x}(2)}{L_{e0} + l_1 \mathbf{x}(1) + l_2 \mathbf{x}(1)^2} \end{pmatrix}$$
(10)

$$g(\mathbf{x}) = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \tag{11}$$

1.2 Problem 2

References