

ECE 6310 - Advanced Electromagnetic Fields: Homework Set #1

Miguel Gomez

13 days - 12 hours - 19 min until deadline

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z
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Problem 1.3

The electric flux density inside a cube is given by:

(a) $\vec{D} = \hat{a}_x(3 + x)$

(b) $\vec{D} = \hat{a}_y(4 + y^2)$

Find the total electric charge enclosed inside the cubical volume when the cube is in the first octant with three edges coincident with the x, y, z axes and one corner at the origin. Each side of the cube is 1 m long.

Ok, this one we can do by using the following expressions from the text [?]:

$$\oiint_s \mathcal{D} ds = \iiint_v \mathcal{q}_{ev} dv = \mathcal{Q}_e \quad (1)$$

$$\mathcal{q}_{ev} = \Delta \cdot \mathcal{D} \quad (2)$$

We apply expression 2 then plug into expression 1 to get the total electric charge.

Problem 1.4

An infinite planar interface between media, as shown in the figure, is formed by having air (medium #1) on the left of the interface and lossless polystyrene (medium #2) to the right of the interface. An electric surface charge density $\sigma_{es} = 0.2 \text{ C/m}^2$ exists along the entire interface. The static electric flux density inside the polystyrene is given by $\vec{D}_2 = 6\hat{a}_x + 3\hat{a}_z \text{ C/m}^2$. Determine the corresponding vector:

- (a) Electric field intensity inside the polystyrene.
- (b) Electric polarization vector inside the polystyrene.
- (c) Electric flux density inside the air medium.
- (d) Electric field intensity inside the air medium.
- (e) Electric polarization vector inside the air medium.

Leave your answers in terms of ε_0, μ_0 .

Problem 1.13

The instantaneous magnetic flux density in free space is given by:

$$\vec{\mathcal{B}} = \hat{a}_x B_x \cos(2y) \sin(\omega t - \pi z) + \hat{a}_y B_y \cos(2x) \cos(\omega t - \pi z)$$

where B_x and B_y are constants. Assuming there are no sources at the observation points x, y , determine the electric displacement current density.

Problem 1.20

The instantaneous electric field inside a conducting rectangular pipe (waveguide) of width a is given by:

$$\vec{\mathcal{E}} = \hat{a}_y E_0 \sin\left(\frac{\pi x}{a}\right) \cos(\omega t - \beta_z z)$$

where β_z is the waveguide's phase constant. Assuming there are no sources within the free-space-filled pipe determine the:

- (a) Corresponding instantaneous magnetic field components inside the conducting pipe.
- (b) Phase constant β_z .
- (c) The height of the waveguide is b .

Problem 2.18

The time-varying electric field inside a lossless dielectric material of polystyrene, of infinite dimensions and with a relative permittivity (dielectric constant) of 2.56, is given by:

$$\vec{\mathcal{E}} = \hat{a}_x 10^{-3} \sin(2\pi \times 10^7 t) \text{ V/m}$$

Determine the corresponding:

- (a) Electric susceptibility of the dielectric material.
- (b) Time-harmonic electric flux density vector.
- (c) Time-harmonic electric polarization vector.
- (d) Time-harmonic displacement current density vector.
- (e) Time-harmonic polarization current density vector defined as the partial derivative of the corresponding electric polarization vector.

Leave your answers in terms of ε_0, μ_0 .

Problem 2.25

Aluminum has a static conductivity of about $\sigma = 3.96 \times 10^7 \text{ S/m}$ and an electron mobility of $\mu_e = 2.2 \times 10^{-3} \text{ m}^2/(\text{V}\cdot\text{s})$. Assuming that an electric field of $\vec{E} = \hat{a}_x 2 \text{ V/m}$ is applied perpendicularly to the square area of an aluminum wafer with cross-sectional area of about 10 cm^2 , find the:

- (a) Electron charge density q_{ve} .
- (b) Electron drift velocity v_e .

- (c) Electric current density J .
- (d) Electric current flowing through the square cross section of the wafer.
- (e) Electron density N_e .

Leave your answers in terms of ε_0, μ_0 .