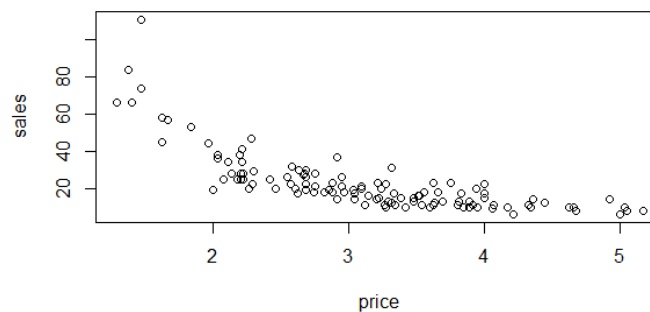


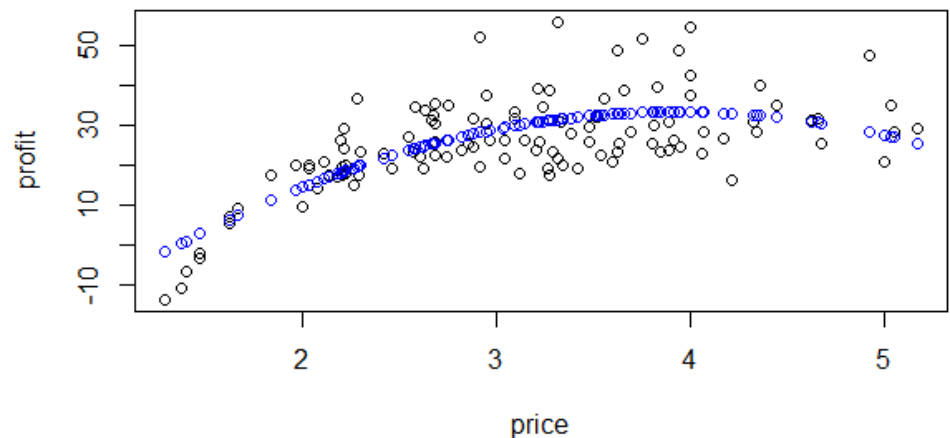
1/29 Class Notes

**1. Milkprice.R**

- a. We started class by importing 'milk.csv' and writing our own script to find the best price to pay for milk (Professor Scott has now uploaded his script 'milkprice.R' on his website)
  - i. Needed to find a model that optimized profit given this data

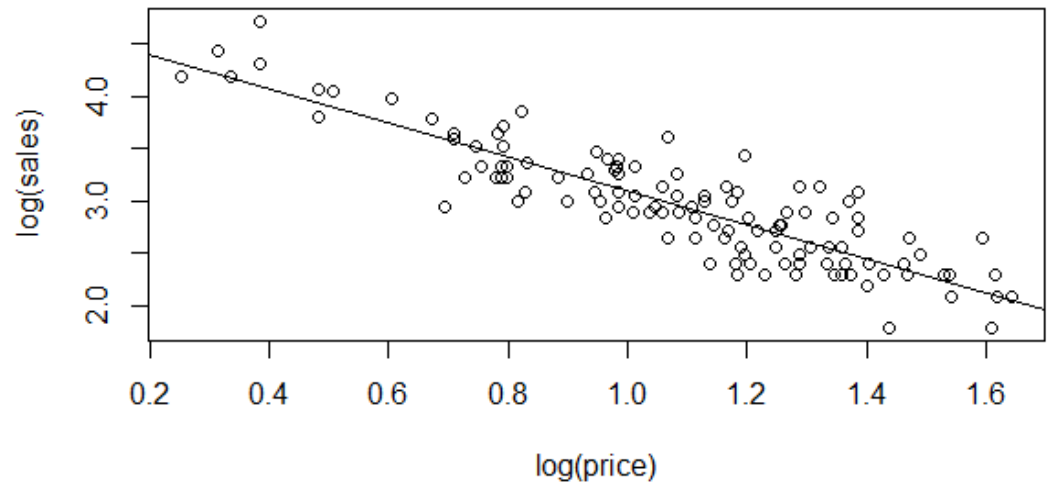


- b. **Method 1:** plot profit vs price and fit a quadratic model
  - i. Profit = revenue (# sold) - cost (# sold)  
Code: `profit = milk$sales * (milk$price - 1.50)`
    1. \$1.50 was assigned as the cost per unit
  - ii. The data appears quadratic so use a linear model to fit a quadratic equation  
Code: `lm2 = lm(profit ~ price + I(price^2), data=milk)`
  - iii. Plot the model. The blue points should give you an idea of the average profit given a price, showing that the optimal price is around 4.



c. **Method 2: Demand curve**

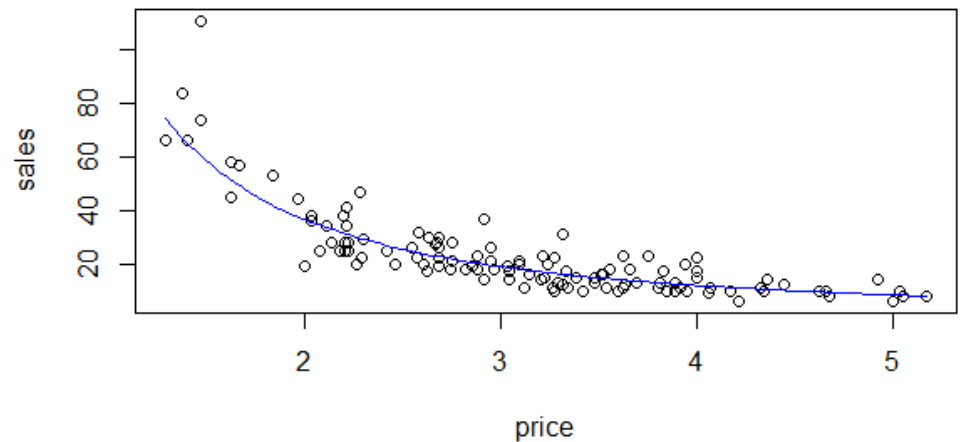
- i. Note that when you plot log of sales vs. log of price, the points appear linear. Use a linear model to find a line of best fit.



- ii. The linear relationship of the logs of both variables implies a Power Law relationship. Based on the Power Law, the intercept and slope (beta[1] and beta[2]) can be plugged into the Power Law equation as K and  $\beta$  to find an equation for profit

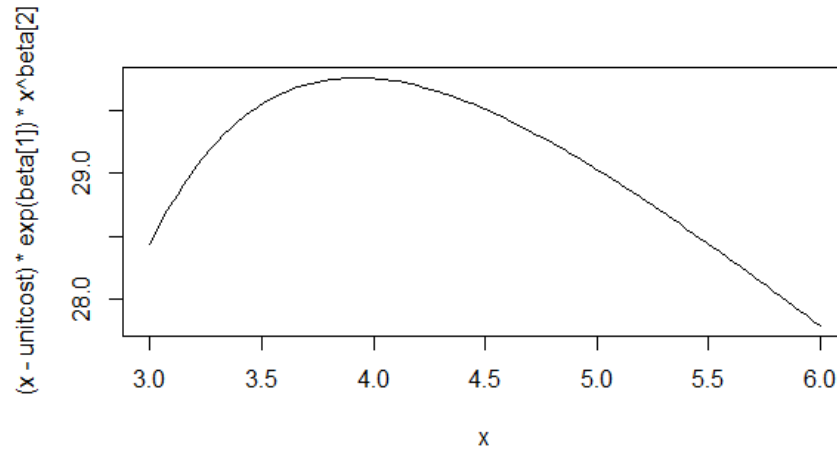
1.  $y = Kx^\beta$
2. Code: `curve(exp(beta[1])*x^beta[2], add=TRUE, col='blue')`

This gives us a curve that fits the data



- iii. We can use R to plot the profit curve as seen below. Here it shows the profit for a price range of 3 to 6.

Code: `curve( (x-unitcost)*exp(beta[1])*x^beta[2], from=3, to=6)`



## 2. Predictions

The rest of class focused on ways to predict where a data point would lie given the data.

- a. Given the equation for a line:  $y = \beta_0 + \beta_1 x_i + e_i$

The equation for a data point ( $x^*$ ) would be:  $y^* = \beta_0 + \beta_1 x^* \pm a * s_e$

- i.  $s_e$  = standard deviation of residuals  
 $a$  = a number, e.g. 1, 2, ... (some multiple)
  - ii.  $a * s_e$  = measure of variation for unpredictable piece
  - iii. Review: The Empirical Rule states that when  $a=1$  around 68% of the data is covered.  $a=2$  covers around 95% of the data.
- b. Coverage Intervals
    - i. The spread of original data points is greater than the spread of residuals, which is why the residuals can be useful in determining a coverage interval to predict data.
    - ii. When using a histogram of data in R, a coverage interval starts at either side and goes in to determine where the interval begins and ends. A central symmetric coverage interval starts at the center and goes out in both directions to cover a certain percentage of data.
    - iii. When comparing a histogram of data and a histogram of residuals of groupwise model (mean of each group), the histogram of residuals is centered around 0 and the 50% coverage interval has a much smaller width.

1. The histogram of residuals has reduced uncertainty so looking at a data's residuals can provide a more accurate predictor.
- iv. The coverage interval of the residuals provides a prediction interval.
  1. To predict using linear data, plot the linear model.
  2. Then, plot the residuals and find the standard deviation of the residuals.
    - a. Code: `sd(resid(model1))`
  3. We can now plot the zones plus or minus a standard deviation on the linear model to give us a ~70% chance of covering the point.

c. Miscellaneous Terms

- i.  $s_e$  = standard deviation of residuals
- ii.  $s_y$  = standard deviation of original data
- iii.  $R^2 = 1 - \left(\frac{s_e}{s_y}\right)^2$ 
  1. The amount of variation in y that can be predicted by x
  2. The higher the  $R^2$ , the better the fit.