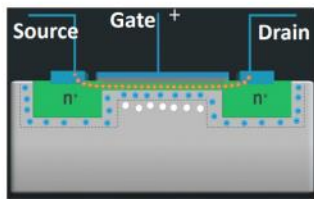
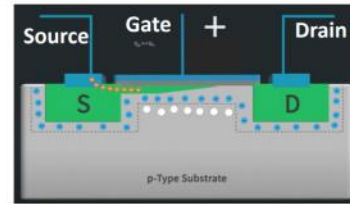
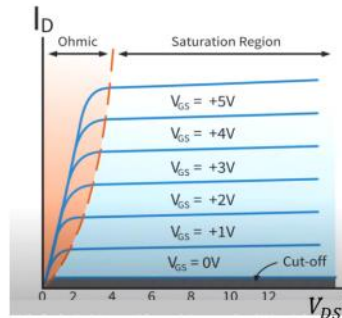


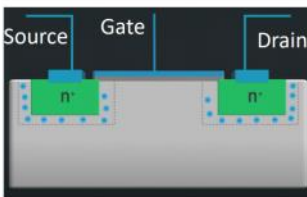
Operation regions of MOSFET



Triode or ohmic region: $V_{GD} > V_{TH}$
 $I_D = k_n [(V_{GS} - V_{TH})V_{DS} - \frac{1}{2}V_{DS}^2]$



Saturation region: $V_{GD} < V_{TH}$
 $I_D = \frac{1}{2}k_n (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS})$

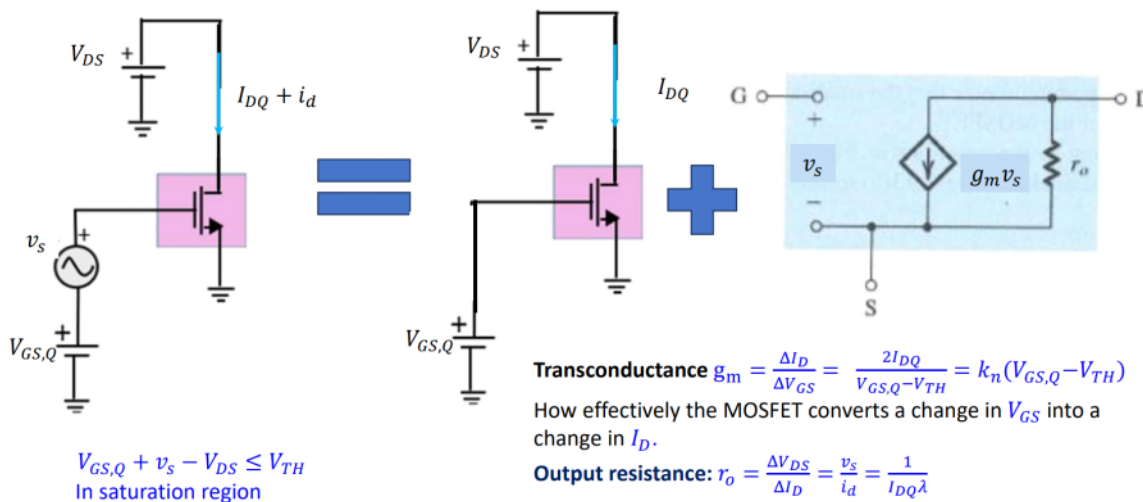


Cut-off region: $V_{GS} < V_{TH}$
 $I_D = 0$

- $\lambda = \frac{L - L'}{V_{DS}L}$: channel length modulation coefficient
- L' : actual channel length

Triode and cut-off region: switching devices
 Saturation region: amplifier

MOSFET—small-signal model



Nmos

N-depletion



$$V_{GS} = +V_C \Rightarrow \text{ON}$$

$$V_{GS} = 0 \Rightarrow \text{ON}$$

$$V_{GS} = -V_C \Rightarrow \text{OFF}$$

Pmos

P-depletion

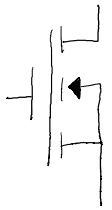


$$V_{GS} = +V_C \Rightarrow \text{OFF}$$

$$V_{GS} = 0 \Rightarrow \text{ON}$$

$$V_{GS} = -V_C \Rightarrow \text{ON}$$

N-enhancement



$$V_{GS} = +V_C \Rightarrow \text{ON}$$

$$V_{GS} = 0 \Rightarrow \text{OFF}$$

$$V_{GS} = -V_C \Rightarrow \text{OFF}$$

P-enhancement



$$V_{GS} = +V_C \Rightarrow \text{OFF}$$

$$V_{GS} = 0 \Rightarrow \text{OFF}$$

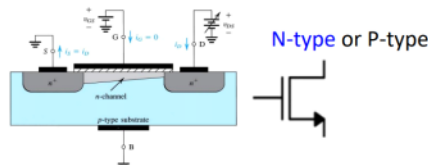
$$V_{GS} = -V_C \Rightarrow \text{ON}$$

MOSFT

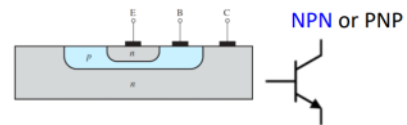
VS.

BJT

Structure



N-type or P-type



NPN or PNP

Symmetric fabrication

Yes

No

Dominant I-V characteristics

$$I_D = \frac{1}{2} k_n (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS}) - \text{Saturation}$$

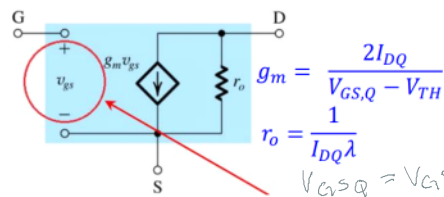
$$I_C = I_S (e^{\frac{V_{BE}}{V_T}} - 1) - \text{forward active}$$

Current control

No current flowing through G and S. The voltage of GS that controls the current through D and S.

A small current flowing through B and E controls a much larger current through C and E.

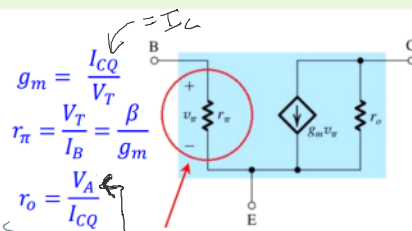
Small-signal model



$$g_m = \frac{2I_{DQ}}{V_{GS,Q} - V_{TH}}$$

$$r_o = \frac{1}{I_{DQ}\lambda}$$

$V_{GS,Q} = V_{GS}$
we think



$$g_m = \frac{I_{CQ}}{V_T}$$

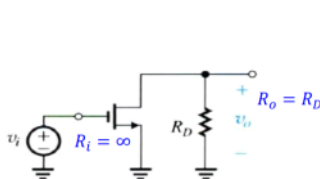
$$r_\pi = \frac{V_T}{I_B} = \frac{\beta}{g_m}$$

$$r_o = \frac{V_A}{I_{CQ}}$$

early voltage effect
miller 15 eq 200

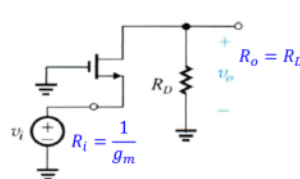
Three basic configurations: MOSFT VS. BJT

MOSFT



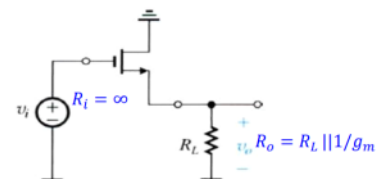
(a) Common-Source (CS)

$$A_v = -g_m R_D$$



(b) Common-Gate (CG)

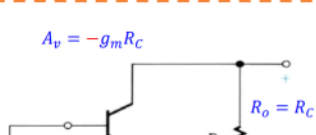
$$A_v = g_m R_D$$



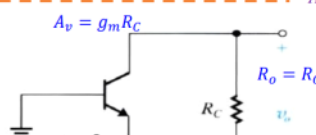
(c) Common-Drain (CD) or Source Follower

$$A_v = \frac{R_L}{R_L + 1/g_m}$$

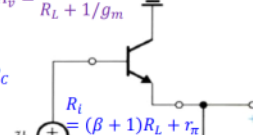
BJT



$$A_v = -g_m R_C$$



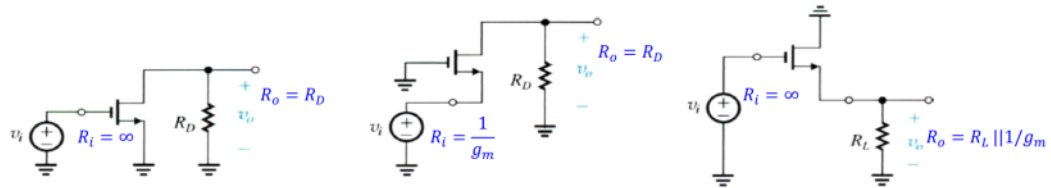
$$A_v = g_m R_C$$



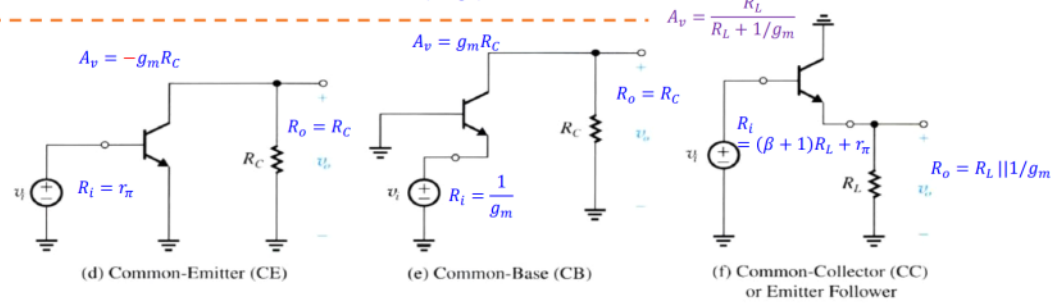
$$A_v = \frac{R_L}{R_L + 1/g_m}$$

Three basic configurations: MOSFT VS. BJT

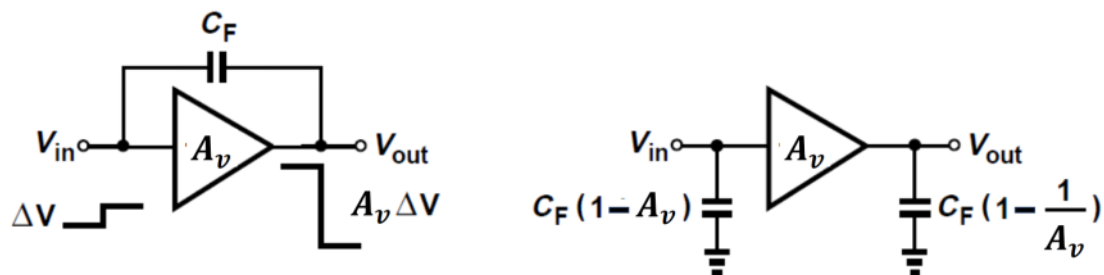
MOSFT



BJT



Example



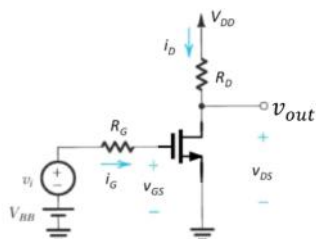
$$A_v = V_{out}/V_{in}$$

Assignments:

8.1:

A MOSFET circuit is shown in Fig. 1. It is assumed that: $V_{DD} = 10\text{ V}$, $R_G = 33\text{ K}\Omega$, $R_D = 5.6\text{ K}\Omega$ and the channel length modulation coefficient $\lambda = 0$. Furthermore, we assume that $V_{TH} = 2\text{ V}$ and $k_n = 0.9 \times 10^{-3}\text{ A/V}^2$.

- To achieve $I_D = 1\text{ mA}$, $V_{GS} = ?$
- To have V_{GS} obtained in (a), $V_{BB} = ?$ Explain why.
- To ensure the MOSFET operating in saturation, how large is the output signal swing?
- Setup a small signal circuit and calculate the component values and voltage gain A_v .
- To achieve a maximum output signal swing for $I_D = 1\text{ mA}$, $R_D = ?$
- If the channel length modulation coefficient $\lambda = 0.5$ and $R_D = 5.6\text{ K}\Omega$ are considered, the output resistance $r_o = ?$ The voltage gain $A_v = ?$



Solution:

$$I_D = \frac{1}{2} k_n (V_{GS} - V_{TH})^2$$

$$(a) I_D = \frac{1}{2} k_n (V_{GS} - V_{TH})^2 \rightarrow V_{GS} = \sqrt{\frac{2I_D}{k_n}} + V_{TH} \approx 3.5\text{ V}$$

$$(b) \text{ Since } I_G = 0 \rightarrow V_{RG} = 0 \rightarrow V_{BB} = V_{GS} = 3.5\text{ V}$$

$$(c) V_{DS} = V_{DD} - R_D I_D = 10 - 5.6\text{ K}\Omega \cdot 1\text{ mA} = 4.4\text{ V}$$

To ensure the MOSFET working in saturation, $V_{DS} \geq V_{GS} - V_{TH} = 1.5\text{ V}$, i.e., $V_{DS,min} = 1.5\text{ V}$. In addition, $V_{DS} \leq V_{DD} = 10\text{ V}$. Thus, the swing of the output signal = $\min\{4.4 - 1.5, 10 - 4.4\} = 2.9\text{ V}$.

$$(d) g_m = \frac{2I_D}{V_{GS} - V_{TH}} = 1.3\text{ mS} \rightarrow A_v = -g_m R_D \approx -7.5$$

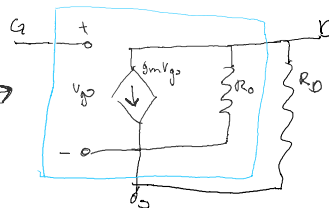
(e) To achieve a maximum output signal swing, we need to ensure the $V_{DS,Q}$ is located in the middle of the available range:

$$V_{range} = V_{DD} - V_{DS,min} = 10 - 1.5 = 8.5\text{ V} \rightarrow V_{DS,Q} = \frac{V_{range}}{2} + V_{DS,min} = 5.75\text{ V}$$

$$\rightarrow R_D = \frac{V_{DD} - V_{DS,Q}}{I_D} = \frac{4.25\text{ V}}{1\text{ mA}} = 4.25\text{ K}\Omega$$

$$(f) r_o = \frac{1}{I_D \lambda} = \frac{1}{1\text{ mA} \cdot 0.5} = 2\text{ K}\Omega$$

$$A_v = -g_m * (R_D || r_o) = -1.3\text{ mS} * (5.6\text{ K}\Omega || 2\text{ K}\Omega) = 1.9$$

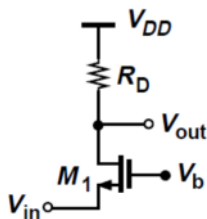


Very similar to BJT analysis

8.2:

A common gate amplifier is given in Fig.2.

- Draw the internal capacitors of the circuit.
- Simplify the circuit by merging the capacitors.
- Is there any floating capacitor in the circuit?
- If yes, how to decompose the floating capacitor into two capacitors connected to AC ground by using Millers theorem?

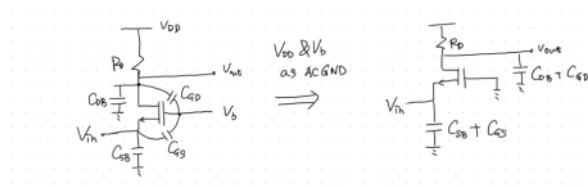


Remember that:

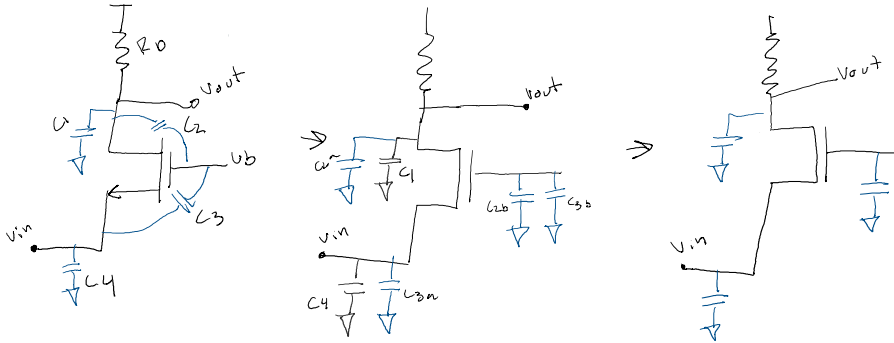
$$C_{in,Miller} = C_f (1 - A_v)$$

$$C_{out,Miller} = C_f (1 - \frac{1}{A_v})$$

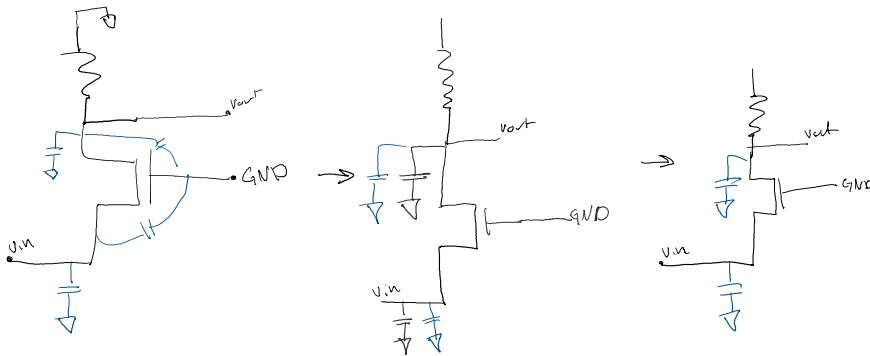
Solution:



No floating capacitor in the circuit.



BUT AS V_B IS AC GND



And the Miller becomes irrelevant!