

# **FSE/tANS Introduction and Implementation**


## **ECSE 6680 Course Project**

**04/22/2024**

# Data compression

 Facebook/Meta ZSTD - replacing gzip

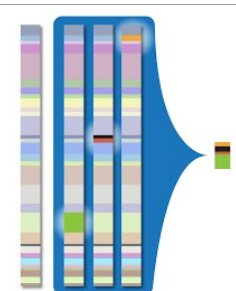
 Apple LZFSE - iPhone, MAC

 CRAM - DNA compressor

 JPEG XL - replacing JPEG ~ 3X smaller

Saving time, transmission costs,  
energy, storage, hardware costs

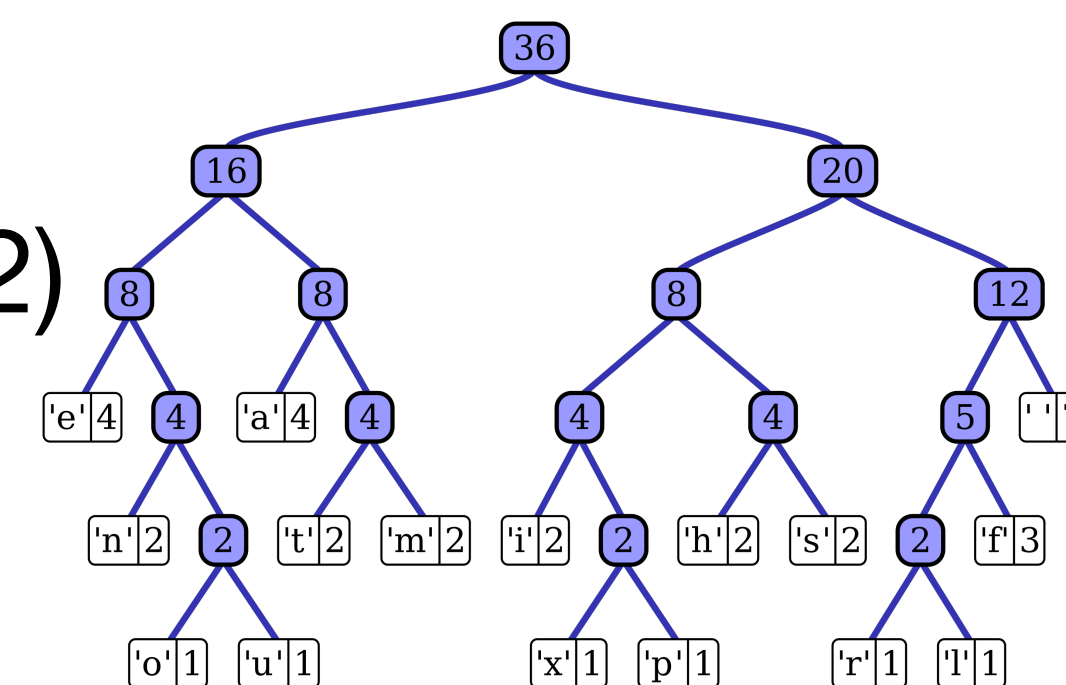
**CRAM:**  
The Data Storage  
Standard  
For Genomics



## Brief history

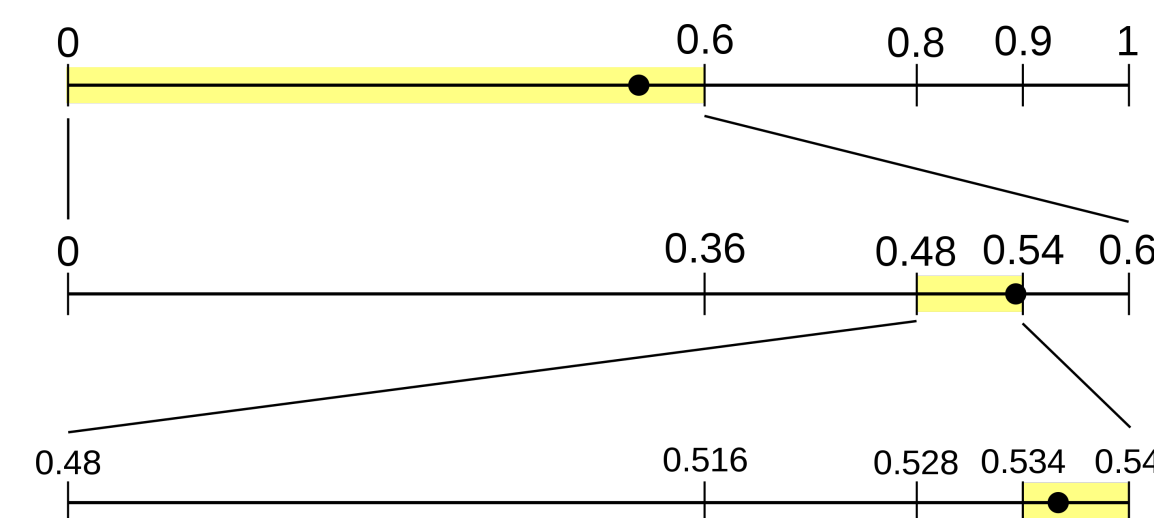
Huffman coding (1952)

Faster



Arithmetic coding (1976)

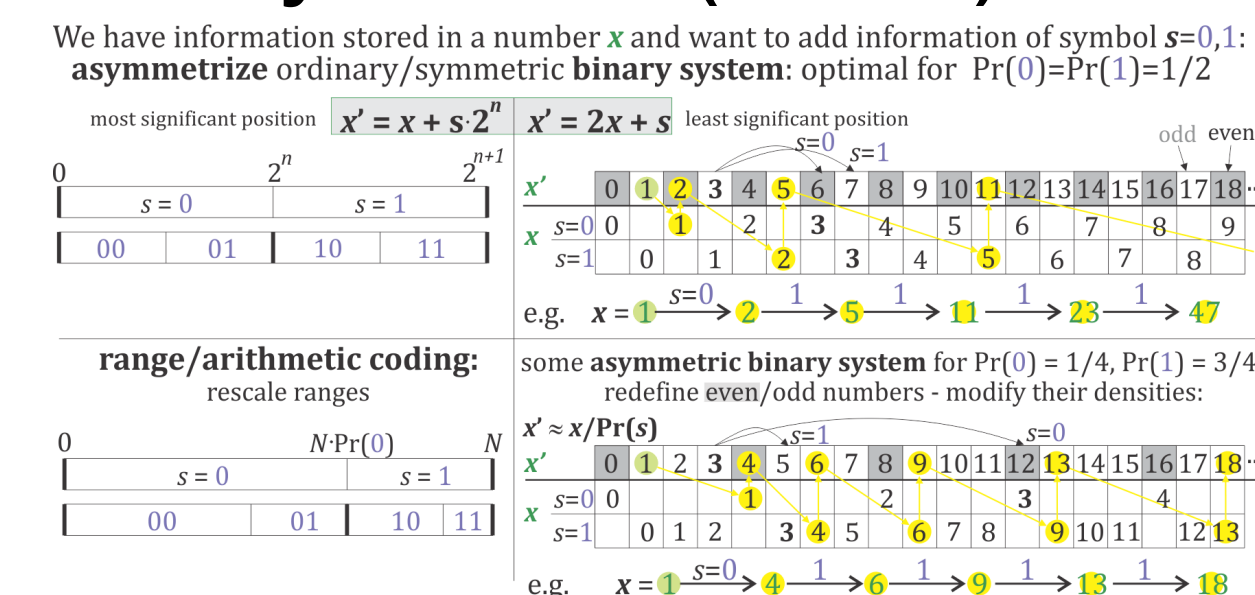
Simpler



Asymmetric numeral systems (2006)

Less memory

**tANS/FSE**



# Symmetric numeral system

Let's assume inputs are digits [0,9]

We want to encode [3,2,4,1,5] into a natural number

32415 is the answer

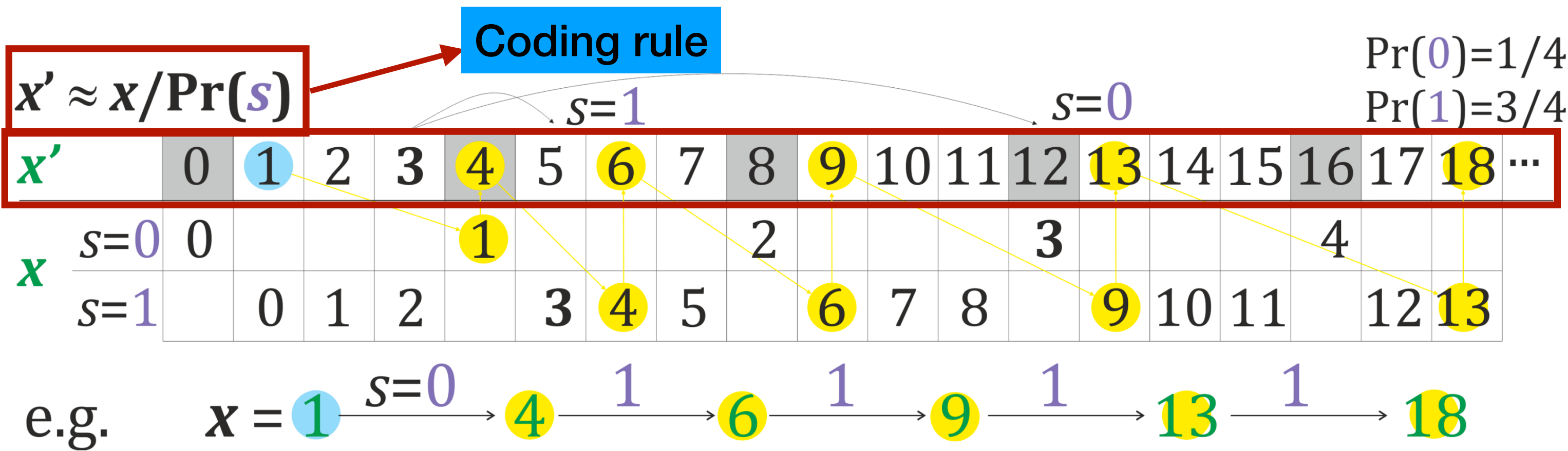
```
# given
data_input = [3,2,4,1,5]
## "encoding" process
x = 0 # ← initial state
x = x*10 + 3 #x = 3
x = x*10 + 2 #x = 32
x = x*10 + 4 #x = 324
x = x*10 + 1 #x = 3241
x = x*10 + 5 #x = 32415 ← final state
```

**If the digits [0,9] have different probabilities than 0.1?**  $\log_2(10) = \log_2 \frac{1}{0.1} = \log_2 \frac{1}{p}$

# What is ANS?

ANS - store information as a natural number  $x$

How to encode 10111 to natural number 18



**Probability of next symbol**

$x'$ : next state

$x$ : previous state

$s$ : symbol that we want to store in  $x$

Grows infinitely  $x \rightarrow \infty$

$x=1$ ,	$s=0$ ,	$x'=4$
$x=4$ ,	$s=1$ ,	$x'=6$
$x=6$ ,	$s=1$ ,	$x'=9$
$x=9$ ,	$s=1$ ,	$x'=13$
...		

# Fix state range and reuse? - renormalization

To prevent  $x \rightarrow \infty$ , enforce  $x \in I = \{L, 2L - 1\}, L = 2^n$

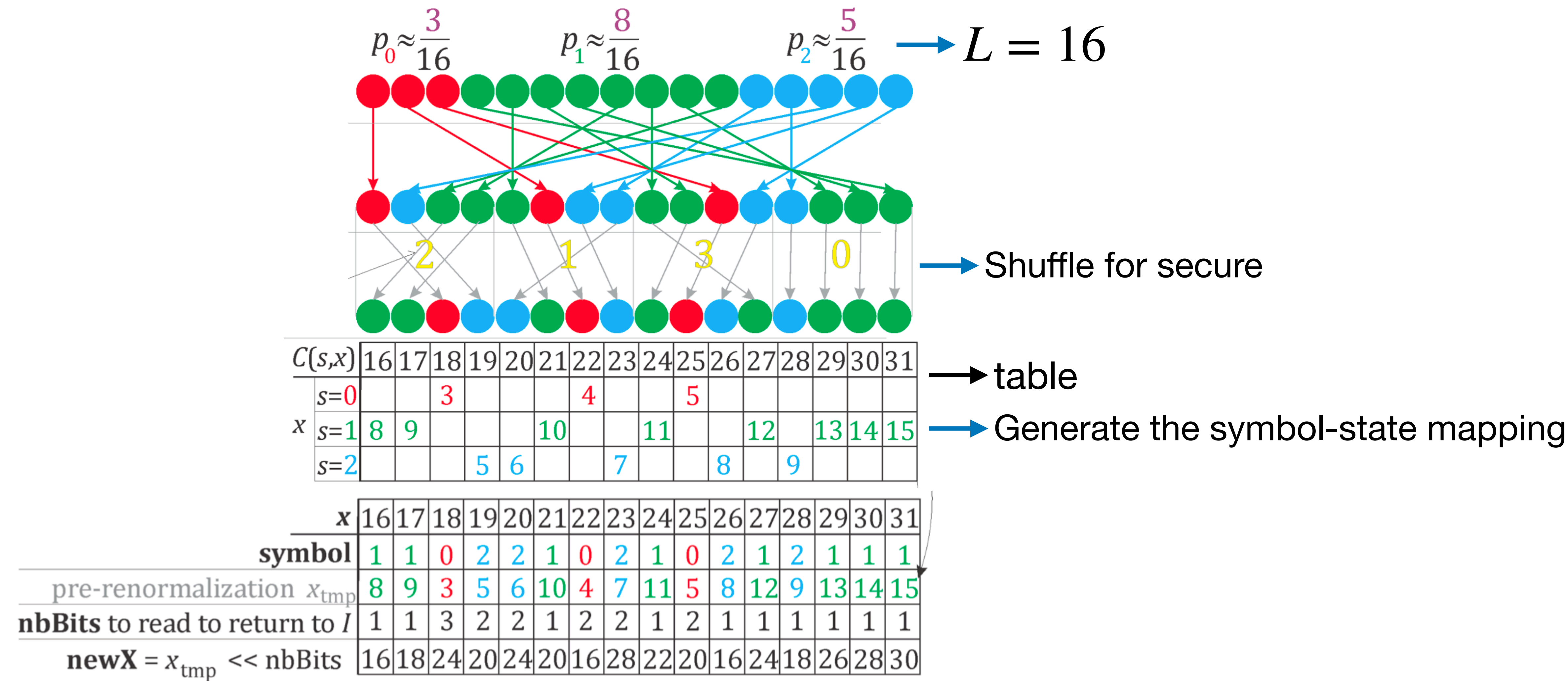
By streaming: transmitting lowest bits to bitstream

```
# input state
x_prev = 22 = 10110b
# stream out bits from x_prev until we are sure base_step(x_shrunk,s) in [8,15]
x_shrunk = 10110b = 22, out_bits = ""
x_shrunk = 1011b = 11, out_bits = "0"
```



# tabled ANS/Finite state entropy

## Another Example: encode 0, 1, 2 with probabilities



# tabled ANS/Finite state entropy-cont.

Another Example: encode 0, 1, 2 with probabilities

$C(s,x)$		16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31
$x$	$s=0$			3				4			5						
	$s=1$	8	9				10			11			12		13	14	15
	$s=2$				5	6			7			8		9			

$x$		16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31
symbol		1	1	0	2	2	1	0	2	1	0	2	1	2	1	1	1
pre-renormalization $x_{tmp}$		8	9	3	5	6	10	4	7	11	5	8	12	9	13	14	15
nbBits to read to return to $l$		1	1	3	2	2	1	2	2	1	2	1	1	1	1	1	1
$newX = x_{tmp} \ll nbBits$		16	18	24	20	24	20	16	28	22	20	16	24	18	26	28	30

# Hardware implementation

## 1. Arithmetic Package (arithmetic\_pkg.vhd)

Provides general arithmetic functions that are essential across various modules, particularly those that compute logarithmic and ceiling functions.

## 2. Entropy Package (entropy\_pkg.vhd)

Manages the entropy coding part of the system, offering functions to convert literal lengths, match lengths, and offsets into codes that are used for efficient storage and retrieval.

## 3. Compressor Package (compressor\_pkg.vhd)

Contains utilities for data compression, including hash functions and mechanisms to manage data streams and buffers effectively.

## 4. FSE Tables Package (fse\_tables\_pkg.vhd)

Stores all necessary tables for the FSE encoding process, such as state transition tables and symbol conversion tables, which are crucial for the encoder's state management.

## 5. Bitstream Merger (bitstream\_2to1\_merger.vhd)

A utility that merges two bitstreams into a single output stream. This functionality is crucial for combining multiple streams of encoded data into a unified format.

## 6. FSE to Single Bitstream Converter (fse2single\_bitstream.vhd)

Converts the multi-part FSE encoded data into a single continuous bitstream, simplifying the output for transmission or storage.

## 7. FSE Encoder (fse\_encoder.vhd)

The core module that interfaces with the entropy, arithmetic, and FSE tables packages to perform the actual data encoding. It processes input sequences and produces encoded bitstreams, along with metadata about the encoding state.