

# Project 1 FYS-STK4155

(Dated: September 15, 2023)

## I. INTRODUCTION

Machine learning is a powerful tool useful in many fields of research. One illustration of its utility is its application to terrain data analysis. Through the creation of terrain models from real data of a specific geographic area, one can effectively anticipate high-risk avalanche zones, potentially leading to life-saving interventions. This method can extend to addressing concerns related to floods, which has become a hot topic this past month (maybe write something about Hans). It can also help in aiding with spatial planning challenges, which is useful in big cities all over the world.

It is fair to say machine learning possesses immense potential to contribute to the solutions of complex and relevant challenges in our modern society, encompassing climate-related issues, urban planning, and life-saving endeavors.

The aim of this report is to study three different regression methods, ordinary least squares (OLS), Ridge and LASSO and see how these methods compare to each other when applied to different data sets. First we are going to look at the Franke function. When plotted between 0 and 1 this function looks like a mountain and a valley, which is a perfect starting point when we later want to apply these methods on digital terrain data taken from <https://earthexplorer.usgs.gov/>.

## II. THEORY

### A. Ordinary least squares (OLS)

### B. Ridge

### C. LASSO

### D. Bias-variance trade-off and resampling techniques

## III. METHOD

In the first part of this project a function called Franke function was used as the data analysed. The Franke func-

tion is given by the following equation:

$$\begin{aligned} f(x, y) = & \frac{3}{4} \exp \left( -\frac{(9x-2)^2}{4} - \frac{(9y-2)^2}{4} \right) \\ & + \frac{3}{4} \exp \left( -\frac{(9x+1)^2}{49} - \frac{(9y+1)^2}{10} \right) \\ & + \frac{1}{2} \exp \left( -\frac{(9x-7)^2}{4} - \frac{(9y-3)^2}{4} \right) \\ & - \frac{1}{5} \exp \left( -(9x-4)^2 - (9y-7)^2 \right) \end{aligned}$$

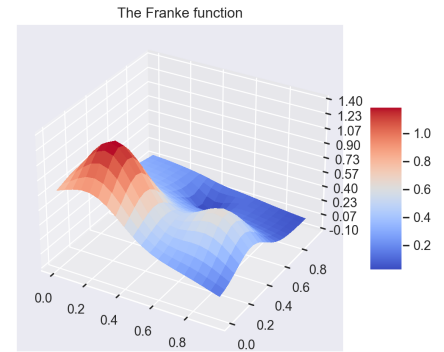


Figure 1. A plot of the Franke function

This function was fitted with the OLS method, where a polynomial with degree 5 was used to create the design matrix. Since the design matrix in this case was noninvertible, singular value decomposition was used to create the  $\beta$ -values needed to create a model of the dataset. The mean square error and the R2 score were calculated for both the testing and training datasets.

Next Ridge regression was used on the Franke function, to see if this method had a better fit than what was obtained with OLS. Different values for  $\lambda$  were used to obtain the best fit as possible.

## IV. RESULTS

## V. DISCUSSION

## VI. CONCLUSION

## REFERENCES

- Reference 1

- Reference 2

## Appendix A: Mean values and variances calculations