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TIONARIES

FUNCTIONS AS OBJECTS

- functions are first class objects:
- have types
- can be elements of data structures like lists
- can appear in expressions
- as part of an assignment statement
- as an argument to a function!!
- when coupled with lists particularly useful to use functions as arguments
- aka higher order programming

def applyToEach (L, f): function thinution as parameter

for i in range(len(L)): """assumes L is a list, f a function e, of L by f(e) """ mutates L by replacing L[i] = f(L[i])each element,

```
def applyToEach(L, f):
```

$$L[i] = f(L[i])$$

for i in range(len(L)):



$$L = [1, -2, 3.4]$$

applyToEach(L, abs)

applyToEach(L, int)

applyToEach(L, fact)

applyToEach(L, fib)

```
def applyToEach(L, f):
```

for i in range(len(L)):

L[i] = f(L[i])

L = [1, -2, 3.4]

applyToEach(L, abs)

[1, 2, 3.4]

applyToEach(L, int)

applyToEach(L, fact)

applyToEach(L, fib)

```
def applyToEach (L, f):
```

for i in range(len(L)):

L[i] = f(L[i])

L = [1, -2, 3.4]

applyToEach(L, abs)

[1, 2, 3.4]

applyToEach(L, int)

[1, 2, 3]

applyToEach(L, fact)

applyToEach(L, fib)

```
def applyToEach (L, f):
```

$$L = [1, -2, 3.4]$$

```
def applyToEach(L, f):
```

$$L[i] = f(L[i])$$

$$L = [1, -2, 3.4]$$

LISTS OF FUNCTIONS pass 16 of

```
applyFuns([abs, int, fact, fib], 4)
                                                                                                            def applyFuns (L, x):
                                                                                   for f in L:
                                                     print(f(x))
                      I function have with no params.
```

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GENERALIZATION OF HOPS

- Python provides a general purpose HOP, map
- 🐃 imple form a unary function and a collection of suitable arguments
- \circ map(abs, [1, -2, 3, -4])
- produces an 'iterable', so need to walk down it for elt in map(abs, [1, -2, 3, -4]): print(elt)
 [1, 2, 3, 4]

general form — an n-ary function and n collections of arguments

L1 = [1, 28, 36]

L2 = [2, 57, 9] for elt in map(min, L1, L2): print(elt)

[1, 28, 9]

LISTS STRINGS, TUPLES, RANGES,

Common operations

- $seq[i] \rightarrow i^{th}$ element of sequence
- len (seq) \rightarrow length of sequence
- seg1 + seg2 \rightarrow concatenation of sequences (not range)
- \circ n*seq \rightarrow sequence that repeats seq n times (not range)
- \mathbb{O} h L seq → True if e contained in sequence
- \mathbb{O} not in seq > True if e contained in sequence
- for e in seq → iterates over elements of sequence

6.00.1X LECTURE

PROPERTIES

list an	range int	tuple an	str ch	Туре Ту
any type	integers	any type	characters	Type of elements
[], [3], [3], [abc', 4]	range(10), range(1,10,2)	(), (3,), ('abc', 4)	'abc'	Examples of literals
Yes	No	No	No	Mutable

6.00.1X LECTURE

HOW TO STORE STUDENT INFO

so far, cap store using separate lists for every info

```
grade
 COUISE
                                                           names
                                ||
                                                         = /['Ana', 'John', 'Denise', 'Katy']
    Щ
                            ['B', 'A+', 'A', 'A']
[2.00, 16.0001, 20.002, 9.01]
```

- a separate list for each item
- each list must have the same length
- refers to info for a different person info stored across lists at same index, each index

6.00.1X LECTURE

STUDENT INFO HOW TO UPDATE/RETRIEVE

```
get_grade(student, name_list, grade_list, course list):
                                                                       grade
                                       COUTSE
return (course, grade)
                                                                                                        = name_list.index(student)
                                                                       = grade_list[i]
                                        course_list[i]
```

- messy if have a lot of different info to keep track of
- must maintain many lists and pass them as arguments
- must always index using integers
- must remember to change multiple lists

6.00.1X LECTURE 17

A DICTIONARY A BETTER AND CLEANER WAY -

- nice to index item of interest directly (not always int)
- nice to use one data structure, no separate lists

A list

3	2	1	0
Elem 4	Elem 3	Elem 2	Elem 1

index alem

A dictionary

:	Key 4	Key 3	Key 2	Key 1
:	Val 4	Val 3	Val 2	Val 1

index by

element

A PYTHON DICTIONARY

- stor
- ke
- Va

my_dict = {} empty empty dictionary		• Value	• key	store pairs of data
custom index by	'Katy'	'John'	'Denise'	'Ana'
element	'A'	'A+'	'A'	'B'

grades

DICTIONARY LOOKUP

- similar to indexing into a list
- looks up the key
- returns the value associated with the key
- if key isn't found, get an error

'Katy'	'John'	'Denise'	'Ana'
'A'	' A+ '	'A'	'B'

```
grades['Sylvan']
                                                   grades['John']
                                                                                                    grades = {'Ana':'B', 'John':'A+', 'Denise':'A', 'Katy':'A'}
→ gives a KeyError
                                                     \rightarrow evaluates to 'A+'
```

6.00.1X LECTURE

DICTIONARY OPERATIONS

'Sylvan'	'Katy'	'John'	'Denise'	'Ana'
'A'	'A'	'A+'	ıΑι	'B'

```
grades = {'Ana':'B', 'John':'A+', 'Denise':'A', 'Katy':'A'}
```

add an entry

```
grades['Sylvan'] = 'A'
```

test if key in dictionary

```
'John' in grades
'Daniel' in grades
```

→ returns True → returns False

delete entry

del(grades['Ana'])

6.00.1X LECTURE

OPERATIONS DICTIONARY

'Katy'	'John'	'Denise'	'Ana'
, V.	' A+ '	1 A 1	'B'

```
grades = {'Ana':'B', 'John':'A+', 'Denise':'A', 'Katy':'A'}
```

get an iterable that acts like a tuple of all keys no guaranteed grades kerrain.

get an iterable that acts like a tuple of all values grades.values() >> returns ['A', 'A', 'A+', 'B']

no guaranteed order

DICTIONARY KEYS and VALUES

- values
- any type (immutable and mutable)
- can be duplicates
- dictionary values can be lists, even other dictionaries!
- keys
- must be **unique**
- immutable type (int, float, string, tuple, bool)
- actually need an object that is **hashable**, but think of as immutable as all immutable types are hashable
- careful with float type as a key
- no order to keys or values!

```
d = \{4:\{1:0\}, (1,3):"twelve", 'const':[3.14,2.7,8.44]\}
```

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dict

- ordered sequence of elements
- look up elements by an integer index
- indices have an order
- index is an integer

- matches "keys" to "values"
- look up one item by another item
- no order is guaranteed
- key can be any immutable type

ANALYZE SONG LYRICS **EXAMPLE: 3 FUNCTIONS TO**

- 1) create a frequency dictionary mapping str:int
- find word that occurs the most and how many times
- use a list, in case there is more than one word
- return a tuple (list, int) for (words_list, highest_freq)
- find the words that occur at least X times
- let user choose "at least X times", so allow as parameterS
- containing the list of words ordered by their frequency return a list of tuples, each tuple is a (list, int)
- IDEA: From song dictionary, find most frequent word. Delete mutating the song dictionary. most common word. Repeat. It works because you are

6.00.1XLECTURE

CREATING A DICTIONARY

```
def lyrics
                                                                                  myDict = {}
return myDict
                                                                    for word in lyrics:
                             else.
                                                      if word in myDict:
                                                                                               _to_frequencies(lyrics):
              myDict[word]
                                         myDict[word]
                П
                                           can iterate over list
                                                        can iterate over keys
                                                 in dictionary
                                   update value
                            associated with key
```

6.00.1X LECTURE

USING THE DICTIONARY

```
def most common words (freqs):
                                         for
                                                       Words
                                                                     best
                                                                                   values
return
                                          ス
                            1-
H
                                                                      ||
                                                      H-
                                                                                    ||
(words, best)
                                                                    max (values)
                          freqs[k]
             words.append(k)
                                       freqs:
                                                                                 freqs.values()
                             ||
||
                                        can iterate over keys
                                 in dictionary
                           best:
                                                                    this is an iterable, so can
                                                              apply built-in function
```

6.00.1X LECTURE

PROPERTIES LEVERAGING DICTIONARY

```
def words_often(freqs, minTimes):
return result
                                                                                                                                                                                            done = False
                                                                                                                                                                      while not done:
                                                                                                                                                                                                               result = []
                                           else:
                                                                                                                            if temp[1] >= minTimes:
                                                                                                                                                temp = most_common_words(freqs)
                      done = True
                                                                                  for w in temp[0]:
                                                                                                      result.append(temp)
                                                             del(freqs[w])
                                    can directly mutate dictionally; makes it easier to iterate
```

6.00.1X LECTURE

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print(words_often(beatles, 5))

FIBONACCI RECURSIVE CODE

def

fib(n):

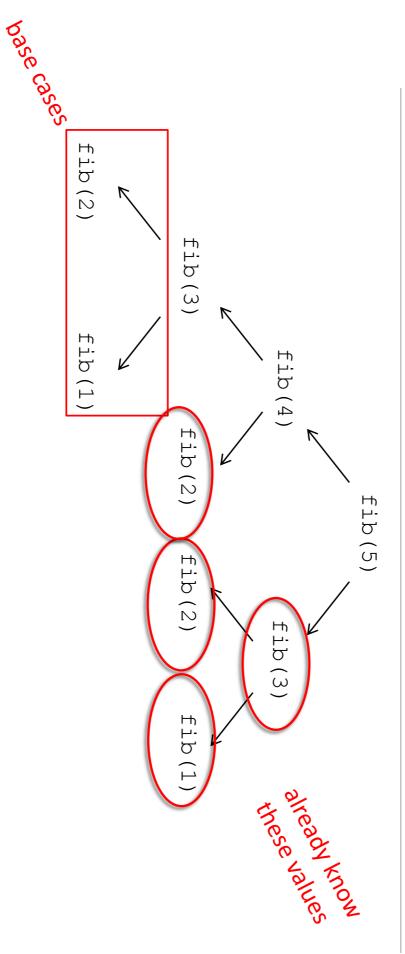
```
two base cases
                                            else:
                                                                                    elif n ==
                                                                                                                             if n == 1:
                       return fib (n-1)
                                                               return 2
                                                                                                         return 1
                                                                                    \sim
                      + fib(n-2)
```

- calls itself twice
- this code is inefficient

6.00.1X LECTURE

INEFFICIENT FIBONACCI

$$fib(n) = fib(n-1) + fib(n-2)$$



- recalculating the same values many times!
- could keep track of already calculated values

6.00.1X LECTURE

FIBONACCI WITH A DICTIONARY

```
def fib_efficient(n, d):
    if n in d:
        return d[n]
    else:
        ans = fib_efficient(n-1, d) + film_efficient(n-2, d)
        d[n] = ans
        return ans

d = {1:1, 2:2} base case
    print(fib_efficient(6, d))
```

- do a lookup first in case already calculated the value
- modify dictionary as progress through function calls

6.00.1X LECTURE 33

GLOBAL VARIABLES

- can be dangerous to use
 - breaks the scoping of variables by function call
 - allows for side effects of changing variable values in ways that affect other computation
- but can be convenient when want to keep track of information inside a function

example - measuring how often fib and fib_efficient are called

6.00.1X LECTURE

TRACKING EFFICIENCY

```
def
                                                                                                                                              fib(n):
                                                                                                                           global numFibCalls
                   else:
                                                                                                          numFibCalls += 1
                                                      elif n == 2:
                                                                                         if n == 1:
                                    return 2
return fib (n-1) + fib (n-2)
                                                                       return 1
                                                                                                                                                 def
                                                                                           global numFibCalls -> outside scope of numFibCalls += 1

if n i--
                                                                                                                                               fibef(n, d):
                                                             0 L S O .
                                                                            return d[n]
                                          ans = fibef (n-1, d) + fibef (n-2, d)
          return ans
                          d[n] = ans
```

6.00.1X LECTURE

TRACKING EFFICIENCY

```
print('function calls', numFibCalls)
                      print(fib_efficient(12, d))
                                               Q
                                                                                                                                    print('function
                                                                                                                                                          print(fib(12))
                                                                                          numFibCalls
                                                                                                                                                                                                         numFibCalls = 0
                                             = \{1:1, 2:2\}
                                                                                              ||
                                                                                                                                      calls', numFibCalls)
```