final project

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descriptive statistics

Distribution

```
# Load necessary libraries
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
##
library(tidyr)
library(ggplot2)
library(GGally)
## Registered S3 method overwritten by 'GGally':
     method from
     +.gg
            ggplot2
library(gridExtra)
## Attaching package: 'gridExtra'
## The following object is masked from 'package:dplyr':
##
##
       combine
# Read the data
data <- read.csv("./Project_1_data.csv")</pre>
data[data == ""] <- NA
# 1. Descriptive statistics table for all variables
skimr::skim(data)
```

Table 1: Data summary

Name	data
Number of rows	948
Number of columns	14

Column type frequency:
character 10
numeric 4

Group variables None

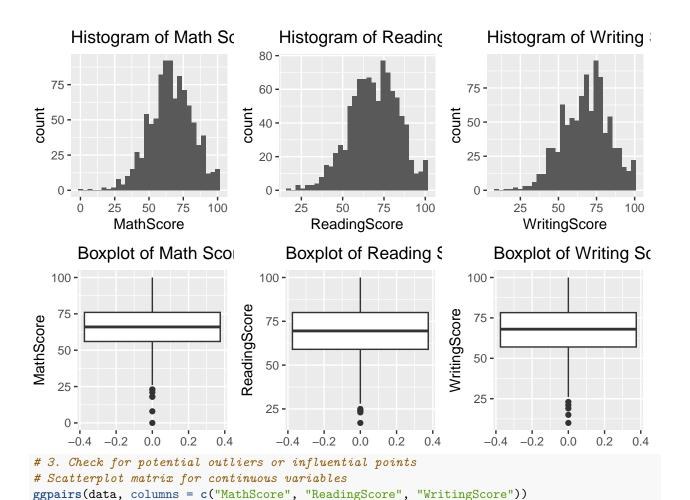
Variable type: character

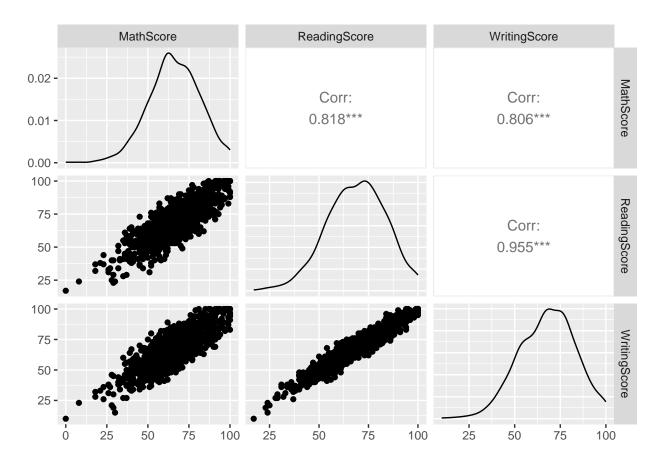
skim_variable	n_missing	complete_rate	min	max	empty	n_unique	whitespace
Gender	0	1.00	4	6	0	2	0
EthnicGroup	59	0.94	7	7	0	5	0
ParentEduc	53	0.94	11	18	0	6	0
LunchType	0	1.00	8	12	0	2	0
TestPrep	55	0.94	4	9	0	2	0
ParentMaritalStatus	49	0.95	6	8	0	4	0
PracticeSport	16	0.98	5	9	0	3	0
IsFirstChild	30	0.97	2	3	0	2	0
TransportMeans	102	0.89	7	10	0	2	0
WklyStudyHours	37	0.96	3	6	0	3	0

Variable type: numeric

skim_variable	n_missing	$complete_rate$	mean	sd	p0	p25	p50	p75	p100	hist
NrSiblings	46	0.95	2.16	1.48	0	1	2.0	3.00	7	
MathScore	0	1.00	65.98	15.53	0	56	66.0	76.00	100	
ReadingScore	0	1.00	68.84	14.80	17	59	69.5	80.00	100	
WritingScore	0	1.00	67.93	15.41	10	57	68.0	78.25	100	

```
# 2. Explore distribution of results and consider potential transformations
# Histograms for continuous variables
hist_math <- ggplot(data, aes(x = MathScore)) + geom_histogram(bins = 30) + ggtitle("Histogram of Math hist_reading <- ggplot(data, aes(x = ReadingScore)) + geom_histogram(bins = 30) + ggtitle("Histogram of hist_writing <- ggplot(data, aes(x = WritingScore)) + geom_histogram(bins = 30) + ggtitle("Histogram of hist_writing <- ggplot(data, aes(y = MathScore)) + geom_boxplot() + ggtitle("Boxplot of Math Scores")
box_reading <- ggplot(data, aes(y = ReadingScore)) + geom_boxplot() + ggtitle("Boxplot of Reading Score box_writing <- ggplot(data, aes(y = WritingScore)) + geom_boxplot() + ggtitle("Boxplot of Writing Score # Grid of plots
grid.arrange(hist_math, hist_reading, hist_writing, box_math, box_reading, box_writing, ncol = 3)</pre>
```





Missing Value

```
library(reshape2)
##
## Attaching package: 'reshape2'
## The following object is masked from 'package:tidyr':
##
##
       smiths
# Creating a function to count NA and empty strings as missing values
count_missing <- function(x) sum(is.na(x) | x == "")</pre>
# Calculating the missing values
missing_values <- sapply(data, function(x) count_missing(x))</pre>
# Creating a dataframe for missing values
missing_data_frame <- data.frame(Variable = names(missing_values), MissingValues = missing_values)
# Convert empty strings to NA
data[data == ""] <- NA</pre>
# Melt the data for visualization
melted_data <- melt(data.frame(row = 1:nrow(data), data), id.vars = 'row')</pre>
# Creating the heatmap
ggplot(melted_data, aes(x = variable, y = row)) +
geom_tile(aes(fill = is.na(value))) +
```

```
scale_fill_manual(values = c('white', 'red'), guide = FALSE) +
theme_minimal() +
theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
labs(x = 'Variables', y = 'Observation Rows', title = 'Missing Data Heatmap')
```

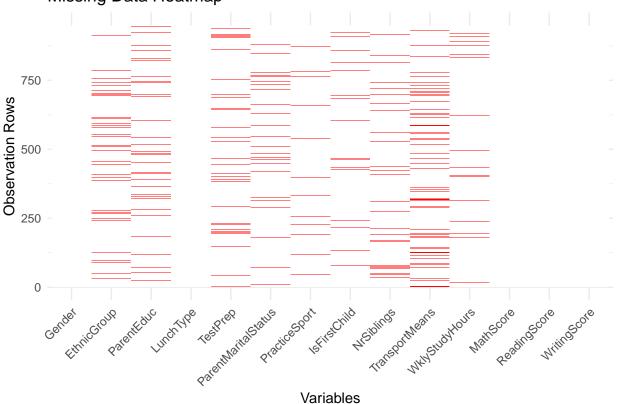
```
## Warning: The `guide` argument in `scale_*()` cannot be `FALSE`. This was deprecated in
## ggplot2 3.3.4.
## i Please use "none" instead.
```

This warning is displayed once every 8 hours.

Call `lifecycle::last_lifecycle_warnings()` to see where this warning was

generated.

Missing Data Heatmap



missing_data_frame

##		Variable	MissingValues
##	Gender	Gender	0
##	EthnicGroup	EthnicGroup	59
##	ParentEduc	ParentEduc	53
##	LunchType	LunchType	0
##	TestPrep	TestPrep	55
##	${\tt ParentMaritalStatus}$	${\tt ParentMaritalStatus}$	49
##	PracticeSport	${\tt PracticeSport}$	16
##	IsFirstChild	IsFirstChild	30
##	NrSiblings	NrSiblings	46
##	TransportMeans	${\tt TransportMeans}$	102
##	WklyStudyHours	WklyStudyHours	37
##	MathScore	MathScore	0
##	ReadingScore	ReadingScore	0

Data Preprocessing

Filling Missing Value

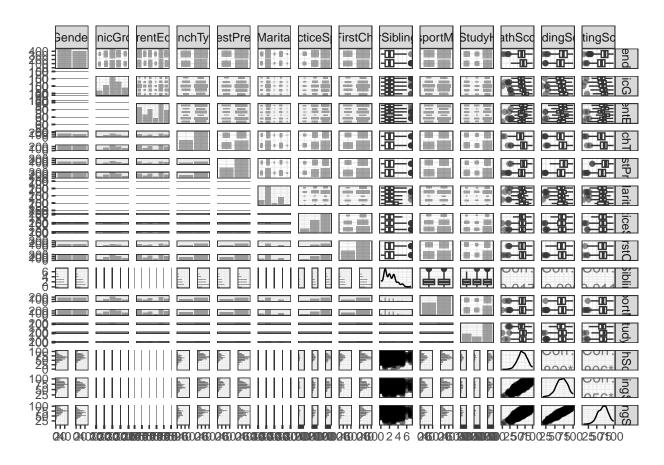
```
# Imputing missing values
# For columns with fewer missing values, replace with mode
get_mode <- function(v) {</pre>
  uniqv <- unique(v)</pre>
  uniqv[which.max(tabulate(match(v, uniqv)))]
data$PracticeSport[is.na(data$PracticeSport)] <- get_mode(data$PracticeSport)</pre>
data$IsFirstChild[is.na(data$IsFirstChild)] <- get_mode(data$IsFirstChild)</pre>
# For columns with more missing values, you can choose to impute or drop
# Imputing with mode (as an example)
data$EthnicGroup[is.na(data$EthnicGroup)] <- get_mode(data$EthnicGroup)</pre>
data$ParentEduc[is.na(data$ParentEduc)] <- get_mode(data$ParentEduc)</pre>
data$TestPrep[is.na(data$TestPrep)] <- get_mode(data$TestPrep)</pre>
data$ParentMaritalStatus[is.na(data$ParentMaritalStatus)] <- get mode(data$TestPrep)
data$WklyStudyHours[is.na(data$WklyStudyHours)] <- get_mode(data$WklyStudyHours)
data$NrSiblings[is.na(data$NrSiblings)] <- get_mode(data$NrSiblings)</pre>
# Alternatively, to drop rows with NA values in these columns-TransportMeans
data <- data %>% drop_na(TransportMeans)
# Creating a function to count NA and empty strings as missing values
count_missing <- function(x) sum(is.na(x) | x == "")</pre>
# Calculating the missing values
missing_values <- sapply(data, function(x) count_missing(x))</pre>
# Creating a dataframe for missing values
missing_data_frame <- data.frame(Variable = names(missing_values), MissingValues = missing_values)
```

Examine correlation/pairwise

Examine the marginal distributions and pairwise relationships between variables

```
# Load necessary libraries
library(tidyverse)
library(ggplot2)
library(GGally)

# draw the pariplot
ggpairs(data, columns=1:14, aes(alpha = 0.3))+
theme_bw()
```

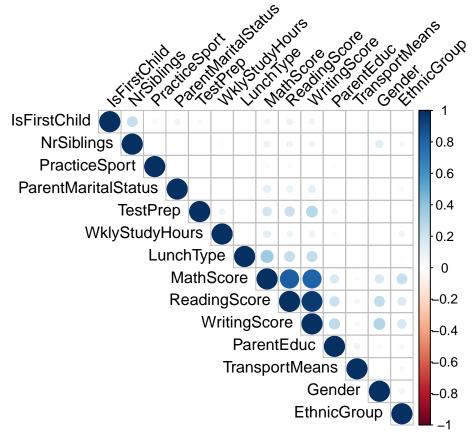


Correlation between variables

```
# Load necessary libraries
library(greybox)
## Package "greybox", v2.0.0 loaded.
##
## Attaching package: 'greybox'
## The following object is masked from 'package:lubridate':
##
##
       hm
## The following object is masked from 'package:tidyr':
##
##
       spread
library(tidyverse)
library(corrplot)
## corrplot 0.92 loaded
\# Compute the Cramer's V correlation between variables
cramer_v_matrix <- assoc(data, method = "auto")</pre>
# Extract the matrix with Cramer's V values
cramer_v_values <- as.matrix(cramer_v_matrix$value)</pre>
```

Print the correlation matrix results
knitr::kable(cramer_v_values, digits = 3)

	CondEthni	Оп	t Tryler ob	Tout	Domont M	- D4 104	-dCF:	- OVE-: CUI-	16E	SAN ALCO	+ M-II-CD	. IOnitin ad
	Gendennin	coenan	LEGICI	Testre	neaprentivi	anracou	caentarite construction	CIMMIN	ımgansı	ONATKIIGADI	tsMy.HoSRoeredi:	
Gender	1.0000.064	0.042	0.000	0.000	0.000	0.000	0.000	0.126	0.000	0.000	$0.168 \ 0.244$	0.294
EthnicGr	comp641.000	0.050	0.018	0.000	0.047	0.000	0.000	0.054	0.044	0.060	$0.240 \ 0.160$	0.177
ParentEd	l100c0420.050	1.000	0.000	0.069	0.000	0.018	0.000	0.000	0.074	0.036	$0.163 \ 0.217$	0.260
LunchTy	p@.0000.018	0.000	1.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	$0.357 \ 0.236$	0.246
TestPrep	0.0000.000	0.069	0.000	1.000	0.000	0.000	0.032	0.000	0.000	0.070	$0.184\ 0.217$	0.286
ParentMa	a 0i.0:10:0:0:0:1	0.000	0.000	0.000	1.000	0.000	0.074	0.000	0.000	0.000	$0.118 \ 0.099$	0.100
PracticeS	000.00 0000 q	0.018	0.000	0.000	0.000	1.000	0.045	0.000	0.000	0.000	$0.022 \ 0.033$	0.012
IsFirstCh	ni 0 d0000.000	0.000	0.000	0.032	0.074	0.045	1.000	0.235	0.000	0.000	$0.061 \ 0.083$	0.075
NrSibling	gs0.1260.054	0.000	0.000	0.000	0.000	0.000	0.235	1.000	0.000	0.024	$0.088 \ 0.081$	0.084
Transpor	t 0/10/2003 .044	0.074	0.000	0.000	0.000	0.000	0.000	0.000	1.000	0.000	$0.030 \ 0.056$	0.047
WklyStu	d 9.H000 s060	0.036	0.000	0.070	0.000	0.000	0.000	0.024	0.000	1.000	$0.119 \ 0.079$	0.075
MathSco	r 0 .1680.240	0.163	0.357	0.184	0.118	0.022	0.061	0.088	0.030	0.119	$1.000 \ 0.820$	0.806
ReadingS	5000 24 40.160	0.217	0.236	0.217	0.099	0.033	0.083	0.081	0.056	0.079	$0.820\ 1.000$	0.956
WritingS	c 0 r 2 940.177	0.260	0.246	0.286	0.100	0.012	0.075	0.084	0.047	0.075	$0.806 \ 0.956$	1.000



Cramér's V (for categorical

variables) varies from 0 (corresponding to no association between the variables) to 1 (complete association) and can reach 1 only when each variable is completely determined by the other.

Strength of association is calculated for nominal vs nominal with a bias corrected Cramer's V, numeric vs numeric with Spearman (default) or Pearson correlation, and nominal vs numeric with ANOVA. There should be a lot of no relation, and no two of the predictors are colinearity. If auto, it will automatically select the compare method for these correlation:

```
library(car)
```

```
## Loading required package: carData
## Attaching package: 'car'
## The following object is masked from 'package:purrr':
##
##
       some
## The following object is masked from 'package:dplyr':
##
##
       recode
set.seed(123)
splitRatio <- 0.8
trainIndex <- sample(seq_len(nrow(data)), size = floor(splitRatio * nrow(data)))</pre>
trainData <- data[trainIndex, ]</pre>
testData <- data[-trainIndex, ]</pre>
# Splitting the train dataset into independent variables (X) and dependent variables (Y)
X_train <- trainData %>% select(-c(MathScore, ReadingScore, WritingScore))
Y_math_train <- trainData$MathScore
Y reading train <-trainData$ReadingScore
Y writing train <- trainData$WritingScore
```

Even if two variables are statistically correlated, it does not necessarily mean that they lead to severe multicollinearity. For example, two variables may be statistically related in some categories, but their overall linear relationship may not be strong. So both are included in the model.

Model Selection

Despite the absence of discernible linear correlations among the variables, the inclusion of interaction terms is justified, guided by prior theoretical knowledge and practical considerations.

```
# Checking for interaction effects (example for math score)
full_model_math_interaction <- lm(Y_math_train ~ (.)^2, data = X_train)
full_model_reading_interaction <- lm(Y_reading_train ~ (.)^2, data = X_train)
full_model_writing_interaction <- lm(Y_writing_train ~ (.)^2, data = X_train)

# backward modeling(compare)
AICmodel_math_interaction =
    step(full_model_math_interaction, trace = 0, direction='backward')
BICmodel_math_interaction =
    step(full_model_math_interaction, scale = log(nrow(X_train)), trace = 0, direction='backward')

# show parameter numbers
num_params_AICmodel <- length(coef(AICmodel_math_interaction))
num_params_BICmodel <- length(coef(BICmodel_math_interaction))</pre>
```

```
cat("AIC Model Parameters:", num_params_AICmodel, "\n")
## AIC Model Parameters: 120
cat("BIC Model Parameters:", num_params_BICmodel, "\n")
## BIC Model Parameters: 246
```

Consequently, a comprehensive model was formulated, encompassing all 11 independent variables along with their respective pairwise interaction terms. In the ensuing stages of the analysis, a focus will be maintained on selecting a parsimonious subset of variables, with an aim to mitigate the risk of overfitting.

```
# try AIC and BIC
model_math_interaction = AICmodel_math_interaction
model_reading_interaction =
   step(full_model_reading_interaction, trace = 0, direction='backward')
model_writing_interaction =
   step(full_model_writing_interaction, trace = 0, direction='backward')
```

Initially, we performed a approach combining automated procedures and criterion-based with both the Akaike Information Criterion (AIC) and the Bayesian Information Criterion (BIC) for model selection. It was observed that the application of the AIC criterion resulted in a model with fewer variables. Thus, we utilized the AIC criterion for backward elimination.

```
# try LASSO
library(glmnet)
## Loading required package: Matrix
## Attaching package: 'Matrix'
## The following objects are masked from 'package:tidyr':
##
##
       expand, pack, unpack
## Loaded glmnet 4.1-8
X_math <- model.matrix(~ Gender + EthnicGroup + ParentEduc +</pre>
                   LunchType + TestPrep + ParentMaritalStatus +
                   PracticeSport + IsFirstChild + NrSiblings +
                   TransportMeans + WklyStudyHours +
                   Gender:LunchType + Gender:PracticeSport +
                   EthnicGroup:ParentEduc + EthnicGroup:IsFirstChild +
                   ParentEduc:TestPrep + ParentEduc:ParentMaritalStatus +
                   ParentEduc:PracticeSport + ParentEduc:IsFirstChild +
                   LunchType:PracticeSport + LunchType:TransportMeans +
                   TestPrep:WklyStudyHours + ParentMaritalStatus:PracticeSport + ParentMaritalStatus:Is
                   data = X train)
# cv
cv_model <- cv.glmnet(X_math, Y_math_train, alpha = 1)</pre>
best_lambda <- cv_model$lambda.min</pre>
lasso_model <- glmnet(X_math, Y_math_train, alpha = 1, lambda = best_lambda)</pre>
coef(lasso_model)
## 121 x 1 sparse Matrix of class "dgCMatrix"
                                                                    s0
```

```
## (Intercept)
                                                           58.4368761
## (Intercept)
## Gendermale
                                                            2.8960783
## EthnicGroupgroup B
## EthnicGroupgroup C
## EthnicGroupgroup D
## EthnicGroupgroup E
                                                            5.8071333
## ParentEducbachelor's degree
## ParentEduchigh school
                                                           -1.3483799
## ParentEducmaster's degree
## ParentEducsome college
## ParentEducsome high school
                                                           -1.7073150
## LunchTypestandard
                                                           8.5356902
## TestPrepnone
                                                           -4.5652098
## ParentMaritalStatusmarried
## ParentMaritalStatusnone
## ParentMaritalStatussingle
## ParentMaritalStatuswidowed
## PracticeSportregularly
## PracticeSportsometimes
## IsFirstChildyes
## NrSiblings
## TransportMeansschool_bus
## WklvStudvHours> 10
                                                            0.2125310
## WklyStudyHours10-May
                                                            0.0202314
## Gendermale:LunchTypestandard
## Gendermale:PracticeSportregularly
                                                            1.2942875
## Gendermale:PracticeSportsometimes
## EthnicGroupgroup B:ParentEducbachelor's degree
## EthnicGroupgroup C:ParentEducbachelor's degree
## EthnicGroupgroup D:ParentEducbachelor's degree
## EthnicGroupgroup E:ParentEducbachelor's degree
                                                           -4.2614010
## EthnicGroupgroup B:ParentEduchigh school
## EthnicGroupgroup C:ParentEduchigh school
## EthnicGroupgroup D:ParentEduchigh school
## EthnicGroupgroup E:ParentEduchigh school
## EthnicGroupgroup B:ParentEducmaster's degree
                                                          0.3791516
## EthnicGroupgroup C:ParentEducmaster's degree
## EthnicGroupgroup D:ParentEducmaster's degree
                                                            4.9106200
## EthnicGroupgroup E:ParentEducmaster's degree
## EthnicGroupgroup B:ParentEducsome college
## EthnicGroupgroup C:ParentEducsome college
## EthnicGroupgroup D:ParentEducsome college
                                                           4.4099481
## EthnicGroupgroup E:ParentEducsome college
## EthnicGroupgroup B:ParentEducsome high school
                                                          -2.4117233
## EthnicGroupgroup C:ParentEducsome high school
                                                          -2.3144843
## EthnicGroupgroup D:ParentEducsome high school
## EthnicGroupgroup E:ParentEducsome high school
                                                           2.4631429
## EthnicGroupgroup B:IsFirstChildyes
## EthnicGroupgroup C:IsFirstChildyes
## EthnicGroupgroup D:IsFirstChildyes
## EthnicGroupgroup E:IsFirstChildyes
## ParentEducbachelor's degree:TestPrepnone
## ParentEduchigh school:TestPrepnone
                                                           -0.5221445
```

```
## ParentEducmaster's degree:TestPrepnone
## ParentEducsome college:TestPrepnone
## ParentEducsome high school:TestPrepnone
## ParentEducbachelor's degree:ParentMaritalStatusmarried
## ParentEduchigh school:ParentMaritalStatusmarried
## ParentEducmaster's degree:ParentMaritalStatusmarried
## ParentEducsome college:ParentMaritalStatusmarried
## ParentEducsome high school:ParentMaritalStatusmarried
## ParentEducbachelor's degree:ParentMaritalStatusnone
                                                          -3.6751603
## ParentEduchigh school:ParentMaritalStatusnone
                                                          -1.5043643
## ParentEducmaster's degree:ParentMaritalStatusnone
## ParentEducsome college:ParentMaritalStatusnone
## ParentEducsome high school:ParentMaritalStatusnone
## ParentEducbachelor's degree:ParentMaritalStatussingle
## ParentEduchigh school:ParentMaritalStatussingle
                                                           0.2274941
## ParentEducmaster's degree:ParentMaritalStatussingle
                                                          -4.2160673
## ParentEducsome college:ParentMaritalStatussingle
## ParentEducsome high school:ParentMaritalStatussingle
## ParentEducbachelor's degree:ParentMaritalStatuswidowed
                                                           6.0875539
## ParentEduchigh school:ParentMaritalStatuswidowed
## ParentEducmaster's degree:ParentMaritalStatuswidowed
## ParentEducsome college:ParentMaritalStatuswidowed
## ParentEducsome high school:ParentMaritalStatuswidowed
## ParentEducbachelor's degree:PracticeSportregularly
                                                           6.9475182
## ParentEduchigh school:PracticeSportregularly
## ParentEducmaster's degree:PracticeSportregularly
                                                          -0.9271534
## ParentEducsome college:PracticeSportregularly
                                                          -0.9034811
## ParentEducsome high school:PracticeSportregularly
## ParentEducbachelor's degree:PracticeSportsometimes
## ParentEduchigh school:PracticeSportsometimes
## ParentEducmaster's degree:PracticeSportsometimes
                                                           1.8605900
## ParentEducsome college:PracticeSportsometimes
## ParentEducsome high school:PracticeSportsometimes
## ParentEducbachelor's degree:IsFirstChildyes
## ParentEduchigh school:IsFirstChildyes
## ParentEducmaster's degree:IsFirstChildyes
## ParentEducsome college:IsFirstChildyes
## ParentEducsome high school:IsFirstChildyes
## LunchTypestandard:PracticeSportregularly
## LunchTypestandard:PracticeSportsometimes
                                                           2.4229902
## LunchTypestandard:TransportMeansschool bus
## TestPrepnone: WklyStudyHours> 10
## TestPrepnone: WklyStudyHours10-May
                                                           1.1072670
## ParentMaritalStatusmarried:PracticeSportregularly
## ParentMaritalStatusnone:PracticeSportregularly
## ParentMaritalStatussingle:PracticeSportregularly
## ParentMaritalStatuswidowed:PracticeSportregularly
## ParentMaritalStatusmarried:PracticeSportsometimes
## ParentMaritalStatusnone:PracticeSportsometimes
## ParentMaritalStatussingle:PracticeSportsometimes
## ParentMaritalStatuswidowed:PracticeSportsometimes
## ParentMaritalStatusmarried:IsFirstChildyes
## ParentMaritalStatusnone:IsFirstChildyes
## ParentMaritalStatussingle:IsFirstChildyes
                                                           0.2873802
```

```
## ParentMaritalStatuswidowed:IsFirstChildyes
## ParentMaritalStatusmarried:TransportMeansschool_bus
                                                            2.1148289
## ParentMaritalStatusnone:TransportMeansschool_bus
## ParentMaritalStatussingle:TransportMeansschool_bus
## ParentMaritalStatuswidowed:TransportMeansschool_bus
## PracticeSportregularly:WklyStudyHours> 10
## PracticeSportsometimes:WklyStudyHours> 10
## PracticeSportregularly:WklyStudyHours10-May
                                                            2.9426880
## PracticeSportsometimes:WklyStudyHours10-May
## IsFirstChildyes:NrSiblings
                                                            0.2857360
## IsFirstChildyes:TransportMeansschool_bus
## IsFirstChildyes:WklyStudyHours> 10
                                                            1.9358455
## IsFirstChildyes:WklyStudyHours10-May
model_math_best = lm(Y_math_train ~ Gender + EthnicGroup + ParentEduc + LunchType + TestPrep + ParentM
# reading LASSO
X_reading <- model.matrix(~ Gender + EthnicGroup + ParentEduc +</pre>
    LunchType + TestPrep + ParentMaritalStatus + PracticeSport +
    IsFirstChild + NrSiblings + TransportMeans + WklyStudyHours +
    Gender:IsFirstChild + LunchType:PracticeSport + LunchType:IsFirstChild +
    TestPrep:NrSiblings + TestPrep:TransportMeans + ParentMaritalStatus:PracticeSport + ParentMaritalSt
cv_model <- cv.glmnet(X_reading, Y_reading_train, alpha = 1)</pre>
best_lambda <- cv_model$lambda.min</pre>
lasso_model <- glmnet(X_reading, Y_reading_train, alpha = 1, lambda = best_lambda)</pre>
coef(lasso_model)
## 49 x 1 sparse Matrix of class "dgCMatrix"
##
                                                               s0
## (Intercept)
                                                      69.24438978
## (Intercept)
## Gendermale
                                                      -9.64456022
## EthnicGroupgroup B
## EthnicGroupgroup C
                                                       0.12187154
## EthnicGroupgroup D
                                                       2.73804550
## EthnicGroupgroup E
                                                       4.32714531
## ParentEducbachelor's degree
                                                       1.00843155
## ParentEduchigh school
                                                      -5.16634609
## ParentEducmaster's degree
                                                       3.61997993
## ParentEducsome college
                                                      -2.23041408
## ParentEducsome high school
                                                      -5.17395739
## LunchTypestandard
                                                       6.79219962
## TestPrepnone
                                                      -6.21291827
                                                       2.37055212
## ParentMaritalStatusmarried
## ParentMaritalStatusnone
                                                       0.41689791
## ParentMaritalStatussingle
## ParentMaritalStatuswidowed
                                                       1.74285608
## PracticeSportregularly
                                                      -2.52686071
## PracticeSportsometimes
## IsFirstChildyes
                                                       1.15235055
## NrSiblings
## TransportMeansschool_bus
                                                       0.08017577
```

```
## WklyStudyHours> 10
## WklyStudyHours10-May
## Gendermale:IsFirstChildyes
                                                      2.62766037
## LunchTypestandard:PracticeSportregularly
## LunchTypestandard:PracticeSportsometimes
                                                      3.07255306
## LunchTypestandard:IsFirstChildyes
                                                     -1.88926071
## TestPrepnone:NrSiblings
                                                     -0.91045866
## TestPrepnone:TransportMeansschool_bus
                                                      2.10087739
## ParentMaritalStatusmarried:PracticeSportregularly 3.63317210
## ParentMaritalStatusnone:PracticeSportregularly
                                                     -1.03469273
## ParentMaritalStatussingle:PracticeSportregularly -0.95977110
## ParentMaritalStatuswidowed:PracticeSportregularly -0.40510097
## ParentMaritalStatusmarried:PracticeSportsometimes
## ParentMaritalStatusnone:PracticeSportsometimes
## ParentMaritalStatussingle:PracticeSportsometimes -1.35869930
## ParentMaritalStatuswidowed:PracticeSportsometimes 3.33778366
## ParentMaritalStatusmarried:IsFirstChildyes
                                                  -0.41359962
## ParentMaritalStatusnone:IsFirstChildyes
## ParentMaritalStatussingle:IsFirstChildyes
                                                     3.11304653
## ParentMaritalStatuswidowed:IsFirstChildyes
                                                      1.11954328
## PracticeSportregularly:WklyStudyHours> 10
## PracticeSportsometimes:WklyStudyHours> 10
## PracticeSportregularly:WklyStudyHours10-May
                                                      2.99309704
## PracticeSportsometimes:WklyStudyHours10-May
                                                     -0.84120400
## NrSiblings:WklyStudyHours> 10
                                                      0.88322964
## NrSiblings:WklyStudyHours10-May
                                                      0.94407262
model_reading_best = lm(Y_reading_train ~ Gender + EthnicGroup + ParentEduc +
    LunchType + TestPrep + ParentMaritalStatus + PracticeSport +
    IsFirstChild + NrSiblings + TransportMeans + WklyStudyHours + LunchType:PracticeSport + ParentMarit
X_writing <- model.matrix(~ Gender + EthnicGroup + ParentEduc +</pre>
    LunchType + TestPrep + ParentMaritalStatus + PracticeSport +
    IsFirstChild + NrSiblings + TransportMeans + WklyStudyHours +
   ParentEduc:IsFirstChild + LunchType:PracticeSport + LunchType:IsFirstChild +
   TestPrep:NrSiblings + ParentMaritalStatus:PracticeSport +
   ParentMaritalStatus:IsFirstChild + PracticeSport:WklyStudyHours +
    IsFirstChild:WklyStudyHours, data = X_train)
# cv
cv_model <- cv.glmnet(X_writing, Y_writing_train, alpha = 1)</pre>
best_lambda <- cv_model$lambda.min</pre>
lasso_model <- glmnet(X_writing, Y_writing_train, alpha = 1, lambda = best_lambda)</pre>
coef(lasso_model)
## 52 x 1 sparse Matrix of class "dgCMatrix"
                                                              s0
##
## (Intercept)
                                                      69.5913009
## (Intercept)
## Gendermale
                                                      -9.1466566
## EthnicGroupgroup B
                                                      -0.8588264
## EthnicGroupgroup C
## EthnicGroupgroup D
                                                      3.9530918
## EthnicGroupgroup E
                                                      2.6507802
## ParentEducbachelor's degree
                                                      2.0339330
```

```
## ParentEduchigh school
                                                     -5.5986108
## ParentEducmaster's degree
                                                      5.7036126
## ParentEducsome college
                                                     -2.9655360
## ParentEducsome high school
                                                     -5.5165771
## LunchTypestandard
                                                      6.0671040
## TestPrepnone
                                                     -8.6298117
## ParentMaritalStatusmarried
                                                       2.4165951
## ParentMaritalStatusnone
## ParentMaritalStatussingle
                                                      0.5886266
## ParentMaritalStatuswidowed
## PracticeSportregularly
## PracticeSportsometimes
## IsFirstChildyes
## NrSiblings
                                                       0.3821740
## TransportMeansschool_bus
                                                       1.2730919
## WklyStudyHours> 10
## WklyStudyHours10-May
                                                       0.4208346
## ParentEducbachelor's degree:IsFirstChildyes
## ParentEduchigh school:IsFirstChildyes
## ParentEducmaster's degree: IsFirstChildyes
## ParentEducsome college:IsFirstChildyes
                                                       2.4844072
## ParentEducsome high school:IsFirstChildyes
## LunchTypestandard:PracticeSportregularly
## LunchTypestandard:PracticeSportsometimes
                                                       2.8821110
## LunchTypestandard:IsFirstChildyes
## TestPrepnone:NrSiblings
                                                     -0.3665883
## ParentMaritalStatusmarried:PracticeSportregularly
                                                      2.1468214
## ParentMaritalStatusnone:PracticeSportregularly
                                                      -2.1837752
## ParentMaritalStatussingle:PracticeSportregularly
                                                     -0.6445970
## ParentMaritalStatuswidowed:PracticeSportregularly
## ParentMaritalStatusmarried:PracticeSportsometimes
## ParentMaritalStatusnone:PracticeSportsometimes
## ParentMaritalStatussingle:PracticeSportsometimes
## ParentMaritalStatuswidowed:PracticeSportsometimes 1.9964773
## ParentMaritalStatusmarried:IsFirstChildyes
## ParentMaritalStatusnone:IsFirstChildyes
## ParentMaritalStatussingle:IsFirstChildyes
                                                      1.4918099
## ParentMaritalStatuswidowed:IsFirstChildyes
                                                      0.2210626
## PracticeSportregularly:WklyStudyHours> 10
## PracticeSportsometimes:WklyStudyHours> 10
## PracticeSportregularly:WklyStudyHours10-May
                                                      3.6295404
## PracticeSportsometimes:WklyStudyHours10-May
## IsFirstChildyes:WklyStudyHours> 10
                                                       1.2960564
## IsFirstChildyes:WklyStudyHours10-May
model_writing_best = lm(Y_writing_train ~ Gender + EthnicGroup + ParentEduc +
   LunchType + TestPrep + ParentMaritalStatus + PracticeSport +
    IsFirstChild + NrSiblings + TransportMeans + WklyStudyHours +
   ParentEduc:IsFirstChild + LunchType:PracticeSport +
    TestPrep:NrSiblings + ParentMaritalStatus:PracticeSport +
    ParentMaritalStatus:IsFirstChild + PracticeSport:WklyStudyHours +
    IsFirstChild:WklyStudyHours, data = X_train)
```

However, the initial process leaving a considerable number of variables, we applied the LASSO (Least Absolute Shrinkage and Selection Operator) method for penalization. Utilizing cross-validation (cv), we identified

the optimal lambda value. Subsequently, all interaction terms with shrinkage coefficients (s0) below 0.5 were eliminated. This refined approach resulted in the derivation of three models that were not only more efficient but also nested.

```
# results
# r.squared
glance_math = broom::glance(model_math_best) |>
    mutate(model = "Math") |>
    select(model, r.squared, adj.r.squared, p.value, AIC, BIC)

glance_reading = broom::glance(model_reading_best) |>
    mutate(model = "Reading") |>
    select(model, r.squared, adj.r.squared, p.value, AIC, BIC)

glance_writing = broom::glance(model_writing_best) |>
    mutate(model = "Writing") |>
    select(model, r.squared, adj.r.squared, p.value, AIC, BIC)

bind_rows(glance_math, glance_reading, glance_writing) |>
    knitr::kable()
```

model	r.squared	adj.r.squared	p.value	AIC	BIC
Math	0.3896522	0.3040798	0	5491.110	5874.986
Reading	0.2822946	0.2334634	0	5460.414	5663.643
Writing	0.3841167	0.3359085	0	5409.882	5640.208

```
png(file = "math.png", width = 800, height = 800)
par(mfrow = c(2, 2))
plot(model_math_best)
mtext("Math Model Diagnostic", outer = TRUE, cex = 1.5, line = -1)
dev.off()
## pdf
##
png(file = "reading.png", width = 800, height = 800)
par(mfrow = c(2, 2))
plot(model_reading_best)
mtext("Reading Model Diagnostic", outer = TRUE, cex = 1.5, line = -1)
dev.off()
## pdf
png(file = "writing.png", width = 800, height = 800)
par(mfrow = c(2, 2))
plot(model_writing_best)
mtext("Writing Model Diagnostic", outer = TRUE, cex = 1.5, line = -1)
dev.off()
## pdf
```

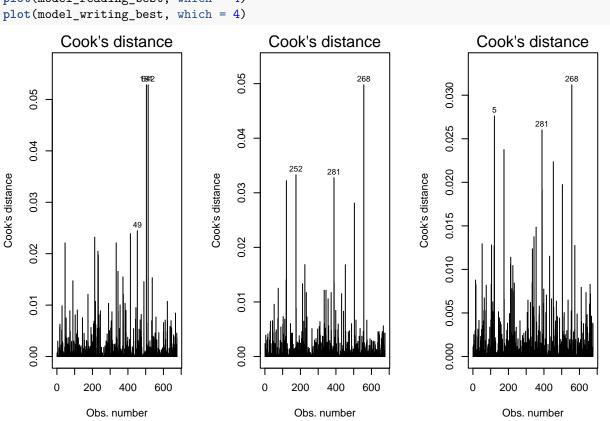
In the diagnostic analysis of our linear regression model, the Residuals versus Fitted values plot exhibited a stochastic distribution of residuals, devoid of any systematic patterns, thereby conforming to the assumptions of homoscedasticity and linearity. The Quantile-Quantile (QQ) plot demonstrated a close alignment of

##

residuals with the theoretical normal distribution, as evidenced by the linear arrangement of data points. Furthermore, the Scale-Location plot revealed a uniform dispersion of residuals around a central horizontal axis, indicative of consistent variance across the spectrum of fitted values. Finally, the examination of the Residuals versus Leverage plot revealed an absence of high-leverage observations, thus suggesting that the model is not unduly influenced by outlier data points.

Influential observations

```
par(mfrow=c(1,3))
plot(model_math_best, which = 4)
plot(model_reading_best, which = 4)
plot(model_writing_best, which = 4)
```



From the analysis of the plots, we identified a few points that appeared to be potential outliers or high-influence observations. However, upon examination, the Cook's distance values for these points were not significantly large. Additionally, when these points were excluded and the model was re-estimated, there was no substantial change in the model's performance. Upon further investigation of these specific data points, no anomalies were detected. Consequently, the final model was retained with these data points included.

multicolinearity

```
vif_values_math <- vif(model_math_best , type = 'predictor')</pre>
print(vif_values_math)
##
                                  GVIF Df GVIF<sup>(1/(2*Df))</sup>
## Gender
                         1.542005e+02
                                                  1.655040
                                                  1.353349
## EthnicGroup
                         4.185669e+07 29
## ParentEduc
                         2.600420e+04 65
                                                  1.081339
## LunchType
                         1.433646e+02 5
                                                  1.643025
```

```
## TestPrep
                       1.154486e+00 1
                                               1.074470
## ParentMaritalStatus 2.805551e+08 34
                                               1.331176
                                               1.357566
## PracticeSport
                     5.013426e+07 29
## TransportMeans
                       1.794224e+03 9
                                               1.516250
## WklyStudyHours
                       1.477385e+02 8
                                               1.366449
##
                                                         Interacts With
## Gender
                                                          PracticeSport
## EthnicGroup
                                                             ParentEduc
## ParentEduc
                       EthnicGroup, ParentMaritalStatus, PracticeSport
## LunchType
                                                          PracticeSport
## TestPrep
## ParentMaritalStatus
                                             ParentEduc, TransportMeans
## PracticeSport
                         Gender, ParentEduc, LunchType, WklyStudyHours
## TransportMeans
                                                    ParentMaritalStatus
## WklyStudyHours
                                                          PracticeSport
##
## Gender
                                     EthnicGroup, ParentEduc, LunchType, TestPrep, ParentMaritalStatus,
## EthnicGroup
                                       Gender, LunchType, TestPrep, ParentMaritalStatus, PracticeSport,
## ParentEduc
                                                                            Gender, LunchType, TestPrep,
## LunchType
                                        Gender, EthnicGroup, ParentEduc, TestPrep, ParentMaritalStatus,
## TestPrep
                       Gender, EthnicGroup, ParentEduc, LunchType, ParentMaritalStatus, PracticeSport,
## ParentMaritalStatus
                                                               Gender, EthnicGroup, LunchType, TestPrep,
## PracticeSport
                                                                             EthnicGroup, TestPrep, Paren
## TransportMeans
                                                   Gender, EthnicGroup, ParentEduc, LunchType, TestPrep,
## WklyStudyHours
                                             Gender, EthnicGroup, ParentEduc, LunchType, TestPrep, Paren
vif_values_writing <- vif(model_writing_best, type = 'predictor')</pre>
print(vif values writing)
##
                               GVIF Df GVIF<sup>(1/(2*Df))</sup>
## Gender
                       1.086453e+00 1
                                               1.042331
## EthnicGroup
                       1.384742e+00 4
                                               1.041528
## ParentEduc
                       2.474226e+01 11
                                               1.157013
## LunchType
                       1.582338e+02 5
                                               1.659319
## TestPrep
                       1.270161e+00 3
                                               1.040662
## ParentMaritalStatus 6.007068e+02 19
                                               1.183376
## PracticeSport
                       4.482670e+03 23
                                               1.200553
## IsFirstChild
                       6.978027e+05 23
                                               1.339793
## NrSiblings
                       1.270161e+00 3
                                               1.040662
## TransportMeans
                       1.069186e+00 1
                                               1.034014
## WklyStudyHours
                       2.010883e+03 11
                                               1.413038
                                                         Interacts With
## Gender
## EthnicGroup
## ParentEduc
                                                           IsFirstChild
## LunchType
                                                          PracticeSport
## TestPrep
                                                             NrSiblings
## ParentMaritalStatus
                                            PracticeSport, IsFirstChild
## PracticeSport
                        LunchType, ParentMaritalStatus, WklyStudyHours
## IsFirstChild
                       ParentEduc, ParentMaritalStatus, WklyStudyHours
## NrSiblings
                                                               TestPrep
## TransportMeans
## WklyStudyHours
                                            PracticeSport, IsFirstChild
##
## Gender
                       EthnicGroup, ParentEduc, LunchType, TestPrep, ParentMaritalStatus, PracticeSport
```

```
## ParentEduc
                                          Gender, EthnicGroup, LunchType, TestPrep, ParentMaritalStatus,
                                          Gender, EthnicGroup, ParentEduc, TestPrep, ParentMaritalStatus
## LunchType
                                      Gender, EthnicGroup, ParentEduc, LunchType, ParentMaritalStatus, P.
## TestPrep
## ParentMaritalStatus
                                                                   Gender, EthnicGroup, ParentEduc, Lunch
## PracticeSport
                                                                                Gender, EthnicGroup, Pare
## IsFirstChild
                                                                                Gender, EthnicGroup, Lunc
                                      Gender, EthnicGroup, ParentEduc, LunchType, ParentMaritalStatus, P.
## NrSiblings
## TransportMeans
                               Gender, EthnicGroup, ParentEduc, LunchType, TestPrep, ParentMaritalStatu
## WklyStudyHours
                                                             Gender, EthnicGroup, ParentEduc, LunchType,
vif_values_reading <- vif(model_reading_best, type = 'predictor')</pre>
print(vif_values_reading)
##
                              GVIF Df GVIF<sup>(1/(2*Df))</sup>
## Gender
                          1.073508 1
                                              1.036102
## EthnicGroup
                          1.364765
                                              1.039638
## ParentEduc
                          1.374557
                                    5
                                              1.032325
## LunchType
                        147.832518
                                    5
                                              1.648075
## TestPrep
                          1.091363 1
                                              1.044683
## ParentMaritalStatus
                         68.897268 19
                                              1.117825
                       4319.902647 23
## PracticeSport
                                              1.199588
## IsFirstChild
                       5843.077251 9
                                              1.619041
## NrSiblings
                        115.835734 5
                                              1.608364
## TransportMeans
                          1.069289 1
                                              1.034064
## WklyStudyHours
                        148.368681 11
                                              1.255155
##
                                                        Interacts With
## Gender
## EthnicGroup
## ParentEduc
## LunchType
                                                         PracticeSport
## TestPrep
## ParentMaritalStatus
                                           PracticeSport, IsFirstChild
## PracticeSport
                       LunchType, ParentMaritalStatus, WklyStudyHours
## IsFirstChild
                                                   ParentMaritalStatus
                                                        WklyStudyHours
## NrSiblings
## TransportMeans
## WklyStudyHours
                                             PracticeSport, NrSiblings
##
## Gender
                       EthnicGroup, ParentEduc, LunchType, TestPrep, ParentMaritalStatus, PracticeSport
                            Gender, ParentEduc, LunchType, TestPrep, ParentMaritalStatus, PracticeSport
## EthnicGroup
                           Gender, EthnicGroup, LunchType, TestPrep, ParentMaritalStatus, PracticeSport
## ParentEduc
                                          Gender, EthnicGroup, ParentEduc, TestPrep, ParentMaritalStatus
## LunchType
## TestPrep
                         Gender, EthnicGroup, ParentEduc, LunchType, ParentMaritalStatus, PracticeSport
                                                                   Gender, EthnicGroup, ParentEduc, Lunch
## ParentMaritalStatus
## PracticeSport
                                                                                Gender, EthnicGroup, Pare
## IsFirstChild
                                                   Gender, EthnicGroup, ParentEduc, LunchType, TestPrep,
                                            Gender, EthnicGroup, ParentEduc, LunchType, TestPrep, Parent
## NrSiblings
                               Gender, EthnicGroup, ParentEduc, LunchType, TestPrep, ParentMaritalStatu
## TransportMeans
## WklyStudyHours
                                                           Gender, EthnicGroup, ParentEduc, LunchType, T
```

Gender, ParentEduc, LunchType, TestPrep, ParentMaritalStatus, PracticeSport

EthnicGroup

model validation

cross validation

No pre-processing

```
library(caret)
## Loading required package: lattice
## Registered S3 method overwritten by 'lava':
     method
                from
##
     print.pcor greybox
##
## Attaching package: 'caret'
## The following object is masked from 'package:greybox':
##
       MAE
## The following object is masked from 'package:purrr':
##
       lift
control <- trainControl(method = "cv", number = 10)</pre>
set.seed(123)
math_model_data <- cbind(X_train, Y_math_train)</pre>
math_model_cv <- train( Y_math_train ~ Gender + EthnicGroup + ParentEduc + LunchType + TestPrep + Paren
    data = math_model_data, method = "lm", trControl = control)
set.seed(124)
reading_model_data <- cbind(X_train, Y_reading_train)</pre>
reading model cv <- train(Y reading train ~ Gender + EthnicGroup + ParentEduc +
    LunchType + TestPrep + ParentMaritalStatus + PracticeSport +
    IsFirstChild + NrSiblings + TransportMeans + WklyStudyHours + LunchType:PracticeSport + ParentMarit
    method = "lm", trControl = control)
set.seed(125)
writing_model_data <- cbind(X_train, Y_writing_train)</pre>
writing_model_cv <- train(Y_writing_train ~ Gender + EthnicGroup + ParentEduc +
    LunchType + TestPrep + ParentMaritalStatus + PracticeSport +
    IsFirstChild + NrSiblings + TransportMeans + WklyStudyHours +
    ParentEduc:IsFirstChild + LunchType:PracticeSport +
    TestPrep:NrSiblings + ParentMaritalStatus:PracticeSport +
    ParentMaritalStatus:IsFirstChild + PracticeSport:WklyStudyHours +
    IsFirstChild:WklyStudyHours, data = writing_model_data,
    method = "lm", trControl = control)
print(math_model_cv)
## Linear Regression
##
## 676 samples
     9 predictor
##
```

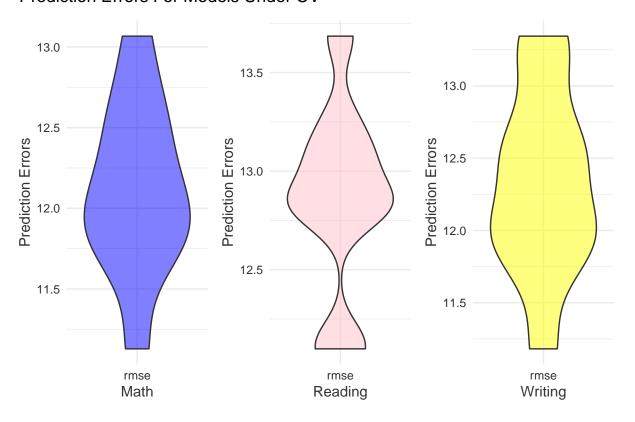
```
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 609, 608, 608, 608, 608, 610, ...
## Resampling results:
##
##
     RMSE
               Rsquared
                          MAE
##
     14.34509 0.2210548 11.58918
## Tuning parameter 'intercept' was held constant at a value of TRUE
print(reading_model_cv)
## Linear Regression
##
## 676 samples
   11 predictor
##
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 609, 609, 606, 609, 609, 607, ...
## Resampling results:
##
##
     RMSE
              Rsquared
                         MAE
##
     13.7283 0.2021777 11.19904
##
## Tuning parameter 'intercept' was held constant at a value of TRUE
print(writing_model_cv)
## Linear Regression
##
## 676 samples
  11 predictor
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 608, 608, 609, 608, 608, 610, ...
## Resampling results:
##
##
     RMSE
               Rsquared MAE
     13.15398 0.299929 10.62044
##
##
## Tuning parameter 'intercept' was held constant at a value of TRUE
library(readr)
library(caret)
library(purrr)
library(tidyverse)
library(plotly)
##
## Attaching package: 'plotly'
## The following object is masked from 'package:ggplot2':
##
##
       last_plot
## The following object is masked from 'package:stats':
```

```
##
##
       filter
## The following object is masked from 'package:graphics':
##
##
       layout
library(modelr)
library(randomForest)
## randomForest 4.7-1.1
## Type rfNews() to see new features/changes/bug fixes.
##
## Attaching package: 'randomForest'
## The following object is masked from 'package:gridExtra':
##
##
       combine
## The following object is masked from 'package:ggplot2':
##
##
       margin
## The following object is masked from 'package:dplyr':
##
##
       combine
library(boot)
## Attaching package: 'boot'
## The following object is masked from 'package:lattice':
##
##
       melanoma
## The following object is masked from 'package:car':
##
##
       logit
library(patchwork)
set.seed(123)
# generate a cv dataframe
cv_df_math =
  crossv_mc(math_model_data, 10) %>%
  mutate(
    train = map(train, as_tibble),
    test = map(test, as_tibble))
# fit the model to the generated CV dataframe
cv_df_math =
  cv_df_math |>
  mutate(
    model = map(train, ~lm( Y_math_train ~ Gender + EthnicGroup + ParentEduc + LunchType + TestPrep + 1
    data = math_model_data)),
    rmse = map2_dbl(model, test, ~rmse(model = .x, data = .y)))
```

```
# plot the prediction error
plot_math <- cv_df_math |>
  select(rmse) |>
  pivot_longer(
   everything(),
   names_to = "model",
   values_to = "rmse") %>%
  ggplot(aes(x = model, y = rmse)) +
  geom_violin(fill = "blue", alpha = 0.5) +
  labs(
   x = "Math",
   y = "Prediction Errors"
  ) +
  theme_minimal() +
  theme(
   plot.title = element_text(hjust = 0.5),
   axis.text = element_text(color = "grey20"),
   axis.title = element_text(color = "grey20")
  )
set.seed(123)
# generate a cv dataframe
cv_df_reading =
  crossv_mc(reading_model_data, 10) %>%
 mutate(
   train = map(train, as tibble),
   test = map(test, as_tibble))
# fit the model to the generated CV dataframe
cv_df_reading =
  cv_df_reading |>
  mutate(
   model = map(train, ~lm(Y_reading_train ~ Gender + EthnicGroup + ParentEduc +
   LunchType + TestPrep + ParentMaritalStatus + PracticeSport +
   IsFirstChild + NrSiblings + TransportMeans + WklyStudyHours + LunchType:PracticeSport + ParentMarit
   rmse = map2_dbl(model, test, ~rmse(model = .x, data = .y)))
# plot the prediction error
plot_reading <- cv_df_reading |>
  select(rmse) |>
 pivot_longer(
   everything(),
   names_to = "model",
   values_to = "rmse") %>%
  ggplot(aes(x = model, y = rmse)) +
  geom_violin(fill = "pink", alpha = 0.5) +
   x = "Reading",
   y = "Prediction Errors"
  theme_minimal() +
  theme(
```

```
plot.title = element_text(hjust = 0.5),
   axis.text = element_text(color = "grey20"),
   axis.title = element_text(color = "grey20")
  )
set.seed(123)
# generate a cv dataframe
cv df writing =
  crossv_mc(writing_model_data, 10) %>%
 mutate(
   train = map(train, as_tibble),
   test = map(test, as_tibble))
# fit the model to the generated CV dataframe
cv_df_writing =
  cv_df_writing |>
  mutate(
   model = map(train, ~lm(Y_writing_train ~ Gender + EthnicGroup + ParentEduc +
   LunchType + TestPrep + ParentMaritalStatus + PracticeSport +
   IsFirstChild + NrSiblings + TransportMeans + WklyStudyHours +
   ParentEduc:IsFirstChild + LunchType:PracticeSport +
   TestPrep:NrSiblings + ParentMaritalStatus:PracticeSport +
   ParentMaritalStatus:IsFirstChild + PracticeSport:WklyStudyHours +
   IsFirstChild:WklyStudyHours, data = writing_model_data)),
   rmse = map2_dbl(model, test, ~rmse(model = .x, data = .y)))
# plot the prediction error
plot_writing <-cv_df_writing |>
  select(rmse) |>
 pivot_longer(
   everything(),
   names_to = "model",
   values_to = "rmse") %>%
  ggplot(aes(x = model, y = rmse)) +
  geom_violin(fill = "yellow", alpha = 0.5) +
  labs(
   x = "Writing",
   v = "Prediction Errors"
  theme minimal() +
  theme(
   plot.title = element_text(hjust = 0.5),
   axis.text = element text(color = "grey20"),
   axis.title = element_text(color = "grey20")
  )
plot_math + plot_reading +
 plot_writing+plot_annotation(title="Prediction Errors For Models Under CV")
```

Prediction Errors For Models Under CV



prediction

```
# Splitting the train dataset into independent variables (X) and dependent variables (Y)
X test<- testData %% select(-c(MathScore, ReadingScore, WritingScore))
Y_math_test <- testData$MathScore</pre>
Y_reading_test <-testData$ReadingScore
Y_writing_test <- testData$WritingScore</pre>
math_predictions <- predict(model_math_best, newdata = X_test)</pre>
reading_predictions <- predict(model_reading_best, newdata = X_test)</pre>
writing predictions <- predict(model writing best, newdata = X test)</pre>
math_mspe <- mean((Y_math_test - math_predictions)^2)</pre>
reading_mspe <- mean((Y_reading_test - reading_predictions)^2)</pre>
writing_mspe <- mean((Y_writing_test - writing_predictions)^2)</pre>
mspe_values <- data.frame(</pre>
  Subject = c("Math", "Reading", "Writing"),
  MSPE = c(math_mspe, reading_mspe, writing_mspe)
library(knitr)
kable(mspe_values, col.names = c("Subject", "MSPE"), caption = "MSPE Values for Different Subjects")
```

Table 6: MSPE Values for Different Subjects

Subject	MSPE
Math	198.3466
Reading	152.9267
Writing	142.8281

Take a look of coefficents. Try to understand model in more practical way.

```
# coef
broom::tidy(model_math_best) |>
  knitr::kable(caption = "Math")
```

Table 7: Math

term	estimate	std.error	statistic	p.value
(Intercept)	59.8236540	7.824529	7.6456552	0.0000000
Gendermale	4.9989664	3.390164	1.4745500	0.1408652
EthnicGroupgroup B	2.1158513	5.390584	0.3925087	0.6948236
EthnicGroupgroup C	-0.3917127	5.103840	-0.0767486	0.9388495
EthnicGroupgroup D	-0.2697026	5.456409	-0.0494286	0.9605944
EthnicGroupgroup E	4.8561321	5.555826	0.8740613	0.3824393
ParentEducbachelor's degree	13.2158169	10.456616	1.2638713	0.2067737
ParentEduchigh school	-1.3788436	8.702785	-0.1584370	0.8741665
ParentEducmaster's degree	-11.1824725	13.312940	-0.8399702	0.4012642
ParentEducsome college	1.2690513	7.903915	0.1605598	0.8724949
ParentEducsome high school	2.8839705	8.905244	0.3238508	0.7461654
LunchTypestandard	2.5820328	3.430405	0.7526903	0.4519352
TestPrepnone	-5.4668672	1.164944	-4.6928142	0.0000034
ParentMaritalStatusmarried	4.4767797	3.717787	1.2041517	0.2290122
ParentMaritalStatusnone	5.1486153	6.329960	0.8133725	0.4163316
ParentMaritalStatussingle	7.1051335	4.343620	1.6357630	0.1024207
ParentMaritalStatuswidowed	32.1825946	13.767636	2.3375542	0.0197426
PracticeSportregularly	-7.0323692	6.092899	-1.1541910	0.2488876
PracticeSportsometimes	-6.2033803	5.900179	-1.0513884	0.2935092
TransportMeansschool_bus	-2.9955588	2.957436	-1.0128904	0.3115263
WklyStudyHours> 10	2.1744283	5.306108	0.4097972	0.6821029
WklyStudyHours10-May	-3.0158131	3.856450	-0.7820179	0.4345167
Gendermale:PracticeSportregularly	2.4088354	3.826334	0.6295413	0.5292376
Gendermale:PracticeSportsometimes	-3.1094030	3.682194	-0.8444429	0.3987631
EthnicGroupgroup B:ParentEducbachelor's degree	12.3301744	10.103598	1.2203746	0.2228088
EthnicGroupgroup C:ParentEducbachelor's degree	15.6483238	9.442126	1.6572881	0.0979910
EthnicGroupgroup D:ParentEducbachelor's degree	11.1026820	9.857639	1.1263023	0.2604939
EthnicGroupgroup E:ParentEducbachelor's degree	17.5929375	10.628403	1.6552757	0.0983986
EthnicGroupgroup B:ParentEduchigh school	-6.6339532	7.086337	-0.9361611	0.3495720
EthnicGroupgroup C:ParentEduchigh school	1.0022039	6.695100	0.1496922	0.8810585
EthnicGroupgroup D:ParentEduchigh school	1.0241333	7.063144	0.1449968	0.8847628
EthnicGroupgroup E:ParentEduchigh school	4.1683624	7.576404	0.5501769	0.5824056
EthnicGroupgroup B:ParentEducmaster's degree	23.2799497	13.355971	1.7430369	0.0818464
EthnicGroupgroup C:ParentEducmaster's degree	15.3169367	12.185689	1.2569611	0.2092634
EthnicGroupgroup D:ParentEducmaster's degree	26.8573940	11.968517	2.2440036	0.0252009
EthnicGroupgroup E:ParentEducmaster's degree	21.6878571	13.395444	1.6190473	0.1059697
EthnicGroupgroup B:ParentEducsome college	0.9014048	6.923716	0.1301909	0.8964596

term	estimate	$\operatorname{std.error}$	statistic	p.value
EthnicGroupgroup C:ParentEducsome college	3.7712301	6.460460	0.5837402	0.5596175
EthnicGroupgroup D:ParentEducsome college	11.1836587	6.773641	1.6510556	0.0992576
EthnicGroupgroup E:ParentEducsome college	2.5687923	7.049554	0.3643907	0.7156964
EthnicGroupgroup B:ParentEducsome high school	-5.2322199	7.387119	-0.7082897	0.4790442
EthnicGroupgroup C:ParentEducsome high school	-0.6264665	7.267877	-0.0861966	0.9313392
EthnicGroupgroup D:ParentEducsome high school	1.5059296	7.255510	0.2075567	0.8356465
EthnicGroupgroup E:ParentEducsome high school	9.7108636	8.278557	1.1730140	0.2412619
ParentEducbachelor's	-21.6431778	7.246291	-2.9867939	0.0029358
degree:ParentMaritalStatusmarried	21.0101110	1.210201	2.0001000	0.002000
ParentEduchigh school:ParentMaritalStatusmarried	0.2578684	4.637813	0.0556013	0.9556782
ParentEducmaster's	-5.6890480	8.429506	-0.6748969	0.5000047
degree:ParentMaritalStatusmarried	0.0000100	0.120000	0.0110000	0.0000011
ParentEducsome college:ParentMaritalStatusmarried	-7.4587586	4.427521	-1.6846354	0.0925860
ParentEducsome high	-6.8910904	5.205234	-1.3238771	0.0923500 0.1860548
school:ParentMaritalStatusmarried	-0.0910904	0.200204	-1.5256771	0.1000340
ParentEducbachelor's	22 7628624	13.278842	-1.7895282	0.0740408
degree:ParentMaritalStatusnone	-23.7628624	13.270042	-1.7090202	0.0740406
e e e e e e e e e e e e e e e e e e e	0.7602507	0 419105	1 0419645	0.9001770
ParentEduchigh school:ParentMaritalStatusnone	-8.7603507	8.413185	-1.0412645	0.2981778
ParentEducmaster's degree:ParentMaritalStatusnone	0.2601949	14.410477	0.0180560	0.9856003
ParentEducsome college:ParentMaritalStatusnone	-5.3820540	7.548785	-0.7129696	0.4761455
ParentEducsome high	-8.1299851	11.423571	-0.7116851	0.4769402
school:ParentMaritalStatusnone			0 5045045	0.00040=4
ParentEducbachelor's	-27.9975589	7.995804	-3.5015315	0.0004974
degree:ParentMaritalStatussingle				
ParentEduchigh school:ParentMaritalStatussingle	1.1510539	5.420215	0.2123632	0.8318968
ParentEducmaster's degree:ParentMaritalStatussingle	-10.4975236	9.553394	-1.0988266	0.2722904
ParentEducsome college:ParentMaritalStatussingle	-13.8823053	5.170519	-2.6848962	0.0074585
ParentEducsome high	-8.4415130	5.906359	-1.4292244	0.1534672
school:ParentMaritalStatussingle				
ParentEducbachelor's	-14.5660804	14.065360	-1.0355995	0.3008118
degree:ParentMaritalStatuswidowed				
ParentEduchigh school:ParentMaritalStatuswidowed	-22.3538476	12.996728	-1.7199596	0.0859624
ParentEducmaster's	-32.9776873	21.234213	-1.5530450	0.1209468
degree:ParentMaritalStatuswidowed				
ParentEducsome college:ParentMaritalStatuswidowed	-5.9891743	12.354242	-0.4847869	0.6280069
ParentEducsome high	-31.1843496	13.996685	-2.2279811	0.0262567
school:ParentMaritalStatuswidowed				
ParentEducbachelor's degree:PracticeSportregularly	2.4921887	7.600560	0.3278954	0.7431067
ParentEduchigh school:PracticeSportregularly	-4.7479893	5.952541	-0.7976408	0.4253988
ParentEducmaster's degree:PracticeSportregularly	-11.5834986	9.179462	-1.2618930	0.2074842
ParentEducsome college:PracticeSportregularly	-2.8096597	5.125701	-0.5481513	0.5837947
ParentEducsome high school:PracticeSportregularly	-3.9740663	5.911862	-0.6722190	0.5017065
ParentEducbachelor's degree:PracticeSportsometimes	-9.8379934	7.378795	-1.3332791	0.1829531
ParentEduchigh school:PracticeSportsometimes	-3.2966005	5.802557	-0.5681289	0.5701629
ParentEducmaster's degree:PracticeSportsometimes	3.4760708	7.539298	0.4610603	0.6449247
ParentEducsome college:PracticeSportsometimes	0.5729083	4.983034	0.1149718	0.9085065
ParentEducsome high school:PracticeSportsometimes	-1.7933565	5.768358	-0.3108955	0.7559895
LunchTypestandard:PracticeSportregularly	7.8623509	3.902305	2.0147967	0.0443776
LunchTypestandard:PracticeSportsometimes	10.9083551	3.774567	2.8899616	0.0039940
ParentMaritalStatusmarried:TransportMeansschool_bus		3.307985	1.8133093	0.0702904
ParentMaritalStatusnone:TransportMeansschool_bus	4.1673088	6.034708	0.6905568	0.4901148
ParentMaritalStatussingle:TransportMeansschool_bus	1.9494148	3.747047	0.5202536	0.4901148 0.6030813
1 archivitativanovavassingie. 11ansportivicanssenooi_bus	1.9494140	0.141041	0.020200	0.0000010

term	estimate	std.error	statistic	p.value
ParentMaritalStatuswidowed:TransportMeansschool_	_bus-13.8706862	9.598489	-1.4450906	0.1489615
PracticeSportregularly:WklyStudyHours> 10	1.7873962	6.016529	0.2970810	0.7665089
PracticeSportsometimes:WklyStudyHours> 10	2.8131491	5.807567	0.4843938	0.6282856
PracticeSportregularly:WklyStudyHours10-May	9.5741323	4.391825	2.1799895	0.0296514
${\bf Practice Sportsometimes: Wkly Study Hours 10-May}$	4.8408421	4.247024	1.1398198	0.2548223

```
broom::tidy(model_reading_best) |>
knitr::kable(caption = "Reading")
```

Table 8: Reading

term	estimate	std.error	statistic	p.value
(Intercept)	66.7294950	6.5129906	10.2455998	0.0000000
Gendermale	-8.3451224	1.0593384	-7.8776741	0.0000000
EthnicGroupgroup B	0.9255796	2.2073855	0.4193103	0.6751318
EthnicGroupgroup C	1.7676168	2.0668039	0.8552417	0.3927415
EthnicGroupgroup D	4.3694159	2.1234404	2.0577059	0.0400280
EthnicGroupgroup E	5.5691293	2.3447971	2.3751008	0.0178416
ParentEducbachelor's degree	0.9593230	1.9583347	0.4898667	0.6243982
ParentEduchigh school	-5.9700940	1.6444629	-3.6304217	0.0003059
ParentEducmaster's degree	3.0739419	2.4233342	1.2684763	0.2050949
ParentEducsome college	-3.4228951	1.5292774	-2.2382434	0.0255526
ParentEducsome high school	-6.2272681	1.7534277	-3.5514826	0.0004116
LunchTypestandard	1.5465446	3.2543084	0.4752299	0.6347873
TestPrepnone	-6.7112750	1.1369352	-5.9029530	0.0000000
ParentMaritalStatusmarried	12.9982171	5.3710658	2.4200443	0.0157996
ParentMaritalStatusnone	25.0534251	9.6932917	2.5846148	0.0099718
ParentMaritalStatussingle	17.1900325	6.2980878	2.7294050	0.0065215
ParentMaritalStatuswidowed	20.3651926	9.6806792	2.1036946	0.0357997
PracticeSportregularly	-8.4725203	6.2381933	-1.3581689	0.1748947
PracticeSportsometimes	-2.8648163	5.9105655	-0.4846941	0.6280613
IsFirstChildyes	10.0828700	3.4087261	2.9579584	0.0032125
NrSiblings	-1.4325336	0.7269284	-1.9706669	0.0491980
$TransportMeansschool_bus$	2.0276616	1.0777747	1.8813410	0.0603850
WklyStudyHours> 10	-4.0765631	5.5292118	-0.7372774	0.4612273
WklyStudyHours10-May	-8.7804016	4.1184180	-2.1319841	0.0333931
LunchTypestandard:PracticeSportregularly	4.2752122	3.7133490	1.1513090	0.2500405
Lunch Type standard: Practice Sportsometimes	7.4223767	3.5916114	2.0665868	0.0391799
ParentMaritalStatusmarried:PracticeSportregularly	2.1171894	5.1522455	0.4109256	0.6812664
ParentMaritalStatusnone:PracticeSportregularly	-13.2554099	8.4242250	-1.5734872	0.1161065
${\bf Parent Marital Status single: Practice Sport regularly}$	-10.5446824	6.2293309	-1.6927472	0.0909964
${\bf Parent Marital Status widowed:} {\bf Practice Sport regularly}$	-15.7467113	10.7332090	-1.4671019	0.1428458
Parent Marital Status married: Practice Sportsometimes	-3.4069333	4.8619672	-0.7007314	0.4837285
Parent Marital Status none: Practice Sportsometimes	-14.4055236	7.9601015	-1.8097161	0.0708147
Parent Marital Status single: Practice Sportsometimes	-12.9439931	5.9797313	-2.1646446	0.0307886
Parent Marital Status widowed: Practice Sportsometimes	-10.3871025	10.9192492	-0.9512653	0.3418334
ParentMaritalStatusmarried:IsFirstChildyes	-10.4573902	3.7160407	-2.8141215	0.0050433
ParentMaritalStatusnone:IsFirstChildyes	-15.2781783	7.2881211	-2.0963124	0.0364515
ParentMaritalStatussingle:IsFirstChildyes	-5.0872414	4.1352014	-1.2302282	0.2190694
${\bf Parent Marital Status widowed: Is First Childyes}$	-4.5530850	7.9795899	-0.5705914	0.5684795
PracticeSportregularly:WklyStudyHours> 10	3.5682387	5.7478515	0.6207952	0.5349582

term	estimate	std.error	statistic	p.value
PracticeSportsometimes:WklyStudyHours> 10	2.8699791	5.5660851	0.5156190	0.6063009
PracticeSportregularly:WklyStudyHours10-May	11.5013304	4.3089635	2.6691640	0.0077993
PracticeSportsometimes:WklyStudyHours10-May	5.4826677	4.1395741	1.3244521	0.1858317
NrSiblings:WklyStudyHours> 10	1.5599932	1.1177197	1.3956927	0.1632972
NrSiblings:WklyStudyHours10-May	2.0696810	0.8583462	2.4112427	0.0161825

```
broom::tidy(model_writing_best) |>
knitr::kable(caption = "Writing")
```

Table 9: Writing

term	estimate	$\operatorname{std.error}$	statistic	p.value
(Intercept)	63.3709846	6.6409190	9.5425023	0.0000000
Gendermale	-9.8669217	1.0224029	-9.6507172	0.0000000
EthnicGroupgroup B	-0.2067857	2.1153119	-0.0977566	0.9221569
EthnicGroupgroup C	1.3435451	1.9866591	0.6762836	0.4991104
EthnicGroupgroup D	5.7975931	2.0367028	2.8465582	0.0045643
EthnicGroupgroup E	4.4379024	2.2613889	1.9624676	0.0501506
ParentEducbachelor's degree	3.8014422	3.3859652	1.1227056	0.2619929
ParentEduchigh school	-11.4098557	2.7739139	-4.1132696	0.0000442
ParentEducmaster's degree	4.5006017	4.0524117	1.1105983	0.2671677
ParentEducsome college	-8.8143126	2.4578101	-3.5862464	0.0003616
ParentEducsome high school	-8.9386870	2.8010267	-3.1912180	0.0014876
LunchTypestandard	1.8520503	3.1483239	0.5882655	0.5565663
TestPrepnone	-7.3456304	1.8869030	-3.8929561	0.0001097
ParentMaritalStatusmarried	11.6927213	5.1736308	2.2600610	0.0241603
ParentMaritalStatusnone	17.0801063	9.3437675	1.8279678	0.0680302
ParentMaritalStatussingle	13.9820111	6.0620775	2.3064719	0.0214100
ParentMaritalStatuswidowed	18.4272852	9.2741784	1.9869453	0.0473639
PracticeSportregularly	-8.3652226	6.0499866	-1.3826845	0.1672547
PracticeSportsometimes	-3.4537144	5.7240259	-0.6033715	0.5464801
IsFirstChildyes	8.7899099	4.2419170	2.0721551	0.0386598
NrSiblings	1.0067232	0.5727539	1.7576891	0.0792891
TransportMeansschool_bus	2.1796409	1.0339310	2.1081106	0.0354183
WklyStudyHours> 10	-0.7970647	5.5864483	-0.1426783	0.8865902
WklyStudyHours10-May	-0.3997597	4.1749272	-0.0957525	0.9237478
ParentEducbachelor's degree:IsFirstChildyes	-2.4899524	4.0774623	-0.6106623	0.5416448
ParentEduchigh school:IsFirstChildyes	6.1861884	3.3680045	1.8367518	0.0667205
ParentEducmaster's degree:IsFirstChildyes	1.5275660	4.8873450	0.3125554	0.7547226
ParentEducsome college:IsFirstChildyes	8.6738003	3.0536356	2.8404831	0.0046510
ParentEducsome high school:IsFirstChildyes	2.9574964	3.4677705	0.8528524	0.3940673
LunchTypestandard:PracticeSportregularly	5.4421952	3.6009281	1.5113313	0.1312087
LunchTypestandard:PracticeSportsometimes	7.8378604	3.4747701	2.2556486	0.0244371
TestPrepnone:NrSiblings	-1.0363150	0.7099890	-1.4596212	0.1448958
ParentMaritalStatusmarried:PracticeSportregularly	4.3272509	4.9576748	0.8728388	0.3830856
ParentMaritalStatusnone:PracticeSportregularly	-11.6096660	8.1309654	-1.4278336	0.1538384
ParentMaritalStatussingle:PracticeSportregularly	-6.1061216	6.0318785	-1.0123085	0.3117817
ParentMaritalStatuswidowed:PracticeSportregularly	-16.4866756	10.3318618	-1.5957120	0.1110578
Parent Marital Status married: Practice Sportsometimes	-1.6078719	4.6764775	-0.3438212	0.7310962
Parent Marital Status none: Practice Sportsometimes	-10.5375101	7.6623981	-1.3752235	0.1695541
Parent Marital Status single: Practice Sportsometimes	-9.1583320	5.7693200	-1.5874197	0.1129226

term	estimate	std.error	statistic	p.value
ParentMaritalStatuswidowed:PracticeSportsometimes	-11.4398918	10.5454267	-1.0848202	0.2784189
ParentMaritalStatusmarried:IsFirstChildyes	-9.6971320	3.5961881	-2.6965030	0.0071957
ParentMaritalStatusnone:IsFirstChildyes	-8.6878943	7.0146922	-1.2385282	0.2159845
ParentMaritalStatussingle:IsFirstChildyes	-5.1212907	4.0082739	-1.2776798	0.2018359
ParentMaritalStatuswidowed:IsFirstChildyes	-1.6510229	7.6782636	-0.2150256	0.8298174
PracticeSportregularly:WklyStudyHours> 10	3.1918173	5.5479415	0.5753156	0.5652846
PracticeSportsometimes:WklyStudyHours> 10	3.9406467	5.4195912	0.7271114	0.4674295
PracticeSportregularly:WklyStudyHours10-May	11.0302513	4.1694733	2.6454783	0.0083624
PracticeSportsometimes:WklyStudyHours10-May	5.5098814	3.9942868	1.3794406	0.1682515
IsFirstChildyes:WklyStudyHours> 10	-0.8801575	3.3630648	-0.2617129	0.7936289
IsFirstChildyes:WklyStudyHours10-May	-5.4687471	2.5802518	-2.1194626	0.0344444