Correction Exercice 3 du TD n° 4

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mémoire initiale: m_4 = \langle \text{fct}, 12, \text{ meth, entier} \rangle. \langle \text{t}, 2, \text{ meth, entier} \rangle. \langle \text{t}, 2, \text{ t}, \text{ t}, \text{ entier} \rangle. \langle \text{t}, 2, \text{ t}, \text{ t}, \text{ entier} \rangle. \langle \text{t}, 2, \text{ t}, \text{ t}, \text{ entier} \rangle. \langle \text{t}, 2, \text{ t}, \text{ t}, \text{ entier} \rangle. \langle \text{t}, 2, \text{ t}, \text{ t}, \text{ t}, \text{ entier} \rangle. \langle \text{t}, 2, \text{ t}, \text{ t},
[affectationT]_{52}: m_4 \vdash affectation(tab(ident(t), 54), 56) \rightarrow m_{12} = AffecterValT(t, ind_0, v_0, m_4)
         avec m_{12} = \text{AffecterValT}(t, 3, 6, m_4) avec m_{12} = m_4 + @tas : [6, 6, 6, 6]
         [appelE]<sub>56</sub>: m_4 \stackrel{eval}{\vdash} \text{appelE}(57, 58) \Rightarrow v_0 = 6
                   [appelI]_{56}: m_4 \vdash appelI(ident(fct), 58) \rightarrow m_0
                            m_5 = \text{ExpParam}(58, \text{Parametre}(\text{fct}, m_4), m_4) = \text{ExpParam}(58, 14, m_4) = \langle max, 1, var, entier \rangle . m_4
                             [\text{vars}]_{18}: m_5 \vdash \text{D\'eclaration}(\text{fct}, m_5) = \text{vars}(19, 22) \rightarrow m_6
                                       [\text{var}]_{19} : m_5 \vdash \text{var}(\text{entier}, \text{ident}(y), \frac{21}{21}) \rightarrow m_6 = \text{DeclVar}(y, v_1, \text{entier}, m_5, 0), \text{ avec } m_6 = \langle y, 5, var, entier \rangle . m_5
                                                [\text{nbre}]_{\textcolor{red}{21}}: m_5 \overset{eval}{\vdash} \text{nbre}(5) \Rightarrow v_1 = 5
                                       [\text{vnil}]_{22}: m_6 \vdash \text{vnil} \rightarrow m_6
                             [instrs]_{23}: m_6 \vdash Corps(fct, m_6) = instrs(24, 39) \rightarrow m_9
                                      [\text{tantquevrai}]_{24}: m_6 \vdash \text{tantque}(25, 28) \rightarrow m_8
                                               [>]_{25}: m_6 \stackrel{eval}{\vdash} > (26, 27) \Rightarrow v_2 > v_3 = 1 > 0 = \text{true}
                                                         [ident]_{26} : m_6 \stackrel{eval}{\vdash} ident(max) \Rightarrow v_2 = 1
                                                         [\text{nbre}]_{27} : m_6 \stackrel{eval}{\vdash} \text{nbre}(0) \Rightarrow v_3 = 0
                                                [instrs]_{28}: m_6 \vdash instrs(29, 32) \rightarrow m_8
                                                          [\text{somme}]_{29}: m_6 \vdash \text{somme}(\text{ident}(y), 31) \longrightarrow m_7 = \text{AffecterVal}(y, \text{Val}(y, m_6) + v_4, m_6)
                                                                   avec m_7 = \text{AffecterVal}(y, 5+1, m_6) = \langle y, 6, \text{ var, entier} \rangle . m_5
                                                                   [\mathrm{ident}]_{31} : m_6 \overset{eval}{\vdash} \mathrm{ident}(\max) \Rightarrow v_4 = 1
                                                          [instrs]_{32}: m_7 \vdash instrs(33, 38) \rightarrow m_8
                                                                   [affectation]_{33}: m_7 \vdash affectation(ident(max), 35) \rightarrow m_8 = AffecterVal(max, v_5, m_7)
                                                                             avec m_8 = \text{AffecterVal}(\max, 0, m_7), m_8 = < y, 6, \text{ var, entier} > . < \max, 0, \text{ var, entier} > . m_4
                                                                            [-]_{25}: m_7 \stackrel{eval}{\vdash} -(36, 37) \Rightarrow v_5 = v_6 - v_7 = 1 - 1 = 0
                                                                                      [ident]_{35}: m_7 \vdash ident(max) \Rightarrow v_6 = 1
                                                                                      [\text{nbre}]_{37}: m_7 \overset{eval}{\vdash} \text{nbre}(1) \Rightarrow v_7 = 1
                                                                   [\text{inil}]_{38}: m_8 \vdash \text{inil} \rightarrow m_8
                                                [\text{tantquefaux}]_{24}: m_8 \vdash \text{tantque}(25, 28) \rightarrow m_8
                                                        [>]_{25} : m_8 \stackrel{eval}{\vdash} > (26, 27) \Rightarrow v_8 > v_9 = 0 > 0 = false
[ident]_{26} : m_8 \stackrel{eval}{\vdash} ident(max) \Rightarrow v_8 = 0
[nbre]_{27} : m_8 \stackrel{eval}{\vdash} nbre(0) \Rightarrow v_9 = 0
                                      [instrs]_{39}: m_8 \vdash instrs(40, 42) \rightarrow m_9
                                                [\text{retour}]_{40}: m_8 \vdash \text{retour}(\text{ident}(y)) \rightarrow m_9 = \text{AffecterVal}(\text{VariableClasse}(m_8), v_{10}, m_8) = \text{AffecterVal}(C, 6, m_8)
                                                          avec m_9 = \langle y, 6, \text{ var, entier} \rangle \cdot \langle \text{max, 0, var, entier} \rangle \cdot \langle \text{fct, 12, meth, entier} \rangle \cdot \langle \text{t, @tas, tab, entier} \rangle.
                                                                                       \langle x, 3, var, entier \rangle. \langle C, 6, var, entier \rangle.
                                                         [ident]_{40}: m_8 \stackrel{eval}{\vdash} ident(y) \Rightarrow v_{10} = 6
                                                [\text{inil}]_{42}: m_9 \vdash \text{inil} \rightarrow m_9
                            [\text{rvars}]_{18}: m_9 \stackrel{retrait}{\vdash} \text{D\'eclaration}(\text{fct}, m_9) = \text{vars}(19, 22) \rightarrow m_{10}
                                      [\text{rvnil}]_{22} : m_9 \stackrel{retrait}{\vdash} \text{vnil} \to m_9
                                      [\text{retrait}]_{19} : m_9 \vdash \text{var}(\text{entier}, \frac{20}{21}) \rightarrow m_{10} = \text{RetirerDecl}(y, m_9) \text{ avec } m_{10} = < \text{max}, 0, \text{ var}, \text{ entier} >.
                                                <fct, 12, meth, entier>.<t, @tas, tab, entier>.<x, 3, var, entier>.<C, 6, var, entier>.[]
                            [\text{rentetes}]_{14}: m_{10} \stackrel{retrait}{\vdash} \text{Parametre(fct, } m_{10}) = \text{entetes}(15, 17) \rightarrow m_{11}
                                                                               retrait
                                      [\text{renil}]_{17}: m_{10} \vdash \text{enil} \rightarrow m_{10}
                                      [\text{rentete}]_{15}: m_{10} \vdash \text{entete}(\text{entier}, \frac{16}{16}) \rightarrow m_{11} = \text{RetirerDecl}(\max, m_{10})
                                               avec m_{11} = <fct, 12, meth, entier>. <t, @tas, tab, entier>. <x, 3, var, entier>. <C, 6, var, *>.[]
                  [\mathrm{ident}]_{56}: m_{11} \overset{eval}{\vdash} \mathrm{VariableClasse}\; (m_{11}) = \mathrm{ident}(\mathrm{C}) \Rightarrow v_0 = 6
         [ident]_{55} : m_4 \stackrel{eval}{\vdash} ident(x) \Rightarrow ind_0 = Val(x, m_4) = 3
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