$biostats_final_combined$

Miao Fu

2023-12-07

summary statistics

Categorical Variables

variable	category	count	percent
gender	female	315	53.662692
gender	male	272	46.337308
ethnic_group	group A	50	8.517888
ethnic_group	group B	123	20.954003
ethnic_group	group C	174	29.642249
ethnic_group	group D	155	26.405451
ethnic_group	group E	85	14.480409
parent_educ	associate's degree	128	21.805792
parent_educ	bachelor's degree	71	12.095400
parent_educ	high school	122	20.783646
parent_educ	master's degree	39	6.643952
parent_educ	some college	116	19.761499
parent_educ	some high school	111	18.909710
lunch_type	free/reduced	206	35.093697
lunch_type	standard	381	64.906303
test_prep	completed	208	35.434412
test_prep	none	379	64.565588
parent_marital_status	divorced	92	15.672913
parent_marital_status	married	343	58.432709
parent_marital_status	single	137	23.339012
parent_marital_status	widowed	15	2.555366
practice_sport	never	68	11.584327
practice_sport	regularly	218	37.137990
practice_sport	sometimes	301	51.277683
is_first_child	no	192	32.708688
is_first_child	yes	395	67.291312
transport_means	private	229	39.011925
transport_means	school_bus	358	60.988075
wkly_study_hours	< 5	154	26.235094
wkly_study_hours	> 10	104	17.717206
wkly_study_hours	5-10	329	56.047700

Numeric Variables

variable	mean	median	sd	minimum	maximum	q1	q3
nr_siblings	2.139693	2	1.481712	0	7	1	3
math_score	66.676320	67	16.113744	0	100	56	78
reading_score	69.846678	70	15.166662	17	100	60	81
writing_score	68.901192	69	15.550000	10	100	58	79

```
## pdf
## 2
```

Test the transformation for outcome variables

```
## pdf
## 2
```

No transformations improved the distribution. Original data were used.

By plotting our the pairwise correlation between variables, there is apparent linearity among the three scores. Other correlation coefficients are relatively small, indicating weak linear relationship between the variables.

```
## pdf
## 2
```

MLR lm()

MLR - Math

```
##
## Call:
## lm(formula = math_score ~ gender + ethnic_group + parent_educ +
       lunch_type + test_prep + parent_marital_status + practice_sport +
##
##
       is_first_child + nr_siblings + transport_means + wkly_study_hours,
      data = df_transformed)
##
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -48.916 -9.265 0.725 10.104 33.013
##
## Coefficients:
##
                                Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                  44.1006
                                             3.6704 12.015 < 2e-16 ***
                                  5.0855
                                              1.1386
                                                      4.467 9.61e-06 ***
## gendermale
## ethnic_groupgroup B
                                  -0.1788
                                              2.3136
                                                     -0.077
                                                             0.93841
## ethnic_groupgroup C
                                 -0.2089
                                             2.2149 -0.094 0.92489
## ethnic_groupgroup D
                                  3.6247
                                              2.2286
                                                      1.626 0.10441
## ethnic_groupgroup E
                                 11.1752
                                              2.4434
                                                      4.574 5.90e-06 ***
## parent_educhigh school
                                  -0.3235
                                             1.8015
                                                     -0.180 0.85757
## parent_educassociate's degree
                                  4.9058
                                              1.7728
                                                     2.767 0.00584 **
                                  3.1933
                                             1.8163
                                                      1.758 0.07927 .
## parent_educsome college
                                             2.0763
## parent_educbachelor's degree
                                  6.6652
                                                     3.210 0.00140 **
```

```
## parent educmaster's degree
                                   6.8096
                                              2.5417
                                                       2.679 0.00760 **
## lunch_typestandard
                                              1.1771
                                                      10.495 < 2e-16 ***
                                  12.3539
## test prepnone
                                  -4.7717
                                              1.2007
                                                      -3.974 7.99e-05 ***
## parent_marital_statusmarried
                                   5.4805
                                              1.6170
                                                       3.389 0.00075 ***
## parent_marital_statussingle
                                   2.1682
                                              1.8454
                                                       1.175
                                                              0.24053
## parent marital statuswidowed
                                                       2.045 0.04134 *
                                   7.7944
                                              3.8119
## practice sportsometimes
                                                       0.827 0.40838
                                   1.5255
                                              1.8439
## practice_sportregularly
                                   1.6701
                                              1.9046
                                                       0.877 0.38092
## is first childyes
                                   1.1303
                                              1.2125
                                                       0.932 0.35162
## nr_siblings
                                   0.7403
                                              0.3844
                                                       1.926
                                                             0.05461 .
## transport_meansschool_bus
                                  -0.4319
                                              1.1629
                                                      -0.371
                                                             0.71050
## wkly_study_hours5-10
                                              1.3429
                                                       2.636
                                                              0.00863 **
                                   3.5394
## wkly_study_hours> 10
                                   3.0384
                                              1.7540
                                                       1.732 0.08378 .
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 13.52 on 564 degrees of freedom
## Multiple R-squared: 0.3221, Adjusted R-squared: 0.2956
## F-statistic: 12.18 on 22 and 564 DF, p-value: < 2.2e-16
```

Coefficients and Significance Levels:

- Intercept (44.1006): The expected value of math_score when all other predictors are at their reference level or zero.
- gendermale (5.0855, p < 0.001): Being male is associated with an average increase of 5.0855 points in math—score compared to females, holding all else constant. This is statistically significant.
- ethnic_group: Only ethnic_groupgroup E (11.1752, p < 0.001) is significant, suggesting students in this group score higher in math compared to the reference group.
- parent_educ: The associate's degree (4.9058, p = 0.00584), bachelor's degree (6.6652, p = 0.00140), and master's degree (6.8096, p = 0.00760) are significant and associated with higher math scores compared to the reference category.
- lunch typestandard (12.3539, p < 0.001): Students with standard lunch type score significantly higher.
- test_prepnone (-4.7717, p < 0.001): Not participating in test preparation is associated with lower math scores.
- parent_marital_status: Married (5.4805, p = 0.00075) and Widowed (7.7944, p = 0.04134) are associated with higher scores.
- practice sport: Not significant.
- is first childyes: Not significant.
- nr siblings (0.7403, p = 0.05461): A borderline significant positive association with math scores.
- transport_meansschool_bus: Not significant.
- wkly_study_hours: Studying 5-10 hours (3.5394, p = 0.00863) shows a significant positive effect.

Residuals:

The spread of residuals suggests the errors are somewhat symmetrically distributed around the predicted values, which is a good sign for linear regression assumptions.

Model Fit:

Residual Standard Error (13.52): Indicates the average difference between the observed values and the values predicted by the model.

R-squared:

- Multiple R-squared (0.3221): About 32.21% of the variability in math_score is explained by the model.
- Adjusted R-squared (0.2956): Adjusts the R-squared for the number of predictors, a better measure for models with multiple predictors.

Statistic & p-value

F-statistic (12.18) and p-value (< 2.2e-16): The model is statistically significant, meaning it performs better than a model with no predictors.

MLR - reading

```
##
## Call:
  lm(formula = reading_score ~ gender + ethnic_group + parent_educ +
##
       lunch_type + test_prep + parent_marital_status + practice_sport +
##
       is first child + nr siblings + transport means + wkly study hours,
##
##
       data = df transformed)
##
## Residuals:
##
       Min
                1Q Median
                                 30
                                        Max
##
  -41.754
           -8.793
                     0.635
                             9.118
                                     30.513
##
## Coefficients:
##
                                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                   60.8028
                                               3.5826 16.972 < 2e-16 ***
                                                       -6.904 1.37e-11 ***
## gendermale
                                   -7.6725
                                               1.1114
## ethnic_groupgroup B
                                   -1.4287
                                               2.2582
                                                       -0.633 0.527220
## ethnic_groupgroup C
                                               2.1619
                                                       -0.396 0.692355
                                   -0.8558
## ethnic_groupgroup D
                                               2.1753
                                   2.5663
                                                        1.180 0.238600
## ethnic_groupgroup E
                                               2.3850
                                                        2.481 0.013402 *
                                    5.9165
## parent_educhigh school
                                                       -0.329 0.742303
                                   -0.5785
                                               1.7584
## parent_educassociate's degree
                                    4.7948
                                               1.7305
                                                        2.771 0.005776 **
## parent educsome college
                                    2.4082
                                               1.7729
                                                        1.358 0.174896
## parent educbachelor's degree
                                               2.0266
                                                        3.627 0.000313 ***
                                   7.3496
## parent_educmaster's degree
                                    8.7149
                                               2.4809
                                                        3.513 0.000479 ***
## lunch_typestandard
                                    8.4374
                                               1.1489
                                                        7.344 7.31e-13 ***
## test_prepnone
                                   -6.2822
                                               1.1720
                                                       -5.360 1.21e-07 ***
## parent_marital_statusmarried
                                   5.2439
                                               1.5783
                                                        3.322 0.000950 ***
## parent_marital_statussingle
                                    1.9235
                                               1.8013
                                                        1.068 0.286046
## parent_marital_statuswidowed
                                    5.5863
                                               3.7208
                                                        1.501 0.133813
## practice_sportsometimes
                                                        0.375 0.707488
                                    0.6757
                                               1.7998
## practice_sportregularly
                                   -0.6843
                                               1.8590
                                                       -0.368 0.712923
## is_first_childyes
                                    1.3046
                                               1.1835
                                                        1.102 0.270780
## nr_siblings
                                    0.3882
                                               0.3752
                                                        1.035 0.301309
                                               1.1351
                                                        0.250 0.802472
## transport_meansschool_bus
                                    0.2841
## wkly_study_hours5-10
                                                        2.047 0.041104 *
                                    2.6835
                                               1.3108
## wkly_study_hours> 10
                                    1.0970
                                               1.7121
                                                        0.641 0.521971
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.2 on 564 degrees of freedom
```

```
## Multiple R-squared: 0.2709, Adjusted R-squared: 0.2425
## F-statistic: 9.527 on 22 and 564 DF, p-value: < 2.2e-16</pre>
```

Coefficients and Significance Levels:

- Intercept (60.8028): The expected value of reading_score when all other predictors are at their reference level or zero.
- **gendermale** (-7.6725, p < 0.001): Being male is associated with an average decrease of 7.6725 points in reading_score compared to females, holding all else constant. This is statistically significant.
- ethnic_group: Only ethnic_groupgroup E (5.9165, p = 0.013402) is significant, suggesting students in this group score higher in reading compared to the reference group.
- parent_educ: The associate's degree (4.7948, p = 0.005776), bachelor's degree (7.3496, p = 0.000313), and master's degree (8.7149, p = 0.000479) are significant and associated with higher reading scores compared to the reference category.
- lunch_typestandard (8.4374, p < 0.001): Students with standard lunch type score significantly higher.
- test_prepnone (-6.2822, p < 0.001): Not participating in test preparation is associated with lower reading scores.
- $parent_marital_statusmarried$ (5.2439, p = 0.000950): Children of married parents score higher.
- practice_sport: Not significant.
- is_first_childyes: Not significant.
- $nr_siblings (0.3882, p = 0.301309)$: No significant association with reading scores.
- transport_meansschool_bus: Not significant.
- wkly_study_hours: Studying 5-10 hours (2.6835, p = 0.041104) shows a significant positive effect.

Residuals:

The spread of residuals suggests the errors are somewhat symmetrically distributed around the predicted values, which is a good sign for linear regression assumptions.

Model Fit:

• Residual Standard Error (13.2): Indicates the average difference between the observed values and the values predicted by the model.

R-squared:

- Multiple R-squared (0.2709): About 27.09% of the variability in reading_score is explained by the model.
- Adjusted R-squared (0.2425): Adjusts the R-squared for the number of predictors, a better measure for models with multiple predictors.

Statistic & p-value

• F-statistic (9.527) and p-value (< 2.2e-16): The model is statistically significant, meaning it performs better than a model with no predictors.

MLR - writing

```
##
## Call:
##
  lm(formula = writing_score ~ gender + ethnic_group + parent_educ +
       lunch_type + test_prep + parent_marital_status + practice_sport +
##
##
       is_first_child + nr_siblings + transport_means + wkly_study_hours,
##
       data = df_transformed)
##
##
  Residuals:
##
                                3Q
       Min
                1Q
                   Median
                                       Max
                                    26.214
##
   -46.922
           -8.043
                     1.071
                             8.811
##
## Coefficients:
##
                                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                 57.808758
                                             3.432409 16.842 < 2e-16 ***
                                                       -8.705 < 2e-16 ***
## gendermale
                                 -9.268845
                                             1.064760
## ethnic_groupgroup B
                                 -1.372239
                                             2.163560
                                                        -0.634 0.526175
## ethnic_groupgroup C
                                  0.005008
                                             2.071256
                                                         0.002 0.998072
## ethnic_groupgroup D
                                  5.010576
                                             2.084123
                                                         2.404 0.016531 *
## ethnic_groupgroup E
                                                         2.634 0.008673 **
                                  6.018419
                                             2.284980
## parent_educhigh school
                                 -0.230994
                                             1.684700
                                                        -0.137 0.890990
## parent_educassociate's degree
                                  6.130783
                                              1.657904
                                                         3.698 0.000239 ***
## parent_educsome college
                                  4.338798
                                              1.698536
                                                         2.554 0.010898 *
## parent_educbachelor's degree
                                  9.217680
                                              1.941668
                                                         4.747 2.62e-06 ***
## parent_educmaster's degree
                                 11.712279
                                              2.376896
                                                         4.928 1.10e-06 ***
## lunch_typestandard
                                  9.390698
                                             1.100772
                                                         8.531 < 2e-16 ***
                                             1.122889
## test_prepnone
                                 -8.754351
                                                        -7.796 3.09e-14 ***
## parent marital statusmarried
                                  5.246610
                                             1.512157
                                                         3.470 0.000561 ***
## parent_marital_statussingle
                                                         1.242 0.214575
                                  2.144248
                                              1.725778
## parent marital statuswidowed
                                  6.877832
                                             3.564779
                                                         1.929 0.054184 .
## practice_sportsometimes
                                                         0.971 0.331863
                                  1.674659
                                              1.724312
## practice_sportregularly
                                                         0.902 0.367574
                                  1.606102
                                             1.781092
## is_first_childyes
                                  1.045414
                                              1.133850
                                                         0.922 0.356921
## nr siblings
                                  0.546033
                                             0.359485
                                                         1.519 0.129340
## transport meansschool bus
                                  0.240107
                                                         0.221 0.825338
                                             1.087508
## wkly_study_hours5-10
                                  2.802323
                                              1.255870
                                                         2.231 0.026048 *
## wkly_study_hours> 10
                                              1.640324
                                                         0.725 0.468881
                                  1.188892
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 12.65 on 564 degrees of freedom
## Multiple R-squared: 0.3634, Adjusted R-squared: 0.3385
## F-statistic: 14.63 on 22 and 564 DF, p-value: < 2.2e-16
```

Coefficients and Significance Levels:

- Intercept (57.808758): The expected value of writing_score when all other predictors are at their reference level or zero.
- gendermale (-9.268845, p < 0.001): Being male is associated with an average decrease of 9.268845 points in writing_score compared to females, holding all else constant. This is statistically significant.
- ethnic_group: ethnic_groupgroup D (5.010576, p = 0.016531) and ethnic_groupgroup E (6.018419, p = 0.008673) are significant, suggesting students in these groups score higher in writing

- compared to the reference group.
- parent_educ: associate's degree (6.130783, p = 0.000239), some college (4.338798, p = 0.010898), bachelor's degree (9.217680, p = 2.62e-06), and master's degree (11.712279, p = 1.10e-06) are significant and associated with higher writing scores compared to the reference category.
- lunch_typestandard (9.390698, p < 0.001): Students with standard lunch type score significantly higher.
- test_prepnone (-8.754351, p < 0.001): Not participating in test preparation is associated with lower writing scores.
- $parent_marital_statusmarried$ (5.246610, p = 0.000561): Children of married parents score higher.
- practice_sport: Not significant.
- is_first_childyes: Not significant.
- $nr_siblings$ (0.546033, p = 0.129340): No significant association with writing scores.
- transport_meansschool_bus: Not significant.
- wkly_study_hours: Studying 5-10 hours (2.802323, p = 0.026048) shows a significant positive effect.

Residuals:

The spread of residuals suggests the errors are somewhat symmetrically distributed around the predicted values, which is a good sign for linear regression assumptions.

Model Fit:

• Residual Standard Error (12.65): Indicates the average difference between the observed values and the values predicted by the model.

R-squared:

- Multiple R-squared (0.3634): About 36.34% of the variability in writing_score is explained by the model.
- Adjusted R-squared (0.3385): Adjusts the R-squared for the number of predictors, a better measure for models with multiple predictors.

Statistic & p-value

• F-statistic (14.63) and p-value (< 2.2e-16): The model is statistically significant, meaning it performs better than a model with no predictors.

Cleaned datasets - updated by Nisha

Step-wise: Backwards Elimination

Math Score

```
##
## Call:
## lm(formula = math_score ~ ., data = math_df)
##
## Residuals:
## Min 1Q Median 3Q Max
```

```
## -54.864 -9.425 0.975 10.116 32.369
##
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                          23.0924
                                     5.9271
                                              3.896 0.000109 ***
                                              4.617 4.80e-06 ***
## gender
                          5.3175
                                      1.1517
## ethnic_group
                          2.7588
                                     0.4910
                                              5.618 3.00e-08 ***
## parent_educ
                          1.5290
                                     0.3843
                                             3.979 7.81e-05 ***
## lunch_type
                          12.6192
                                     1.2000 10.516 < 2e-16 ***
## test_prep
                         -5.2239
                                     1.2078 -4.325 1.80e-05 ***
## parent_marital_status
                          0.7239
                                     0.8331
                                             0.869 0.385282
## practice_sport
                           0.6461
                                     0.8845
                                              0.730 0.465418
## is_first_child
                           0.7792
                                     1.2313
                                             0.633 0.527061
## nr_siblings
                           0.6981
                                    0.3884
                                             1.797 0.072825 .
                                     1.1745
                                              0.217 0.828116
## transport_means
                           0.2551
## wkly_study_hours
                           2.0684
                                     0.8749
                                              2.364 0.018402 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.82 on 575 degrees of freedom
## Multiple R-squared: 0.2779, Adjusted R-squared: 0.2641
## F-statistic: 20.11 on 11 and 575 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ gender + ethnic_group + parent_educ +
##
       lunch_type + test_prep + parent_marital_status + practice_sport +
##
       is_first_child + nr_siblings + wkly_study_hours, data = math_df)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
  -54.777
           -9.369
                    1.069
                           10.160
                                   32.206
##
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         23.4423
                                     5.6992
                                             4.113 4.47e-05 ***
## gender
                          5.3217
                                      1.1506
                                              4.625 4.62e-06 ***
## ethnic_group
                                     0.4904
                                              5.619 2.99e-08 ***
                          2.7555
## parent educ
                          1.5300
                                     0.3839
                                              3.985 7.61e-05 ***
                                     1.1990 10.527 < 2e-16 ***
## lunch_type
                          12.6219
## test_prep
                          -5.2041
                                     1.2033 -4.325 1.80e-05 ***
                                             0.872
## parent_marital_status
                                                      0.3837
                         0.7256
                                     0.8324
## practice_sport
                           0.6470
                                     0.8837
                                              0.732
                                                      0.4644
                                              0.636
                                                      0.5249
## is_first_child
                           0.7826
                                     1.2301
                           0.6981
                                     0.3881
                                              1.799
                                                       0.0726 .
## nr_siblings
                                              2.376
## wkly_study_hours
                           2.0752
                                     0.8736
                                                     0.0178 *
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.81 on 576 degrees of freedom
## Multiple R-squared: 0.2778, Adjusted R-squared: 0.2653
## F-statistic: 22.16 on 10 and 576 DF, p-value: < 2.2e-16
```

```
## Call:
## lm(formula = math_score ~ gender + ethnic_group + parent_educ +
       lunch_type + test_prep + parent_marital_status + practice_sport +
       nr_siblings + wkly_study_hours, data = math_df)
##
##
## Residuals:
      Min
                10 Median
                                30
                                       Max
## -54.413 -9.258
                    0.787
                             9.904 32.464
##
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                      5.1120
                                              4.899 1.25e-06 ***
                          25.0419
                           5.3263
                                      1.1500
                                              4.632 4.48e-06 ***
## gender
## ethnic_group
                                      0.4901
                           2.7538
                                             5.619 3.00e-08 ***
                                      0.3837
                                              3.989 7.48e-05 ***
## parent_educ
                          1.5308
## lunch_type
                          12.6288
                                      1.1983
                                              10.539 < 2e-16 ***
                                             -4.374 1.45e-05 ***
                          -5.2506
                                      1.2005
## test_prep
## parent_marital_status
                          0.6824
                                      0.8292
                                               0.823
                                                       0.4109
                                               0.683
                                                       0.4946
## practice_sport
                           0.6017
                                      0.8804
## nr siblings
                           0.6776
                                      0.3866
                                               1.753
                                                       0.0802
## wkly_study_hours
                           2.0800
                                      0.8731
                                               2.382
                                                       0.0175 *
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.81 on 577 degrees of freedom
## Multiple R-squared: 0.2773, Adjusted R-squared: 0.266
## F-statistic: 24.6 on 9 and 577 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ gender + ethnic_group + parent_educ +
       lunch_type + test_prep + parent_marital_status + nr_siblings +
##
       wkly_study_hours, data = math_df)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
## -54.042 -9.171
                    0.792 10.144
                                  32.974
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
                                      4.6939
                                              5.629 2.83e-08 ***
## (Intercept)
                          26.4222
## gender
                           5.3307
                                      1.1494
                                              4.638 4.36e-06 ***
## ethnic_group
                                               5.624 2.90e-08 ***
                                      0.4899
                           2.7553
## parent educ
                          1.5138
                                      0.3828
                                               3.955 8.60e-05 ***
                                      1.1973 10.528 < 2e-16 ***
## lunch_type
                          12.6050
## test_prep
                          -5.2588
                                      1.1999
                                             -4.383 1.39e-05 ***
## parent_marital_status
                          0.7058
                                      0.8281
                                               0.852
                                                       0.3944
## nr siblings
                           0.6790
                                      0.3864
                                               1.757
                                                       0.0794 .
                                             2.394
## wkly_study_hours
                           2.0891
                                      0.8726
                                                       0.0170 *
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.8 on 578 degrees of freedom
## Multiple R-squared: 0.2767, Adjusted R-squared: 0.2667
```

```
## F-statistic: 27.64 on 8 and 578 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ gender + ethnic_group + parent_educ +
       lunch_type + test_prep + nr_siblings + wkly_study_hours,
##
       data = math_df)
##
## Residuals:
      Min
               1Q Median
                               30
                                      Max
## -53.440 -8.894 0.776 10.134 32.889
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    28.0713
                                4.2756
                                         6.565 1.15e-10 ***
## gender
                     5.3017
                                1.1486
                                         4.616 4.83e-06 ***
## ethnic_group
                     2.7439
                                0.4896
                                         5.605 3.23e-08 ***
                                0.3826
                                         3.976 7.90e-05 ***
## parent_educ
                     1.5210
## lunch_type
                    12.5737
                                1.1964 10.510 < 2e-16 ***
                                1.1989 -4.414 1.21e-05 ***
## test_prep
                     -5.2926
## nr_siblings
                     0.6927
                                0.3860
                                         1.795
                                                  0.0732 .
## wkly_study_hours
                     2.0825
                                0.8723
                                         2.387
                                                 0.0173 *
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.8 on 579 degrees of freedom
## Multiple R-squared: 0.2758, Adjusted R-squared: 0.2671
## F-statistic: 31.5 on 7 and 579 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ gender + ethnic_group + parent_educ +
##
       lunch type + test prep + wkly study hours, data = math df)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -52.943 -9.439
                    0.630 10.403 31.459
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                    29.7605
                                4.1787
                                         7.122 3.16e-12 ***
## gender
                     5.2204
                                1.1499
                                         4.540 6.85e-06 ***
                                0.4904
## ethnic_group
                     2.7208
                                         5.549 4.39e-08 ***
                                0.3833
                                         3.947 8.88e-05 ***
## parent_educ
                     1.5128
## lunch_type
                    12.5868
                                1.1987 10.501 < 2e-16 ***
## test_prep
                    -5.3895
                                1.2000 -4.491 8.55e-06 ***
## wkly_study_hours
                     2.1599
                                0.8729
                                         2.474
                                                0.0136 *
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.82 on 580 degrees of freedom
## Multiple R-squared: 0.2718, Adjusted R-squared: 0.2642
## F-statistic: 36.08 on 6 and 580 DF, p-value: < 2.2e-16
```

```
## Start: AIC=3095.24
## math_score ~ gender + ethnic_group + parent_educ + lunch_type +
      test prep + parent marital status + practice sport + is first child +
##
      nr_siblings + transport_means + wkly_study_hours
##
##
                          Df Sum of Sq
                                          RSS
## - transport means
                                 9.0 109886 3093.3
                                  76.5 109954 3093.6
## - is first child
                           1
## - practice_sport
                           1
                                 102.0 109979 3093.8
## - parent_marital_status 1
                                144.3 110022 3094.0
## <none>
                                      109877 3095.2
                                617.2 110495 3096.5
## - nr_siblings
                           1
                                1068.1 110945 3098.9
## - wkly_study_hours
                           1
## - parent_educ
                                3025.1 112902 3109.2
                           1
## - test_prep
                                3574.7 113452 3112.0
                           1
                               4073.6 113951 3114.6
## - gender
                           1
                              6032.2 115910 3124.6
## - ethnic_group
                           1
## - lunch_type
                               21130.5 131008 3196.5
## Step: AIC=3093.29
## math_score ~ gender + ethnic_group + parent_educ + lunch_type +
      test_prep + parent_marital_status + practice_sport + is_first_child +
##
      nr_siblings + wkly_study_hours
##
##
                          Df Sum of Sq
                                          RSS
                                                 ATC
## - is_first_child
                           1
                                 77.2 109964 3091.7
## - practice_sport
                                 102.3 109989 3091.8
                           1
## - parent_marital_status 1
                                145.0 110031 3092.1
                                      109886 3093.3
## <none>
                                617.2 110504 3094.6
## - nr siblings
                           1
                                1076.6 110963 3097.0
## - wkly_study_hours
                           1
## - parent_educ
                           1
                                3029.8 112916 3107.3
                                3568.0 113454 3110.0
## - test_prep
                           1
                           1 4081.2 113968 3112.7
## - gender
                                6023.6 115910 3122.6
## - ethnic group
                           1
## - lunch_type
                           1 21141.9 131028 3194.6
##
## Step: AIC=3091.7
## math_score ~ gender + ethnic_group + parent_educ + lunch_type +
      test_prep + parent_marital_status + practice_sport + nr_siblings +
##
##
      wkly study hours
##
                          Df Sum of Sa
                                          RSS
                                  89.0 110053 3090.2
## - practice_sport
                          1
                                 129.1 110093 3090.4
## - parent_marital_status 1
                                       109964 3091.7
## <none>
## - nr_siblings
                                585.5 110549 3092.8
                           1
## - wkly_study_hours
                                1081.6 111045 3095.4
                           1
## - parent_educ
                           1
                                3032.9 112996 3105.7
                                3645.7 113609 3108.8
## - test_prep
                           1
                           1 4088.5 114052 3111.1
## - gender
                          1 6016.6 115980 3121.0
## - ethnic group
## - lunch type
                          1 21166.9 131130 3193.0
##
```

```
## Step: AIC=3090.18
## math_score ~ gender + ethnic_group + parent_educ + lunch_type +
       test prep + parent marital status + nr siblings + wkly study hours
##
##
##
                           Df Sum of Sq
                                            RSS
                                                   ATC
## - parent marital status
                                   138.3 110191 3088.9
                           1
## <none>
                                         110053 3090.2
## - nr siblings
                             1
                                   587.9 110640 3091.3
## - wkly_study_hours
                            1
                                  1091.4 111144 3094.0
## - parent_educ
                            1
                                  2978.5 113031 3103.9
## - test_prep
                            1
                                  3657.3 113710 3107.4
## - gender
                            1
                                  4095.3 114148 3109.6
## - ethnic_group
                                  6022.9 116075 3119.5
                            1
## - lunch_type
                            1
                                 21105.0 131158 3191.2
##
## Step: AIC=3088.91
  math_score ~ gender + ethnic_group + parent_educ + lunch_type +
##
       test_prep + nr_siblings + wkly_study_hours
##
##
                      Df Sum of Sq
                                       RSS
## <none>
                                    110191 3088.9
## - nr siblings
                             613.0 110804 3090.2
## - wkly_study_hours
                            1084.6 111275 3092.7
                       1
## - parent_educ
                       1
                            3008.2 113199 3102.7
## - test_prep
                       1
                            3708.6 113900 3106.3
## - gender
                       1
                            4054.4 114245 3108.1
## - ethnic_group
                            5977.9 116169 3117.9
                       1
## - lunch_type
                       1
                           21020.1 131211 3189.4
```

With manual elimination, the model we obtained was Math Score \sim Gender + Ethnic Group + Parent Education + Lunch Type + Test Prep + Weekly Study Hours.

When using the single-function method, the model obtained with the lowest AIC was Math Score \sim Gender + Ethnic Group + Parent Education + Lunch Type + Test Prep + Number of Siblings + Weekly Study Hours. Both models' MSEs are within 0.5 points of each other, while the single function had a lower MSE by about 1 point.

Reading Score

```
##
## lm(formula = reading_score ~ ., data = reading_df)
##
## Residuals:
##
       Min
                1Q Median
                                 3Q
                                        Max
## -46.401 -9.051
                     0.404
                             9.807
                                     33.637
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                              10.673 < 2e-16 ***
                          61.3874
                                       5.7518
                          -7.5190
## gender
                                       1.1176
                                               -6.728 4.18e-11 ***
## ethnic_group
                                       0.4765
                                                3.816 0.00015 ***
                           1.8185
## parent_educ
                           1.7505
                                       0.3729
                                                4.694 3.35e-06 ***
## lunch_type
                                                7.410 4.53e-13 ***
                           8.6295
                                       1.1646
                                       1.1721 -5.676 2.19e-08 ***
## test_prep
                          -6.6530
```

```
## parent_marital_status
                          0.5050
                                     0.8085
                                              0.625 0.53247
                                     0.8583 -0.813 0.41684
## practice_sport
                          -0.6974
                          0.9079
## is first child
                                      1.1949
                                              0.760 0.44768
## nr_siblings
                          0.3178
                                      0.3770
                                              0.843 0.39960
## transport means
                          0.8813
                                      1.1398
                                              0.773 0.43969
## wkly study hours
                                     0.8490
                                              1.197 0.23180
                          1.0163
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.41 on 575 degrees of freedom
## Multiple R-squared: 0.2323, Adjusted R-squared: 0.2177
## F-statistic: 15.82 on 11 and 575 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ gender + ethnic_group + parent_educ +
       lunch_type + test_prep + practice_sport + is_first_child +
##
       nr_siblings + transport_means + wkly_study_hours, data = reading_df)
##
## Residuals:
               1Q Median
                                3Q
      Min
                                      Max
## -45.962 -9.031
                    0.340
                             9.774 33.510
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                    62.6218
                                5.3988 11.599 < 2e-16 ***
                                 1.1166 -6.752 3.56e-11 ***
                    -7.5395
## gender
## ethnic_group
                     1.8103
                                0.4761
                                        3.803 0.000158 ***
## parent_educ
                                0.3726
                                         4.713 3.06e-06 ***
                     1.7562
## lunch_type
                     8.6086
                                1.1635
                                         7.399 4.88e-13 ***
## test_prep
                                1.1706 -5.707 1.84e-08 ***
                    -6.6809
## practice_sport
                    -0.6789
                                0.8574 -0.792 0.428771
## is_first_child
                     0.8467
                                 1.1902
                                         0.711 0.477108
## nr_siblings
                     0.3259
                                0.3765
                                         0.865 0.387178
## transport_means
                     0.8883
                                1.1391
                                         0.780 0.435820
## wkly_study_hours
                     1.0114
                                0.8485
                                         1.192 0.233773
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.41 on 576 degrees of freedom
## Multiple R-squared: 0.2318, Adjusted R-squared: 0.2185
## F-statistic: 17.38 on 10 and 576 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ gender + ethnic_group + parent_educ +
##
       lunch_type + test_prep + practice_sport + nr_siblings + transport_means +
       wkly_study_hours, data = reading_df)
##
##
## Residuals:
      Min
                1Q Median
                                3Q
                                       Max
## -45.609 -8.970 0.378
                            9.579 32.976
## Coefficients:
```

```
##
                   Estimate Std. Error t value Pr(>|t|)
                                4.8978 13.115 < 2e-16 ***
## (Intercept)
                    64.2344
                                1.1161 -6.749 3.62e-11 ***
## gender
                    -7.5327
## ethnic_group
                     1.8094
                                0.4759
                                         3.802 0.000159 ***
## parent_educ
                     1.7565
                                0.3725
                                         4.716 3.02e-06 ***
                                1.1629
                                        7.411 4.49e-13 ***
## lunch type
                     8.6180
                               1.1681 -5.761 1.36e-08 ***
## test_prep
                    -6.7298
## practice_sport
                    -0.7300
                                0.8540 -0.855 0.393012
## nr_siblings
                     0.3027
                                0.3750
                                         0.807 0.419780
## transport_means
                     0.8979
                                1.1386
                                         0.789 0.430634
## wkly_study_hours
                     1.0168
                                0.8481
                                         1.199 0.231087
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.4 on 577 degrees of freedom
## Multiple R-squared: 0.2312, Adjusted R-squared: 0.2192
## F-statistic: 19.27 on 9 and 577 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ gender + ethnic_group + parent_educ +
       lunch_type + test_prep + practice_sport + nr_siblings + wkly_study_hours,
       data = reading_df)
##
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -45.293 -8.920
                    0.575
                            9.576 32.489
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                    65.5028
                                4.6247 14.164 < 2e-16 ***
## gender
                    -7.5180
                                1.1155 -6.739 3.86e-11 ***
## ethnic_group
                     1.7978
                                0.4755
                                         3.781 0.000172 ***
                     1.7603
                                0.3723
                                         4.728 2.85e-06 ***
## parent_educ
## lunch_type
                     8.6274
                                1.1625
                                         7.422 4.16e-13 ***
## test_prep
                    -6.6611
                                1.1645 -5.720 1.71e-08 ***
## practice_sport
                    -0.7272
                                0.8537 -0.852 0.394695
## nr_siblings
                     0.3025
                                0.3748
                                         0.807 0.419988
## wkly study hours
                     1.0410
                                0.8473
                                         1.229 0.219699
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.4 on 578 degrees of freedom
## Multiple R-squared: 0.2303, Adjusted R-squared: 0.2197
## F-statistic: 21.62 on 8 and 578 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ gender + ethnic_group + parent_educ +
##
       lunch_type + test_prep + practice_sport + wkly_study_hours,
##
       data = reading df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
```

```
## -45.079 -8.940 0.773 9.687 32.757
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                    66.2290
                                4.5350 14.604 < 2e-16 ***
                    -7.5535
                                1.1143 -6.779 3.00e-11 ***
## gender
                     1.7877
                                0.4752
                                         3.762 0.000186 ***
## ethnic_group
                                0.3722
                                         4.721 2.95e-06 ***
## parent educ
                     1.7569
## lunch_type
                     8.6333
                                1.1621
                                         7.429 3.94e-13 ***
## test_prep
                                1.1629 -5.764 1.33e-08 ***
                    -6.7034
                    -0.7223
## practice_sport
                                0.8534 -0.846 0.397676
                                0.8460
                                        1.270 0.204455
## wkly_study_hours
                    1.0748
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.39 on 579 degrees of freedom
## Multiple R-squared: 0.2295, Adjusted R-squared: 0.2201
## F-statistic: 24.63 on 7 and 579 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ gender + ethnic_group + parent_educ +
##
       lunch_type + test_prep + wkly_study_hours, data = reading_df)
##
## Residuals:
      Min
                1Q Median
                               ЗQ
                                      Max
## -45.551 -8.822
                    0.863
                            9.721
                                  32.252
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
                                4.0483 15.933 < 2e-16 ***
## (Intercept)
                    64.5007
                    -7.5573
                                1.1140 -6.784 2.90e-11 ***
## gender
## ethnic_group
                     1.7865
                                0.4751
                                         3.761 0.000187 ***
## parent_educ
                     1.7770
                                0.3713
                                         4.786 2.16e-06 ***
## lunch_type
                     8.6631
                                1.1613
                                        7.460 3.18e-13 ***
## test_prep
                     -6.6919
                                1.1626 -5.756 1.39e-08 ***
                                0.8457
                                         1.258 0.208928
## wkly_study_hours
                     1.0638
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.39 on 580 degrees of freedom
## Multiple R-squared: 0.2285, Adjusted R-squared: 0.2205
## F-statistic: 28.63 on 6 and 580 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ gender + ethnic_group + parent_educ +
##
       lunch_type + test_prep, data = reading_df)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -44.354 -8.959 0.802
                            9.901 32.216
## Coefficients:
```

```
##
               Estimate Std. Error t value Pr(>|t|)
                            3.6485 18.285 < 2e-16 ***
## (Intercept)
                66.7121
## gender
                -7.5066
                            1.1139 -6.739 3.84e-11 ***
                                    3.773 0.000178 ***
## ethnic_group
                1.7930
                            0.4753
## parent educ
                 1.7606
                            0.3713
                                     4.742 2.66e-06 ***
                 8.6667
                                    7.459 3.18e-13 ***
## lunch type
                            1.1618
                -6.8289
                            1.1580 -5.897 6.28e-09 ***
## test_prep
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.4 on 581 degrees of freedom
## Multiple R-squared: 0.2264, Adjusted R-squared: 0.2197
## F-statistic: 34.01 on 5 and 581 DF, p-value: < 2.2e-16
## Start: AIC=3060.01
## reading_score ~ gender + ethnic_group + parent_educ + lunch_type +
##
       test_prep + parent_marital_status + practice_sport + is_first_child +
##
       nr_siblings + transport_means + wkly_study_hours
##
                          Df Sum of Sq
##
                                          RSS
## - parent_marital_status 1
                                 70.2 103547 3058.4
## - is_first_child
                                 103.9 103581 3058.6
                           1
## - transport_means
                                107.6 103584 3058.6
                           1
                                 118.8 103595 3058.7
## - practice_sport
                           1
## - nr_siblings
                                 127.9 103605 3058.7
                           1
## - wkly study hours
                          1
                                257.8 103734 3059.5
## <none>
                                       103477 3060.0
## - ethnic_group
                                2621.0 106098 3072.7
                           1
## - parent_educ
                           1
                                3965.2 107442 3080.1
## - test_prep
                           1
                                5798.3 109275 3090.0
## - gender
                           1
                                8145.0 111622 3102.5
                                9881.5 113358 3111.6
## - lunch_type
                           1
##
## Step: AIC=3058.41
## reading_score ~ gender + ethnic_group + parent_educ + lunch_type +
##
       test_prep + practice_sport + is_first_child + nr_siblings +
##
       transport_means + wkly_study_hours
##
##
                     Df Sum of Sq
                                     RSS
                                            ATC
## - is_first_child
                             91.0 103638 3056.9
                      1
## - transport_means
                            109.3 103656 3057.0
                      1
## - practice_sport
                           112.7 103660 3057.1
## - nr siblings
                           134.6 103681 3057.2
                      1
## - wkly study hours 1
                            255.4 103802 3057.8
## <none>
                                  103547 3058.4
## - ethnic_group
                           2599.5 106146 3071.0
                      1
## - parent_educ
                      1
                           3993.6 107540 3078.6
## - test prep
                      1
                           5855.5 109402 3088.7
## - gender
                      1
                           8196.5 111743 3101.1
## - lunch_type
                           9841.8 113389 3109.7
##
## Step: AIC=3056.92
## reading_score ~ gender + ethnic_group + parent_educ + lunch_type +
##
       test_prep + practice_sport + nr_siblings + transport_means +
```

```
##
       wkly_study_hours
##
##
                      Df Sum of Sq
                                      RSS
                                              AIC
                            111.7 103750 3055.6
## - transport_means
                       1
## - nr_siblings
                             117.1 103755 3055.6
                             131.2 103769 3055.7
## - practice_sport
                       1
## - wkly_study_hours 1
                             258.1 103896 3056.4
## <none>
                                   103638 3056.9
                            2597.0 106235 3069.4
## - ethnic_group
                       1
## - parent_educ
                       1
                            3994.8 107633 3077.1
## - test_prep
                       1
                            5962.1 109600 3087.8
                            8182.2 111820 3099.5
## - gender
                       1
                            9864.6 113502 3108.3
## - lunch_type
                       1
##
## Step: AIC=3055.56
## reading_score ~ gender + ethnic_group + parent_educ + lunch_type +
##
       test_prep + practice_sport + nr_siblings + wkly_study_hours
##
                      Df Sum of Sq
##
                                      RSS
                                             ATC
## - nr siblings
                       1
                            116.9 103866 3054.2
                             130.2 103880 3054.3
## - practice_sport
                       1
## - wkly_study_hours 1
                             271.0 104021 3055.1
## <none>
                                   103750 3055.6
## - ethnic_group
                            2566.2 106316 3067.9
                       1
                            4012.9 107762 3075.8
## - parent_educ
                       1
## - test_prep
                       1
                            5873.7 109623 3085.9
## - gender
                            8152.7 111902 3098.0
                       1
                            9887.1 113637 3107.0
## - lunch_type
                       1
##
## Step: AIC=3054.22
## reading_score ~ gender + ethnic_group + parent_educ + lunch_type +
##
       test_prep + practice_sport + wkly_study_hours
##
##
                      Df Sum of Sq
                                      RSS
                                             AIC
## - practice_sport
                             128.5 103995 3052.9
## - wkly_study_hours 1
                             289.5 104156 3053.8
## <none>
                                   103866 3054.2
## - ethnic_group
                            2539.1 106406 3066.4
                       1
## - parent_educ
                       1
                            3997.8 107864 3074.4
                            5960.5 109827 3085.0
## - test_prep
                       1
## - gender
                       1
                            8242.7 112109 3097.0
## - lunch_type
                       1
                            9901.1 113768 3105.7
## Step: AIC=3052.94
## reading_score ~ gender + ethnic_group + parent_educ + lunch_type +
##
       test_prep + wkly_study_hours
##
##
                                      RSS
                      Df Sum of Sq
                                              AIC
## - wkly_study_hours 1
                             283.7 104279 3052.5
## <none>
                                   103995 3052.9
## - ethnic_group
                            2535.8 106531 3065.1
                       1
## - parent_educ
                       1
                            4106.5 108102 3073.7
## - test_prep
                       1
                            5941.0 109936 3083.6
## - gender
                            8251.2 112246 3095.8
```

```
## - lunch_type
                             9978.6 113974 3104.7
##
## Step: AIC=3052.54
  reading_score ~ gender + ethnic_group + parent_educ + lunch_type +
##
       test_prep
##
                  Df Sum of Sq
##
                                   RSS
                                          AIC
## <none>
                                104279 3052.5
## - ethnic_group
                         2554.7 106833 3064.8
                   1
## - parent_educ
                   1
                         4036.2 108315 3072.8
## - test_prep
                   1
                         6241.3 110520 3084.7
## - gender
                   1
                         8151.5 112430 3094.7
## - lunch_type
                   1
                         9987.0 114266 3104.2
```

With manual elimination, the model we obtained was Reading Score \sim Gender + Ethnic Group + Parent Education + Lunch Type + Test Prep.

When using the single-function method, the model obtained with the lowest AIC was Reading Score \sim Gender + Ethnic Group + Parent Education + Lunch Type + Test Prep. The one-function model had a lower MSE than the manually-calculated model by about 14 points and a higher R-squared value by about 10 points.

Writing Score

```
##
## Call:
## lm(formula = writing_score ~ ., data = writing_df)
##
## Residuals:
##
       Min
                1Q
                   Median
                                 3Q
                                        Max
## -51.711
           -8.503
                     0.758
                             9.459
                                    28.543
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                       5.5195
                                              10.708
                                                       < 2e-16 ***
                          59.1030
## gender
                          -9.1137
                                       1.0725
                                               -8.498
                                                       < 2e-16 ***
## ethnic_group
                           2.2059
                                       0.4572
                                                4.824 1.80e-06 ***
## parent_educ
                           2.3308
                                       0.3579
                                                6.513 1.61e-10 ***
## lunch_type
                                                8.525
                           9.5265
                                       1.1175
                                                       < 2e-16 ***
## test_prep
                          -8.9524
                                               -7.960 9.25e-15 ***
                                       1.1247
## parent_marital_status
                                                0.985
                           0.7645
                                       0.7758
                                                         0.325
## practice_sport
                           0.4809
                                       0.8237
                                                0.584
                                                         0.560
## is_first_child
                           0.6009
                                                0.524
                                                         0.600
                                       1.1466
## nr_siblings
                           0.4607
                                       0.3617
                                                1.274
                                                         0.203
## transport_means
                           0.7647
                                       1.0937
                                                0.699
                                                         0.485
## wkly_study_hours
                           1.1007
                                       0.8147
                                                1.351
                                                         0.177
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 12.87 on 575 degrees of freedom
## Multiple R-squared: 0.3275, Adjusted R-squared: 0.3147
## F-statistic: 25.46 on 11 and 575 DF, p-value: < 2.2e-16
```

```
## Call:
## lm(formula = writing_score ~ gender + ethnic_group + parent_educ +
       lunch_type + test_prep + parent_marital_status + practice_sport +
       nr_siblings + transport_means + wkly_study_hours, data = writing_df)
##
##
## Residuals:
      Min
                10 Median
                                30
                                       Max
## -51.434 -8.291
                                    28.702
                     0.834
                             9.509
##
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          60.3211
                                      5.0031 12.057 < 2e-16 ***
                          -9.1103
                                      1.0718 -8.500 < 2e-16 ***
## gender
                                      0.4570
## ethnic_group
                           2.2047
                                               4.825 1.80e-06 ***
                           2.3314
                                      0.3576
                                               6.519 1.55e-10 ***
## parent_educ
## lunch_type
                           9.5317
                                      1.1168
                                               8.535 < 2e-16 ***
                                      1.1219 -8.012 6.28e-15 ***
## test_prep
                          -8.9887
## parent_marital_status
                         0.7312
                                      0.7727
                                               0.946
                                                        0.344
                                      0.8205
                                               0.544
                                                        0.587
## practice_sport
                           0.4462
## nr siblings
                           0.4449
                                      0.3602
                                               1.235
                                                        0.217
## transport_means
                           0.7719
                                      1.0930
                                               0.706
                                                        0.480
## wkly_study_hours
                                      0.8142
                                               1.356
                                                        0.176
                           1.1041
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 12.86 on 576 degrees of freedom
## Multiple R-squared: 0.3272, Adjusted R-squared: 0.3155
## F-statistic: 28.01 on 10 and 576 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + ethnic_group + parent_educ +
##
       lunch_type + test_prep + parent_marital_status + nr_siblings +
##
       transport_means + wkly_study_hours, data = writing_df)
##
## Residuals:
##
      Min
                10 Median
                                3Q
                                       Max
## -51.159 -8.417
                    0.695
                             9.645
                                    28.655
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          61.3413
                                      4.6352 13.234 < 2e-16 ***
                                      1.0711 -8.502 < 2e-16 ***
## gender
                          -9.1071
                                      0.4567
                                               4.830 1.75e-06 ***
## ethnic_group
                           2.2058
                                      0.3567
                                               6.501 1.72e-10 ***
## parent_educ
                           2.3188
## lunch_type
                          9.5141
                                      1.1156
                                               8.528 < 2e-16 ***
## test_prep
                          -8.9949
                                      1.1211 -8.023 5.79e-15 ***
                         0.7486
                                      0.7716
                                               0.970
                                                        0.332
## parent_marital_status
                                              1.239
                                                        0.216
## nr_siblings
                           0.4460
                                      0.3600
## transport_means
                           0.7742
                                      1.0923
                                               0.709
                                                        0.479
## wkly_study_hours
                           1.1108
                                      0.8136
                                               1.365
                                                        0.173
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
```

```
## Residual standard error: 12.86 on 577 degrees of freedom
## Multiple R-squared: 0.3269, Adjusted R-squared: 0.3164
## F-statistic: 31.13 on 9 and 577 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + ethnic_group + parent_educ +
       lunch_type + test_prep + parent_marital_status + nr_siblings +
##
       wkly_study_hours, data = writing_df)
##
## Residuals:
      Min
               1Q Median
                                3Q
                                      Max
## -50.889 -8.443
                    0.979
                             9.527
                                   28.924
##
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                         62,4294
                                     4.3717 14.280 < 2e-16 ***
## gender
                          -9.0942
                                      1.0705 -8.495 < 2e-16 ***
## ethnic_group
                          2.1959
                                     0.4563
                                              4.813 1.90e-06 ***
## parent_educ
                          2.3220
                                     0.3565
                                              6.514 1.60e-10 ***
## lunch_type
                                              8.540 < 2e-16 ***
                          9.5223
                                     1.1151
## test prep
                          -8.9355
                                     1.1175 -7.996 7.04e-15 ***
## parent_marital_status
                         0.7535
                                     0.7712
                                              0.977
                                                        0.329
## nr siblings
                           0.4457
                                     0.3599
                                              1.238
                                                        0.216
                           1.1318
                                              1.393
                                                        0.164
## wkly_study_hours
                                     0.8127
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 12.85 on 578 degrees of freedom
## Multiple R-squared: 0.3263, Adjusted R-squared: 0.317
## F-statistic: 34.99 on 8 and 578 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + ethnic_group + parent_educ +
##
       lunch_type + test_prep + nr_siblings + wkly_study_hours,
##
       data = writing df)
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -50.246 -8.263 0.690
                            9.167 28.855
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                     64.1899
                                3.9829 16.116 < 2e-16 ***
                     -9.1252
                                 1.0700 -8.528 < 2e-16 ***
## gender
## ethnic_group
                     2.1838
                                0.4561
                                         4.788 2.14e-06 ***
                     2.3296
                                0.3564
                                         6.537 1.38e-10 ***
## parent_educ
## lunch_type
                     9.4888
                                         8.514 < 2e-16 ***
                                1.1145
## test_prep
                     -8.9716
                                1.1169 -8.033 5.35e-15 ***
## nr_siblings
                     0.4603
                                0.3595
                                         1.280
                                                   0.201
## wkly_study_hours
                     1.1248
                                0.8126
                                         1.384
                                                   0.167
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 12.85 on 579 degrees of freedom
## Multiple R-squared: 0.3252, Adjusted R-squared: 0.317
## F-statistic: 39.86 on 7 and 579 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + ethnic_group + parent_educ +
       lunch_type + test_prep + wkly_study_hours, data = writing_df)
##
## Residuals:
##
      Min
                10 Median
                                3Q
                                       Max
## -49.917 -8.391
                    0.613
                             9.143 29.293
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                     65.3125
                                 3.8874 16.801 < 2e-16 ***
## gender
                     -9.1792
                                 1.0698 -8.581 < 2e-16 ***
## ethnic_group
                     2.1684
                                 0.4562
                                         4.753 2.53e-06 ***
                                 0.3566
                                        6.519 1.54e-10 ***
## parent_educ
                     2.3242
## lunch_type
                     9.4976
                                1.1151 8.517 < 2e-16 ***
## test prep
                     -9.0360
                                 1.1163 -8.094 3.40e-15 ***
## wkly_study_hours
                     1.1762
                                0.8121
                                          1.448
                                                   0.148
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 12.86 on 580 degrees of freedom
## Multiple R-squared: 0.3233, Adjusted R-squared: 0.3163
## F-statistic: 46.18 on 6 and 580 DF, p-value: < 2.2e-16
## Start: AIC=3011.6
## writing_score ~ gender + ethnic_group + parent_educ + lunch_type +
##
       test_prep + parent_marital_status + practice_sport + is_first_child +
##
       nr_siblings + transport_means + wkly_study_hours
##
                           Df Sum of Sq
                                           RSS
                                  45.5 95330 3009.9
## - is first child
                            1
## - practice_sport
                           1
                                   56.5 95341 3009.9
## - transport_means
                                  81.0 95366 3010.1
                            1
## - parent_marital_status 1
                                  160.9 95446 3010.6
## - nr_siblings
                            1
                                 268.8 95554 3011.2
## - wkly_study_hours
                           1
                                  302.5 95587 3011.5
                                         95285 3011.6
## <none>
## - ethnic_group
                                 3856.7 99142 3032.9
                            1
## - parent_educ
                            1
                                7030.2 102315 3051.4
                                10498.8 105784 3070.9
## - test_prep
                            1
## - gender
                            1
                                11966.3 107251 3079.0
                                12042.4 107327 3079.5
## - lunch_type
                            1
## Step: AIC=3009.88
## writing_score ~ gender + ethnic_group + parent_educ + lunch_type +
##
       test_prep + parent_marital_status + practice_sport + nr_siblings +
##
       transport means + wkly study hours
##
```

```
##
                           Df Sum of Sq
                                           RSS
                                                  AIC
                                  48.9 95379 3008.2
## - practice_sport
                            1
## - transport means
                                  82.6 95413 3008.4
## - parent_marital_status 1
                                  148.2 95479 3008.8
## - nr_siblings
                            1
                                  252.5 95583 3009.4
## - wkly study hours
                                  304.4 95635 3009.8
                            1
                                         95330 3009.9
## <none>
## - ethnic_group
                                 3852.7 99183 3031.1
                            1
## - parent_educ
                            1
                                7033.6 102364 3049.7
## - test_prep
                            1 10624.5 105955 3069.9
## - gender
                            1 11957.7 107288 3077.2
## - lunch_type
                              12056.6 107387 3077.8
                            1
##
## Step: AIC=3008.18
## writing_score ~ gender + ethnic_group + parent_educ + lunch_type +
##
       test_prep + parent_marital_status + nr_siblings + transport_means +
##
       wkly_study_hours
##
##
                           Df Sum of Sq
                                           RSS
                                                  AIC
## - transport means
                            1
                                 83.0 95462 3006.7
                                  155.6 95535 3007.1
## - parent_marital_status 1
## - nr_siblings
                                  253.7 95633 3007.7
                            1
## - wkly_study_hours
                                  308.2 95688 3008.1
                            1
                                         95379 3008.2
## <none>
                                 3856.6 99236 3029.4
## - ethnic_group
                            1
## - parent_educ
                            1
                                 6987.2 102367 3047.7
## - test_prep
                                10640.3 106020 3068.3
                            1
                                11949.7 107329 3075.5
## - gender
                            1
                                12022.2 107402 3075.9
## - lunch_type
                            1
##
## Step: AIC=3006.69
## writing_score ~ gender + ethnic_group + parent_educ + lunch_type +
##
       test_prep + parent_marital_status + nr_siblings + wkly_study_hours
##
##
                           Df Sum of Sq
                                           RSS
                                                  AIC
                                  157.7
                                        95620 3005.7
## - parent_marital_status
                           1
## - nr siblings
                                  253.3 95716 3006.2
## - wkly_study_hours
                                  320.3 95783 3006.7
                            1
## <none>
                                         95462 3006.7
                                 3825.5 99288 3027.8
## - ethnic_group
                            1
                                7007.4 102470 3046.3
## - parent educ
                            1
## - test_prep
                            1 10559.2 106022 3066.3
                                11919.4 107382 3073.8
## - gender
                            1
                               12044.3 107507 3074.4
## - lunch_type
                            1
## Step: AIC=3005.66
## writing_score ~ gender + ethnic_group + parent_educ + lunch_type +
##
       test_prep + nr_siblings + wkly_study_hours
##
##
                      Df Sum of Sq
                                      RSS
                                             AIC
                             270.7
                                    95891 3005.3
## - nr_siblings
                       1
## - wkly_study_hours
                             316.4 95936 3005.6
## <none>
                                    95620 3005.7
## - ethnic group
                            3786.2 99406 3026.4
```

```
## - parent_educ
                            7057.0 102677 3045.5
                       1
## - test_prep
                           10656.5 106277 3065.7
                       1
## - lunch type
                       1
                           11971.1 107591 3072.9
## - gender
                           12011.2 107631 3073.1
                       1
##
## Step: AIC=3005.32
## writing_score ~ gender + ethnic_group + parent_educ + lunch_type +
       test_prep + wkly_study_hours
##
##
##
                      Df Sum of Sq
                                       RSS
                                              AIC
## <none>
                                     95891 3005.3
## - wkly_study_hours
                                     96238 3005.4
                             346.8
## - ethnic_group
                            3735.6 99626 3025.8
                       1
## - parent_educ
                       1
                            7025.2 102916 3044.8
## - test_prep
                           10832.0 106723 3066.1
                       1
## - lunch_type
                       1
                           11993.5 107884 3072.5
## - gender
                           12172.7 108064 3073.5
                       1
```

With manual elimination, the model we obtained was Writing Score \sim Gender + Ethnic Group + Parent Education + Lunch Type + Test Prep.

When using the single-function method, the model obtained with the lowest AIC was Writing Score \sim Gender + Ethnic Group + Parent Education + Lunch Type + Test Prep + Weekly Study Hours. Both models had equal R-squared values and MSEs within 0.6 points of each other.

Step-wise: Forward Elimination

Math Score

```
##
## Call:
## lm(formula = math_score ~ gender, data = step_df)
##
## Residuals:
##
                1Q Median
                                3Q
      Min
                                       Max
## -63.933 -10.393
                    0.147 11.107
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                58.014
                             2.029 28.596 < 2e-16 ***
                                     4.511 7.8e-06 ***
## gender
                  5.920
                             1.312
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 15.85 on 585 degrees of freedom
## Multiple R-squared: 0.03362,
                                    Adjusted R-squared: 0.03196
## F-statistic: 20.35 on 1 and 585 DF, p-value: 7.801e-06
##
## Call:
## lm(formula = math_score ~ ethnic_group, data = step_df)
## Residuals:
```

```
10 Median
                               3Q
## -66.134 -9.256
                   0.744 10.805 39.112
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                           1.8778 30.230 < 2e-16 ***
                56.7656
## (Intercept)
                            0.5553
                                   5.624 2.9e-08 ***
## ethnic_group
                 3.1227
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 15.71 on 585 degrees of freedom
## Multiple R-squared: 0.05129,
                                  Adjusted R-squared:
## F-statistic: 31.62 on 1 and 585 DF, p-value: 2.9e-08
##
## Call:
## lm(formula = math_score ~ parent_educ, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -63.753 -9.889
                   0.823 11.399
                                  35.247
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 62.3292
                          1.4986 41.591
## parent_educ 1.4240
                           0.4408
                                  3.231
                                           0.0013 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 15.99 on 585 degrees of freedom
## Multiple R-squared: 0.01753,
                                  Adjusted R-squared: 0.01585
## F-statistic: 10.44 on 1 and 585 DF, p-value: 0.001304
##
## Call:
## lm(formula = math_score ~ lunch_type, data = step_df)
## Residuals:
##
      Min
               10 Median
                               3Q
## -58.286 -10.286
                   0.787 10.787 41.714
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                45.360
                            2.212
                                    20.51
                                           <2e-16 ***
## (Intercept)
## lunch_type
                12.926
                            1.288
                                    10.03
                                           <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.9 on 585 degrees of freedom
## Multiple R-squared: 0.1468, Adjusted R-squared: 0.1454
## F-statistic: 100.7 on 1 and 585 DF, p-value: < 2.2e-16
```

```
## Call:
## lm(formula = math_score ~ parent_marital_status, data = step_df)
## Residuals:
               1Q Median
                               3Q
                                      Max
## -67.017 -10.235 -0.017 11.374 33.765
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         65.8442
                                     2.1578 30.514
                                                      <2e-16 ***
## parent_marital_status
                         0.3911
                                     0.9647
                                              0.405
                                                       0.685
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 16.13 on 585 degrees of freedom
## Multiple R-squared: 0.0002809, Adjusted R-squared: -0.001428
## F-statistic: 0.1644 on 1 and 585 DF, p-value: 0.6853
##
## Call:
## lm(formula = math_score ~ practice_sport, data = step_df)
## Residuals:
               1Q Median
                               3Q
## -66.873 -10.344
                    0.127 11.391 33.391
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
                  66.0793
                              2.4052 27.473
                                               <2e-16 ***
## (Intercept)
                   0.2647
                              1.0247
                                       0.258
                                                0.796
## practice_sport
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 16.13 on 585 degrees of freedom
## Multiple R-squared: 0.000114, Adjusted R-squared: -0.001595
## F-statistic: 0.06671 on 1 and 585 DF, p-value: 0.7963
##
## Call:
## lm(formula = math_score ~ is_first_child, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
## -67.008 -10.008 -0.008 11.005 34.005
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
                   64.982
                               2.464 26.371
                                               <2e-16 ***
## (Intercept)
                    1.013
                               1.418
                                      0.714
                                                0.475
## is_first_child
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 16.12 on 585 degrees of freedom
## Multiple R-squared: 0.000871, Adjusted R-squared: -0.0008369
```

```
## F-statistic: 0.51 on 1 and 585 DF, p-value: 0.4754
##
## Call:
## lm(formula = math_score ~ nr_siblings, data = step_df)
## Residuals:
      Min
               1Q Median
                               3Q
## -67.271 -10.234
                   0.112 11.037
                                   33.803
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
                           1.1675 55.841
## (Intercept) 65.1969
                                            <2e-16 ***
## nr_siblings 0.6914
                           0.4487
                                    1.541
                                             0.124
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 16.09 on 585 degrees of freedom
## Multiple R-squared: 0.004042,
                                  Adjusted R-squared: 0.00234
## F-statistic: 2.374 on 1 and 585 DF, p-value: 0.1239
##
## Call:
## lm(formula = math_score ~ transport_means, data = step_df)
## Residuals:
##
      Min
               10 Median
                               3Q
                                      Max
## -66.696 -10.646
                    0.304 11.304 33.354
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
                  66.59705
                              2.29558 29.011
                                                <2e-16 ***
## (Intercept)
                                                 0.971
## transport means 0.04924
                              1.36467
                                       0.036
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 16.13 on 585 degrees of freedom
## Multiple R-squared: 2.226e-06, Adjusted R-squared: -0.001707
## F-statistic: 0.001302 on 1 and 585 DF, p-value: 0.9712
##
## Call:
## lm(formula = math_score ~ wkly_study_hours, data = step_df)
## Residuals:
      Min
               10 Median
                               3Q
                                      Max
## -69.545 -9.902
                    0.098 11.598 33.742
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                     61.614
                                2.038 30.236 < 2e-16 ***
## wkly_study_hours
                      2.644
                                 1.007
                                         2.627 0.00885 **
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 16.03 on 585 degrees of freedom
## Multiple R-squared: 0.01166, Adjusted R-squared: 0.009966
## F-statistic: 6.899 on 1 and 585 DF, p-value: 0.008851
##
## Call:
## lm(formula = math_score ~ test_prep, data = step_df)
## Residuals:
      Min
               1Q Median
                               30
                                      Max
## -64.715 -9.715 -0.250 11.285 35.285
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                            2.353 32.214 < 2e-16 ***
## (Intercept)
                75.785
                -5.535
                            1.373 -4.032 6.26e-05 ***
## test_prep
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 15.91 on 585 degrees of freedom
## Multiple R-squared: 0.02704,
                                  Adjusted R-squared: 0.02538
## F-statistic: 16.26 on 1 and 585 DF, p-value: 6.26e-05
##
## Call:
## lm(formula = math_score ~ lunch_type + gender, data = step_df)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -56.033 -10.487   0.692   10.335   38.692
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                38.127
                            2.744 13.894 < 2e-16 ***
                12.632
                            1.271
                                   9.939 < 2e-16 ***
## lunch_type
                 5.274
                            1.216
                                  4.336 1.71e-05 ***
## gender
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.67 on 584 degrees of freedom
## Multiple R-squared: 0.1734, Adjusted R-squared: 0.1706
## F-statistic: 61.27 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
## -57.960 -9.607
                   0.552 10.353 36.199
##
```

```
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
                            2.6533 13.776 < 2e-16 ***
## (Intercept)
                36.5522
                            1.2560 10.069 < 2e-16 ***
## lunch_type
                12.6467
## ethnic_group
                 2.9205
                            0.5134
                                    5.688 2.03e-08 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14.51 on 584 degrees of freedom
## Multiple R-squared: 0.1916, Adjusted R-squared: 0.1888
## F-statistic: 69.22 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + parent_educ, data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -55.223 -10.409
                   0.879 10.845
                                  41.828
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 40.7657
                           2.5292 16.118 < 2e-16 ***
## lunch_type
               12.9827
                           1.2752 10.181 < 2e-16 ***
## parent_educ
                1.4745
                           0.4066
                                    3.627 0.000312 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 14.74 on 584 degrees of freedom
## Multiple R-squared: 0.1656, Adjusted R-squared: 0.1628
## F-statistic: 57.96 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + parent_marital_status,
      data = step_df)
##
##
## Residuals:
      Min
               10 Median
                               30
                                      Max
## -58.875 -10.434
                   0.865 10.845 41.826
## Coefficients:
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                     2.9633 14.785
                         43.8110
                                                      <2e-16 ***
                         12.9612
                                     1.2895 10.052
                                                      <2e-16 ***
## lunch_type
## parent_marital_status
                         0.7009
                                     0.8920
                                              0.786
                                                       0.432
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 14.9 on 584 degrees of freedom
## Multiple R-squared: 0.1477, Adjusted R-squared: 0.1448
## F-statistic: 50.61 on 2 and 584 DF, p-value: < 2.2e-16
```

```
## Call:
## lm(formula = math_score ~ lunch_type + practice_sport, data = step_df)
## Residuals:
               1Q Median
                               3Q
                                      Max
## -58.678 -10.536  0.919  10.893  41.322
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  44.0952
                              3.1203 14.132
                                               <2e-16 ***
## lunch_type
                  12.9480
                              1.2896 10.041
                                               <2e-16 ***
                  0.5449
                              0.9475
                                      0.575
                                                0.565
## practice_sport
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 14.91 on 584 degrees of freedom
## Multiple R-squared: 0.1473, Adjusted R-squared: 0.1444
## F-statistic: 50.45 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + is_first_child, data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               ЗQ
                                      Max
## -58.571 -10.529
                   0.513 10.513 42.279
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                  43.9538
                              3.0975 14.190
                                               <2e-16 ***
                   12.9159
                              1.2890
                                     10.020
                                               <2e-16 ***
## lunch_type
## is_first_child
                  0.8508
                              1.3113
                                       0.649
                                                0.517
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 14.9 on 584 degrees of freedom
## Multiple R-squared: 0.1474, Adjusted R-squared: 0.1445
## F-statistic: 50.5 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + nr_siblings, data = step_df)
##
## Residuals:
                1Q Median
                               3Q
                                      Max
## -58.877 -10.432
                    0.756 10.529
                                  41.123
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                                            <2e-16 ***
## (Intercept) 43.9040
                           2.3785 18.459
## lunch_type
               12.9222
                           1.2864 10.045
                                            <2e-16 ***
## nr_siblings 0.6836
                           0.4147
                                   1.648
                                            0.0998 .
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

```
##
## Residual standard error: 14.87 on 584 degrees of freedom
## Multiple R-squared: 0.1508, Adjusted R-squared: 0.1479
## F-statistic: 51.84 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + transport_means, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -58.246 -10.246
                   0.754 10.827 41.652
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   45.5226
                               2.9870 15.240
                                                <2e-16 ***
## lunch_type
                   12.9274
                               1.2895 10.025
                                                <2e-16 ***
                               1.2617 -0.081
                                                 0.936
## transport_means -0.1021
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.91 on 584 degrees of freedom
## Multiple R-squared: 0.1468, Adjusted R-squared: 0.1439
## F-statistic: 50.26 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + wkly_study_hours, data = step_df)
##
## Residuals:
      Min
                1Q Median
                               3Q
                                      Max
## -61.136 -10.433
                   0.947 10.485 41.485
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
                                2.8257 14.282 < 2e-16 ***
## (Intercept)
                    40.3568
## lunch_type
                    12.9173
                                1.2807 10.086 < 2e-16 ***
                                0.9297
                                         2.819 0.00498 **
## wkly_study_hours
                     2.6206
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.81 on 584 degrees of freedom
## Multiple R-squared: 0.1583, Adjusted R-squared: 0.1554
## F-statistic: 54.91 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + test_prep, data = step_df)
## Residuals:
##
      Min
                1Q Median
                               3Q
## -56.071 -10.175
                    0.899 10.377 38.003
##
```

```
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                54.819
                            2.965
                                    18.49 < 2e-16 ***
                            1.266
                                    10.35 < 2e-16 ***
                13.104
## lunch_type
## test_prep
                -5.926
                            1.264
                                    -4.69 3.41e-06 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.64 on 584 degrees of freedom
## Multiple R-squared: 0.1778, Adjusted R-squared: 0.175
## F-statistic: 63.14 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -57.960 -9.607 0.552 10.353 36.199
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                            2.6533 13.776 < 2e-16 ***
## (Intercept)
                36.5522
                            1.2560 10.069 < 2e-16 ***
                12.6467
## lunch_type
                 2.9205
                            0.5134
                                    5.688 2.03e-08 ***
## ethnic_group
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14.51 on 584 degrees of freedom
## Multiple R-squared: 0.1916, Adjusted R-squared: 0.1888
## F-statistic: 69.22 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + gender,
##
      data = step_df)
##
## Residuals:
               10 Median
                               3Q
      Min
## -55.717 -9.148
                            9.845 34.370
                   0.015
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                                   9.556 < 2e-16 ***
                29.3670
                            3.0731
## (Intercept)
                                   9.978 < 2e-16 ***
                12.3544
                            1.2382
## lunch_type
## ethnic_group
                2.9138
                            0.5054
                                   5.765 1.32e-08 ***
## gender
                 5.2540
                            1.1842 4.437 1.09e-05 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.29 on 583 degrees of freedom
## Multiple R-squared: 0.218, Adjusted R-squared: 0.214
## F-statistic: 54.18 on 3 and 583 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + parent_educ,
       data = step_df)
##
## Residuals:
      Min
               10 Median
                               30
                                      Max
## -55.234 -9.790
                   0.258 10.355 36.529
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
                            2.8632 11.458 < 2e-16 ***
                32.8065
## (Intercept)
## lunch_type
                            1.2456 10.203 < 2e-16 ***
                 12,7088
## ethnic_group
                                    5.486 6.14e-08 ***
                 2.7998
                            0.5104
                 1.3189
## parent_educ
                            0.3978
                                    3.315 0.000972 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.39 on 583 degrees of freedom
## Multiple R-squared: 0.2066, Adjusted R-squared: 0.2025
## F-statistic: 50.6 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + parent_marital_status,
##
       data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -58.657 -9.579
                    0.554 10.482 36.308
##
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          34.6762
                                     3.2998 10.509 < 2e-16 ***
## lunch_type
                         12.6870
                                     1.2568 10.094 < 2e-16 ***
## ethnic_group
                          2.9334
                                     0.5136
                                              5.711 1.79e-08 ***
## parent_marital_status
                          0.8312
                                     0.8691
                                              0.956
                                                       0.339
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.51 on 583 degrees of freedom
## Multiple R-squared: 0.1929, Adjusted R-squared: 0.1887
## F-statistic: 46.44 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + practice_sport,
##
      data = step_df)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -58.356 -9.474 0.605 10.400 35.802
## Coefficients:
```

```
Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                              3.4130 10.334 < 2e-16 ***
                  35.2709
## lunch_type
                  12.6688
                              1.2573 10.076 < 2e-16 ***
                   2.9209
                              0.5137
                                       5.686 2.06e-08 ***
## ethnic_group
## practice_sport
                   0.5514
                              0.9231
                                       0.597
                                                0.551
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.52 on 583 degrees of freedom
## Multiple R-squared: 0.1921, Adjusted R-squared: 0.188
## F-statistic: 46.21 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + is_first_child,
      data = step_df)
##
## Residuals:
      Min
               1Q Median
                               30
                                      Max
## -58.244 -9.840
                   0.756 10.162 36.762
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                 35.1542
                              3.3914 10.366 < 2e-16 ***
                  12.6365
                              1.2567 10.055 < 2e-16 ***
## lunch_type
## ethnic_group
                   2.9203
                              0.5137
                                       5.685 2.07e-08 ***
## is_first_child
                  0.8461
                              1.2775
                                       0.662
                                                0.508
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.52 on 583 degrees of freedom
## Multiple R-squared: 0.1922, Adjusted R-squared: 0.1881
## F-statistic: 46.25 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + nr_siblings,
      data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -58.600 -9.548
                   0.345 10.095 35.510
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                34.8937
                            2.7968 12.476 < 2e-16 ***
## (Intercept)
                12.6400
                            1.2535
                                   10.084 < 2e-16 ***
## lunch_type
## ethnic_group
                                    5.746 1.47e-08 ***
                 2.9450
                            0.5125
                                    1.842
                                              0.066 .
## nr_siblings
                 0.7439
                            0.4039
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.48 on 583 degrees of freedom
## Multiple R-squared: 0.1963, Adjusted R-squared: 0.1922
```

```
## F-statistic: 47.46 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + transport_means,
       data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -58.006 -9.633
                    0.620 10.310 36.265
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
                   36.3653
                               3.3263 10.933 < 2e-16 ***
## (Intercept)
## lunch type
                   12.6452
                               1.2572 10.058 < 2e-16 ***
## ethnic_group
                    2.9220
                               0.5141
                                       5.684 2.08e-08 ***
## transport_means
                    0.1147
                               1.2297
                                       0.093
                                                 0.926
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 14.52 on 583 degrees of freedom
## Multiple R-squared: 0.1916, Adjusted R-squared: 0.1875
## F-statistic: 46.07 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + wkly_study_hours,
       data = step_df)
##
## Residuals:
      Min
                1Q Median
                               3Q
                                      Max
## -60.754 -9.175
                    0.814
                            9.769 36.003
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
                                3.1451 10.078 < 2e-16 ***
## (Intercept)
                    31.6953
## lunch_type
                    12.6394
                                1.2485 10.123 < 2e-16 ***
                     2.9056
                                0.5104
                                        5.693 1.98e-08 ***
## ethnic_group
                     2.5674
                                0.9057
                                         2.835 0.00474 **
## wkly_study_hours
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.43 on 583 degrees of freedom
## Multiple R-squared: 0.2026, Adjusted R-squared: 0.1985
## F-statistic: 49.38 on 3 and 583 DF, p-value: < 2.2e-16
##
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep,
##
       data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
```

```
## -55.800 -9.572 1.075 10.329 32.657
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                45.9342
                            3.2818 13.997 < 2e-16 ***
                            1.2345 10.389 < 2e-16 ***
## lunch type
                12.8245
                                    5.700 1.91e-08 ***
## ethnic_group
                2.8753
                            0.5044
                            1.2310 -4.705 3.17e-06 ***
## test_prep
                -5.7920
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.26 on 583 degrees of freedom
## Multiple R-squared: 0.2212, Adjusted R-squared: 0.2172
## F-statistic: 55.19 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep,
##
      data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               30
## -55.800 -9.572
                   1.075 10.329 32.657
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                            3.2818 13.997 < 2e-16 ***
## (Intercept)
                45.9342
## lunch_type
                12.8245
                            1.2345 10.389 < 2e-16 ***
                            0.5044
                                    5.700 1.91e-08 ***
## ethnic_group
                 2.8753
                -5.7920
                            1.2310 -4.705 3.17e-06 ***
## test_prep
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.26 on 583 degrees of freedom
## Multiple R-squared: 0.2212, Adjusted R-squared: 0.2172
## F-statistic: 55.19 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
##
      gender, data = step_df)
##
## Residuals:
##
      Min
               10 Median
                               3Q
                                      Max
## -53.734 -10.013
                   0.383
                            9.970 32.599
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                 38.700
                             3.642 10.627 < 2e-16 ***
                             1.218 10.294 < 2e-16 ***
## lunch_type
                 12.538
## ethnic_group
                  2.870
                             0.497
                                     5.776 1.25e-08 ***
## test_prep
                 -5.573
                             1.214 -4.591 5.40e-06 ***
## gender
                  5.031
                             1.165
                                    4.317 1.86e-05 ***
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14.05 on 582 degrees of freedom
## Multiple R-squared: 0.2454, Adjusted R-squared: 0.2402
## F-statistic: 47.31 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
      parent_educ, data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
## -52.947 -9.121
                   1.049 10.283 32.938
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                42.2241
                            3.4203 12.345 < 2e-16 ***
## (Intercept)
                12.8917
                            1.2230 10.541 < 2e-16 ***
## lunch_type
## ethnic_group
                 2.7498
                            0.5010
                                    5.489 6.04e-08 ***
                -5.8907
                            1.2197 -4.830 1.75e-06 ***
## test_prep
## parent_educ
                 1.3626
                            0.3905
                                   3.489 0.000521 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.12 on 582 degrees of freedom
## Multiple R-squared: 0.2371, Adjusted R-squared: 0.2319
## F-statistic: 45.23 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
##
      parent marital status, data = step df)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -56.400 -9.670
                   1.073 10.241 32.769
##
## Coefficients:
                        Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                         44.2993
                                     3.8406 11.534 < 2e-16 ***
## lunch_type
                         12.8575
                                     1.2355 10.407 < 2e-16 ***
## ethnic_group
                         2.8864
                                     0.5048
                                             5.718 1.72e-08 ***
                         -5.7590
                                     1.2320 -4.674 3.67e-06 ***
## test_prep
## parent_marital_status
                         0.7007
                                     0.8544
                                             0.820
                                                       0.413
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.26 on 582 degrees of freedom
## Multiple R-squared: 0.2221, Adjusted R-squared: 0.2167
## F-statistic: 41.54 on 4 and 582 DF, p-value: < 2.2e-16
```

```
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
      practice_sport, data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -56.155 -9.277 1.001 10.183 32.311
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  44.7832
                              3.9179 11.430 < 2e-16 ***
                  12.8438
                              1.2358 10.393 < 2e-16 ***
## lunch_type
                              0.5048
## ethnic_group
                   2.8757
                                      5.697 1.94e-08 ***
                  -5.7822
                              1.2319 -4.694 3.35e-06 ***
## test_prep
## practice_sport
                  0.4885
                              0.9070
                                      0.539
                                                 0.59
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.27 on 582 degrees of freedom
## Multiple R-squared: 0.2216, Adjusted R-squared: 0.2162
## F-statistic: 41.42 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
##
      is_first_child, data = step_df)
##
## Residuals:
##
     Min
             1Q Median
                           3Q
                                 Max
## -55.99 -9.71
                 1.07 10.31 33.03
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                  45.0129
                              3.9442 11.412 < 2e-16 ***
                              1.2355 10.374 < 2e-16 ***
## lunch_type
                  12.8173
## ethnic_group
                   2.8753
                              0.5048
                                      5.696 1.95e-08 ***
                              1.2337 -4.672 3.70e-06 ***
## test_prep
                  -5.7640
## is_first_child 0.5302
                              1.2571
                                      0.422
                                                0.673
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.27 on 582 degrees of freedom
## Multiple R-squared: 0.2214, Adjusted R-squared: 0.2161
## F-statistic: 41.38 on 4 and 582 DF, p-value: < 2.2e-16
##
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
      nr_siblings, data = step_df)
##
## Residuals:
      Min
               1Q Median
                               3Q
## -56.400 -9.375 1.049 10.075 32.111
##
```

```
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
                            3.4213 12.953 < 2e-16 ***
## (Intercept)
                44.3155
                            1.2327 10.396 < 2e-16 ***
## lunch_type
                12.8156
## ethnic_group
                 2.8976
                            0.5039
                                    5.750 1.44e-08 ***
                -5.6936
                            1.2307 -4.626 4.59e-06 ***
## test prep
## nr siblings
                 0.6545
                                    1.647
                            0.3975
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.24 on 582 degrees of freedom
## Multiple R-squared: 0.2248, Adjusted R-squared: 0.2195
## F-statistic: 42.19 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
       transport_means, data = step_df)
##
## Residuals:
      Min
               1Q Median
                               30
                                      Max
## -55.993 -9.355
                   0.889 10.216 32.935
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                   45.1465
                               3.7597 12.008 < 2e-16 ***
                               1.2354 10.376 < 2e-16 ***
## lunch_type
                   12.8187
## ethnic_group
                    2.8817
                               0.5050
                                       5.706 1.84e-08 ***
                   -5.8298
                               1.2350 -4.720 2.95e-06 ***
## test_prep
                    0.5211
                               1.2110
                                       0.430
                                                 0.667
## transport_means
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14.27 on 582 degrees of freedom
## Multiple R-squared: 0.2214, Adjusted R-squared: 0.2161
## F-statistic: 41.38 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
##
       wkly_study_hours, data = step_df)
##
## Residuals:
##
      Min
               10 Median
                               3Q
                                      Max
## -58.284 -9.309
                    0.857
                            9.743 32.666
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                    41.3369
                                3.7728 10.957 < 2e-16 ***
                                1.2293 10.420 < 2e-16 ***
## lunch_type
                    12.8095
## ethnic_group
                     2.8648
                                0.5023
                                         5.703 1.88e-08 ***
## test_prep
                    -5.5040
                                1.2315 -4.469 9.44e-06 ***
## wkly_study_hours
                     2.1836
                                0.8954
                                         2.439
                                                  0.015 *
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14.2 on 582 degrees of freedom
## Multiple R-squared: 0.2291, Adjusted R-squared: 0.2238
## F-statistic: 43.23 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
       gender, data = step_df)
##
## Residuals:
##
      Min
                1Q Median
                               3Q
                                      Max
## -53.734 -10.013
                            9.970 32.599
                    0.383
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                 38.700
                             3.642 10.627 < 2e-16 ***
## (Intercept)
## lunch_type
                 12.538
                             1.218 10.294 < 2e-16 ***
                  2.870
                             0.497
                                     5.776 1.25e-08 ***
## ethnic_group
## test_prep
                 -5.573
                             1.214 -4.591 5.40e-06 ***
                  5.031
                                    4.317 1.86e-05 ***
## gender
                             1.165
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.05 on 582 degrees of freedom
## Multiple R-squared: 0.2454, Adjusted R-squared: 0.2402
## F-statistic: 47.31 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
##
       gender + parent_educ, data = step_df)
##
## Residuals:
##
      Min
                1Q Median
                               3Q
                                      Max
## -50.514 -9.535
                    0.837 10.037
                                  30.067
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                34.2503
                            3.7807
                                     9.059 < 2e-16 ***
## lunch_type
                12.5942
                            1.2039 10.461 < 2e-16 ***
## ethnic_group
                 2.7340
                            0.4925
                                     5.552 4.31e-08 ***
                            1.2000 -4.723 2.92e-06 ***
## test_prep
                -5.6676
## gender
                 5.3234
                            1.1542
                                     4.612 4.91e-06 ***
## parent_educ
                 1.4796
                            0.3847
                                     3.846 0.000133 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 13.88 on 581 degrees of freedom
## Multiple R-squared: 0.2641, Adjusted R-squared: 0.2578
## F-statistic: 41.7 on 5 and 581 DF, p-value: < 2.2e-16
```

##

```
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
       gender + parent_marital_status, data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -54.421 -9.827
                   0.520 10.165 32.709
##
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         36.7294
                                     4.1646
                                             8.820 < 2e-16 ***
                                     1.2187 10.318 < 2e-16 ***
                         12.5744
## lunch_type
## ethnic_group
                          2.8835
                                     0.4972
                                              5.800 1.09e-08 ***
## test_prep
                         -5.5329
                                     1.2146 -4.555 6.38e-06 ***
                          5.0681
                                     1.1660
                                              4.347 1.63e-05 ***
## gender
## parent_marital_status
                          0.8215
                                     0.8420
                                              0.976
                                                        0.33
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.05 on 581 degrees of freedom
## Multiple R-squared: 0.2466, Adjusted R-squared: 0.2401
## F-statistic: 38.03 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
       gender + practice_sport, data = step_df)
##
## Residuals:
      Min
               10 Median
                               3Q
                                      Max
## -54.066 -9.907 0.260 10.048 32.249
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  37.6369
                            4.2012 8.959 < 2e-16 ***
## lunch_type
                  12.5562
                              1.2193 10.298 < 2e-16 ***
                              0.4973
                                       5.773 1.27e-08 ***
## ethnic_group
                   2.8709
                   -5.5643
                              1.2148 -4.581 5.68e-06 ***
## test_prep
## gender
                   5.0253
                              1.1661
                                      4.310 1.92e-05 ***
                              0.8936 0.509
## practice_sport 0.4544
                                                0.611
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.06 on 581 degrees of freedom
## Multiple R-squared: 0.2457, Adjusted R-squared: 0.2392
## F-statistic: 37.85 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
       gender + is_first_child, data = step_df)
##
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
```

```
## -53.902 -9.853 0.541 10.069 32.437
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                  37.8925
                              4.2227
                                      8.973 < 2e-16 ***
                  12.5318
                              1.2190 10.280 < 2e-16 ***
## lunch_type
                                      5.772 1.28e-08 ***
## ethnic_group
                  2.8706
                              0.4974
## test_prep
                  -5.5487
                              1.2165 -4.561 6.21e-06 ***
## gender
                   5.0255
                              1.1662
                                       4.309 1.92e-05 ***
## is_first_child
                  0.4690
                              1.2386
                                       0.379
                                                0.705
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.06 on 581 degrees of freedom
## Multiple R-squared: 0.2455, Adjusted R-squared: 0.239
## F-statistic: 37.82 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
      gender + nr_siblings, data = step_df)
##
##
## Residuals:
##
      Min
               1Q Median
                               30
                                      Max
                   0.056 10.049 34.165
## -54.359 -9.453
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                36.8121
                            3.7775
                                    9.745 < 2e-16 ***
## (Intercept)
                12.5237
                            1.2156 10.303 < 2e-16 ***
## lunch_type
## ethnic_group 2.8949
                            0.4962
                                    5.835 8.96e-09 ***
## test_prep
                -5.4619
                            1.2129 -4.503 8.10e-06 ***
## gender
                 5.1091
                            1.1637
                                    4.390 1.35e-05 ***
## nr_siblings
                 0.7178
                            0.3917
                                    1.833 0.0674 .
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14.02 on 581 degrees of freedom
## Multiple R-squared: 0.2497, Adjusted R-squared: 0.2432
## F-statistic: 38.67 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
##
      gender + transport_means, data = step_df)
##
## Residuals:
##
               10 Median
                               3Q
      Min
                                      Max
## -53.896 -10.039
                    0.299
                            9.852 32.878
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   38.0574
                               4.0535
                                       9.389 < 2e-16 ***
                               1.2190 10.282 < 2e-16 ***
## lunch_type
                   12.5335
```

```
2.8759
                               0.4976
                                       5.780 1.22e-08 ***
## ethnic_group
                               1.2179 -4.602 5.14e-06 ***
## test_prep
                   -5.6049
                               1.1663
## gender
                    5.0233
                                        4.307 1.94e-05 ***
## transport_means
                    0.4322
                               1.1933
                                        0.362
                                                 0.717
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.06 on 581 degrees of freedom
## Multiple R-squared: 0.2455, Adjusted R-squared: 0.239
## F-statistic: 37.81 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
##
       gender + wkly_study_hours, data = step_df)
##
## Residuals:
##
      Min
                1Q Median
                               3Q
                                      Max
## -56.095 -9.508
                    0.175 10.116 34.314
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    34.5555
                                4.0481
                                         8.536 < 2e-16 ***
## lunch_type
                    12.5298
                                1.2135 10.325 < 2e-16 ***
                     2.8609
                                0.4952
                                         5.778 1.24e-08 ***
## ethnic_group
## test_prep
                    -5.3087
                                1.2148
                                        -4.370 1.47e-05 ***
                     4.9272
                                1.1618
                                         4.241 2.59e-05 ***
## gender
## wkly_study_hours
                     2.0392
                                0.8833
                                         2.309
                                                0.0213 *
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.99 on 581 degrees of freedom
## Multiple R-squared: 0.2522, Adjusted R-squared: 0.2458
## F-statistic: 39.19 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
       gender + parent_educ, data = step_df)
##
##
## Residuals:
      Min
               10 Median
                               3Q
                                      Max
## -50.514 -9.535
                    0.837 10.037
                                   30.067
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                34.2503
                            3.7807
                                    9.059 < 2e-16 ***
                            1.2039 10.461 < 2e-16 ***
## lunch_type
                12.5942
                                     5.552 4.31e-08 ***
## ethnic_group
                 2.7340
                            0.4925
                            1.2000 -4.723 2.92e-06 ***
## test_prep
                -5.6676
## gender
                 5.3234
                            1.1542
                                     4.612 4.91e-06 ***
## parent_educ
                 1.4796
                            0.3847
                                     3.846 0.000133 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 13.88 on 581 degrees of freedom
## Multiple R-squared: 0.2641, Adjusted R-squared: 0.2578
## F-statistic: 41.7 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
       gender + parent_educ + parent_marital_status, data = step_df)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -51.161 -9.524
                    0.562 10.079 30.168
##
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                          32.4681
                                      4.2647
                                              7.613 1.09e-13 ***
## lunch_type
                          12.6273
                                      1.2047 10.482 < 2e-16 ***
## ethnic_group
                          2.7467
                                      0.4928
                                              5.574 3.82e-08 ***
## test_prep
                          -5.6302
                                      1.2009 -4.688 3.44e-06 ***
                          5.3563
                                               4.637 4.36e-06 ***
## gender
                                      1.1550
## parent educ
                           1.4721
                                      0.3849
                                               3.825 0.000145 ***
## parent_marital_status
                           0.7524
                                      0.8325
                                               0.904 0.366512
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.88 on 580 degrees of freedom
## Multiple R-squared: 0.2651, Adjusted R-squared: 0.2575
## F-statistic: 34.88 on 6 and 580 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
       gender + parent_educ + practice_sport, data = step_df)
##
## Residuals:
      Min
##
                1Q Median
                                3Q
                                       Max
                   0.825
## -50.967 -9.382
                             9.975 29.595
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  32.6121
                              4.3479
                                       7.501 2.40e-13 ***
                               1.2049 10.475 < 2e-16 ***
## lunch_type
                   12.6220
                   2.7329
                               0.4927
                                        5.547 4.42e-08 ***
## ethnic_group
## test_prep
                   -5.6556
                               1.2005
                                      -4.711 3.09e-06 ***
                   5.3193
                               1.1547
                                        4.607 5.03e-06 ***
## gender
## parent_educ
                   1.4986
                               0.3857
                                        3.886 0.000114 ***
## practice_sport
                   0.6758
                               0.8848
                                        0.764 0.445283
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.89 on 580 degrees of freedom
## Multiple R-squared: 0.2648, Adjusted R-squared: 0.2572
## F-statistic: 34.82 on 6 and 580 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
       gender + parent_educ + is_first_child, data = step_df)
##
## Residuals:
      Min
               10 Median
                               30
                                      Max
## -50.673 -9.645
                    0.774
                            9.999 30.373
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  33.5052
                              4.3272
                                       7.743 4.35e-14 ***
                  12.5885
                              1.2050 10.447 < 2e-16 ***
## lunch_type
## ethnic_group
                   2.7342
                              0.4929
                                       5.548 4.41e-08 ***
                              1.2026 -4.694 3.35e-06 ***
## test_prep
                   -5.6448
## gender
                   5.3185
                              1.1552
                                        4.604 5.10e-06 ***
                   1.4786
                               0.3850
                                        3.840 0.000136 ***
## parent_educ
## is_first_child
                   0.4345
                               1.2242
                                       0.355 0.722808
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.89 on 580 degrees of freedom
## Multiple R-squared: 0.2643, Adjusted R-squared: 0.2566
## F-statistic: 34.72 on 6 and 580 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
       gender + parent_educ + nr_siblings, data = step_df)
##
##
## Residuals:
      Min
               10 Median
                                3Q
                                      Max
## -51.136 -9.280
                    0.816 10.107 31.298
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                            3.9112
                                    8.253 1.05e-15 ***
## (Intercept)
                32.2786
                12.5799
                            1.2012 10.472 < 2e-16 ***
## lunch_type
## ethnic group
                2.7582
                            0.4915
                                    5.611 3.11e-08 ***
                -5.5537
                            1.1988 -4.633 4.46e-06 ***
## test_prep
## gender
                 5.4060
                             1.1524
                                     4.691 3.39e-06 ***
## parent_educ
                 1.4896
                            0.3839
                                     3.880 0.000116 ***
## nr_siblings
                 0.7382
                             0.3871
                                     1.907 0.056968 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.85 on 580 degrees of freedom
## Multiple R-squared: 0.2687, Adjusted R-squared: 0.2611
## F-statistic: 35.51 on 6 and 580 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
##
       gender + parent_educ + transport_means, data = step_df)
```

```
##
## Residuals:
                1Q Median
      Min
                                30
## -50.661 -9.669
                    0.663
                            9.877
                                   30.273
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
                                4.1648
                                       8.089 3.53e-15 ***
## (Intercept)
                    33.6893
## lunch_type
                    12.5902
                                1.2049 10.449 < 2e-16 ***
## ethnic_group
                    2.7389
                                0.4931
                                        5.555 4.25e-08 ***
## test_prep
                    -5.6954
                                1.2040
                                       -4.730 2.82e-06 ***
                     5.3167
                                       4.602 5.15e-06 ***
## gender
                                1.1553
## parent_educ
                     1.4782
                                0.3850
                                        3.839 0.000137 ***
## transport_means
                     0.3801
                                1.1795
                                       0.322 0.747350
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 13.89 on 580 degrees of freedom
## Multiple R-squared: 0.2642, Adjusted R-squared: 0.2566
## F-statistic: 34.71 on 6 and 580 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
       gender + parent_educ + wkly_study_hours, data = step_df)
##
## Residuals:
      Min
                10 Median
                                3Q
                                       Max
## -52.943 -9.439
                     0.630 10.403 31.459
##
## Coefficients:
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                     29.7605
                                 4.1787
                                         7.122 3.16e-12 ***
                     12.5868
                                 1.1987 10.501 < 2e-16 ***
## lunch_type
## ethnic_group
                     2.7208
                                 0.4904
                                         5.549 4.39e-08 ***
## test_prep
                     -5.3895
                                 1.2000 -4.491 8.55e-06 ***
                                          4.540 6.85e-06 ***
## gender
                     5.2204
                                 1.1499
## parent_educ
                     1.5128
                                 0.3833
                                          3.947 8.88e-05 ***
## wkly_study_hours
                     2.1599
                                 0.8729
                                          2.474
                                                  0.0136 *
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.82 on 580 degrees of freedom
## Multiple R-squared: 0.2718, Adjusted R-squared: 0.2642
## F-statistic: 36.08 on 6 and 580 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
##
       gender + parent_educ + wkly_study_hours, data = step_df)
##
## Residuals:
      Min
                1Q Median
                                3Q
## -52.943 -9.439
                    0.630 10.403 31.459
```

```
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
                                 4.1787
                                         7.122 3.16e-12 ***
## (Intercept)
                     29.7605
## lunch_type
                     12.5868
                                 1.1987 10.501 < 2e-16 ***
                     2.7208
                                 0.4904
                                         5.549 4.39e-08 ***
## ethnic_group
## test_prep
                     -5.3895
                                1.2000 -4.491 8.55e-06 ***
                                          4.540 6.85e-06 ***
## gender
                     5.2204
                                 1.1499
## parent_educ
                     1.5128
                                 0.3833
                                          3.947 8.88e-05 ***
                                 0.8729
## wkly_study_hours
                     2.1599
                                          2.474 0.0136 *
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.82 on 580 degrees of freedom
## Multiple R-squared: 0.2718, Adjusted R-squared: 0.2642
## F-statistic: 36.08 on 6 and 580 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
       gender + parent educ + wkly study hours + parent marital status,
##
##
       data = step df)
##
## Residuals:
##
                1Q Median
                                3Q
      Min
                                       Max
                    0.583 10.152 31.582
## -53.608 -9.405
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          27.9334
                                      4.6228
                                              6.043 2.72e-09 ***
                                      1.1994 10.523 < 2e-16 ***
                         12.6206
## lunch_type
## ethnic_group
                          2.7336
                                      0.4906
                                              5.572 3.87e-08 ***
## test_prep
                          -5.3507
                                      1.2009
                                             -4.456 1.00e-05 ***
## gender
                          5.2537
                                      1.1506
                                               4.566 6.08e-06 ***
                                               3.926 9.68e-05 ***
## parent_educ
                           1.5052
                                     0.3834
## wkly_study_hours
                           2.1654
                                      0.8731
                                               2.480
                                                       0.0134 *
                                      0.8289
                                               0.925
                                                       0.3555
## parent_marital_status
                           0.7665
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.82 on 579 degrees of freedom
## Multiple R-squared: 0.2729, Adjusted R-squared: 0.2641
## F-statistic: 31.04 on 7 and 579 DF, p-value: < 2.2e-16
##
## Call:
  lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
##
       gender + parent_educ + wkly_study_hours + practice_sport,
##
       data = step_df)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -53.363 -9.358
                    0.643 10.342 30.921
##
```

```
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                    28.2228
                                4.6818
                                        6.028 2.95e-09 ***
                    12.6133
                                 1.1997 10.514 < 2e-16 ***
## lunch_type
## ethnic_group
                     2.7197
                                0.4906
                                         5.544 4.49e-08 ***
                                1.2006 -4.481 8.97e-06 ***
## test_prep
                    -5.3794
## gender
                                         4.535 7.01e-06 ***
                     5.2170
                                1.1504
                                         3.984 7.64e-05 ***
                                0.3842
## parent educ
                     1.5307
## wkly_study_hours
                     2.1502
                                0.8734
                                         2.462
                                                 0.0141 *
## practice_sport
                     0.6427
                                0.8811
                                         0.729
                                                 0.4660
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.83 on 579 degrees of freedom
## Multiple R-squared: 0.2724, Adjusted R-squared: 0.2636
## F-statistic: 30.97 on 7 and 579 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
       gender + parent educ + wkly study hours + is first child,
##
##
       data = step df)
##
## Residuals:
##
                1Q Median
                                3Q
      Min
                                      Max
                    0.708 10.528 31.314
## -53.096 -9.567
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    29.0370
                                4.6723
                                         6.215 9.84e-10 ***
                                 1.1997 10.487 < 2e-16 ***
## lunch_type
                    12.5812
                                0.4907
## ethnic_group
                     2.7209
                                         5.545 4.48e-08 ***
## test_prep
                    -5.3675
                                1.2026 -4.463 9.71e-06 ***
## gender
                     5.2157
                                1.1509
                                         4.532 7.10e-06 ***
                                         3.941 9.09e-05 ***
## parent_educ
                     1.5119
                                0.3836
## wkly_study_hours
                     2.1588
                                0.8736
                                         2.471
                                                 0.0138 *
## is_first_child
                     0.4232
                                1.2189
                                         0.347
                                                 0.7286
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.83 on 579 degrees of freedom
## Multiple R-squared: 0.2719, Adjusted R-squared: 0.2631
## F-statistic: 30.89 on 7 and 579 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
##
       gender + parent_educ + wkly_study_hours + nr_siblings, data = step_df)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -53.440 -8.894 0.776 10.134 32.889
## Coefficients:
```

```
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                4.2756
                                        6.565 1.15e-10 ***
                    28.0713
## lunch_type
                    12.5737
                                1.1964 10.510 < 2e-16 ***
                     2.7439
                                0.4896
                                         5.605 3.23e-08 ***
## ethnic_group
## test_prep
                    -5.2926
                                1.1989 -4.414 1.21e-05 ***
                                1.1486
                                        4.616 4.83e-06 ***
## gender
                     5.3017
                                0.3826
                                         3.976 7.90e-05 ***
## parent educ
                     1.5210
                     2.0825
## wkly_study_hours
                                0.8723
                                         2.387
                                                 0.0173 *
## nr_siblings
                     0.6927
                                0.3860
                                         1.795
                                                 0.0732 .
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.8 on 579 degrees of freedom
## Multiple R-squared: 0.2758, Adjusted R-squared: 0.2671
## F-statistic: 31.5 on 7 and 579 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = math_score ~ lunch_type + ethnic_group + test_prep +
       gender + parent_educ + wkly_study_hours + transport_means,
##
       data = step df)
##
## Residuals:
                1Q Median
                               30
## -53.041 -9.471
                    0.579 10.519 31.633
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
                                4.5026
                                         6.523 1.50e-10 ***
## (Intercept)
                    29.3703
                                1.1997 10.489 < 2e-16 ***
## lunch_type
                    12.5840
                     2.7243
                                0.4910
                                        5.549 4.39e-08 ***
## ethnic_group
## test_prep
                    -5.4106
                                1.2044 -4.493 8.50e-06 ***
## gender
                     5.2159
                                1.1510
                                         4.531 7.12e-06 ***
## parent_educ
                     1.5117
                                0.3836
                                         3.941 9.12e-05 ***
## wkly_study_hours
                     2.1524
                                0.8742
                                         2.462 0.0141 *
## transport_means
                     0.2749
                                1.1752
                                         0.234
                                                 0.8151
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.83 on 579 degrees of freedom
## Multiple R-squared: 0.2718, Adjusted R-squared: 0.263
## F-statistic: 30.88 on 7 and 579 DF, p-value: < 2.2e-16
## Start: AIC=3264.33
## math_score ~ 1
##
                          Df Sum of Sq
                                          RSS
## + lunch_type
                               22340.6 129816 3173.1
                           1
## + ethnic_group
                                7803.7 144353 3235.4
                           1
                                5114.8 147042 3246.3
## + gender
                           1
## + test_prep
                           1
                                4114.3 148042 3250.2
## + parent_educ
                           1
                                2667.1 149489 3256.0
## + wkly_study_hours
                           1 1773.4 150383 3259.5
## + nr_siblings
                                615.0 151541 3264.0
                           1
```

```
## <none>
                                     152157 3264.3
## + is_first_child 1
                              132.5 152024 3265.8
## + parent marital status 1
                              42.7 152114 3266.2
## + practice_sport 1
                               17.3 152139 3266.3
## + transport means
                         1
                               0.3 152156 3266.3
##
## Step: AIC=3173.12
## math_score ~ lunch_type
##
                                               AIC
##
                                        RSS
                         Df Sum of Sq
## + ethnic_group
                              6815.3 123001 3143.5
                              4711.5 125104 3153.4
## + test_prep
                          1
                          1 4049.1 125767 3156.5
## + gender
                         1 2859.4 126956 3162.0
## + parent_educ
## + wkly_study_hours
                         1 1742.6 128073 3167.2
## + nr_siblings
                          1 601.2 129215 3172.4
## <none>
                                     129816 3173.1
                            137.1 129679 3174.5
## + parent_marital_status 1
                               93.5 129722 3174.7
## + is_first_child 1
## + practice sport
                          1
                               73.5 129742 3174.8
## + transport_means
                         1
                                1.5 129814 3175.1
## Step: AIC=3143.47
## math_score ~ lunch_type + ethnic_group
##
                         Df Sum of Sq
                                        RSS
## + test_prep
                              4499.7 118501 3123.6
                          1
                              4017.7 118983 3126.0
## + gender
                          1
                         1 2276.0 120725 3134.5
## + parent_educ
## + wkly_study_hours
                        1 1672.4 121328 3137.4
## + nr_siblings
                          1 711.4 122289 3142.1
## <none>
                                     123001 3143.5
                            192.7 122808 3144.6
## + parent_marital_status 1
                               92.5 122908 3145.0
## + is_first_child 1
                               75.2 122925 3145.1
## + practice sport
                          1
                          1
                                1.8 122999 3145.5
## + transport_means
##
## Step: AIC=3123.59
## math_score ~ lunch_type + ethnic_group + test_prep
##
##
                         Df Sum of Sq
                                        RSS
                              3676.9 114824 3107.1
## + gender
                          1
                              2428.1 116073 3113.4
## + parent_educ
                          1
## + wkly_study_hours
                         1 1198.6 117302 3119.6
                         1 549.5 117951 3122.9
## + nr_siblings
                                     118501 3123.6
## <none>
                             136.8 118364 3124.9
## + parent_marital_status 1
                              59.0 118442 3125.3
## + practice_sport 1
## + transport_means
                          1
                               37.7 118463 3125.4
## + is_first_child
                          1
                                36.2 118465 3125.4
##
## Step: AIC=3107.09
## math_score ~ lunch_type + ethnic_group + test_prep + gender
##
```

```
RSS
##
                           Df Sum of Sq
## + parent_educ
                                2850.64 111973 3094.3
## + wkly study hours
                                1043.73 113780 3103.7
## + nr_siblings
                                 659.98 114164 3105.7
## <none>
                                         114824 3107.1
## + parent marital status 1
                                 187.79 114636 3108.1
## + practice sport
                            1
                                  51.08 114773 3108.8
## + is first child
                            1
                                  28.33 114796 3108.9
## + transport means
                            1
                                   25.92 114798 3109.0
##
## Step: AIC=3094.33
## math_score ~ lunch_type + ethnic_group + test_prep + gender +
##
       parent_educ
##
##
                           Df Sum of Sq
                                            RSS
                                                   ATC
## + wkly_study_hours
                                1169.53 110804 3090.2
## + nr_siblings
                            1
                                 697.97 111275 3092.7
## <none>
                                         111973 3094.3
                                 157.45 111816 3095.5
## + parent_marital_status 1
## + practice sport
                            1
                                 112.52 111861 3095.7
## + is_first_child
                            1
                                  24.31 111949 3096.2
## + transport_means
                            1
                                   20.05 111953 3096.2
##
## Step: AIC=3090.17
## math_score ~ lunch_type + ethnic_group + test_prep + gender +
##
       parent_educ + wkly_study_hours
##
##
                           Df Sum of Sq
                                            RSS
## + nr_siblings
                                 613.00 110191 3088.9
## <none>
                                         110804 3090.2
## + parent_marital_status 1
                                  163.41 110640 3091.3
## + practice_sport
                            1
                                 101.74 110702 3091.6
## + is_first_child
                            1
                                  23.06 110781 3092.1
                                  10.47 110793 3092.1
## + transport_means
                            1
##
## Step: AIC=3088.91
## math_score ~ lunch_type + ethnic_group + test_prep + gender +
##
       parent_educ + wkly_study_hours + nr_siblings
##
##
                           Df Sum of Sq
                                            RSS
                                                   ATC
                                         110191 3088.9
## <none>
## + parent marital status 1
                                138.323 110053 3090.2
## + practice sport
                            1
                                 98.281 110093 3090.4
## + is_first_child
                            1
                                 48.607 110142 3090.7
## + transport_means
                            1
                                 10.595 110180 3090.9
```

The model we obtained is Math Score \sim Lunch Type + Ethnic Group + Test Prep + Gender + Parent Education + Weekly Study Hours.

When using the single-function method, the model obtained with the lowest AIC was Math Score \sim Lunch Type + Ethnic Group + Test Prep + Gender + Parent Education + Weekly Study Hours + Number of Siblings. This method resulted in a model that had a slightly lower MSE by a difference of about 1 point and approximately the same R-squared/Adjusted R-squared values.

Reading Score

```
##
## Call:
## lm(formula = reading_score ~ gender, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -56.152 -10.018 -0.152 10.915 33.982
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                80.286
                          1.888 42.521 < 2e-16 ***
                            1.221 -5.841 8.6e-09 ***
                -7.134
## gender
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.76 on 585 degrees of freedom
## Multiple R-squared: 0.05511,
                                   Adjusted R-squared: 0.05349
## F-statistic: 34.12 on 1 and 585 DF, p-value: 8.604e-09
##
## Call:
## lm(formula = reading_score ~ ethnic_group, data = step_df)
##
## Residuals:
##
               1Q Median
      Min
                               ЗQ
                                      Max
## -52.477 -10.415
                   0.398 10.523 34.773
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
                63.1022
                         1.7901 35.251 < 2e-16 ***
## (Intercept)
## ethnic_group 2.1251
                            0.5293 4.015 6.73e-05 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.97 on 585 degrees of freedom
## Multiple R-squared: 0.02681,
                                  Adjusted R-squared: 0.02515
## F-statistic: 16.12 on 1 and 585 DF, p-value: 6.732e-05
##
## Call:
## lm(formula = reading_score ~ parent_educ, data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -48.850 -10.691 0.363 10.756 34.150
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 63.9035
                           1.3965
                                  45.76 < 2e-16 ***
## parent_educ 1.9468
                           0.4107
                                     4.74 2.69e-06 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.9 on 585 degrees of freedom
```

```
## Multiple R-squared: 0.03698,
                                   Adjusted R-squared: 0.03534
## F-statistic: 22.47 on 1 and 585 DF, p-value: 2.688e-06
##
## Call:
## lm(formula = reading_score ~ lunch_type, data = step_df)
##
## Residuals:
      \mathtt{Min}
##
               1Q Median
                               3Q
                                      Max
## -47.558 -9.558 0.294 10.442 35.442
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 56.410
                            2.178 25.898 < 2e-16 ***
## lunch_type
                 8.148
                            1.269 6.422 2.79e-10 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.67 on 585 degrees of freedom
## Multiple R-squared: 0.06585,
                                   Adjusted R-squared: 0.06425
## F-statistic: 41.24 on 1 and 585 DF, p-value: 2.791e-10
##
## lm(formula = reading_score ~ parent_marital_status, data = step_df)
## Residuals:
      Min
               10 Median
                               30
                                      Max
## -53.351 -10.195  0.649  11.227  30.805
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
                                     2.0306 33.792 <2e-16 ***
## (Intercept)
                         68.6169
                         0.5780
                                     0.9078 0.637
## parent_marital_status
                                                       0.525
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 15.17 on 585 degrees of freedom
## Multiple R-squared: 0.0006925, Adjusted R-squared:
## F-statistic: 0.4054 on 1 and 585 DF, p-value: 0.5246
## Call:
## lm(formula = reading_score ~ practice_sport, data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -52.008 -10.135 0.739 10.992 30.992
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  72.3876
                              2.2614 32.011
                                               <2e-16 ***
## practice_sport -1.1265
                              0.9634 - 1.169
                                                0.243
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 15.16 on 585 degrees of freedom
## Multiple R-squared: 0.002332,
                                  Adjusted R-squared: 0.0006262
## F-statistic: 1.367 on 1 and 585 DF, p-value: 0.2428
##
## Call:
## lm(formula = reading_score ~ is_first_child, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
                   0.744 11.744 30.995
## -53.256 -10.256
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                   67.755
                               2.319 29.223 <2e-16 ***
## is_first_child
                    1.250
                               1.334
                                     0.937
                                               0.349
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 15.17 on 585 degrees of freedom
## Multiple R-squared: 0.001499, Adjusted R-squared: -0.000208
## F-statistic: 0.8781 on 1 and 585 DF, p-value: 0.3491
##
## Call:
## lm(formula = reading_score ~ nr_siblings, data = step_df)
## Residuals:
##
               1Q Median
                               3Q
      Min
## -53.241 -10.199
                  0.676 11.217 31.134
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 68.8661
                          1.1000 62.603 <2e-16 ***
## nr_siblings 0.4583
                           0.4228
                                  1.084
                                            0.279
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 15.16 on 585 degrees of freedom
## Multiple R-squared: 0.002004, Adjusted R-squared:
                                                       0.0002984
## F-statistic: 1.175 on 1 and 585 DF, p-value: 0.2788
##
## Call:
## lm(formula = reading_score ~ transport_means, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
## -52.989 -9.989
                   0.376 11.193 30.376
##
```

```
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 69.2601
                              2.1605 32.057
## transport_means    0.3644
                               1.2844 0.284
                                                0.777
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 15.18 on 585 degrees of freedom
## Multiple R-squared: 0.0001376, Adjusted R-squared: -0.001572
## F-statistic: 0.08048 on 1 and 585 DF, p-value: 0.7767
##
## Call:
## lm(formula = reading_score ~ wkly_study_hours, data = step_df)
## Residuals:
      Min
               1Q Median
                               3Q
## -54.127 -10.127 1.053 11.553 30.233
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    67.5878
                                1.9267
                                        35.08
                                                <2e-16 ***
                    1.1797
                                0.9517
                                         1.24
                                                 0.216
## wkly_study_hours
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 15.16 on 585 degrees of freedom
## Multiple R-squared: 0.00262, Adjusted R-squared: 0.0009147
## F-statistic: 1.537 on 1 and 585 DF, p-value: 0.2156
##
## Call:
## lm(formula = reading_score ~ test_prep, data = step_df)
## Residuals:
      Min
               1Q Median
                               ЗQ
                                      Max
## -50.644 -9.861
                   1.139 10.748 32.356
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                80.077
                            2.201
                                   36.38 < 2e-16 ***
## test_prep
                -6.217
                            1.284
                                  -4.84 1.66e-06 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.88 on 585 degrees of freedom
## Multiple R-squared: 0.03851, Adjusted R-squared: 0.03686
## F-statistic: 23.43 on 1 and 585 DF, p-value: 1.662e-06
##
## Call:
## lm(formula = reading_score ~ lunch_type, data = step_df)
##
```

```
## Residuals:
##
      Min
               1Q Median
                               30
                                      Max
## -47.558 -9.558 0.294 10.442 35.442
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 56.410
                            2.178 25.898 < 2e-16 ***
                                  6.422 2.79e-10 ***
## lunch_type
                 8.148
                            1.269
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.67 on 585 degrees of freedom
## Multiple R-squared: 0.06585,
                                  Adjusted R-squared: 0.06425
## F-statistic: 41.24 on 1 and 585 DF, p-value: 2.791e-10
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender, data = step_df)
## Residuals:
               1Q Median
                               3Q
      Min
                                      Max
                   0.779 10.207 39.779
## -50.793 -9.292
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                66.795
                            2.653 25.175 < 2e-16 ***
                            1.229
                                   6.974 8.37e-12 ***
                 8.570
## lunch_type
## gender
                -7.572
                            1.176 -6.438 2.53e-10 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.19 on 584 degrees of freedom
## Multiple R-squared: 0.1278, Adjusted R-squared: 0.1248
## F-statistic: 42.77 on 2 and 584 DF, p-value: < 2.2e-16
## Call:
## lm(formula = reading_score ~ lunch_type + ethnic_group, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -47.335 -9.333 -0.287 10.664 34.663
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                50.3851
                            2.6504 19.010 < 2e-16 ***
## (Intercept)
                 7.9566
                            1.2547
                                     6.342 4.56e-10 ***
## lunch_type
## ethnic_group
                            0.5128
                                     3.896 0.000109 ***
                 1.9978
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.5 on 584 degrees of freedom
## Multiple R-squared: 0.08951,
                                  Adjusted R-squared: 0.08639
## F-statistic: 28.71 on 2 and 584 DF, p-value: 1.283e-12
```

```
##
## Call:
## lm(formula = reading_score ~ lunch_type + parent_educ, data = step_df)
## Residuals:
##
      Min
               1Q Median
                                3Q
                                      Max
## -43.447 -9.436 0.372 10.505 35.595
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 50.2445
                           2.4668 20.369 < 2e-16 ***
                8.2236
                           1.2437
                                     6.612 8.57e-11 ***
## lunch_type
                1.9788
                           0.3965
                                    4.990 7.97e-07 ***
## parent_educ
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14.38 on 584 degrees of freedom
## Multiple R-squared: 0.1041, Adjusted R-squared: 0.101
## F-statistic: 33.91 on 2 and 584 DF, p-value: 1.165e-14
##
## Call:
## lm(formula = reading_score ~ lunch_type + parent_marital_status,
      data = step_df)
##
## Residuals:
##
               1Q Median
                               3Q
      Min
                                      Max
## -48.208 -9.528
                   0.379 10.606 36.339
##
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         54.7005
                                     2.9181 18.745 < 2e-16 ***
## lunch_type
                          8.1864
                                      1.2698
                                              6.447 2.39e-10 ***
                          0.7737
                                      0.8784
                                              0.881
                                                       0.379
## parent_marital_status
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14.67 on 584 degrees of freedom
## Multiple R-squared: 0.06709,
                                   Adjusted R-squared: 0.06389
## F-statistic:
                  21 on 2 and 584 DF, p-value: 1.561e-09
##
## Call:
## lm(formula = reading_score ~ lunch_type + practice_sport, data = step_df)
##
## Residuals:
               1Q Median
                               ЗQ
                                      Max
## -46.875 -9.777
                    0.064 11.015 36.125
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  58.6184
                              3.0712 19.086 < 2e-16 ***
                   8.1097
                              1.2693
                                      6.389 3.41e-10 ***
## lunch_type
## practice_sport -0.9510
                              0.9326 - 1.020
                                                0.308
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.67 on 584 degrees of freedom
## Multiple R-squared: 0.06751,
                                   Adjusted R-squared: 0.06432
## F-statistic: 21.14 on 2 and 584 DF, p-value: 1.368e-09
##
## Call:
## lm(formula = reading_score ~ lunch_type + is_first_child, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
## -47.943 -9.943 0.057 10.923 36.206
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                   54.512
                               3.050 17.875 < 2e-16 ***
## lunch_type
                    8.134
                               1.269
                                     6.409 3.02e-10 ***
                               1.291
## is_first_child
                    1.148
                                       0.890
                                                0.374
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.67 on 584 degrees of freedom
## Multiple R-squared: 0.06711,
                                  Adjusted R-squared: 0.06392
## F-statistic: 21.01 on 2 and 584 DF, p-value: 1.549e-09
##
## Call:
## lm(formula = reading_score ~ lunch_type + nr_siblings, data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               30
                                      Max
## -47.950 -9.595 -0.043 10.657 36.410
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                           2.3455 23.639 < 2e-16 ***
## (Intercept) 55.4448
## lunch_type
                8.1452
                           1.2686
                                   6.421 2.81e-10 ***
                0.4533
                           0.4090
                                    1.109
                                             0.268
## nr_siblings
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.67 on 584 degrees of freedom
## Multiple R-squared: 0.06781,
                                  Adjusted R-squared: 0.06462
## F-statistic: 21.24 on 2 and 584 DF, p-value: 1.245e-09
##
## Call:
## lm(formula = reading_score ~ lunch_type + transport_means, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
```

```
## -47.665 -9.541 0.190 10.604 35.604
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                    55.983
                                2.942 19.030 < 2e-16 ***
                     8.145
                                1.270 6.413 2.94e-10 ***
## lunch type
                     0.269
                                      0.216
## transport means
                                1.243
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.68 on 584 degrees of freedom
## Multiple R-squared: 0.06592,
                                   Adjusted R-squared: 0.06273
## F-statistic: 20.61 on 2 and 584 DF, p-value: 2.246e-09
##
## Call:
## lm(formula = reading_score ~ lunch_type + wkly_study_hours, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -48.825 -9.232
                   0.196 11.031 35.340
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
                    54.1859
                                2.7980 19.366 < 2e-16 ***
## (Intercept)
## lunch type
                     8.1438
                                1.2681
                                        6.422 2.79e-10 ***
## wkly_study_hours
                     1.1651
                                0.9206
                                        1.266
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 14.66 on 584 degrees of freedom
## Multiple R-squared: 0.06841,
                                 Adjusted R-squared: 0.06522
## F-statistic: 21.44 on 2 and 584 DF, p-value: 1.033e-09
##
## lm(formula = reading_score ~ lunch_type + test_prep, data = step_df)
##
## Residuals:
      Min
               1Q Median
##
                               3Q
                                      Max
## -45.142 -9.312 0.517 10.222 31.393
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                            2.907 22.952 < 2e-16 ***
## (Intercept)
                66.731
                                   6.717 4.41e-11 ***
## lunch_type
                 8.341
                            1.242
## test_prep
                -6.466
                            1.239 -5.218 2.52e-07 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.35 on 584 degrees of freedom
## Multiple R-squared: 0.1075, Adjusted R-squared: 0.1044
## F-statistic: 35.16 on 2 and 584 DF, p-value: 3.829e-15
```

```
##
## Call:
## lm(formula = reading_score ~ lunch_type + ethnic_group, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -47.335 -9.333 -0.287 10.664 34.663
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                50.3851
                            2.6504 19.010 < 2e-16 ***
                 7.9566
                            1.2547
                                     6.342 4.56e-10 ***
## lunch_type
                 1.9978
                            0.5128
                                     3.896 0.000109 ***
## ethnic_group
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14.5 on 584 degrees of freedom
## Multiple R-squared: 0.08951, Adjusted R-squared: 0.08639
## F-statistic: 28.71 on 2 and 584 DF, p-value: 1.283e-12
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + ethnic_group,
      data = step_df)
##
## Residuals:
##
               1Q Median
                               3Q
      Min
                                      Max
## -50.575 -8.989
                   0.425 10.621 35.996
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                            3.0128 20.167 < 2e-16 ***
                60.7592
## lunch_type
                 8.3786
                            1.2138
                                    6.903 1.34e-11 ***
                -7.5858
                            1.1609 -6.534 1.39e-10 ***
## gender
## ethnic_group
                2.0076
                            0.4955
                                    4.052 5.77e-05 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.01 on 583 degrees of freedom
## Multiple R-squared: 0.1516, Adjusted R-squared: 0.1473
## F-statistic: 34.74 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + parent_educ,
##
       data = step_df)
##
## Residuals:
               10 Median
      Min
                               3Q
                                      Max
## -46.857 -9.511
                    0.684
                            9.884 39.712
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 60.6267
                           2.9148 20.799 < 2e-16 ***
```

```
## lunch_type
                8.6194
                           1.2071
                                   7.141 2.77e-12 ***
                           1.1578 -6.226 9.16e-10 ***
               -7.2082
## gender
## parent_educ
               1.8194
                           0.3852
                                   4.724 2.90e-06 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.94 on 583 degrees of freedom
## Multiple R-squared: 0.1599, Adjusted R-squared: 0.1556
## F-statistic: 36.99 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + parent_marital_status,
##
      data = step df)
##
## Residuals:
      Min
               1Q Median
                               ЗQ
## -51.286 -9.439
                   1.115 10.061 39.860
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         65.4297
                                     3.2818 19.937 < 2e-16 ***
                          8.5985
                                             6.991 7.52e-12 ***
## lunch_type
                                     1.2300
                         -7.5453
                                     1.1772 -6.410 3.01e-10 ***
## gender
                         0.6012
                                     0.8501
                                             0.707
                                                        0.48
## parent marital status
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14.2 on 583 degrees of freedom
## Multiple R-squared: 0.1285, Adjusted R-squared: 0.124
## F-statistic: 28.65 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + practice_sport,
##
      data = step_df)
##
## Residuals:
      Min
               10 Median
                               3Q
## -50.144 -9.527
                    0.987
                            9.973 40.417
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
                              3.3707 20.429 < 2e-16 ***
                  68.8601
## (Intercept)
                   8.5334
                              1.2294
                                       6.941 1.04e-11 ***
## lunch_type
## gender
                  -7.5607
                              1.1762 -6.428 2.69e-10 ***
## practice_sport -0.8962
                              0.9020 -0.994
                                                0.321
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.19 on 583 degrees of freedom
## Multiple R-squared: 0.1292, Adjusted R-squared: 0.1247
## F-statistic: 28.84 on 3 and 583 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + is_first_child,
      data = step_df)
## Residuals:
               10 Median
      Min
                               30
                                      Max
## -51.221 -9.298 0.811 10.295 40.625
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
                   64.736
                               3.348 19.337 < 2e-16 ***
## (Intercept)
                    8.556
                               1.229
                                       6.962 9.07e-12 ***
## lunch_type
## gender
                   -7.588
                               1.176 -6.451 2.33e-10 ***
## is_first_child
                   1.259
                               1.249
                                       1.008
                                                0.314
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.19 on 583 degrees of freedom
## Multiple R-squared: 0.1293, Adjusted R-squared: 0.1248
## F-statistic: 28.85 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + nr_siblings,
##
      data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -51.092 -9.393
                   0.876 10.073 39.442
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 65.9647
                           2.8018 23.544 < 2e-16 ***
## lunch_type
                                   6.970 8.62e-12 ***
                8.5657
                           1.2290
## gender
               -7.5340
                           1.1770 -6.401 3.17e-10 ***
## nr_siblings 0.3653
                           0.3959
                                    0.923
                                             0.357
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.19 on 583 degrees of freedom
## Multiple R-squared: 0.129, Adjusted R-squared: 0.1245
## F-statistic: 28.79 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + transport_means,
##
      data = step_df)
##
## Residuals:
     Min
             1Q Median
                           3Q
                                 Max
## -50.95 -9.44 1.01 10.06 40.01
## Coefficients:
```

```
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                               3.2578 20.320 < 2e-16 ***
                   66.1997
## lunch_type
                    8.5656
                               1.2299
                                       6.965 8.91e-12 ***
## gender
                   -7.5770
                               1.1771 -6.437 2.55e-10 ***
## transport_means
                    0.3787
                               1.2018
                                       0.315
                                                 0.753
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.2 on 583 degrees of freedom
## Multiple R-squared: 0.1279, Adjusted R-squared: 0.1234
## F-statistic: 28.5 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + wkly_study_hours,
      data = step_df)
##
## Residuals:
      Min
               1Q Median
                               30
                                      Max
## -52.360 -9.194 0.891 10.101 39.701
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    64.2095
                                3.1118 20.634 < 2e-16 ***
                                1.2273
## lunch_type
                     8.5696
                                         6.983 7.91e-12 ***
## gender
                    -7.6506
                                1.1757 -6.508 1.65e-10 ***
                    1.4107
                                0.8904
                                        1.584
                                                  0.114
## wkly_study_hours
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.17 on 583 degrees of freedom
## Multiple R-squared: 0.1315, Adjusted R-squared: 0.127
## F-statistic: 29.42 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep,
      data = step_df)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -48.365 -9.154 -0.154 10.259 35.673
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                78.035
                            3.251 24.004 < 2e-16 ***
## (Intercept)
## lunch_type
                 8.789
                            1.198
                                    7.339 7.27e-13 ***
                -7.845
                            1.147 -6.842 1.98e-11 ***
## gender
## test_prep
                -6.807
                            1.194 -5.700 1.90e-08 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.82 on 583 degrees of freedom
## Multiple R-squared: 0.1738, Adjusted R-squared: 0.1695
```

```
## F-statistic: 40.88 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep,
       data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -48.365 -9.154 -0.154 10.259 35.673
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
               78.035
## (Intercept)
                            3.251 24.004 < 2e-16 ***
## lunch_type
                 8.789
                            1.198
                                   7.339 7.27e-13 ***
## gender
                -7.845
                            1.147 -6.842 1.98e-11 ***
                            1.194 -5.700 1.90e-08 ***
## test_prep
                -6.807
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 13.82 on 583 degrees of freedom
## Multiple R-squared: 0.1738, Adjusted R-squared: 0.1695
## F-statistic: 40.88 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
       ethnic_group, data = step_df)
##
## Residuals:
      \mathtt{Min}
               1Q Median
                               3Q
                                      Max
## -48.185 -9.696
                   0.309 10.143 32.043
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
               72.0069
                            3.5370 20.358 < 2e-16 ***
## (Intercept)
## lunch_type
                 8.5998
                            1.1830
                                    7.269 1.17e-12 ***
                -7.8550
## gender
                            1.1318 -6.940 1.05e-11 ***
## test_prep
                -6.7166
                            1.1790 -5.697 1.94e-08 ***
                                    4.051 5.79e-05 ***
                1.9554
                            0.4827
## ethnic_group
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.64 on 582 degrees of freedom
## Multiple R-squared: 0.1965, Adjusted R-squared: 0.1909
## F-statistic: 35.57 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
##
      parent_educ, data = step_df)
##
## Residuals:
```

```
10 Median
      Min
                               3Q
## -44.299 -9.218
                   0.751
                            9.968 35.537
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 71.9074
                           3.4168 21.045 < 2e-16 ***
                                   7.532 1.91e-13 ***
## lunch_type
                8.8432
                           1.1740
## gender
               -7.4774
                           1.1264 -6.638 7.29e-11 ***
## test_prep
               -6.9179
                           1.1709 -5.908 5.89e-09 ***
## parent_educ 1.8616
                           0.3745
                                   4.971 8.78e-07 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.55 on 582 degrees of freedom
## Multiple R-squared: 0.2074, Adjusted R-squared: 0.202
## F-statistic: 38.08 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
      parent_marital_status, data = step_df)
##
##
## Residuals:
      Min
               1Q Median
                               30
## -48.737 -9.103 -0.278 10.348 35.746
## Coefficients:
                        Estimate Std. Error t value Pr(>|t|)
                         76.9929
                                     3.7914 20.307 < 2e-16 ***
## (Intercept)
                          8.8095
                                              7.348 6.86e-13 ***
## lunch_type
                                     1.1989
## gender
                         -7.8246
                                     1.1480
                                            -6.816 2.34e-11 ***
## test_prep
                         -6.7856
                                     1.1956 -5.675 2.19e-08 ***
## parent_marital_status
                         0.4435
                                     0.8287
                                              0.535
                                                       0.593
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.83 on 582 degrees of freedom
## Multiple R-squared: 0.1742, Adjusted R-squared: 0.1685
## F-statistic: 30.69 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
##
      practice_sport, data = step_df)
##
## Residuals:
               1Q Median
                               3Q
                                      Max
## -47.657 -9.459
                    0.208 10.426 36.350
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  80.2982
                              3.8445 20.887 < 2e-16 ***
                  8.7502
                              1.1979
                                      7.305 9.20e-13 ***
## lunch_type
                  -7.8337
                              1.1465 -6.833 2.10e-11 ***
## gender
```

```
## test_prep
                  -6.8260
                              1.1941 -5.716 1.74e-08 ***
                              0.8786 -1.102
## practice_sport -0.9684
                                                0.271
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.82 on 582 degrees of freedom
## Multiple R-squared: 0.1755, Adjusted R-squared: 0.1699
## F-statistic: 30.97 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
      is_first_child, data = step_df)
##
## Residuals:
##
      Min
               10 Median
                               3Q
                                      Max
## -48.685 -9.416
                   0.207 10.392 36.301
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
                  76.499
                               3.870 19.768 < 2e-16 ***
## (Intercept)
## lunch_type
                    8.777
                               1.198
                                      7.326 7.97e-13 ***
## gender
                   -7.854
                               1.147 -6.847 1.92e-11 ***
## test_prep
                   -6.760
                               1.196 -5.651 2.50e-08 ***
## is_first_child
                    0.892
                               1.218
                                      0.732
                                                0.464
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.83 on 582 degrees of freedom
## Multiple R-squared: 0.1746, Adjusted R-squared: 0.1689
## F-statistic: 30.77 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
      nr_siblings, data = step_df)
##
##
## Residuals:
               1Q Median
##
      Min
                               3Q
                                      Max
## -48.590 -9.317 -0.259 10.162 35.459
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 77.3862
                           3.3955 22.791 < 2e-16 ***
## lunch_type
                8.7848
                           1.1982
                                    7.332 7.65e-13 ***
               -7.8168
                           1.1480
                                   -6.809 2.45e-11 ***
## gender
## test_prep
               -6.7676
                           1.1963
                                   -5.657 2.41e-08 ***
              0.2569
                           0.3862
                                    0.665
                                             0.506
## nr_siblings
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.83 on 582 degrees of freedom
## Multiple R-squared: 0.1744, Adjusted R-squared: 0.1687
## F-statistic: 30.74 on 4 and 582 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
       transport_means, data = step_df)
## Residuals:
      Min
               10 Median
                               30
                                      Max
## -48.692 -9.409
                    0.168 10.344 36.162
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
                   76.7815
                               3.6696 20.924 < 2e-16 ***
## (Intercept)
## lunch_type
                    8.7812
                               1.1981
                                        7.329 7.78e-13 ***
                   -7.8595
## gender
                               1.1473 -6.851 1.88e-11 ***
                   -6.8710
                               1.1978 -5.736 1.56e-08 ***
## test_prep
## transport_means
                    0.8653
                               1.1733
                                       0.737
                                                 0.461
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.83 on 582 degrees of freedom
## Multiple R-squared: 0.1746, Adjusted R-squared: 0.1689
## F-statistic: 30.77 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
##
       wkly_study_hours, data = step_df)
##
## Residuals:
               1Q Median
      Min
                               3Q
                                      Max
## -49.466 -9.300 -0.300
                            9.722 35.695
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    76.0874
                                3.7085 20.517 < 2e-16 ***
## lunch_type
                     8.7848
                                1.1974
                                        7.336 7.40e-13 ***
## gender
                    -7.8932
                                1.1473 -6.880 1.55e-11 ***
## test_prep
                    -6.6835
                                1.1994 -5.572 3.85e-08 ***
## wkly_study_hours
                     0.9514
                                0.8722
                                         1.091
                                                  0.276
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.82 on 582 degrees of freedom
## Multiple R-squared: 0.1755, Adjusted R-squared: 0.1698
## F-statistic: 30.97 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
      parent_educ, data = step_df)
##
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -44.299 -9.218 0.751
                            9.968 35.537
```

```
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 71.9074
                           3.4168 21.045 < 2e-16 ***
## lunch_type
                8.8432
                           1.1740
                                    7.532 1.91e-13 ***
               -7.4774
                           1.1264 -6.638 7.29e-11 ***
## gender
               -6.9179
                           1.1709 -5.908 5.89e-09 ***
## test_prep
## parent_educ
               1.8616
                           0.3745
                                   4.971 8.78e-07 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.55 on 582 degrees of freedom
## Multiple R-squared: 0.2074, Adjusted R-squared: 0.202
## F-statistic: 38.08 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
##
       parent_educ + ethnic_group, data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               30
                                       Max
## -44.354 -8.959
                    0.802
                            9.901 32.216
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                            3.6485 18.285 < 2e-16 ***
## (Intercept)
                66.7121
## lunch_type
                 8.6667
                            1.1618
                                    7.459 3.18e-13 ***
                -7.5066
                            1.1139 -6.739 3.84e-11 ***
## gender
                -6.8289
                            1.1580 -5.897 6.28e-09 ***
## test_prep
                 1.7606
                            0.3713
                                    4.742 2.66e-06 ***
## parent_educ
                            0.4753
                                    3.773 0.000178 ***
## ethnic_group
                 1.7930
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 13.4 on 581 degrees of freedom
## Multiple R-squared: 0.2264, Adjusted R-squared: 0.2197
## F-statistic: 34.01 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
       parent_educ + parent_marital_status, data = step_df)
##
##
## Residuals:
                                3Q
##
      Min
               1Q Median
                                      Max
## -44.611 -9.180
                   0.629
                            9.997
                                   35.598
##
## Coefficients:
                        Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                         71.0626
                                     3.9046 18.200 < 2e-16 ***
## lunch_type
                         8.8598
                                      1.1754
                                             7.538 1.85e-13 ***
## gender
                         -7.4614
                                     1.1278 -6.616 8.39e-11 ***
                         -6.9001
                                     1.1724 -5.886 6.71e-09 ***
## test_prep
```

```
1.8582
                                     0.3748
                                              4.958 9.38e-07 ***
## parent educ
                                              0.448
                                                       0.654
## parent_marital_status
                          0.3641
                                     0.8126
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.56 on 581 degrees of freedom
## Multiple R-squared: 0.2077, Adjusted R-squared: 0.2009
## F-statistic: 30.47 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
       parent_educ + practice_sport, data = step_df)
##
## Residuals:
##
      Min
                10 Median
                               3Q
                                      Max
## -43.833 -9.145
                    0.826 10.176 36.026
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
                              4.0101 18.353 < 2e-16 ***
## (Intercept)
                  73.5975
                                       7.502 2.36e-13 ***
## lunch type
                   8.8147
                              1.1749
## gender
                  -7.4732
                              1.1268 -6.632 7.57e-11 ***
## test_prep
                  -6.9303
                              1.1713 -5.917 5.62e-09 ***
                   1.8421
                              0.3754
                                      4.907 1.20e-06 ***
## parent_educ
## practice_sport -0.6958
                              0.8635 -0.806
                                                0.421
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 13.55 on 581 degrees of freedom
## Multiple R-squared: 0.2083, Adjusted R-squared: 0.2015
## F-statistic: 30.58 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
       parent_educ + is_first_child, data = step_df)
##
## Residuals:
      Min
               1Q Median
                               30
                                      Max
## -44.608 -9.313 0.700 10.098 36.135
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                  70.4526
                              3.9845 17.682 < 2e-16 ***
                   8.8320
                              1.1746
                                       7.519 2.10e-13 ***
## lunch_type
                   -7.4870
                              1.1270 -6.643 7.06e-11 ***
## gender
                  -6.8734
                              1.1731 -5.859 7.79e-09 ***
## test_prep
                   1.8596
                              0.3747
                                       4.963 9.11e-07 ***
## parent_educ
## is_first_child
                   0.8488
                              1.1944
                                       0.711
                                                0.478
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.55 on 581 degrees of freedom
```

```
## Multiple R-squared: 0.2081, Adjusted R-squared: 0.2013
## F-statistic: 30.54 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
##
       parent_educ + nr_siblings, data = step_df)
## Residuals:
      Min
               1Q Median
                               30
                                      Max
## -44.540 -9.254
                    0.737 10.246 35.299
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 71.1703
                           3.5545 20.023 < 2e-16 ***
## lunch_type
                8.8386
                           1.1745
                                    7.526 2.01e-13 ***
## gender
                -7.4452
                           1.1277
                                   -6.602 9.14e-11 ***
               -6.8742
                           1.1727 -5.862 7.69e-09 ***
## test_prep
## parent_educ
               1.8659
                           0.3747
                                    4.980 8.39e-07 ***
## nr_siblings
                0.2862
                           0.3786
                                    0.756
                                              0.45
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.55 on 581 degrees of freedom
## Multiple R-squared: 0.2082, Adjusted R-squared: 0.2014
## F-statistic: 30.56 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
##
      parent_educ + transport_means, data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               30
                                      Max
## -44.611 -9.130
                    0.694 10.057
                                   35.997
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                   70.7390
                               3.7978 18.626 < 2e-16 ***
                                       7.523 2.05e-13 ***
## lunch_type
                    8.8358
                               1.1746
## gender
                   -7.4916
                               1.1271 -6.647 6.91e-11 ***
                   -6.9777
                               1.1744 -5.941 4.88e-09 ***
## test_prep
                               0.3747
                                        4.962 9.18e-07 ***
## parent_educ
                    1.8591
                               1.1502
                                       0.706
                                                  0.48
## transport_means
                    0.8121
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.55 on 581 degrees of freedom
## Multiple R-squared: 0.2081, Adjusted R-squared: 0.2013
## F-statistic: 30.54 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
```

```
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
##
       parent_educ + wkly_study_hours, data = step_df)
##
## Residuals:
      Min
                1Q Median
                                3Q
                                       Max
## -45.535 -9.074
                    0.847
                             9.928 35.562
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
                                 3.8570 18.046 < 2e-16 ***
## (Intercept)
                     69.6040
## lunch_type
                     8.8388
                                 1.1734
                                         7.533 1.91e-13 ***
                     -7.5299
                                 1.1266 -6.684 5.46e-11 ***
## gender
## test_prep
                     -6.7761
                                 1.1754
                                        -5.765 1.33e-08 ***
## parent_educ
                     1.8781
                                 0.3745
                                         5.015 7.06e-07 ***
                      1.0987
                                 0.8552
                                          1.285
                                                   0.199
## wkly_study_hours
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.54 on 581 degrees of freedom
## Multiple R-squared: 0.2097, Adjusted R-squared: 0.2029
## F-statistic: 30.83 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
##
       parent_educ + ethnic_group, data = step_df)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -44.354 -8.959
                     0.802
                             9.901
                                   32.216
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 66.7121
                            3.6485 18.285 < 2e-16 ***
## lunch_type
                 8.6667
                            1.1618
                                     7.459 3.18e-13 ***
## gender
                 -7.5066
                            1.1139 -6.739 3.84e-11 ***
                 -6.8289
                             1.1580 -5.897 6.28e-09 ***
## test_prep
                  1.7606
                            0.3713
                                     4.742 2.66e-06 ***
## parent_educ
## ethnic_group
                  1.7930
                             0.4753
                                    3.773 0.000178 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.4 on 581 degrees of freedom
## Multiple R-squared: 0.2264, Adjusted R-squared: 0.2197
## F-statistic: 34.01 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
##
       parent_educ + ethnic_group + parent_marital_status, data = step_df)
##
## Residuals:
      Min
                1Q Median
                                30
## -44.741 -8.668
                   0.860 10.107 32.276
```

```
##
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
                                     4.1173 15.944 < 2e-16 ***
## (Intercept)
                         65.6456
## lunch_type
                          8.6865
                                     1.1631
                                              7.469 2.99e-13 ***
                                     1.1151 -6.714 4.51e-11 ***
## gender
                         -7.4869
                                     1.1594 -5.871 7.31e-09 ***
## test_prep
                         -6.8065
                                              4.726 2.88e-06 ***
## parent_educ
                          1.7561
                                     0.3716
## ethnic_group
                          1.8006
                                     0.4757
                                              3.785 0.00017 ***
## parent_marital_status
                          0.4502
                                     0.8037
                                              0.560 0.57557
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.4 on 580 degrees of freedom
## Multiple R-squared: 0.2268, Adjusted R-squared: 0.2188
## F-statistic: 28.36 on 6 and 580 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
       parent_educ + ethnic_group + practice_sport, data = step_df)
##
##
## Residuals:
                1Q Median
      Min
                                30
## -43.882 -9.319
                    0.845 10.001 32.709
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
                              4.1955 16.309 < 2e-16 ***
## (Intercept)
                  68.4230
                   8.6377
                              1.1627
                                       7.429 3.93e-13 ***
## lunch_type
## gender
                  -7.5024
                              1.1142 -6.734 3.99e-11 ***
## test_prep
                  -6.8414
                              1.1584 -5.906 5.98e-09 ***
## parent_educ
                   1.7408
                              0.3721
                                       4.678 3.61e-06 ***
## ethnic_group
                   1.7943
                              0.4754
                                       3.774 0.000177 ***
## practice_sport -0.7058
                              0.8538 -0.827 0.408769
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.4 on 580 degrees of freedom
## Multiple R-squared: 0.2273, Adjusted R-squared: 0.2193
## F-statistic: 28.44 on 6 and 580 DF, p-value: < 2.2e-16
##
## Call:
  lm(formula = reading_score ~ lunch_type + gender + test_prep +
       parent_educ + ethnic_group + is_first_child, data = step_df)
##
##
## Residuals:
               10 Median
      Min
                                3Q
                                      Max
## -44.665 -9.187
                    0.886 10.213 32.816
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
                  65.2492
                             4.1744 15.631 < 2e-16 ***
## (Intercept)
```

```
8.6555
                               1.1624
                                        7.446 3.50e-13 ***
## lunch_type
                               1.1144 -6.745 3.72e-11 ***
## gender
                   -7.5162
## test_prep
                   -6.7841
                               1.1602 -5.848 8.33e-09 ***
                               0.3714
                                        4.735 2.76e-06 ***
## parent_educ
                    1.7587
## ethnic_group
                    1.7934
                               0.4755
                                        3.772 0.000179 ***
                                        0.722 0.470481
## is first child
                   0.8529
                               1.1810
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 13.4 on 580 degrees of freedom
## Multiple R-squared: 0.2271, Adjusted R-squared: 0.2191
## F-statistic: 28.4 on 6 and 580 DF, p-value: < 2.2e-16
##
## Call:
  lm(formula = reading_score ~ lunch_type + gender + test_prep +
##
       parent_educ + ethnic_group + nr_siblings, data = step_df)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -44.626 -8.902
                    0.850
                             9.677 32.420
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                             3.7839 17.403 < 2e-16 ***
                65.8499
## (Intercept)
                 8.6605
                             1.1621
                                      7.452 3.35e-13 ***
## lunch_type
                             1.1149 -6.701 4.92e-11 ***
                -7.4705
## gender
## test_prep
                 -6.7791
                             1.1597 -5.845 8.44e-09 ***
## parent_educ
                 1.7650
                                     4.752 2.54e-06 ***
                             0.3714
                 1.8036
                             0.4755
## ethnic_group
                                      3.793 0.000165 ***
                  0.3228
                             0.3744
                                     0.862 0.388988
## nr_siblings
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.4 on 580 degrees of freedom
## Multiple R-squared: 0.2274, Adjusted R-squared: 0.2194
## F-statistic: 28.45 on 6 and 580 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
##
       parent_educ + ethnic_group + transport_means, data = step_df)
##
## Residuals:
      Min
                1Q Median
                                3Q
                                       Max
                     0.790
                             9.849
                                    32.728
## -44.717 -8.855
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
                                4.0171 16.260 < 2e-16 ***
## (Intercept)
                    65.3191
                    8.6569
                                1.1622
                                        7.449 3.44e-13 ***
## lunch_type
## gender
                   -7.5233
                                1.1144 -6.751 3.56e-11 ***
                   -6.8978
                                1.1613 -5.940 4.93e-09 ***
## test_prep
                                       4.731 2.81e-06 ***
## parent_educ
                     1.7571
                                0.3714
```

```
## ethnic_group
                     1.8051
                               0.4756
                                         3.795 0.000163 ***
                     0.9440
                               1.1377
                                        0.830 0.407036
## transport_means
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.4 on 580 degrees of freedom
## Multiple R-squared: 0.2273, Adjusted R-squared: 0.2193
## F-statistic: 28.44 on 6 and 580 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = reading_score ~ lunch_type + gender + test_prep +
       parent_educ + ethnic_group + wkly_study_hours, data = step_df)
##
## Residuals:
##
      Min
                10 Median
                                3Q
                                       Max
## -45.551 -8.822
                    0.863
                            9.721 32.252
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                    64.5007
                                4.0483 15.933 < 2e-16 ***
## lunch type
                     8.6631
                                1.1613
                                         7.460 3.18e-13 ***
## gender
                     -7.5573
                                1.1140 -6.784 2.90e-11 ***
## test_prep
                     -6.6919
                                1.1626 -5.756 1.39e-08 ***
                                         4.786 2.16e-06 ***
## parent_educ
                     1.7770
                                0.3713
## ethnic_group
                     1.7865
                                0.4751
                                          3.761 0.000187 ***
                                0.8457
                                         1.258 0.208928
## wkly_study_hours
                     1.0638
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.39 on 580 degrees of freedom
## Multiple R-squared: 0.2285, Adjusted R-squared: 0.2205
## F-statistic: 28.63 on 6 and 580 DF, p-value: < 2.2e-16
## Start: AIC=3193.22
## reading score ~ 1
##
                          Df Sum of Sq
                                           RSS
## + lunch_type
                                8876.3 125920 3155.2
                           1
## + gender
                           1
                                7428.6 127368 3161.9
## + test_prep
                           1
                                5190.3 129606 3172.2
## + parent_educ
                                4985.3 129811 3173.1
                            1
                                3614.0 131182 3179.3
## + ethnic_group
                            1
## <none>
                                        134796 3193.2
## + wkly_study_hours
                           1
                                 353.1 134443 3193.7
## + practice_sport
                                 314.3 134482 3193.9
                            1
## + nr_siblings
                            1
                                 270.2 134526 3194.0
## + is_first_child
                                 202.0 134594 3194.3
                            1
## + parent_marital_status 1
                                93.3 134703 3194.8
                                  18.5 134778 3195.1
## + transport_means
                            1
##
## Step: AIC=3155.24
## reading_score ~ lunch_type
##
```

```
##
                           Df Sum of Sq
                                           RSS
                                                  AIC
## + gender
                                 8344.3 117576 3117.0
                            1
## + test_prep
                                 5609.0 120311 3130.5
                                 5149.8 120770 3132.7
## + parent_educ
                            1
## + ethnic_group
                                 3189.3 122731 3142.2
## <none>
                                        125920 3155.2
## + wkly study hours
                                344.5 125575 3155.6
                           1
## + nr siblings
                                 264.4 125655 3156.0
                            1
## + practice_sport
                            1
                                 223.8 125696 3156.2
## + is_first_child
                            1
                                170.4 125749 3156.4
## + parent_marital_status 1
                                167.1 125753 3156.5
                                 10.1 125910 3157.2
## + transport_means
                            1
##
## Step: AIC=3116.99
## reading_score ~ lunch_type + gender
##
##
                                           RSS
                                                  AIC
                           Df Sum of Sq
## + test_prep
                                6206.4 111369 3087.2
                                 4334.5 113241 3096.9
## + parent_educ
                            1
## + ethnic group
                            1
                                 3220.4 114355 3102.7
## + wkly_study_hours
                            1
                                 504.0 117072 3116.5
## <none>
                                        117576 3117.0
                                  204.6 117371 3118.0
## + is_first_child
                            1
## + practice sport
                                 198.7 117377 3118.0
                            1
## + nr siblings
                            1
                                171.4 117404 3118.1
## + parent_marital_status 1
                                100.8 117475 3118.5
## + transport_means
                                 20.0 117556 3118.9
                            1
##
## Step: AIC=3087.16
## reading_score ~ lunch_type + gender + test_prep
##
##
                           Df Sum of Sq
                                           RSS
                                                  AIC
## + parent_educ
                                 4535.8 106833 3064.8
## + ethnic_group
                                 3054.3 108315 3072.8
                            1
## <none>
                                        111369 3087.2
## + practice_sport
                                 232.0 111137 3087.9
                            1
## + wkly study hours
                           1
                                227.2 111142 3088.0
## + transport_means
                            1
                                104.0 111265 3088.6
## + is_first_child
                            1
                                 102.5 111267 3088.6
                                84.6 111285 3088.7
## + nr_siblings
                            1
## + parent_marital_status 1
                                 54.8 111314 3088.9
##
## Step: AIC=3064.75
## reading_score ~ lunch_type + gender + test_prep + parent_educ
                           Df Sum of Sq
##
                                           RSS
                                                  AIC
## + ethnic_group
                                2554.69 104279 3052.5
## <none>
                                        106833 3064.8
## + wkly_study_hours
                            1
                                 302.64 106531 3065.1
## + practice_sport
                            1
                                 119.26 106714 3066.1
## + nr_siblings
                               104.94 106728 3066.2
                            1
## + is_first_child
                            1
                               92.77 106741 3066.2
## + transport_means
                            1
                              91.59 106742 3066.2
## + parent marital status 1
                                36.91 106796 3066.6
```

```
##
## Step: AIC=3052.54
  reading_score ~ lunch_type + gender + test_prep + parent_educ +
##
       ethnic_group
##
##
                           Df Sum of Sq
                                            RSS
                                                   AIC
## <none>
                                         104279 3052.5
## + wkly_study_hours
                            1
                                 283.719 103995 3052.9
## + nr_siblings
                            1
                                133.453 104145 3053.8
## + transport_means
                            1
                                123.629 104155 3053.8
## + practice_sport
                            1
                                122.719 104156 3053.8
## + is_first_child
                            1
                                 93.682 104185 3054.0
## + parent_marital_status 1
                                 56.388 104222 3054.2
```

The model we obtained is Reading Score \sim Lunch Type + Gender + Test Prep + Parent Education + Ethnic Group.

When using the single-function method, the model obtained with the lowest AIC was Reading Score \sim Lunch Type + Gender + Test Prep + Parent Education + Ethnic Group. Both models at equal MSE and R-squared values.

Writing Score

```
##
## lm(formula = writing_score ~ gender, data = step_df)
## Residuals:
##
      Min
                10 Median
                                3Q
                                       Max
## -62.943 -10.221
                    1.057
                           11.057
                                    35.779
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                81.665
                             1.912 42.714 < 2e-16 ***
                 -8.722
                             1.237 -7.053 4.96e-12 ***
## gender
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.94 on 585 degrees of freedom
## Multiple R-squared: 0.07837,
                                    Adjusted R-squared: 0.07679
## F-statistic: 49.74 on 1 and 585 DF, p-value: 4.964e-12
##
## Call:
## lm(formula = writing_score ~ ethnic_group, data = step_df)
##
## Residuals:
##
      Min
                10 Median
                                3Q
                                       Max
## -58.452 -10.868
                    0.548 11.548 33.716
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                60.6995
                             1.8250 33.259 < 2e-16 ***
## ethnic group
                 2.5842
                             0.5397
                                      4.788 2.13e-06 ***
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 15.27 on 585 degrees of freedom
## Multiple R-squared: 0.03772,
                                  Adjusted R-squared: 0.03607
## F-statistic: 22.93 on 1 and 585 DF, p-value: 2.132e-06
##
## Call:
## lm(formula = writing_score ~ parent_educ, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
## -53.707 -10.533 0.172 11.232 36.293
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 61.1771
                          1.4150 43.23 < 2e-16 ***
## parent_educ
                2.5301
                           0.4162
                                   6.08 2.18e-09 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 15.09 on 585 degrees of freedom
## Multiple R-squared: 0.05943,
                                  Adjusted R-squared: 0.05782
## F-statistic: 36.96 on 1 and 585 DF, p-value: 2.176e-09
##
## Call:
## lm(formula = writing_score ~ lunch_type, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
## -53.165 -9.584 0.835 10.997 36.835
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 54.327
                            2.224 24.430 < 2e-16 ***
                            1.295
                                  6.822 2.24e-11 ***
## lunch_type
                 8.838
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.98 on 585 degrees of freedom
## Multiple R-squared: 0.0737, Adjusted R-squared: 0.07212
## F-statistic: 46.54 on 1 and 585 DF, p-value: 2.242e-11
##
## Call:
## lm(formula = writing_score ~ parent_marital_status, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
## -59.767 -10.774  0.226  10.726  32.218
##
```

```
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                        66.7887
                                   2.0806 32.101
## parent_marital_status    0.9928
                                     0.9301 1.067
                                                      0.286
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 15.55 on 585 degrees of freedom
## Multiple R-squared: 0.001944, Adjusted R-squared: 0.0002376
## F-statistic: 1.139 on 1 and 585 DF, p-value: 0.2862
##
## Call:
## lm(formula = writing_score ~ practice_sport, data = step_df)
## Residuals:
      Min
               1Q Median
                               3Q
## -58.898 -10.902  0.102  10.102  31.102
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 68.91193
                             2.32122 29.688
                                               <2e-16 ***
## practice_sport -0.00476
                             0.98893 -0.005
                                                0.996
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 15.56 on 585 degrees of freedom
## Multiple R-squared: 3.96e-08, Adjusted R-squared: -0.001709
## F-statistic: 2.317e-05 on 1 and 585 DF, p-value: 0.9962
##
## Call:
## lm(formula = writing_score ~ is_first_child, data = step_df)
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -59.182 -11.182 -0.182 10.677 31.677
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                  67.4636
                              2.3781 28.368
                                               <2e-16 ***
## is_first_child
                  0.8594
                              1.3688
                                     0.628
                                                 0.53
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 15.56 on 585 degrees of freedom
## Multiple R-squared: 0.0006734, Adjusted R-squared: -0.001035
## F-statistic: 0.3942 on 1 and 585 DF, p-value: 0.5304
##
## Call:
## lm(formula = writing_score ~ nr_siblings, data = step_df)
##
```

```
## Residuals:
##
               1Q Median
      Min
                               30
                                      Max
## -59.469 -10.639 0.531 10.851 32.511
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
                67.489
                            1.127 59.898
## (Intercept)
                                            <2e-16 ***
## nr_siblings
                 0.660
                            0.433
                                  1.524
                                             0.128
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 15.53 on 585 degrees of freedom
## Multiple R-squared: 0.003955, Adjusted R-squared: 0.002252
## F-statistic: 2.323 on 1 and 585 DF, p-value: 0.128
##
## Call:
## lm(formula = writing_score ~ transport_means, data = step_df)
## Residuals:
             1Q Median
                           3Q
                                 Max
## -58.93 -10.86
                 0.14 10.14 31.14
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
                  68.79315
                              2.21527 31.054
                                                <2e-16 ***
## (Intercept)
                                                 0.959
## transport_means 0.06711
                              1.31692
                                       0.051
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 15.56 on 585 degrees of freedom
## Multiple R-squared: 4.439e-06, Adjusted R-squared: -0.001705
## F-statistic: 0.002597 on 1 and 585 DF, p-value: 0.9594
##
## Call:
## lm(formula = writing_score ~ wkly_study_hours, data = step_df)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -60.381 -10.654
                   0.346 10.346 32.346
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                    66.2897
                                1.9747 33.569
                                                 <2e-16 ***
## wkly_study_hours
                    1.3638
                                0.9754
                                        1.398
                                                  0.163
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 15.54 on 585 degrees of freedom
## Multiple R-squared: 0.003331, Adjusted R-squared: 0.001627
## F-statistic: 1.955 on 1 and 585 DF, p-value: 0.1626
```

```
## Call:
## lm(formula = writing_score ~ test_prep, data = step_df)
## Residuals:
               1Q Median
                               3Q
## -55.902 -10.365 1.098 10.635 34.098
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                82.828
                            2.222 37.276 < 2e-16 ***
## test_prep
                -8.463
                            1.297 -6.527 1.46e-10 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 15.03 on 585 degrees of freedom
## Multiple R-squared: 0.06788, Adjusted R-squared: 0.06629
## F-statistic: 42.6 on 1 and 585 DF, p-value: 1.455e-10
##
## Call:
## lm(formula = writing_score ~ gender, data = step_df)
## Residuals:
               1Q Median
                               3Q
                   1.057 11.057 35.779
## -62.943 -10.221
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                81.665
                            1.912 42.714 < 2e-16 ***
## (Intercept)
                -8.722
                            1.237 -7.053 4.96e-12 ***
## gender
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.94 on 585 degrees of freedom
## Multiple R-squared: 0.07837, Adjusted R-squared: 0.07679
## F-statistic: 49.74 on 1 and 585 DF, p-value: 4.964e-12
##
## Call:
## lm(formula = writing_score ~ gender + ethnic_group, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
## -62.505 -9.545
                   0.098 10.042 31.042
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                            2.4855 29.550 < 2e-16 ***
## (Intercept)
                73.4485
## gender
                -8.7532
                            1.2118 -7.223 1.59e-12 ***
                            0.5175 5.030 6.53e-07 ***
## ethnic_group 2.6032
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.64 on 584 degrees of freedom
```

```
## Multiple R-squared: 0.1166, Adjusted R-squared: 0.1136
## F-statistic: 38.56 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + parent_educ, data = step_df)
##
## Residuals:
      Min
##
               1Q Median
                               3Q
                                      Max
## -57.908 -9.667
                    1.092 10.506 32.092
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 73.8127
                           2.2951 32.162 < 2e-16 ***
               -8.2503
                           1.2058 -6.842 1.98e-11 ***
## parent_educ
                                    5.840 8.65e-09 ***
                2.3460
                           0.4017
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.54 on 584 degrees of freedom
## Multiple R-squared: 0.1292, Adjusted R-squared: 0.1262
## F-statistic: 43.33 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + parent_marital_status,
##
       data = step_df)
##
## Residuals:
     Min
             1Q Median
                           3Q
## -63.61 -10.14 0.86 11.17 35.08
##
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         79.9463
                                     2.7411 29.166 < 2e-16 ***
                                     1.2376 -7.018 6.25e-12 ***
## gender
                         -8.6860
## parent_marital_status
                         0.7829
                                     0.8945
                                              0.875
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14.94 on 584 degrees of freedom
## Multiple R-squared: 0.07958,
                                   Adjusted R-squared: 0.07642
## F-statistic: 25.25 on 2 and 584 DF, p-value: 3.051e-11
##
## Call:
## lm(formula = writing_score ~ gender + practice_sport, data = step_df)
##
## Residuals:
               1Q Median
                               3Q
      Min
                                      Max
## -62.979 -10.208
                   1.021 11.069 35.744
##
## Coefficients:
```

```
Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                             2.86260 28.491 < 2e-16 ***
                 81.55789
                             1.23778 -7.047 5.17e-12 ***
## gender
                 -8.72276
                             0.95023
## practice_sport 0.04786
                                       0.050
                                                 0.96
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.95 on 584 degrees of freedom
## Multiple R-squared: 0.07837, Adjusted R-squared: 0.07522
## F-statistic: 24.83 on 2 and 584 DF, p-value: 4.469e-11
##
## Call:
## lm(formula = writing_score ~ gender + is_first_child, data = step_df)
## Residuals:
      Min
               1Q Median
                               3Q
## -63.274 -10.538   0.726   10.726   35.462
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
                  80.0245
## (Intercept)
                              2.8956 27.636 < 2e-16 ***
## gender
                  -8.7356
                              1.2373 -7.060 4.73e-12 ***
## is_first_child 0.9924
                              1.3151 0.755
                                               0.451
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.95 on 584 degrees of freedom
## Multiple R-squared: 0.07927,
                                   Adjusted R-squared: 0.07611
## F-statistic: 25.14 on 2 and 584 DF, p-value: 3.366e-11
##
## Call:
## lm(formula = writing_score ~ gender + nr_siblings, data = step_df)
## Residuals:
               1Q Median
                               3Q
## -63.397 -10.338   0.827   11.044   33.032
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 80.3850
                           2.1355 37.643 < 2e-16 ***
               -8.6648
                           1.2366 -7.007 6.73e-12 ***
## gender
## nr_siblings 0.5590
                           0.4165
                                              0.18
                                   1.342
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.93 on 584 degrees of freedom
## Multiple R-squared: 0.0812, Adjusted R-squared: 0.07806
## F-statistic: 25.81 on 2 and 584 DF, p-value: 1.821e-11
##
## Call:
```

```
## lm(formula = writing_score ~ gender + transport_means, data = step_df)
##
## Residuals:
##
               1Q Median
      Min
                               3Q
                                      Max
## -63.022 -10.197
                  0.978 10.978 35.902
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                   81.3488
                               2.7755 29.310 < 2e-16 ***
                               1.2379 -7.049 5.12e-12 ***
## gender
                   -8.7252
## transport_means
                   0.1991
                               1.2655
                                       0.157
                                                 0.875
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 14.95 on 584 degrees of freedom
## Multiple R-squared: 0.07841,
                                 Adjusted R-squared: 0.07525
## F-statistic: 24.84 on 2 and 584 DF, p-value: 4.419e-11
##
## Call:
## lm(formula = writing_score ~ gender + wkly_study_hours, data = step_df)
## Residuals:
##
               1Q Median
                               3Q
      Min
## -64.774 -9.664
                    0.874 10.874 35.689
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
                                2.5677 30.629 < 2e-16 ***
## (Intercept)
                    78.6452
## gender
                    -8.8145
                                1.2356 -7.134 2.9e-12 ***
## wkly_study_hours
                    1.6476
                                0.9371
                                        1.758
                                                0.0793 .
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.91 on 584 degrees of freedom
## Multiple R-squared: 0.08322,
                                   Adjusted R-squared: 0.08008
## F-statistic: 26.51 on 2 and 584 DF, p-value: 9.578e-12
##
## Call:
## lm(formula = writing_score ~ gender + test_prep, data = step_df)
##
## Residuals:
##
                               3Q
      Min
               1Q Median
                                      Max
## -59.967 -9.747 1.033
                            9.143 32.095
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
                96.714
                            2.795 34.605 < 2e-16 ***
## (Intercept)
                            1.188 -7.629 9.7e-14 ***
## gender
                -9.063
## test_prep
                -8.842
                            1.239 -7.139 2.8e-12 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 14.34 on 584 degrees of freedom
## Multiple R-squared: 0.1523, Adjusted R-squared: 0.1494
## F-statistic: 52.48 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type, data = step_df)
## Residuals:
      Min
               1Q Median
                               30
                                      Max
## -57.095 -9.170 0.754
                            9.754 37.105
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                66.944
                            2.668 25.087 < 2e-16 ***
## gender
                -9.200
                            1.183 -7.777 3.37e-14 ***
## lunch_type
                 9.351
                            1.236
                                   7.566 1.51e-13 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 14.27 on 584 degrees of freedom
## Multiple R-squared: 0.1606, Adjusted R-squared: 0.1578
## F-statistic: 55.88 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + parent_educ, data = step_df)
## Residuals:
      Min
               1Q Median
                               30
## -57.908 -9.667 1.092 10.506 32.092
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 73.8127
                           2.2951 32.162 < 2e-16 ***
                           1.2058 -6.842 1.98e-11 ***
## gender
               -8.2503
## parent_educ 2.3460
                           0.4017
                                    5.840 8.65e-09 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 14.54 on 584 degrees of freedom
## Multiple R-squared: 0.1292, Adjusted R-squared: 0.1262
## F-statistic: 43.33 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + ethnic_group, data = step_df)
##
## Residuals:
               1Q Median
                               3Q
      Min
                                      Max
## -62.505 -9.545
                   0.098 10.042 31.042
##
## Coefficients:
```

```
Estimate Std. Error t value Pr(>|t|)
                73.4485
                            2.4855 29.550 < 2e-16 ***
## (Intercept)
## gender
                -8.7532
                            1.2118 -7.223 1.59e-12 ***
                            0.5175
                                   5.030 6.53e-07 ***
## ethnic_group
                 2.6032
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.64 on 584 degrees of freedom
## Multiple R-squared: 0.1166, Adjusted R-squared: 0.1136
## F-statistic: 38.56 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + parent_educ, data = step_df)
## Residuals:
      Min
               1Q Median
                               3Q
## -57.908 -9.667
                  1.092 10.506 32.092
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 73.8127
                           2.2951 32.162 < 2e-16 ***
               -8.2503
                           1.2058 -6.842 1.98e-11 ***
## gender
## parent_educ 2.3460
                           0.4017 5.840 8.65e-09 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.54 on 584 degrees of freedom
## Multiple R-squared: 0.1292, Adjusted R-squared: 0.1262
## F-statistic: 43.33 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + parent_marital_status,
      data = step df)
##
## Residuals:
             1Q Median
                           3Q
                                 Max
## -63.61 -10.14
                 0.86 11.17 35.08
##
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         79.9463
                                     2.7411 29.166 < 2e-16 ***
                                     1.2376 -7.018 6.25e-12 ***
                         -8.6860
## gender
## parent_marital_status
                         0.7829
                                     0.8945
                                             0.875
                                                      0.382
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.94 on 584 degrees of freedom
## Multiple R-squared: 0.07958,
                                   Adjusted R-squared: 0.07642
## F-statistic: 25.25 on 2 and 584 DF, p-value: 3.051e-11
```

```
## Call:
## lm(formula = writing_score ~ gender + practice_sport, data = step_df)
## Residuals:
               1Q Median
                               3Q
                                      Max
## -62.979 -10.208 1.021 11.069 35.744
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 81.55789
                             2.86260 28.491 < 2e-16 ***
                             1.23778 -7.047 5.17e-12 ***
## gender
                 -8.72276
## practice_sport 0.04786
                             0.95023
                                     0.050
                                                0.96
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14.95 on 584 degrees of freedom
## Multiple R-squared: 0.07837,
                                   Adjusted R-squared: 0.07522
## F-statistic: 24.83 on 2 and 584 DF, p-value: 4.469e-11
##
## Call:
## lm(formula = writing_score ~ gender + is_first_child, data = step_df)
##
## Residuals:
##
               1Q Median
      Min
                               ЗQ
                                      Max
## -63.274 -10.538   0.726   10.726   35.462
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
                  80.0245
                              2.8956 27.636 < 2e-16 ***
## (Intercept)
                  -8.7356
## gender
                              1.2373 -7.060 4.73e-12 ***
## is_first_child 0.9924
                              1.3151
                                     0.755
                                               0.451
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 14.95 on 584 degrees of freedom
## Multiple R-squared: 0.07927, Adjusted R-squared: 0.07611
## F-statistic: 25.14 on 2 and 584 DF, p-value: 3.366e-11
##
## Call:
## lm(formula = writing_score ~ gender + nr_siblings, data = step_df)
##
## Residuals:
               1Q Median
                               3Q
                                      Max
## -63.397 -10.338
                   0.827 11.044 33.032
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                           2.1355 37.643 < 2e-16 ***
## (Intercept) 80.3850
## gender
               -8.6648
                           1.2366 -7.007 6.73e-12 ***
## nr_siblings 0.5590
                           0.4165
                                  1.342
                                             0.18
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

```
##
## Residual standard error: 14.93 on 584 degrees of freedom
## Multiple R-squared: 0.0812, Adjusted R-squared: 0.07806
## F-statistic: 25.81 on 2 and 584 DF, p-value: 1.821e-11
##
## Call:
## lm(formula = writing_score ~ gender + transport_means, data = step_df)
## Residuals:
##
                               3Q
      Min
               1Q Median
                                      Max
## -63.022 -10.197 0.978 10.978 35.902
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   81.3488
                               2.7755 29.310 < 2e-16 ***
                   -8.7252
                               1.2379 -7.049 5.12e-12 ***
## gender
## transport_means 0.1991
                               1.2655
                                      0.157
                                                 0.875
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.95 on 584 degrees of freedom
## Multiple R-squared: 0.07841,
                                   Adjusted R-squared: 0.07525
## F-statistic: 24.84 on 2 and 584 DF, p-value: 4.419e-11
##
## Call:
## lm(formula = writing_score ~ gender + wkly_study_hours, data = step_df)
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -64.774 -9.664 0.874 10.874 35.689
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
                                2.5677 30.629 < 2e-16 ***
## (Intercept)
                    78.6452
## gender
                    -8.8145
                                1.2356 -7.134 2.9e-12 ***
## wkly_study_hours
                    1.6476
                                0.9371
                                        1.758
                                                0.0793 .
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.91 on 584 degrees of freedom
## Multiple R-squared: 0.08322,
                                   Adjusted R-squared: 0.08008
## F-statistic: 26.51 on 2 and 584 DF, p-value: 9.578e-12
##
## Call:
## lm(formula = writing_score ~ gender + test_prep, data = step_df)
## Residuals:
##
      Min
               1Q Median
                               3Q
## -59.967 -9.747
                   1.033
                            9.143 32.095
##
```

```
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                96.714
                            2.795 34.605 < 2e-16 ***
                            1.188 -7.629 9.7e-14 ***
## gender
                -9.063
## test_prep
                -8.842
                            1.239 -7.139 2.8e-12 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.34 on 584 degrees of freedom
## Multiple R-squared: 0.1523, Adjusted R-squared: 0.1494
## F-statistic: 52.48 on 2 and 584 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep,
      data = step_df)
## Residuals:
      Min
               1Q Median
                               30
                                      Max
## -53.831 -8.831 0.523 10.523 31.585
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 82.055
                            3.197 25.665 < 2e-16 ***
                -9.567
                            1.128 -8.484 < 2e-16 ***
## gender
## lunch_type
                 9.645
                            1.178
                                   8.189 1.67e-15 ***
                            1.174 -7.791 3.05e-14 ***
                -9.151
## test_prep
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.59 on 583 degrees of freedom
## Multiple R-squared: 0.2398, Adjusted R-squared: 0.2359
## F-statistic: 61.3 on 3 and 583 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
      ethnic_group, data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -53.611 -8.743 0.158
                            9.306 30.331
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                74.6928
                            3.4518 21.639 < 2e-16 ***
## (Intercept)
## gender
                -9.5795
                            1.1045 -8.673 < 2e-16 ***
## lunch_type
                 9.4139
                                   8.154 2.17e-15 ***
                            1.1545
## test_prep
                -9.0404
                            1.1506 -7.857 1.91e-14 ***
## ethnic_group 2.3883
                            0.4711
                                   5.070 5.36e-07 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.31 on 582 degrees of freedom
```

```
## Multiple R-squared: 0.2719, Adjusted R-squared: 0.2669
## F-statistic: 54.35 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
##
      parent_educ, data = step_df)
## Residuals:
      Min
               1Q Median
                               30
                                      Max
## -48.527 -8.462
                   1.122
                            9.869 31.408
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 74.0611
                           3.3057 22.404 < 2e-16 ***
## gender
               -9.0877
                           1.0898 -8.339 5.44e-16 ***
## lunch_type
                9.7157
                           1.1358
                                   8.554 < 2e-16 ***
               -9.2954
                           1.1328 -8.206 1.48e-15 ***
## test_prep
## parent_educ 2.4286
                           0.3623
                                   6.703 4.83e-11 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.11 on 582 degrees of freedom
## Multiple R-squared: 0.2943, Adjusted R-squared: 0.2894
## F-statistic: 60.67 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
      parent_marital_status, data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               30
                                      Max
## -54.489 -8.733 0.295 10.431 31.714
##
## Coefficients:
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         80.2119
                                     3.7267 21.524 < 2e-16 ***
## gender
                         -9.5312
                                     1.1284 -8.447 2.40e-16 ***
                                             8.215 1.38e-15 ***
## lunch_type
                          9.6811
                                     1.1785
## test_prep
                         -9.1130
                                     1.1752 -7.754 4.00e-14 ***
## parent_marital_status
                         0.7844
                                     0.8146
                                              0.963
                                                       0.336
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.59 on 582 degrees of freedom
## Multiple R-squared: 0.241, Adjusted R-squared: 0.2358
## F-statistic: 46.2 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
      practice sport, data = step df)
```

```
##
## Residuals:
      Min
               1Q Median
                               30
## -53.946 -8.831 0.403 10.517 31.475
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
                              3.7848 21.584 < 2e-16 ***
## (Intercept)
                  81.6893
## gender
                  -9.5689
                              1.1287 -8.478 < 2e-16 ***
## lunch_type
                  9.6514
                              1.1793
                                      8.184 1.74e-15 ***
## test_prep
                  -9.1478
                              1.1756 -7.781 3.29e-14 ***
                              0.8649
                                               0.856
## practice_sport
                  0.1566
                                     0.181
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.6 on 582 degrees of freedom
## Multiple R-squared: 0.2398, Adjusted R-squared: 0.2346
## F-statistic: 45.91 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
##
      is_first_child, data = step_df)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -53.971 -8.971 0.389 10.403 31.857
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                  81.3888
                              3.8074 21.376 < 2e-16 ***
## gender
                  -9.5713
                              1.1286 -8.480 < 2e-16 ***
## lunch_type
                   9.6400
                              1.1788
                                     8.178 1.82e-15 ***
## test_prep
                  -9.1306
                              1.1771 -7.757 3.91e-14 ***
## is_first_child
                  0.3871
                              1.1987
                                     0.323
                                               0.747
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.6 on 582 degrees of freedom
## Multiple R-squared: 0.2399, Adjusted R-squared: 0.2347
## F-statistic: 45.93 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
      nr_siblings, data = step_df)
##
## Residuals:
               10 Median
                               3Q
      Min
                                      Max
## -54.183 -8.822
                   0.580 10.432 31.251
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 81.0394
                           3.3375 24.282 < 2e-16 ***
```

```
## gender
               -9.5231
                           1.1283 -8.440 2.53e-16 ***
## lunch_type
                9.6385
                           1.1777
                                    8.184 1.74e-15 ***
## test_prep
               -9.0891
                           1.1758
                                   -7.730 4.75e-14 ***
## nr_siblings
                0.4023
                           0.3796
                                    1.060
                                              0.29
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.59 on 582 degrees of freedom
## Multiple R-squared: 0.2413, Adjusted R-squared: 0.236
## F-statistic: 46.26 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
##
      transport_means, data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -54.114 -8.753 0.370 10.598 32.008
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
                   80.9705
## (Intercept)
                               3.6093 22.434 < 2e-16 ***
## gender
                   -9.5797
                               1.1284 -8.490 < 2e-16 ***
## lunch_type
                    9.6383
                               1.1784
                                       8.179 1.81e-15 ***
## test_prep
                   -9.2062
                               1.1782
                                      -7.814 2.60e-14 ***
## transport_means 0.7488
                               1.1540
                                       0.649
                                                 0.517
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.6 on 582 degrees of freedom
## Multiple R-squared: 0.2403, Adjusted R-squared: 0.2351
## F-statistic: 46.03 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
      wkly_study_hours, data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -55.020 -8.634
                   0.366 10.344 31.608
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
                                3.6464 21.927 < 2e-16 ***
## (Intercept)
                    79.9537
## gender
                    -9.6192
                                1.1281
                                       -8.527 < 2e-16 ***
                     9.6405
                                1.1774
                                         8.188 1.69e-15 ***
## lunch_type
                    -9.0175
                                1.1793 -7.646 8.60e-14 ***
## test_prep
## wkly_study_hours
                    1.0266
                                0.8576
                                         1.197
                                                  0.232
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.59 on 582 degrees of freedom
```

```
## Multiple R-squared: 0.2417, Adjusted R-squared: 0.2364
## F-statistic: 46.37 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
##
      parent_educ, data = step_df)
## Residuals:
      Min
               1Q Median
                               30
                                      Max
## -48.527 -8.462
                   1.122
                            9.869 31.408
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 74.0611
                           3.3057 22.404 < 2e-16 ***
## gender
               -9.0877
                           1.0898 -8.339 5.44e-16 ***
## lunch_type
                9.7157
                           1.1358
                                    8.554 < 2e-16 ***
               -9.2954
                           1.1328 -8.206 1.48e-15 ***
## test_prep
## parent_educ
               2.4286
                           0.3623
                                   6.703 4.83e-11 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 13.11 on 582 degrees of freedom
## Multiple R-squared: 0.2943, Adjusted R-squared: 0.2894
## F-statistic: 60.67 on 4 and 582 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
      parent_educ + ethnic_group, data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               30
                                      Max
## -48.594 -8.422 0.710
                            9.201 29.415
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                            3.5050 19.332 < 2e-16 ***
## (Intercept)
                67.7575
                -9.1231
                            1.0701 -8.526 < 2e-16 ***
## gender
                 9.5016
                                    8.513 < 2e-16 ***
## lunch_type
                            1.1161
## test_prep
                -9.1875
                            1.1125 -8.258 9.99e-16 ***
                 2.3061
                            0.3567
                                     6.466 2.14e-10 ***
## parent_educ
                            0.4566
## ethnic_group
                 2.1756
                                   4.765 2.39e-06 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 12.87 on 581 degrees of freedom
## Multiple R-squared: 0.3208, Adjusted R-squared: 0.315
## F-statistic: 54.89 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
```

```
##
       parent_educ + parent_marital_status, data = step_df)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -49.111 -8.640
                    1.036
                             9.795 31.521
##
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                          72.4812
                                      3.7758 19.196 < 2e-16 ***
## gender
                          -9.0578
                                      1.0906 -8.305 7.02e-16 ***
## lunch_type
                           9.7468
                                      1.1367
                                               8.575 < 2e-16 ***
                          -9.2621
                                      1.1337
                                             -8.170 1.94e-15 ***
## test_prep
## parent_educ
                           2.4224
                                      0.3625
                                               6.683 5.49e-11 ***
                                               0.867
                                                        0.387
## parent_marital_status
                           0.6809
                                      0.7858
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 13.11 on 581 degrees of freedom
## Multiple R-squared: 0.2952, Adjusted R-squared: 0.2891
## F-statistic: 48.67 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
       parent_educ + practice_sport, data = step_df)
##
## Residuals:
      Min
                10 Median
                                3Q
                                       Max
                             9.907 31.045
## -48.874 -8.565
                    1.021
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   72.8024
                               3.8806 18.761 < 2e-16 ***
                               1.0904 -8.337 5.53e-16 ***
                   -9.0908
## gender
## lunch_type
                    9.7369
                               1.1370
                                        8.564 < 2e-16 ***
## test_prep
                   -9.2862
                               1.1335 -8.192 1.64e-15 ***
                    2.4431
                                        6.725 4.20e-11 ***
## parent_educ
                               0.3633
                    0.5182
                               0.8356
                                        0.620
                                                 0.535
## practice_sport
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.11 on 581 degrees of freedom
## Multiple R-squared: 0.2947, Adjusted R-squared: 0.2887
## F-statistic: 48.56 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
       parent_educ + is_first_child, data = step_df)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
  -48.647 -8.375
                    1.027
                             9.788
                                   31.641
##
```

```
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                              3.8563 19.058 < 2e-16 ***
                 73.4943
                  -9.0914
                              1.0907 -8.335 5.62e-16 ***
## gender
## lunch_type
                   9.7114
                              1.1368
                                       8.542 < 2e-16 ***
                              1.1353 -8.172 1.90e-15 ***
## test_prep
                  -9.2781
                                       6.695 5.08e-11 ***
## parent educ
                   2.4278
                              0.3626
## is_first_child
                  0.3307
                              1.1560
                                       0.286
                                                0.775
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.12 on 581 degrees of freedom
## Multiple R-squared: 0.2944, Adjusted R-squared: 0.2883
## F-statistic: 48.48 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
##
       parent_educ + nr_siblings, data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               30
                                      Max
## -48.897 -8.679
                            9.568 31.042
                    0.964
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                           3.4363 21.222 < 2e-16 ***
## (Intercept) 72.9266
## gender
               -9.0381
                           1.0902 -8.291 7.85e-16 ***
                                    8.551 < 2e-16 ***
## lunch_type
                9.7086
                           1.1354
                -9.2282
                           1.1337 -8.140 2.42e-15 ***
## test_prep
                2.4353
                           0.3622
                                     6.723 4.25e-11 ***
## parent_educ
## nr_siblings
                0.4404
                           0.3660
                                    1.203
                                             0.229
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 13.1 on 581 degrees of freedom
## Multiple R-squared: 0.296, Adjusted R-squared:
## F-statistic: 48.86 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
       parent_educ + transport_means, data = step_df)
##
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -48.788 -8.350
                   1.076
                            9.626 31.792
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                   73.0836
                               3.6747 19.888 < 2e-16 ***
## gender
                   -9.0996
                               1.0906 -8.344 5.25e-16 ***
## lunch_type
                    9.7095
                               1.1365
                                       8.543 < 2e-16 ***
## test_prep
                               1.1364 -8.224 1.29e-15 ***
                   -9.3455
```

```
2.4265
                               0.3625
                                        6.693 5.14e-11 ***
## parent educ
                                       0.610
                                                 0.542
## transport_means
                    0.6794
                               1.1129
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.12 on 581 degrees of freedom
## Multiple R-squared: 0.2947, Adjusted R-squared: 0.2887
## F-statistic: 48.56 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
       parent_educ + wkly_study_hours, data = step_df)
##
## Residuals:
##
      Min
                10 Median
                               3Q
                                      Max
## -49.897 -8.394
                    0.862
                            9.572 31.435
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                3.7299 19.171 < 2e-16 ***
                    71.5065
                                1.0894 -8.395 3.56e-16 ***
## gender
                    -9.1459
                                         8.558 < 2e-16 ***
## lunch_type
                     9.7108
                                1.1347
## test_prep
                    -9.1382
                                1.1367 -8.039 5.08e-15 ***
                     2.4469
                                0.3622
                                         6.756 3.44e-11 ***
## parent_educ
                     1.2185
                                0.8270
                                         1.473
                                                  0.141
## wkly_study_hours
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.09 on 581 degrees of freedom
## Multiple R-squared: 0.2969, Adjusted R-squared: 0.2909
## F-statistic: 49.07 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
##
       parent_educ + ethnic_group, data = step_df)
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -48.594 -8.422
                   0.710
                            9.201 29.415
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                67.7575
                            3.5050 19.332 < 2e-16 ***
                -9.1231
                            1.0701 -8.526 < 2e-16 ***
## gender
## lunch_type
                 9.5016
                            1.1161
                                     8.513 < 2e-16 ***
                -9.1875
                            1.1125 -8.258 9.99e-16 ***
## test_prep
## parent_educ
                 2.3061
                            0.3567
                                     6.466 2.14e-10 ***
## ethnic_group
                 2.1756
                            0.4566
                                    4.765 2.39e-06 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 12.87 on 581 degrees of freedom
```

```
## Multiple R-squared: 0.3208, Adjusted R-squared: 0.315
## F-statistic: 54.89 on 5 and 581 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
##
       parent_educ + ethnic_group + parent_marital_status, data = step_df)
##
## Residuals:
      Min
                10 Median
                                3Q
                                       Max
                                    29.473
                    0.835
                             9.426
## -49.269 -8.482
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          65.8964
                                      3.9529
                                             16.670 < 2e-16 ***
                                      1.0706 -8.490 < 2e-16 ***
                         -9.0888
## gender
## lunch_type
                          9.5362
                                      1.1166
                                              8.540 < 2e-16 ***
                                      1.1131
                                             -8.219 1.35e-15 ***
## test_prep
                          -9.1484
## parent_educ
                          2.2982
                                      0.3567
                                              6.442 2.47e-10 ***
## ethnic_group
                                      0.4567
                                              4.792 2.10e-06 ***
                           2.1888
## parent_marital_status
                          0.7856
                                      0.7717
                                              1.018
                                                       0.309
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 12.87 on 580 degrees of freedom
## Multiple R-squared: 0.322, Adjusted R-squared: 0.315
## F-statistic: 45.92 on 6 and 580 DF, p-value: < 2.2e-16
##
## Call:
  lm(formula = writing_score ~ gender + lunch_type + test_prep +
       parent_educ + ethnic_group + practice_sport, data = step_df)
##
## Residuals:
                1Q Median
                                3Q
      Min
                                       Max
## -48.933 -8.411
                    0.853
                            9.389
                                    29.030
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   66.5308
                              4.0315 16.503 < 2e-16 ***
## gender
                   -9.1262
                              1.0706 -8.524 < 2e-16 ***
## lunch_type
                   9.5224
                              1.1173
                                       8.523 < 2e-16 ***
## test_prep
                   -9.1785
                              1.1132 -8.245 1.11e-15 ***
## parent_educ
                    2.3203
                               0.3576
                                        6.489 1.86e-10 ***
                    2.1747
                               0.4568
                                        4.761 2.44e-06 ***
## ethnic_group
## practice_sport
                   0.5060
                               0.8204
                                        0.617
                                                 0.538
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 12.88 on 580 degrees of freedom
## Multiple R-squared: 0.3213, Adjusted R-squared: 0.3142
## F-statistic: 45.75 on 6 and 580 DF, p-value: < 2.2e-16
```

```
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
      parent_educ + ethnic_group + is_first_child, data = step_df)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -48.716 -8.536
                    0.728
                             9.239
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                  67.1816
                              4.0118 16.746 < 2e-16 ***
                               1.0710 -8.522 < 2e-16 ***
                   -9.1269
## gender
## lunch_type
                   9.4971
                               1.1171
                                       8.501 < 2e-16 ***
## test_prep
                   -9.1698
                              1.1150 -8.224 1.29e-15 ***
                   2.3054
                               0.3570
                                       6.458 2.24e-10 ***
## parent_educ
## ethnic_group
                    2.1757
                               0.4569
                                        4.762 2.43e-06 ***
                               1.1350
                                       0.296
## is_first_child
                   0.3357
                                                 0.767
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 12.88 on 580 degrees of freedom
## Multiple R-squared: 0.3209, Adjusted R-squared: 0.3139
## F-statistic: 45.68 on 6 and 580 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
##
       parent_educ + ethnic_group + nr_siblings, data = step_df)
##
## Residuals:
##
      Min
                                3Q
                1Q Median
                                       Max
                    0.877
## -49.002 -8.116
                             9.056
                                    28.949
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 66.4622
                             3.6317 18.301 < 2e-16 ***
                             1.0701 -8.475 < 2e-16 ***
## gender
                -9.0688
                 9.4922
                             1.1154
                                     8.510 < 2e-16 ***
## lunch_type
## test prep
                 -9.1126
                             1.1131 -8.187 1.71e-15 ***
                             0.3564
                                    6.488 1.87e-10 ***
## parent_educ
                 2.3127
## ethnic_group
                 2.1915
                             0.4564
                                    4.802 2.01e-06 ***
## nr_siblings
                 0.4849
                             0.3594
                                    1.349
                                               0.178
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 12.86 on 580 degrees of freedom
## Multiple R-squared: 0.3229, Adjusted R-squared: 0.3159
## F-statistic: 46.11 on 6 and 580 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
       parent_educ + ethnic_group + transport_means, data = step_df)
##
```

```
## Residuals:
##
               1Q Median
      Min
                               30
                                      Max
                            9.219 29.122
## -48.917 -8.476 0.575
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
                               3.8595 17.235 < 2e-16 ***
## (Intercept)
                   66.5192
                               1.0706 -8.535 < 2e-16 ***
## gender
                   -9.1379
## lunch_type
                    9.4928
                               1.1166
                                       8.502 < 2e-16 ***
## test_prep
                   -9.2487
                               1.1157 -8.289 7.95e-16 ***
## parent_educ
                    2.3030
                               0.3568
                                       6.454 2.30e-10 ***
                                       4.785 2.18e-06 ***
                               0.4569
## ethnic_group
                    2.1863
## transport_means
                    0.8391
                               1.0930
                                       0.768
                                                 0.443
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 12.87 on 580 degrees of freedom
## Multiple R-squared: 0.3215, Adjusted R-squared: 0.3145
## F-statistic: 45.81 on 6 and 580 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = writing_score ~ gender + lunch_type + test_prep +
      parent_educ + ethnic_group + wkly_study_hours, data = step_df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -49.917 -8.391
                    0.613
                            9.143 29.293
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
                                3.8874 16.801 < 2e-16 ***
## (Intercept)
                    65.3125
## gender
                    -9.1792
                                1.0698 -8.581 < 2e-16 ***
## lunch_type
                     9.4976
                                1.1151
                                         8.517 < 2e-16 ***
## test_prep
                    -9.0360
                                1.1163 -8.094 3.40e-15 ***
## parent_educ
                     2.3242
                                0.3566
                                        6.519 1.54e-10 ***
                     2.1684
                                0.4562
                                         4.753 2.53e-06 ***
## ethnic_group
                    1.1762
## wkly_study_hours
                                0.8121
                                         1.448
                                                  0.148
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 12.86 on 580 degrees of freedom
## Multiple R-squared: 0.3233, Adjusted R-squared: 0.3163
## F-statistic: 46.18 on 6 and 580 DF, p-value: < 2.2e-16
## Start: AIC=3222.53
## writing_score ~ 1
##
##
                          Df Sum of Sq
                                          RSS
## + gender
                           1 11104.5 130592 3176.6
## + lunch_type
                           1
                               10442.9 131253 3179.6
## + test_prep
                           1 9618.7 132078 3183.3
## + parent educ
                           1 8420.5 133276 3188.6
## + ethnic_group
                           1 5344.3 136352 3202.0
```

```
## + nr siblings
                                 560.4 141136 3222.2
## <none>
                                       141696 3222.5
## + wkly_study_hours
                                472.0 141224 3222.6
## + parent_marital_status 1
                               275.4 141421 3223.4
                               95.4 141601 3224.1
## + is first child
                          1
## + transport means
                                0.6 141696 3224.5
                          1
## + practice sport
                          1
                                0.0 141696 3224.5
##
## Step: AIC=3176.62
## writing_score ~ gender
##
                          Df Sum of Sq
##
                                         RSS
                                                AIC
## + lunch_type
                               11657.0 118935 3123.7
                          1 10482.9 120109 3129.5
## + test_prep
## + parent_educ
                          1 7206.7 123385 3145.3
                             5423.0 125169 3153.7
## + ethnic_group
                           1
## + wkly_study_hours
                          1 687.6 129904 3175.5
## <none>
                                      130592 3176.6
## + nr siblings
                          1
                               401.5 130190 3176.8
                               171.1 130421 3177.9
## + parent marital status 1
## + is_first_child
                          1
                               127.2 130465 3178.0
## + transport_means
                          1
                                5.5 130586 3178.6
                                0.6 130591 3178.6
## + practice_sport
                          1
##
## Step: AIC=3123.74
## writing_score ~ gender + lunch_type
##
                          Df Sum of Sq
##
                                         RSS
## + test_prep
                          1 11216.2 107719 3067.6
## + parent_educ
                          1
                             7367.0 111568 3088.2
## + ethnic_group
                          1
                             4829.4 114105 3101.4
                          1 686.4 118248 3122.3
## + wkly_study_hours
## <none>
                                       118935 3123.7
                             385.6 118549 3123.8
276.7 118658 3124.4
100.6 118834 3125.2
## + nr_siblings
                           1
## + parent_marital_status 1
## + is_first_child
                          1
## + practice sport
                          1
                                15.9 118919 3125.7
## + transport_means
                          1
                                 1.3 118933 3125.7
##
## Step: AIC=3067.59
## writing_score ~ gender + lunch_type + test_prep
##
##
                          Df Sum of Sa
                                         RSS
## + parent_educ
                          1
                                7719.9 99999 3025.9
                                4556.1 103162 3044.2
## + ethnic_group
                          1
                                       107719 3067.6
## <none>
                               264.6 107454 3068.2
## + wkly_study_hours
                          1
                               207.4 107511 3068.5
## + nr_siblings
                           1
## + parent_marital_status 1
                               171.3 107547 3068.7
                               77.9 107641 3069.2
## + transport_means
                           1
                                19.3 107699 3069.5
## + is_first_child
                           1
## + practice_sport
                          1
                                6.1 107713 3069.6
##
## Step: AIC=3025.94
```

```
## writing_score ~ gender + lunch_type + test_prep + parent_educ
##
                           Df Sum of Sq
##
                                           RSS
## + ethnic_group
                                  3761.0 96238 3005.4
                            1
## + wkly study hours
                                   372.2 99626 3025.8
## <none>
                                         99999 3025.9
## + nr siblings
                            1
                                   248.6 99750 3026.5
## + parent marital status
                            1
                                   129.1 99870 3027.2
## + practice sport
                            1
                                    66.2 99933 3027.6
## + transport_means
                            1
                                    64.1 99935 3027.6
## + is_first_child
                            1
                                    14.1 99985 3027.9
##
## Step: AIC=3005.44
## writing_score ~ gender + lunch_type + test_prep + parent_educ +
##
       ethnic_group
##
##
                           Df Sum of Sq
                                           RSS
                                                  AIC
## + wkly_study_hours
                                  346.82 95891 3005.3
                                         96238 3005.4
## <none>
                                  301.18 95936 3005.6
## + nr siblings
## + parent_marital_status
                           1
                                  171.69 96066 3006.4
## + transport means
                            1
                                   97.68 96140 3006.8
## + practice_sport
                            1
                                   63.09 96175 3007.1
## + is first child
                            1
                                   14.52 96223 3007.3
##
## Step: AIC=3005.32
## writing_score ~ gender + lunch_type + test_prep + parent_educ +
       ethnic_group + wkly_study_hours
##
##
                           Df Sum of Sq
##
                                           RSS
                                                  AIC
## <none>
                                         95891 3005.3
## + nr_siblings
                                 270.733 95620 3005.7
                            1
## + parent_marital_status
                            1
                                 175.061 95716 3006.2
## + transport_means
                            1
                                  84.868 95806 3006.8
## + practice sport
                            1
                                  58.664 95832 3007.0
## + is_first_child
                                  13.991 95877 3007.2
                            1
```

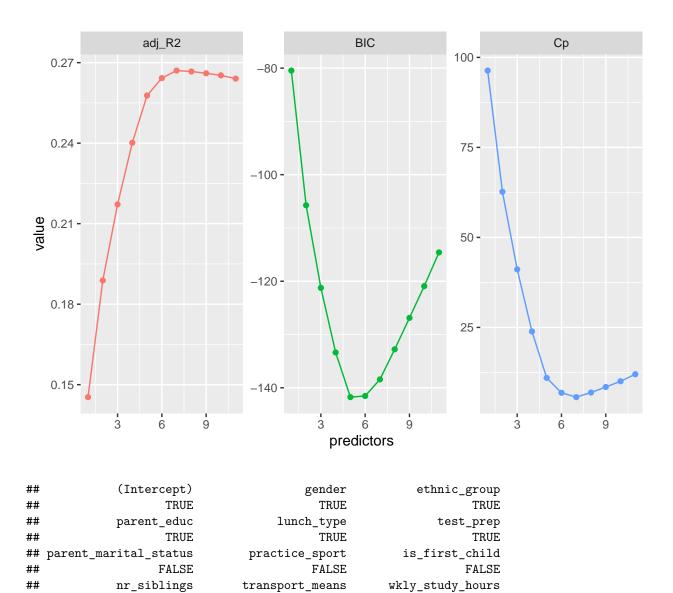
The model we obtained is Writing Score \sim Lunch Type + Ethnic Group + Test Prep + Gender + Parent Education + Weekly Study Hours.

When using the single-function method, the model obtained with the lowest AIC was Writing Score \sim Gender + Lunch Type + Test Prep + Parent Education + Ethnic Group + Weekly Study Hours. Both models had R-squared values and MSEs within 0.6 points of each other.

It seems that when using the single-function method, for all scores and for both forwards and backwards elimination, extra variables were included despite their individual p-values > 0.05; therefore the manually-selected models should be used for comparison and validation.

Criteria-based approach - Adjusted R², Cp, BIC

(Note: BIC has a larger penalty, leading to less predictors present within the model.) Math Score



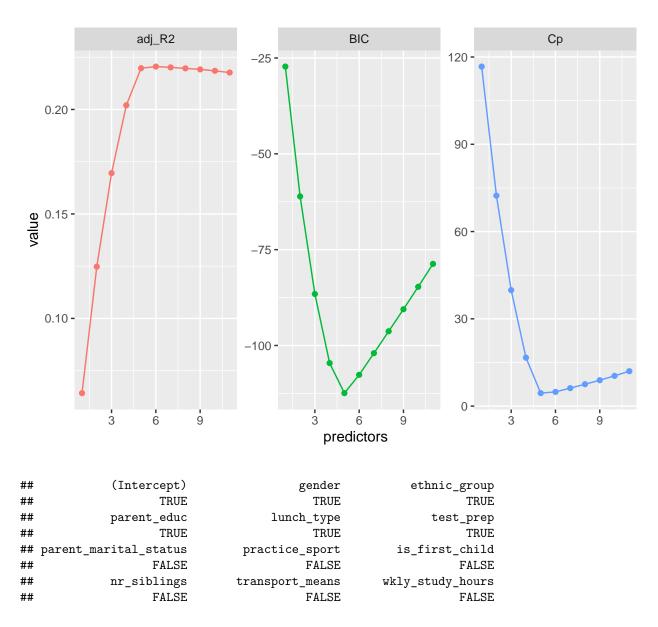
To predict math score, the adjusted R^2 statistic, Cp, and BIC plots in combination show that a 7-variable model is optimal. The predictors selected are: gender, ethnic_group, parent_educ, lunch_type, test_prep, nr_siblings, and wkly study_hours.

FALSE

TRUE

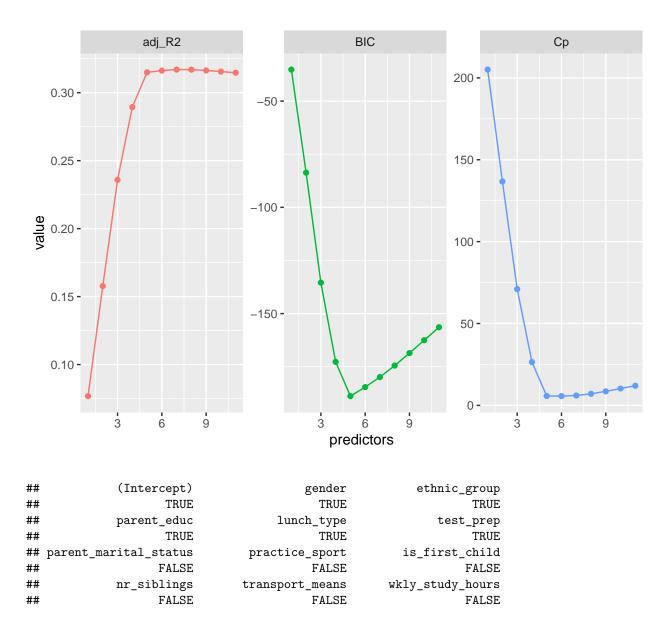
Reading Score

TRUE



To predict reading score, the adjusted R^2 statistic and Cp and BIC plots shows that a 5-variable model is optimal. The predictors selected are: gender, ethnic_group, parent_educ, lunch_type, test_prep.

Writing Score

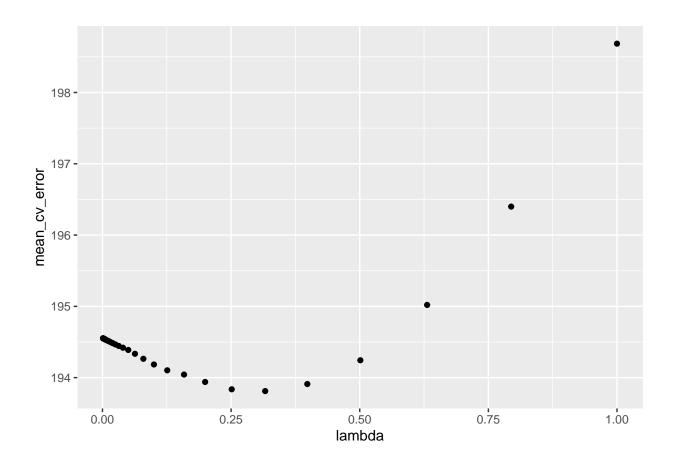


To predict writing score, the adjusted R^2, Cp, and BIC statistics show that a 5-variable model is optimal. The predictors selected are: gender, ethnic_group, parent_educ, lunch_type, test_prep

Limitation: noting that the plots maximum and minimum are not that obvious.

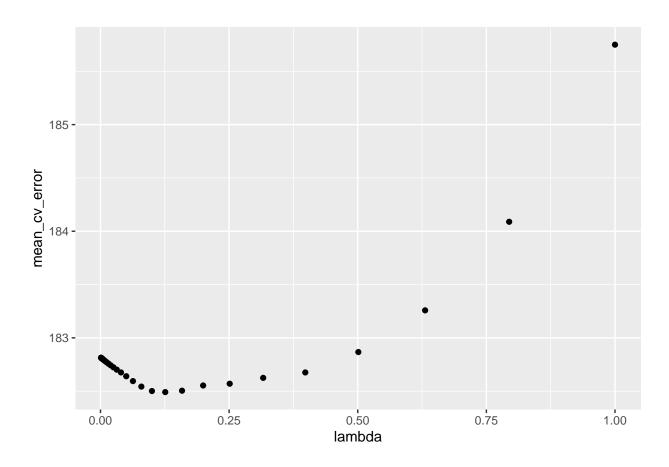
LASSO approach -

Maths score:



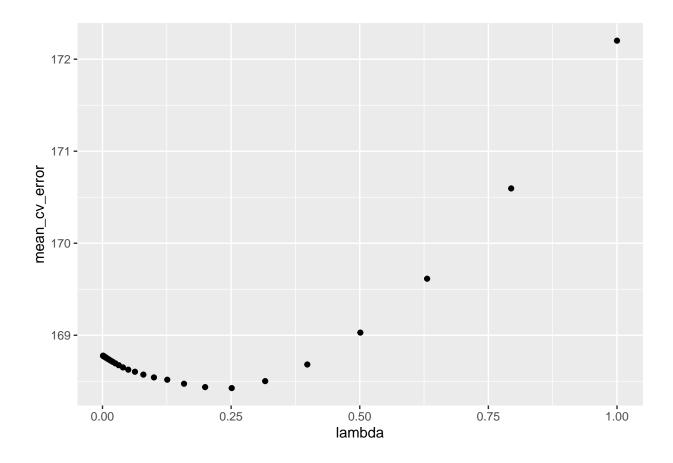
```
## 12 x 1 sparse Matrix of class "dgCMatrix"
## (Intercept)
                         30.9514949
## gender
                          4.6893056
## ethnic_group
                          2.5085903
## parent_educ
                          1.2932847
## lunch_type
                         11.9603880
## test_prep
                         -4.7061459
## parent_marital_status  0.2406793
## practice_sport
                          0.1053101
## is_first_child
## nr_siblings
                          0.4775542
## transport_means
## wkly_study_hours
                          1.6725295
```

Reading score:



```
## 12 x 1 sparse Matrix of class "dgCMatrix"
## (Intercept)
                         63.0168462
## gender
                         -7.2578814
## ethnic_group
                          1.7148165
## parent_educ
                          1.6792539
## lunch_type
                          8.3560449
## test_prep
                         -6.4054407
## parent_marital_status  0.3113991
## practice_sport
                         -0.5218650
## is_first_child
                          0.6325478
## nr_siblings
                          0.2364662
## transport_means
                          0.6090418
## wkly_study_hours
                          0.8425385
```

Writing score:



```
## 12 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept)
                         64.24045111
                         -8.58684295
## gender
## ethnic_group
                          2.00086017
## parent_educ
                          2.16675381
## lunch_type
                          8.95045903
## test_prep
                         -8.47239858
## parent_marital_status  0.40572033
## practice_sport
                          0.04910284
## is_first_child
## nr_siblings
                          0.29894240
## transport_means
                          0.22598323
## wkly_study_hours
                          0.76604805
```

Cross Validation

Here are the summary of all the models that have been created in this project.

We will be performing cross validation to select the best model resulted from the models above.

subject	method	(Intercept)	gender	ethnic_group	parent_educ	lunch_type	test_prep	parent_marital_statusX	practice_sport	is_first_child	nr_siblings	transport_means	wkly_study_hours
math	theoretical	X	X	X	X	X	X	l	X	X	X	X	X
math	backward_manual	X	X	X	X	X	X	NA	NA	NA	NA	NA	X
math	backward_func	X	X	X	X	X	X	NA	NA	NA	X	NA	X
math	forward_manual	X	X	X	X	X	X	NA	NA	NA	NA	NA	X
math	forward_func	X	X	X	X	X	X	NA	NA	NA	X	NA	X
math	criteria	X	X	X	X	X	X	NA	NA	NA	X	NA	NA
reading	theoretical	X	X	X	X	X	X	X	X	X	X	X	X
reading	backward_manual	X	X	X	X	X	X	NA	NA	NA	NA	NA	NA
reading	backward_func	X	X	X	X	X	X	NA	NA	NA	NA	NA	NA
reading	forward_manual	X	X	X	X	X	X	NA	NA	NA	NA	NA	NA
reading	forward_func	X	X	X	X	X	X	NA	NA	NA	NA	NA	NA
reading	criteria	X	X	X	X	X	X	NA	NA	NA	NA	NA	NA
writing	theoretical	X	X	X	X	X	X	X	X	X	X	X	X
writing	backward_manual	X	X	X	X	X	X	NA	NA	NA	NA	NA	NA
writing	backward_func	X	X	X	X	X	X	NA	NA	NA	NA	NA	X
writing	forward_manual	X	X	X	X	X	X	NA	NA	NA	NA	NA	NA
writing	forward_func	X	X	X	X	X	X	NA	NA	NA	NA	NA	X
writing	criteria	X	X	X	X	X	X	NA	NA	NA	NA	NA	NA

Method from the lecture code

Method using crossv_mc

Notice how practice_sport and transport_means are not selected in any of the model selections methods. This will be reported at the effect modifier section.

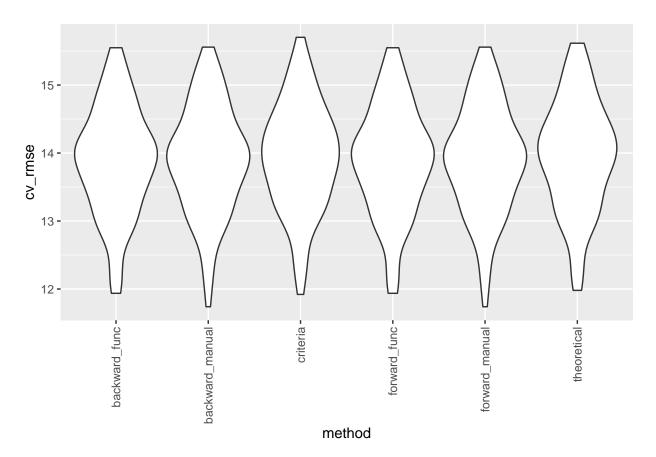
Cross Validation - Math

Method from the lecture codes

method	RMSE
theoretical	13.96975
backward_manual	13.82973
backward_func	13.84664
forward_manual	13.88238
forward_func	13.89506
criteria	13.9035

The model with the best RMSE for Math is math_score \sim gender + ethnic_group + parent_educ + lunch_type + test_prep + wkly_study_hours, which uses backward_manual as a method of approach.

$Method\ using\ crossv_mc$



411	
method	average_rmse
backward_func	13.88519
backward_manual	13.89653
criteria	13.94264
forward_func	13.88519
forward_manual	13.89653
theoretical	13.96494

We noticed that the best model is the one that uses forward elimination with one line code and backward elimination with one line code. The model is math_score \sim lunch_type + ethnic_group + test_prep + gender + parent_educ + wkly_study_hours + nr_siblings

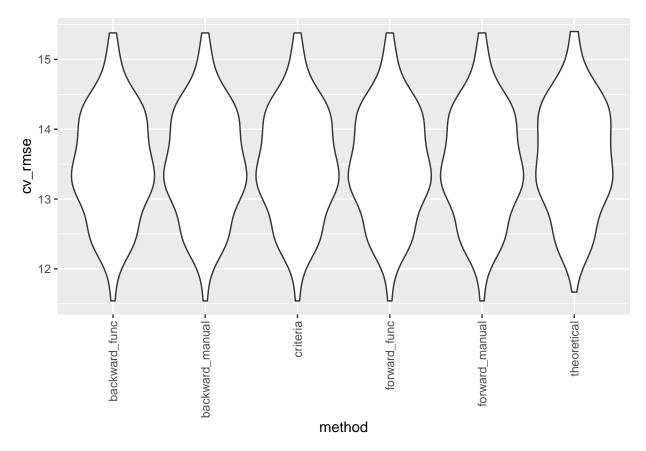
Cross Validation - Reading

Method from the lecture codes

method	RMSE
theoretical	13.53786
backward_manual	13.42876
backward_func	13.53256
forward_manual	13.42892
forward_func	13.40176
criteria	13.53827

The model with the best MSE for Reading is reading_score \sim lunch_type + gender + test_prep + parent_educ + ethnic_group, which uses forward_func as a method of approach.

Method using crossv_mc



method	average_rmse
backward_func	13.49136
backward_manual	13.49136
criteria	13.49136
forward_func	13.49136
forward_manual	13.49136
theoretical	13.57974

We noticed that the best model is the model that is picked by forward and backward elimination method and criterion based approach. The model is reading_score \sim lunch_type + gender + test_prep + parent_educ + ethnic_group

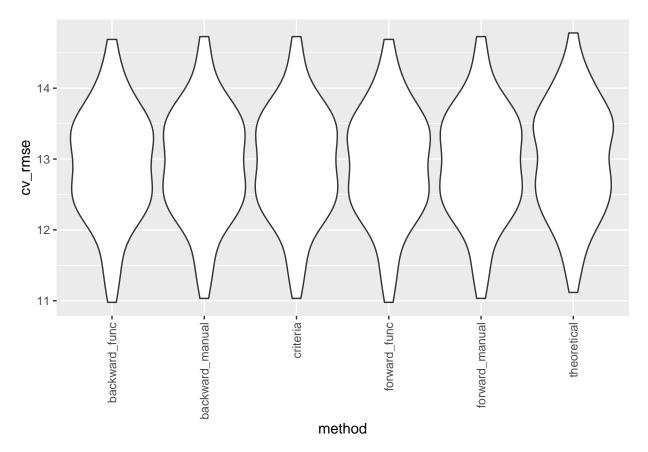
Cross Validation - Writing

Method from the lecture codes

method	RMSE
theoretical	12.95331
backward_manual	12.93239
backward_func	12.90413
forward_manual	12.88047
forward_func	12.90165
criteria	12.9846

The model with the best RMSE for Writing is writing_score \sim gender + lunch_type + test_prep + parent_educ + ethnic_group, which uses forward_manual as a method of approach.

Method using crossv_mc



method	average_rmse
backward_func	12.91828
backward_manual	12.92630
criteria	12.92630
forward_func	12.91828
forward_manual	12.92630
theoretical	12.99816

We noticed that the best model is the one that uses forward elimination with one line code and backward elimination with one line code. The model is writing_score \sim gender + lunch_type + test_prep + parent_educ + ethnic_group + wkly_study_hours

Effect Modifier

We will take a logical approach to get the effect modification within the variables.

• The variables provided to measure the scores are gender, ethnic_group, parent_educ, lunch_type, test_prep, parent_marital_status, practice_sport, is_first_child, nr_siblings, transport_means, wkly_study_hours. is_first_child and the nr_siblings can be related since if the person have no siblings, then the probability that they are the first child is 1.

Table 1: Math: Effect Modifiers

term	estimate	std.error	statistic	p.value

Table 2: Math: Effect Modifiers

term	df	sumsq	meansq	statistic	p.value
gender:parent_educ:wkly_study_hours	1	897.5483	897.5483	4.631138	0.0319176
lunch_type:parent_educ:nr_siblings	1	813.4566	813.4566	4.197245	0.0410579
ethnic_group:parent_educ:nr_siblings	1	1071.3950	1071.3950	5.528146	0.0191349
ethnic_group:test_prep:gender:parent_educ	1	863.8791	863.8791	4.457413	0.0352901
test_prep:parent_educ:wkly_study_hours:nr_siblings	1	826.2449	826.2449	4.263230	0.0395069

- If the person practice sports(practice_sport, then they are less likely to take the bus (transport_means) back to their location.
- gender, ethnic_group, parent_educ, parent_marital_status, transport_means can all affect the person's family financial background. This can be reflected directly with lunch_type. We will only evaluate the effect of gender, ethnic_group on lunch_type.
- practice_sport can affect the wkly_study_hours as the sports will take up chunks of time to study.

The models that will be used in the effect modifier section are the models that are selected using crossv_mc() function, i.e.

 $math_score \sim lunch_type + ethnic_group + test_prep + gender + parent_educ + wkly_study_hours + nr_siblings$

 $reading_score \sim lunch_type + gender + test_prep + parent_educ + ethnic_group$

 $writing_score \sim gender + lunch_type + test_prep + parent_educ + ethnic_group + wkly_study_hours$

Here are the procedures for identifying effect modifiers and find confounders of the Here are all the possible effect interactions if we load in all of the predictors.

Confounder

Confounding - Math

gender, test_prep -> wkly_study_hours test_prep -> nr_siblings

Confounding - Reading

We don't have any confounders for reading score

Table 3: Reading: Effect Modifiers

term	estimate	std.error	statistic	p.value
gender:test_prep:parent_educ	-33.40163	16.725711	-1.997023	0.0463105
gender:parent_educ:ethnic_group	-18.01760	8.758346	-2.057193	0.0401344
gender:test_prep:parent_educ:ethnic_group	11.49205	5.215602	2.203399	0.0279767

Table 4: Reading: Effect Modifiers

term	df	sumsq	meansq	statistic	p.value
------	----	-------	--------	-----------	---------

Table 5: Writing: Effect Modifiers

term	estimate	std.error	statistic	p.value
gender:parent_educ	209.92353	101.75896	2.062949	0.0396106
gender:ethnic_group	264.43446	104.48977	2.530721	0.0116750
lunch_type:ethnic_group	219.15381	102.26064	2.143091	0.0325666
test_prep:ethnic_group	225.26774	93.16287	2.417999	0.0159468
parent_educ:ethnic_group	128.59525	51.38254	2.502703	0.0126289
ethnic_group:wkly_study_hours	176.64885	79.70299	2.216339	0.0270979
gender:lunch_type:ethnic_group	-136.89072	64.06973	-2.136590	0.0330948
gender:test_prep:ethnic_group	-140.46161	61.08977	-2.299266	0.0218830
lunch_type:test_prep:ethnic_group	-116.03710	57.16244	-2.029954	0.0428669
gender:parent_educ:ethnic_group	-84.44651	32.57196	-2.592614	0.0097915
lunch_type:parent_educ:ethnic_group	-65.47354	30.63015	-2.137552	0.0330161
test_prep:parent_educ:ethnic_group	-70.55002	29.42971	-2.397238	0.0168690
gender:ethnic_group:wkly_study_hours	-111.42142	50.74926	-2.195528	0.0285643
test_prep:ethnic_group:wkly_study_hours	-93.44450	45.77314	-2.041470	0.0417054
parent_educ:ethnic_group:wkly_study_hours	-51.09440	23.81042	-2.145884	0.0323418
gender:lunch_type:parent_educ:ethnic_group	41.96424	19.67854	2.132487	0.0334319
gender:test_prep:parent_educ:ethnic_group	43.89948	19.36842	2.266549	0.0238254
lunch_type:test_prep:parent_educ:ethnic_group	34.55358	17.23924	2.004356	0.0455470
gender:parent_educ:ethnic_group:wkly_study_hours	33.08582	15.18358	2.179052	0.0297734

Table 6: Writing: Effect Modifiers

term	df	sumsq	meansq	statistic	p.value
gender:parent_educ:wkly_study_hours	1	1013.717	1013.717	6.018977	0.0144781

Table 7: math: full under CV

term	estimate	std.error	statistic	p.value
(Intercept)	28.0712943	4.2756226	6.565429	0.0000000
lunch_type	12.5737137	1.1964102	10.509534	0.0000000
ethnic_group	2.7439281	0.4895913	5.604528	0.0000000
test_prep	-5.2926304	1.1989408	-4.414422	0.0000121
gender	5.3016818	1.1486346	4.615638	0.0000048
parent_educ	1.5210046	0.3825700	3.975754	0.0000790
wkly_study_hours	2.0824941	0.8723498	2.387224	0.0172960
nr_siblings	0.6926991	0.3859641	1.794724	0.0732191

Table 8: math: without Gender

term	estimate	std.error	statistic	p.value
(Intercept)	35.8588529	3.9968205	8.971845	0.0000000
lunch_type	12.8699814	1.2154184	10.588931	0.0000000
ethnic_group	2.7563514	0.4980796	5.533957	0.0000000
test_prep	-5.5052544	1.2188454	-4.516778	0.0000076
parent_educ	1.4061946	0.3883852	3.620618	0.0003196
wkly_study_hours	2.2357475	0.8868446	2.521014	0.0119687
nr_siblings	0.6224711	0.3923565	1.586494	0.1131724

Table 9: math: without Lunch Type

term	estimate	std.error	statistic	p.value
(Intercept)	46.5624715	4.2486221	10.959429	0.0000000
ethnic_group	2.9517064	0.5333555	5.534219	0.0000000
test_prep	-4.8719574	1.3064508	-3.729155	0.0002110
gender	5.9493280	1.2505281	4.757453	0.0000025
parent_educ	1.4728518	0.4170780	3.531358	0.0004463
wkly_study_hours	2.1024658	0.9511021	2.210558	0.0274560
nr_siblings	0.7174494	0.4208005	1.704963	0.0887368

Table 10: math: without Test Prep

term	estimate	std.error	statistic	p.value
(Intercept)	18.4754298	3.7400301	4.939915	0.0000010
lunch_type	12.3973873	1.2146505	10.206547	0.0000000
ethnic_group	2.7880487	0.4972292	5.607171	0.0000000
gender	5.4965040	1.1659354	4.714244	0.0000030
parent_educ	1.4931204	0.3885663	3.842640	0.0001352
wkly_study_hours	2.4337489	0.8824495	2.757947	0.0059999
nr_siblings	0.7694383	0.3916691	1.964511	0.0499479

Table 11: math: without Parent Education

term	estimate	std.error	statistic	p.value
(Intercept)	32.9359482	4.1487671	7.938732	0.0000000
lunch_type	12.5167463	1.2114984	10.331624	0.0000000
ethnic_group	2.8841686	0.4945127	5.832345	0.0000000
test_prep	-5.2139275	1.2139826	-4.294895	0.0000205
gender	5.0047625	1.1607425	4.311691	0.0000190
wkly_study_hours	1.9631840	0.8828917	2.223584	0.0265609
nr_siblings	0.6744634	0.3908320	1.725712	0.0849319

Table 12: math: without Ethnic Group

term	estimate	std.error	statistic	p.value
(Intercept)	36.0431862	4.1364418	8.713573	0.0000000
lunch_type	12.8444847	1.2263736	10.473550	0.0000000
test_prep	-5.4298042	1.2297146	-4.415500	0.0000120
gender	5.3370727	1.1783449	4.529296	0.0000072
parent_educ	1.6754839	0.3914515	4.280183	0.0000218
wkly_study_hours	2.1423461	0.8948602	2.394057	0.0169798
nr_siblings	0.6356448	0.3958156	1.605912	0.1088376

Table 13: math: without Weekly Study Hours

term	estimate	std.error	statistic	p.value
(Intercept)	32.2785820	3.9112360	8.252783	0.0000000
lunch_type	12.5799355	1.2012438	10.472425	0.0000000
ethnic_group	2.7582360	0.4915337	5.611489	0.0000000
test_prep	-5.5536954	1.1987695	-4.632830	0.0000045
gender	5.4060487	1.1524423	4.690949	0.0000034
parent_educ	1.4895871	0.3838892	3.880252	0.0001163
nr_siblings	0.7382445	0.3870506	1.907359	0.0569678

Table 14: math: without Number of Siblings

term	estimate	std.error	statistic	p.value
(Intercept)	29.760538	4.1787141	7.121937	0.0000000
lunch_type	12.586815	1.1986764	10.500595	0.0000000
ethnic_group	2.720752	0.4903572	5.548511	0.0000000
test_prep	-5.389546	1.2000152	-4.491231	0.0000085
gender	5.220415	1.1499372	4.539739	0.0000069
parent_educ	1.512845	0.3832748	3.947155	0.0000888
wkly_study_hours	2.159886	0.8729500	2.474238	0.0136371

Table 15: reading: full under CV

term	estimate	std.error	statistic	p.value
(Intercept)	66.712128	3.6484858	18.284881	0.00e+00
lunch_type	8.666712	1.1618414	7.459462	0.00e+00
gender	-7.506622	1.1138734	-6.739206	0.00e+00
test_prep	-6.828881	1.1580310	-5.896976	0.00e+00
parent_educ	1.760626	0.3712699	4.742173	2.70e-06
ethnic_group	1.793048	0.4752616	3.772761	1.78e-04

Table 16: reading: without Gender $\,$

term	estimate	std.error	statistic	p.value
(Intercept)	55.468110	3.3661817	16.478050	0.0000000
lunch_type	8.247206	1.2036296	6.851947	0.0000000
test_prep	-6.514335	1.2004315	-5.426661	0.0000001
parent_educ	1.925653	0.3843380	5.010310	0.0000007
ethnic_group	1.770801	0.4930517	3.591512	0.0003566

Table 17: reading: without Lunch Type

term	estimate	std.error	statistic	p.value
(Intercept)	79.532319	3.3660323	23.627913	0.0000000
gender	-7.061453	1.1633176	-6.070099	0.0000000
test_prep	-6.543314	1.2105129	-5.405407	0.0000001
parent_educ	1.726992	0.3882795	4.447807	0.0000104
ethnic_group	1.935796	0.4966690	3.897558	0.0001085

Table 18: reading: without Test Prep

term	estimate	std.error	statistic	p.value
(Intercept)	55.415717	3.1939548	17.350188	0.0000000
lunch_type	8.440218	1.1944245	7.066347	0.0000000
gender	-7.241882	1.1448065	-6.325857	0.0000000
parent_educ	1.715858	0.3818108	4.494000	0.0000084
ethnic_group	1.850135	0.4887557	3.785399	0.0001694

Table 19: reading: without Parent Education

term	estimate	std.error	statistic	p.value
(Intercept)	72.006949	3.5369813	20.358306	0.00e+00
lunch_type	8.599800	1.1830081	7.269434	0.00e+00
gender	-7.855014	1.1317801	-6.940407	0.00e+00
test_prep	-6.716589	1.1789687	-5.697004	0.00e+00
ethnic_group	1.955447	0.4826977	4.051080	5.79e-05

Table 20: reading: without Ethnic Group

term	estimate	std.error	statistic	p.value
(Intercept)	71.907404	3.4168330	21.045045	0e+00
lunch_type	8.843208	1.1740235	7.532394	0e+00
gender	-7.477432	1.1264389	-6.638116	0e+00
test_prep	-6.917873	1.1708798	-5.908269	0e+00
parent_educ	1.861556	0.3744912	4.970894	9e-07

Table 21: Writing: full under CV

term	estimate	std.error	statistic	p.value
(Intercept)	65.312482	3.8873510	16.801283	0.0000000
gender	-9.179189	1.0697572	-8.580629	0.0000000
lunch_type	9.497555	1.1150980	8.517238	0.0000000
test_prep	-9.036032	1.1163435	-8.094312	0.0000000
parent_educ	2.324218	0.3565507	6.518618	0.0000000
ethnic_group	2.168352	0.4561667	4.753419	0.0000025
wkly_study_hours	1.176186	0.8120831	1.448357	0.1480577

Table 22: Writing: without Gender

term	estimate	std.error	statistic	p.value
(Intercept)	52.1053044	3.7861927	13.761926	0.0000000
lunch_type	8.9861099	1.1810512	7.608569	0.0000000
test_prep	-8.6843663	1.1832649	-7.339326	0.0000000
parent_educ	2.5218719	0.3773897	6.682407	0.0000000
ethnic_group	2.1427345	0.4838283	4.428708	0.0000113
wkly_study_hours	0.9240399	0.8607815	1.073489	0.2834972

Confounding - Writing

We can see, removing gender will lower wkly_study_hours by 0.2142857, removing test_prep will lower wkly_study_hours by 0.5238095, and removing parent_educ will lower wkly_study_hours by 0.1573129.

Hence, gender, test_prep, parent_educ could be potential confounder for wkly_study_hours

[1] 0.2142857

[1] 0.5238095

[1] 0.1573129

Table 23: Writing: without Lunch Type

term	estimate	std.error	statistic	p.value
(Intercept)	79.325906	3.7325524	21.252456	0.0000000
gender	-8.692165	1.1320889	-7.677988	0.0000000
test_prep	-8.720881	1.1824309	-7.375383	0.0000000
parent_educ	2.287624	0.3778387	6.054500	0.0000000
ethnic_group	2.324677	0.4830459	4.812539	0.0000019
wkly_study_hours	1.193361	0.8606285	1.386616	0.1660908

Table 24: Writing: without Test Prep

term	estimate	std.error	statistic	p.value
(Intercept)	49.216447	3.5208066	13.978742	0.0000000
gender	-8.861298	1.1268300	-7.863917	0.0000000
lunch_type	9.198386	1.1747364	7.830171	0.0000000
parent_educ	2.274969	0.3757718	6.054123	0.0000000
ethnic_group	2.239439	0.4807388	4.658328	0.0000040
wkly_study_hours	1.791765	0.8522239	2.102458	0.0359429

Table 25: Writing: without Parent Education

term	estimate	std.error	statistic	p.value
(Intercept)	72.6791532	3.8499827	18.877787	0.0000000
gender	-9.6297006	1.1049839	-8.714788	0.0000000
lunch_type	9.4099646	1.1541452	8.153189	0.0000000
test_prep	-8.9118520	1.1553500	-7.713552	0.0000000
ethnic_group	2.3836134	0.4709357	5.061441	0.0000006
wkly_study_hours	0.9907309	0.8400647	1.179351	0.2387413

Table 26: Writing: without Ethnic Group

term	estimate	std.error	statistic	p.value
(Intercept)	71.506520	3.7298885	19.171222	0.0000000
gender	-9.145910	1.0894332	-8.395108	0.0000000
lunch_type	9.710824	1.1347127	8.557958	0.0000000
test_prep	-9.138195	1.1366900	-8.039303	0.0000000
parent_educ	2.446910	0.3621638	6.756362	0.0000000
wkly_study_hours	1.218475	0.8269878	1.473390	0.1411875

Table 27: Writing: without Weekly Study Hours

term	estimate	std.error	statistic	p.value
(Intercept)	67.757450	3.5049950	19.331682	0.0e+00
gender	-9.123124	1.0700661	-8.525758	0.0e+00
lunch_type	9.501565	1.1161475	8.512822	0.0e+00
test_prep	-9.187450	1.1124869	-8.258479	0.0e+00
parent_educ	2.306126	0.3566683	6.465745	0.0e+00
ethnic_group	2.175590	0.4565701	4.765073	2.4e-06

Leverage one score

Effect of adding Writing, Reading scores on Maths model

Effect of adding Maths, Writing scores on Reading model

Effect of adding Maths, Reading scores on Writing model

Combined table

model_name	MSE
maths_reading+writing	31.67574
maths_original	187.71873
reading_maths+writing	16.36549
reading_original	177.64685
writing_maths+reading	12.79564
writing_original	163.35751

We can see that the MSE all significantly decreased after adding other scores to fit one score's model, indicating that leveraging other scores to enhance one score's model is possible and successful.

Test potential overfitting issue - maths example

[1] "MSE on Test Set: 31.2708965516677"

[1] "Mean MSE across Folds: 32.5279607340191"

The model performs as well on test set and also across folds. Adding other scores to one score's best fit model did enhance the model.