



Robotics

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Goal for this course

- Design: soft hand design **x1**
- Perception: vision, point cloud, tactile, force/torque **x1**
- Planning: sampling-based, optimization-based, learning-based **x3**
- Control: feedback, multi-modal **x2**
- Learning: imitation learning, RL **x2**
- Simulation tool (pybullet, matlab, OpenRAVE, Issac Nvidia, Gazebo)
- **How to get a robot moving!**



Today agenda

- Paper reading (~30 mins)
- Why imitation learning (IL) (~5)
- Key ingredients of IL (~5)
- Data collection (~5)
- Learning algorithms (~20)
- Limits of IL (~5)
- Examples and applications (~20)
 - Motion
 - Hand IK
 - Force-relevant task
 - Multi-modal task



Why imitation learning?

Special-Purpose Robot Automation



custom-built
robots



human expert
programming



special-purpose
behaviors

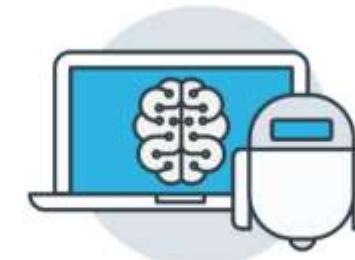
General-Purpose Robot Autonomy



general-purpose
robots



Robot Learning



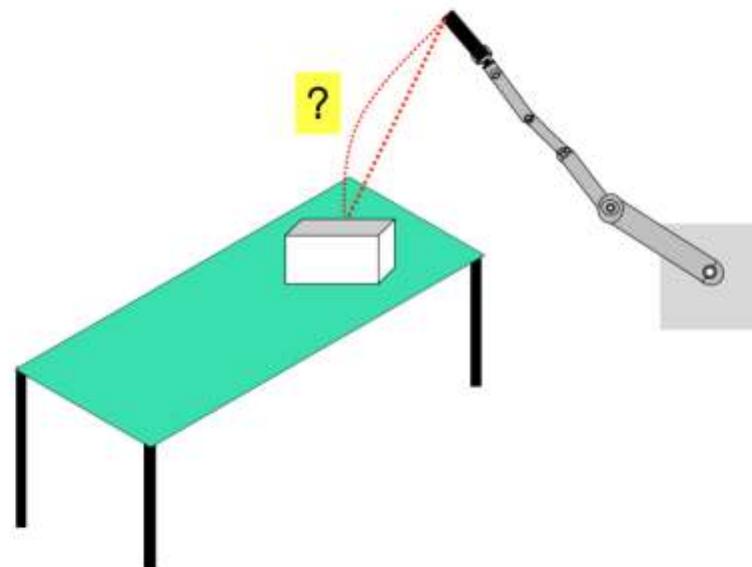
general-purpose
behaviors



Why imitation learning?

Motivation

How can we learn optimal controllers to perform a task from data?



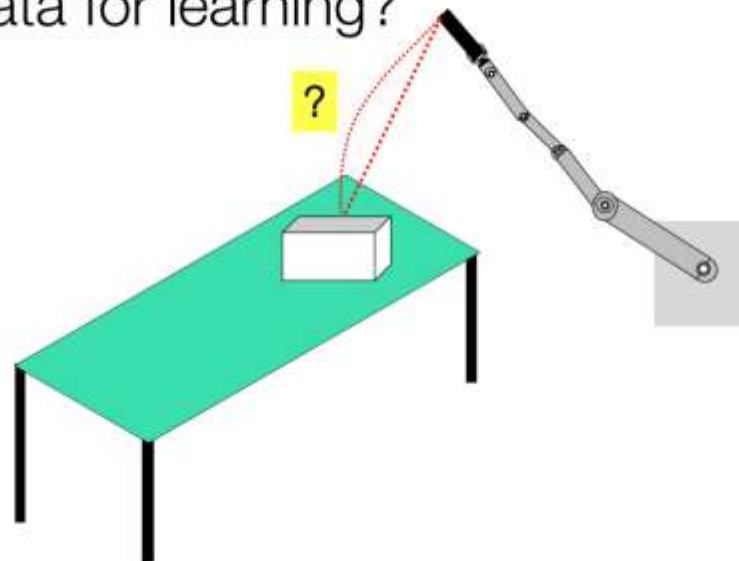


Why imitation learning?

Motivation

How can we learn optimal controllers to perform a task from data?

- Use data-driven approaches to learn optimal controllers
- How do we gather data for learning?





Why imitation learning?

Learning is critical for getting robots to work in the real world.



object variation



environment uncertainty



adaptation



Why imitation learning?

Robots should have the ability to **learn skills
and **adapt** these skills to new scenarios.**



Why imitation learning?

Imitation is a crucial aspect of skill development, because it allows us to **learn new things quickly and efficiently by watching those around us**. Most children learn everything from gross motor movements, to speech, to interactive play skills by watching parents, caregivers, siblings, and peers perform these behaviors.



<https://www.mayinstitute.org/news/acl/asd-and-dd-child-focused/what-is-imitation-and-why-is-it-important/#:~:text=Imitation%20is%20a%20crucial%20aspect,and%20peers%20perform%20these%20behaviors.>



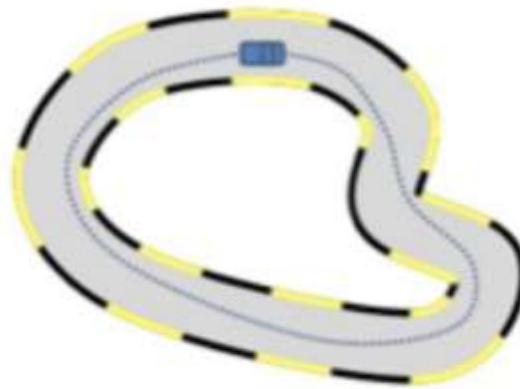
Why imitation learning?

Imitation Learning in a Nutshell

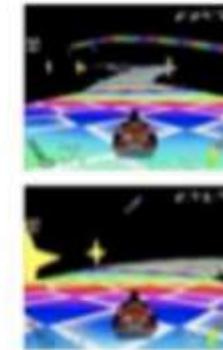
Given: demonstrations or demonstrator

Goal: train a policy to mimic demonstrations

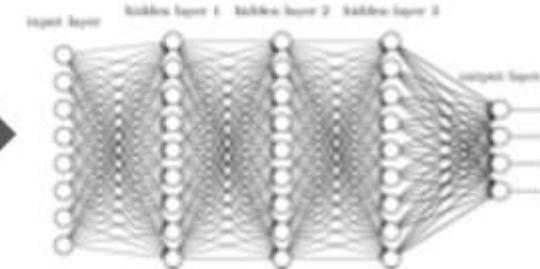
Expert Demonstrations



State/Action Pairs



Learning





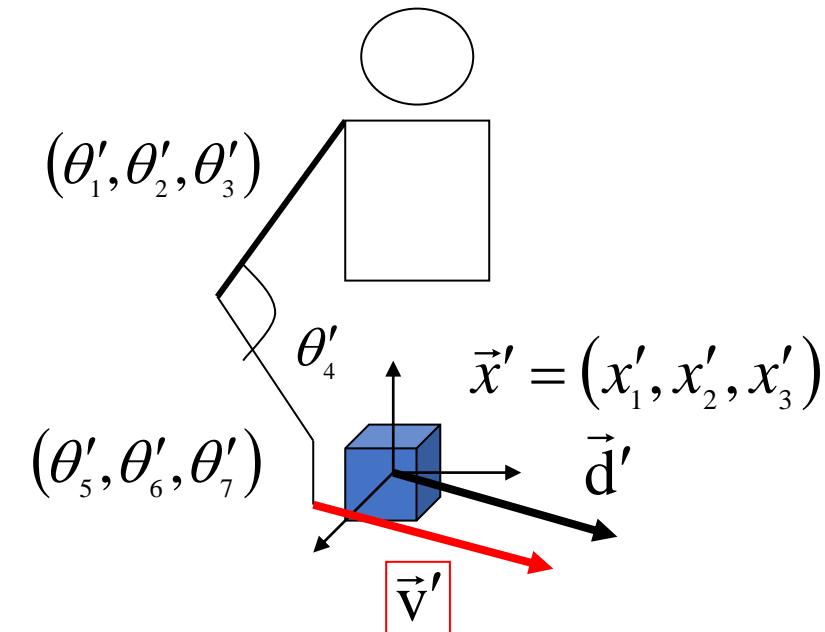
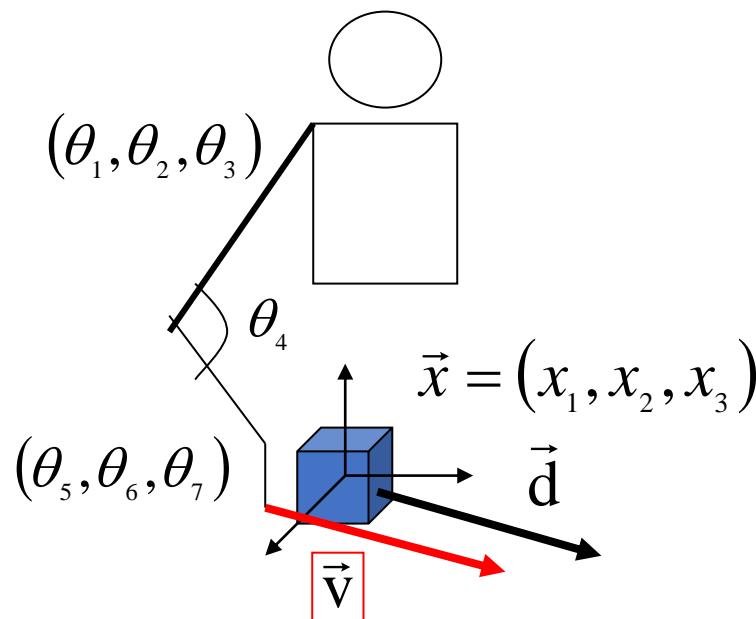
Imitation learning

$\vec{x} = \vec{x}'$ Same Object, same target location

$\vec{d} = \vec{d}'$ Same direction of motion

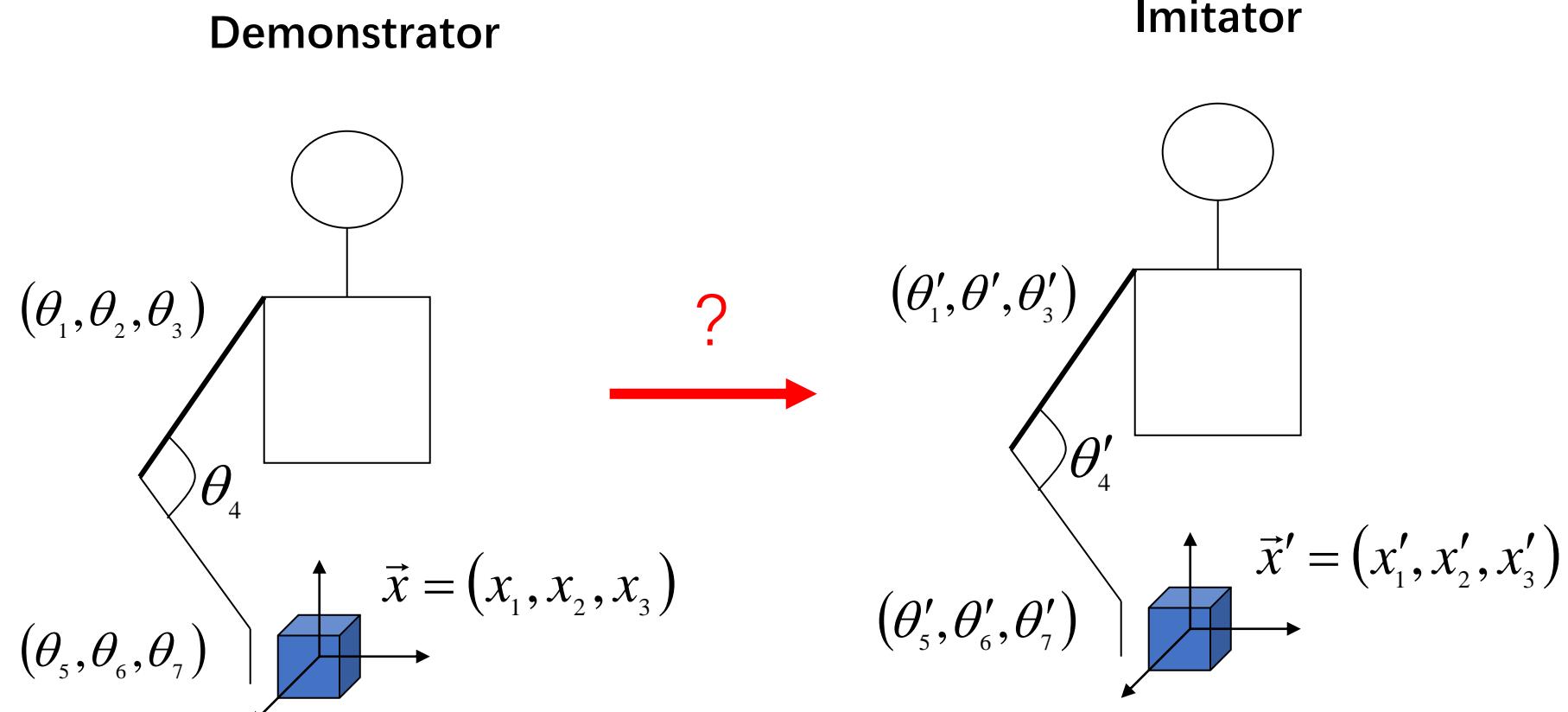
$\vec{v} = \vec{v}'$ Same speed, same force

$\vec{\theta} = \vec{\theta}'$ Same posture





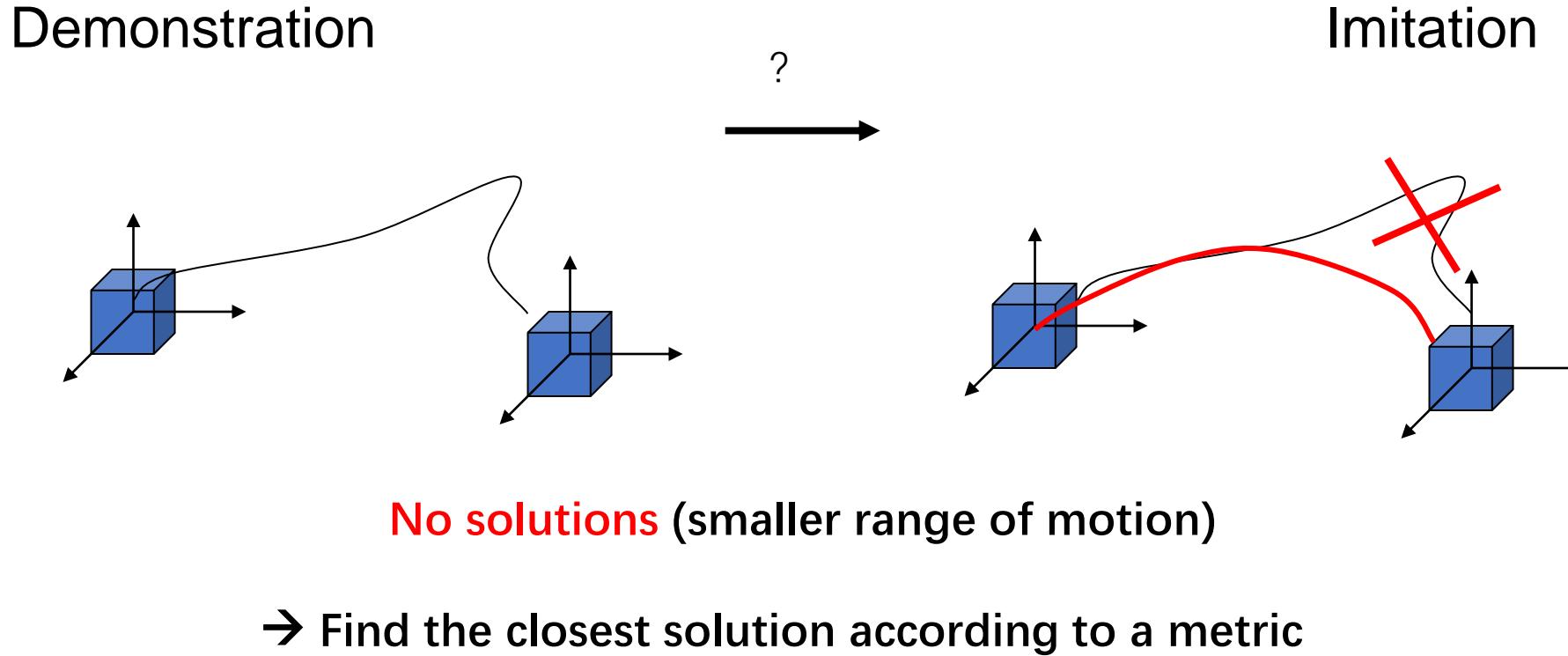
Imitation learning



The Transfer problem



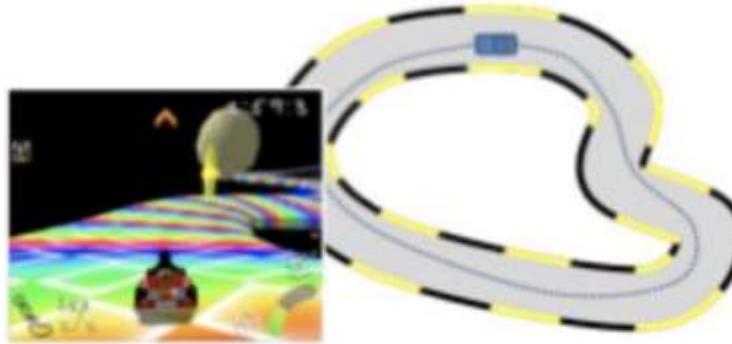
Imitation learning



**How to Imitate?
The correspondence problem**



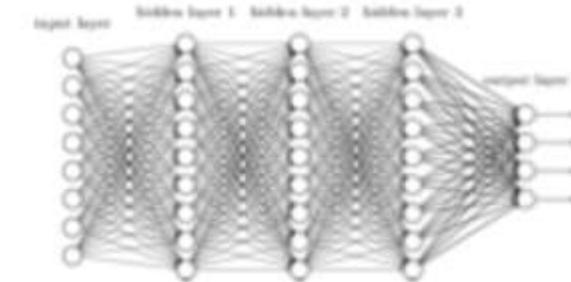
Key ingredients of IL



① Demonstrations or Demonstrator



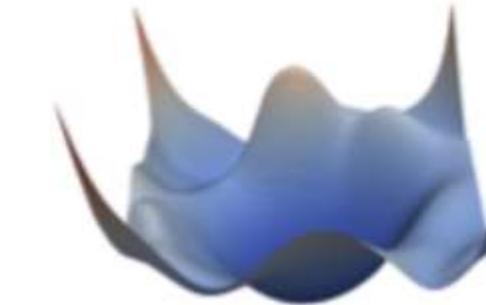
Environment / Simulator ②



Policy Class ③



Loss Function



Learning Algorithm





Key ingredients of IL

Considerations

Learning human skills through LFD requires the following questions:

- What/Who to imitate?
- How to imitate?
- When to imitate?



Key ingredients of IL

Demonstrator

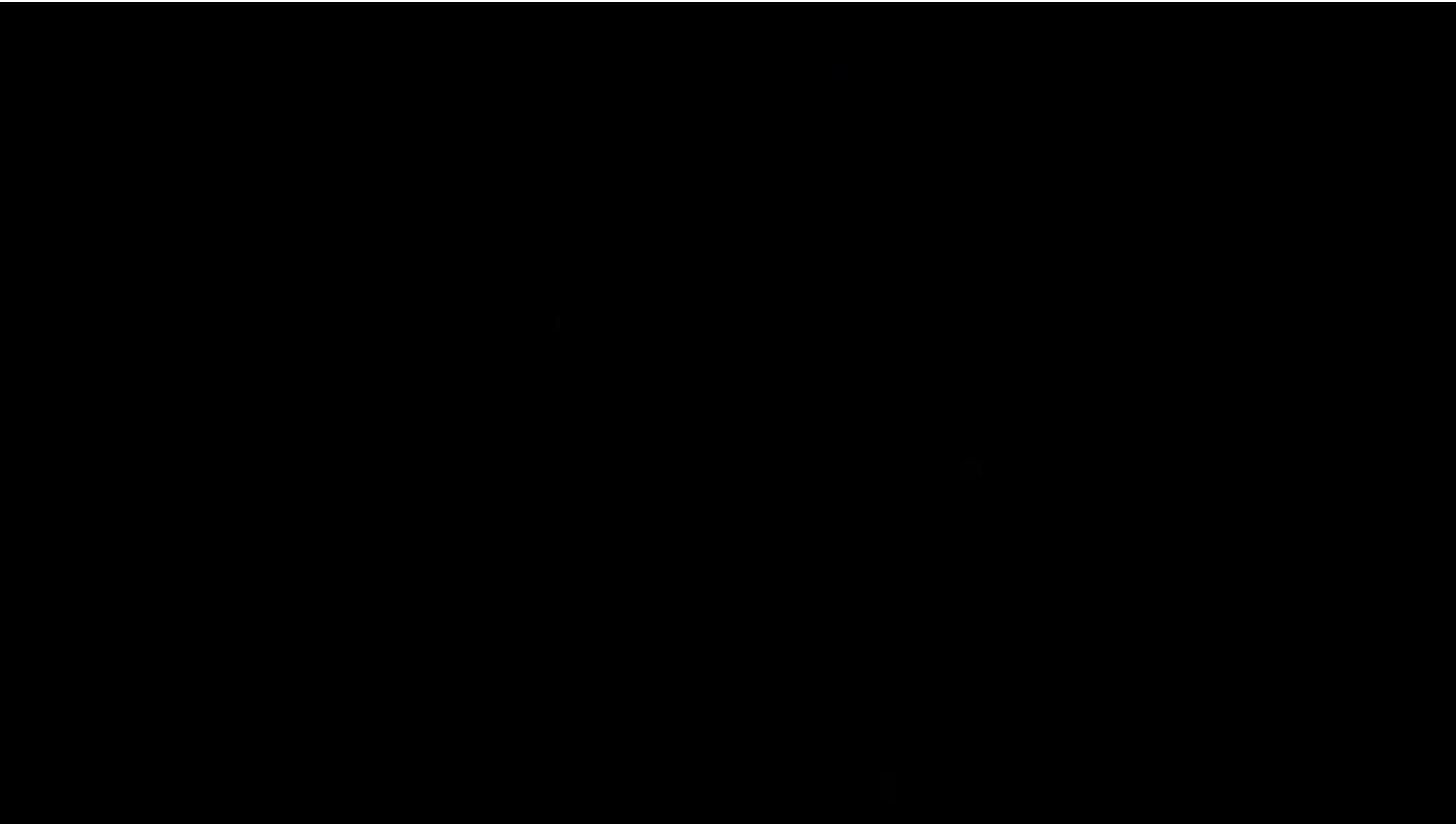
Teleoperation
+
Data glove





Key ingredients of IL

Demonstrator





Key ingredients of IL

Demonstrator

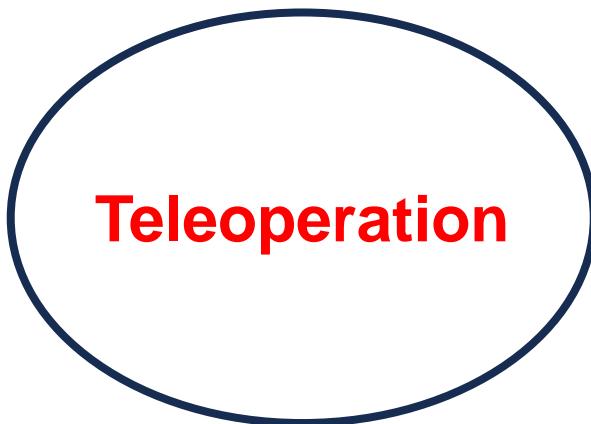
Teleoperation
+
EMG





Key ingredients of IL

Demonstrator



Teleoperation Interfaces

- Graphical user interface/Tablet
- Joysticks
- More complex devices (e.g., exoskeleton)



Da Vinci Surgical Robot



Key ingredients of IL

Demonstrator

Kinesthetic



<https://www.youtube.com/channel/UCqnvGUfdlr94mddDQamEBGA>



Key ingredients of IL

Demonstrator

Kinesthetic
+
Tactile





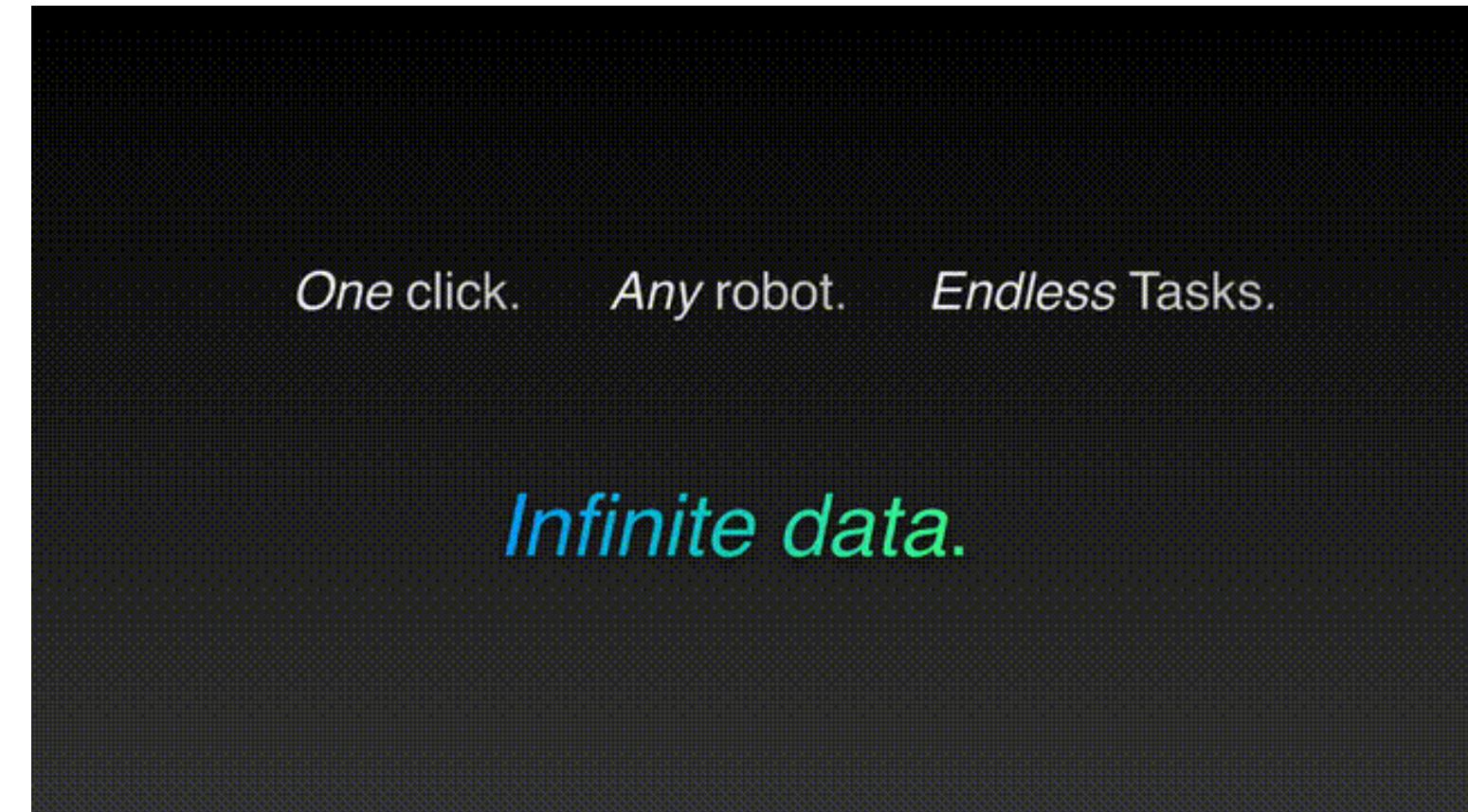
Key ingredients of IL

Demonstrator

Simulation

CMU清华MIT引爆全球首个Agent无限流，机器人「007」加班自学停不下来！具身智能被革命

Original 新智元 2023-11-04 14:27 Posted on 北京



Computer Science > Robotics

(Submitted on 2 Nov 2023)

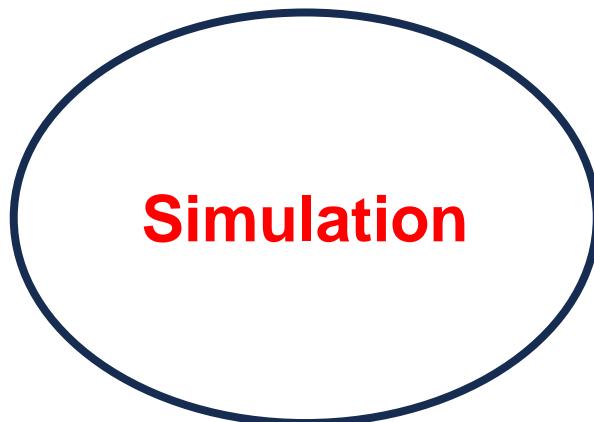
RoboGen: Towards Unleashing Infinite Data for Automated Robot Learning via Generative Simulation

Yufei Wang, Zhou Xian, Feng Chen, Tsun-Hsuan Wang, Yian Wang, Katerina Fragkiadaki, Zackory Erickson, David Held, Chuang Gan



Key ingredients of IL

Demonstrator



Agile Autonomy: Learning High-Speed Flight in the Wild

Antonio Loquercio*, Elia Kaufmann*, René Ranftl,
Matthias Müller, Vladlen Koltun, Davide Scaramuzza



University of
Zurich^{UZH}



*these authors contributed equally



Key ingredients of IL

Demonstrator

Motion capture





Key ingredients of IL

Demonstrator

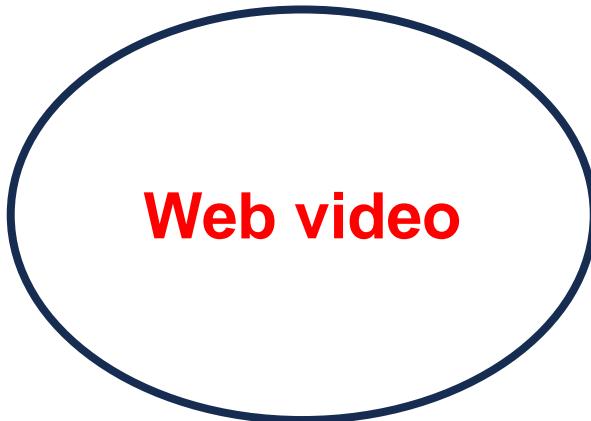
Motion capture



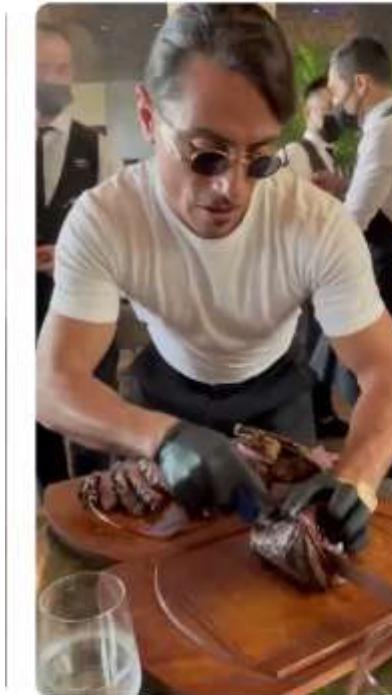


Key ingredients of IL

Demonstrator



Web video



Salt Bae
7.2M views



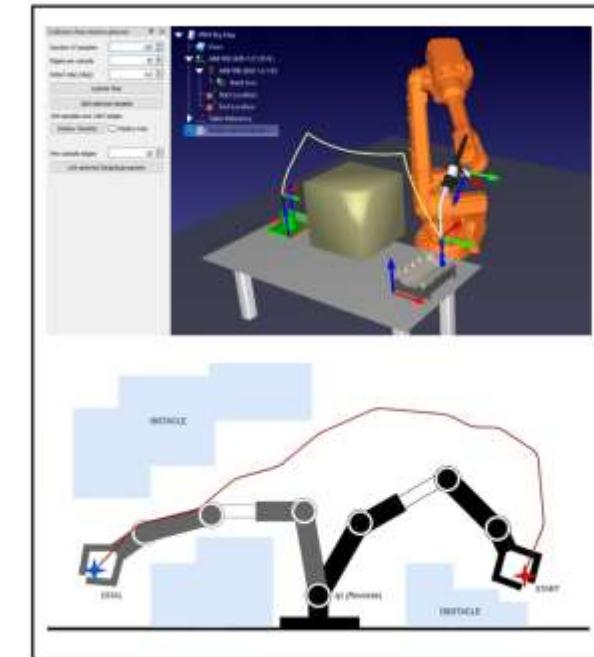
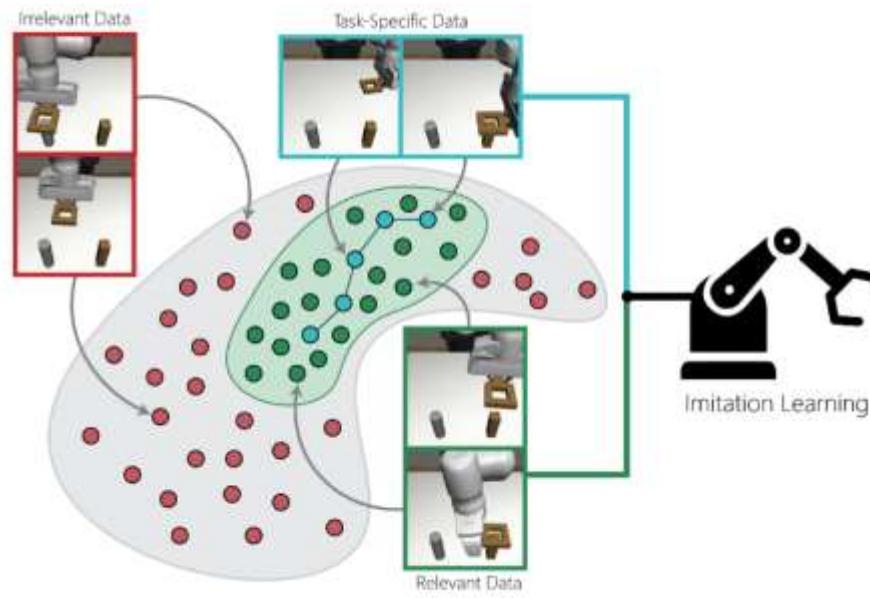
POV Chefs Cooking 500+
Meals #food #chef #cookin...
19K views



Difference between
teppanyaki and hibachi



Data collection



Task distribution





Data collection

Imitation learning is very good at
in-distribution tasks, but not so good at out-
distribution tasks.

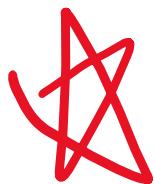




Data collection or exp design

- Task variations
- Environments
- Demonstrator variance
- Invariant relation

We need to
design the exps
according to these
rules.



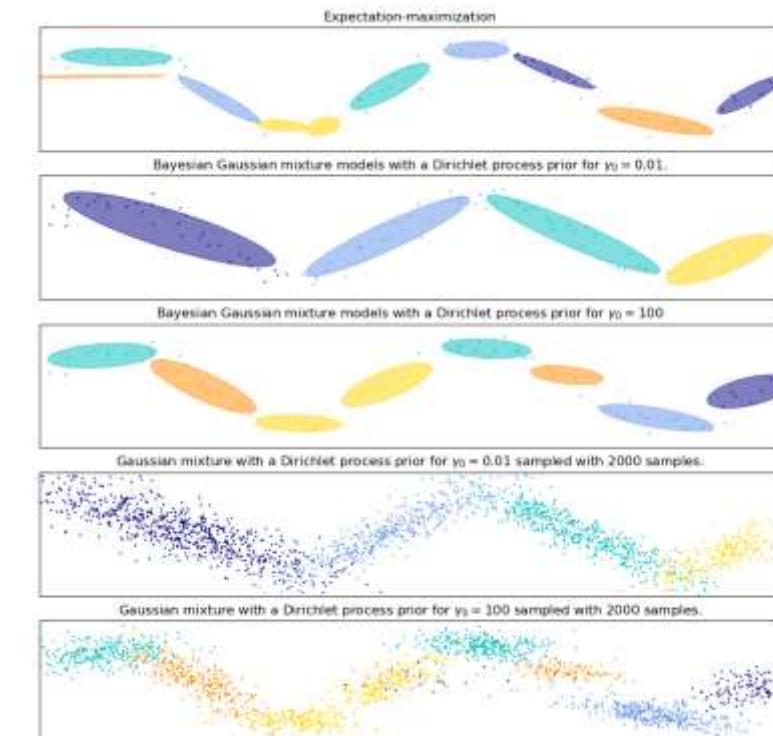
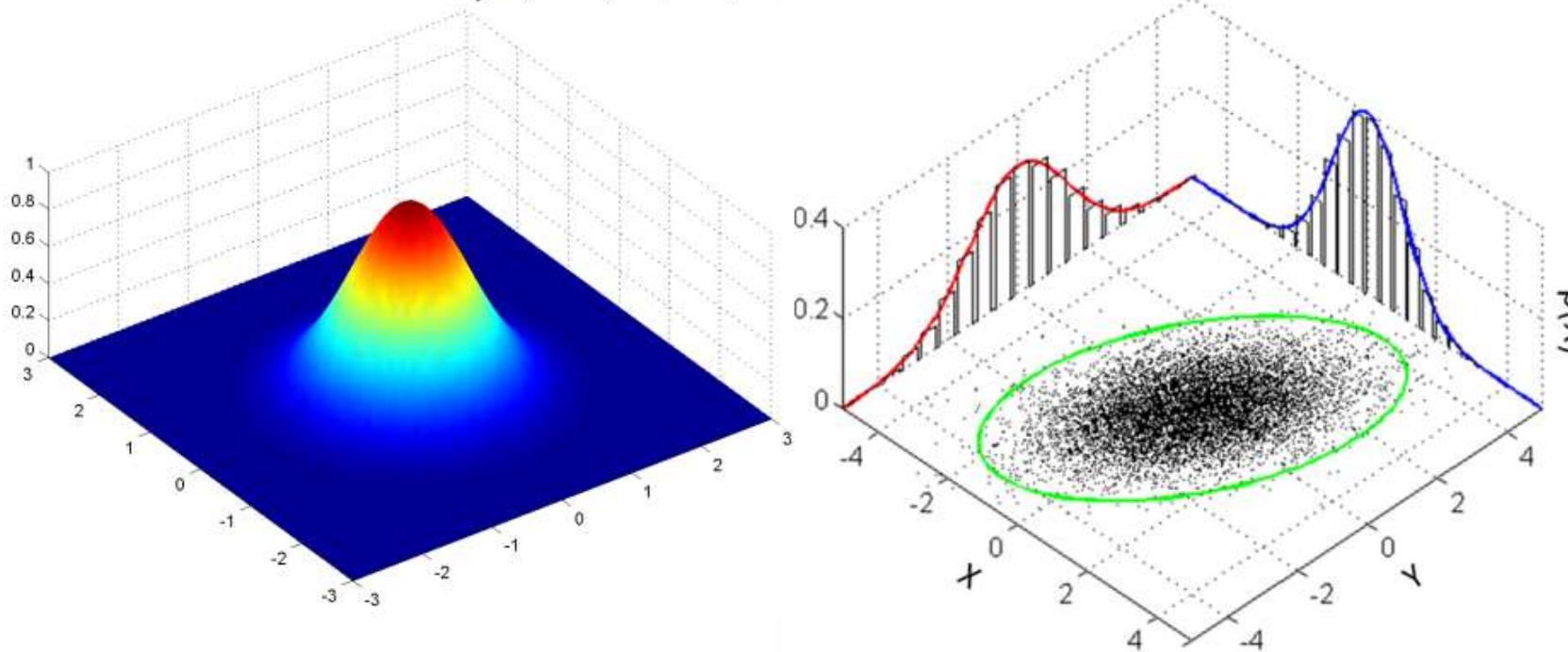


GMM

Learning algorithms

- Recall the Gaussian distribution:

$$P(\mathbf{x} | \boldsymbol{\mu}, \boldsymbol{\Sigma}) = \frac{1}{\sqrt{(2\pi)^d |\boldsymbol{\Sigma}|}} \exp \left(-\frac{1}{2} (\mathbf{x} - \boldsymbol{\mu})^\top \boldsymbol{\Sigma}^{-1} (\mathbf{x} - \boldsymbol{\mu}) \right)$$





Learning algorithms

Multivariate Gaussian distribution

Univariate Gaussian distribution:

$$\mathcal{N}(\mu, \sigma^2) = (2\pi\sigma^2)^{-\frac{1}{2}} \exp\left(-\frac{1}{2\sigma^2}(x - \mu)^2\right)$$

Radial basis function (RBF)

$x \in \mathbb{R}$ Datapoint

$\mu \in \mathbb{R}$ Center (or mean)

$\sigma^2 \in \mathbb{R}$ Variance

Parameters $\{\mu, \sigma^2\}$

Multivariate Gaussian distribution:

$$\mathcal{N}(\boldsymbol{\mu}, \boldsymbol{\Sigma}) = \frac{1}{(2\pi)^{\frac{D}{2}} |\boldsymbol{\Sigma}|^{\frac{1}{2}}} \exp\left(-\frac{1}{2} (\mathbf{x} - \boldsymbol{\mu})^\top \boldsymbol{\Sigma}^{-1} (\mathbf{x} - \boldsymbol{\mu})\right)$$

$\mathbf{x} \in \mathbb{R}^D$ Datapoint

$\boldsymbol{\mu} \in \mathbb{R}^D$ Center (or mean)

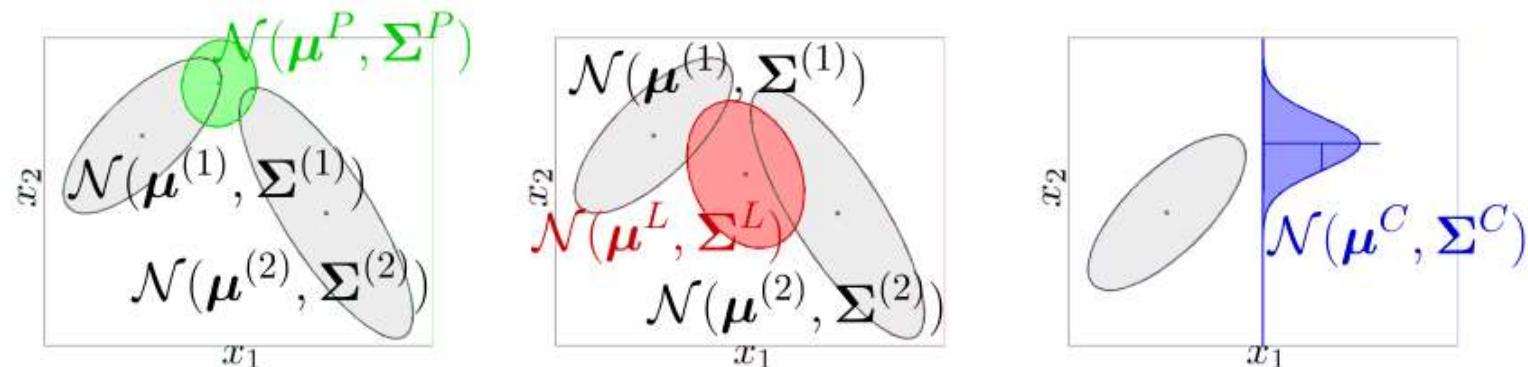
$\boldsymbol{\Sigma} \in \mathbb{R}^{D \times D}$ Covariance matrix

Parameters $\{\boldsymbol{\mu}, \boldsymbol{\Sigma}\}$



Learning algorithms

Properties of Gaussian distributions



Linear combination:

$$\mathcal{N}(\mu^L, \Sigma^L) \sim \frac{1}{2} \mathcal{N}(\mu^{(1)}, \Sigma^{(1)}) + \frac{1}{2} \mathcal{N}(\mu^{(2)}, \Sigma^{(2)})$$

Product of Gaussians:

$$c \mathcal{N}(\mu^P, \Sigma^P) \sim \mathcal{N}(\mu^{(1)}, \Sigma^{(1)}) \cdot \mathcal{N}(\mu^{(2)}, \Sigma^{(2)})$$

Conditional probability:

$$\mathcal{N}(\mu^C, \Sigma^C) \sim \mathcal{P}(x_2 | x_1)$$



Learning algorithms

Product of Gaussians

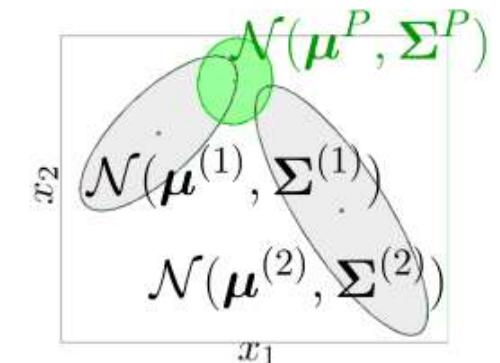
The product of two Gaussian distributions $\mathcal{N}(\boldsymbol{\mu}^{(1)}, \Sigma^{(1)})$ and $\mathcal{N}(\boldsymbol{\mu}^{(2)}, \Sigma^{(2)})$ is defined by

$$c \mathcal{N}(\boldsymbol{\mu}^P, \Sigma^P) = \mathcal{N}(\boldsymbol{\mu}^{(1)}, \Sigma^{(1)}) \cdot \mathcal{N}(\boldsymbol{\mu}^{(2)}, \Sigma^{(2)}),$$

with $c = \mathcal{N}(\boldsymbol{\mu}^{(1)} | \boldsymbol{\mu}^{(2)}, \Sigma^{(1)} + \Sigma^{(2)})$,

$$\Sigma^P = \left(\Sigma^{(1)-1} + \Sigma^{(2)-1} \right)^{-1},$$

$$\boldsymbol{\mu}^P = \Sigma^P \left(\Sigma^{(1)-1} \boldsymbol{\mu}^{(1)} + \Sigma^{(2)-1} \boldsymbol{\mu}^{(2)} \right).$$





Learning algorithms

28

Conditional probability

Let $\mathbf{x} \sim \mathcal{N}(\boldsymbol{\mu}, \boldsymbol{\Sigma})$ be defined by

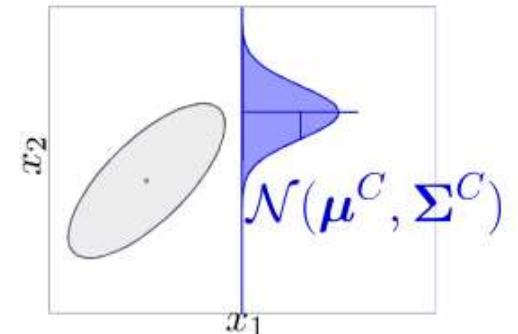
$$\mathbf{x} = \begin{pmatrix} \mathbf{x}_1 \\ \mathbf{x}_2 \end{pmatrix}, \quad \boldsymbol{\mu} = \begin{pmatrix} \boldsymbol{\mu}_1 \\ \boldsymbol{\mu}_2 \end{pmatrix}, \quad \boldsymbol{\Sigma} = \begin{pmatrix} \boldsymbol{\Sigma}_{11} & \boldsymbol{\Sigma}_{12} \\ \boldsymbol{\Sigma}_{21} & \boldsymbol{\Sigma}_{22} \end{pmatrix}.$$

The conditional probability $\mathcal{P}(\mathbf{x}_2|\mathbf{x}_1)$ is defined by

$$\mathcal{P}(\mathbf{x}_2|\mathbf{x}_1) \sim \mathcal{N}(\boldsymbol{\mu}^C, \boldsymbol{\Sigma}^C),$$

with $\boldsymbol{\mu}^C = \boldsymbol{\mu}_2 + \boldsymbol{\Sigma}_{21}(\boldsymbol{\Sigma}_{11})^{-1}(\mathbf{x}_1 - \boldsymbol{\mu}_1)$,

$$\boldsymbol{\Sigma}^C = \boldsymbol{\Sigma}_{22} - \boldsymbol{\Sigma}_{21}(\boldsymbol{\Sigma}_{11})^{-1}\boldsymbol{\Sigma}_{12}.$$

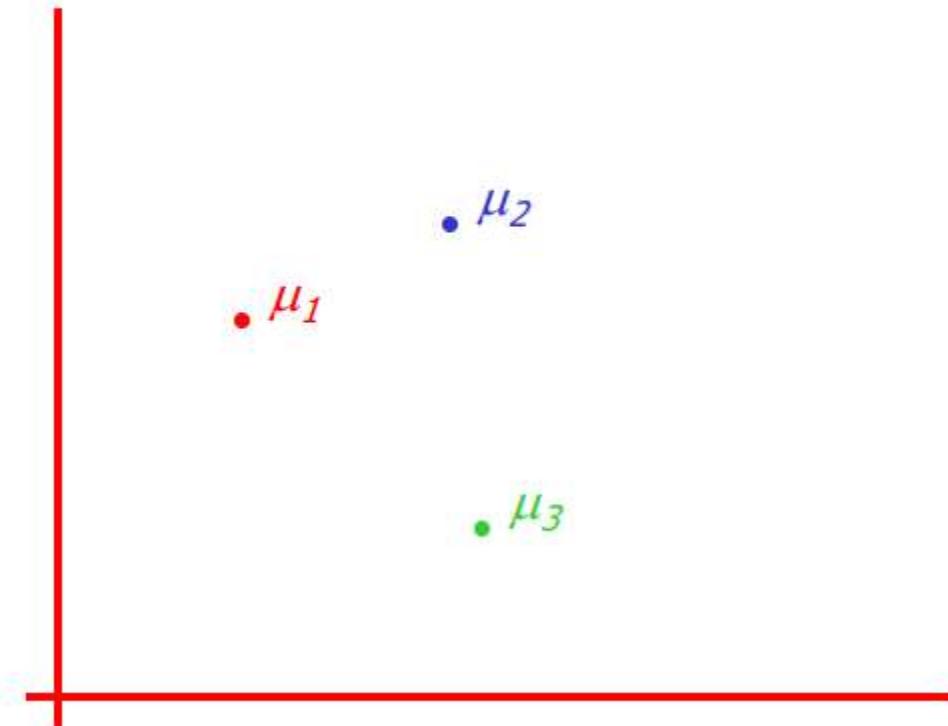




Learning algorithms

The GMM assumption

- There are k components. The i 'th component is called ω_i
- Component ω_i has an associated mean vector μ_i



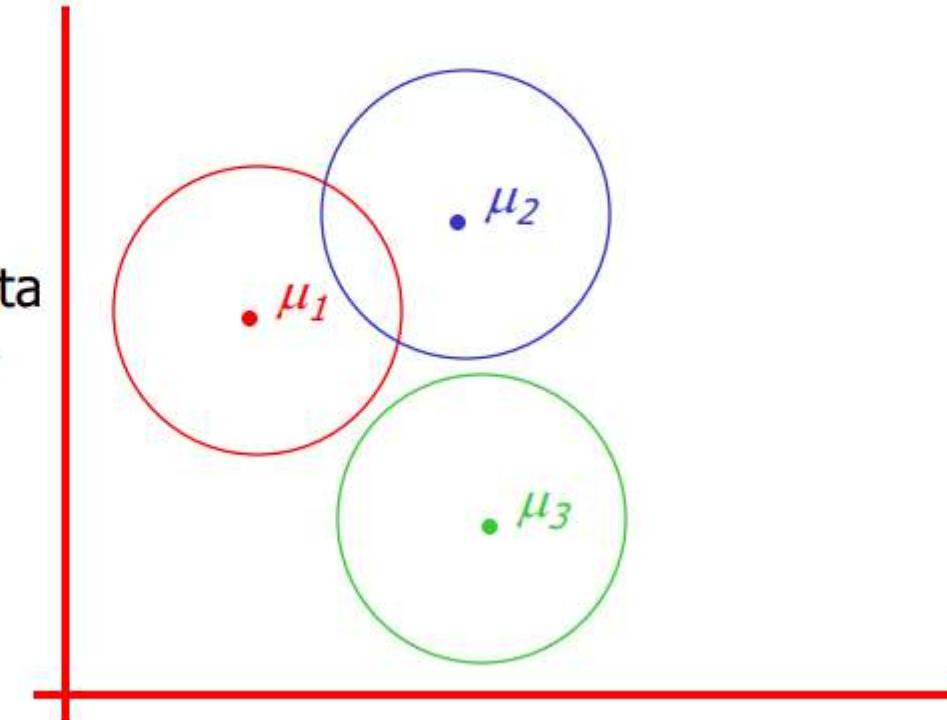


Learning algorithms

The GMM assumption

- There are k components. The i 'th component is called ω_i
- Component ω_i has an associated mean vector μ_i
- Each component generates data from a Gaussian with mean μ_i and covariance matrix $\sigma^2 \mathbf{I}$

Assume that each datapoint is generated according to the following recipe:





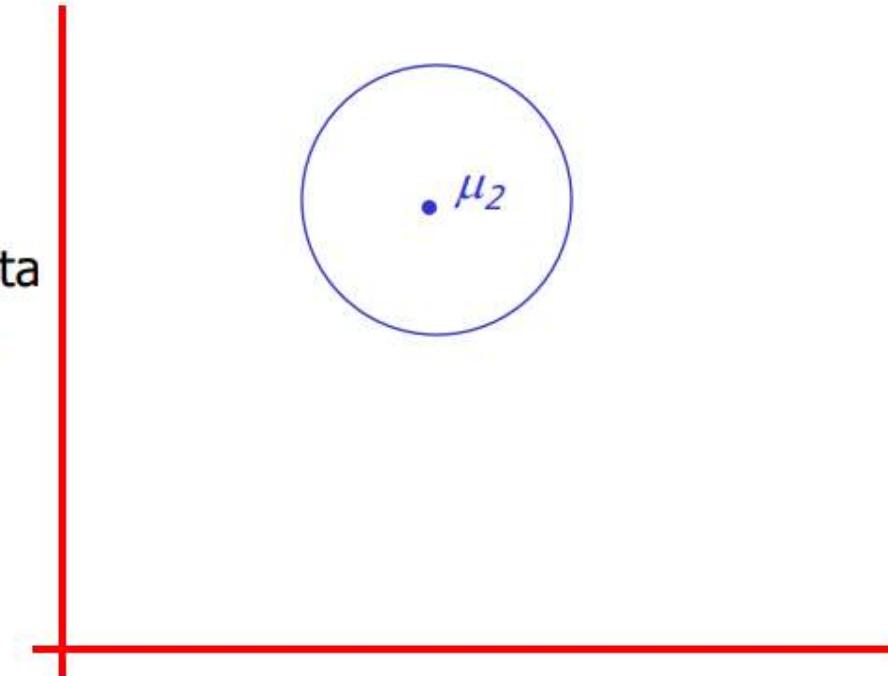
Learning algorithms

The GMM assumption

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Assume that each datapoint is generated according to the following recipe:

1. Pick a component at random: choose component i with probability $P(\omega_i)$.





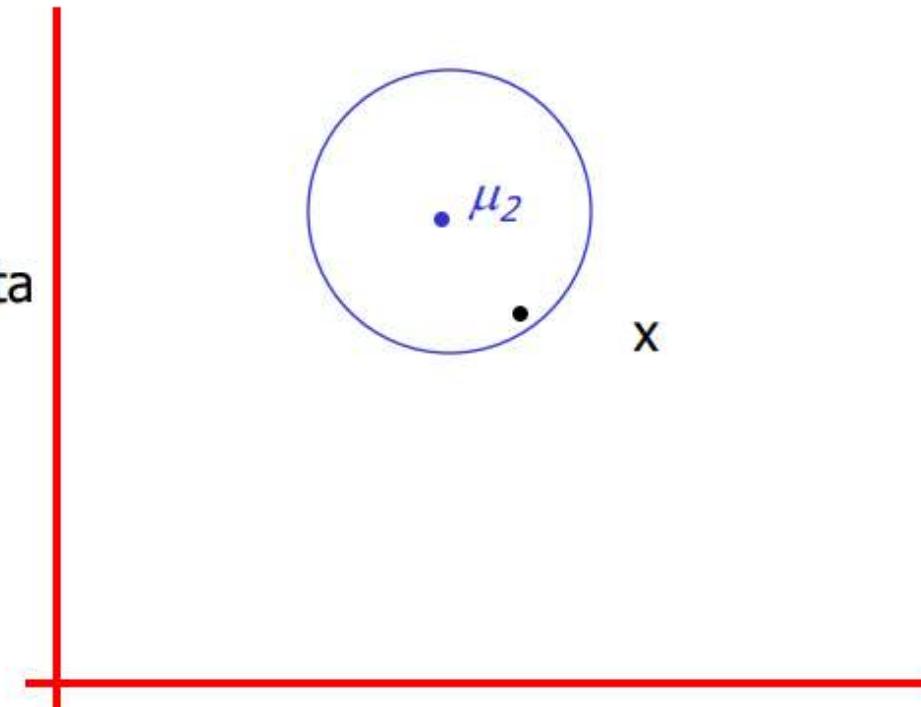
Learning algorithms

The GMM assumption

- There are k components. The i 'th component is called ω_i
- Component ω_i has an associated mean vector μ_i
- Each component generates data from a Gaussian with mean μ_i and covariance matrix $\sigma^2 \mathbf{I}$

Assume that each datapoint is generated according to the following recipe:

1. Pick a component at random: choose component i with probability $P(\omega_i)$.
2. Datapoint $\sim N(\mu_i, \sigma^2 \mathbf{I})$





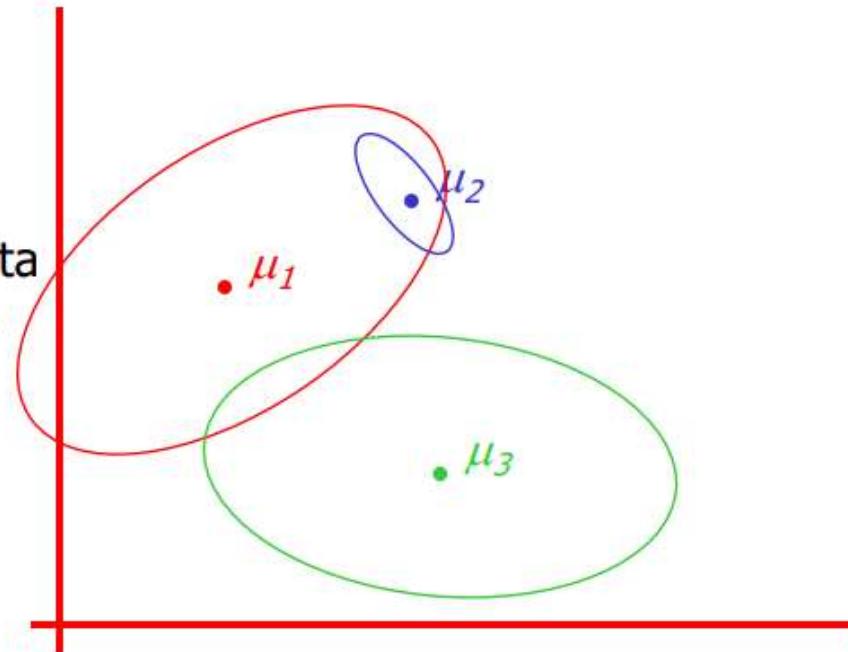
Learning algorithms

The General GMM assumption

- There are k components. The i 'th component is called ω_i
- Component ω_i has an associated mean vector μ_i
- Each component generates data from a Gaussian with mean μ_i and covariance matrix Σ_i

Assume that each datapoint is generated according to the following recipe:

1. Pick a component at random: choose component i with probability $P(\omega_i)$.
2. Datapoint $\sim N(\mu_i, \Sigma_i)$





Learning algorithms

Mixture Models

- Formally a Mixture Model is the weighted sum of a number of pdfs where the weights are determined by a distribution π

$$p(x) = \sum_{k=0}^k \pi_i f_i(x)$$

where $\sum_{i=0}^k \pi_i = 1$

$$p(x) = \sum_{i=0}^k \pi_i f_i(x)$$



Learning algorithms

Gaussian Mixture Models

- GMM: the weighted sum of a number of Gaussians where the weights are determined by a distribution π

$$p(x) = \pi_0 N(x|\mu_0, \Sigma_0) + \pi_1 N(x|\mu_1, \Sigma_1) + \dots + \pi_k N(x|\mu_k, \Sigma_k)$$

$$\text{where } \sum_{i=0}^k \pi_i = 1$$

$$p(x) = \sum_{i=0}^k \pi_i N(x|\mu_k, \Sigma_k)$$



Learning algorithms

E.M. for General GMMs

Iterate. On the t 'th iteration let our estimates be

$$\lambda_t = \{ \mu_1(t), \mu_2(t) \dots \mu_c(t), \Sigma_1(t), \Sigma_2(t) \dots \Sigma_c(t), p_1(t), p_2(t) \dots p_c(t) \}$$

①

E-step: Compute “expected” clusters of all datapoints

$$P(w_i|x_k, \lambda_t) = \frac{p(x_k|w_i, \lambda_t)P(w_i|\lambda_t)}{p(x_k|\lambda_t)} = \frac{p(x_k|w_i, \mu_i(t), \Sigma_i(t))p_i(t)}{\sum_{j=1}^c p(x_k|w_j, \mu_j(t), \Sigma_j(t))p_j(t)}$$

Just evaluate a Gaussian at x_k

②

M-step: Estimate μ , Σ given our data's class membership distributions

$$\mu_i(t+1) = \frac{\sum_k P(w_i|x_k, \lambda_t)x_k}{\sum_k P(w_i|x_k, \lambda_t)}$$

$$\Sigma_i(t+1) = \frac{\sum_k P(w_i|x_k, \lambda_t)[x_k - \mu_i(t+1)][x_k - \mu_i(t+1)]^T}{\sum_k P(w_i|x_k, \lambda_t)}$$

$$p_i(t+1) = \frac{\sum_k P(w_i|x_k, \lambda_t)}{R}$$

$R = \# \text{records}$



Learning algorithms (video)



**Gaussian
Mixture
Models**



Learning algorithms

$$\dot{x} = f(x)$$

Example:

→ exp design

(Human intelligence)

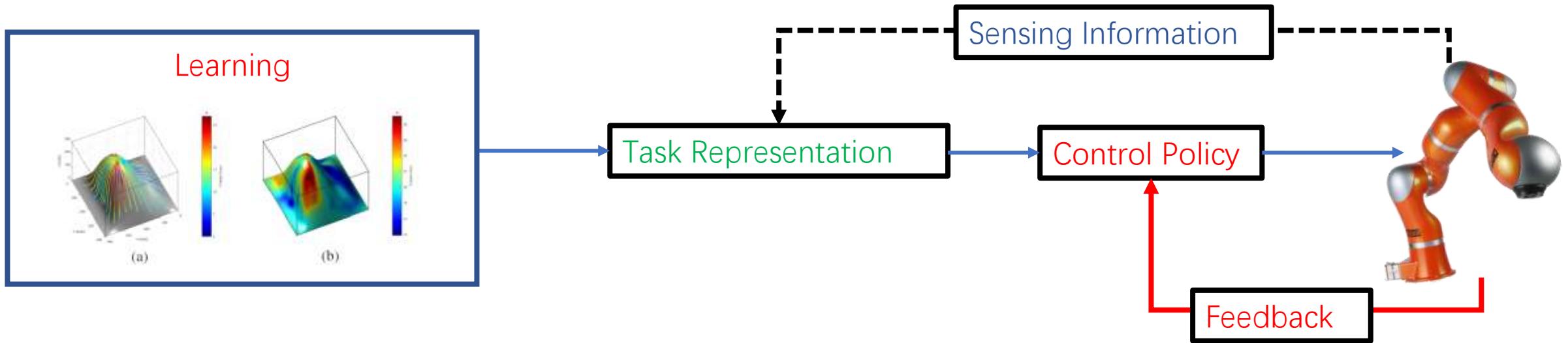
→ collect data $\{ \dot{x}_k, x_k \}_{k=1 \dots N}$ (pre-processing)

→ GMM (\dot{x}_k, x_k) Model training

→ Online prediction $\dot{x}_k \leftarrow GMRC(x_k)$



How to Implement?



Leverage the power of learning techniques and nonlinear control



Learning algorithms

LWR

C. G. Atkeson, A. W. Moore, and S. Schaal. Locally weighted learning for control. *Artificial Intelligence Review*, 11(1-5):75–113, 1997

W.S. Cleveland. Robust locally weighted regression and smoothing scatterplots. *American Statistical Association* 74(368):829–836, 1979

GMR

Z. Ghahramani and M. I. Jordan. Supervised learning from incomplete data via an EM approach. In *Advances in Neural Information Processing Systems (NIPS)*, volume 6, pages 120–127, 1994

S. Calinon. Mixture models for the analysis, edition, and synthesis of continuous time series. *Mixture Models and Applications*, Springer, 2019

GPR

C.K.I. Williams and C.E. Rasmussen. Gaussian processes for regression. In *Advances in Neural Information Processing Systems (NIPS)*, pages 514–520, 1996

C.E. Rasmussen and C.K.I. Williams. *Gaussian processes for machine learning*. MIT Press, Cambridge, MA, USA, 2006

S. Roberts, M. Osborne, M. Ebden, S. Reece, N. Gibson, and S. Aigrain. Gaussian processes for time-series modelling. *Philosophical Trans. of the Royal Society A*, 371(1984):1–25, 2012

GPIS

O. Williams and A. Fitzgibbon. Gaussian Process Implicit Surfaces. In *Gaussian Processes in Practice*, 2007



Limitation of traditional learning algorithms

- Limited training data
- Can only handle vector state
- Typically assume a Gaussian distribution
- Assume continuous system
 - Difficult to model hybrid system
- Can not deal with multi-modal control
- Good at modeling motion primitive or low-level physical skill



Learning algorithms

exp design:

hardware

sensor

proto.col.

intention

interface

data collection:

joint angles

pos/rot

force

Tactile -
vision

:

Learning Alg

GMM

GP

SVM

:

Deep learning

LLM

RT-2.



Limits of IL

Problem 1: Correspondence Problem

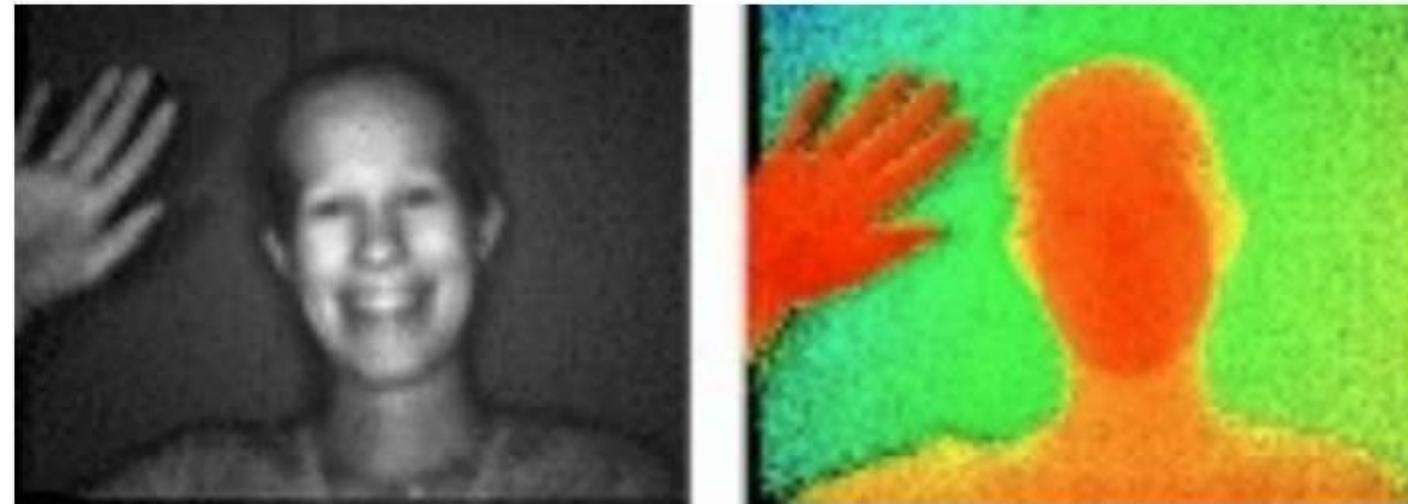


Even when the robot looks more like the human, its body does not have the same range and dynamics of motion.



Limits of IL

Problem 1: Correspondence Problem



Robots do not perceive things like we do.

Sonars, infrared sensors, lasers are common on robots and easier to process than information from cameras.

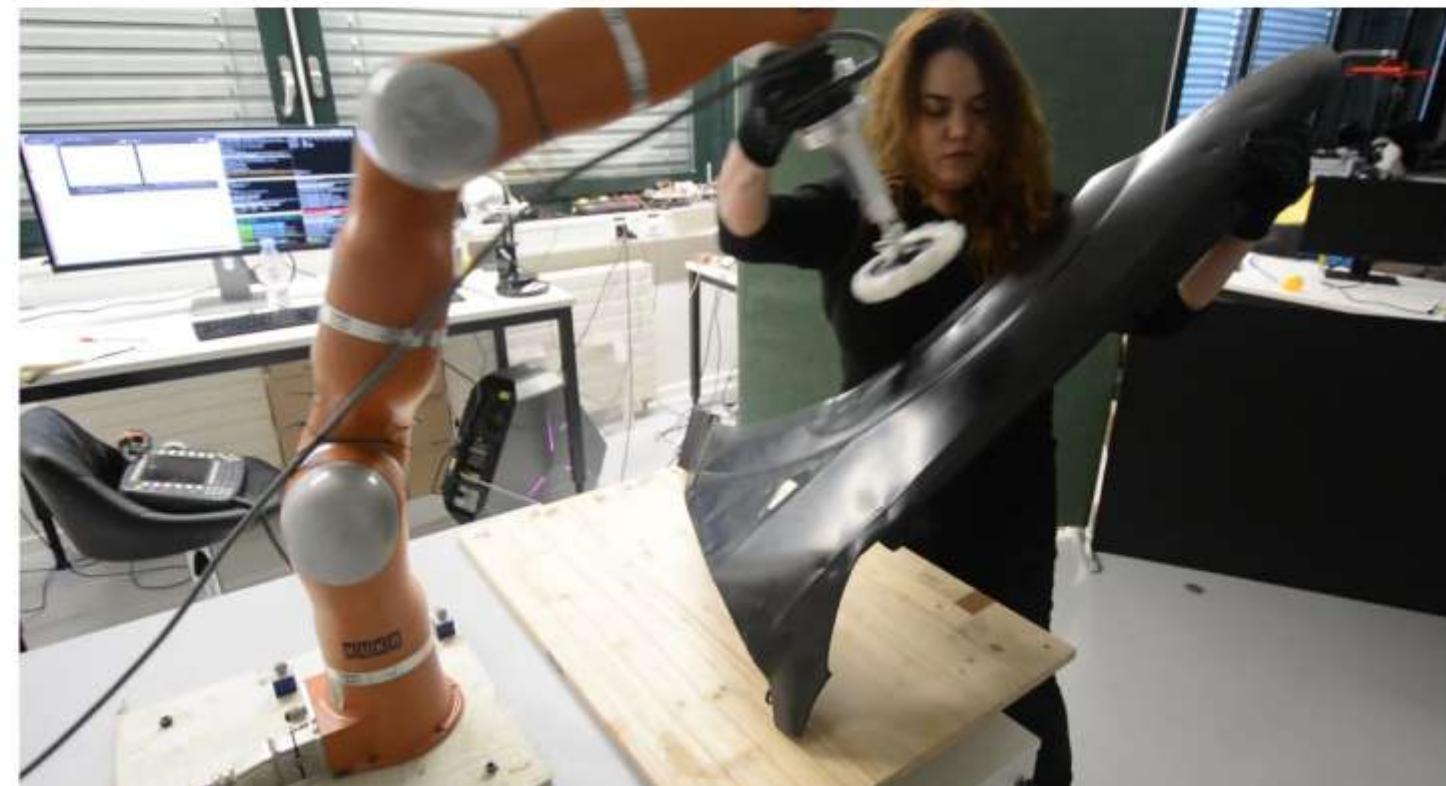


Limits of IL

Problem 1: Correspondence Problem

- Teachers need to train themselves before training the robots.

Sometimes
super herd!!!





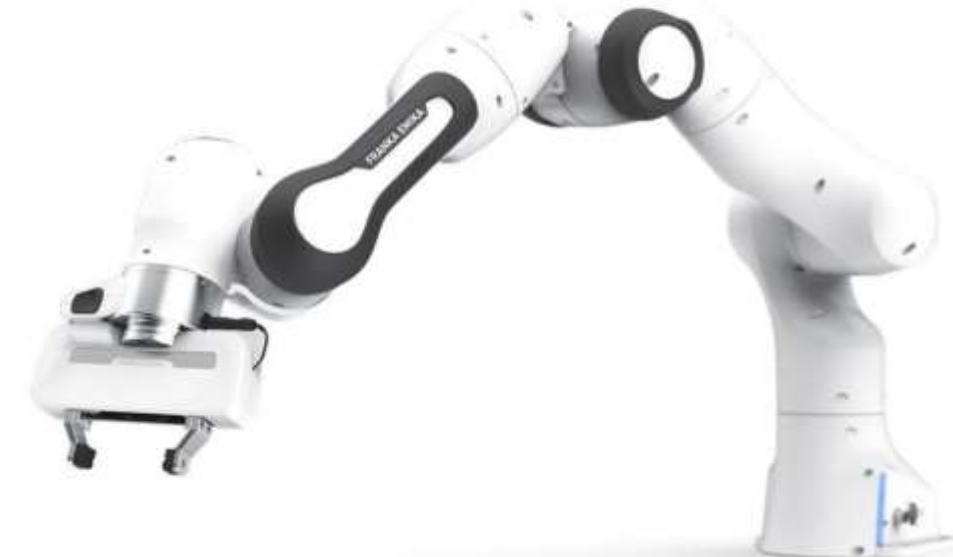
Limits of IL

Problem 2: Learning is Data-Sensitive

- Data is robot-dependent



UR5: 6DOF



Franka Panda: 7DOF



Limits of IL

Problem 2: Learning is Data-Sensitive

- Data is environment-dependent



Model Learned at EPFL



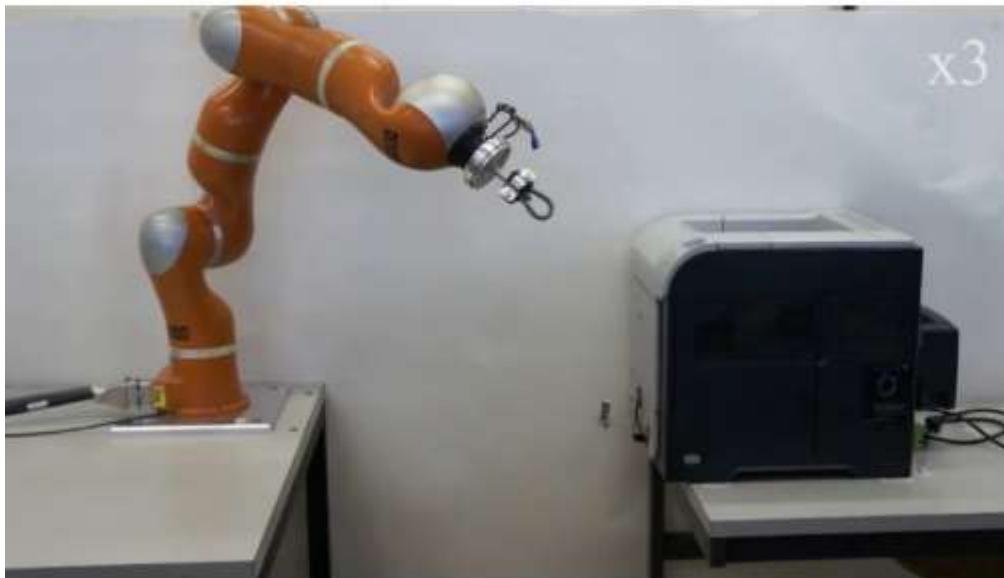
Model transferred at AIST/JRL



Limits of IL

Problem 2: Learning is Data-Sensitive

Need Transfer Learning methods



Model Learned at EPFL



Model transferred at AIST/JRL



Limits of IL

Problem 3: Variability in Task Definition

- Question: **What does it mean to perform a task?**
- Multiple ways to accomplish a task:
 - multiple motions





Limits of IL

Problem 3: Variability in Task Definition

- Question: **What does it mean to perform a task?**
- Multiple ways to accomplish a task:
 - multiple motions
 - multiple tools





Limits of IL

Current/Future Research Directions: Learn from Small Datasets

- Learn from small datasets: Reduce the number of demonstrations needed
- Combine heterogeneous data types
- Improve teaching interactions

one-shot learning



Today agenda

- Paper reading (~30 mins)
- Why imitation learning (IL) (~5)
- Key ingredients of IL (~5)
- Data collection (~5)
- Learning algorithms (~20)
- Limits of IL (~5)
- Examples and applications (~20)
 - Motion
 - Hand IK
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Applications

Modelling Hitting Task using Dynamical Systems-Based Control

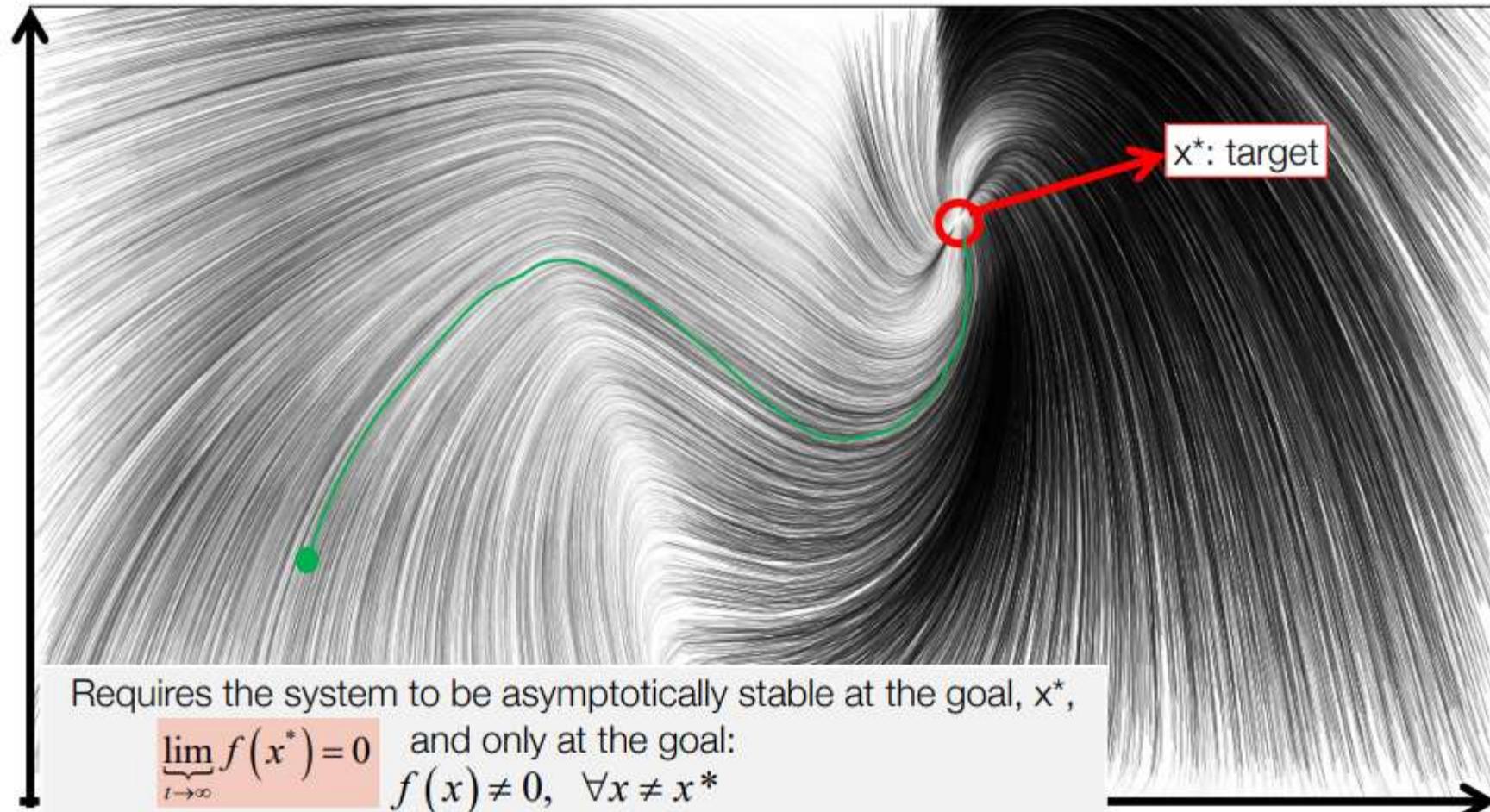
- Collect Demonstrations of hitting a golf ball using kinesthetic teaching
- Collect the recorded robot states and velocity at each time step
- We could generate a dynamical system representing this motion:
$$\dot{x} = f(x)$$





Applications

Modelling Hitting Task using Dynamical Systems-Based Control

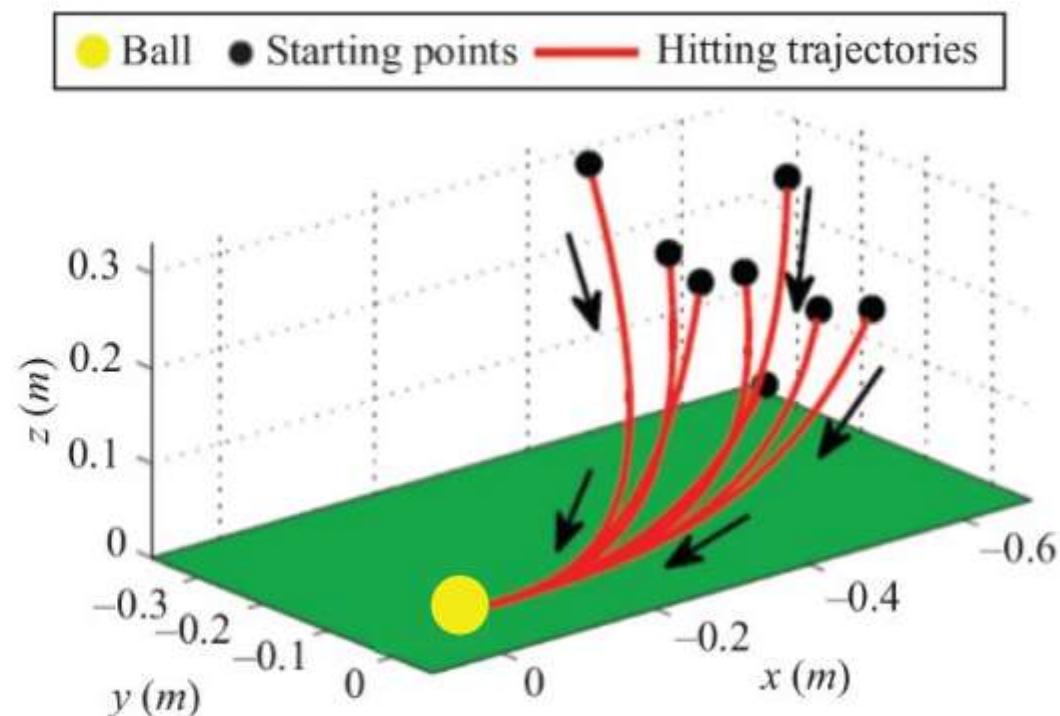




Applications

Modelling Hitting Task using Dynamical Systems-Based Control

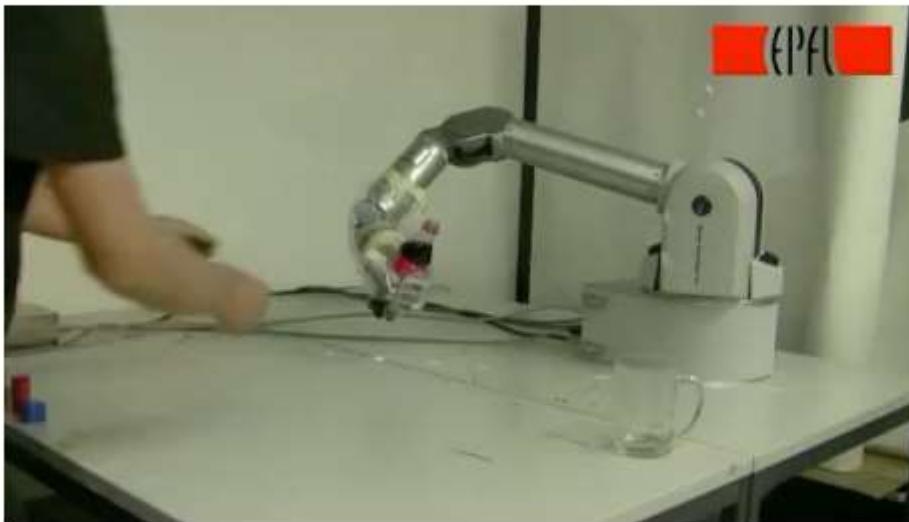
- We could generate a dynamical system representing this motion:
 $\dot{x} = f(x)$
- Guarantees asymptotically reaching and stabilizing at attractor: $\lim_{\{t \rightarrow \infty\}} x = x^*$, where
 x^* : Ball Location





Applications

Teaching Compliant Control: What happens when stiffness not considered?



Too stiff: Liquid spills from jerking



Too compliant: Liquid spills from glass

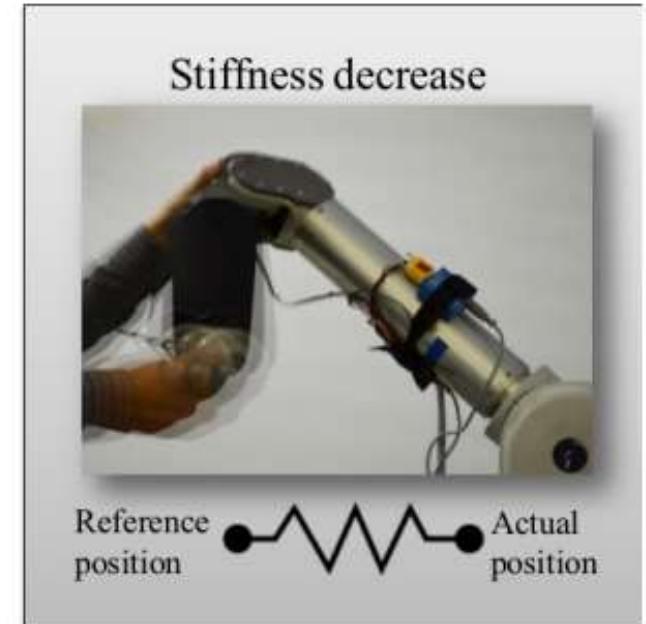
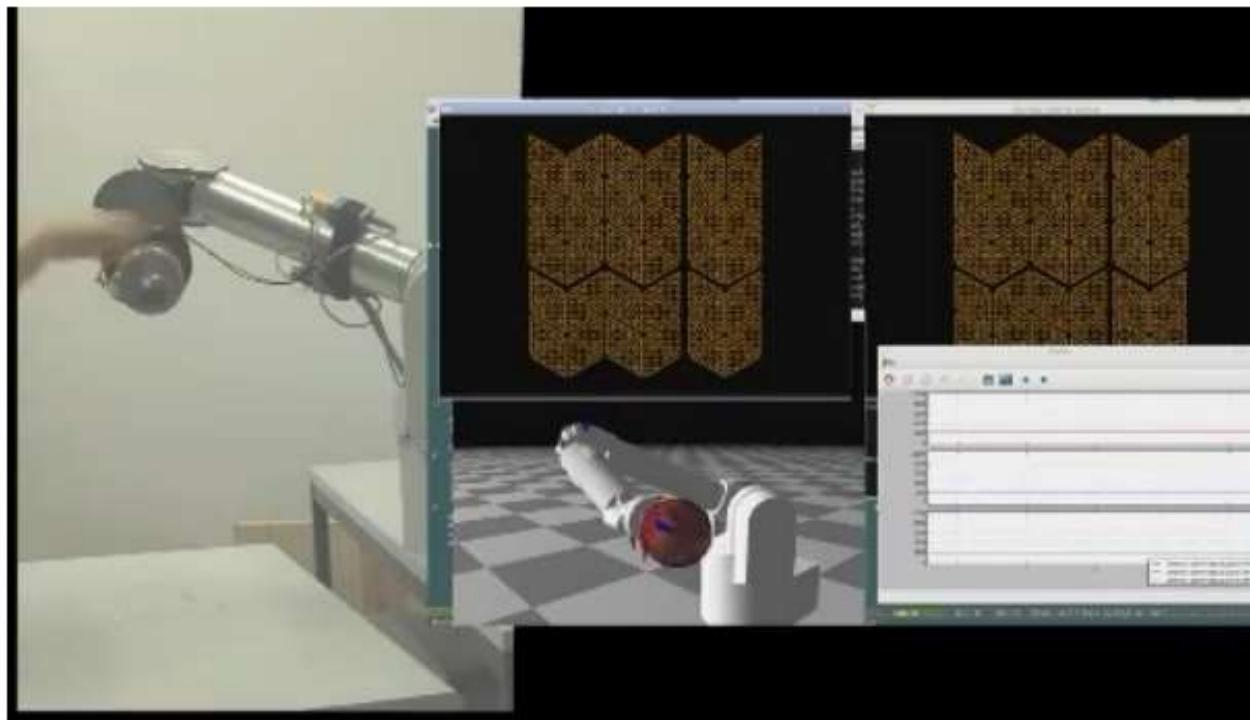
How can we teach robot when to increase and decrease compliance?



Applications

Teaching Compliant Control: Adding Compliance

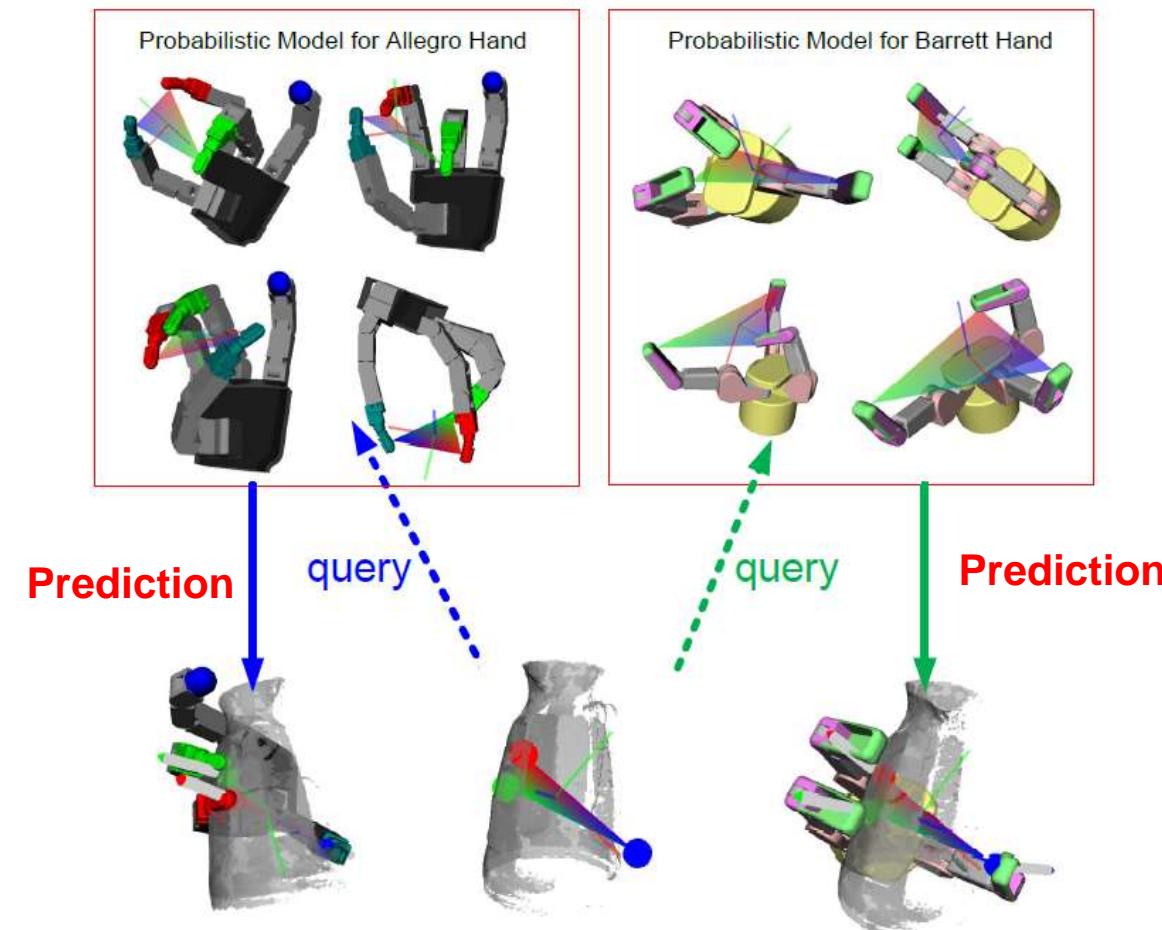
Teaching *decrease* in stiffness by wiggling the robot





Applications

Probabilistic Hand Inverse Kinematics





Applications

Virtual Frame



$$\{\mathcal{G}^i, i = 1 \dots N_g\}$$

Grasp Configuration $\mathcal{G} = \{\Theta, L, N\}$

$$L = [L_1, L_2, L_3] \in \mathbb{R}^3$$

$$L_i = \|\mathbf{p}^i - \mathbf{p}^o\|$$

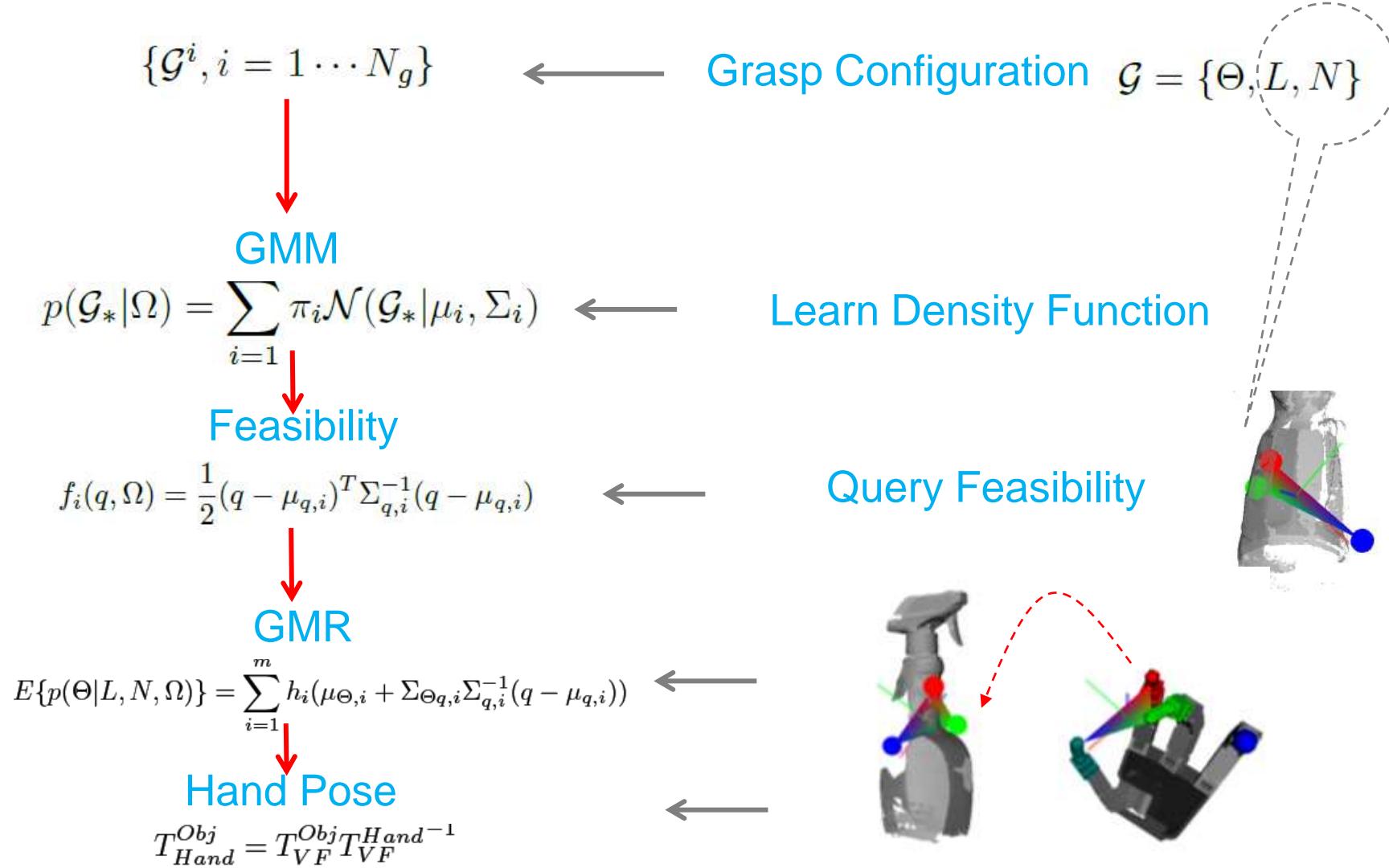
$$N = [N_1, N_2, N_3] \in \mathbb{R}^3$$

$$N_2 = \mathbf{n}^1 \cdot \mathbf{n}^3$$

$$T_{VF}^{Hand} = \begin{bmatrix} R^o & \mathbf{p}^o \\ [0, 0, 0] & 1 \end{bmatrix} \in \mathbb{R}^{4 \times 4}$$

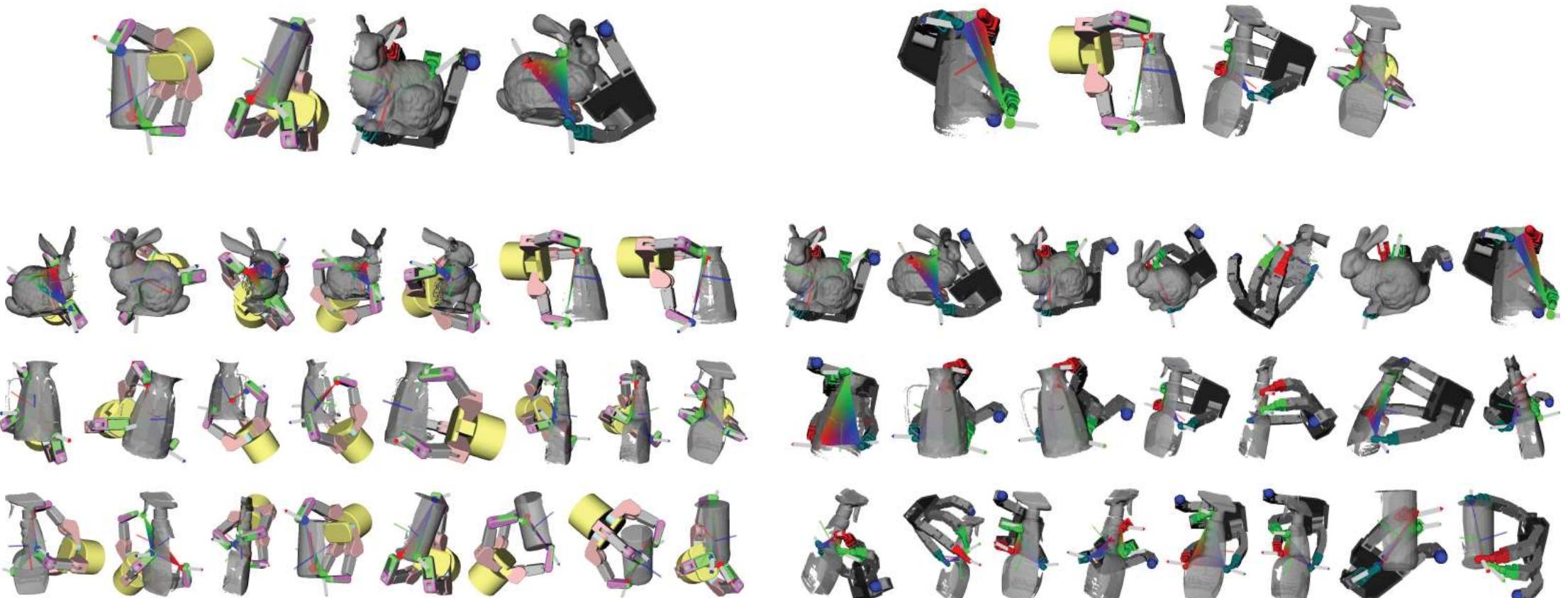


Applications



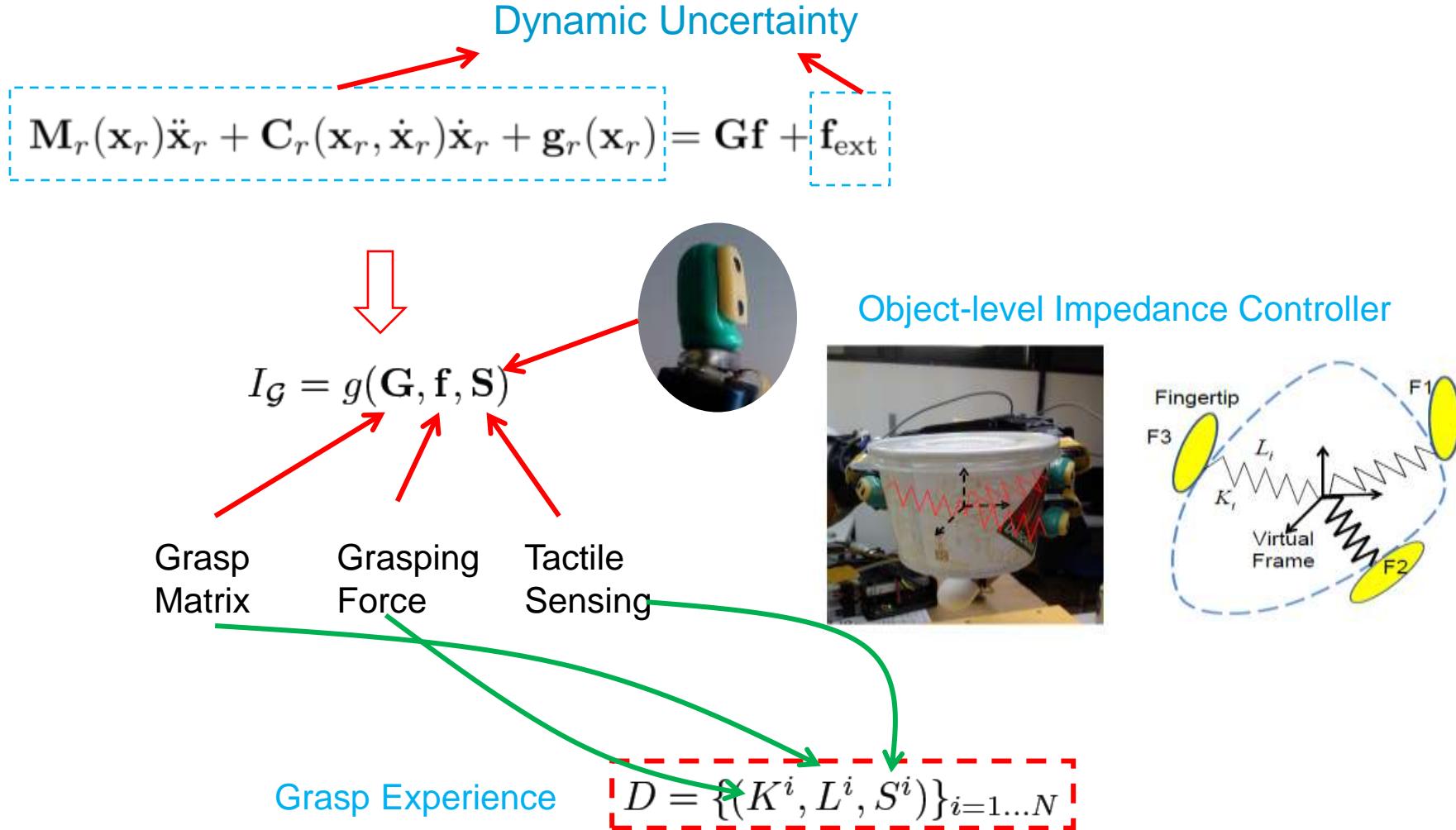


Applications





Applications





Applications

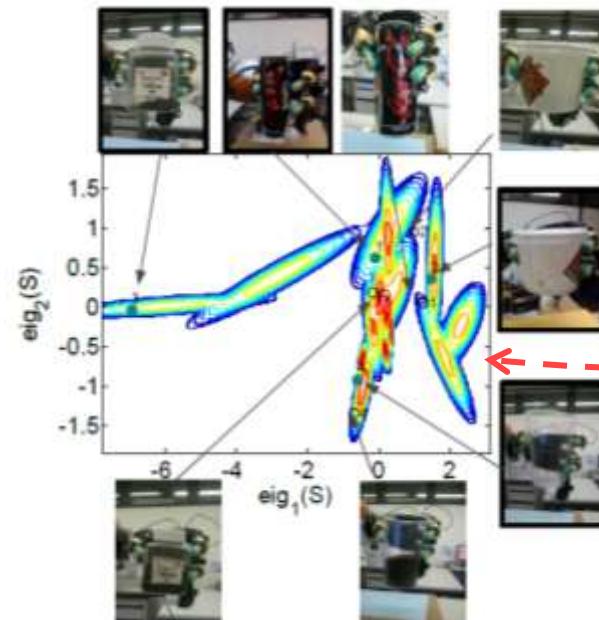
$$D = \{(K^i, L^i, S^i)\}_{i=1 \dots N}$$

Grasp Experience

$$X_* = (K_*, L_*, S_*)$$

$$p(X_* | \Omega) = \sum_{i=1}^m \pi_i \mathcal{N}(X_* | \mu_i, \Sigma_i)$$

Learn Density Function



Stability Estimation



Applications

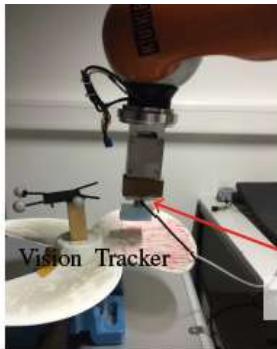
Learning of Grasp Adaptation through
Experience and Tactile Sensing

Miao Li, Yasemin Bekiroglu,
Danica Kragic and Aude Billard

IROS 2014

Experimental Results

Fan Blade Cleaning



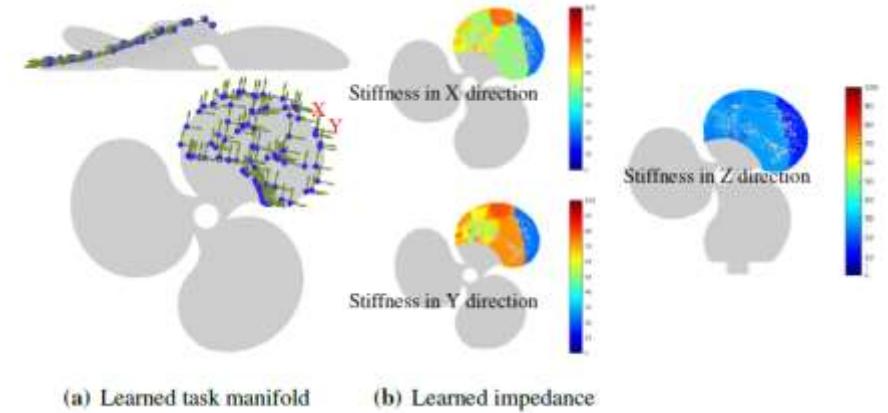
(a) Robot setup



(b) Human demonstration

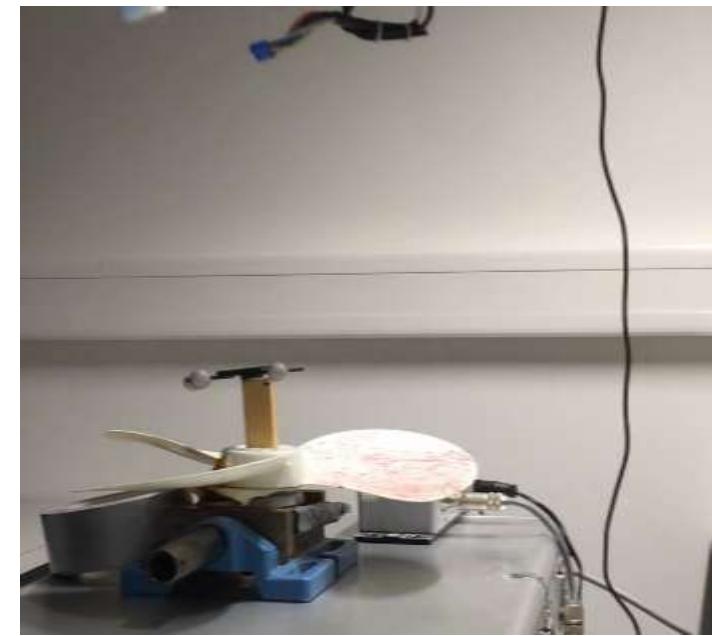
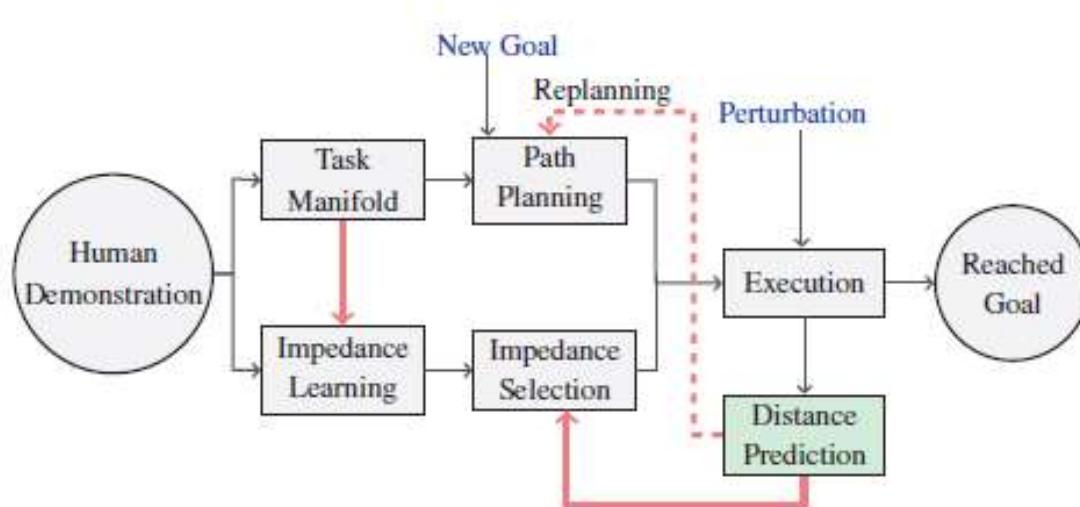


(c) Kinesthetic teaching

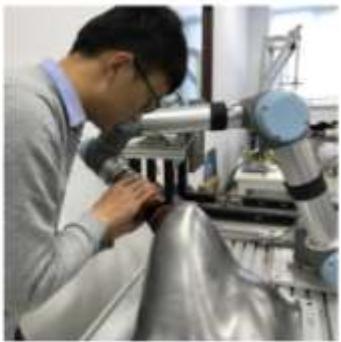


(a) Learned task manifold

(b) Learned impedance



Polishing



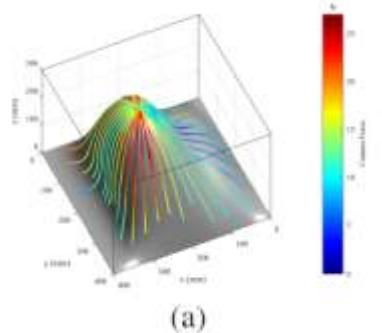
Learning force-dominant skills from human demonstration

Xiao Gao, Jie Ling, Xiaohui Xiao and Miao Li

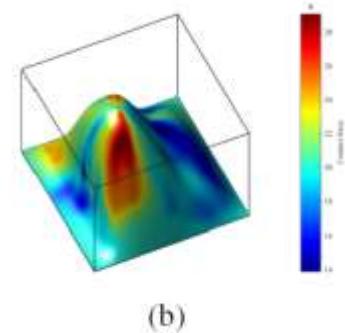


Xiao Gao

This video is submitted to IROS 2018



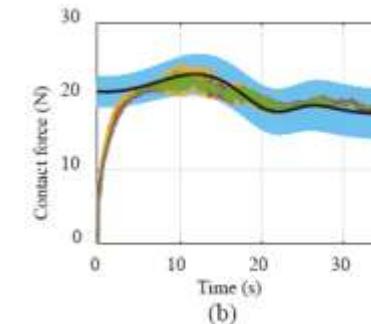
(a)



(b)



(a)



(b)

X. Gao *et al.* “Learning Force-dominant Skills from Human Demonstration”, Submitted to IROS 2018

Assembly

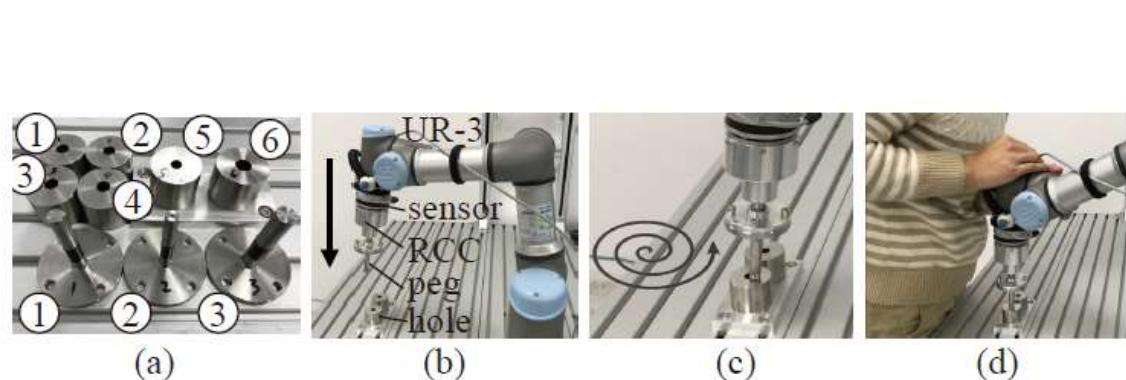
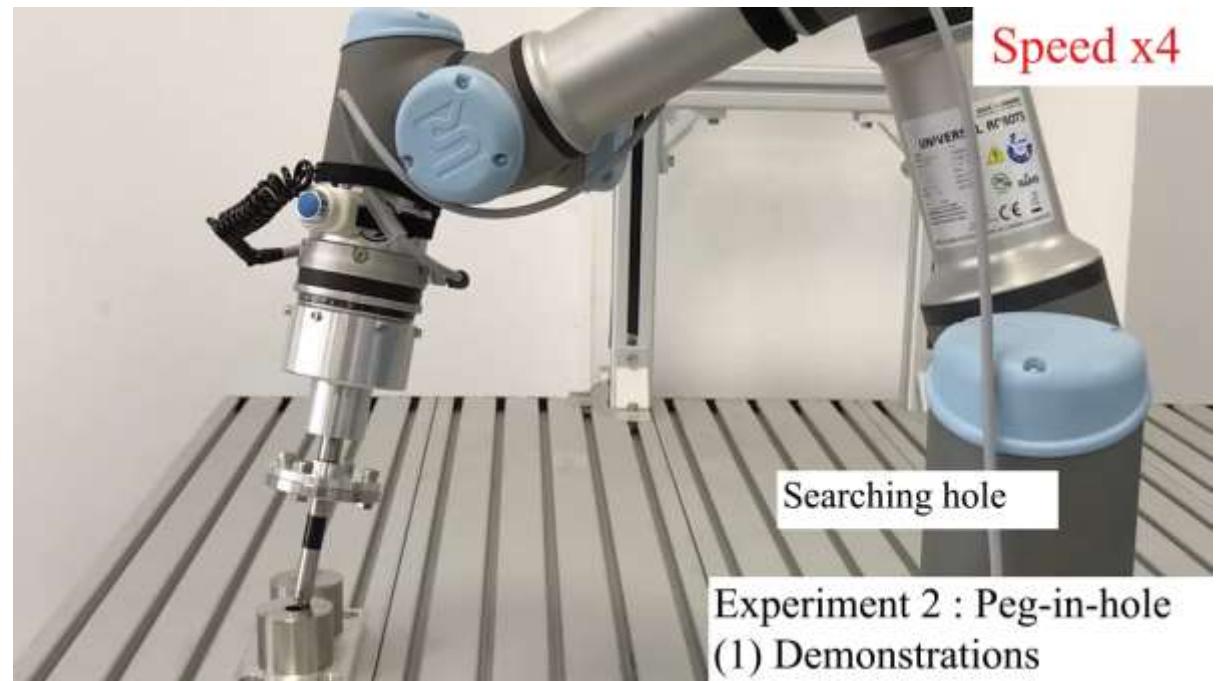
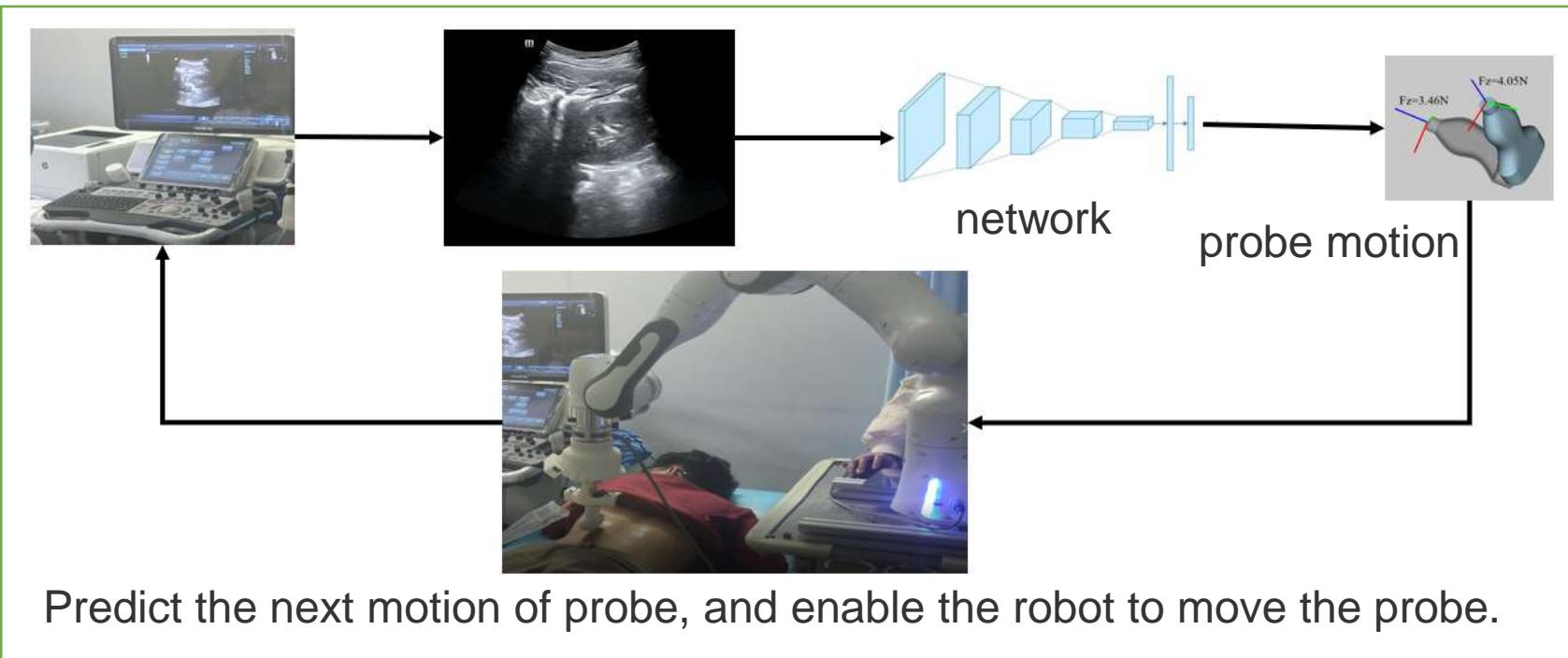
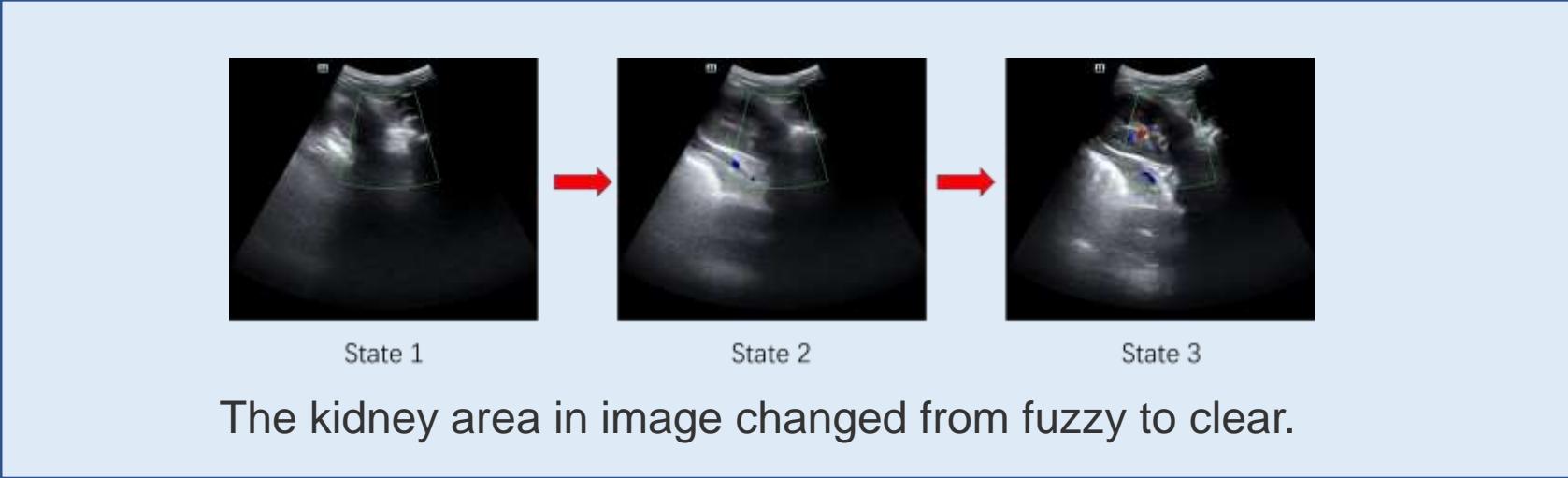


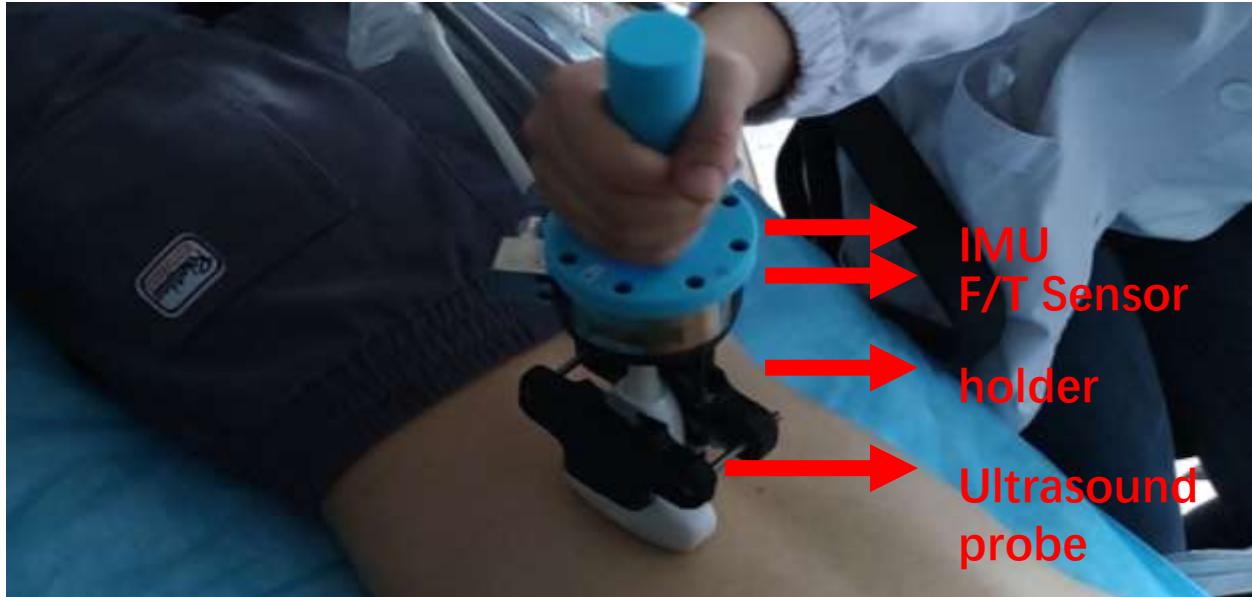
Fig. 12. Experiment setup and demonstration phase by collaborative insertions. **a:** The three pegs and six holes. **b:** The peg was moving towards the hole. **c:** Searching the hole by an Archimedean spiral movement. **d:** Collaborative insertions.



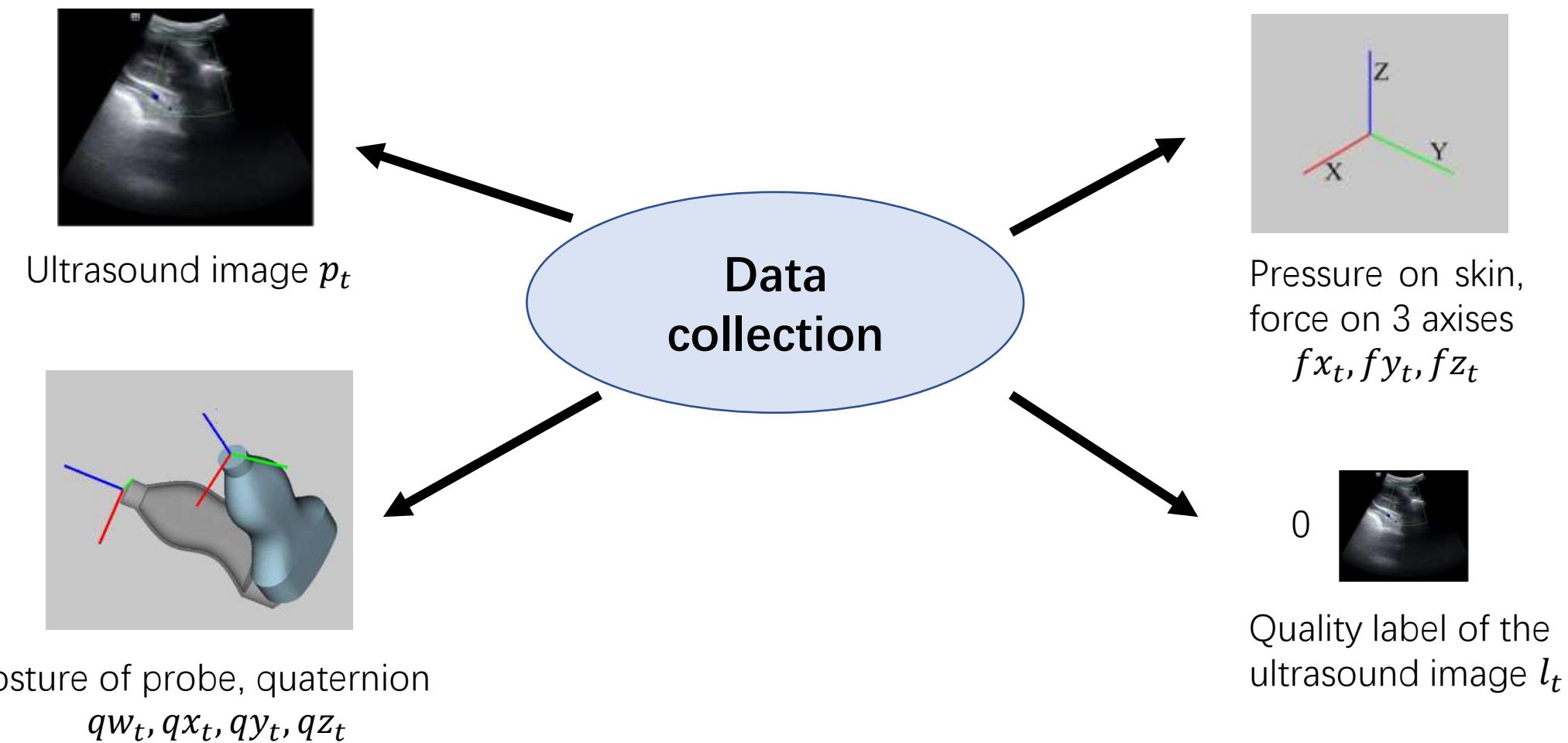
Learning the moving strategy of probe



Collect the probe motion data



Keep the contact point between the probe and the human body unchanged when collecting data.



Collect data from 5 persons

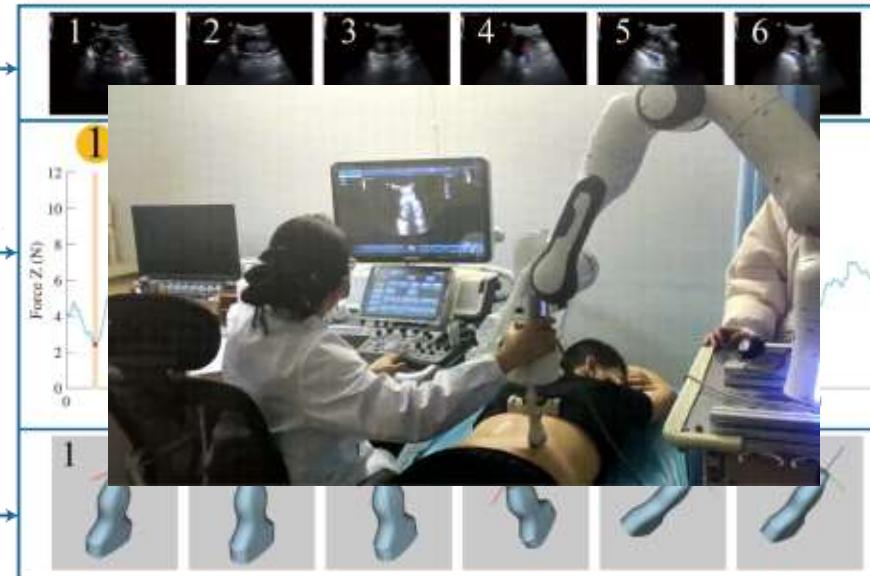
Person	1	2	3	4	5
Quantity of data	776	1348	596	919	1552



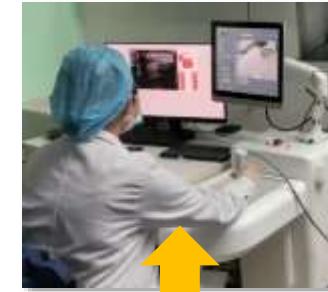
临床数据采集



多模态技能学习

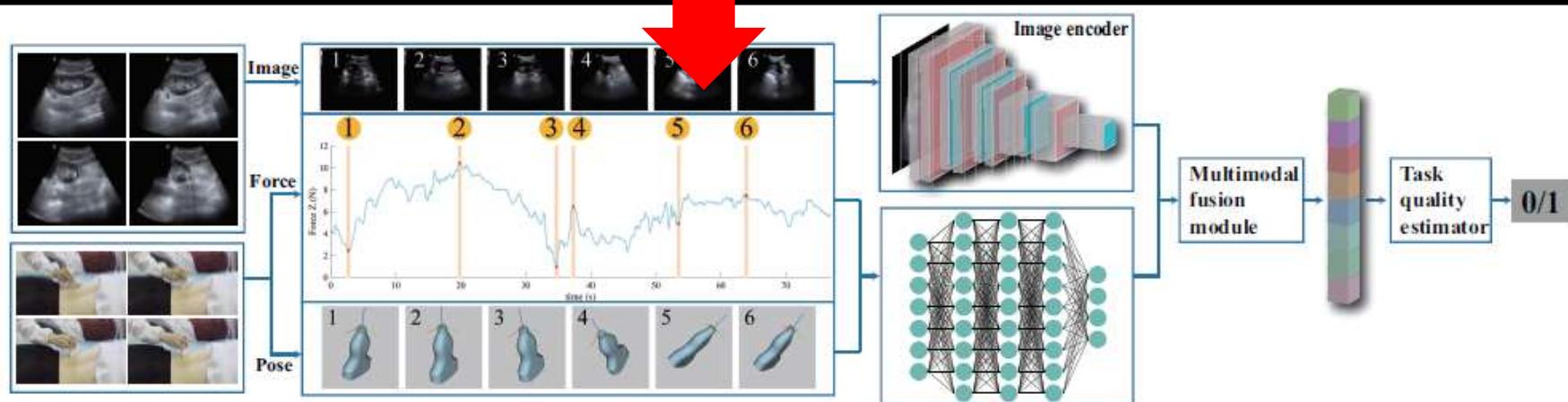


样机测试场景



robotic ultrasound system has become an emerging topic recently.

Learning of Robotic Ultrasound Scanning Skills Through
Experience and Guided Exploration





Goal for this course

- Design: soft hand design **x1**
- Perception: vision, point cloud, tactile, force/torque **x1**
- Planning: sampling-based, optimization-based, learning-based **x3**
- Control: feedback, multi-modal **x2**
- Learning: imitation learning, RL **x2**
- Simulation tool (pybullet, matlab, OpenRAVE, Issac Nvidia, Gazebo)
- How to get a robot moving!

Robotics today !

Learning Object-level Impedance Control for Robust Grasping and Dexterous Manipulation

Miao Li*, Hang Yin*, Kenji Tahara+, and Aude Billard*

*Learning Algorithms and Systems Laboratory (LASA)

Ecole Polytechnique Federale de Lausanne (EPFL)

+Faculty of Engineering, Kyushu University, Japan

ICRA-2014, HongKong

Overview

“Learning Object-level Impedance Control for Robust Grasping and Dexterous Manipulation”

Motivation

Model — Object-level Impedance Controller

Approach — Learning from Human Demonstration

Experiments and implementation

Conclusion

Motivation

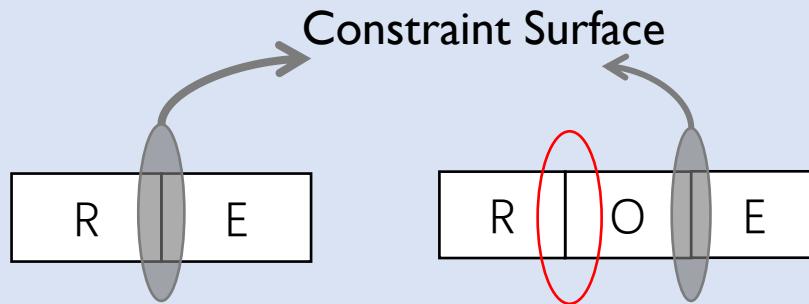
How to specify the proper impedance for a given task?

Our Answer:

The desired **object-level** impedance can be learnt from
human demonstration

Motivation

Contact Task:



- R: robot
- O: object
- E: environment



Object-level Impedance Control



Robust
Grasping

Dexterous
Manipulatio
n



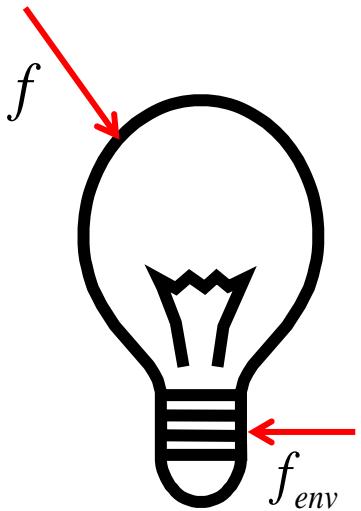
Keep object stable

Object-Centric

Move object to
desired configuration

The desired interactions are represented in the object frame

Object-level Impedance Control

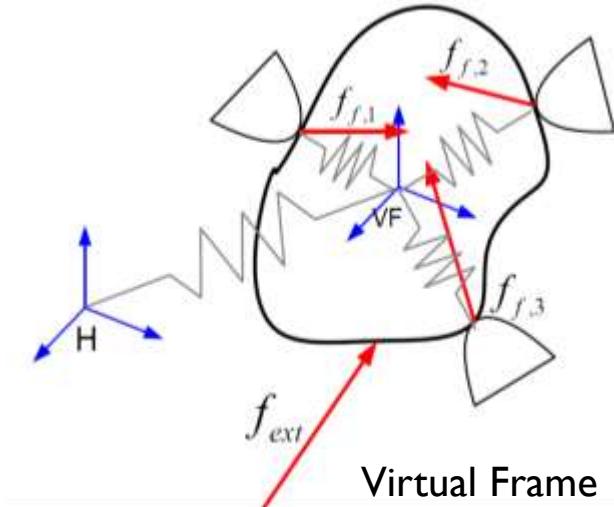


Object Dynamics:

$$\mathbf{f} + \mathbf{f}_{env} = m\ddot{\mathbf{x}}$$

Desired Behavior:

$$\mathbf{f}_{env} = M\ddot{\mathbf{x}} + D(\dot{\mathbf{x}} - \dot{\mathbf{x}}_d) + K(\mathbf{x} - \mathbf{x}_d)$$



Object-level Impedance Control

$$\mathbf{f} = mM^{-1}D(\dot{\mathbf{x}}_d - \dot{\mathbf{x}}) + mM^{-1}K(\mathbf{x}_d - \mathbf{x}) + (mM^{-1} - I)\mathbf{f}_{env}$$

Object-level Impedance Control

$$\mathbf{f} = mM^{-1}D(\dot{\mathbf{x}}_d - \dot{\mathbf{x}}) + mM^{-1}K(\mathbf{x}_d - \mathbf{x}) + (mM^{-1} - I)\mathbf{f}_{env}$$

Actual Trajectory

Object-level Impedance Control

$$\mathbf{f} = mM^{-1}D(\dot{\mathbf{x}}_d - \dot{\mathbf{x}}) + mM^{-1}K(\mathbf{x}_d - \mathbf{x}) + (mM^{-1} - I)\mathbf{f}_{env}$$

The diagram illustrates the decomposition of force into three components. A vertical arrow points upwards, representing the desired trajectory. A diagonal arrow points from left to right, representing the actual trajectory. A red diagonal arrow points from the origin towards the top-right, representing the environment interaction. The equation above the diagram shows how these components are combined to produce the total force \mathbf{f} .

Desired Trajectory Actual Trajectory

Object-level Impedance Control

$$\mathbf{f} = mM^{-1}D(\dot{\mathbf{x}}_d - \dot{\mathbf{x}}) + mM^{-1}K(\mathbf{x}_d - \mathbf{x}) + (mM^{-1} - I)\mathbf{f}_{env}$$

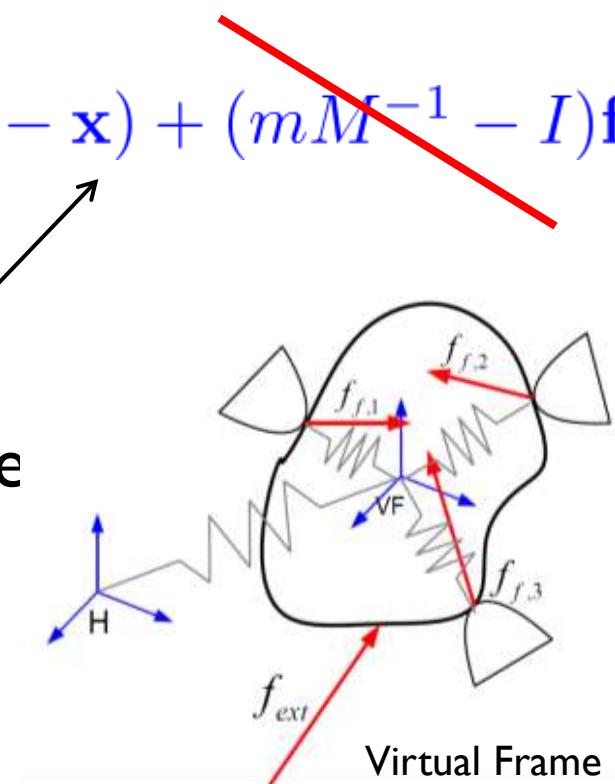
The diagram illustrates the decomposition of force into desired and actual trajectory components. It shows two vectors originating from the same point: a vertical arrow labeled "Desired Trajectory" pointing upwards, and a diagonal arrow labeled "Actual Trajectory" pointing towards the top-right. A third vector, representing the total force, is shown as a diagonal line segment starting from the tip of the "Actual Trajectory" arrow and ending at the tip of the "Desired Trajectory" arrow. Red circles highlight the terms $mM^{-1}D(\dot{\mathbf{x}}_d - \dot{\mathbf{x}})$ and $mM^{-1}K(\mathbf{x}_d - \mathbf{x})$ in the equation, while a red line through $(mM^{-1} - I)\mathbf{f}_{env}$ indicates it is being subtracted.

Object-level Impedance Control

$$\mathbf{f} = mM^{-1}\mathbf{D}(\dot{\mathbf{x}}_d - \dot{\mathbf{x}}) + mM^{-1}\mathbf{K}(\mathbf{x}_d - \mathbf{x}) + (mM^{-1} - I)\mathbf{f}_{env}$$

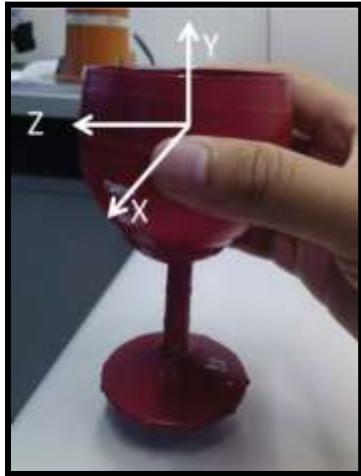
Desired Trajectory

Actual Traje



Robust Grasping

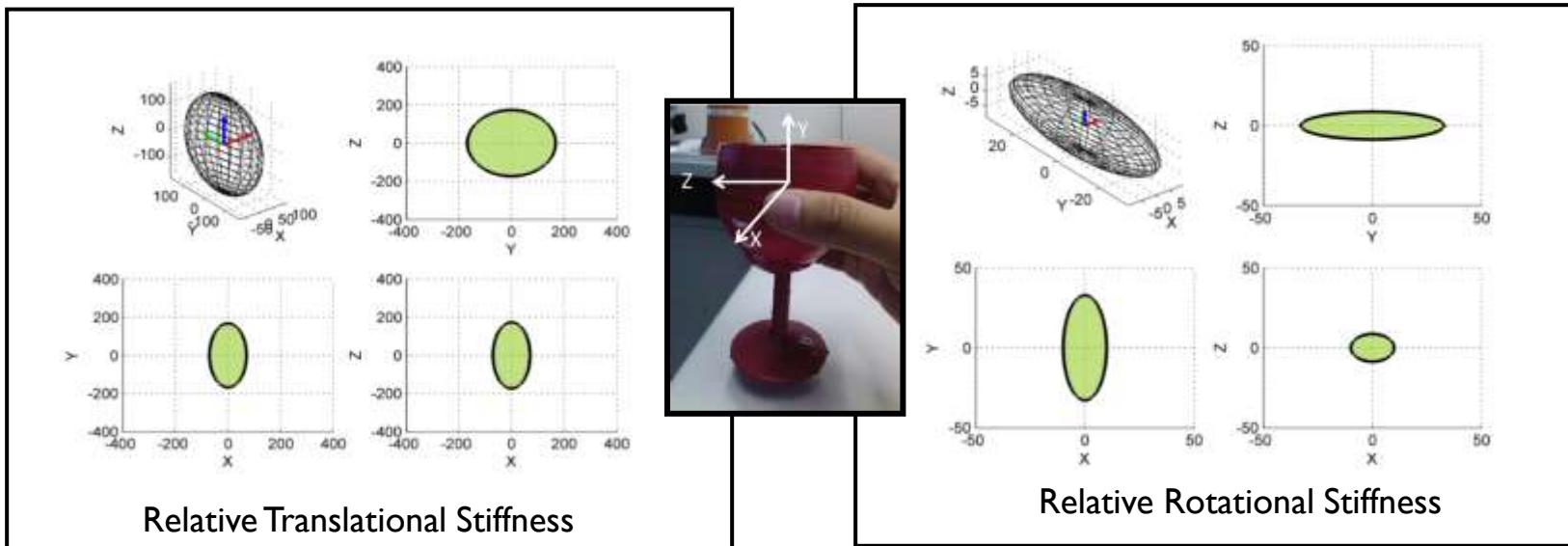
$$\mathbf{f} = D(\dot{\mathbf{x}}_d - \dot{\mathbf{x}}) + K(\mathbf{x}_d - \mathbf{x})$$



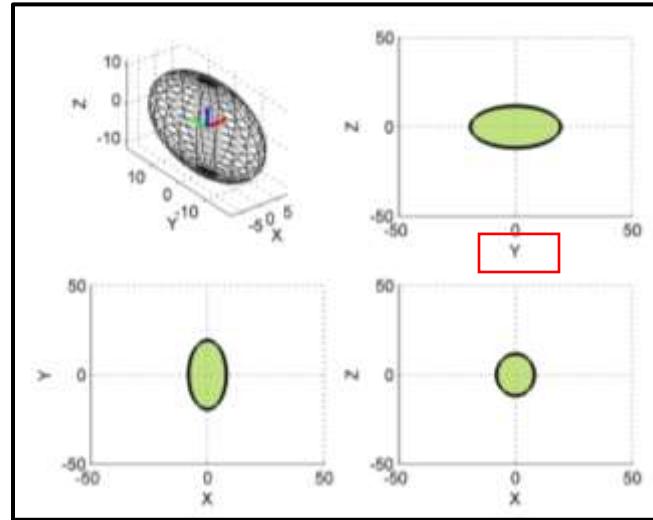
Relative Stiffness: the object stiffness in one direction is inversely proportional to the variance of displacement under perturbation in the corresponding direction

Robust Grasping

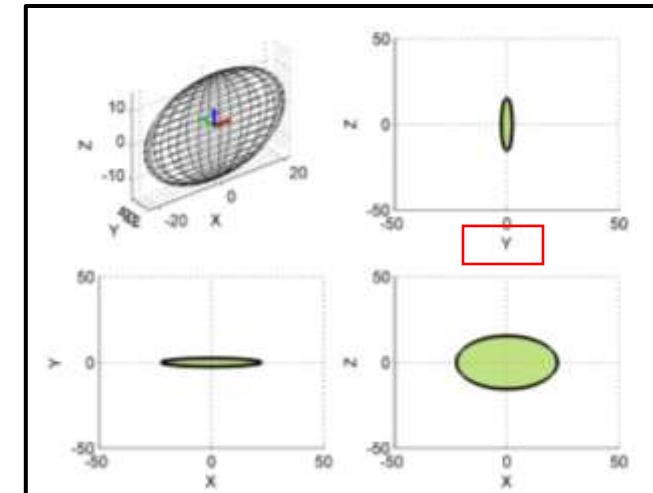
$$K = \alpha \left\{ \frac{1}{N} \sum_{i=1}^N (\mathbf{x}^i - \mathbf{x}_r)(\mathbf{x}^i - \mathbf{x}_r)^T \right\}^{-1}$$



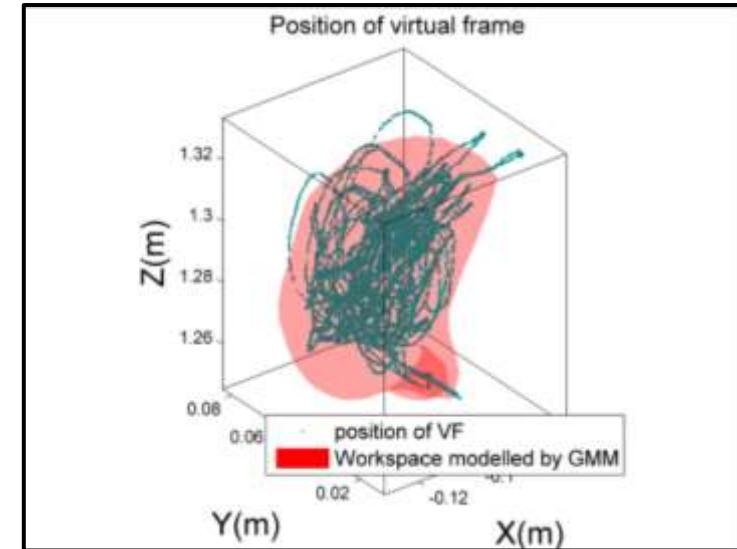
Robust Grasping



Relative Rotational Stiffness



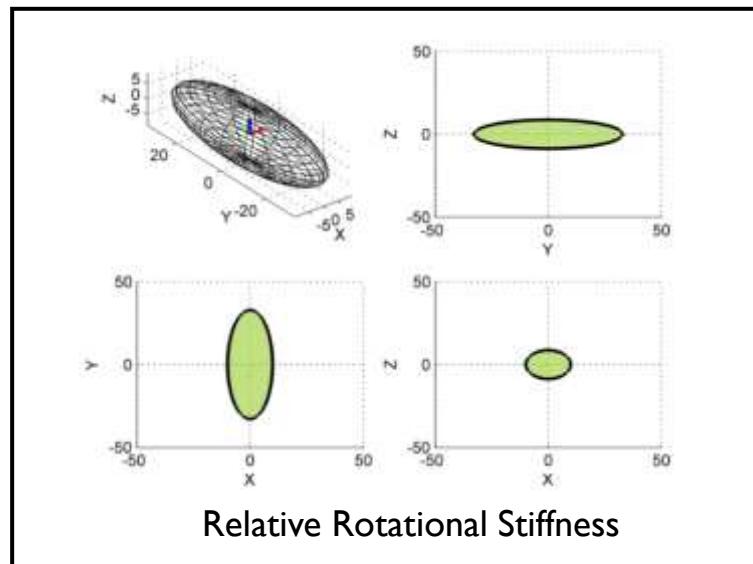
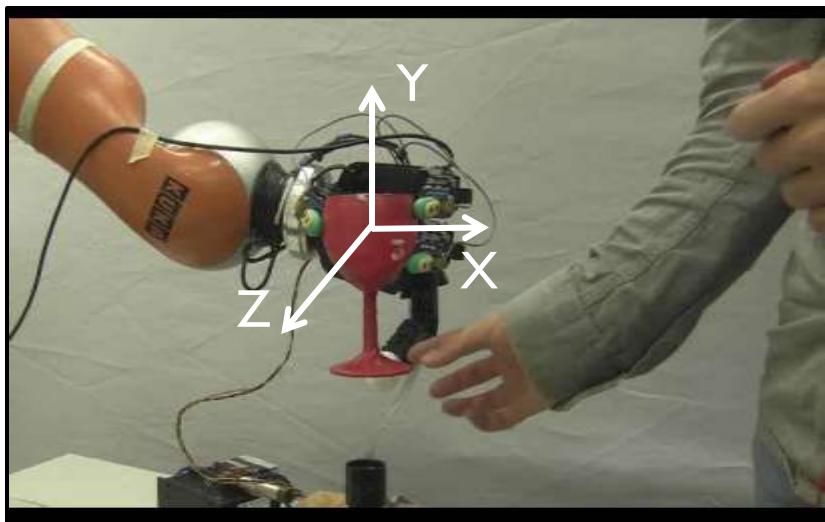
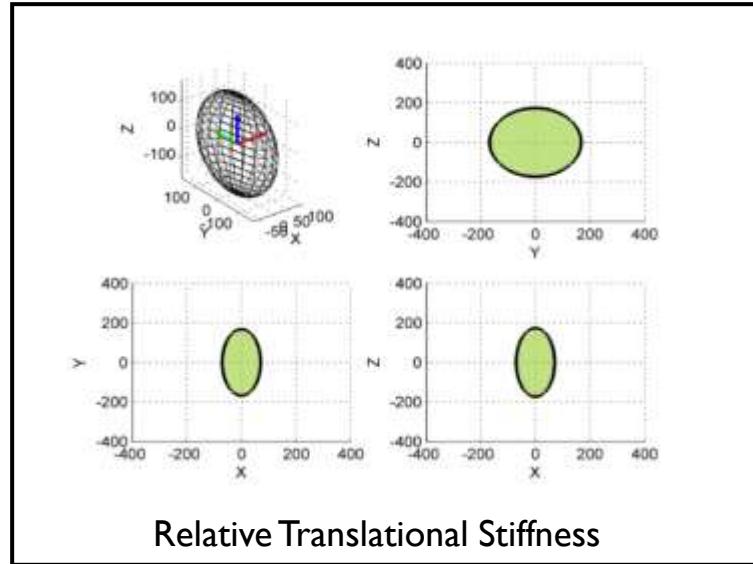
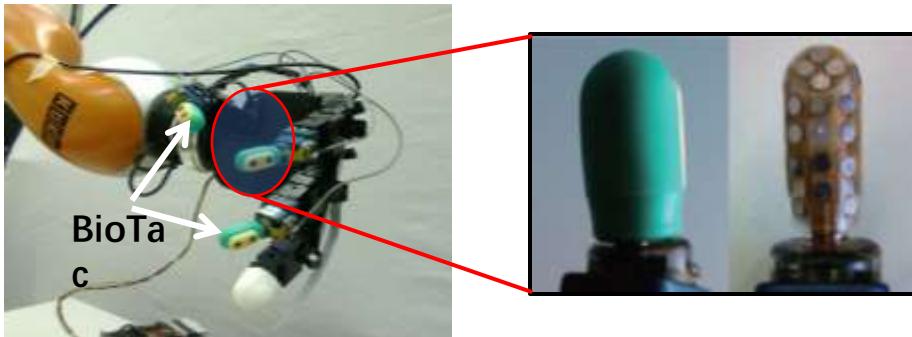
Robust Grasping: Workspace



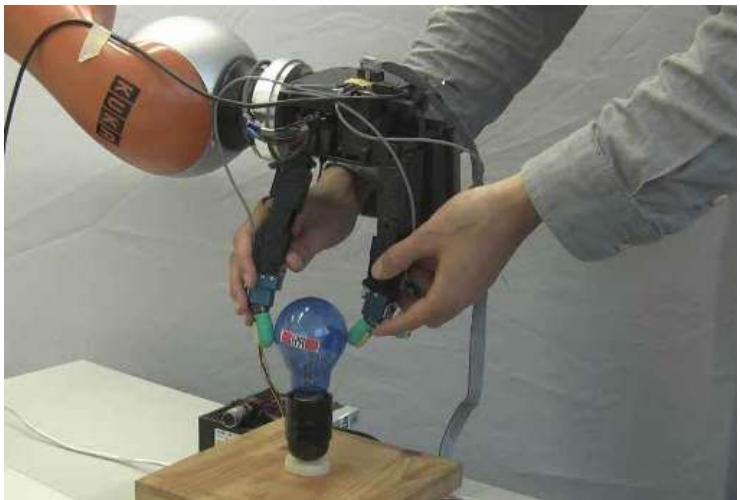
$$p(\mathbf{x}) = \sum_{k=1}^K \pi_k \mathcal{N}(\mathbf{x} | \boldsymbol{\mu}_k, \boldsymbol{\Sigma}_k)$$

$$K = \alpha \left\{ \frac{1}{N} \sum_{i=1}^N (\mathbf{x}^i - \mathbf{x}_r)(\mathbf{x}^i - \mathbf{x}_r)^T \right\}^{-1}$$

Robust Grasping



Dexterous Manipulation



Human demonstration

Optimization:

$$\min_{K, \mathbf{x}_r} \sum_{i=1}^{N_t} \|\mathbf{f}_{f,o}(i) - \{K(\mathbf{x}_r - \mathbf{x}(i))\}\|^2$$

s.t.

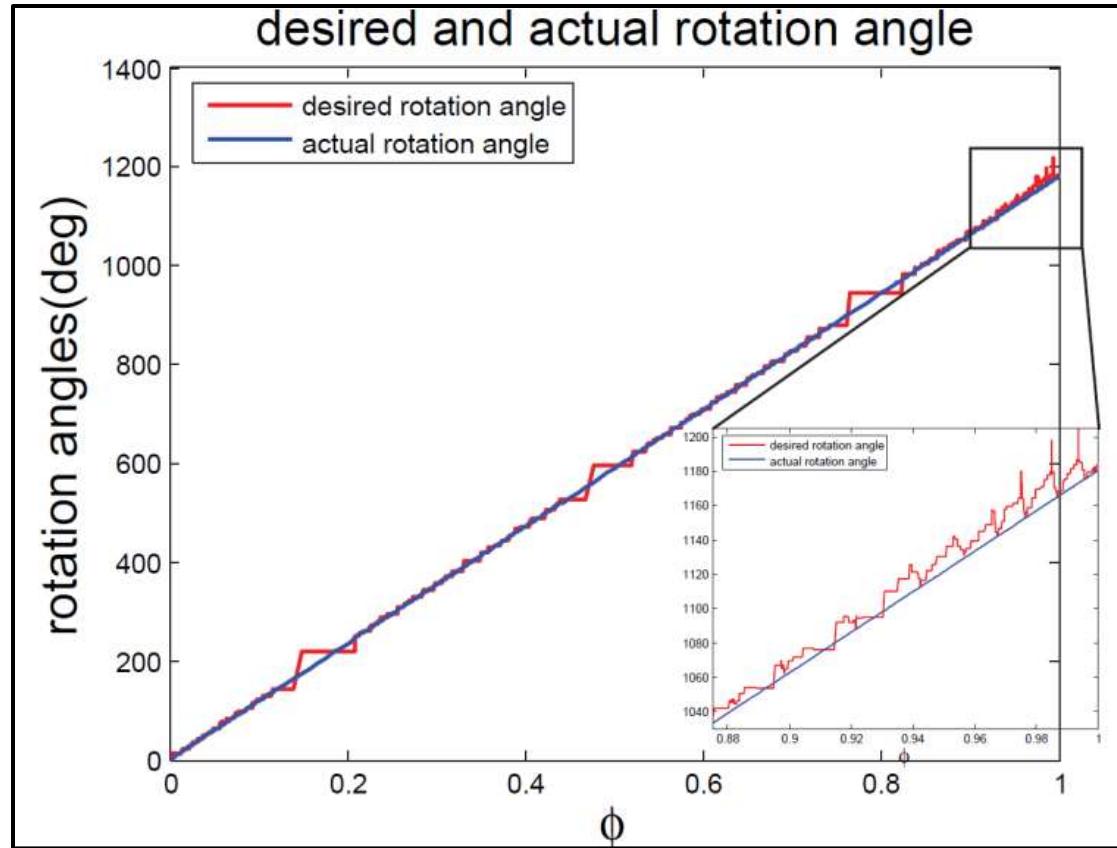
$$K_{i,j} \leq k_{lim}, \quad i = 1 \dots 6, j = 1 \dots 6;$$

$$\|\mathbf{x}_r - \mathbf{x}(i)\| \leq \Delta x_{lim}, \quad i = 1 \dots N_t;$$

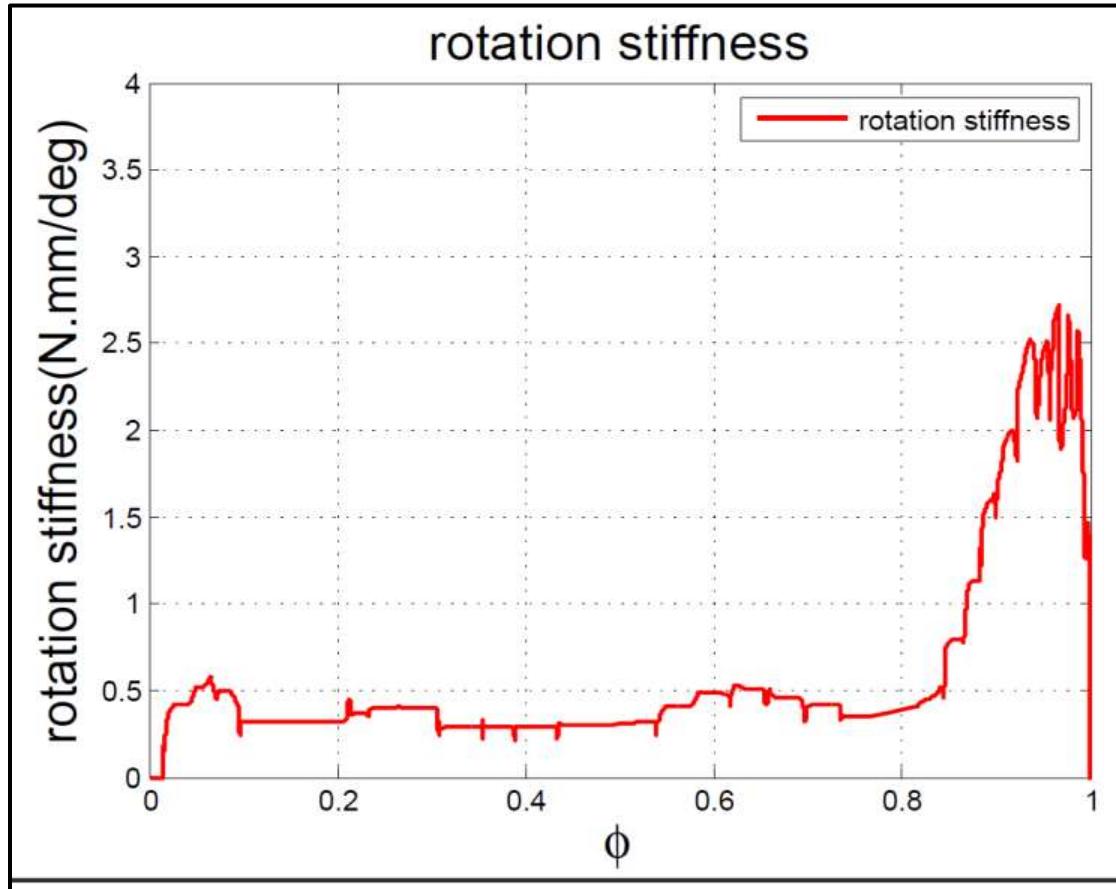
$$\|\dot{\mathbf{x}}_r - \dot{\mathbf{x}}(i)\| \leq \Delta \dot{x}_{lim}, \quad i = 1 \dots N_t;$$

Stiffness Learning: the object force and motion are recorded from human demonstration, and used to learn an impedance model.

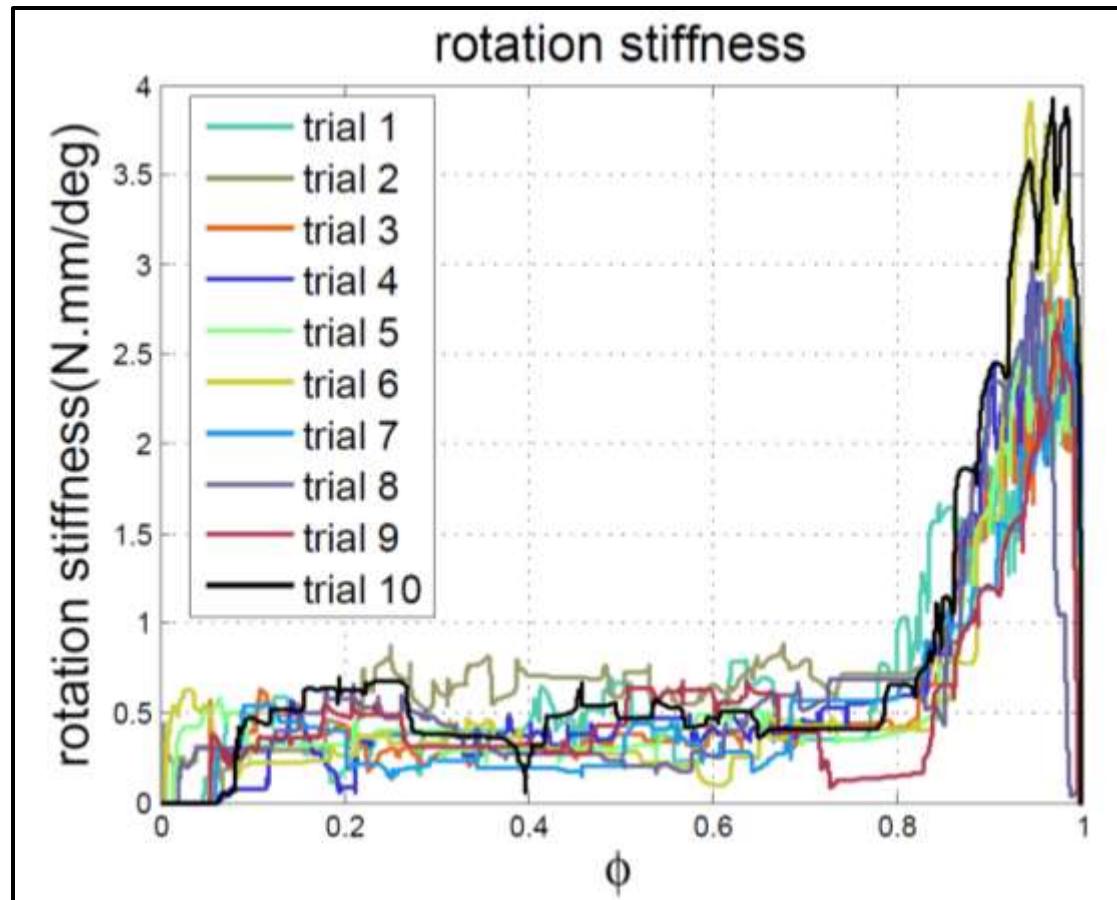
Dexterous Manipulation



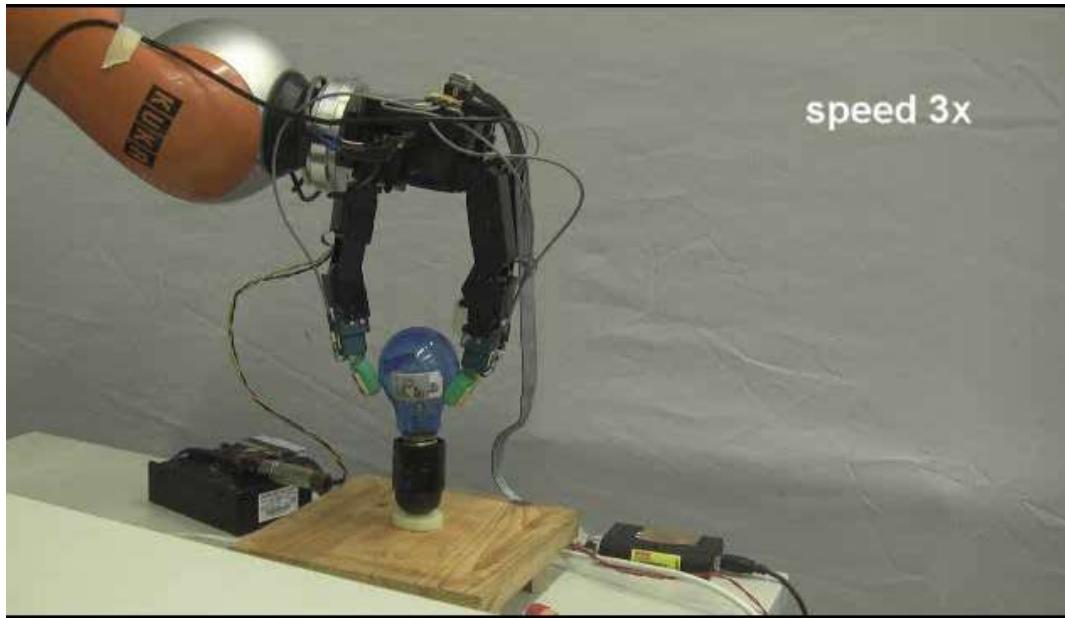
Dexterous Manipulation



Dexterous Manipulation



Dexterous Manipulation



Conclusion

- We introduced an **object-level impedance learning approach** for robust grasping and dexterous manipulation.
- We modeled the boundary of the **workspace** using a Gaussian Mixture Model.
- This learning approach could be **applied in multiple ways**, such as grasp adaptation (IROS 2014 paper), grasp synthesis and tool use tasks.

Miao Li, Yasemin Bekiroglu, Danica Kragic and Aude Billard, “Learning of Grasp Adaptation through Experience and Tactile Sensing”, IROS 2014

Thanks for your attention!



Swiss National Center of Robotics Research

JSPS Grant-in-Aid for Young Scientists
(A) (25700028)