



# Robotics

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# Goal for this course

- Design: soft hand design **x1**
- Perception: vision, point cloud, tactile, force/torque **x1**
- Planning: sampling-based, optimization-based, learning-based **x3**
- Control: feedback, multi-modal **x2**
- Learning: imitation learning, RL **x2**
- Simulation tool (pybullet, matlab, OpenRAVE, Issac Nvidia, Gazebo)
- **How to get a robot moving!**

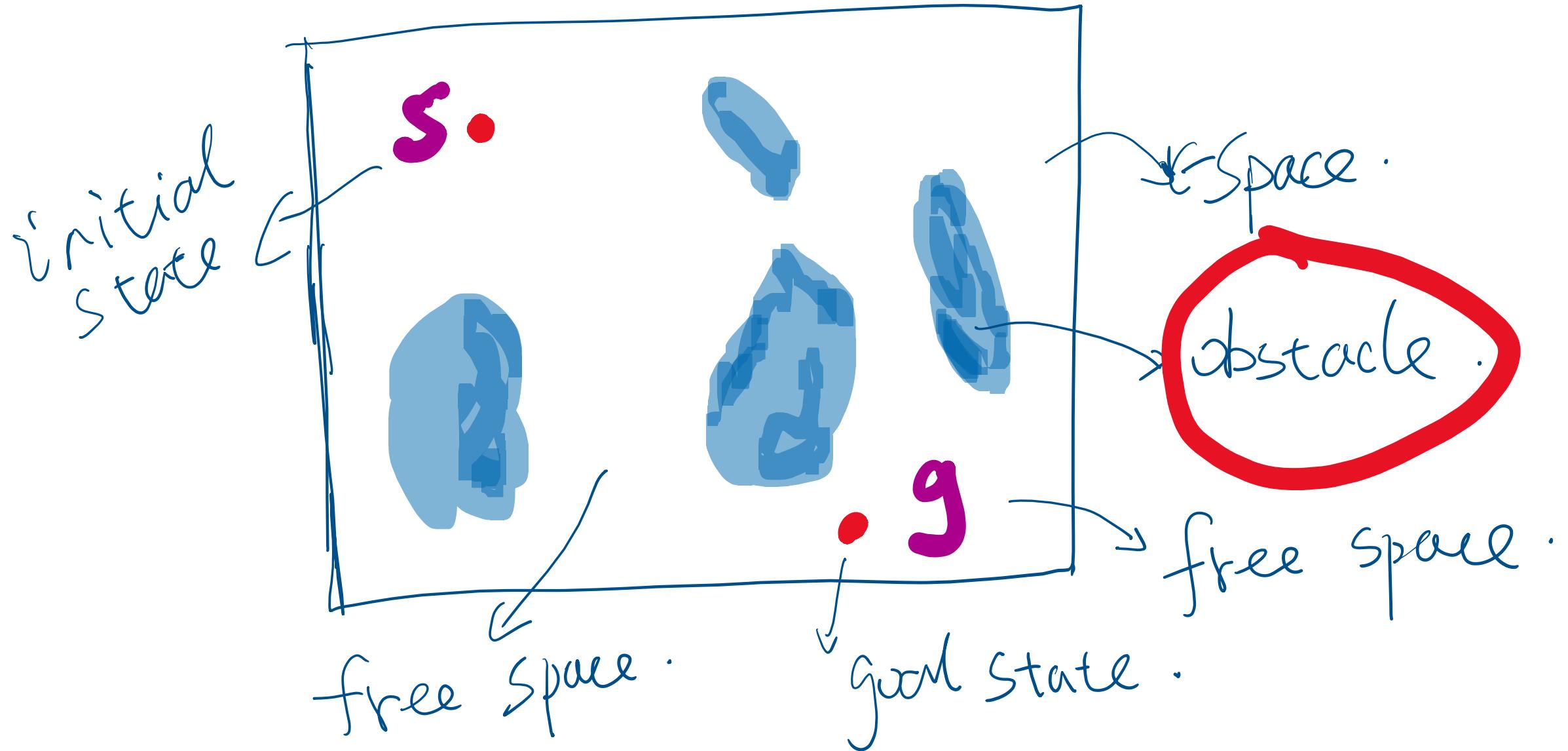


# Today's Agenda

- Recap of sampling-based approach (~10)
- Recap of optimization-based approach (~20)
- Drawback of sampling and optimization (~5)
- Recap of perception-action loop (~2)
- Learning-based motion planning (~5)
- Imitation learning (~20)
- Reinforcement learning (~10)

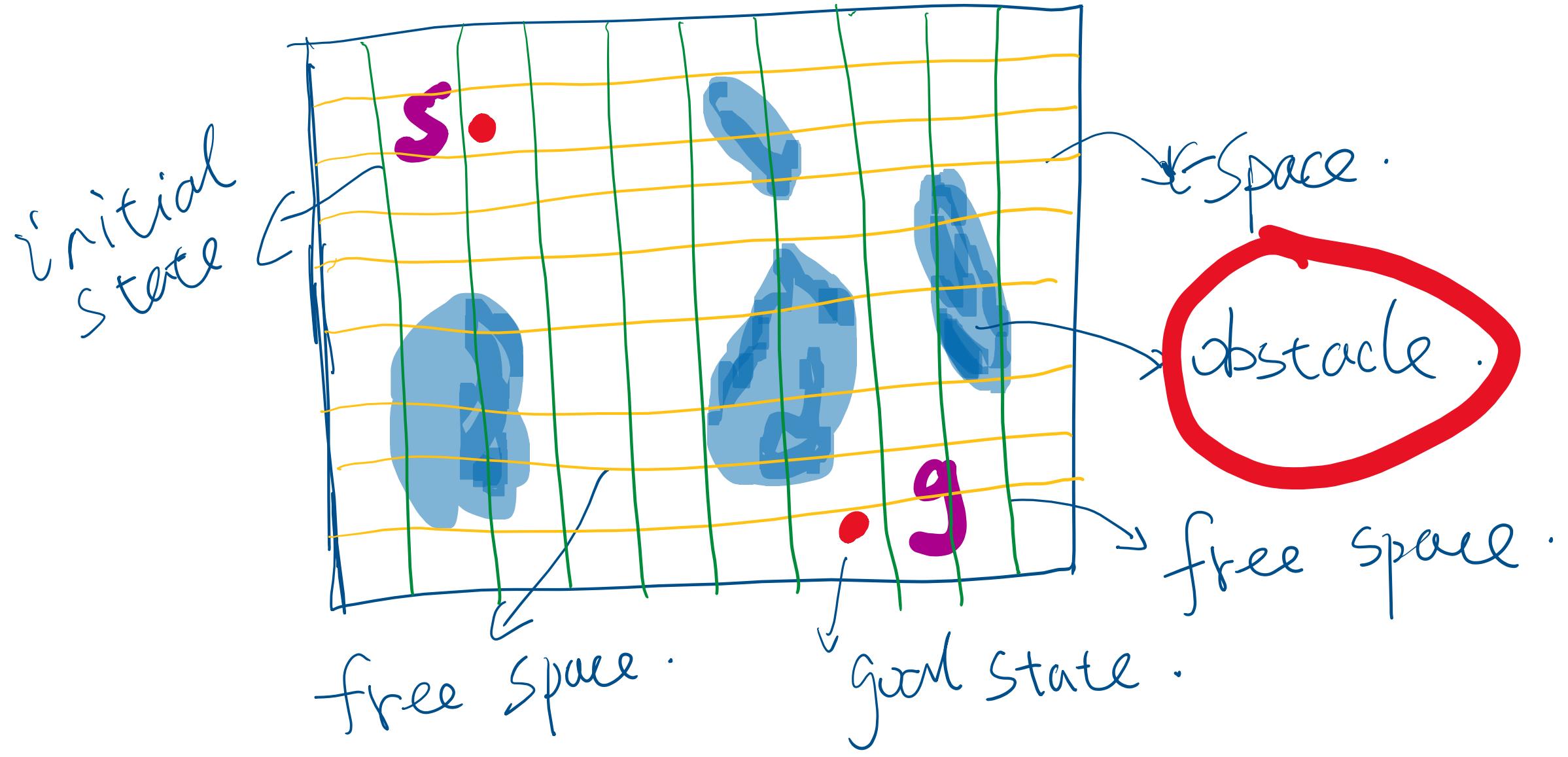


# Motion Planning in 2D





# Motion Planning in Grid World



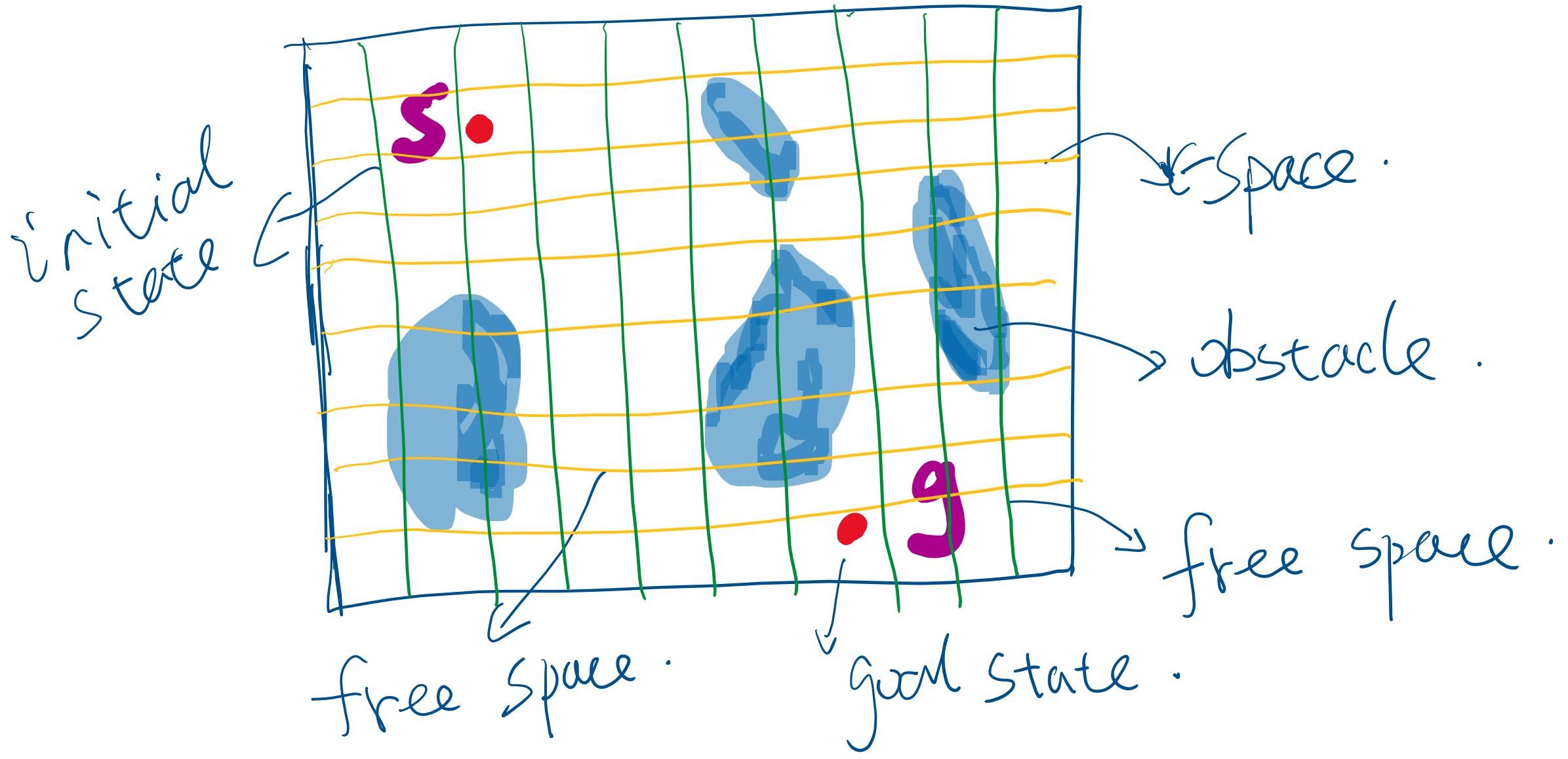


# Recap of sampling-based approach

- Completely describing and optimally exploring is too hard in high dimension space
- It is not necessary
- Limit ourselves to finding a “good” sampling

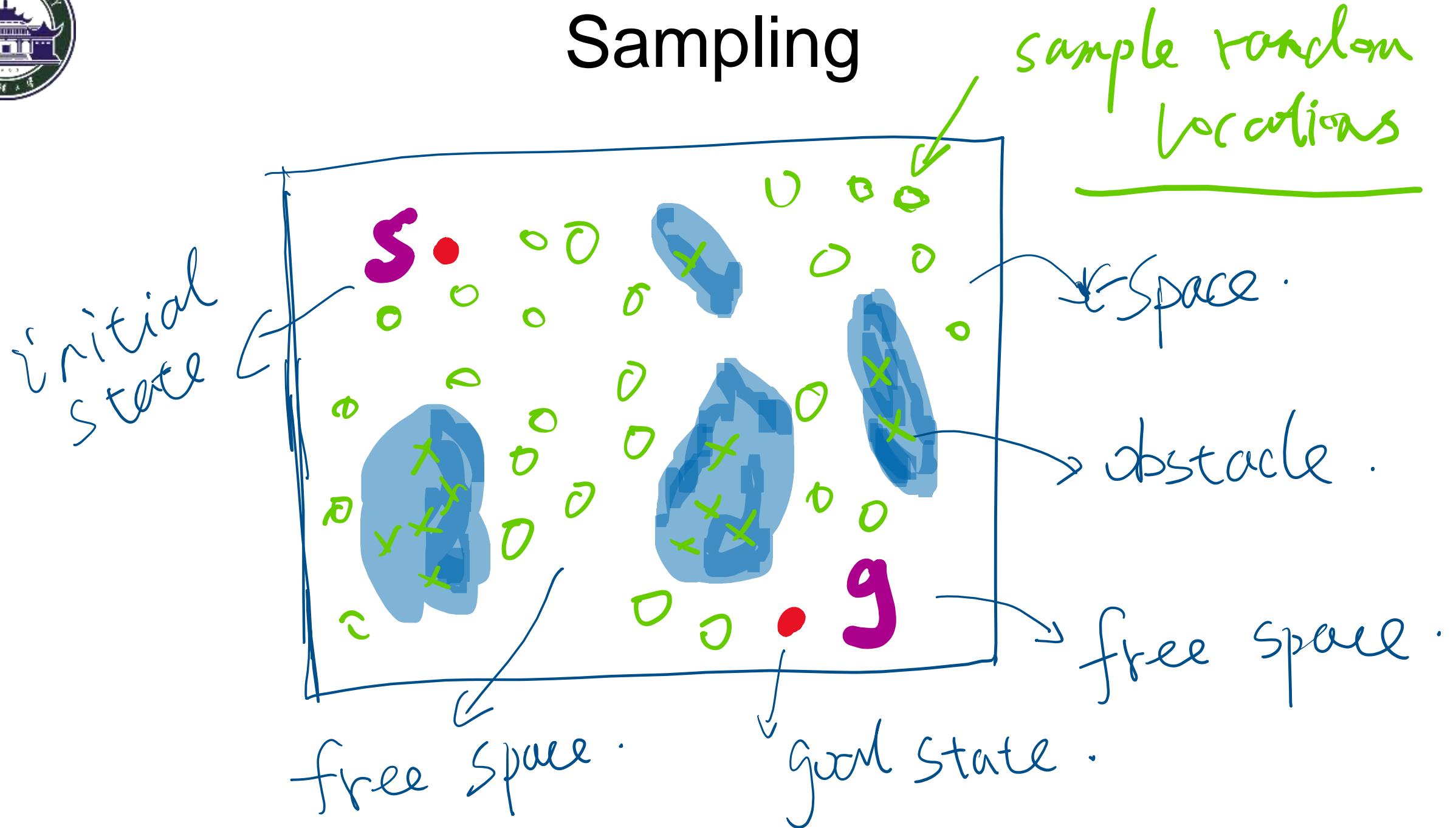


# Sampling



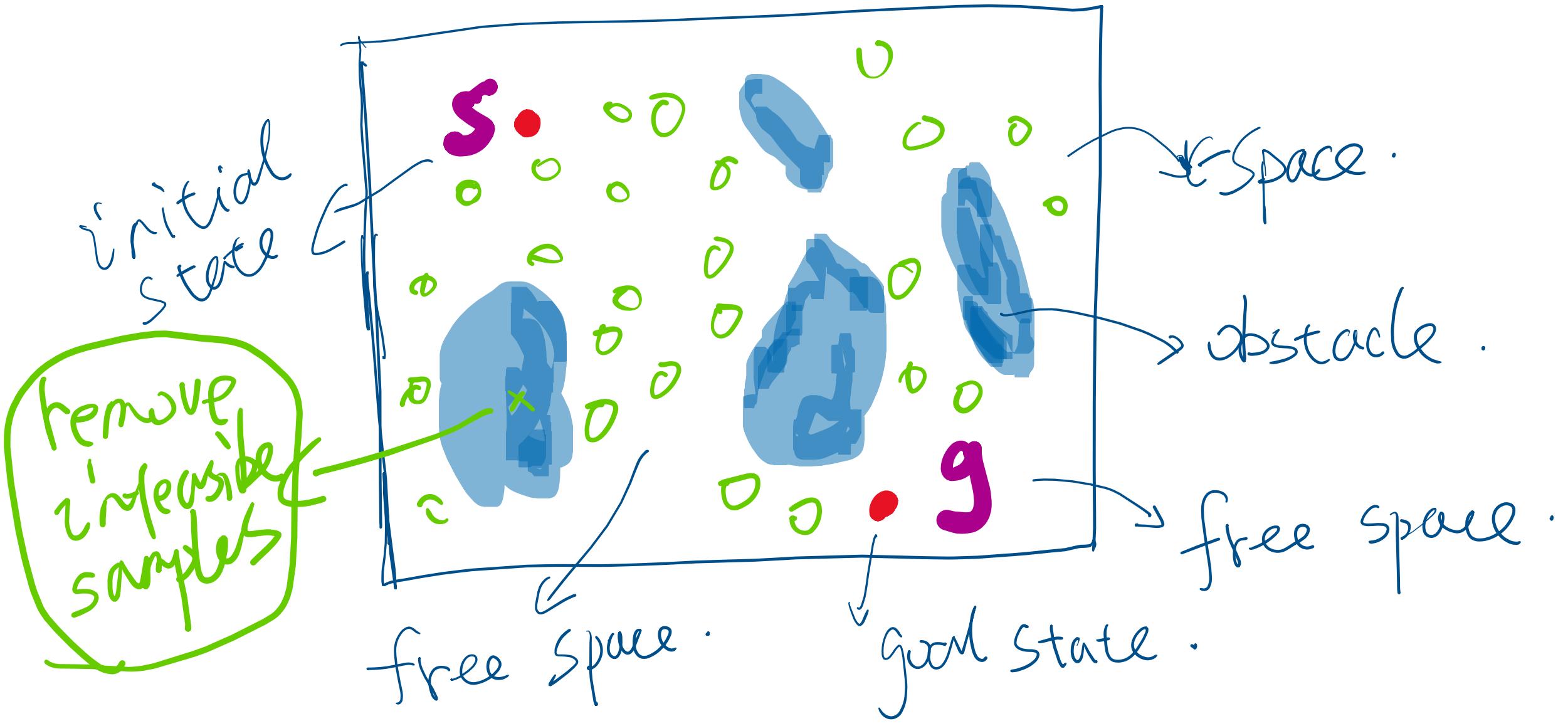


# Sampling



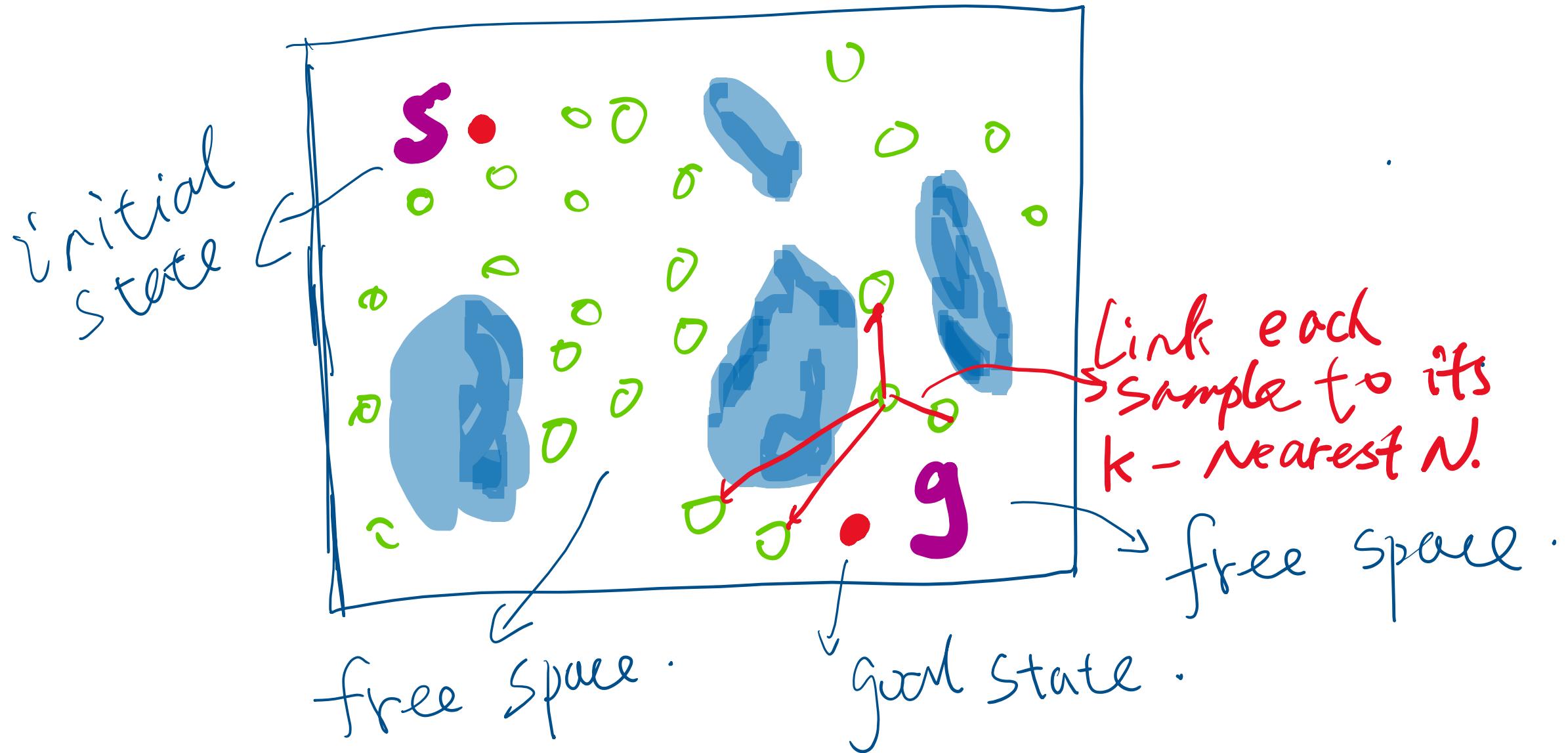


# Sampling



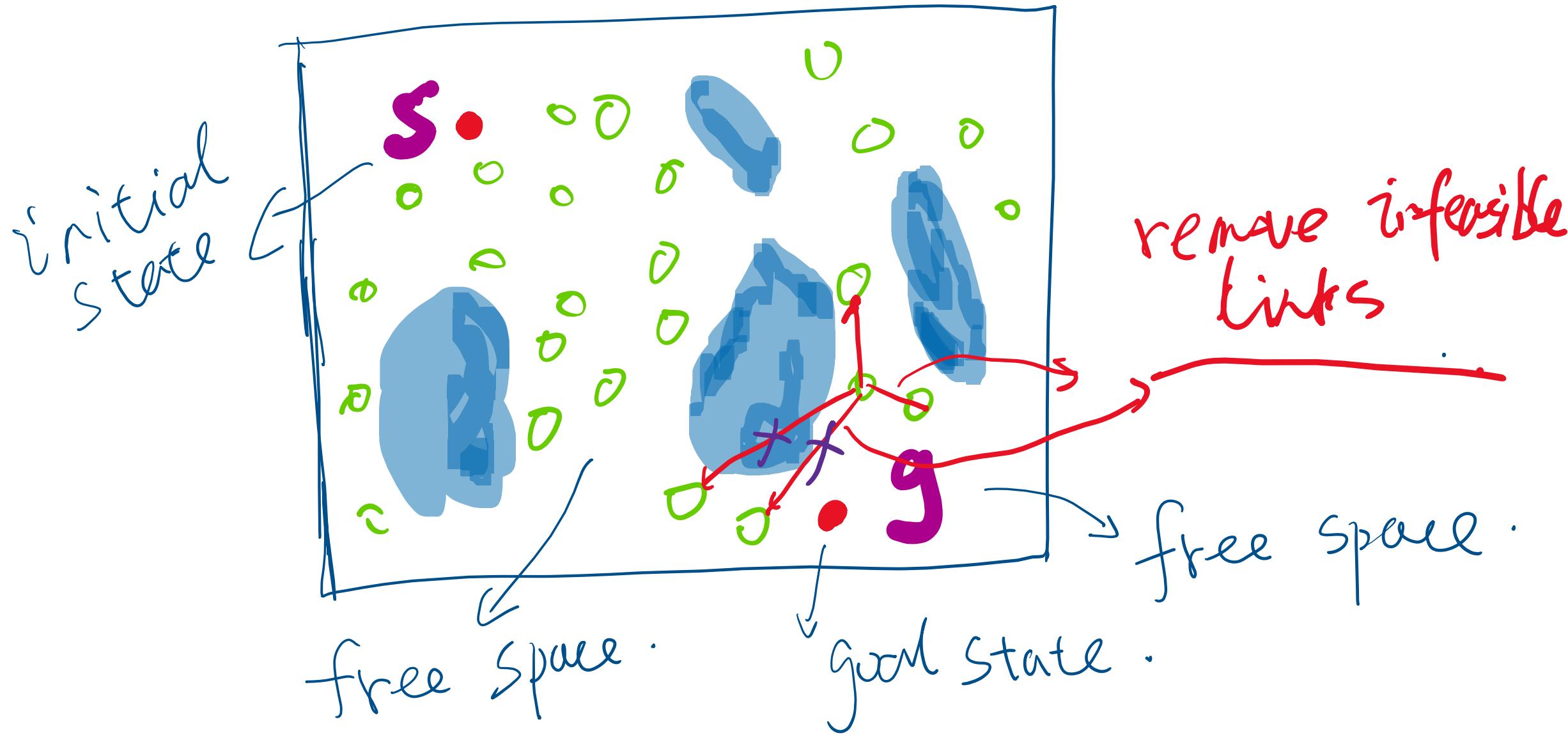


# Sampling



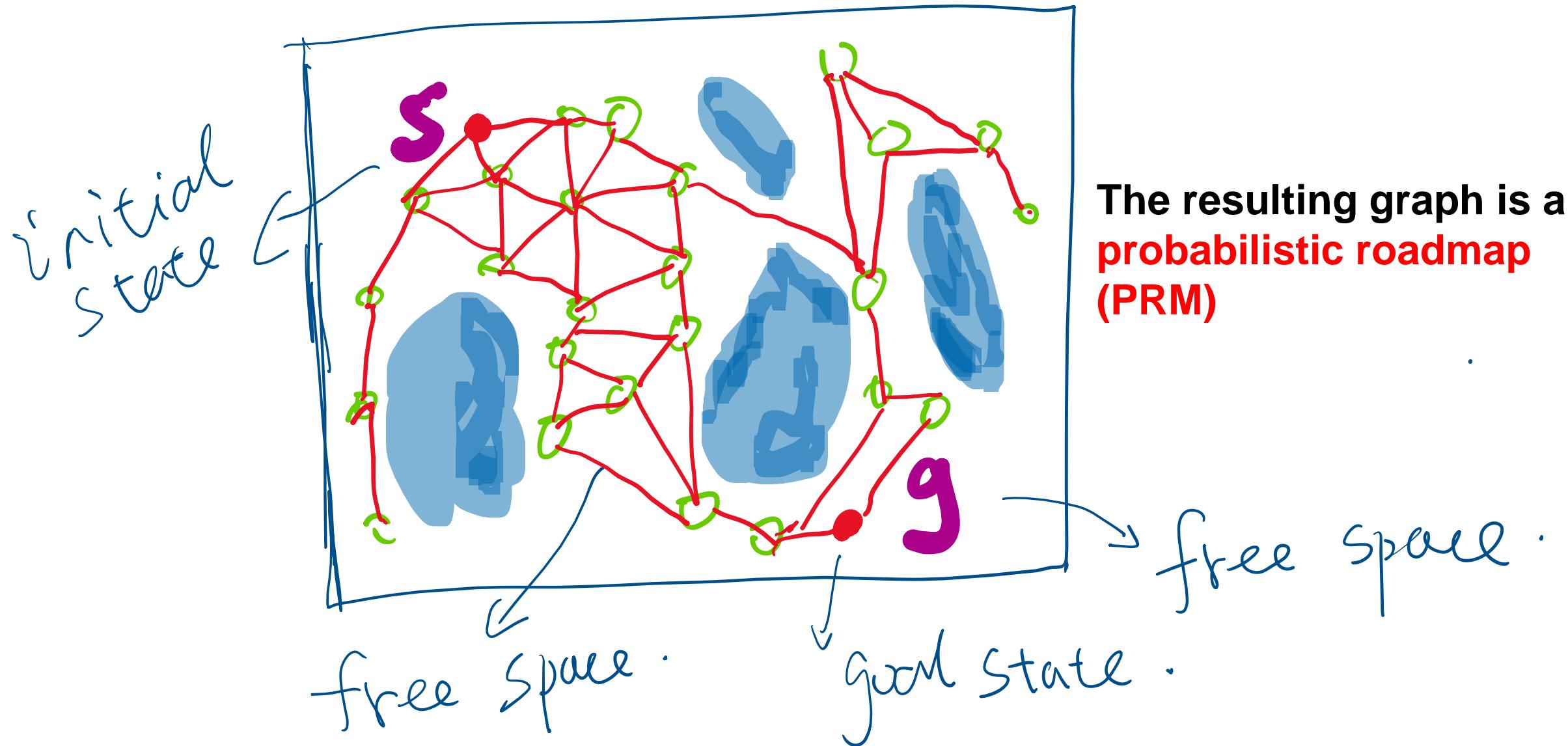


# Sampling



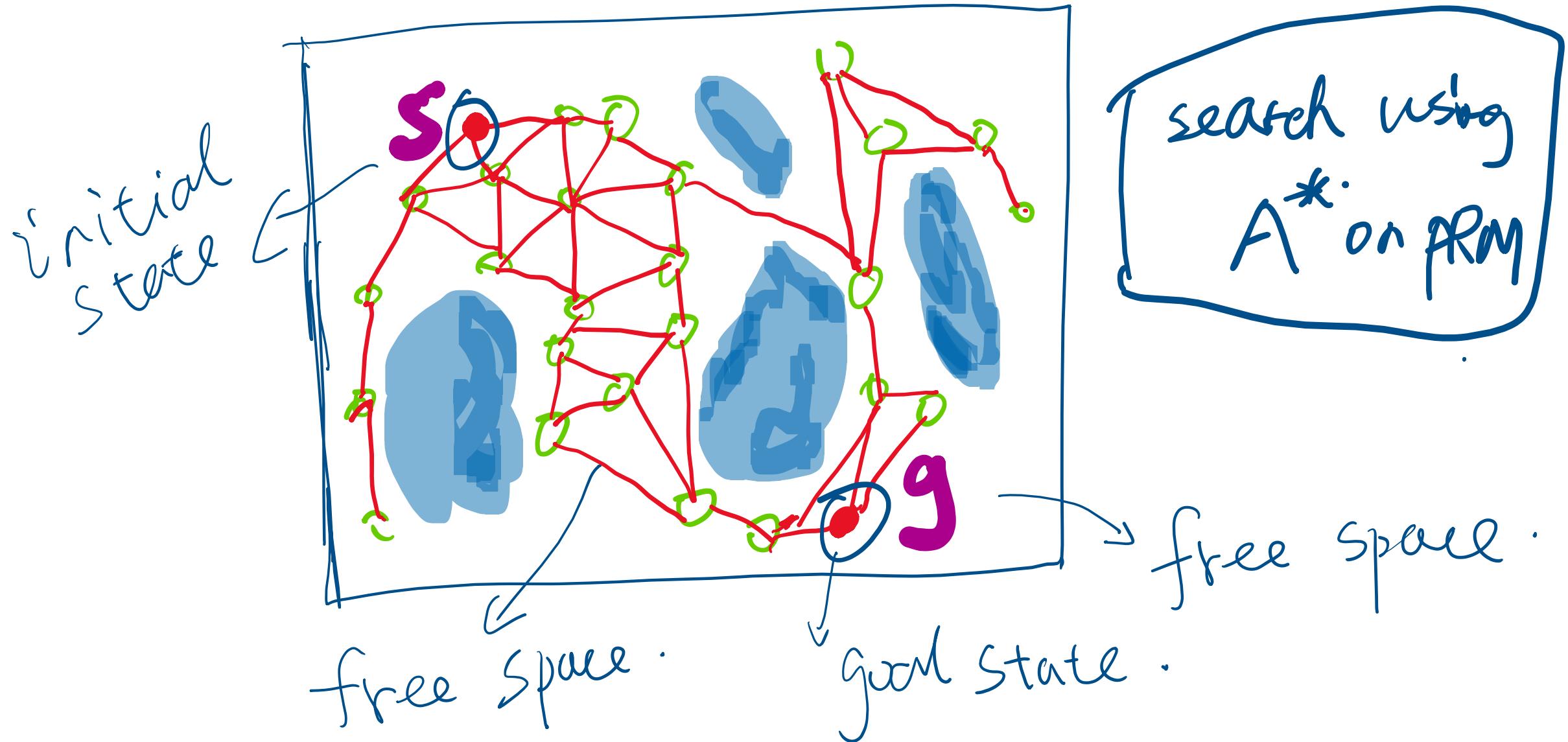


# PRM (probabilistic roadmap)



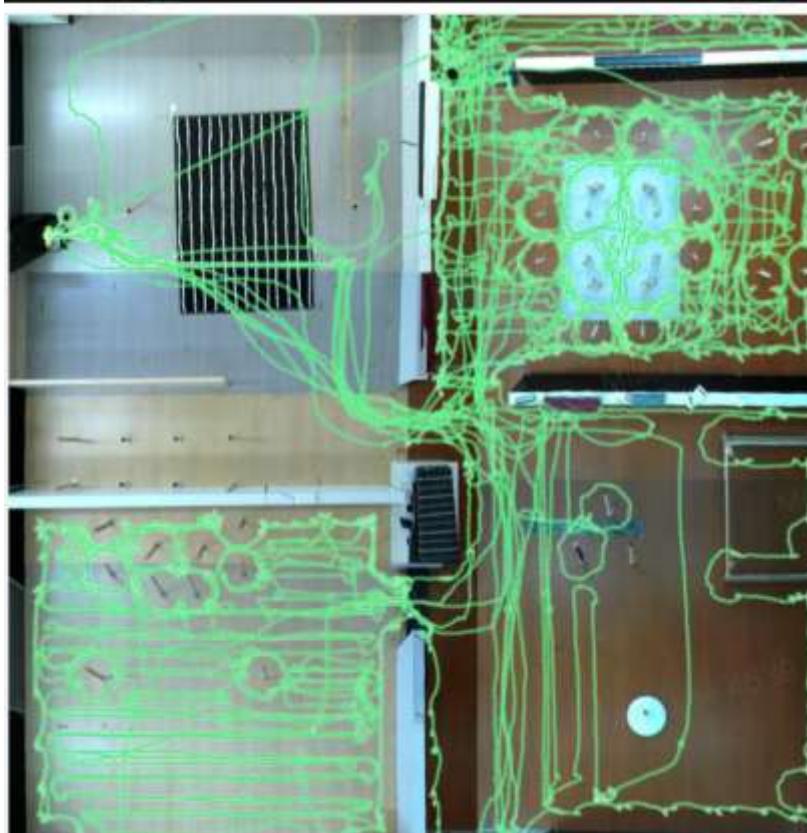


# PRM (probabilistic roadmap)





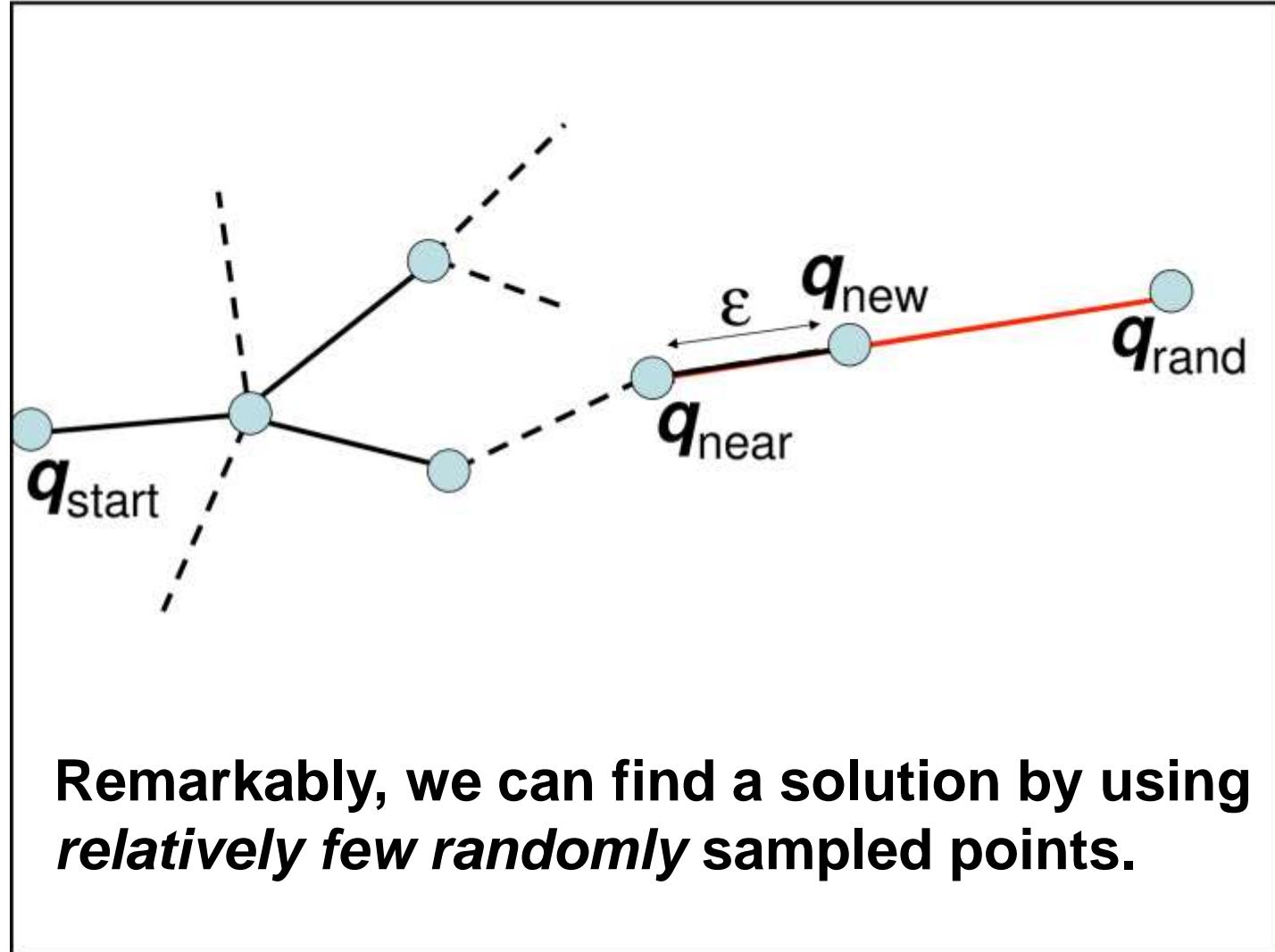
# Example





# RRT

Rapidly Exploring Random Trees



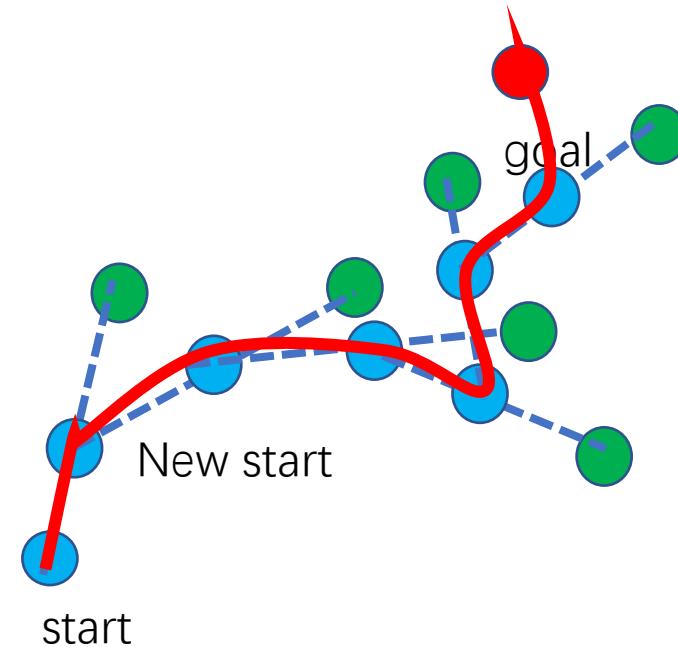


# RRT

## RRT Algorithm ( $x_{\text{start}}, x_{\text{goal}}$ , step, n)

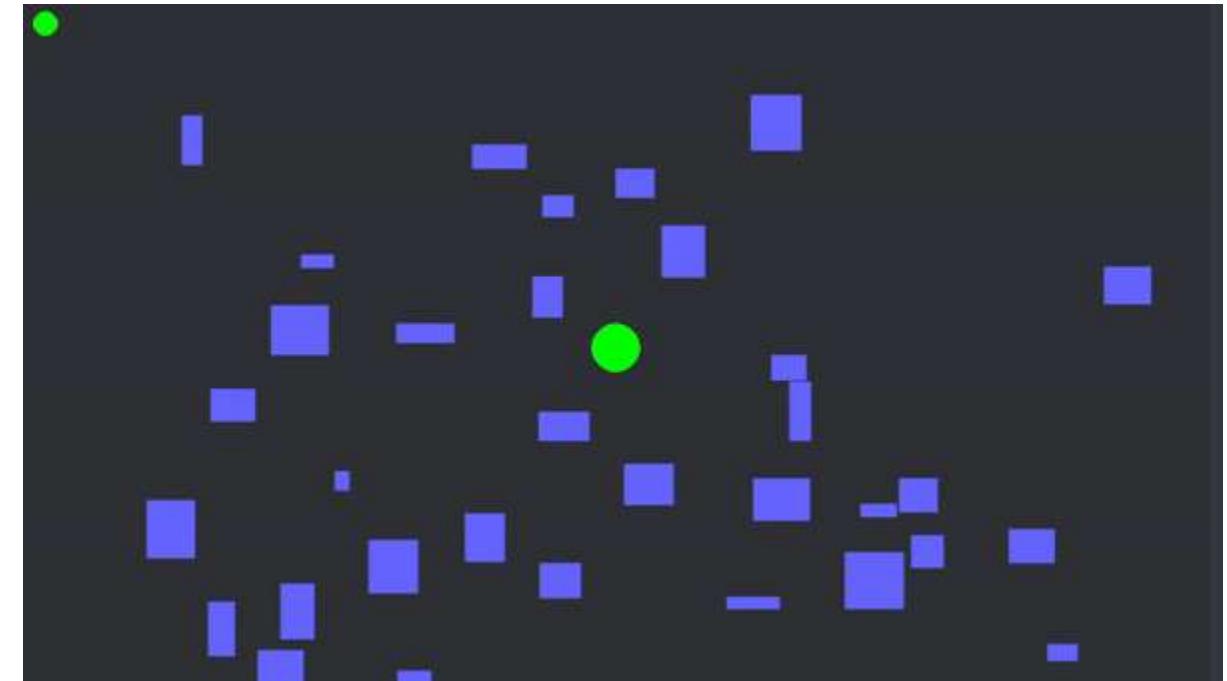
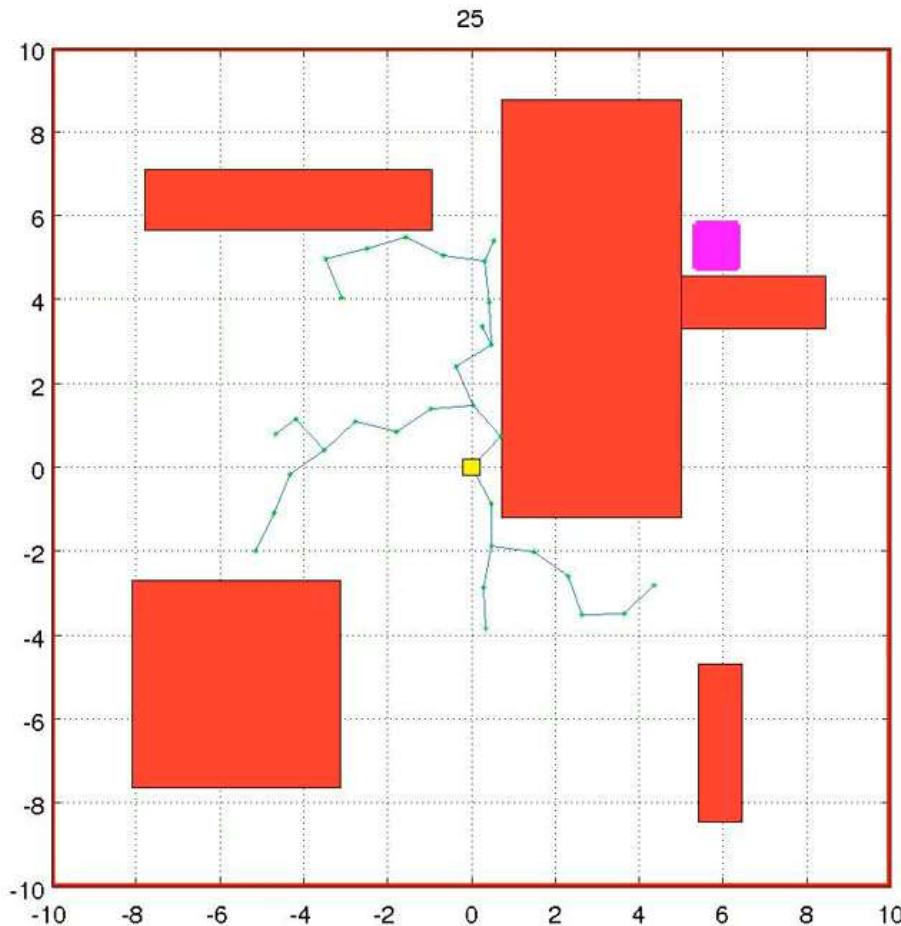
```
1   G.initialize( $x_{\text{start}}$ )
2   for  $i = 1$  to n do
3        $x_{\text{rand}} = \text{Sample}()$ 
4        $x_{\text{near}} = \text{near}(x_{\text{rand}}, G)$ 
5        $x_{\text{new}} = \text{steer}(x_{\text{rand}}, x_{\text{near}}, \text{step\_size})$ 
6       G.add_node( $x_{\text{new}}$ )
7       G.add_edge( $x_{\text{new}}, x_{\text{near}}$ )
8       if  $x_{\text{new}} = x_{\text{goal}}$ 
9           success()
```

- J-C. Latombe. Robot Motion Planning. Kluwer. 1991.
- S. Lavalle. Planning Algorithms. 2006.  
<http://msl.cs.uiuc.edu/planning/>
- H. Choset et al., Principles of Robot Motion: Theory, Algorithms, and Implementations. 2006.



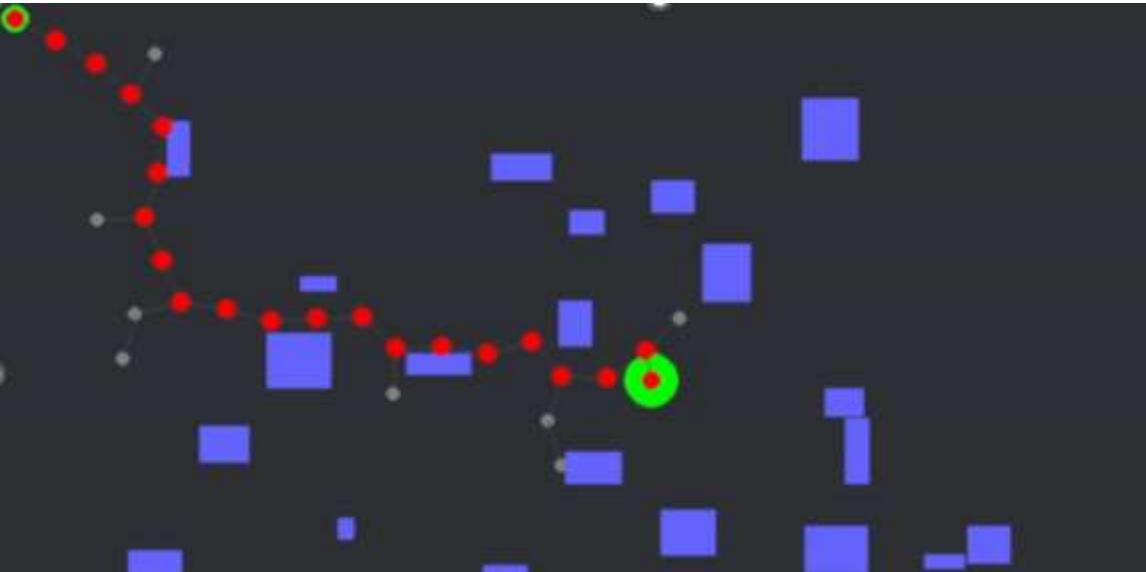


# RRT





# RRT revisit

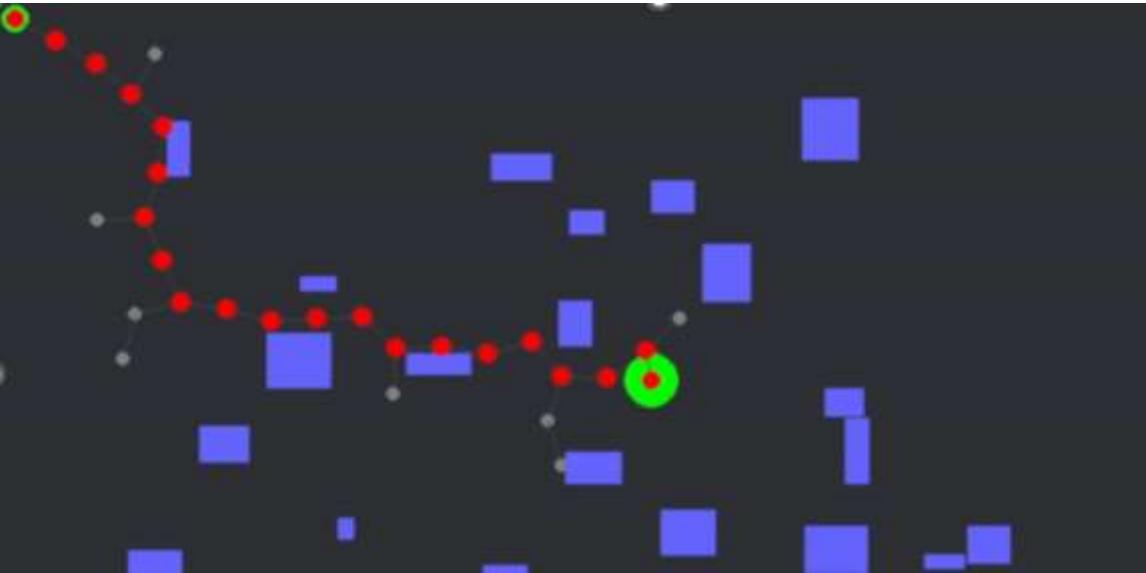


- Few control params of the solution
- Near to collisions
- Ignore trivial solution
- Path quality can be bad
- Quite different with different seeds
- Additional steps for collision checking

**What is the problem with this approach?**



# RRT revisit



**RRT is not optimal**

**What is the problem with this approach?**



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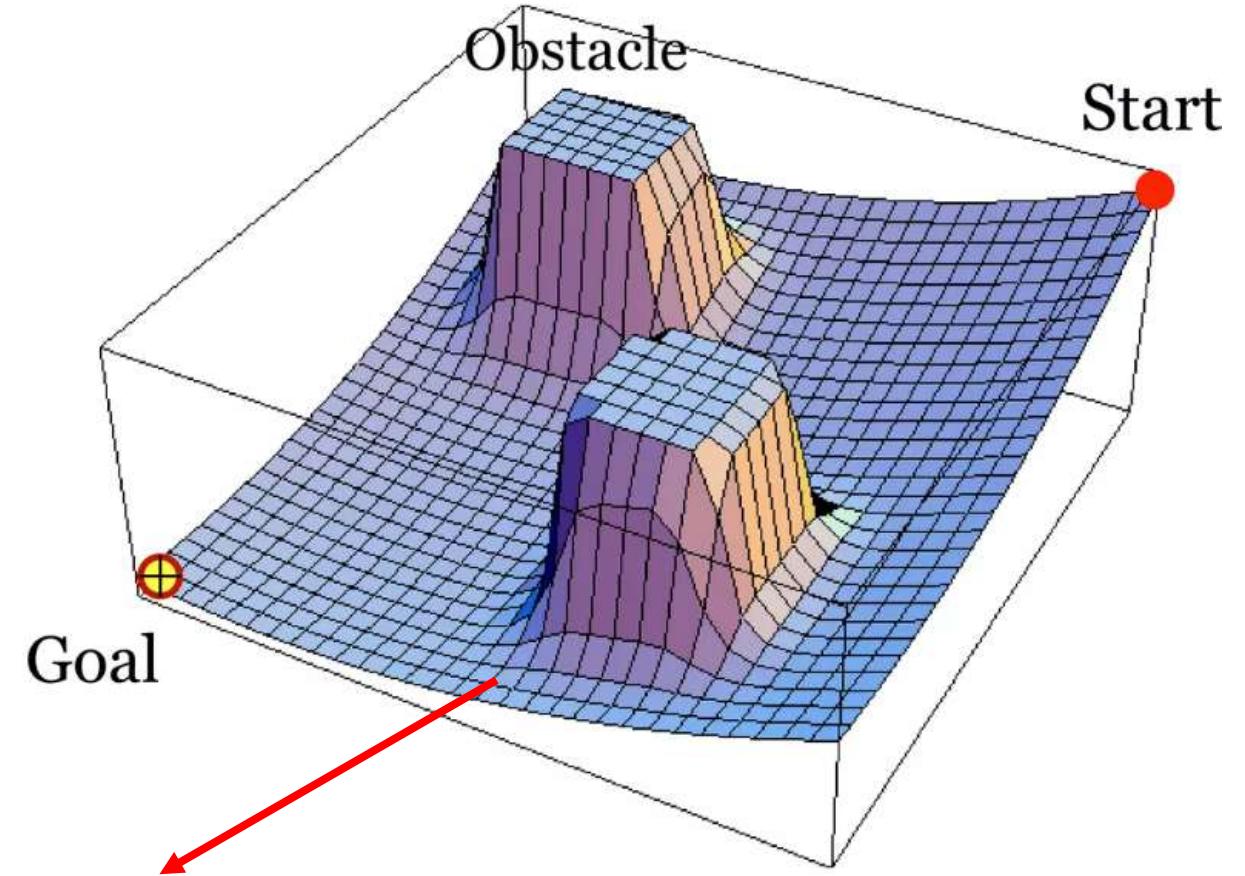


# Recap of optimization-based approach

Can we develop a motion planner  
that relies on **cost function**  
instead?



# Potential field method

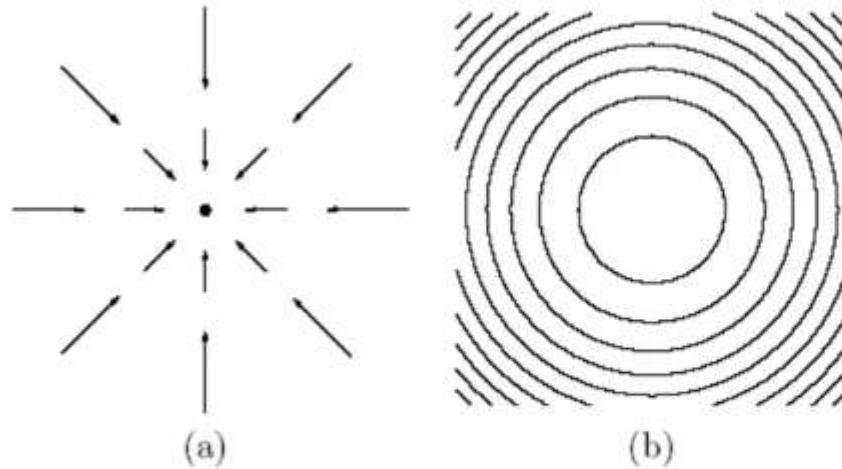


**Can we create such a cost function?**

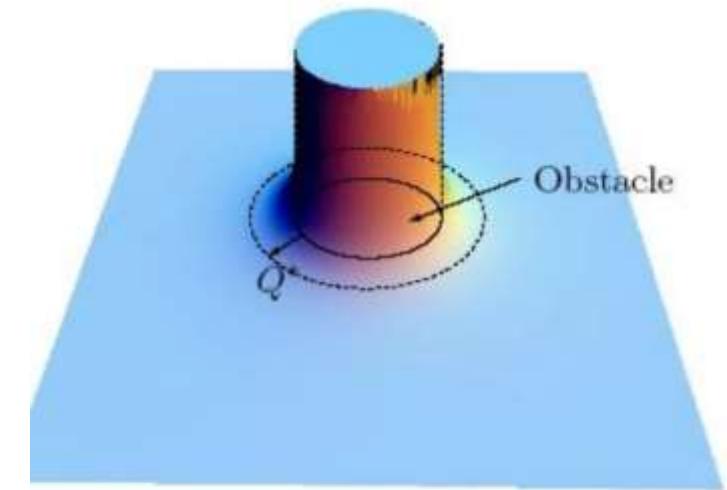


# Potential field method

**Attraction**



**Repulsion**

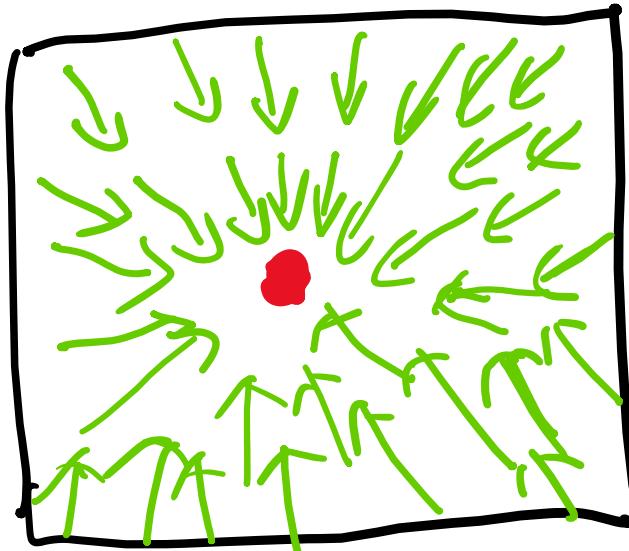


**Minimize the cost function**

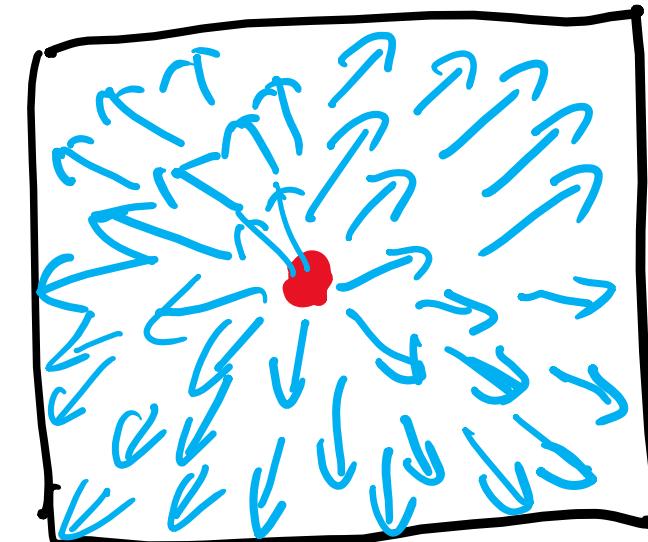


# Potential field method

Attraction



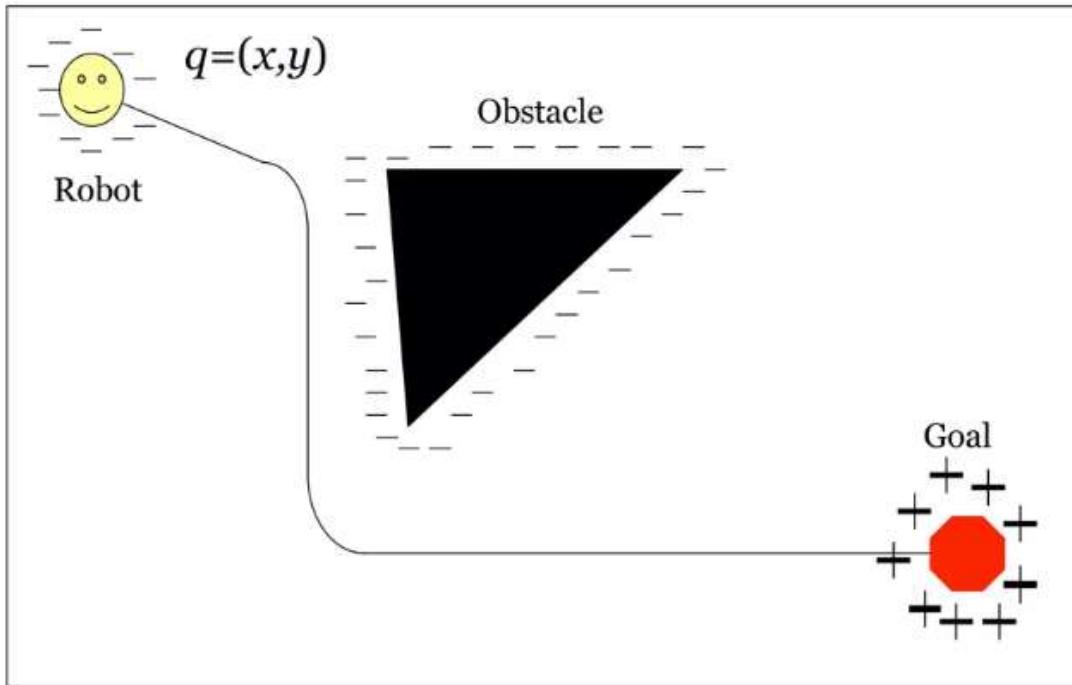
Repulsion



Gradient



# Cost function as potential



differential potential :

$$U(q)$$

artificial force -

$$F(q) = -\nabla U(q)$$

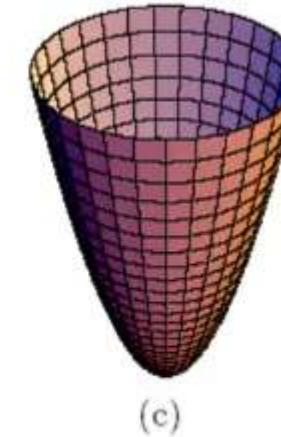
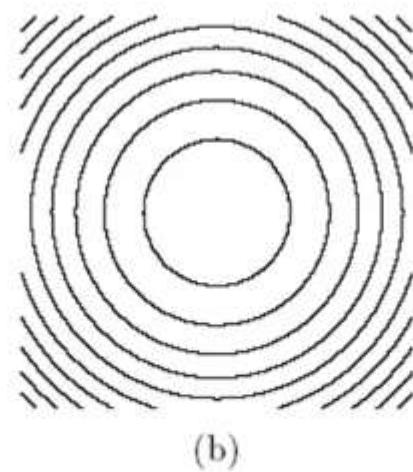
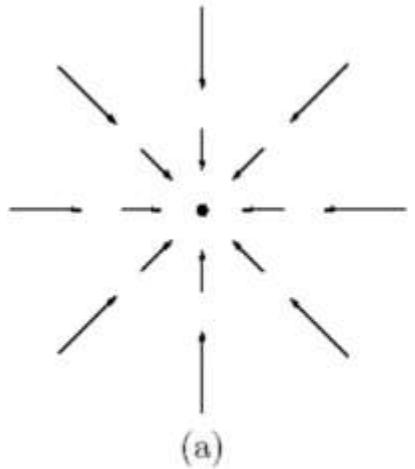
gradient

$$\nabla U(q) = \begin{bmatrix} \frac{\partial U(q)}{\partial x} \\ \frac{\partial U(q)}{\partial y} \end{bmatrix}$$



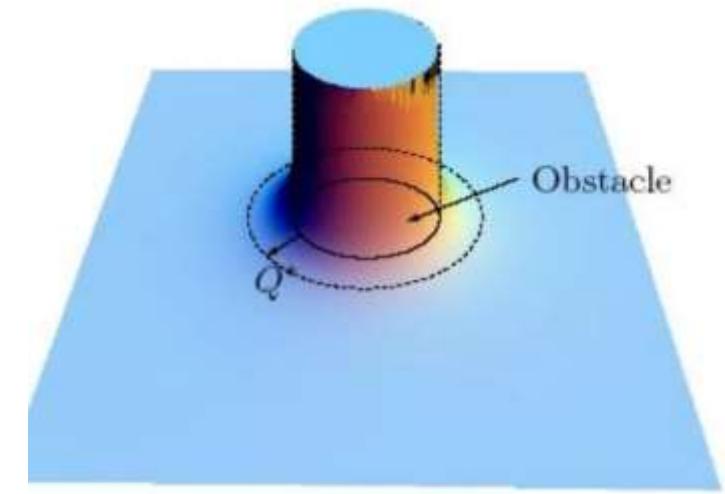
# Potential field method

Attraction



$$V_{act}(q)$$

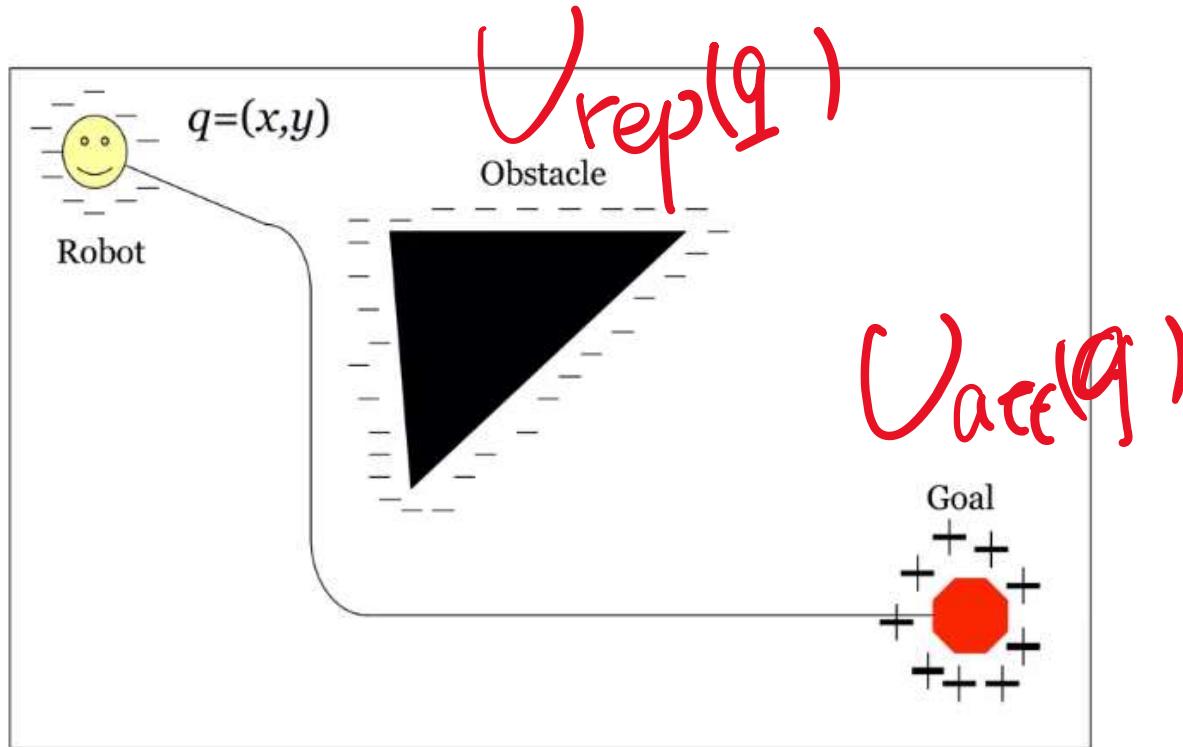
Repulsion



$$V_{rep}(q)$$



# Potential field method



$$U(q) = U_{atc}(q) + U_{rep}(q)$$

$U_{atc}(q) \rightarrow$  move to the goal

$U_{rep}(q) \rightarrow$  avoid obstacles.



# Potential field method

attractive potential.

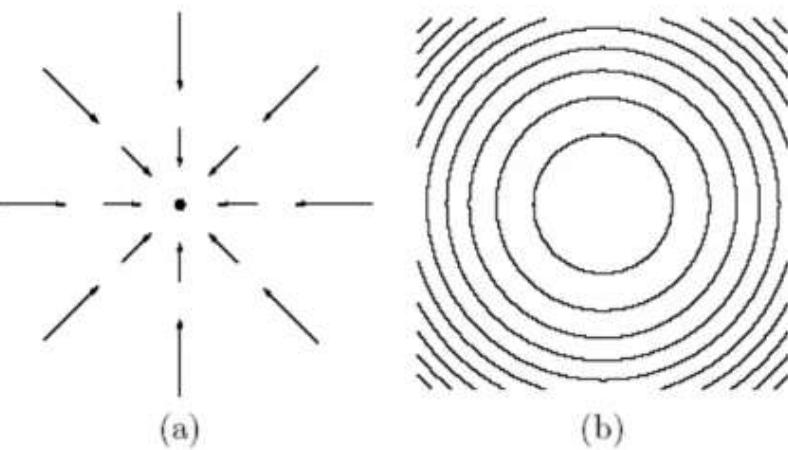
examples:

quadratic potential:

$$V_{att}(\underline{q}) = \frac{1}{2} k_{att} d_{goal}^2(\underline{q})$$

$d_{goal}$   $\downarrow$   
 $R^+$ , positive scaling parameter

$$d_{goal} = \|\underline{q} - \underline{q}_{goal}\|$$





# Potential field method

attractive

potential.



differentiable

$$U_{\text{act}}(q) = \frac{1}{2} k_{\text{act}} d_{\text{goal}}^2(q)$$

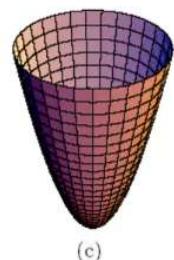
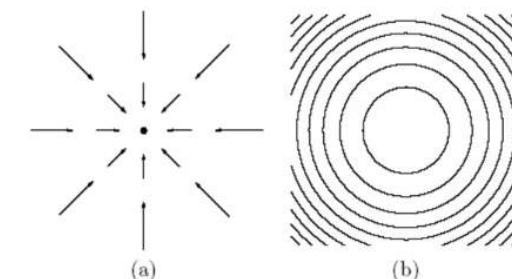
force

$$\cancel{\star} F_{\text{act}}(q) = -\nabla U_{\text{act}}(q)$$

$$= -k_{\text{act}} d_{\text{goal}} \nabla d_{\text{goal}}$$

$$= -K_{\text{act}}(q - q_{\text{goal}})$$

$$d_{\text{goal}} = \|q - q_{\text{goal}}\|$$



converge linear  
towards the  
goal



# Potential field method

repulsive potential.

$$U_{rep}(q) = \begin{cases} \frac{1}{2} k_{rep} \left( \frac{1}{d_{obj}(q)} - \frac{1}{Q^*} \right)^2 & d_{obj}(q) \leq Q^* \\ 0 & d_{obj}(q) > Q^* \end{cases}$$

where

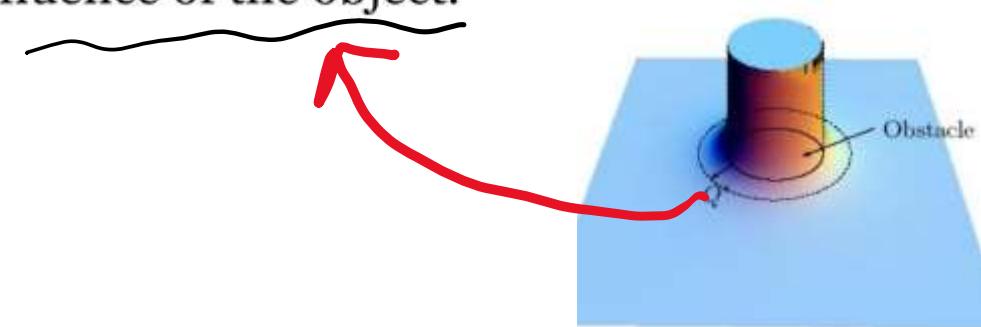
- ◊  $k_{rep}$  is again a scaling factor,
- ◊  $d_{obj}$  is the minimal distance from  $q$  to the object and
- ◊  $Q^*$  is the distance of influence of the object.

key idea :

generate a force  
away from  
~~all known~~ obstacles

① Very Strong : close

② Zero : far away.





# Potential field method

repulsive potential.

$$U_{rep}(q) = \begin{cases} \frac{1}{2} k_{rep} \left( \frac{1}{d_{obj}(q)} - \frac{1}{Q^*} \right)^2 & d_{obj}(q) \leq Q^* \\ 0 & d_{obj}(q) > Q^* \end{cases}$$

where

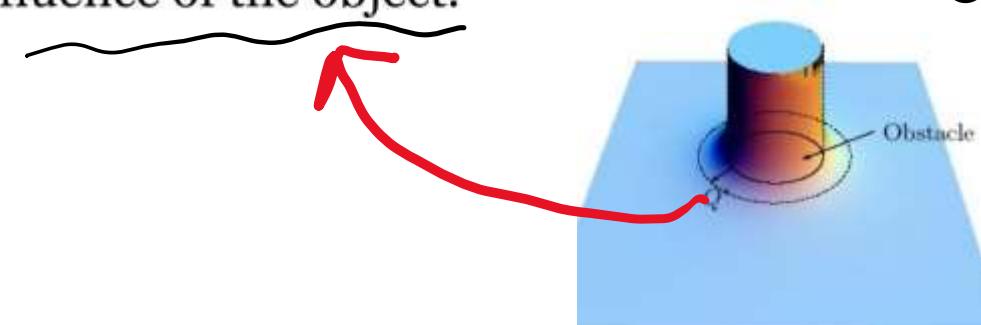
- ◊  $k_{rep}$  is again a scaling factor,
- ◊  $d_{obj}$  is the minimal distance from  $q$  to the object and
- ◊  $Q^*$  is the distance of influence of the object.

$$d_{obj}(q) \rightarrow 0, U_{rep} \rightarrow +\infty$$

?

$$d_{obj} = Q^*, U_{rep} \rightarrow 0$$

$$d_{obj} > Q^* \quad U_{rep} = 0$$





# Potential field method

repulsive force.

$$U_{rep}(q) = \begin{cases} \frac{1}{2} k_{rep} \left( \frac{1}{d_{obj}(q)} - \frac{1}{Q^*} \right)^2 & d_{obj}(q) \leq Q^* \\ 0 & d_{obj}(q) > Q^* \end{cases}$$



$$F_{rep}(q) = -\nabla U_{rep}(q) = \begin{cases} k_{rep} \left( \frac{1}{d_{obj}(q)} - \frac{1}{Q^*} \right) \cdot \frac{1}{d_{obj}^2} \cdot \nabla d_{obj} & d_{obj}(q) \leq Q^* \\ 0 & d_{obj}(q) > Q^* \end{cases}$$

where

- ◊  $k_{rep}$  is again a scaling factor,
- ◊  $d_{obj}$  is the minimal distance from  $q$  to the object and
- ◊  $Q^*$  is the distance of influence of the object.

$\nabla d_{obj} = \begin{bmatrix} \frac{\partial d_{obj}}{\partial x} \\ \frac{\partial d_{obj}}{\partial y} \end{bmatrix}$

$f_{rep}(q) \uparrow$  when  $d_{obj} \downarrow$



# Potential field method

repulsive force.

$$U_{rep}(q) = \begin{cases} \frac{1}{2} k_{rep} \left( \frac{1}{d_{obj}(q)} - \frac{1}{Q^*} \right)^2 & d_{obj}(q) \leq Q^* \\ 0 & d_{obj}(q) > Q^* \end{cases}$$



$$F_{rep}(q) = -\nabla U_{rep}(q) = \begin{cases} k_{rep} \left( \frac{1}{d_{obj}(q)} - \frac{1}{Q^*} \right) \cdot \frac{1}{d_{obj}^2} \cdot \nabla d_{obj} & d_{obj}(q) \leq Q^* \\ 0 & d_{obj}(q) > Q^* \end{cases}$$

where

- ◊  $k_{rep}$  is again a scaling factor,
- ◊  $d_{obj}$  is the minimal distance from  $q$  to the object and
- ◊  $Q^*$  is the distance of influence of the object.



Flow to compute  $d_{obj}$  }.

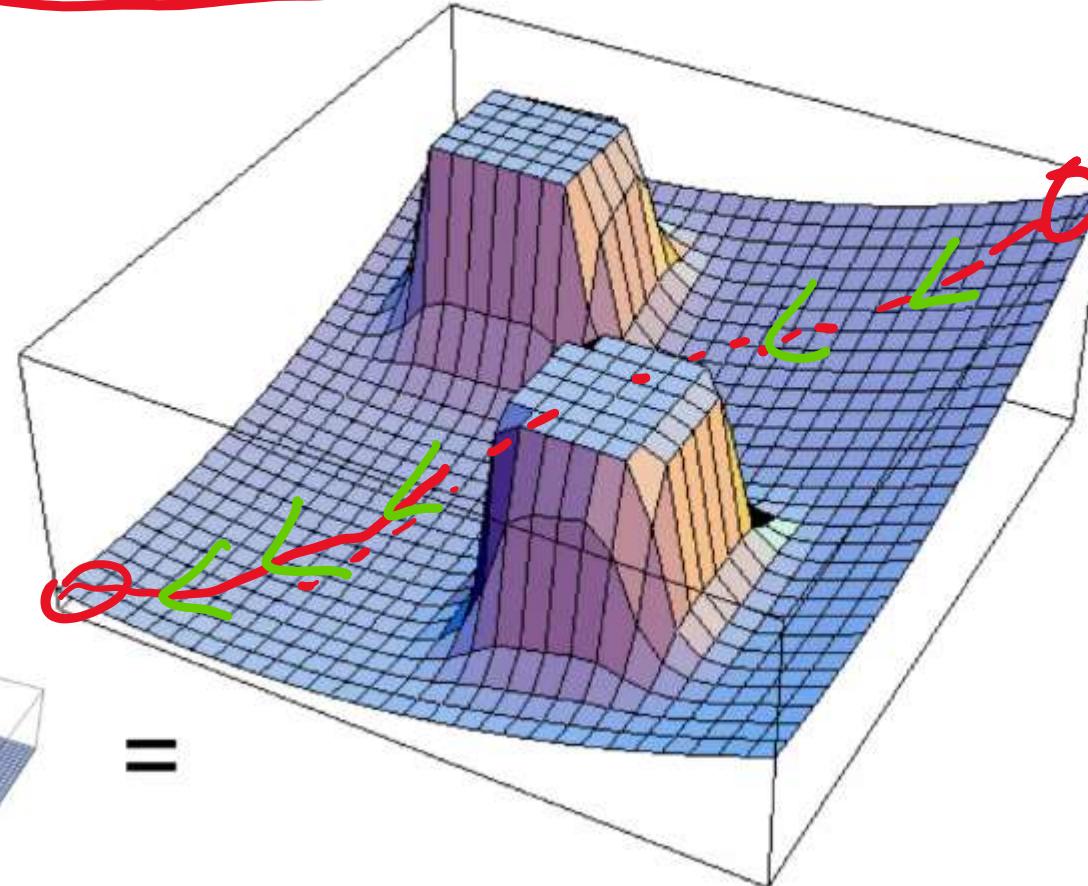
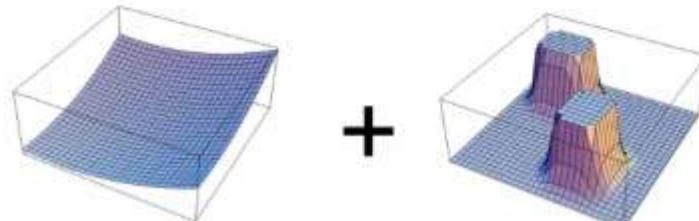
geometry



# Potential field method

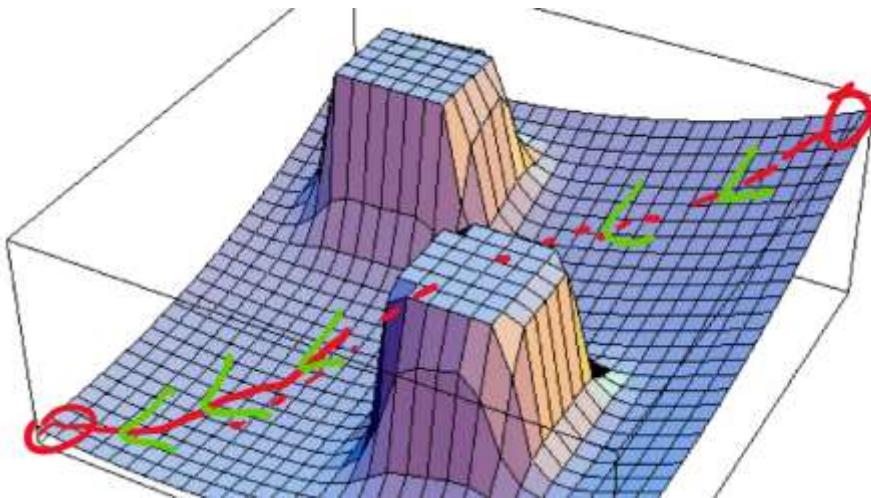
$$F(q) = F_{att}(q) + F_{rep}(q) = -\nabla U(q)$$

A first-order optimization algorithm such as **gradient descent** (also known as **steepest descent**) can be used to minimize this function by taking steps proportional to the negative of the gradient.





# Potential field method



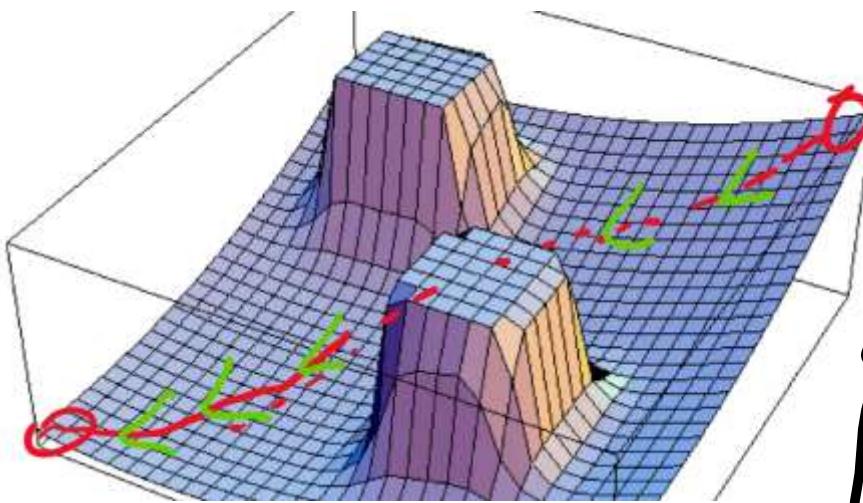
problems:

- Local minima
- Hand crafted potential function
- Hard to compute distance
- Minimal distance may not be continuous
- No passage between closely spaces obstacles
- Oscillation

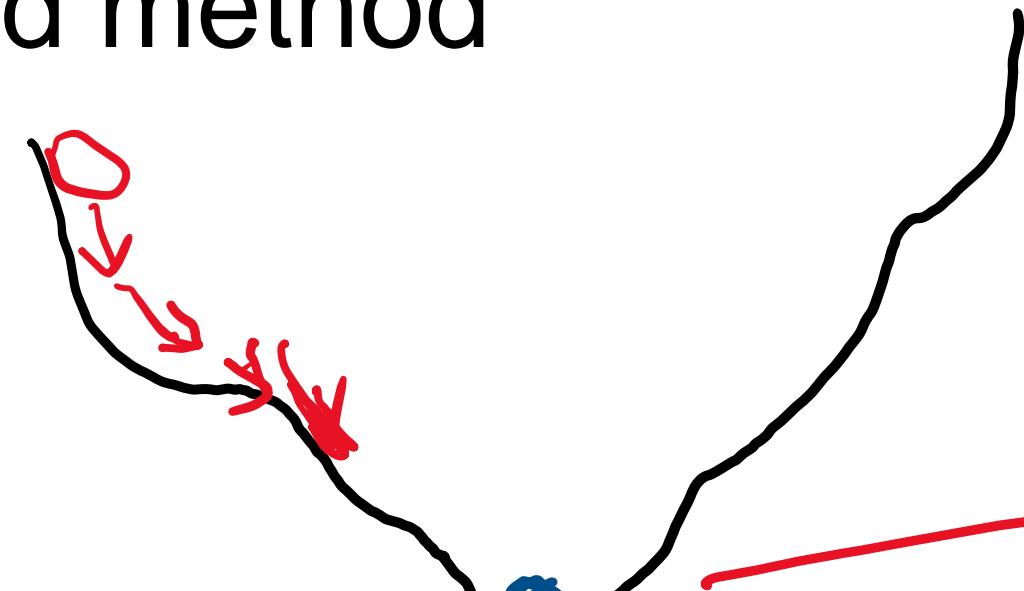


# Potential field method

Reactive control:



open question:

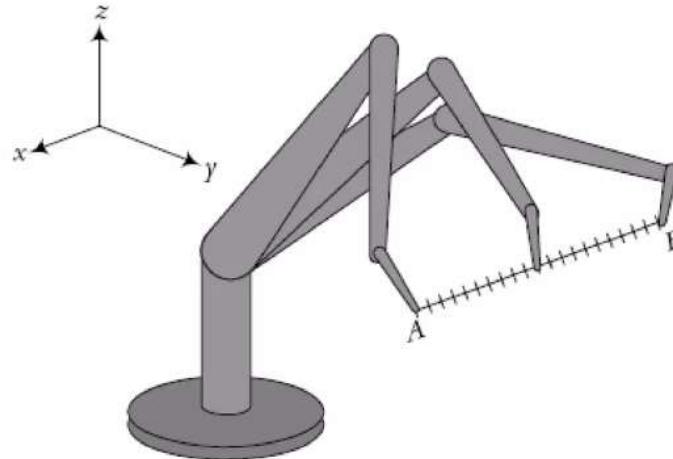


Can we design a "potential function" that can globally converge to a desired point?

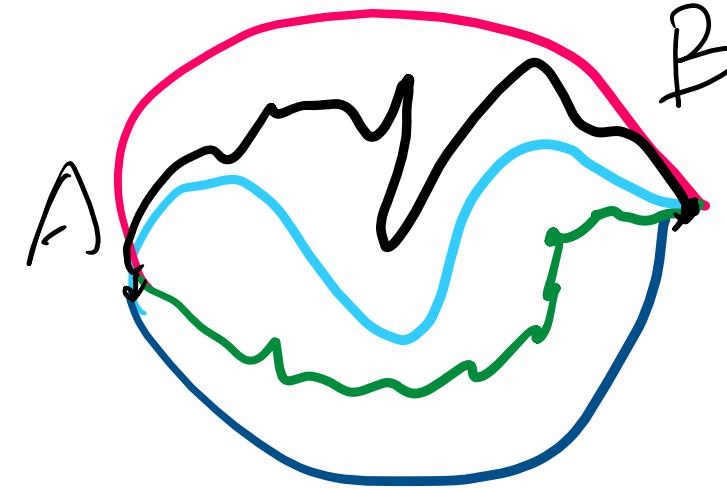
"potential function"



# Trajectory planning (Cartesian space)



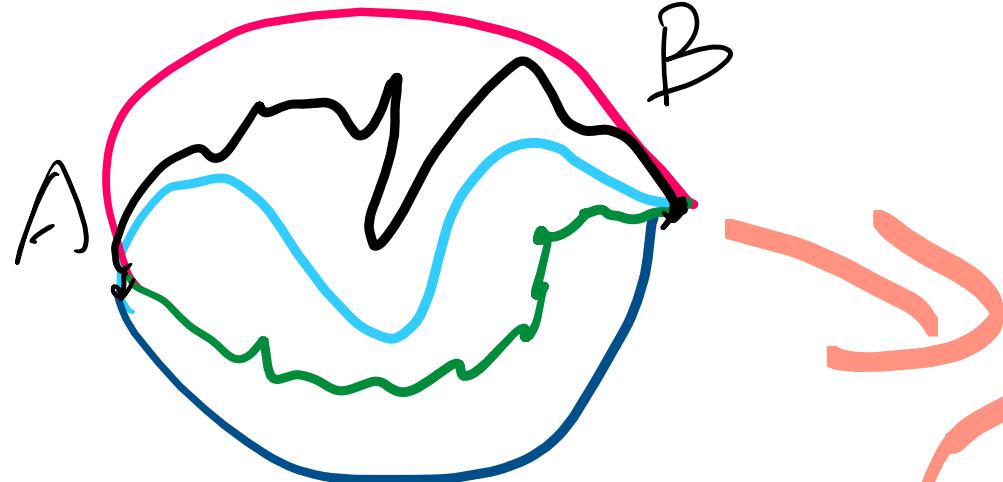
Sequential motions of a robot to follow a straight line



- **Cartesian space trajectories are very difficult to visualize**
- **Computationally expensive:** IK at each intermediate point



# Trajectory planning (Cartesian space)



polynomial

any other form of  
trajectory?



**POLYNOMIAL**

Terms

$$f(x) = 3x^3 - 4x^2 + 7x + 18$$

Variable & their Exponent

Constant Term

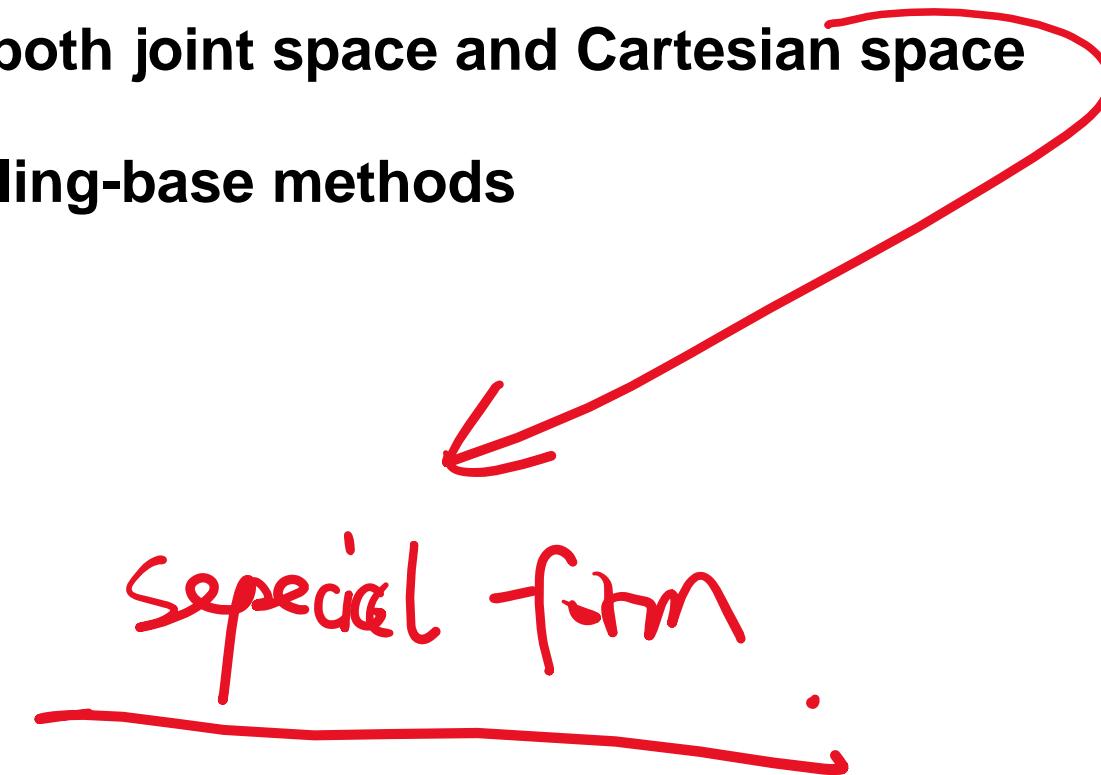
Leading Coefficient

Coefficients



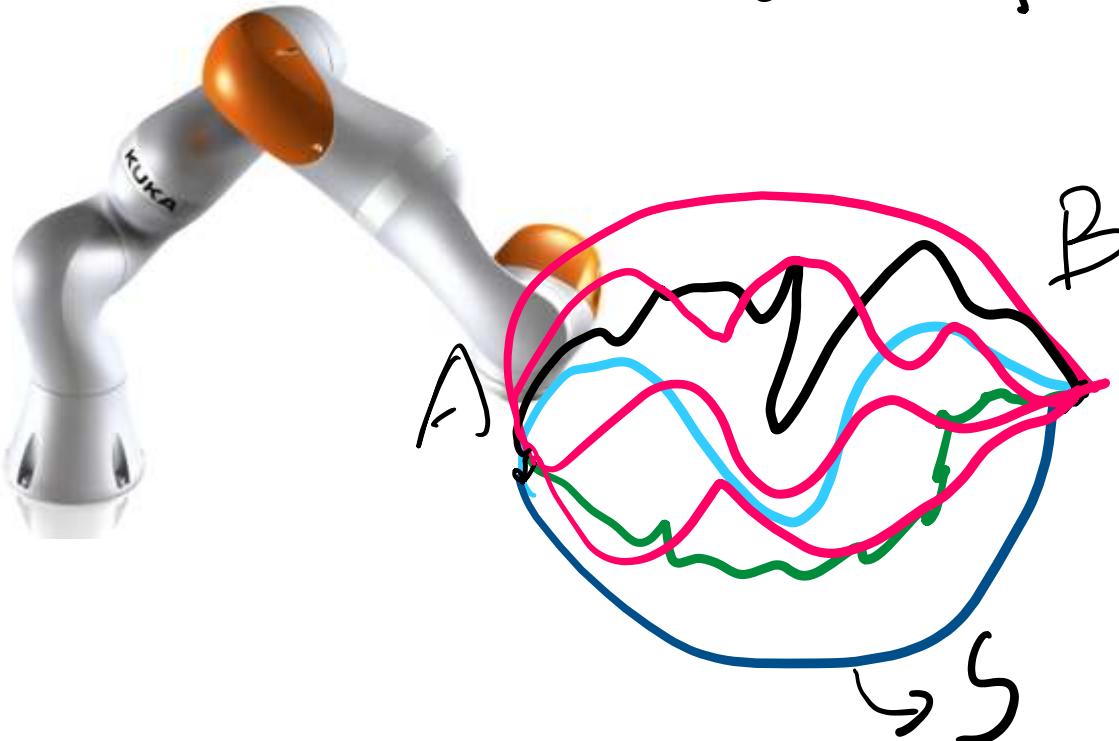
# Trajectory planning

- The key idea of trajectory planning is to use some form of trj representation to choose the proper trj profile (polynomial...)
- This process can be applied in both joint space and **Cartesian space**
- Have more flexibility than sampling-base methods





# Trajectory optimization



Cost function:  $V: S \rightarrow R^+$

- path length
- efficiency
- obstacle avoidance
- uncertainty reduction
- predictability
- legibility/ intent expression
- human comfort
- naturalness

difficult to represent.



# Trajectory optimization

Cost function:  $V: S \rightarrow \mathbb{R}^+$

$t_{kj}$  optimization:

$$S^* = \arg \min_{S \in E} U(S)$$

St. 1  $S(0) = q_s$

$$S(T) = \underline{g}_g$$

## other constraints

- path length
  - efficiency
  - obstacle avoidance
  - uncertainty reduction
  - predictability
  - legibility/ intent expression
  - human comfort
  - naturalness

difficult to represent.

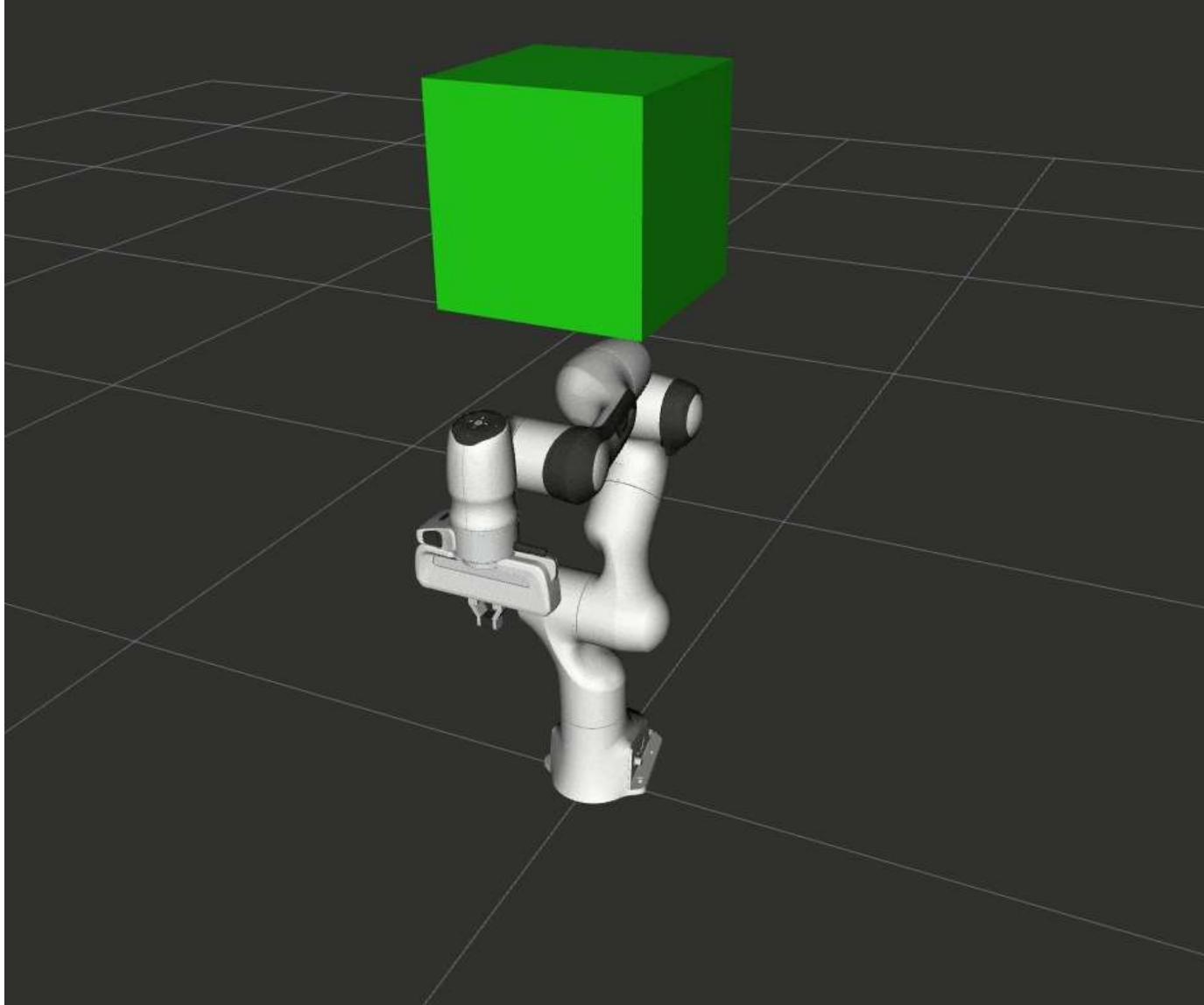


# Trajectory optimization

- Optimization-based motion planning approaches, such as Nonlinear Programming (NLP) and Mixed-Integer Programming (MIP), solve optimization problems, and find solutions using gradient descent while satisfying constraints.
- For instance, CHOMP optimizes a cost functional using covariant gradient descent while TrajOpt solves a sequential convex optimization and performs convex collision checking.
- Various tasks including navigation, grasping, manipulation, collision-avoidance, running, cooking, and flying under various conditions.
- Local optimal (a general problem for nonlinear optimization)



# Trajectory optimization





# Trajectory Optimization

$$\min_{\theta_{1:T}} \sum_t \|\theta_{t+1} - \theta_t\|^2 + \text{other costs}$$

subject to  $\theta_0$  = start state,  $\theta_T$  in goal set

joint limits



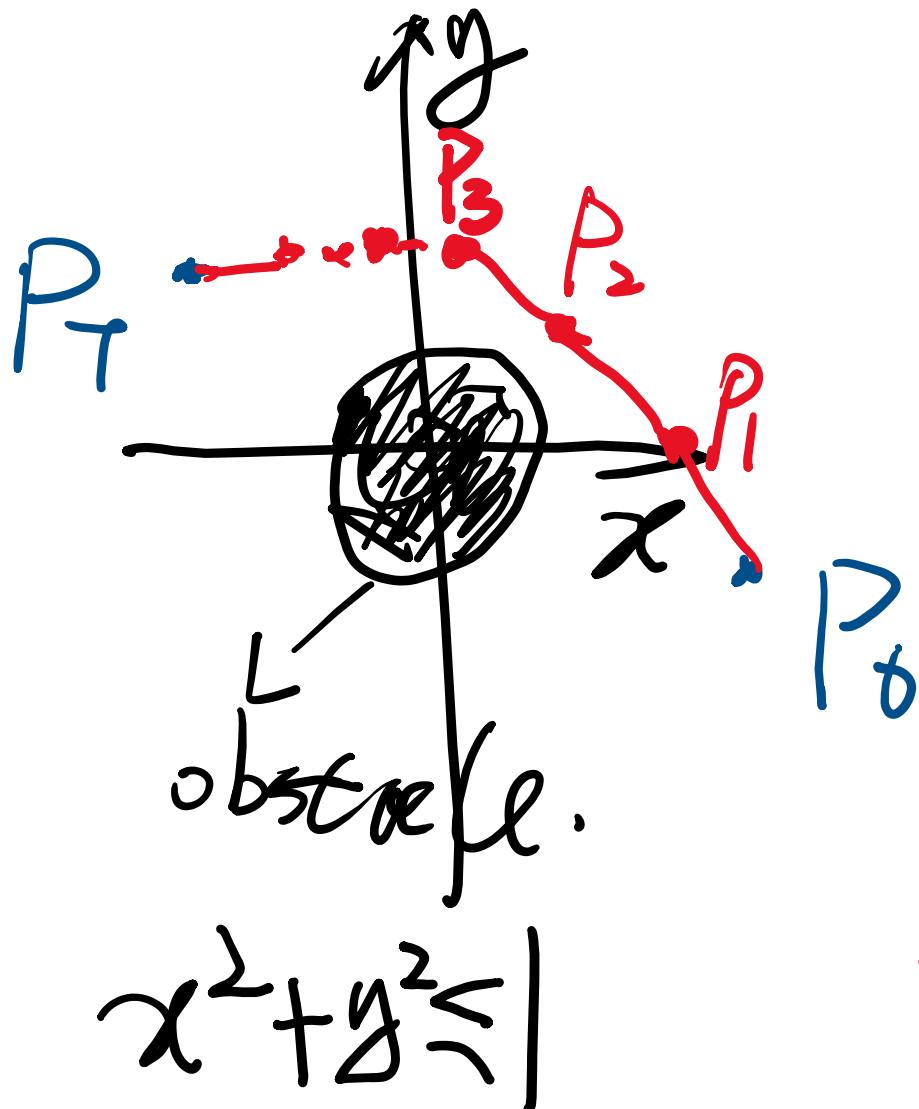
for all robot parts, for all obstacles:  
no collision  $\longrightarrow$  **non-convex**

***Solution method: sequential convex optimization***



# Trajectory optimization

(Example)



$$\min_{P_0 \dots P_T} : \sum_n \|(P_n - P_{n-1})\|^2 + \text{other cost}$$

S.t.:

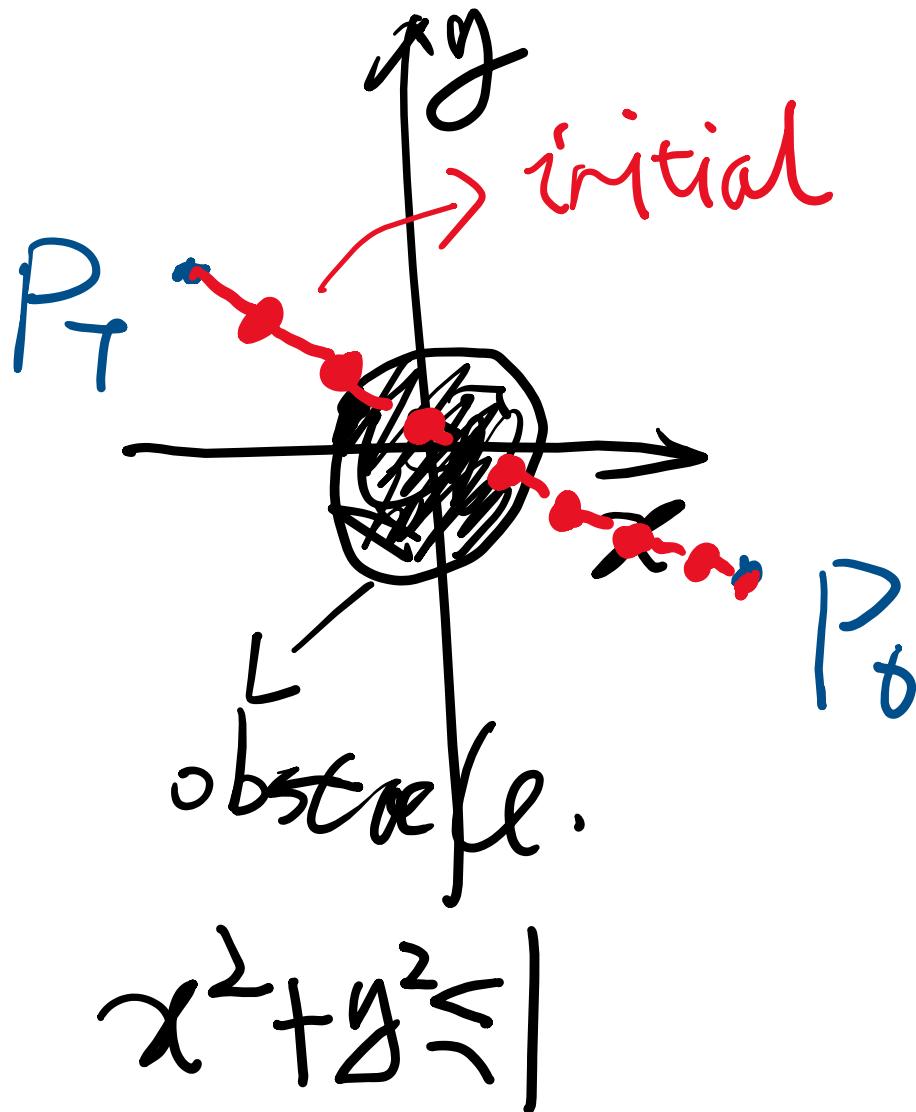
$$\|P_n\| \geq 1 + s_{\text{safe}}$$

try to play with this example



# Trajectory optimization

(Example)

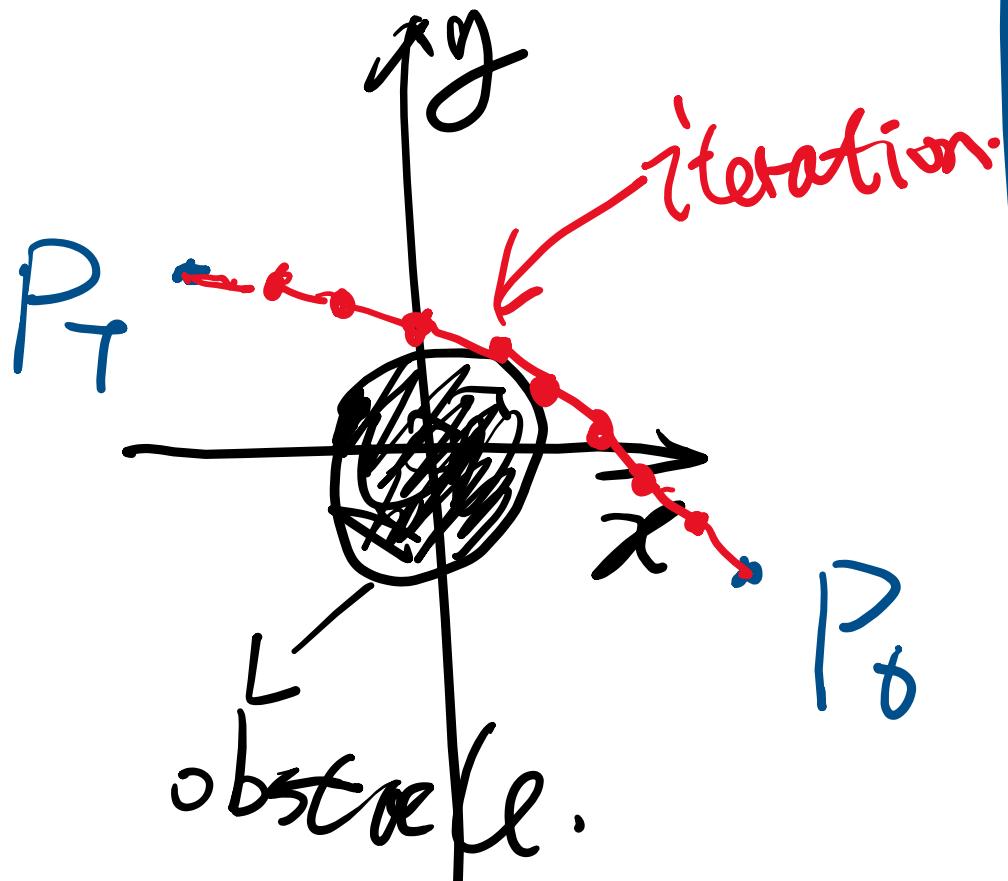


$$\begin{aligned} \min_{P_0 \dots P_T} : & \sum_n \|(P_n - P_{n-1})\|^2 \\ & + \text{other cost} \\ \text{S.t.: } & \|P_n\| \geq 1 + s_{\text{safe}}. \end{aligned}$$



# Trajectory optimization

(Example)



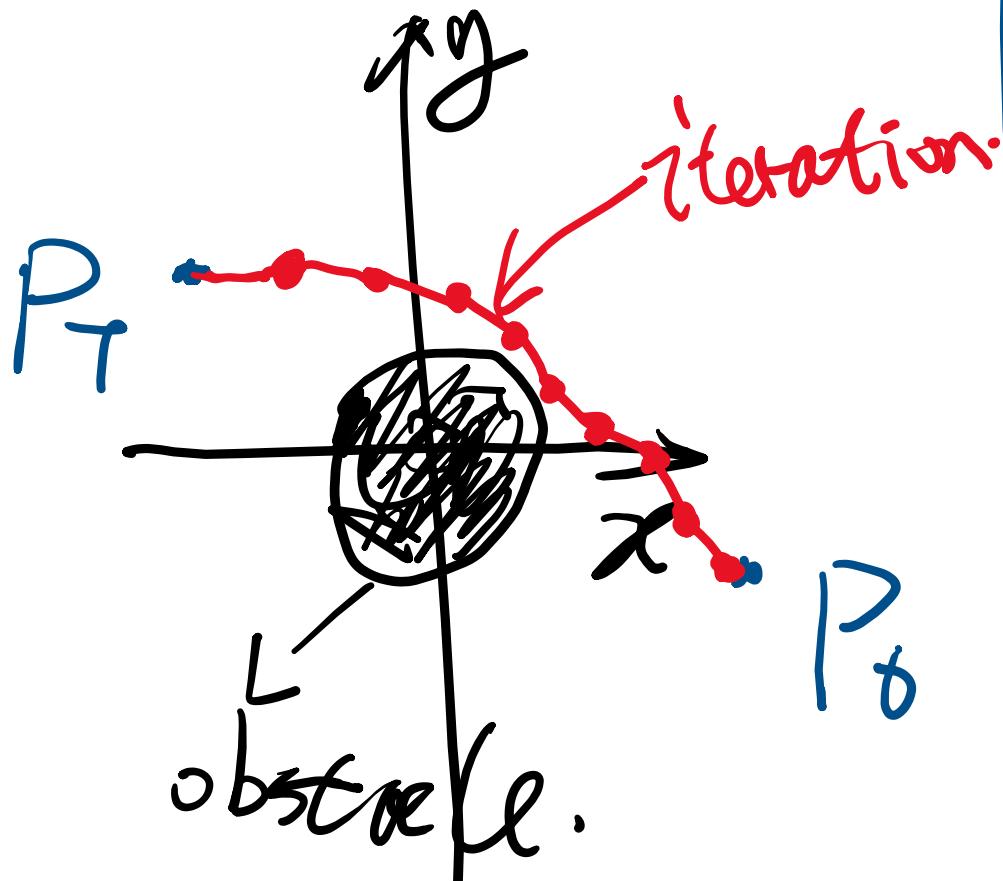
$$x^2 + y^2 \leq 1$$

$$\begin{aligned} \min_{P_0 \dots P_T} : & \sum_n \|(P_n - P_{n-1})\|^2 \\ & + \text{other cost} \\ \text{S.t.: } & \|P_n\| \geq 1 + s_{\text{safe}}. \end{aligned}$$



# Trajectory optimization

(Example)

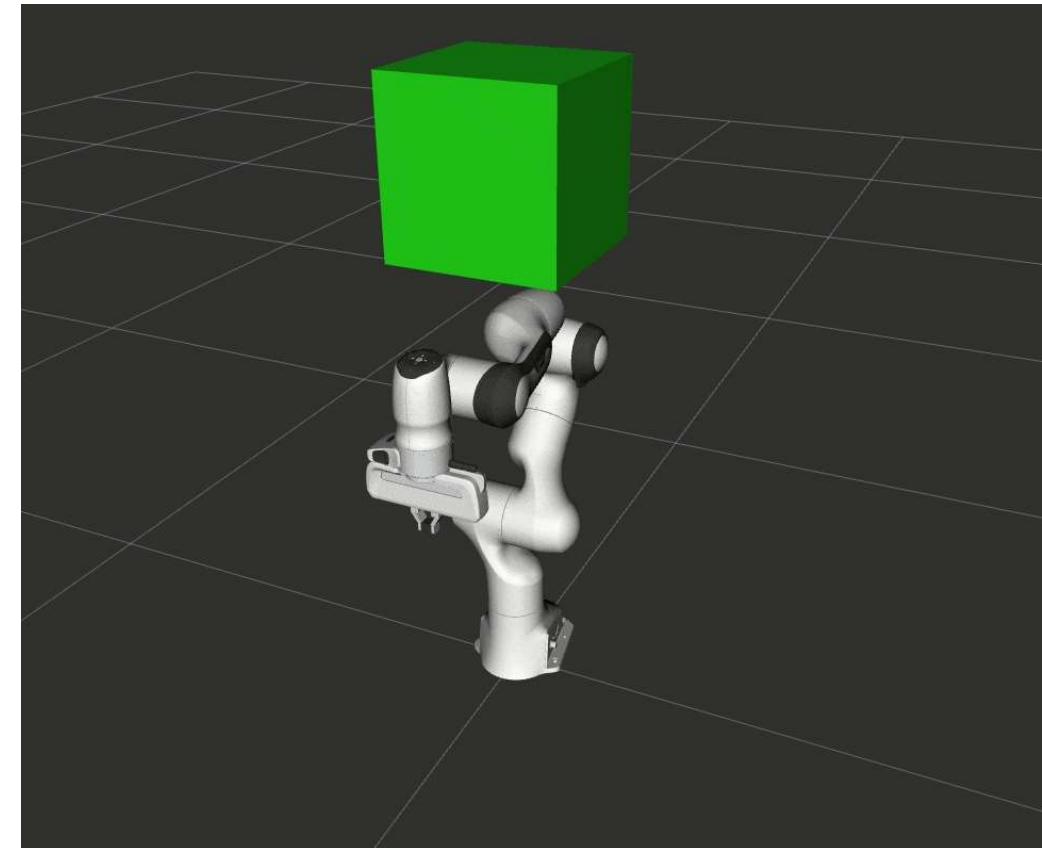
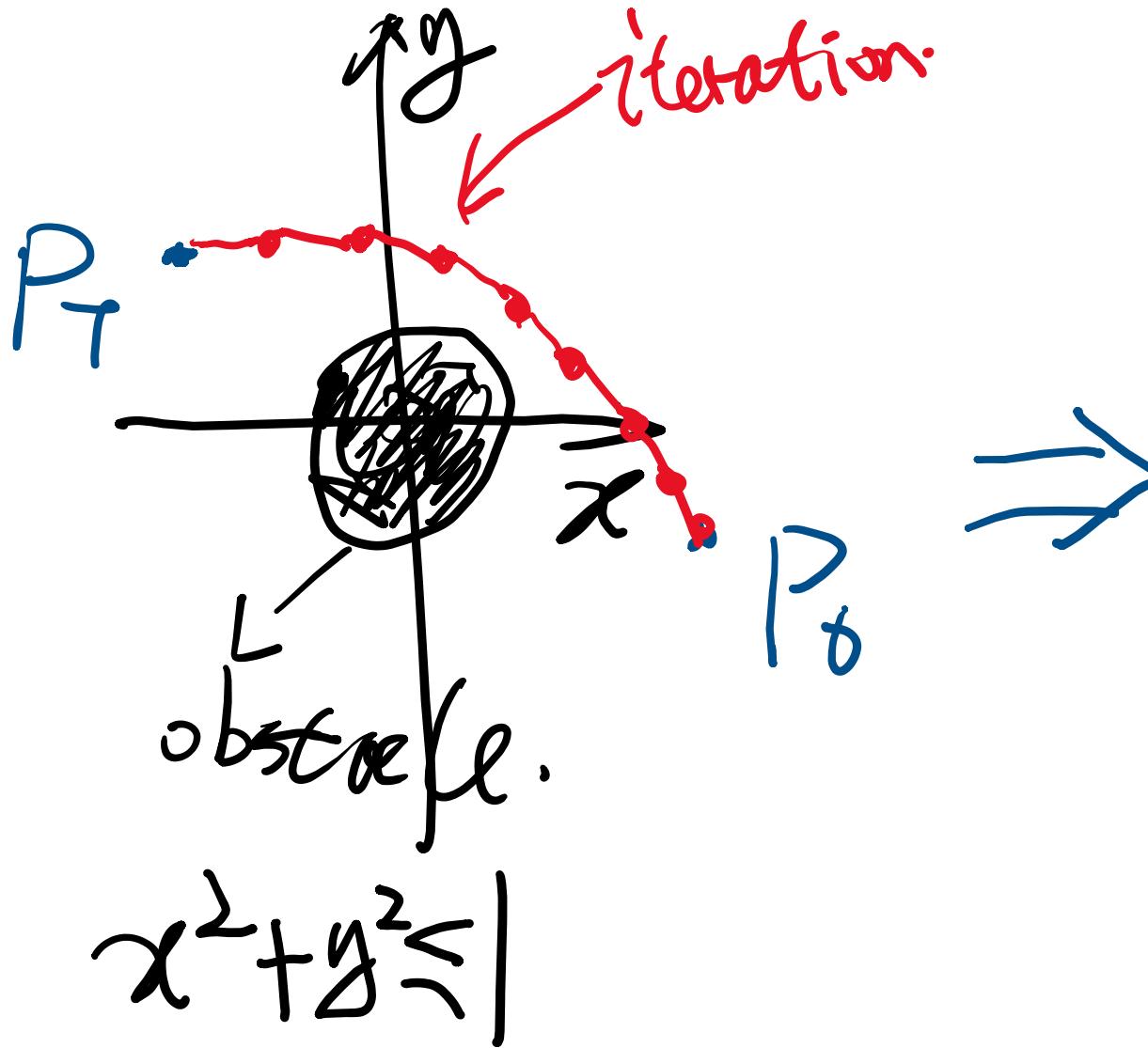


$$\begin{aligned} \min_{P_0 \dots P_T} : & \sum_n \|(P_n - P_{n-1})\|^2 \\ & + \text{other cost} \\ \text{S.t.: } & \|P_n\| \geq 1 + s_{\text{safe}}. \end{aligned}$$



# Trajectory optimization

(Example)



more complex constraints



# Trajectory optimization

## Efficient Trajectory Optimization for Robot Motion Planning

Yu Zhao, Hsien-Chung Lin, and Masayoshi Tomizuka

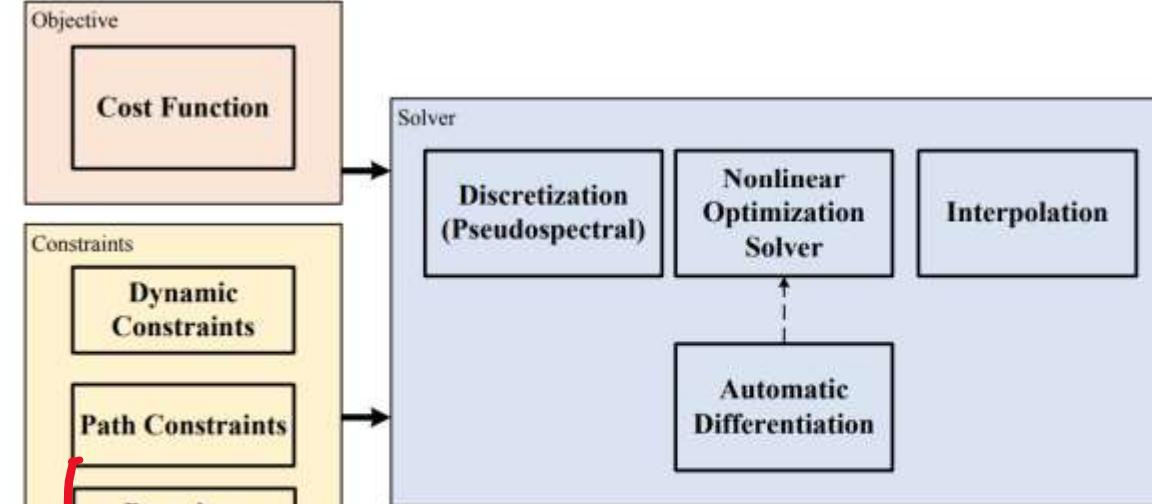
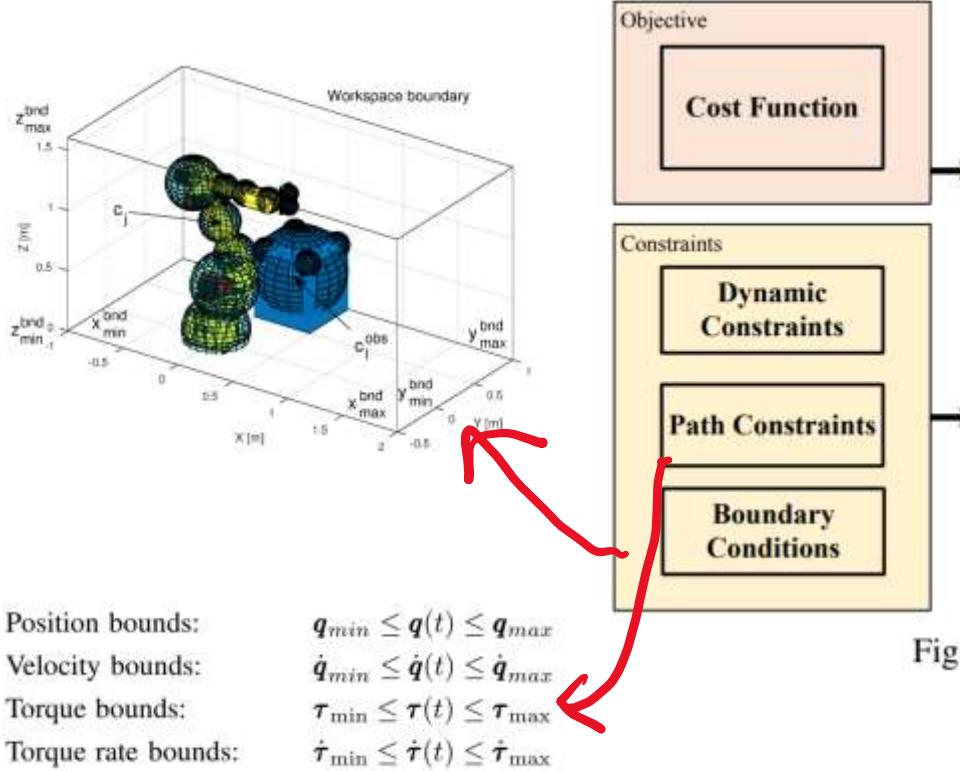
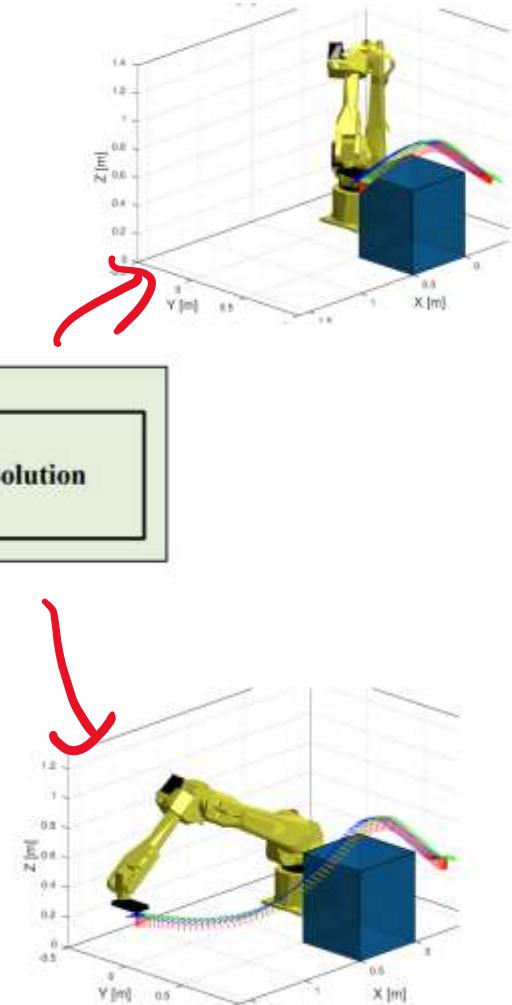


Fig. 2: Efficient numerical method for trajectory optimization





# Trajectory optimization

STOMP: Stochastic Trajectory Optimization for Motion Planning

Mrinal Kalakrishnan<sup>1</sup>

Sachin Chitta<sup>2</sup>

Evangelos Theodorou<sup>1</sup>

Peter Pastor<sup>1</sup>

Stefan Schaal<sup>1</sup>

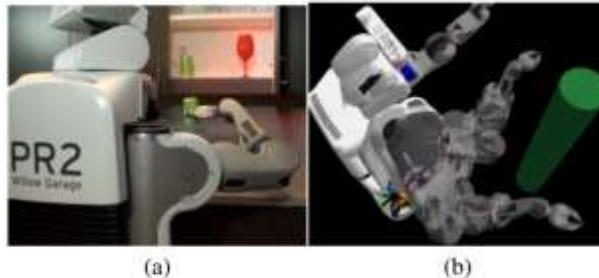
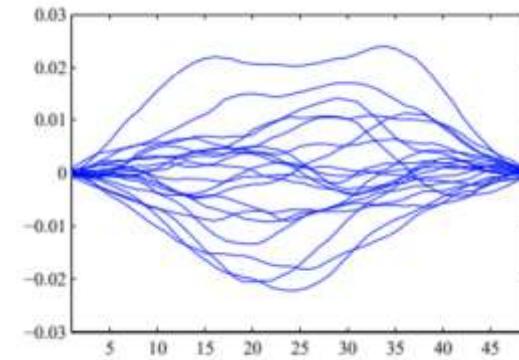
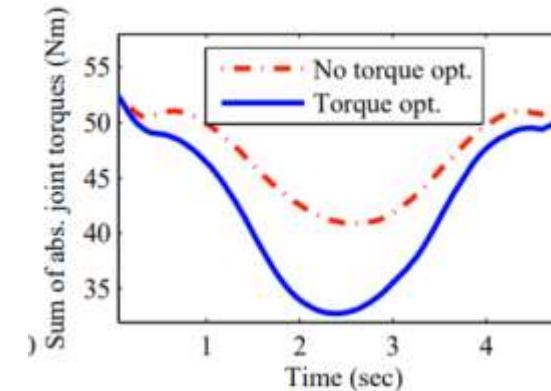


Fig. 1. (a) The Willow Garage PR2 robot manipulating objects in a household environment. (b) Simulation of the PR2 robot avoiding a pole in a torque-optimal fashion.



$$\min_{\tilde{\theta}} \mathbb{E} \left[ \sum_{i=1}^N q(\tilde{\theta}_i) + \frac{1}{2} \tilde{\theta}^\top \mathbf{R} \tilde{\theta} \right]$$

STOMP is an algorithm that performs local optimization, i.e. it finds a locally optimum trajectory rather than a global one. Hence, performance will vary depending on the initial



Sample locally  
optimize locally



# Today's Agenda

- Recap of sampling-based approach (~10)
- Recap of optimization-based approach (~20)
- **Drawback of sampling and optimization (~5)**
- Recap of perception-action loop (~2)
- Learning-based motion planning (~5)
- Imitation learning (~20)
- Reinforcement learning (~10)



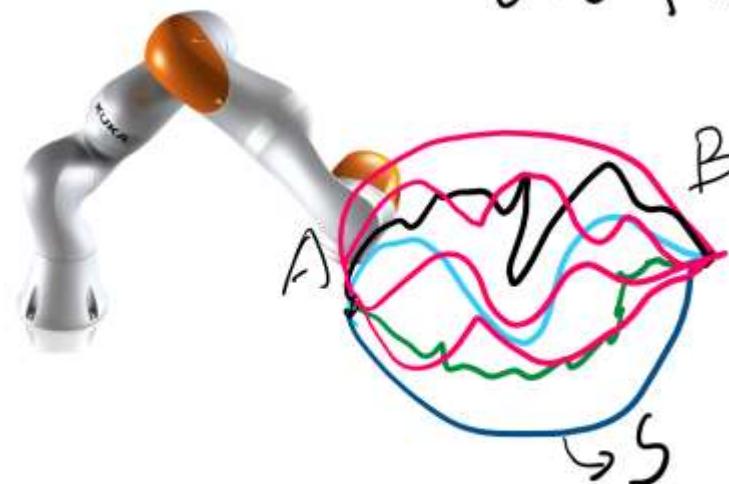
# Drawback of sampling and optimization-based approaches

- **Flexibility**
- **Human-like**
- **Reactive**
- **Sensory feedback**



# Drawback of sampling and optimization-based approaches

- **Flexibility**
- Human-like
- Reactive
- Sensory feed



Cost function:  $V: S \rightarrow R^+$

- path length
- efficiency
- obstacle avoidance
- uncertainty reduction
- predictability
- legibility / intent expression
- human comfort
- naturalness

difficult to represent.



# Drawback of sampling and optimization-based approaches

- Flexibility
- Human-like
- Reactive
- Sensory feedback



<https://www.therobotreport.com/researchers-develop-human-aware-motion-planning-algorithm/>



# Drawback of sampling and optimization-based approaches

- Flexibility
- Human-like
- Reactive
- Sensory feedback

[https://www.youtube.com/watch?v=-9JrDMBg2HE&t=38s&ab\\_channel=MITCSAIL](https://www.youtube.com/watch?v=-9JrDMBg2HE&t=38s&ab_channel=MITCSAIL)



# Drawback of sampling and optimization-based approaches

- **Flexibility**
- **Human-like**
- **Reactive**
- **Sensory feed**

Reactive Human-to-Robot Handovers of Arbitrary Objects





# Drawback of sampling and optimization-based approaches

- Flexibility
- Human-like
- **Reactive**
- Sensory feed

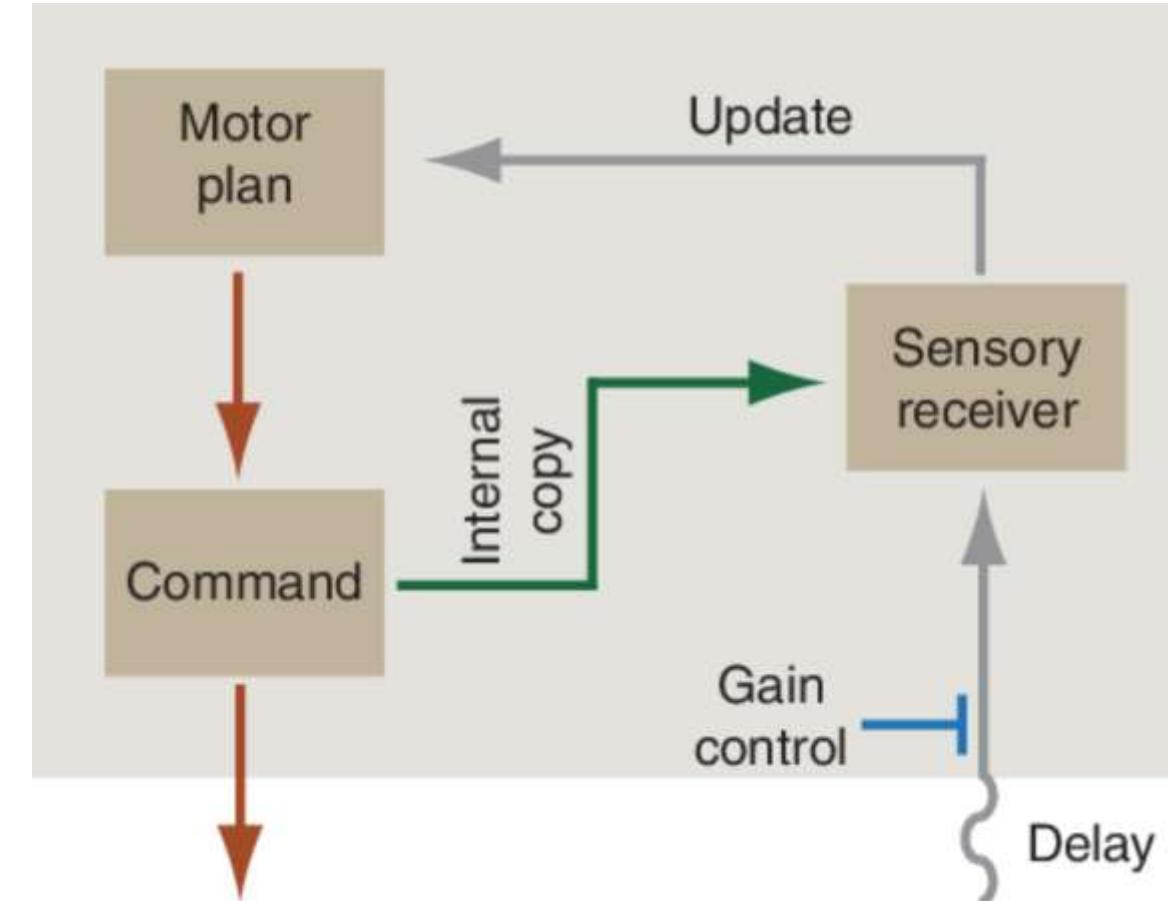


[https://research.nvidia.com/publication/2021-03\\_reactive-human-robot-handovers-arbitrary-objects](https://research.nvidia.com/publication/2021-03_reactive-human-robot-handovers-arbitrary-objects)



# Drawback of sampling and optimization-based approaches

- Flexibility
- Human-like
- Reactive
- **Sensory feedback**



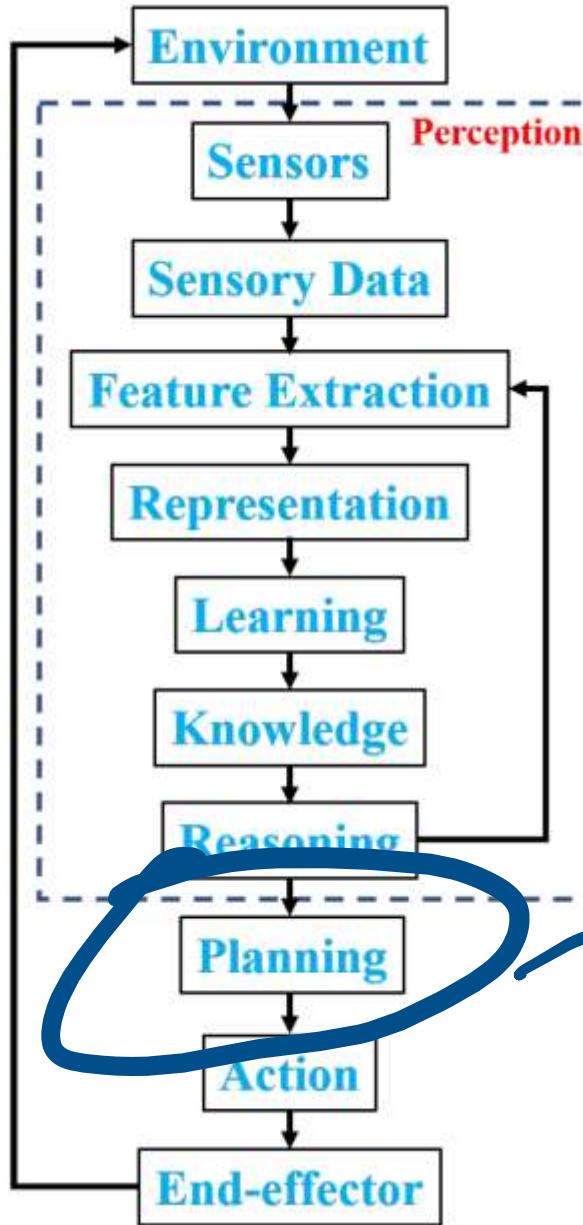


# Today's Agenda

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- Learning-based motion planning (~5)
- Imitation learning (~20)
- Reinforcement learning (~10)



# Planning in Robotics

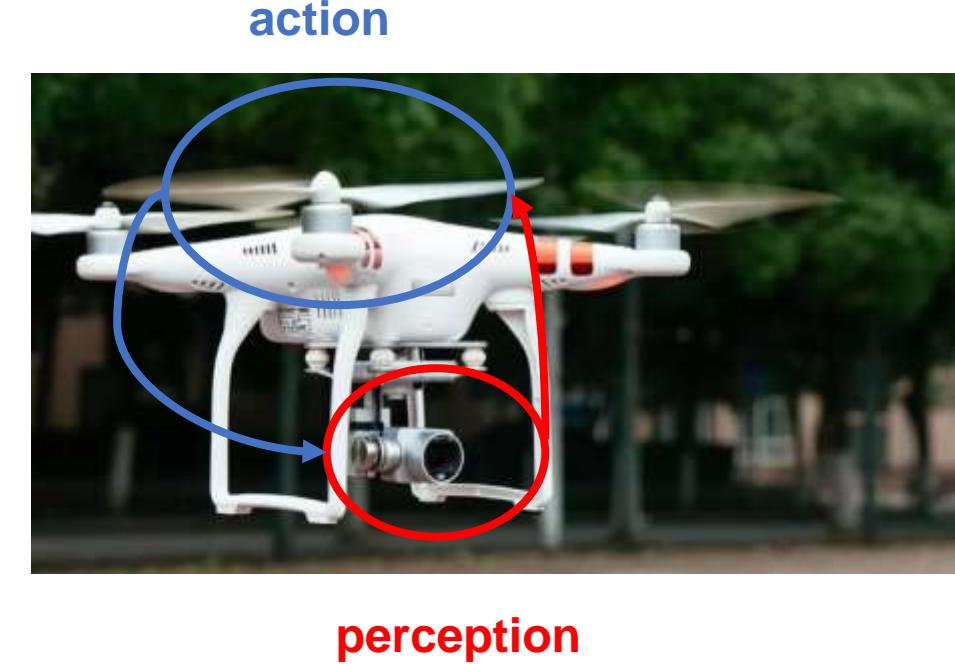
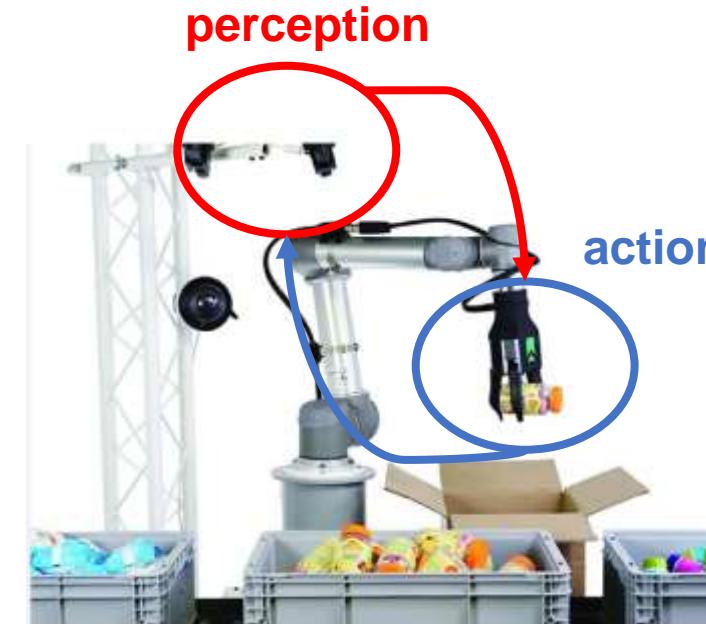
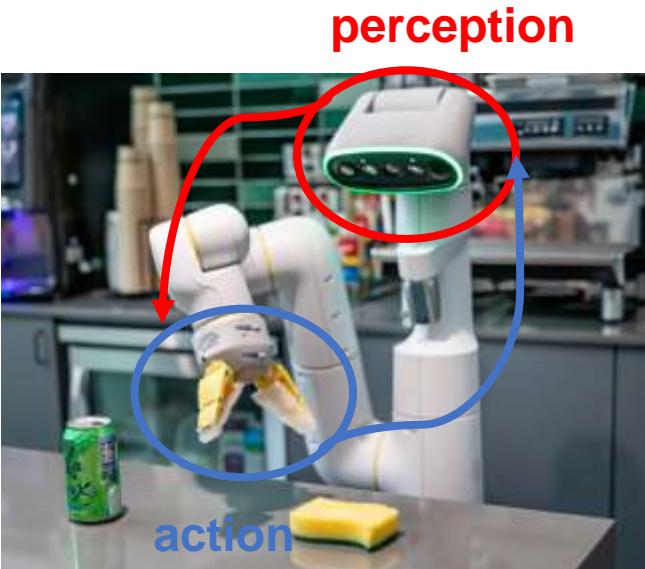


Robotics – Learn the **mapping** from perception to action

real-time .  
↙  
fast sampling      ↓  
fast optimization



# Motion Planning in Robotics



Robotics – Learn the **mapping** from perception to action

↓ *not just a  $y=f(x)$*



# Today's Agenda

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- **Imitation learning (~20)**
- Reinforcement learning (~10)



# Learning

## Learning Modes

Explicit Learning:  
Reinforcement  
Verbal instructions

Implicit Learning:  
Observational learning  
**Imitation learning**



# Imitation learning

Learning seems to be a negative force in evolution.  
How can learning have evolved?

*Learning serves as a pacemaker for evolution, when exploratory behavior leads to a breakthrough for the survival of the species, the capacity for that kind of exploratory behavior and the imitation of this act is favored by natural selection.*



# Imitation learning

## Imitation Capabilities in Animals

Which species may exhibit imitation is still a main area of discussion and debate

One differentiates “true” imitation from copying (flocking, schooling, following), stimulus enhancement, contagion or emulation

Biological Inspiration





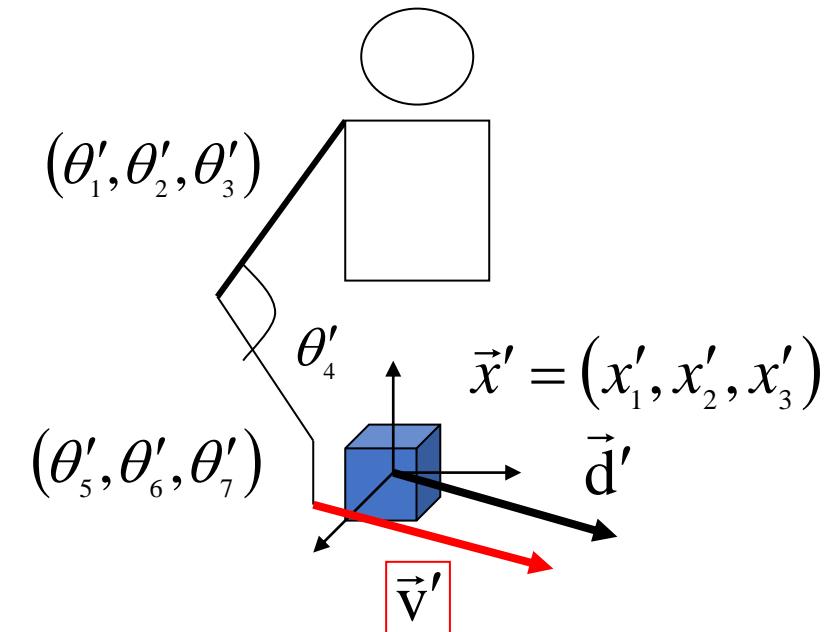
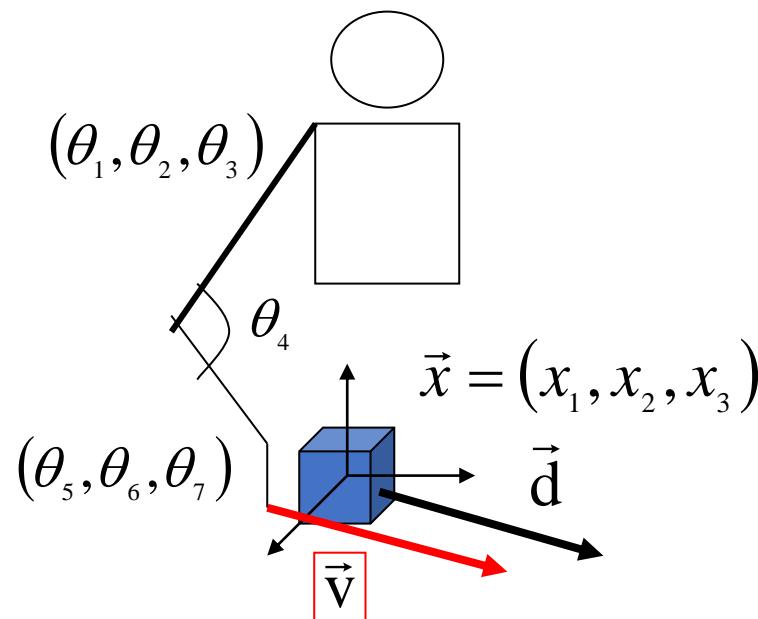
# Imitation learning

$\vec{x} = \vec{x}'$       Same Object, same target location

$\vec{d} = \vec{d}'$       Same direction of motion

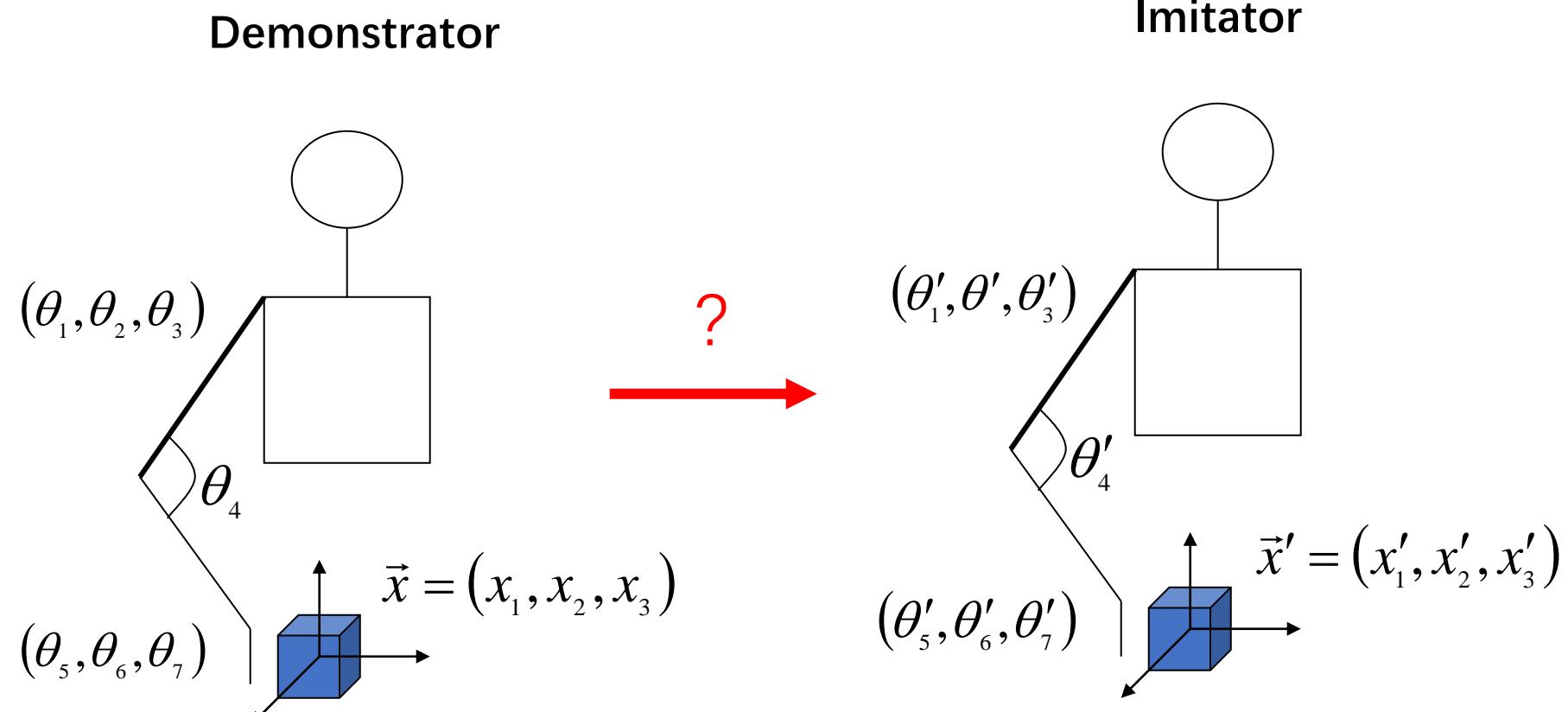
$\vec{v} = \vec{v}'$       Same speed, same force

$\vec{\theta} = \vec{\theta}'$       Same posture





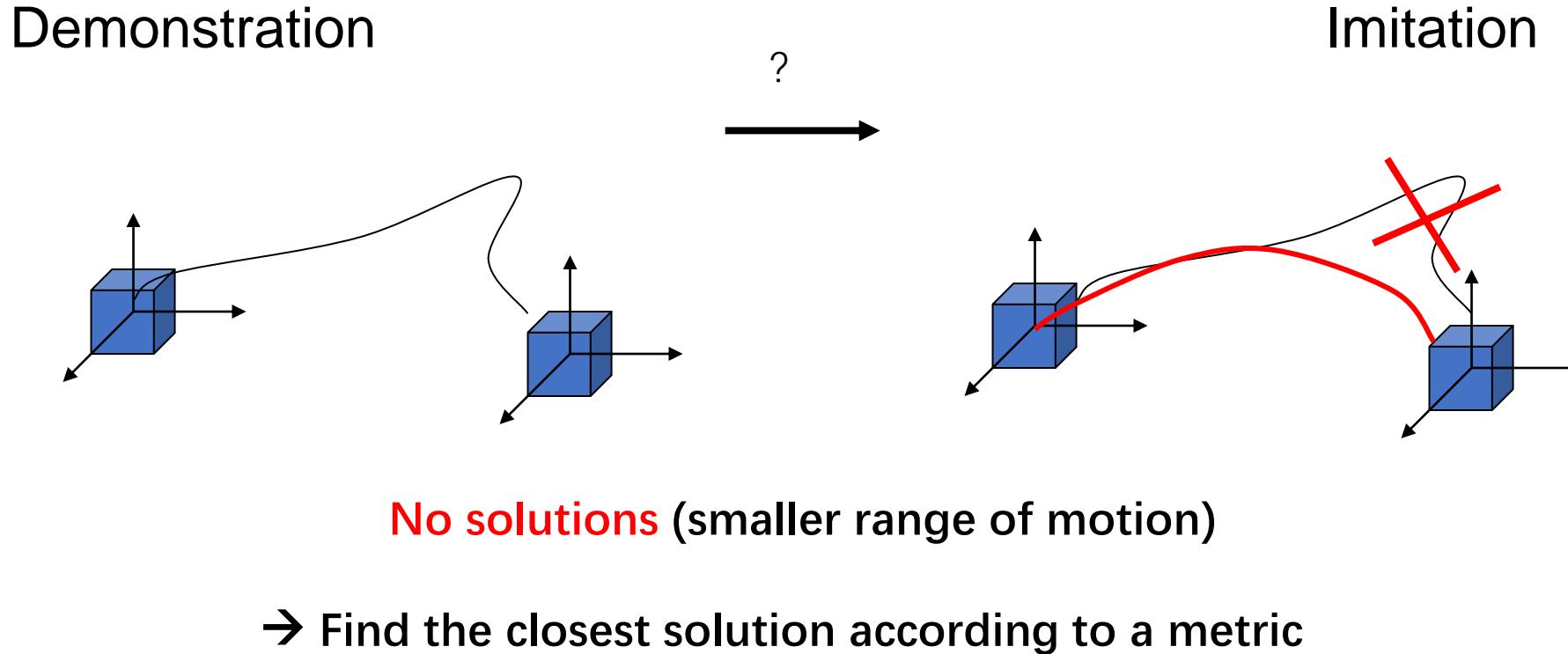
# Imitation learning



The Transfer problem



# Imitation learning



**How to Imitate?  
The correspondence problem**



# Imitation learning

*Learning What to imitate*



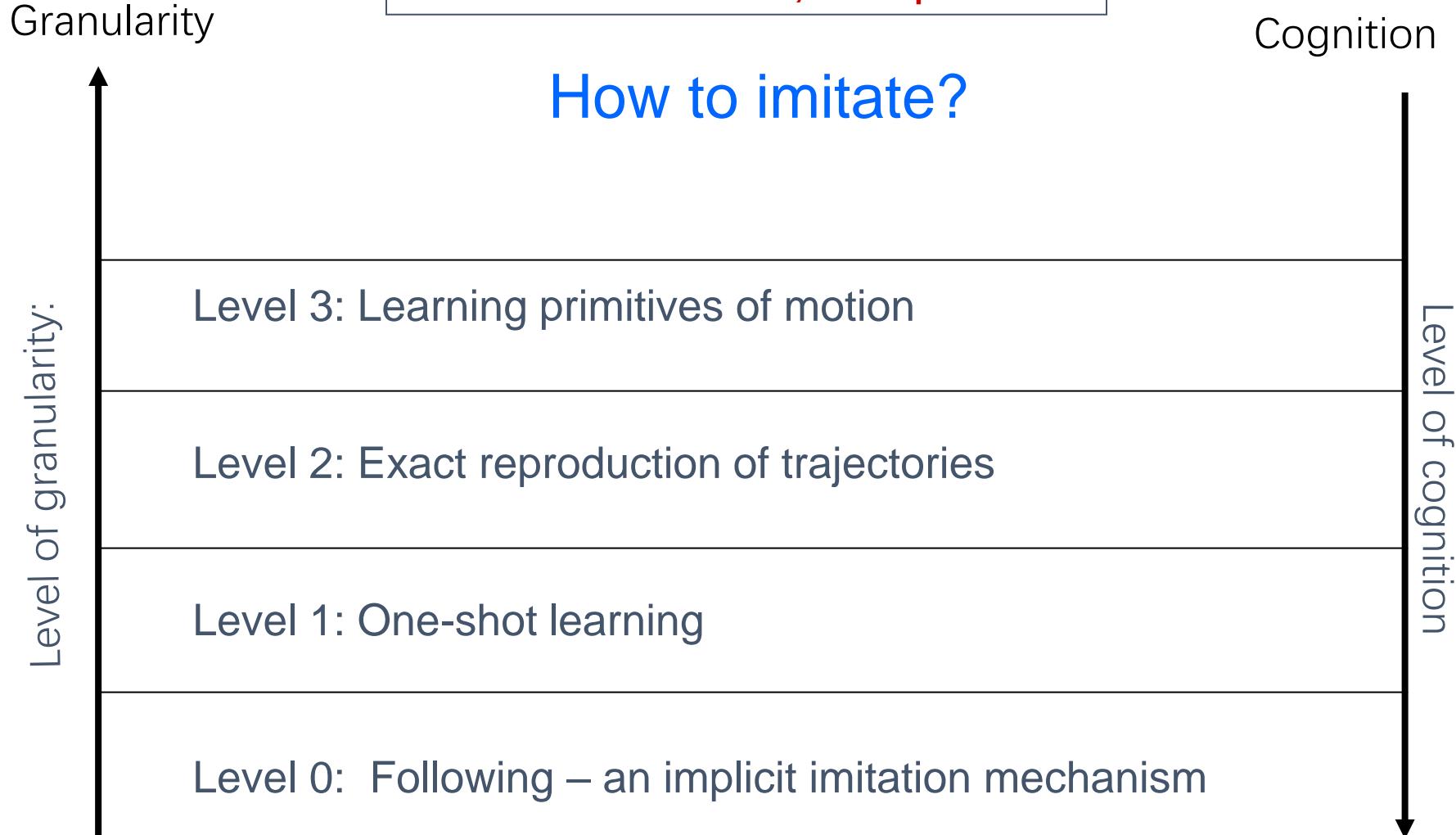
Imitation learning – Programming by Demonstration:

- A way **to speed up learning**, to reduce the search space
- A way **to share** with robots the same **vocabulary** of motor skills



# Imitation learning

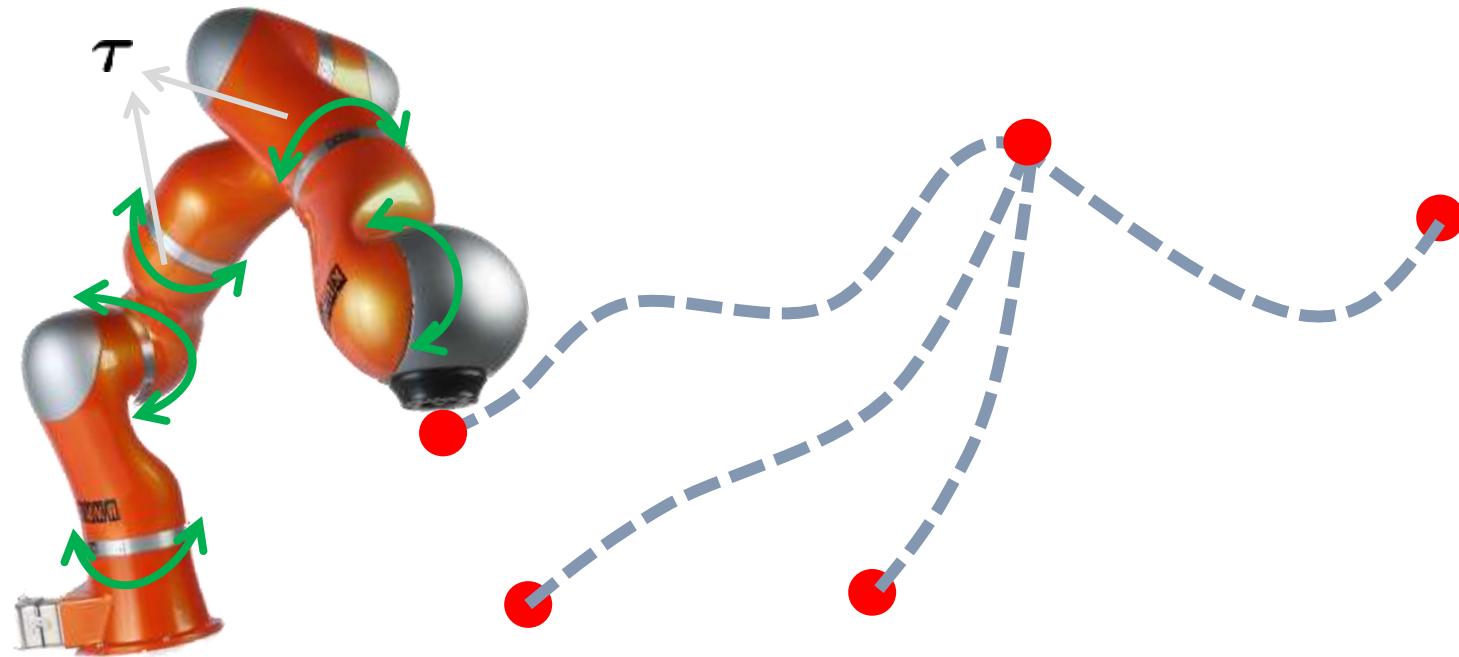
Imitation Learning in Robots  
Prof. Aude Billard, lasa.epfl.ch





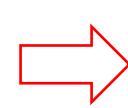
# Imitation learning

$$\mathbf{M}_h(\boldsymbol{\theta})\ddot{\boldsymbol{\theta}}_r + \mathbf{C}_h(\boldsymbol{\theta}, \dot{\boldsymbol{\theta}})\dot{\boldsymbol{\theta}} + \mathbf{g}_h(\boldsymbol{\theta}) = \boldsymbol{\tau}$$

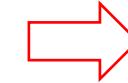




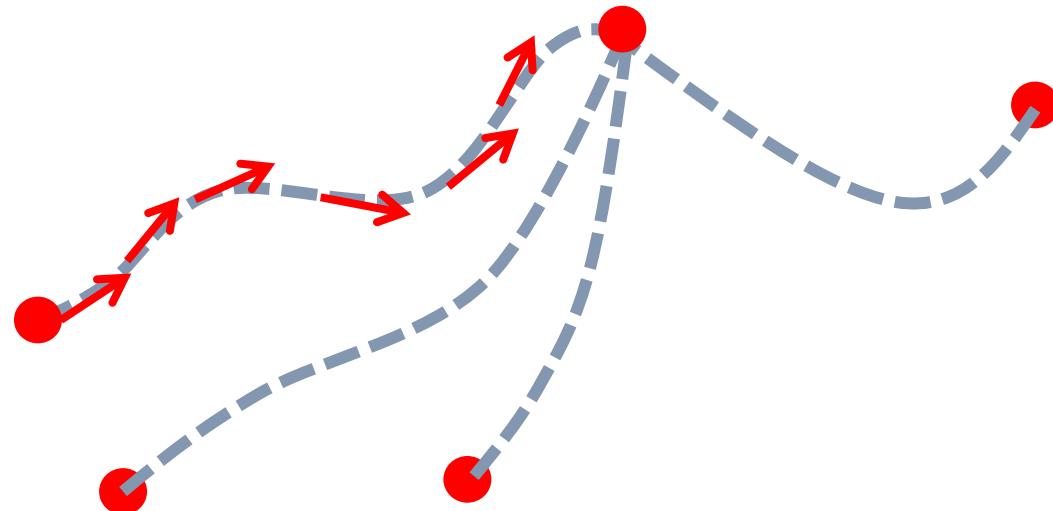
# Imitation learning



learning



$\dot{x} = f(x)$

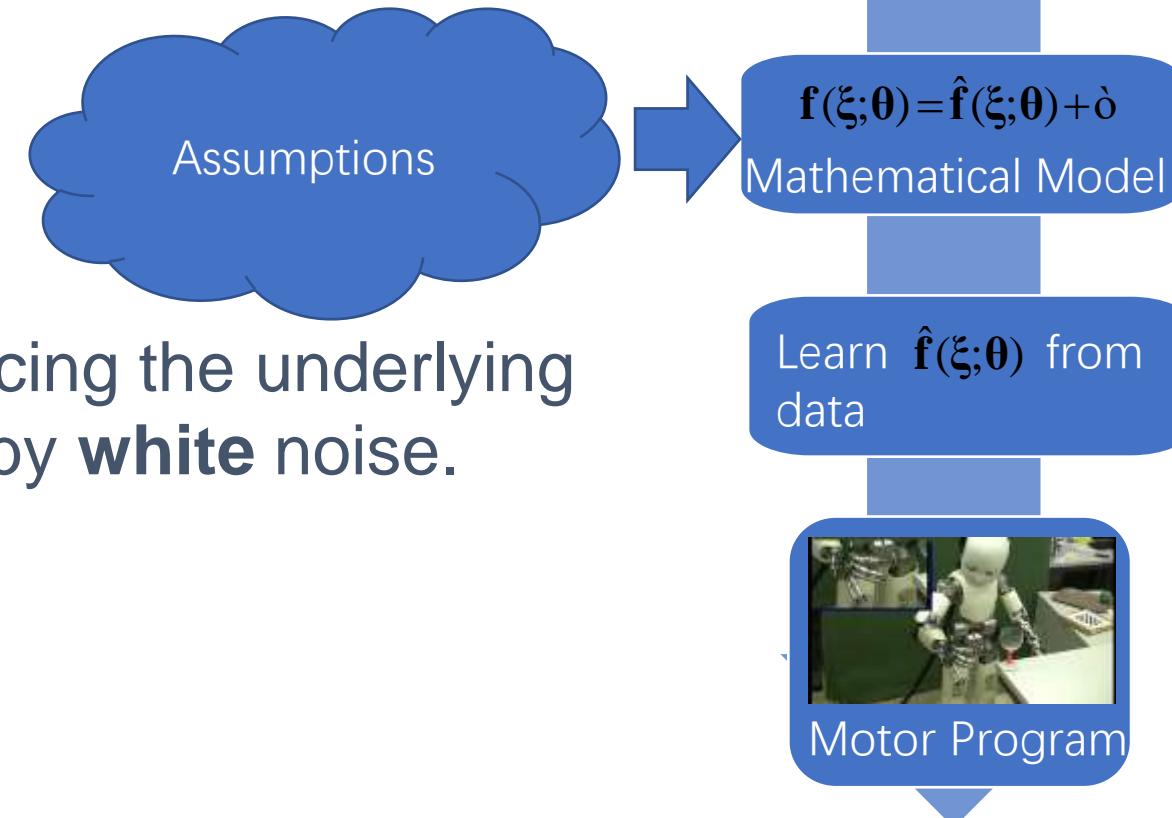




# Imitation learning

## *Programming by Demonstration (Imitation Learning)*

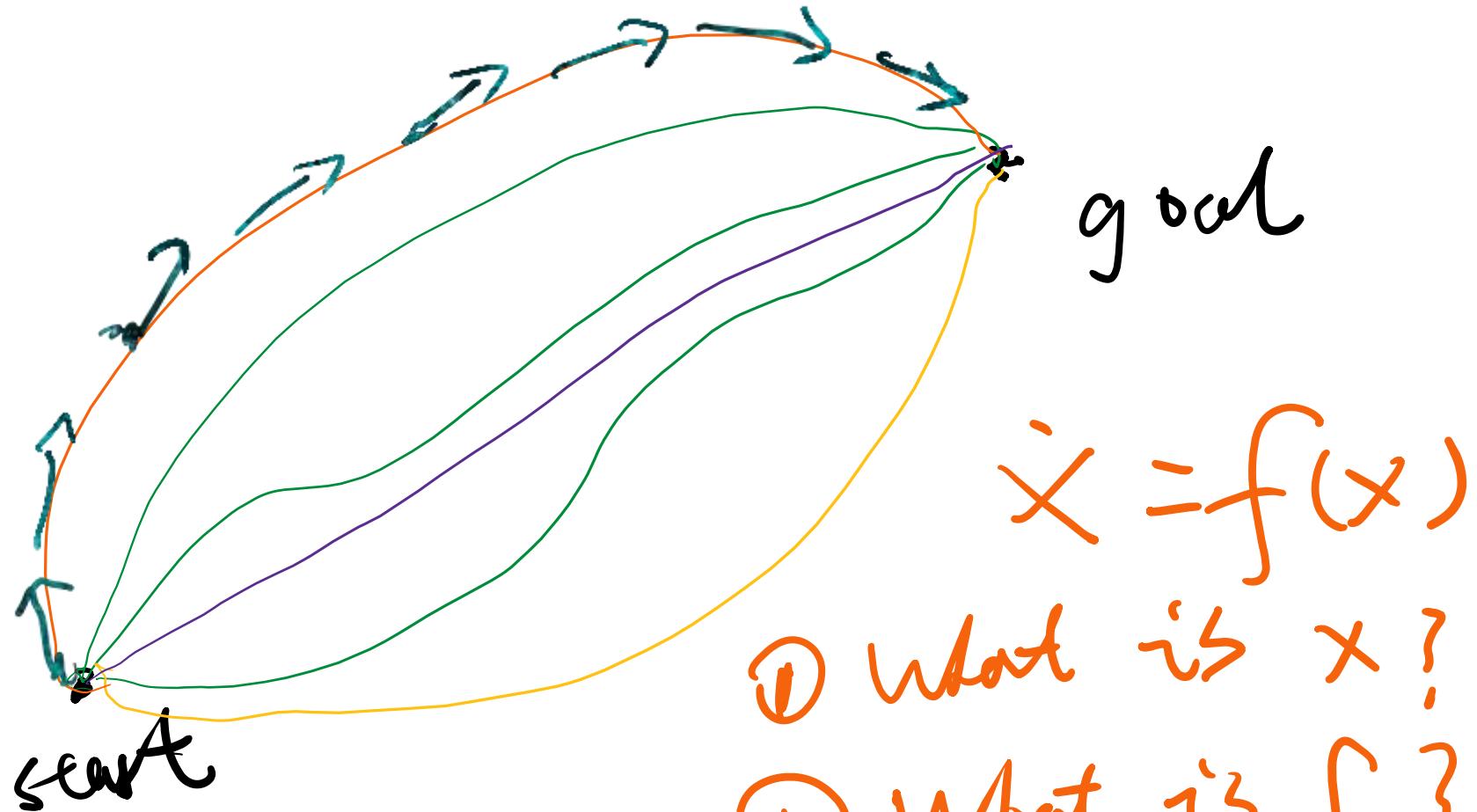
- ▶ A task is characterized by an underlying deterministic relationship between the **relevant** variables



- ▶ Demonstration: reproducing the underlying relationships corrupted by **white** noise.



# Imitation learning



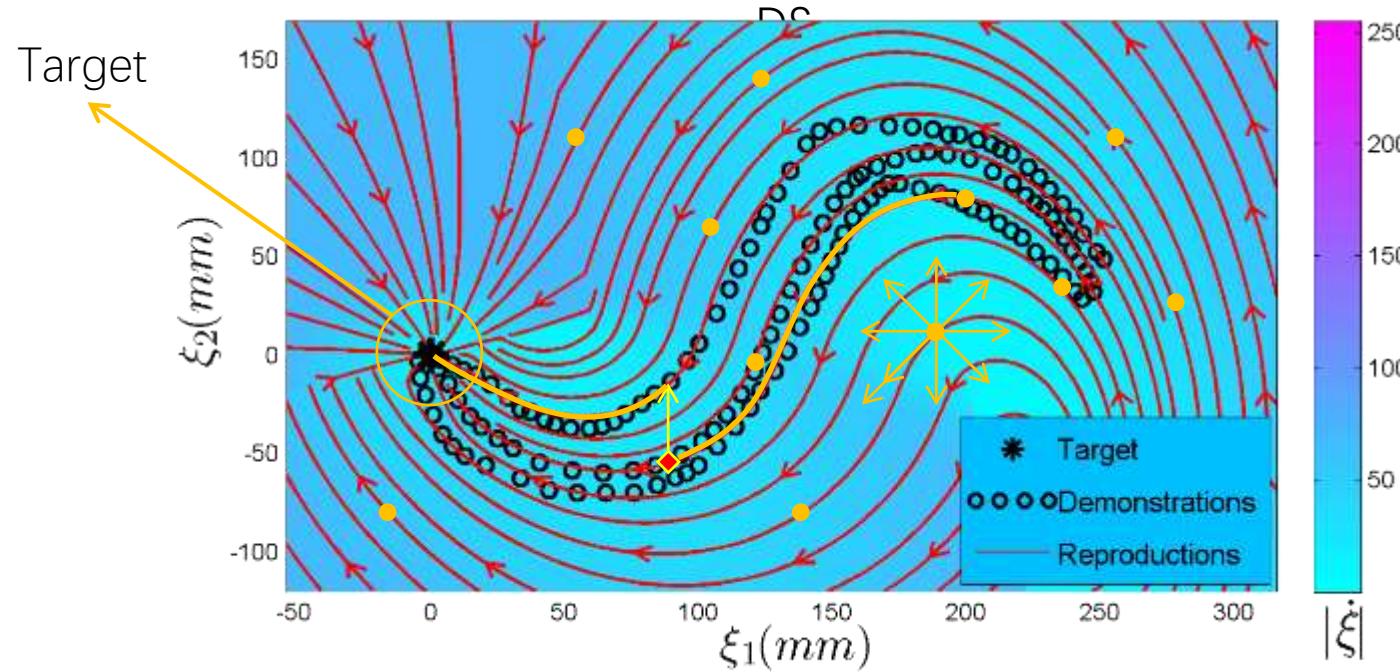
Question: collision?



# Imitation learning

$$\dot{\xi} = f(\xi)$$

Streamlines of a *globally asymptotically* stable



Given: Some demonstrations of a point-to-point motion.

Learned: Globally asymptotically stable map from states to velocities stable at the sole target.



# Imitation learning

exp design:

hardware

sensor

proto.col.

intention

interface

data collection:

joint angles

pos/rot

force

tactile -  
vision

:

learning alg

GMM

GP

SVM

:

Deep learning

LLM

RT-2.



# Imitation learning

exp design:

hardware

Sens.

Protocol

intention

interface

data collection:

joint angles

Tactile -  
vision

:

Learning Alg.

GMM

M

:

Deep learning

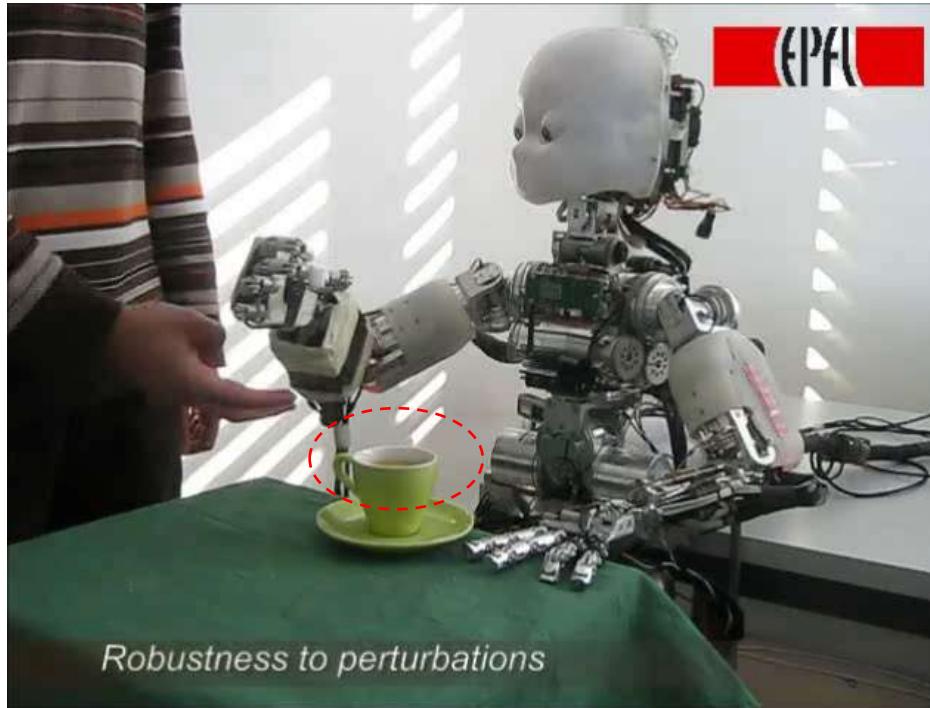
LLM

RT-2.

More details will be introduced in  
imitation learning course!



# Imitation learning





# Imitation learning

## Google Deep Learning for Grasping

Learning Hand-Eye Coordination for Robotic Grasping with Deep Learning  
and Large-Scale Data Collection

Sergey Levine  
Peter Pastor  
Alex Krizhevsky

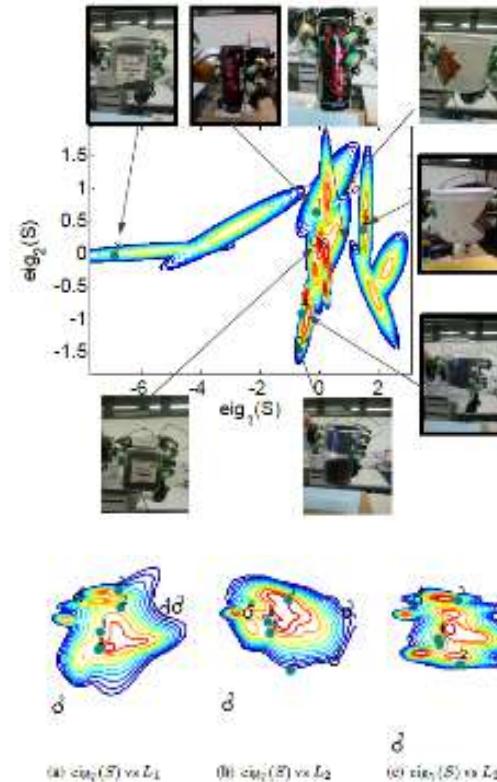
SLEVINE@GOOGLE.COM  
PETERPASTOR@GOOGLE.COM  
AKRIZHEVSKY@GOOGLE.COM



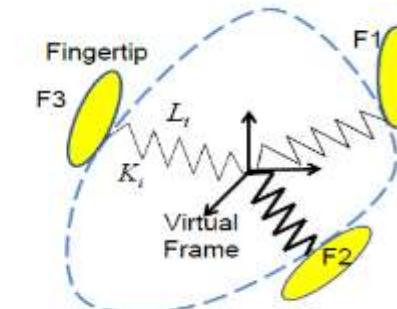


# Imitation learning

Stability = sensory information  
+ motor action



## Object-level Impedance Controller



Learning of Grasp Adaptation through  
Experience and Tactile Sensing

Miao Li, Yasemin Bekiroglu,  
Danica Kragic and Aude Billard

IROS 2014



# Imitation learning

Student project intro

- 1. ultrasound Robot
- 2. GraspAda



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- Imitation learning (~20)
- Reinforcement learning (~10)



# Goal for this course

- Design: soft hand design **x1**
- Perception: vision, point cloud, tactile, force/torque **x1**
- Planning: sampling-based, optimization-based, **learning-based x3**
- Control: feedback, multi-modal **x2**
- Learning: imitation learning, RL **x2**
- Simulation tool (pybullet, matlab, OpenRAVE, Issac Nvidia, Gazebo)
- **How to get a robot moving!**