BrainData application

Chanwoo Lee, September 7, 2020

1 Data transformation

goal: find a reasonable rank try extreme case: full rank —> vectorized SVM

1.1 Simulation setting

I perform 5 folded cross validation based on 4 different data sets. The following shows how data sets are generated from the raw brain data set.

- 1. Method 1: The raw brain data set $X_i \in \mathbb{R}^{68 \times 68}$ for $i = 1, \dots, 212$.
- 2. Method 2: The centered brain data set such that $\boldsymbol{X}_i^{(2)} = \boldsymbol{X}_i \bar{\boldsymbol{X}}$ for $i = 1, \dots, 212$, where $\bar{\boldsymbol{X}} = \frac{1}{212} \sum_{i=1}^{212} \boldsymbol{X}_i$.
- 3. Method 3: The normalized brain data set such that $X_i^{(3)} = X_i / ||X_i||_F$ for $i = 1, \dots 212$.
- 4. Method 4: The normalized and centered brain data set such that $\boldsymbol{X}_i^{(4)} = (\boldsymbol{X}_i \bar{\boldsymbol{X}}) / \|\boldsymbol{X}_i \bar{\boldsymbol{X}}\|_F$ for $i = 1, \dots, 212$.

I set all initializations are the same on each simulation by setting the same seed number.

1.2 Simulation result

How Y is simulated?

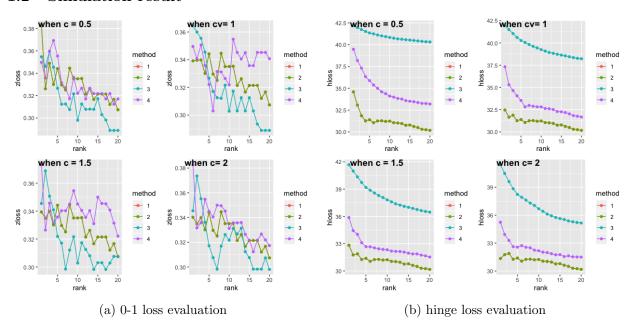


Figure 1: The figures plot the loss values according to given rank and cost in $\{1, ..., 20\} \times \{0.5, 1, 1.5, 2\}$

I found one interesting phenomenon. Method 1 and Method 2 have the exactly same output results. One reason I did not observe this phenomenon in previous experiment is that I did not use the same true coefficient matrix \boldsymbol{B} . I checked that with the same true coefficient matrix \boldsymbol{B} and same set seed number, the outputs from Method 1 and Method 2 are the same. Figure 1 shows that Method 1 works best in hinge loss evaluation and Method 3 performs best in 0-1 loss. From this simulation I

decided to use Method 1 because if we use Method 3, we might lose direct interpretation of coefficient matrix \boldsymbol{B} . To be specific, without normalization each entry of \boldsymbol{B} represents how important the brain connection is, which can be applied to all individual with the same magnitude. However, the weight of importance is changed to each individual if we use normalized \boldsymbol{B} .

Practical consideration: should we adjust covariates, e.g. age, gender? How?

2 Cross Validation results.

First simulation is to find overall range of cost value. I perform cross validation with cost values in $\{0.01, 0.1, 1, 10, 100\}$. I set the 3 multiple initializations to estimate the classifiers. We can see that cost values greater than 0.1 converges to the same output with cost = 0.1 as the rank size increases.

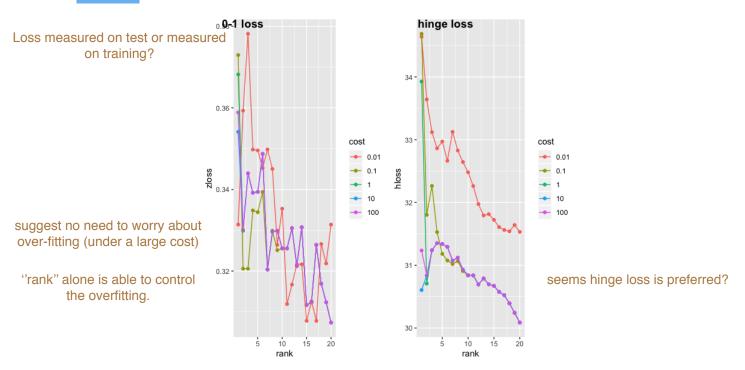


Figure 2: Cross validation results. The left figure shows 0-1 loss evaluation according to rank and cost combinations while the right one shows hinge loss evaluation.

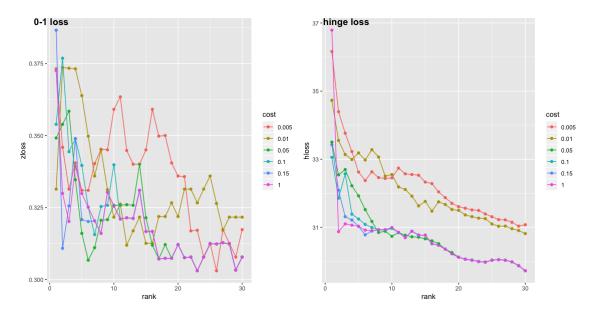


Figure 3: Cross validation results. The left figure shows 0-1 loss evaluation according to rank and cost combinations while the right one shows hinge loss evaluation.

try full rank r = 68 (i.e. classical SVM).

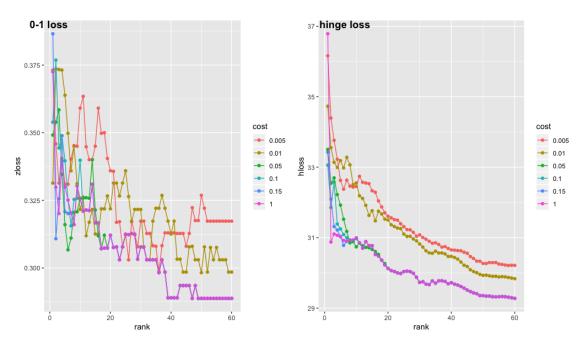


Figure 4: Cross validation results. The left figure shows 0-1 loss evaluation according to rank and cost combinations while the right one shows hinge loss evaluation.