# Package 'tensorsparse'

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Type Package

Title Multiway Clustering via Tensor Block Models		
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Suggests cluster		
<b>Description</b> Implements the multiway sparse clustering approach of M. Wang and Y. Zeng, "Multiway clustering via tensor block models". Advances in Neural Information Processing System 32 (NeurIPS), 715-725, 2019.		
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chooseClusteringSize Select the clustering size for order-3 sparse tensor clustering via BIC

## Description

Select the clustering size for three-way clustering. The function searches over a range of clustering sizes and outputs the one that minimizes BIC. The clustering size  $(d_1, d_2, d_3)$  is a length-3 vector consisting of the number of clusters in each mode.

#### Usage

```
chooseClusteringSize(
    x,
    k,
    r,
    l,
    lambda = 0,
    sim.times = 1,
    method = "L0",
    n.cores = NULL
)
```

## Arguments

X	a three-dimensional array
k	a vector, the possible numbers of clusters at mode 1
r	a vector, the possible numbers of clusters at mode 2
1	a vector, the possible numbers of clusters at mode 3
lambda	a numeric value, regularization coefficient
sim.times	the number of simulation replicates when performing clustering
method	two options: "L0", "L1". "L0" indicates L0 penalty, and "L1" indicates Lasso penalty
n.cores	the number of cores in parallel implementation

## Value

```
a list estimated_krl a 1*3 matrix consisting of the estimated clustering size BIC a vector consisting of the BIC value for all combinations of clustering sizes
```

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chooseLambda Select the regularization coefficient for or ing via BIC	rder-3 sparse tensor cluster-
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## Description

Select the regularization coefficient for three-way clustering. The clustering size is assumed to be known. The function searches over a range of regularization sizes and outputs the one that minimizes the BIC.

## Usage

```
chooseLambda(x, k, r, 1, lambda = NULL, method = "L0")
```

## Arguments

X	a three-dimensional array
k	an positive integer, the numbers of clusters at mode 1
r	an positive integer, the numbers of clusters at mode 2
1	an positive integer, the numbers of clusters at mode 3
lambda	a vector of possible lambda, eg: lambda = $c(0,50,100,200)$
method	two options: "L0", "L1". "L0" indicates L0 penalty, and "L1" indicates Lasso penalty

#### Value

a list
lambda the lambda with lowest BIC
BIC the BIC for each lambda in the given range
nonzeromus the number of clusters with non-zero means

getOrder3Tensor

Generate a random order-3 tensor

## Description

Generate an order-3 random tensor based on tensor block model.

## Usage

```
getOrder3Tensor(
    n,
    p,
    q,
    k = NULL,
    r = NULL,
    1 = NULL,
```

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```
error = 3,
sort = TRUE,
sparse.percent = 0,
center = FALSE,
seed = NULL,
mumin = -3,
mumax = 3
```

#### **Arguments**

n	the dimension at mode 1
p	the dimension at mode 2
q	the dimension at mode 3
k	an positive integer, the numbers of clusters at mode 1
r	an positive integer, the numbers of clusters at mode 2
1	an positive integer, the numbers of clusters at mode 3
error	a positive numeric value, noise level
sort	if TRUE, the tensor entries belonging to the same cluster would be assumed together
sparse.percent	the proportion of zero entries based on the Gaussian tensor block model
center	if True, the data tensor would be centered to zero-mean before clustering
seed	a positive integer, used to specify the random seed
mumin	a numeric value, the lower bound of the block mean
mumax	a numeric value, the upper bound of the block mean

#### Value

```
a list
x the tensor
truthX the underlying signal tensor following block model
truthCs true cluster label assignment at mode 1
truthDs true cluster label assignment at mode 2
truthEs true cluster label assignment at mode 3
mus the block means
binaryX the 0-1 tensor (0:the mean signal = 0; 1:the mean signal != 0)
```

## **Examples**

```
getOrder3Tensor(20,20,20,2,2,2)$x
```

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getOrder4Tensor Generate a random order-4 tensor
--

## Description

Generate a random order-4 tensor based on tensor block model.

## Usage

```
getOrder4Tensor(
  n,
  p,
  q,
  s,
  k = NULL,
  r = NULL,
  1 = NULL,
  m = NULL,
  error = 3,
  sort = TRUE,
  sparse.percent = 0,
  center = FALSE,
  seed = NULL,
  mumin = -3,
  mumax = 3
```

## Arguments

n	the dimension at mode 1
p	the dimension at mode 2
q	the dimension at mode 3
S	the dimension at mode 4
k	an positive integer, the numbers of clusters at mode 1
r	an positive integer, the numbers of clusters at mode 2
1	an positive integer, the numbers of clusters at mode 3
m	an positive integer, the numbers of clusters at mode 4
error	a positive numeric value, noise level
sort	if TRUE, the tensor entries belonging to the same cluster would be assumed together
sparse.percent	the proportion of zero entries based on the Gaussian tensor block model
center	if True, the data tensor would be centered to zero-mean before clustering
seed	a positive integer, used to specify the random seed
mumin	a numeric value, the lower bound of the block mean
mumax	a numeric value, the upper bound of the block mean

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#### Value

```
a list
x the tensor
truthX the underlying signal tensor following block model
truthCs true cluster label assignment at mode 1
truthDs true cluster label assignment at mode 2
truthEs true cluster label assignment at mode 3
truthFs true cluster label assignment at mode 4
mus the block means
binaryX the 0-1 tensor (0:the mean signal = 0; 1:the mean signal != 0)
```

## **Examples**

```
getOrder4Tensor(10,10,10,10,2,2,2,2)
```

tbmClustering

Perform tensor clustering via tensor block model (TBM)

## Description

Perform tensor clustering via tensor block model (TBM) method.

## Usage

```
tbmClustering(
    x,
    k,
    r,
    l,
    lambda = 0,
    max.iter = 1000,
    threshold = 1e-10,
    sim.times = 1,
    trace = FALSE,
    Cs.init = NULL,
    Ds.init = NULL,
    Es.init = NULL,
    method = "L0"
)
```

## Arguments

Χ	an order-3 data tensor
k	an positive integer, the numbers of clusters at mode 1
r	an positive integer, the numbers of clusters at mode 2
1	an positive integer, the numbers of clusters at mode 3
lambda	a numeric value, regularization coefficient

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max.iter	a positive integer, the maximum numbers of iteration
threshold	a positive small numeric value for convergence threshold
sim.times	the number of simulation replicates when performing clustering
trace	logic value, print result per each iteration if TRUE
Cs.init	vector or NULL, initial cluster label assignment at mode 1
Ds.init	vector or NULL, initial cluster label assignment at mode 2
Es.init	vector or NULL, initial cluster label assignment at mode 3
method	two options: "L0", "L1". "L0" indicates L0 penalty, and "L1" indicates Lasso penalty

#### Value

a list
judgeX estimated underlying signal tensor
Cs clustering result at mode 1
Ds clustering result at mode 2
Es clustering result at mode 3
mus estimated block means

## Author(s)

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## References

M. Wang and Y. Zeng, "Multiway clustering via tensoe block models". Advances in Neural Information Processing System 32 (NeurIPS), 715-725, 2019.

## **Examples**

```
x = getOrder3Tensor(20,20,20,2,2,2)$x
tbmClustering(x,2,2,2)
```

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