R documentation

of all in 'man/'

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Description

Create a Tensor-class object from an array, matrix, or vector.

Usage

```
as.tensor(x, drop = FALSE)
```

Arguments

x an instance of array, matrix, or vector drop whether or not modes of 1 should be dropped

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Value

```
a Tensor-class object
```

Examples

```
#From vector
vec <- runif(100); vecT <- as.tensor(vec); vecT
#From matrix
mat <- matrix(runif(1000),nrow=100,ncol=10)
matT <- as.tensor(mat); matT
#From array
indices <- c(10,20,30,40)
arr <- array(runif(prod(indices)), dim = indices)
arrT <- as.tensor(arr); arrT</pre>
```

dim-methods

Mode Getter for Tensor

Description

Return the vector of modes from a tensor

Usage

```
## S4 method for signature 'Tensor'
dim(x)
```

Arguments

Х

the Tensor instance

Details

```
dim(x)
```

Value

an integer vector of the modes associated with x

```
tnsr <- rand_tensor()
dim(tnsr)</pre>
```

fold 3

fold	General Folding of Matrix	

Description

General folding of a matrix into a Tensor. This is designed to be the inverse function to unfold-methods, with the same ordering of the indices. This amounts to following: if we were to unfold a Tensor using a set of row_idx and col_idx, then we can fold the resulting matrix back into the original Tensor using the same row_idx and col_idx.

Usage

```
fold(mat, row_idx = NULL, col_idx = NULL, modes = NULL)
```

Arguments

mat	matrix to be folded into a Tensor
row_idx	the indices of the modes that are mapped onto the row space
col_idx	the indices of the modes that are mapped onto the column space
modes	the modes of the output Tensor

Details

This function uses aperm as the primary workhorse.

Value

Tensor object with modes given by modes

References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009, Vol. 51, No. 3 (September 2009), pp. 455-500. URL: https://www.jstor.org/stable/25662308.

See Also

```
unfold-methods
```

```
tnsr <- new('Tensor',3L,c(3L,4L,5L),data=runif(60))
matT3<-unfold(tnsr,row_idx=2,col_idx=c(3,1))
identical(fold(matT3,row_idx=2,col_idx=c(3,1),modes=c(3,4,5)),tnsr)</pre>
```

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hosvd

(Truncated-)Higher-order SVD

Description

Higher-order SVD of a K-Tensor. Write the K-Tensor as a (m-mode) product of a core Tensor (possibly smaller modes) and K orthogonal factor matrices. Truncations can be specified via ranks (making them smaller than the original modes of the K-Tensor will result in a truncation). For the mathematical details on HOSVD, consult Lathauwer et. al. (2000).

Usage

```
hosvd(tnsr, ranks = NULL)
```

Arguments

tnsr Tensor with K modes

ranks a vector of desired modes in the output core tensor, default is tnsr@modes

Details

A progress bar is included to help monitor operations on large tensors.

Value

a list containing the following:

Z core tensor with modes speficied by ranks

U a list of orthogonal matrices, one for each mode

est estimate of tnsr after compression

fnorm_resid the Frobenius norm of the error fnorm(est-tnsr) - if there was no truncation, then
 this is on the order of mach_eps * fnorm.

Note

The length of ranks must match tnsr@num_modes.

References

L. Lathauwer, B.Moor, J. Vandewalle, "A multilinear singular value decomposition". Journal of Matrix Analysis and Applications 2000, Vol. 21, No. 4, pp. 1253–1278.

See Also

tucker

```
tnsr <- rand_tensor(c(6,7,8))
hosvdD <-hosvd(tnsr)
hosvdD$fnorm_resid
hosvdD2 <-hosvd(tnsr,ranks=c(3,3,4))
hosvdD2$fnorm_resid</pre>
```

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kronecker_list

List Kronecker Product

Description

Returns the Kronecker product from a list of matrices or vectors. Commonly used for n-mode products and various Tensor decompositions.

Usage

```
kronecker_list(L)
```

Arguments

ı

list of matrices or vectors

Value

matrix that is the Kronecker product

Examples

```
smalllizt <- list('mat1' = matrix(runif(12),ncol=4),
'mat2' = matrix(runif(12),ncol=4),
'mat3' = matrix(runif(12),ncol=4))
dim(kronecker_list(smalllizt))</pre>
```

rand_tensor

Tensor with Random Entries

Description

Generate a Tensor with specified modes with iid normal(0,1) entries.

Usage

```
rand_{tensor}(modes = c(3, 4, 5), drop = FALSE)
```

Arguments

modes the modes of the output Tensor

drop whether or not modes equal to 1 should be dropped

Value

a Tensor object with modes given by modes

Note

Default rand_tensor() generates a 3-Tensor with modes c(3,4,5).

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Examples

```
rand_tensor()
rand_tensor(c(4,4,4))
rand_tensor(c(10,2,1),TRUE)
```

sele_rank

Rank selection

Description

Estimate the Tucker rank of coefficient tensor based on BIC criterion. The choice of BIC aims to balance between the goodness-of-fit for the data and the degree of freedom in the population model.

Usage

```
sele_rank(
   tsr,
   X_covar1 = NULL,
   X_covar2 = NULL,
   X_covar3 = NULL,
   rank_range,
   Nsim = 10,
   cons = "non",
   lambda = 0.1,
   alpha = 1,
   solver = "CG",
   dist
)
```

Arguments

tsr	response tensor with 3 modes
X_covar1	covariate on first mode
X_covar2	covariate on second mode
X_covar3	covariate on third mode
rank_range	a matrix containing rank candidates on each row
Nsim	max number of iterations if update does not convergence
cons	the constraint method, "non" for without constraint, "vanilla" for global scale down at each iteration,
	"penalty" for adding log-barrier penalty to object function.
lambda	penalty coefficient for "penalty" constraint
alpha	max norm constraint on linear predictor
solver	solver for solving object function when using "penalty" constraint, see "details"
dist	distribution of response tensor, see "details"

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Details

For rank selection, recommend using non-constraint version.

Constraint penalty adds log-barrier regularizer to general object function (negative log-likelihood). The main function uses solver in function "optim" to solve the objective function. The "solver" passes to the argument "method" in function "optim".

dist specifies three distributions of response tensor: binary, poisson and normal distributions.

Value

a list containing the following:

rank a vector with selected rank with minimal BIC

result a matrix containing rank candidate and its loglikelihood and BIC on each row

Examples

```
seed=24
dist='binary'
data=sim_data(seed, whole_shape = c(20,20,20),
core_shape=c(3,3,3),p=c(5,5,5),dist=dist, dup=5, signal=4)
rank_range = rbind(c(3,3,3),c(3,3,2),c(3,2,2),c(2,2,2),c(3,2,3))
re = sele_rank(data$tsr[[1]],data$X_covar1,data$X_covar2,data$X_covar3,
    rank_range = rank_range,Nsim=10,cons = 'non',dist = dist)
```

sim_data

Simulation of tensor regression models

Description

Generate response tensors with multiple covariates under different simulation models, specifically for tensors with 3 modes

Usage

```
sim_data(
    seed,
    whole_shape = c(20, 20, 20),
    core_shape = c(3, 3, 3),
    p = c(3, 3, 0),
    dist,
    dup,
    signal,
    block = rep(FALSE, 3)
)
```

Arguments

```
seed a random seed for generating data
whole_shape a vector containing dimension of the tensor
core_shape a vector containing Tucker rank of the coefficient tensor
```

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p	a vector containing numbers of covariates on each mode, see "details"
dist	distribution of response tensor, see "details"
dup	number of simulated tensors from the same linear predictor
signal	a scalar controlling the max norm of the linear predictor
block	a vector containing boolean variables, see "details"

Details

By default non-positive entry in p indicates no covariate on the corresponding mode of the tensor. dist specifies three distributions of response tensor: binary, poisson or normal distribution. block specifies whether the coefficient factor matrix is a membership matrix, set to TRUE when

utilizing the stochastic block model

Value

a list containing the following:

tsr a list of simulated tensors, with the number of replicates specified by dup

X_covar1 a matrix, covariate on first mode

X_covar2 a matrix, covariate on second mode

X_covar3 a matrix, covariate on third mode

W a list of orthogonal coefficient matrices - one for each mode, with the number of columns given by core_shape

G an array, core tensor with size specified by core_shape

C_ts an array, coefficient tensor, Tucker product of G,A,B,C

U an array, linear predictor,i.e. Tucker product of C_ts,X_covar1,X_covar2,X_covar3

Examples

```
seed = 34
dist = 'binary'
data=sim_data(seed, whole_shape = c(20,20,20), core_shape=c(3,3,3),
p=c(5,5,5),dist=dist, dup=5, signal=4)
```

Tensor-class

S4 Class for a Tensor

Description

An S4 class for a tensor with arbitrary number of modes. The Tensor class extends the base "array" class to include additional tensor manipulation (folding, unfolding, reshaping, subsetting) as well as a formal class definition that enables more explicit tensor algebra.

Slots

```
num_modes number of modes (integer)modes vector of modes (integer), aka sizes/extents/dimensionsdata actual data of the tensor, which can be 'array' or 'vector'
```

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Note

All of the decompositions and regression models in this package require a Tensor input.

Author(s)

```
James Li <jamesyili@gmail.com>
```

References

James Li, Jacob Bien, Martin T. Wells (2018). rTensor: An R Package for Multidimensional Array (Tensor) Unfolding, Multiplication, and Decomposition. Journal of Statistical Software, Vol. 87, No. 10, 1-31. URL: http://www.jstatsoft.org/v087/i10/.

See Also

```
as.tensor
```

tensor_regress

Generalized Tensor Regression

Description

Tensor-response regression given covariates on multiple modes. Main function in the package. The function takes a response tensor, multiple covariate matrices, and a desired Tucker rank as input. The output is a constrained MLE for the coefficient tensor.

max number of iterations if update does not convergence

Usage

```
tensor_regress(
   tsr,
   X_covar1 = NULL,
   X_covar2 = NULL,
   X_covar3 = NULL,
   core_shape,
   Nsim = 20,
   cons = c("non", "vanilla", "penalty"),
   lambda = 0.1,
   alpha = 1,
   solver = "CG",
   dist = c("binary", "poisson", "normal")
)
```

Arguments

Nsim

tsr response tensor with 3 modes	
X_covar1 covariate on first mode	
X_covar2 covariate on second mode	
X_covar3 covariate on third mode	
core_shape the Tucker rank of the regression coefficien	nts

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cons	the constraint method, "non" for without constraint, "vanilla" for global scale down at each iteration, "penalty" for adding log-barrier penalty to object function
lambda	penalty coefficient for "penalty" constraint
alpha	max norm constraint on linear predictor
solver	solver for solving object function when using "penalty" constraint, see "details"
dist	distribution of the response tensor, see "details"

Details

Constraint penalty adds log-barrier regularizer to general object function (negative log-likelihood). The main function uses solver in function "optim" to solve the objective function. The "solver" passes to the argument "method" in function "optim".

dist specifies three distributions of response tensor: binary, poisson and normal distribution.

Value

a list containing the following:

W a list of orthogonal coefficient matrices - one for each mode, with the number of columns given by core_shape

G an array, core tensor with the size specified by core_shape

C_ts an array, coefficient tensor, Tucker product of G,A,B,C

U linear predictor,i.e. Tucker product of C_ts,X_covar1,X_covar2,X_covar3

1glk a vector containing loglikelihood at convergence

sigma a scalar, estimated error variance (for Gaussian tensor) or dispersion parameter (for Bernoulli and Poisson tensors)

violate a vector listing whether each iteration violates the max norm constraint on the linear predictor, 1 indicates violation

References

"Exponential Tensor Regression with Covariates on Multiple Modes". Under the review of NeurIPS 2020.

```
seed = 34
dist = 'binary'
data=sim_data(seed, whole_shape = c(20,20,20), core_shape=c(3,3,3),
p=c(5,5,5),dist=dist, dup=5, signal=4)
re = tensor_regress(data$tsr[[1]],data$X_covar1,data$X_covar2,data$X_covar3,
core_shape=c(3,3,3),Nsim=10, cons = 'non', dist = dist)
```

ttl 11

ttl Tensor Times List

Description

Contracted (m-Mode) product between a Tensor of arbitrary number of modes and a list of matrices. The result is folded back into Tensor.

Usage

```
ttl(tnsr, list_mat, ms = NULL)
```

Arguments

tnsr Tensor object with K modes

list_mat a list of matrices

ms a vector of modes to contract on (order should match the order of list_mat)

Details

Performs ttm repeated for a single Tensor and a list of matrices on multiple modes. For instance, suppose we want to do multiply a Tensor object tnsr with three matrices mat1, mat2, mat3 on modes 1, 2, and 3. We could do ttm(ttm(ttm(tnsr,mat1,1),mat2,2),3), or we could do ttl(tnsr,list(mat1,mat2,mat3),c(1,2,3)). The order of the matrices in the list should obviously match the order of the modes. This is a common operation for various Tensor decompositions such as CP and Tucker. For the math on the m-Mode Product, see Kolda and Bader (2009).

Value

Tensor object with K modes

Note

The returned Tensor does not drop any modes equal to 1.

References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009, Vol. 51, No. 3 (September 2009), pp. 455-500. URL: https://www.jstor.org/stable/25662308

See Also

ttm

```
tnsr <- new('Tensor',3L,c(3L,4L,5L),data=runif(60))
lizt <- list('mat1' = matrix(runif(30),ncol=3),
'mat2' = matrix(runif(40),ncol=4),
'mat3' = matrix(runif(50),ncol=5))
ttl(tnsr,lizt,ms=c(1,2,3))</pre>
```

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ttm

Tensor Matrix Product (m-Mode Product)

Description

Contracted (m-Mode) product between a Tensor of arbitrary number of modes and a matrix. The result is folded back into Tensor.

Usage

```
ttm(tnsr, mat, m = NULL)
```

Arguments

tnsr Tensor object with K modes

mat input matrix with same number columns as the mth mode of tnsr

m the mode to contract on

Details

By definition, the number of columns in mat must match the mth mode of tnsr. For the math on the m-Mode Product, see Kolda and Bader (2009).

Value

a Tensor object with K modes

Note

The mth mode of tnsr must match the number of columns in mat. By default, the returned Tensor does not drop any modes equal to 1.

References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009, Vol. 51, No. 3 (September 2009), pp. 455-500. URL: https://www.jstor.org/stable/25662308

See Also

ttl

```
tnsr <- new('Tensor',3L,c(3L,4L,5L),data=runif(60))
mat <- matrix(runif(50),ncol=5)
ttm(tnsr,mat,m=3)</pre>
```

tucker 13

tucker	Tucker Decomposition	

Description

The Tucker decomposition of a tensor. Approximates a K-Tensor using a n-mode product of a core tensor (with modes specified by ranks) with orthogonal factor matrices. If there is no truncation in all the modes (i.e. ranks = tnsr@modes), then this is the same as the HOSVD, hosvd. This is an iterative algorithm, with two possible stopping conditions: either relative error in Frobenius norm has gotten below tol, or the max_iter number of iterations has been reached. For more details on the Tucker decomposition, consult Kolda and Bader (2009).

Usage

```
tucker(tnsr, ranks = NULL, max_iter = 25, tol = 1e-05)
```

Arguments

tnsr Tensor with K modes

ranks a vector of the modes of the output core Tensor

max_iter maximum number of iterations if error stays above tol

tol relative Frobenius norm error tolerance

Details

Uses the Alternating Least Squares (ALS) estimation procedure also known as Higher-Order Orthogonal Iteration (HOOI). Intialized using a (Truncated-)HOSVD. A progress bar is included to help monitor operations on large tensors.

Value

a list containing the following:

Z the core tensor, with modes specified by ranks

U a list of orthgonal factor matrices - one for each mode, with the number of columns of the matrices given by ranks

conv whether or not resid < tol by the last iteration

est estimate of ther after compression

norm_percent the percent of Frobenius norm explained by the approximation

fnorm_resid the Frobenius norm of the error fnorm(est-tnsr)

all_resids vector containing the Frobenius norm of error for all the iterations

Note

The length of ranks must match tnsr@num_modes.

References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009, Vol. 51, No. 3 (September 2009), pp. 455-500. URL: https://www.jstor.org/stable/25662308

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See Also

hosvd

Examples

```
tnsr <- rand_tensor(c(4,4,4,4))
tuckerD <- tucker(tnsr,ranks=c(2,2,2,2))
tuckerD$conv
tuckerD$norm_percent
plot(tuckerD$all_resids)</pre>
```

unfold-methods

Tensor Unfolding

Description

Unfolds the tensor into a matrix, with the modes in rs onto the rows and modes in cs onto the columns. Note that c(rs,cs) must have the same elements (order doesn't matter) as x@modes. Within the rows and columns, the order of the unfolding is determined by the order of the modes. This convention is consistent with Kolda and Bader (2009).

Usage

```
unfold(tnsr, row_idx, col_idx)
```

Arguments

tnsr the Tensor instance

row_idx the indices of the modes to map onto the row space col_idx the indices of the modes to map onto the column space

Details

```
unfold(tnsr,row_idx=NULL,col_idx=NULL)
```

Value

```
matrix with prod(row_idx) rows and prod(col_idx) columns
```

References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009, Vol. 51, No. 3 (September 2009), pp. 455-500. URL: https://www.jstor.org/stable/25662308.

```
tnsr <- rand_tensor()
matT3<-unfold(tnsr,row_idx=2,col_idx=c(3,1))</pre>
```

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