

# Graphic Lasso: Why bad estimation?

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- Why the simulation in Matlab, Line 133 gives a bad estimation?

## 1 Possible Reasons

### 1. Threshold for “nonzero”

In the original Matlab code, we use “ $\sim=$ ” to check whether the element is equal to 0 or not, which may be too strict for “nonzero”. Therefore, I use  $1e^{-10}$  as the threshold for “nonzero”, i.e., the element with absolute value smaller than  $1e^{-10}$  is considered as 0.

### 2. Tuning parameter

In the original Matlab code, we use function `GLasso`, which gives the results after BIC selection. However, the BIC criterion may not be good enough in this case. Figures 1, 2, and 3 plot the true  $\Omega$ , and  $\hat{\Omega}$  with BIC criterion and given  $\rho$ .

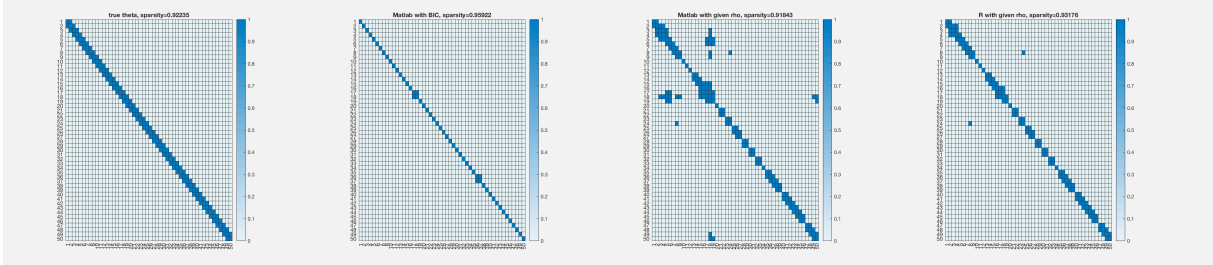


Figure 1: True  $\Omega$  versus  $\hat{\Omega}$  given by (1) Matlab with BIC (2) Matlab with  $\rho = 0.5$ , and (3) R package with  $\rho = 0.5$ . Here  $k = 1$  corresponding to the chain network setting.

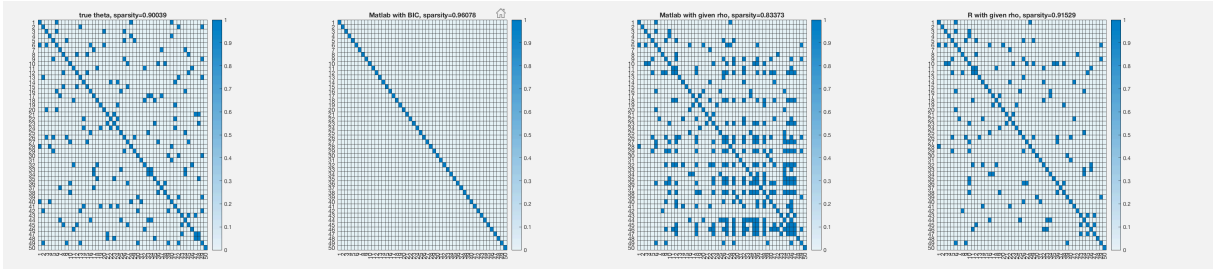


Figure 2: True  $\Omega$  versus  $\hat{\Omega}$  given by (1) Matlab with BIC (2) Matlab with  $\rho = 0.3$ , and (3) R package with  $\rho = 0.3$ . Here  $k = 3$  corresponding to the m-nearest network setting.

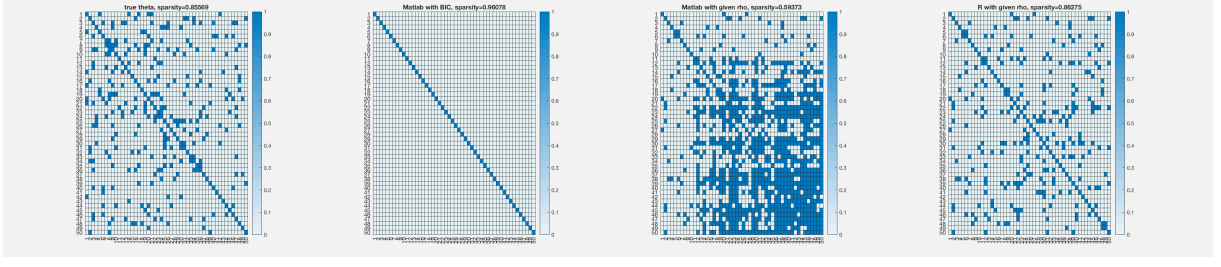


Figure 3: True  $\Omega$  versus  $\hat{\Omega}$  given by (1) Matlab with BIC (2) Matlab with  $\rho = 0.2$ , and (3) R package with  $\rho = 0.2$ . Here  $k = 5$  corresponding to the random network setting.

From these figures, we know that BIC criterion may not be a good way to determine the  $\rho$  in this model. With given specific  $\rho$ , the Matlab and R implementations will give better results.

### 3. Matlab vs R implementation

According to above simulations, we would like to compare the Matlab and R implementation with given tuning parameter  $\rho$  and check which implementation is more sensitive to the parameter. Here we take random network as an example, i.e.,  $k = 5$ . Figures 4, 5, 6, and 7 plot the true  $\Omega$  and  $\hat{\Omega}$  given by Matlab and R with different  $\rho$ .

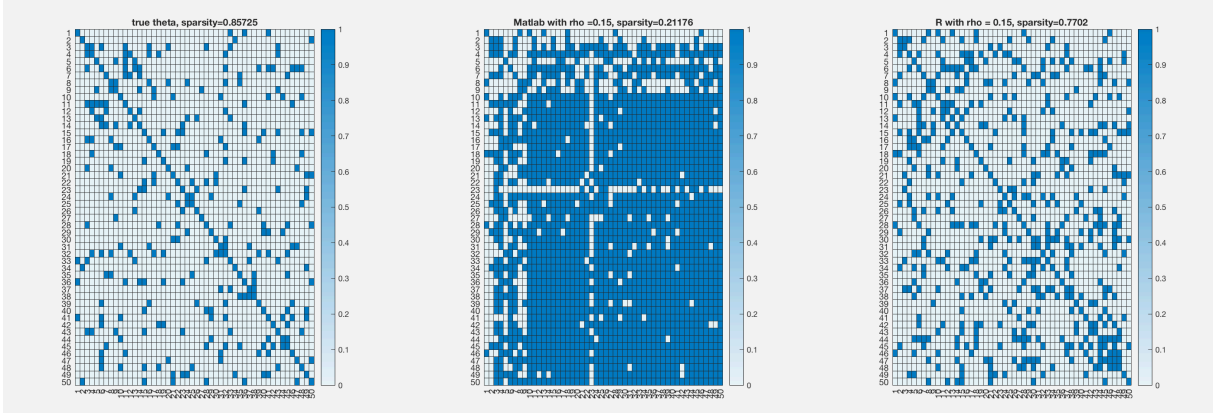


Figure 4: True  $\Omega$  versus  $\hat{\Omega}$  given by Matlab and R package with  $\rho = 0.15$ .

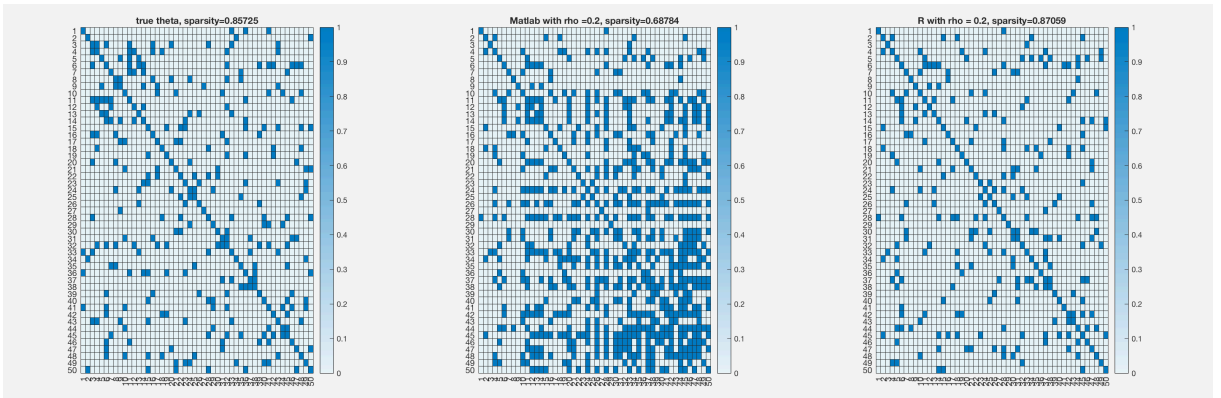


Figure 5: True  $\Omega$  versus  $\hat{\Omega}$  given by Matlab and R package with  $\rho = 0.2$ .

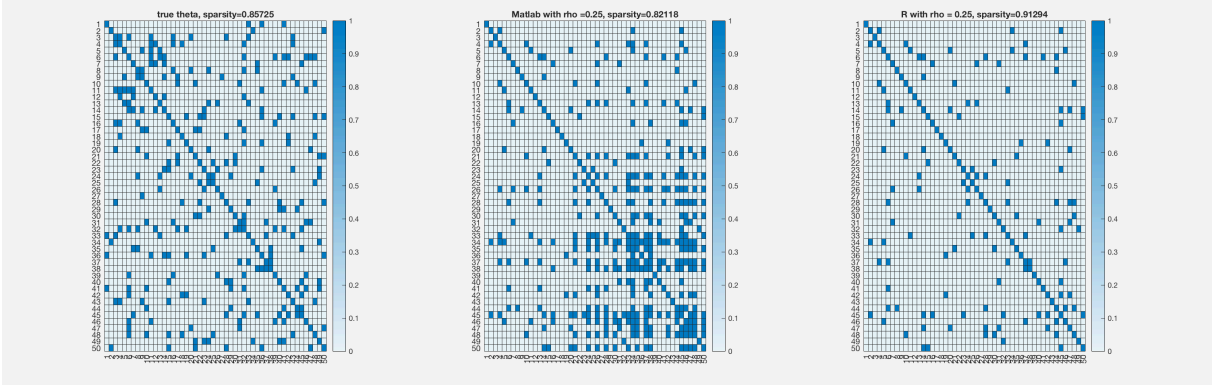


Figure 6: True  $\Omega$  versus  $\hat{\Omega}$  given by Matlab and R package with  $\rho = 0.25$ .

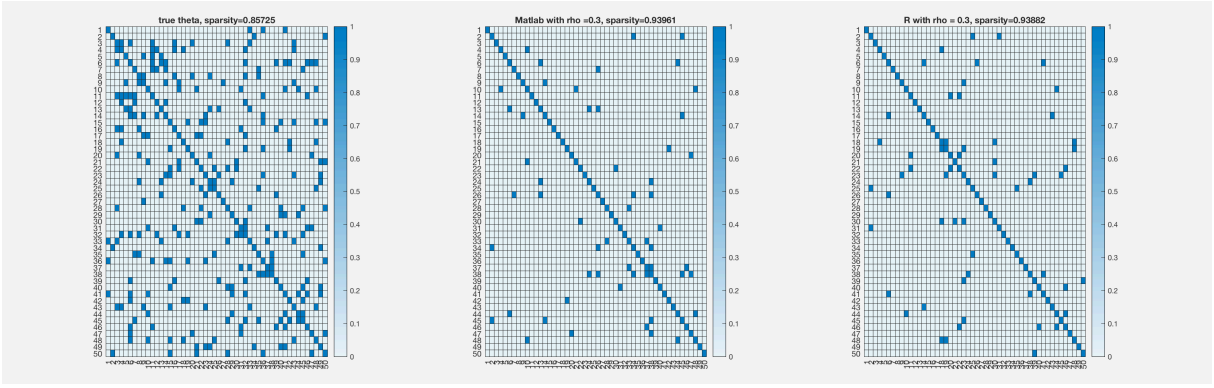


Figure 7: True  $\Omega$  versus  $\hat{\Omega}$  given by Matlab and R package with  $\rho = 0.3$ .

According to the figures, we can see that Matlab code may be more sensitive to the tuning parameter and R implementation gives better estimation with proper  $\rho$ .

**Conclusion:** Based on the mentioned analysis, I believe the method itself works. The threshold for “nonzero”, criterion for tuning parameter selection, and the Matlab implementation affect the performance of estimation. I believe we should use the R package `glasso`.

## 2 Next

Next, I would love to try ROC/AUC criterion for selecting tuning parameter.