

COSC 2P12 Assignment 1

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1.

a) 100100100001110_2 base 2 to base 3

$$100100100001110_2 = (1 \times 2^{14}) + (1 \times 2^{11}) + (0 \times 2^8) + (1 \times 2^3) + (1 \times 2^2) + (1 \times 2^1) \\ = 18702_{10}$$

3	18702		
	6234	r0	LSP
	2078	r0	
	692	r2	
	230	r2	
	76	r2	
	25	r1	
	8	r1	
	2	r2	
	0	r2	MSB

$$\therefore 100100100001110_2 = 22112200_3$$

b) $0xC72_{16}$ to base 2

$$C_{16} + 7_{16} + 2_{16}$$

$$C_{16} = 1100_2$$

$$7_{16} = 0111$$

$$2_{16} = 0010$$

$$\therefore 0xC72_{16} = 1100 \mid 0111 \mid 0010_2$$

C 7 2

2.

a) $145 - 129 = 16$

positive sign

$$\begin{array}{r} 145 \\ - 9871 \\ \hline 10016 \end{array}$$

$$\begin{array}{r} 9999 \\ - 129 \\ \hline 9870 \\ + 1 \\ \hline 9871 \end{array}$$

$$6) 129 - 145 = -16$$

Negative sign

$$\begin{array}{r} 0129 \\ + 9855 \\ \hline 9984 \end{array}$$

$$\begin{array}{r} 9999 \\ - 9989 \\ \hline 0010 \\ + 1 \\ \hline 0011 \end{array}$$

$$\begin{array}{r} 9999 \\ - 145 \\ \hline 9854 \\ + 1 \\ \hline 9855 \end{array}$$

3.

$$a) \begin{array}{r} 000111 \\ + 7 \\ \hline \end{array} - \begin{array}{r} 001100 \\ + 12 \\ \hline \end{array} = 00101 \quad \begin{array}{l} \text{must find 2's} \\ \text{complement of } -12 \end{array}$$

$$\begin{array}{r} 001100 \\ 110011 \\ \hline + 1 \\ \hline 110100 = -12 \end{array}$$

$$\begin{array}{r} 000111 \\ + 110100 \\ \hline 111011 \rightarrow \# \text{ is in 2's complement form} \end{array}$$

$$\begin{array}{r} 111011 \\ 000100 \\ \hline + 1 \\ \hline 000101 = -5 \end{array}$$

$$b) \begin{array}{r} 000111 \\ + 7 \\ \hline \end{array} - \begin{array}{r} 101011 \\ - 20 \\ \hline \end{array} = 011011$$

$$\begin{array}{r} 000111 \\ + 010100 \\ \hline 011011 \end{array}$$

$$\begin{array}{l} 010100 = 20 \\ 101011 = -\# \\ \therefore 101011 = -20 \end{array}$$

4.

$$a) AC + C(A' + AB)$$

$$= AC + C(A' + B)$$

$$= AC + A'C + BC$$

$$= C(A + A') + BC$$

$$= C(1) + BC$$

$$= C + BC$$

$$= C$$

Absorption Law #11 on slides

Distribution Law #12 on slides

Distributive Law in reverse #12 on slides

Complement Law #6 on slides

Identity Law #4 on slides

Absorption Law #11 on slides

$$\begin{aligned}
 & b) (A+B)'(C+D+E)' + (A+B)' \\
 & = A'B'(C+D+E)' + (A+B)' \quad \text{Demorgan's Law} \\
 & = A'B'C'D'E' + (A+B)' \quad \text{Demorgan's Law} \\
 & = A'B'C'D'E' + A'B' \quad \text{Demorgan's Law} \\
 & = A'B' \quad \text{Absorption Law \#10 on slides}
 \end{aligned}$$

5. On logic circuit

6.

a)

D	C	B	A	a	b	c	d	e	f	g
0	0	0	0	1	0	1	0	1	1	1
0	0	0	1	1	1	1	0	0	1	0
0	0	1	0	1	0	0	1	0	0	1
0	0	1	1	0	1	1	0	1	1	0
0	1	0	0	0	0	1	1	1	1	1
0	1	0	1	1	1	0	0	1	1	0
0	1	1	0	0	0	0	0	0	0	0
0	1	1	1	0	0	1	1	1	0	1
1	0	0	0	1	1	0	0	0	1	1
1	0	0	1	1	1	1	1	0	1	1
1	0	1	0	1	1	1	1	1	0	0
1	0	1	1	X	X	X	X	X	X	X
1	1	0	0	X	X	X	X	X	X	X
1	1	0	1	X	X	X	X	X	X	X
1	1	1	0	X	X	X	X	X	X	X
1	1	1	1	X	X	X	X	X	X	X

* checks were placed to help with K-Map drawing (disregard them)

b)

	a K-Map			
	A'B'	AB	AB	AB'
C'D'	1	1	0	1
C'D	1	1	X	1
CD	X	X	X	X
CD'	0	0	0	1

$$AB' + A'C'$$

b K-Map

	$A'B'$	$A'B$	AB	AB'
$C'D'$	0	0	1	1
$C'D$	1	1	x	1
CD	x	x	x	x
CD'	0	0	0	1

$$AB' + AC' + D$$

c K-Map

	$A'B'$	$A'B$	AB	AB'
$C'D'$	1	0	1	1
$C'D$	0	1	x	1
CD	x	x	x	x
CD'	1	0	1	0

$$B'C'D' + A'B'C + AB + AC' + BD$$

d K-Map

	$A'B'$	$A'B$	AB	AB'
$C'D'$	0	1	0	0
$C'D$	0	1	x	1
CD	x	x	x	x
CD'	1	0	1	0

$$A'BC' + A'B'C + ABC + AD$$

e K-Map

	$A'B'$	$A'B$	AB	AB'
$C'D'$	1	0	1	0
$C'D$	0	1	x	0
CD	x	x	x	x
CD'	1	0	1	1

$$A'B'D' + AB + BD + AC$$

F	K-Map				
	$A'B'$	$A'B$	AB	AB'	
$C'D'$	1	0	1	1	$AC' + B'$
$C'D$	1	0	X	1	
CD	X	X	X	X	
CD'	1	0	0	1	

g	K-Map				
	$A'B'$	$A'B$	AB	AB'	
$C'D'$	1	1	0	0	$A'C'D' + ABC + A'B' + AD$
$C'D$	1	0	X	1	
CD	X	X	X	X	
CD'	1	0	1	0	

c) On logic circuit