

CARTNot only Classification and Regression Trees

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Introduction



Talk goals

- How decision trees work
- Common problems and advantages
- What they can be used for

Focus on classification





About me

- @datapythonista http://datapythonista.github.io/
- Python user since 2006
- Active Django developer, 2007 2012
 - GSoC 2009: Django localization
- Master in Artificial Intelligence, 2012
- Master in Finance 2014
- Currently working at Bank of America Merrill Lynch in London
- Owner of Quantitative Mining
 - Machine learning applied to digital marketing



Warm up example



Example: The geek party

- We want to **predict attendance** to the geek party
- We know for each possible attendee:
 - Their age
 - The distance from their home to the event location





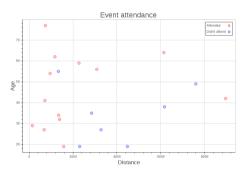
Let's get some data first...

		age	distance	attended
•	0	38	6169.98	False
	1	49	7598.87	False
import pandas as pd	2	27	3276.07	False
data = {'age': [38, 49, 27, 19, 54, 29, 19, 42, 34, 64, 19, 62, 27, 77, 55, 41, 56, 32, 59, 35],	3	19	1570.43	True
'distance': [6169.98, 7598.87, 3276.07, 1570.43, 951.76,	4	54	951.76	True
139.97, 4476.89, 8958.77, 1336.44, 6138.85, 2298.68, 1167.92, 676.30, 736.85, 1326.52,	5	29	139.97	True
712.13, 3083.07, 1382.64, 2267.55, 2844.18], 'attended': [False, False, False, True, True, True, False,	6	19	4476.89	False
True, True, True, False, True, True, True,	7	42	8958.77	True
False, True, True, True, False]}	8	34	1336.44	True
df = pd.DataFrame(data)	9	64	6138.85	True
	10	19	2298.68	False
	11	62	1167.92	True



...and visualize it

```
from bokeh.plotting import figure, show
p = figure(title = 'Event attendance')
p.xaxis.axis_label = 'Distance'
p.vaxis.axis label = 'Age'
p.circle(df[df.attended]['distance'],
         df[df.attended]['age'].
         color='red'.
         legend='Attended',
         fill_alpha=0.2,
         size=10)
p.circle(df[~df.attended]['distance'],
         df[~df.attended]['age'],
         color='blue'.
         legend="Didn't attend".
         fill alpha=0.2,
         size=10)
show(p)
```

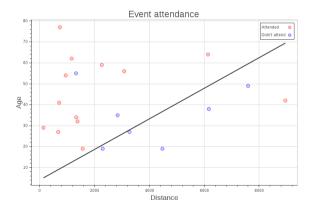




Using a linear model



Linear model





How is the model?

$$\theta_{intercept} + \theta_{age} \cdot age + \theta_{distance} \cdot distance >= 0$$
 (1)



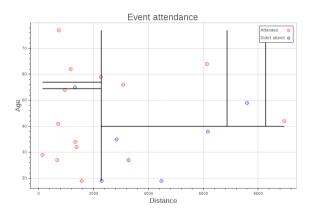
Using a decision tree

```
from sklearn.tree import DecisionTreeClassifier

dtree = DecisionTreeClassifier()
dtree.fit(df[['age', 'distance']], df['attended'])
cart_plot(dtree)
```



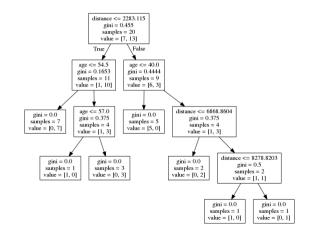
Decision tree





How is the model?

```
def decision tree model (age, distance):
    if distance >= 2283.11:
        if age >= 40.00:
            if distance >= 6868.86:
                if distance >= 8278.82:
                     return True
                else.
                     return False
            else.
                return True
        else:
            return False
    else:
        if age >= 54.50:
            if age >= 57.00:
                return True
            else:
                return False
        else:
            return True
```



Properties



Overfitting

- Decision trees LOVE to overfit
- But it's easy to make them generalize with their parameters:
 - min samples leaf
 - min_samples_split
 - max depth
 - max leaf nodes



Standardization / Normalization

- Not required
- Using original units we will be able to understand the tree better



Feature selection

- We get feature selection for free
- If a feature is not relevant, it is not used in the tree
- sklearn: Gives you the feature importances:

```
>>> list(zip(['age', 'distance'],
... dtree.feature_importances_))
[('age', 0.5844155844155845), ('distance', 0.41558441558441556)]
```



Feature extraction and data cleaning

- We need to take care of it
- Most of the times, we can improve more the results by better data, than by better models



Categorical variables and missing values

- Decision trees can deal with them
- But this depends on the implementation, sklearn uses float without missing values



Binning

- Very useful for decision trees
- Two types:
 - Unify values. e.g. 20, 20, 30, 30, 30, 40, 50, 50
 - Binary variables. e.g. lives_in_the_city (yes/no)
- We can add domain knowledge to the classifier
- Avoid Highly-branching attributes bias
- Where to cut cyclic variables? e.g. hour of the day





Unbalanced data

- According to the literature, decision tree is biased towards the dominant class
- In my experience, it behaves much better than linear models without changes
- But classical techniques like weighting can be applied

Training





Basic algorithm

```
def train_decision_tree(x, y):
    feature, value = get_best_split(x, y)

    x_left, y_left = x[x[feature] < value], y[x[feature] < value]
    if len(y_left.unique()) > 1:
        left_node = train_decision_tree(x_left, y_left)
    else:
        left_node = None

    x_right, y_right = x[x[feature] >= value], y[x[feature] >= value]
    if len(y_right.unique()) > 1:
        right_node = train_decision_tree(x_right, y_right)
    else:
        right_node = None

return Node(feature, value, left_node, right_node)
```



Training

Splitting

Candidate split 1	age	18	19	21	27	29	34	38	42	49	54	62	64
	attended	F	F	Т	F	Т	Т	F	Т	F	Т	Т	Т

Split True False
Left 0 1
Right 7 4

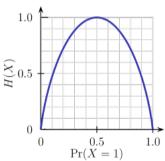
Split	True	False
Left	0	2
Right	7	3



Entropy

For a given subset¹:

$$entropy = -Pr_{attending} \cdot \log_2 Pr_{attending} - Pr_{\neg attending} \cdot \log_2 Pr_{\neg attending}$$
 (2)



¹Note that pure splits have an entropy of $0 \cdot \infty = 0$

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Information gain

For a given **split**:

$$information_gain = entropy_{parent} - \left(\frac{items_{left}}{items_{total}} \cdot entropy_{left} + \frac{items_{right}}{items_{total}} \cdot entropy_{right}\right) \quad (3)$$





Best split algorithm

```
def get best split(x, v):
    best split = None
    best entropy = 1.
    for feature in x.columns.values:
        column = x[feature]
        for value in column.iterrows():
            a = y[column < value] == class_a_value
            b = v[column < value] == class b value
            left weight = (a + b) / len(v.index)
            left entropy = entropy(a, b)
            a = y[column >= value] == class_a_value
            b = v[column >= value] == class b value
            right items = (a + b) / len(v.index)
            right entropy = entropy (a, b)
            split entropy = left weight * left etropy +
     right_weight * right_entropy
            if split entropy < best entropy:
                best_split = (feature, value)
                best entropy = split entropy
    return best_split
```

Uses





Other uses

- Exploratory analysis
 - Visualize your model to see if it makes sense
 - Detect problems in your data
- Probability estimation
 - Uses frequencies
 - Linear models use distance to the decision boundary, which IMHO is a worse heuristic
- Regression
 - Simple method: Constant value for each split
 - Advanced methods: Linear regression (or other) for each split

Appendix





Tree to nodes





Cart plot (I)

```
from collections import namedtuple, deque
from functools import partial
class NodeRanges(namedtuple('NodeRanges', 'node, max_x, min_x, max_y, min_y')):
    pass
def cart plot(nodes):
    nodes = tree to nodes(dtree)
    plot = base_plot()
    add_line = partial(plot.line, line_color='black', line_width=2)
    stack = deque()
    stack.append(NodeRanges(node=nodes[0],
                            max_x=df['distance'].max(),
                            min x=df['distance'].min(),
                            max_y=df['age'].max(),
                            min_y=df['age'].min()))
# (continues)
```



Cart plot (II)

```
while len(stack):
    node, max x, min_x, max_y, min_y = stack.pop()
    feature, threshold, left, right = node
    if feature == 'distance' .
        add_line(x=[threshold, threshold], y=[min_y, max_y])
    elif feature == 'age':
        add line(x=[min x, max x], v=[threshold, threshold])
    else:
        continue
    stack.append(NodeRanges(node=nodes[left].
                            max x=threshold if feature == 'distance' else max x.
                            min x=min x.
                            max_y=threshold if feature == 'age' else max_y,
                            min v=min v))
    stack.append(NodeRanges(node=nodes[right],
                            max_x=max_x
                            min_x=threshold if feature == 'distance' else min_x,
                            max_v=max_v,
                            min_y=threshold if feature == 'age' else min_y))
```

show(plot)