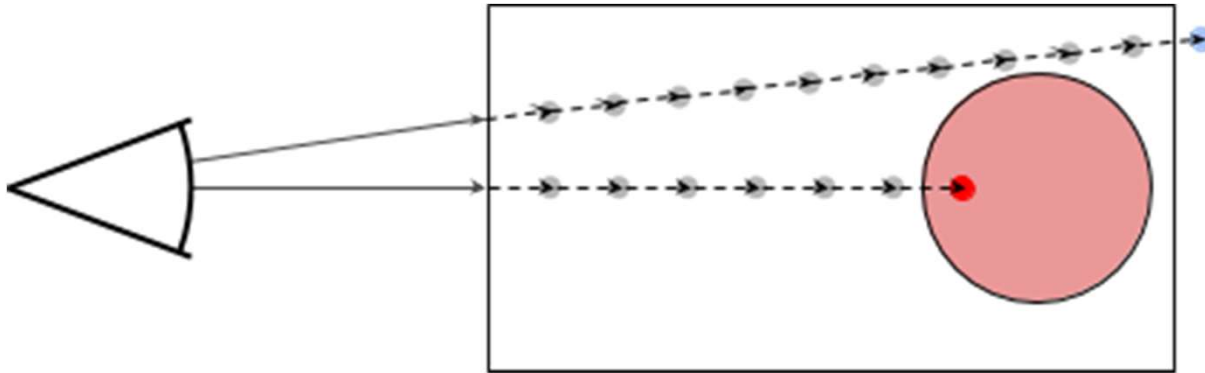# Raymarching

Raymarching

- Step along a ray until hit or max distance

Height Field

- Surfaces that can be described by a function $y = f(x, z)$
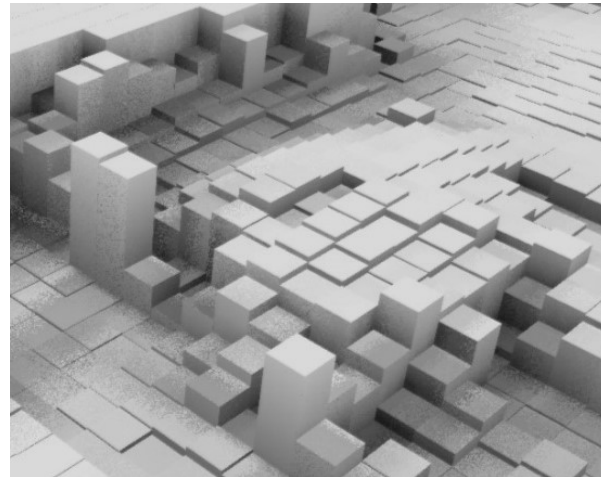- Examples: terrain, measurements sampled on a plane, 2D scalar field

1	2	1	2	2	1
2	1	2	1	10	1
3	1	2	6	9	0
4	1	2	5	0	0
5	1	2	3	0	0
6	1	2	2	1	0

Height Field

- Grid that stores a height at each position

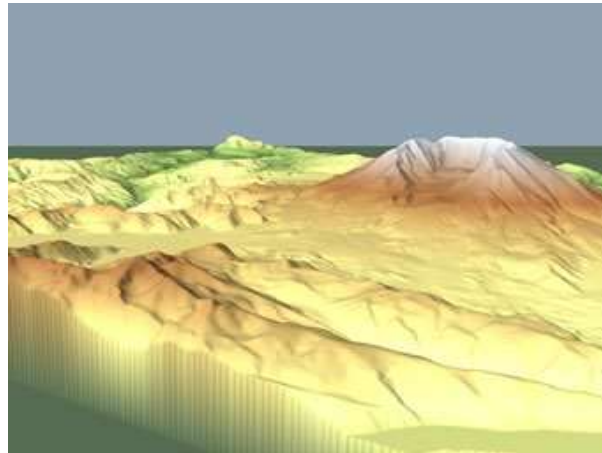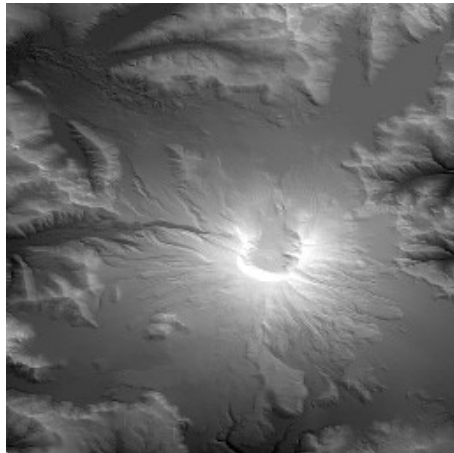| 1	2	1	2	2	1
2	1	2	1	10	1
3	1	2	6	9	0
4	1	2	5	0	0
5	1	2	3	0	0
6	1	2	2	1	0

Height Field

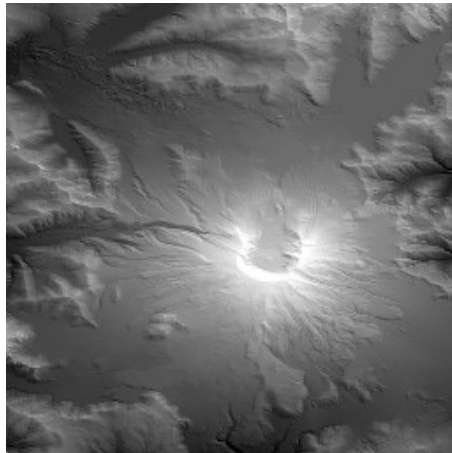- Can use mathematical function to create grid values
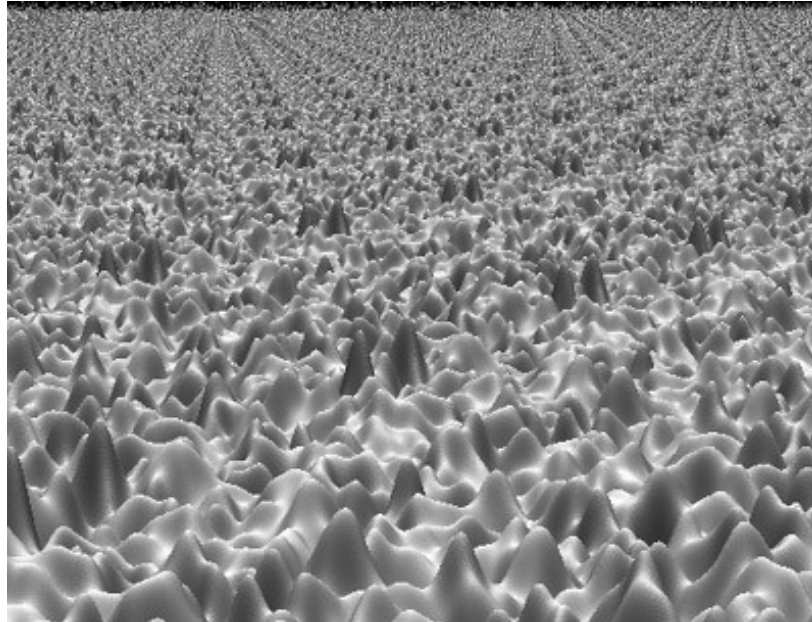
Height Field
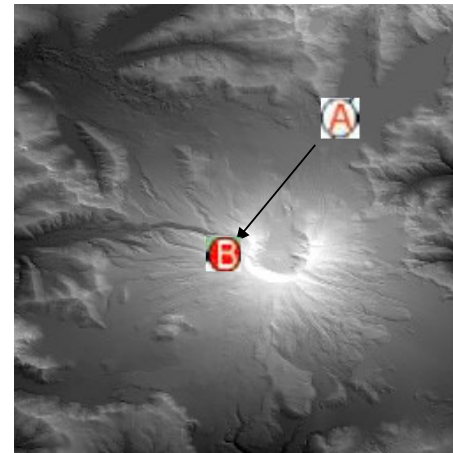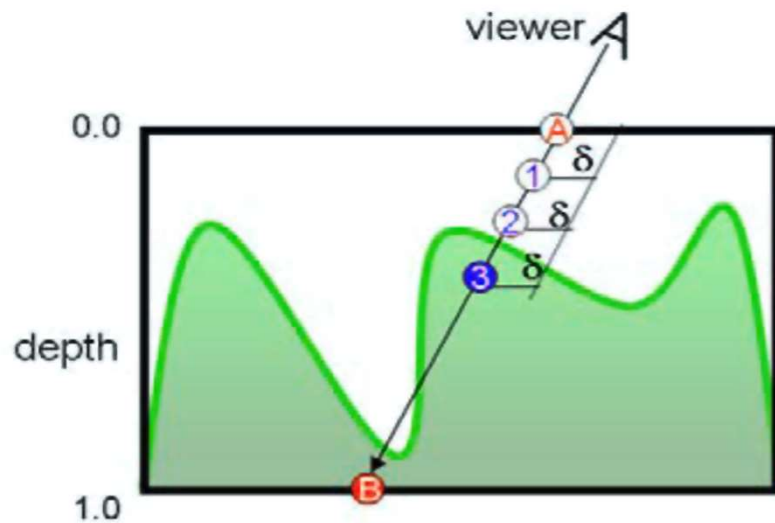
- Can use texture to store grid

Height Field

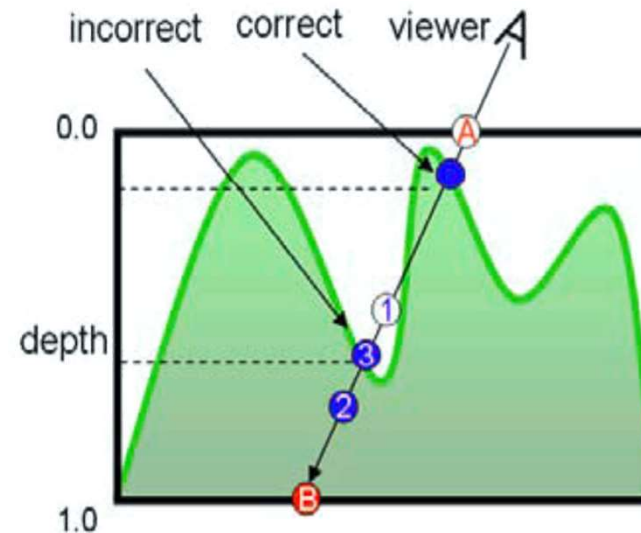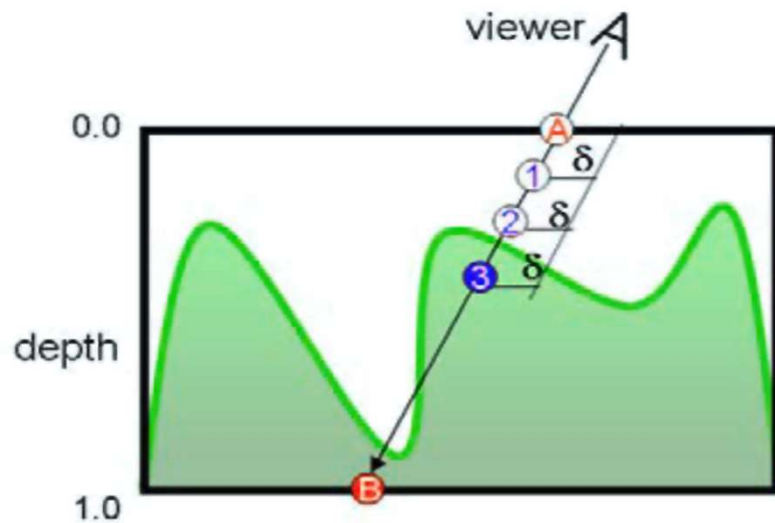- Can render with different methods

Raymarching Height Field
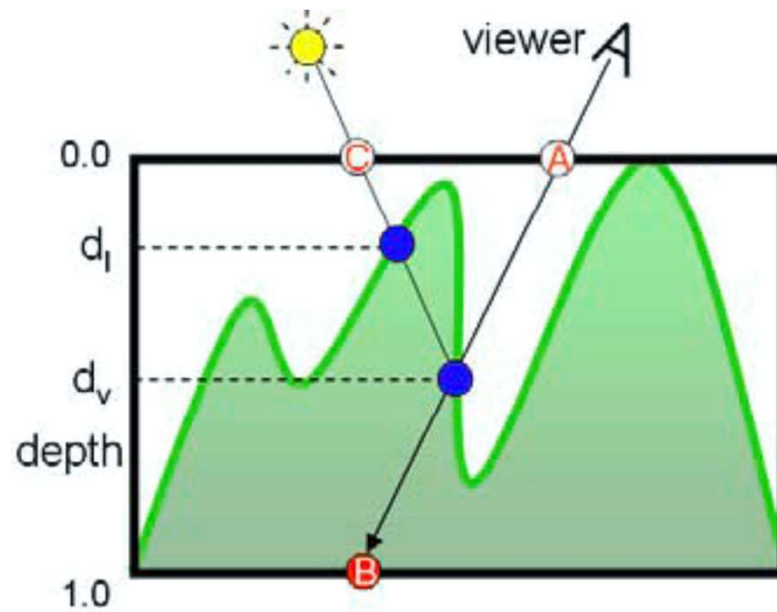
- Step with small increments along ray

Raymarching Height Field

- Step with small increments along ray
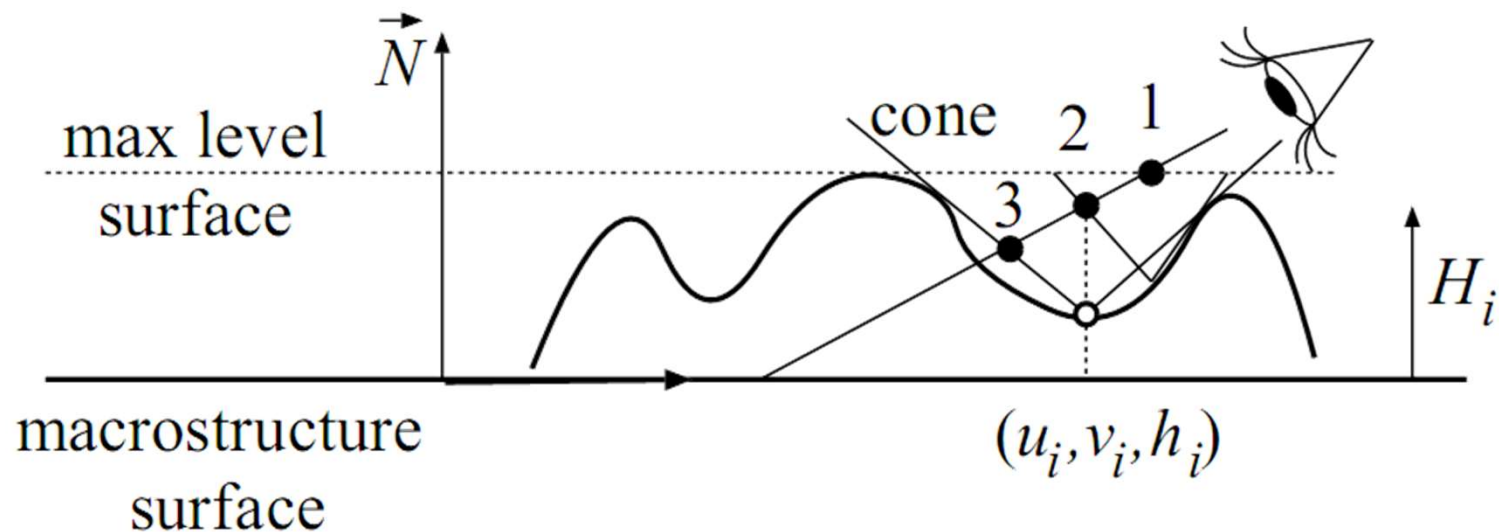
- Interval bisection

Shadowing

- Send shadow feeler ray

Accelerating Height Field Rendering

- Help texture
  - Each texel stores cone of empty space above
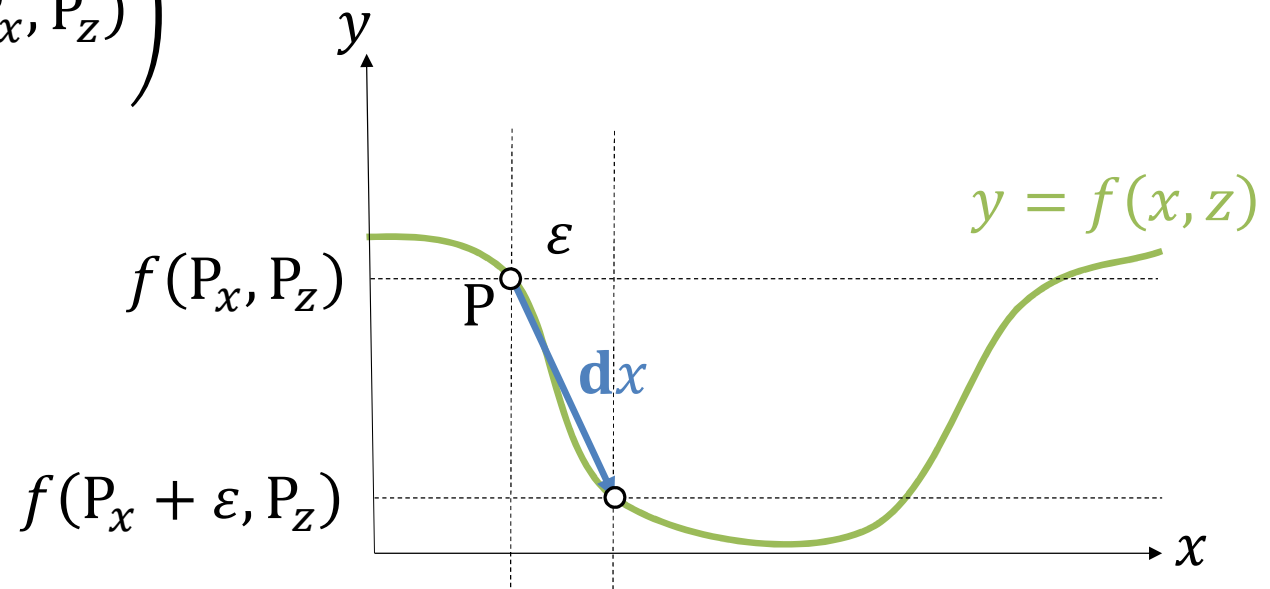 - Only store opening angle (1 additional value per texel)

Height Field Normals

Calculating Height Field Normals

- $\mathbf{d}x = \begin{pmatrix} \varepsilon \\ f(\mathrm{P}_x + \varepsilon, \mathrm{P}_z) - f(\mathrm{P}_x, \mathrm{P}_z) \\ 0 \end{pmatrix}$
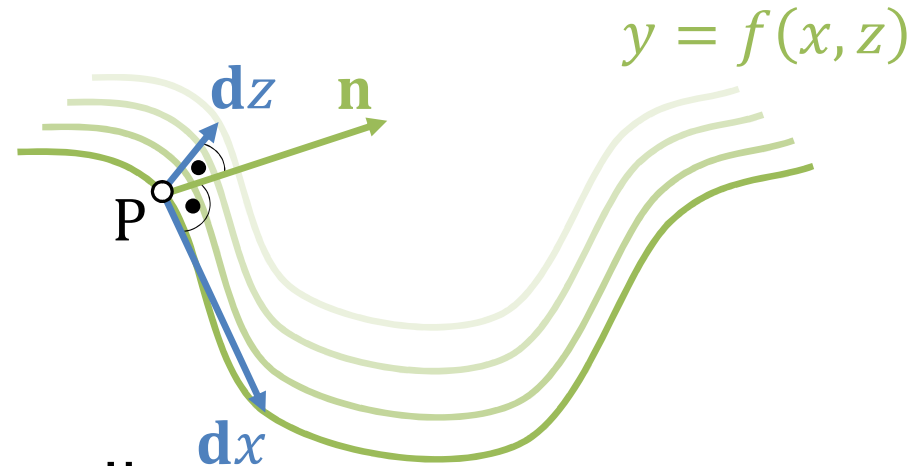
Calculating Height Field Normals

- $\mathbf{d}z = \begin{pmatrix} 0 \\ \dfrac{f(P_x, P_z + \varepsilon) - f(P_x, P_z)}{\varepsilon} \end{pmatrix}$
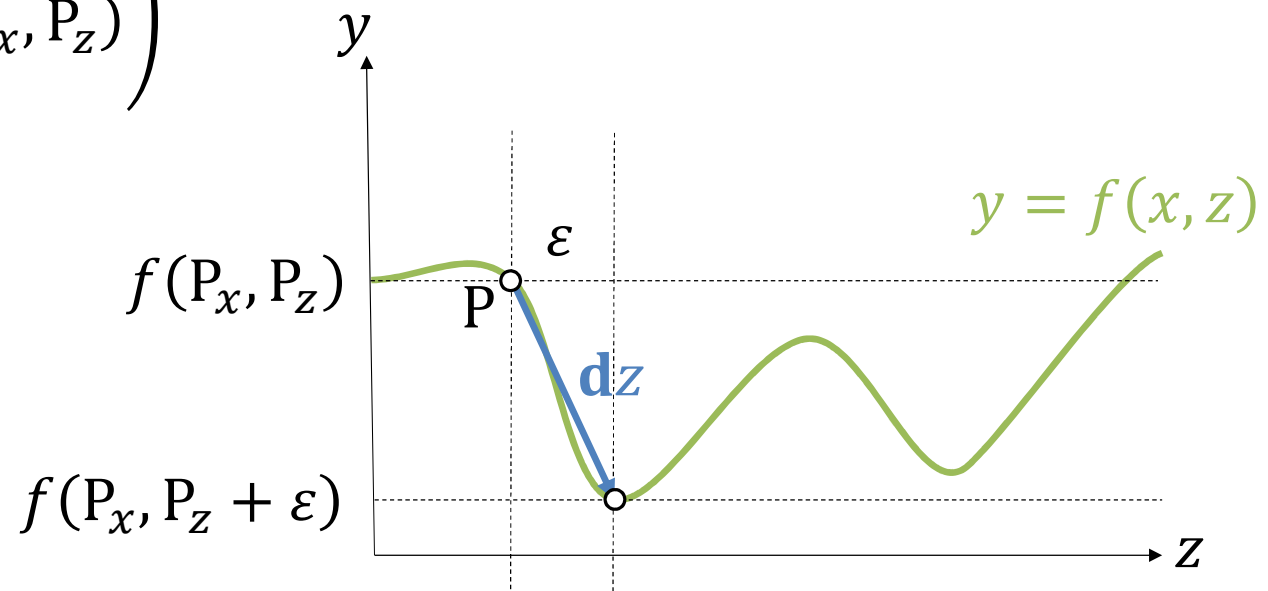
Calculating Height Field Normals

- $\mathbf{d}x = \begin{pmatrix} \varepsilon \\ f(\mathrm{P}_x + \varepsilon, \mathrm{P}_z) - f(\mathrm{P}_x, \mathrm{P}_z) \\ 0 \end{pmatrix}$

- $\mathbf{d}z = \begin{pmatrix} 0 \\ f(\mathrm{P}_x, \mathrm{P}_z + \varepsilon) - f(\mathrm{P}_x, \mathrm{P}_z) \\ \varepsilon \end{pmatrix}$

$y = f(x, z)$

- $\mathbf{n} = \|\mathbf{d}z \times \mathbf{d}x\| = \left\| \begin{matrix} f(\mathrm{P}_x, \mathrm{P}_z) - f(\mathrm{P}_x + \varepsilon, \mathrm{P}_z) \\ \varepsilon \\ f(\mathrm{P}_x, \mathrm{P}_z) - f(\mathrm{P}_x, \mathrm{P}_z + \varepsilon) \end{matrix} \right\|$
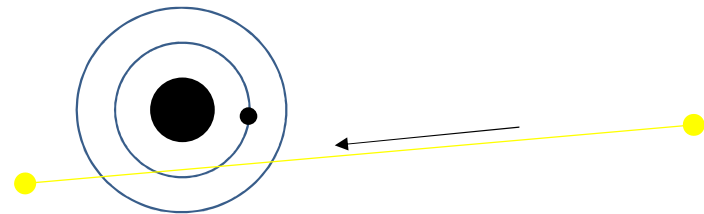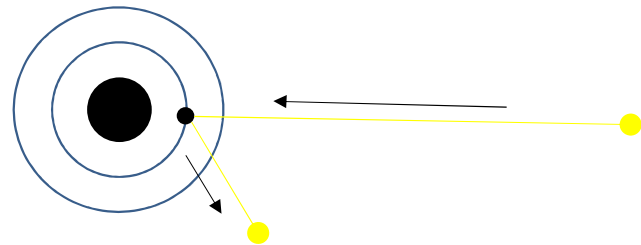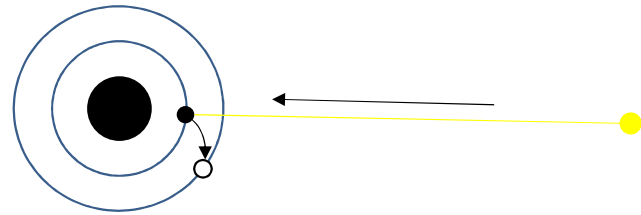
Volume Rendering

Horizon: Zero Dawn, Guerrilla Games

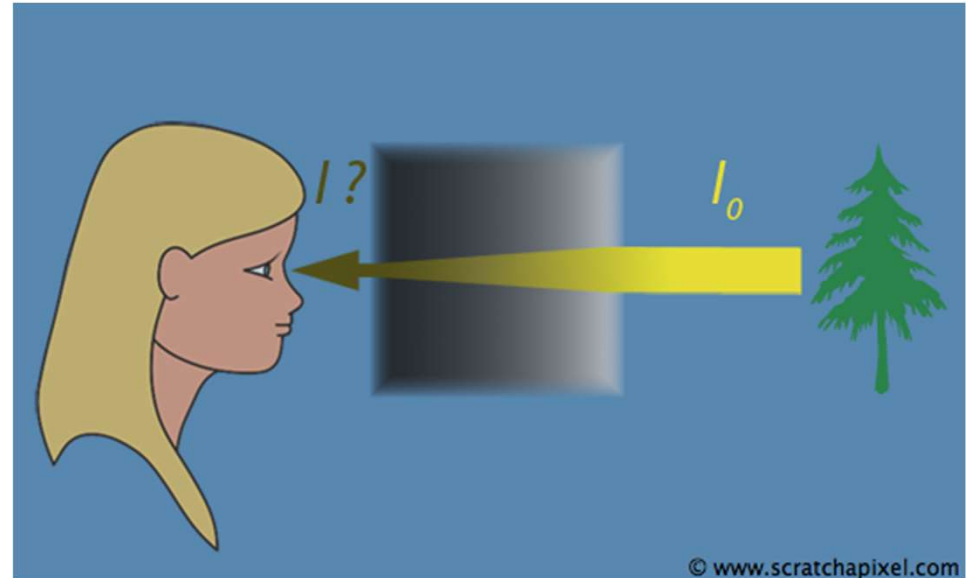# What's Happening to Light Hitting a Particle ?

- Absorption

- Scattering into a random direction

- Passing through

Volume Rendering – Transmittance

- Light is attenuated as it travels through a medium

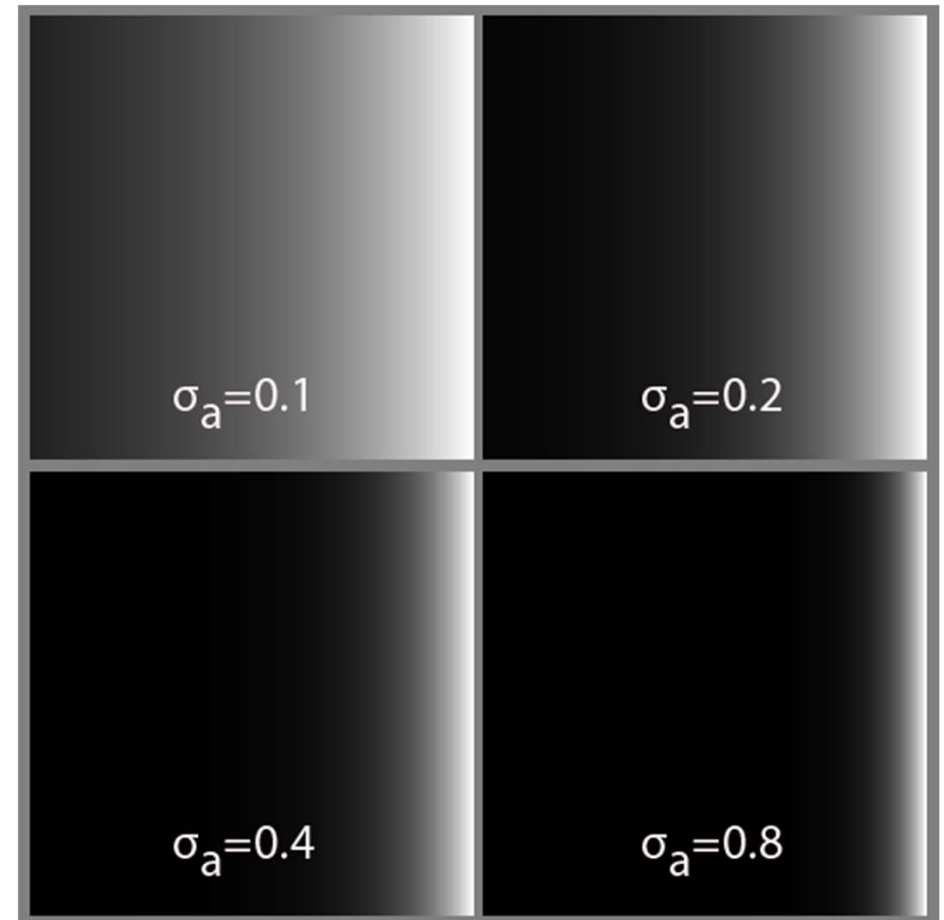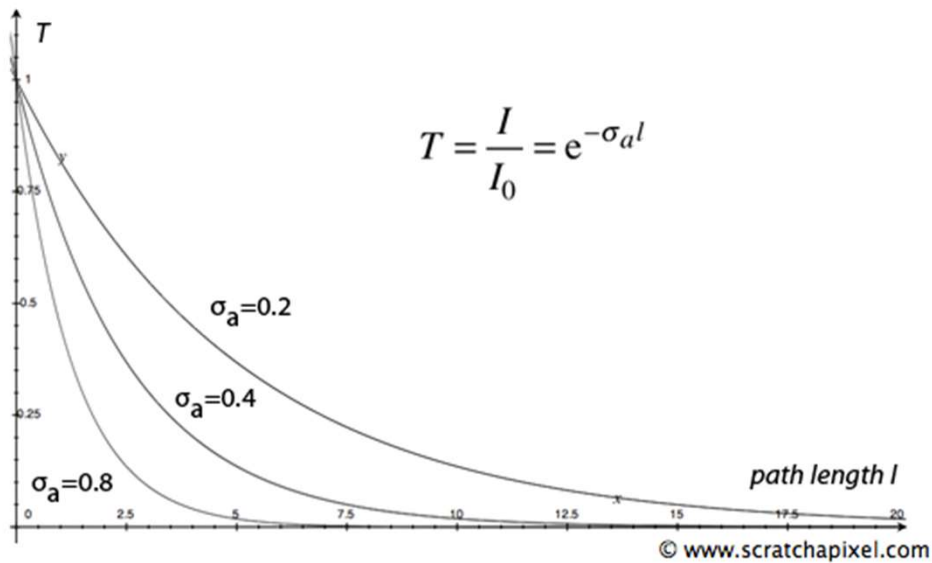- **Transmittance** is the ratio between light received and the incident light

$$T = \frac{I}{I_0}$$

Lambert-Beer's law – Absorption

- Light attenuation due to **absorption**

$$T = e^{-\sigma_a l}$$

$$T = \frac{I}{I_0} = e^{-\sigma_a l}$$

$\sigma_a=0.2$

$\sigma_a=0.4$

$\sigma_a=0.8$

path length *l*

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$\sigma_a=0.1$ $\sigma_a=0.2$

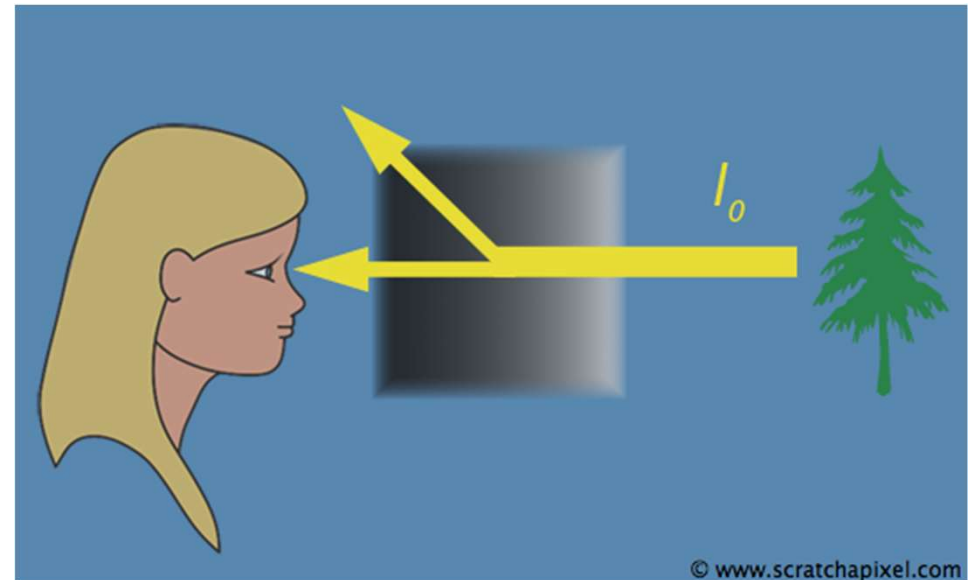$\sigma_a=0.4$ $\sigma_a=0.8$

Lambert-Beer's law – Absorption + Scattering

- Light attenuation due to **absorption** and **out-scattering**
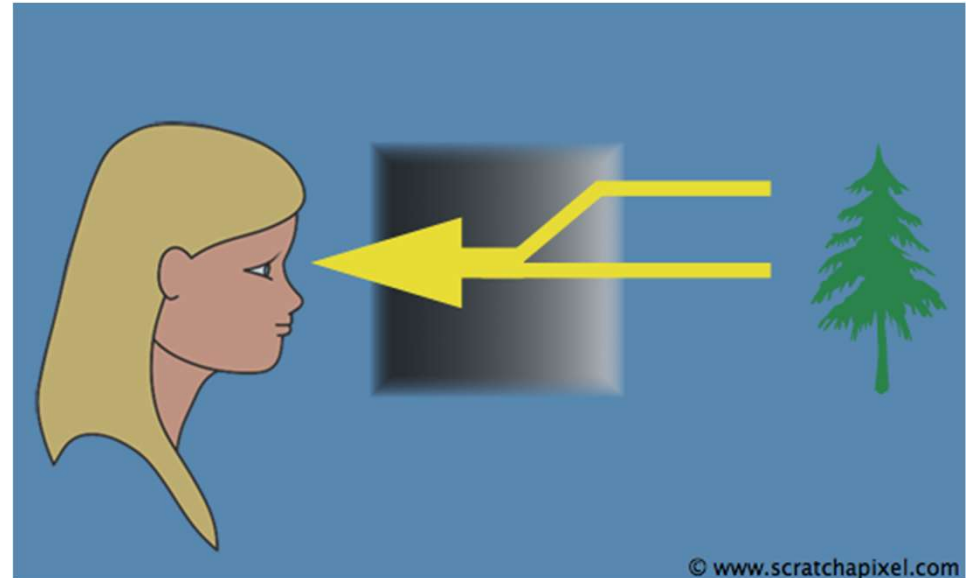
$$T = e^{-(\sigma_a + \sigma_s)l} = e^{-\sigma_t l}$$

- σ_t is also known as **extinction** or **attenuation** coefficient
- For solids $\sigma_t = \infty$

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In-Scattering

- Photons from other light paths join the light path that carries photons to the eye.

Light Travelling Through a Media