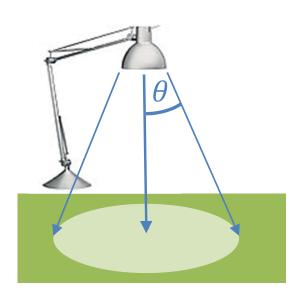
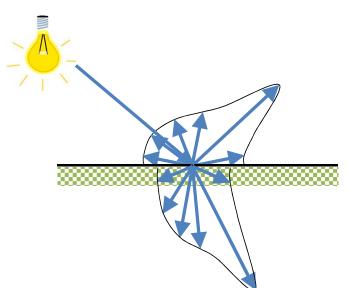
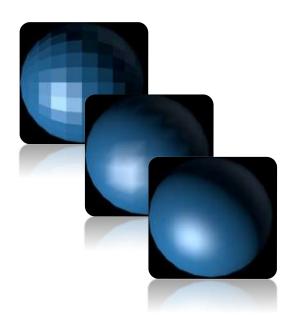


**Light Sources** 

Reflection Models Shading Models

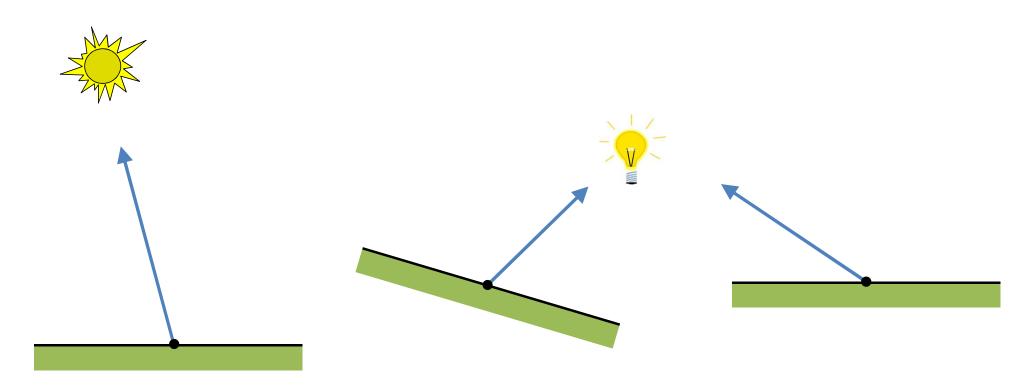






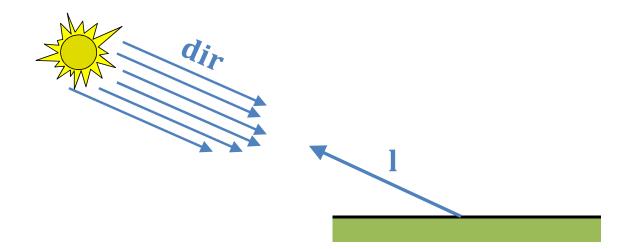
# **Light Sources**

Where is the light coming from?



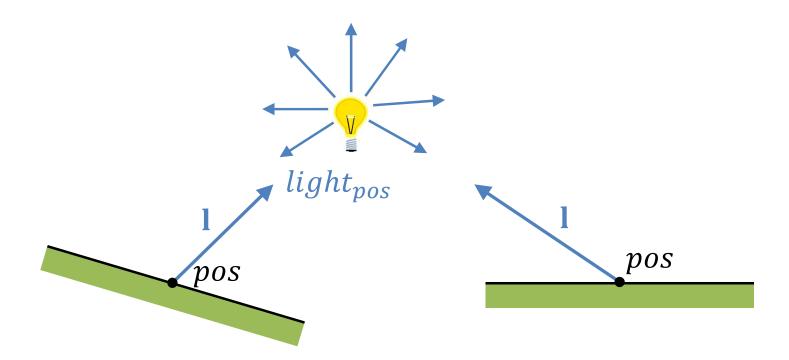
### **Directional Light**

- Light source is infinitely far away
- Light rays are parallel, like sun
- 1 ... direction to the light = -dir



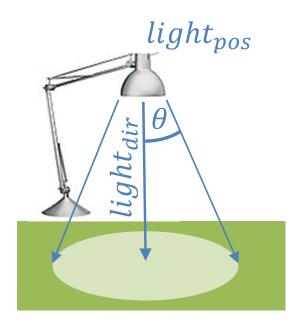
### **Point Light**

• Has a certain position in space  $l = normalize(light_{pos} - pos)$ 



### **Spot Light**

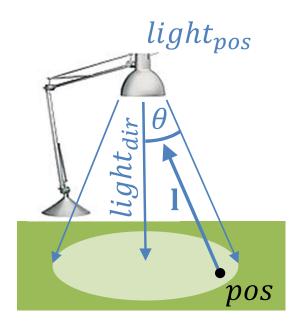
- Has a certain position and cone in space
- Cone can be specified by opening angle and central direction



# **Spot Light**

Point is in cone iff

$$\cos^{-1} dot(l, -light_{dir}) < \theta$$

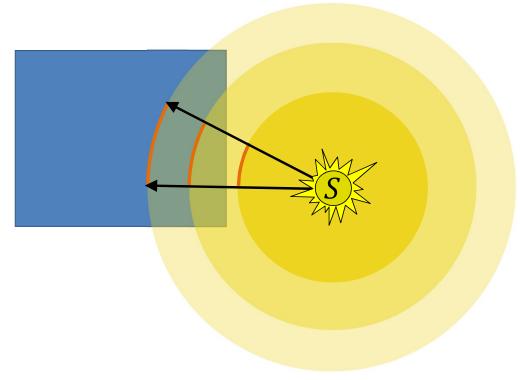


### **Point Light Attenuation**

- Point light energy emitted is distributed across surface of a sphere
- Further object receive less energy per surface area

$$S = \frac{S_{intensity} * S_{color}}{4\pi r^2}$$

Inverse-square law



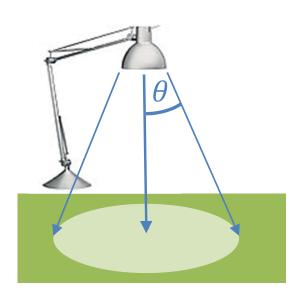
# **Multiple Light Sources**

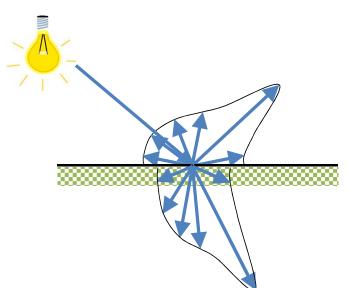
- Have a linear light response
- $Total\ light = \sum Light_i$

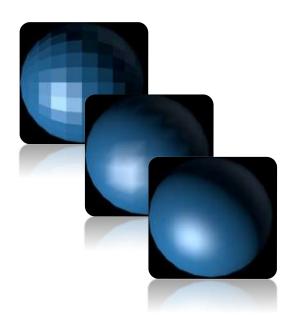


**Light Sources** 

Reflection Models Shading Models





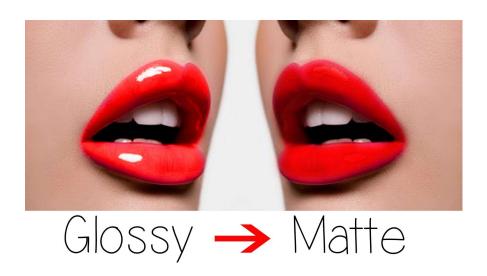


# **Light-Material Interaction**



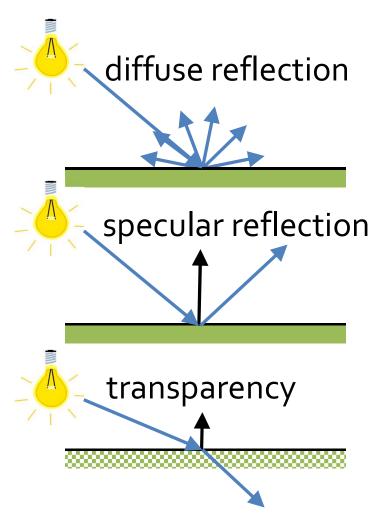
### Reflection/Illumination/Lighting model

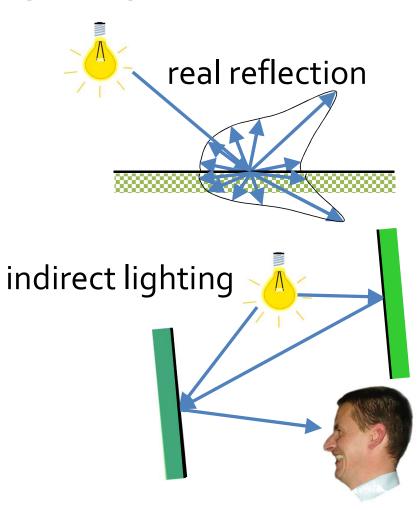
- How is light reflected by a surface?
- What is the resulting color?
- What properties can we simulate with a given model?
- What lighting effects can we create?



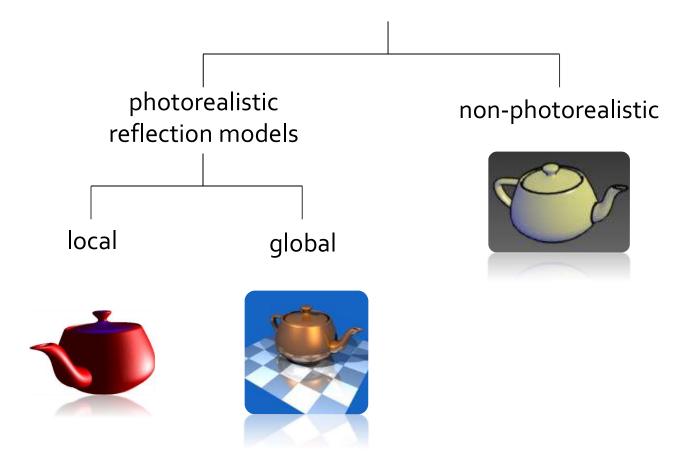


### Surface lighting effects

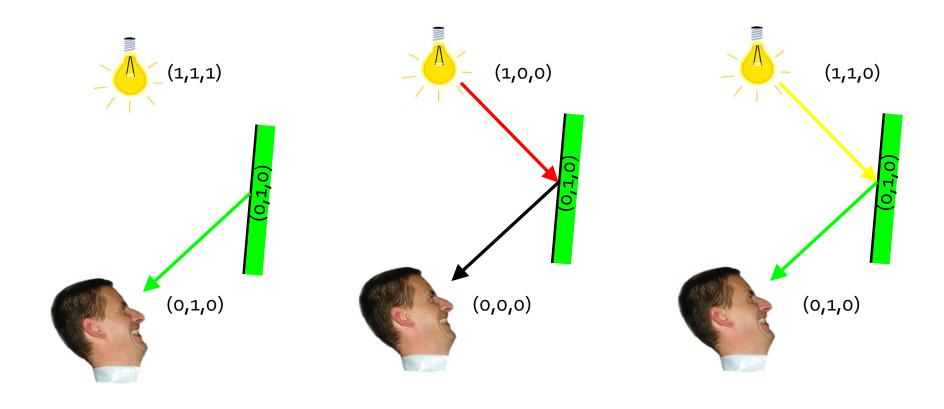




# **Lighting Models**



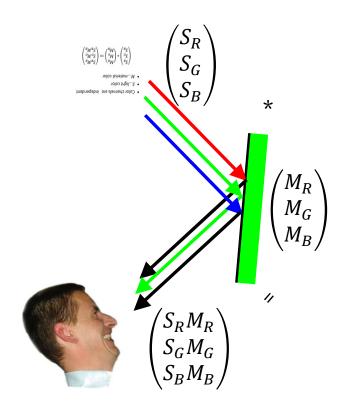
# **Light-Material Interaction**



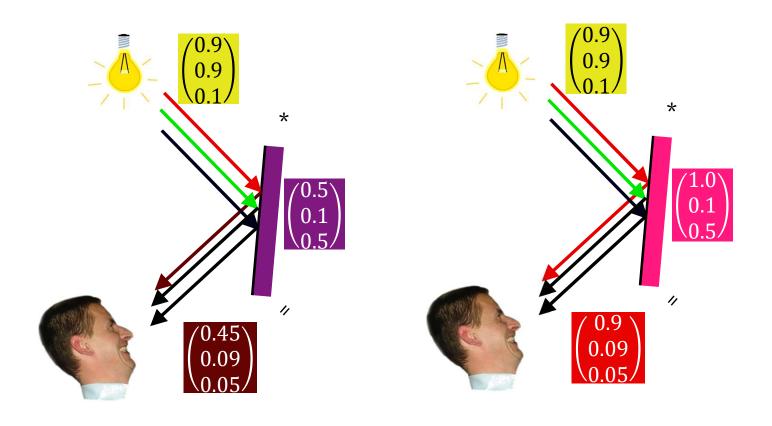
### Color Multiplication – "\*" Operator

- Color channels are independent
- S...light color
- M...material color

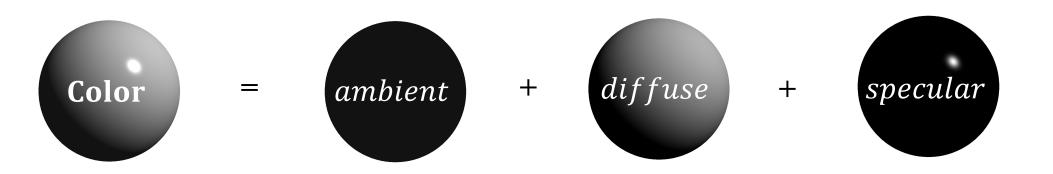
$$\begin{pmatrix} S_R \\ S_G \\ S_B \end{pmatrix} * \begin{pmatrix} M_R \\ M_G \\ M_B \end{pmatrix} \coloneqq \begin{pmatrix} S_R M_R \\ S_G M_G \\ S_B M_B \end{pmatrix}$$



# Color Multiplication – "\*" Operator



### **Phong Illumination Model**



component ... lighting model component

### **Ambient Light Reflection**



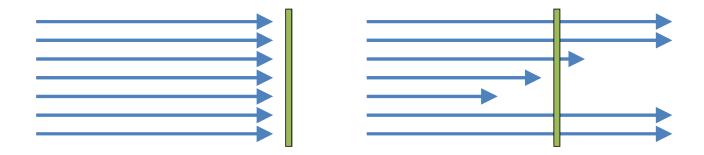
- Background light
  - No direction because scattered so often
  - "Color inside shadow"
  - Approximation of global diffuse lighting effects
- $S_{amb}$ ...ambient light color
- *M<sub>amb</sub>*...ambient material color

$$ambient = M_{amb} * S_{amb}$$

### **Diffuse Light Reflection**

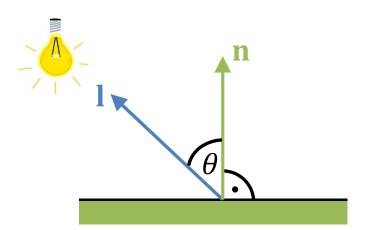
diffuse

- The flatter light falls on a surface, the darker it will appear
- Ideal diffuse reflectors (Lambertian reflectors)
- Brightness depends on orientation of surface



#### **Lamberts Law**

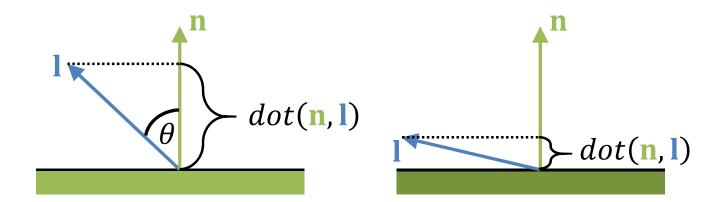
- Diffuse brightness is dependent on angle between
  - n ... surface normal and
  - 1 ... direction to the light



#### **Lamberts Law**



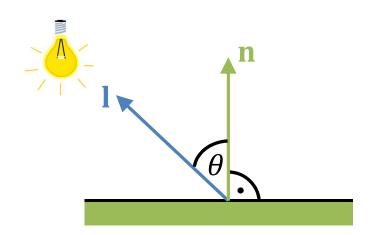
- Diffuse brightness is dependent on angle between
  - n ... surface normal and
  - 1 ... direction to the light
- $\cos \theta = dot(\mathbf{n}, \mathbf{l})$



# **Diffuse Light Reflection**



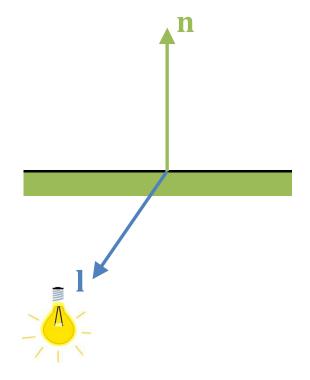
- $S_{diff}$ ...diffuse light color
- $M_{diff}$ ... diffuse material color
- $diffuse = M_{diff} * S_{diff} \cdot dot(\mathbf{n}, \mathbf{l})$



# **Light from Behind**



- Should be ignored
- $diffuse = M_{diff} * S_{diff} \cdot \max(0, dot(\mathbf{n}, \mathbf{l}))$

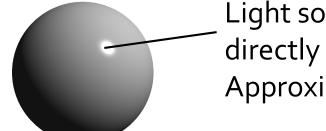


#### **Effect of Ambient + Diffuse**



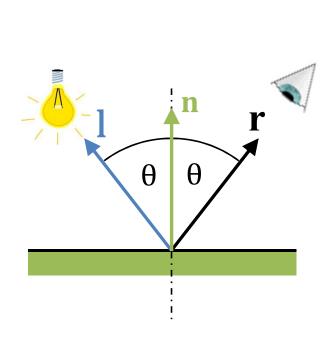
### **Specular Highlights**

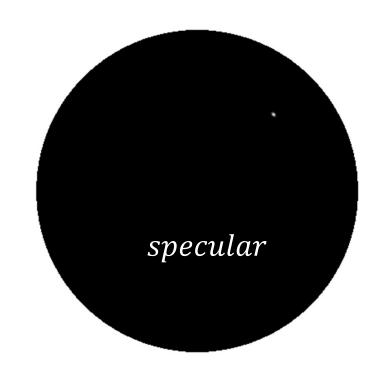




Light source reflection directly into the viewer's eye Approximate image of light source

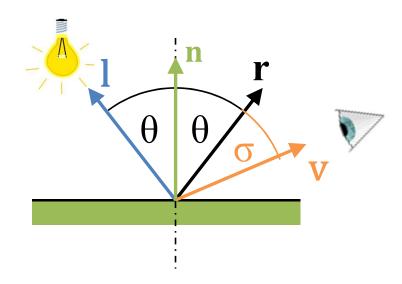
#### **Mirror Reflection**

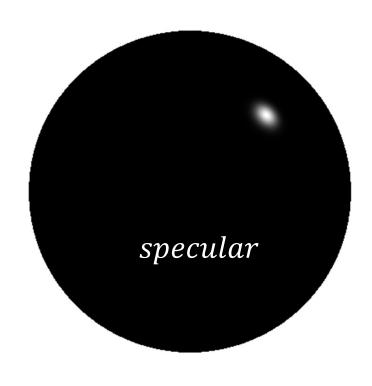




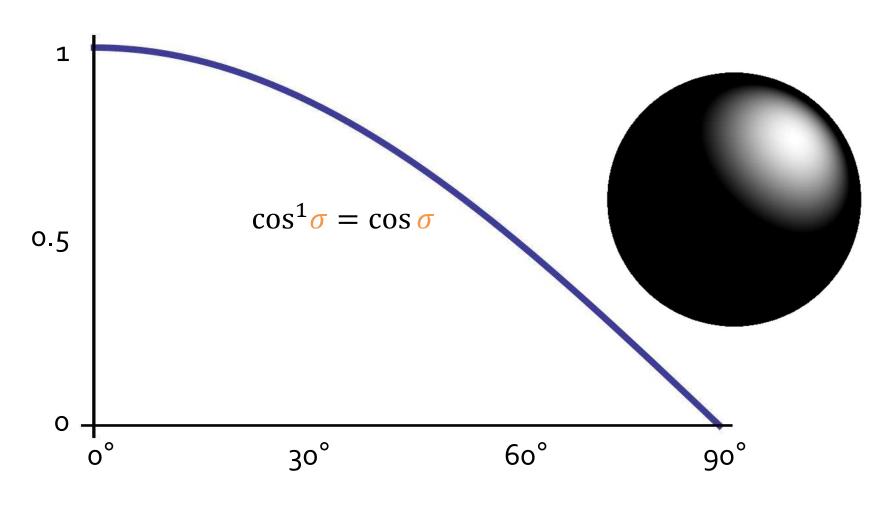
### **Empirical Specular Reflection**

- $S_{\text{spec}}$ ... specular light color
- $M_{\rm spec}$ ... specular material color
- $specular = M_{spec} * S_{spec} \cdot cos^p \sigma$

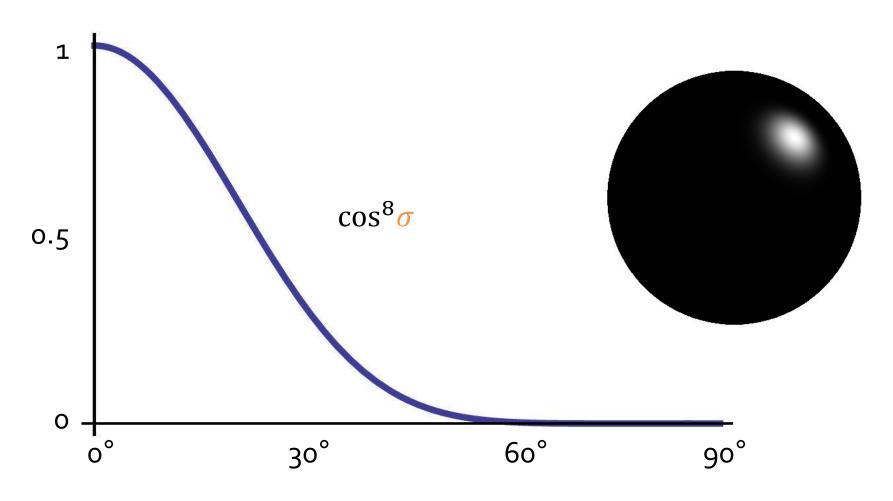




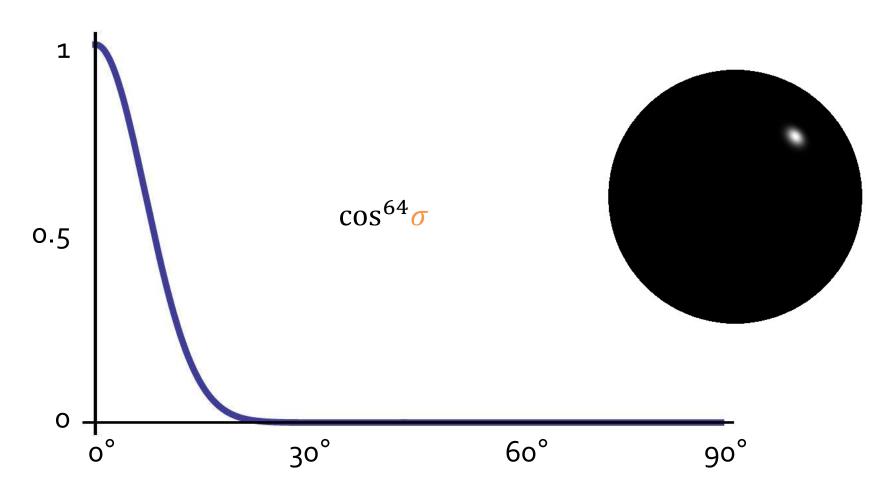
# Specular Reflection Coefficient p=1



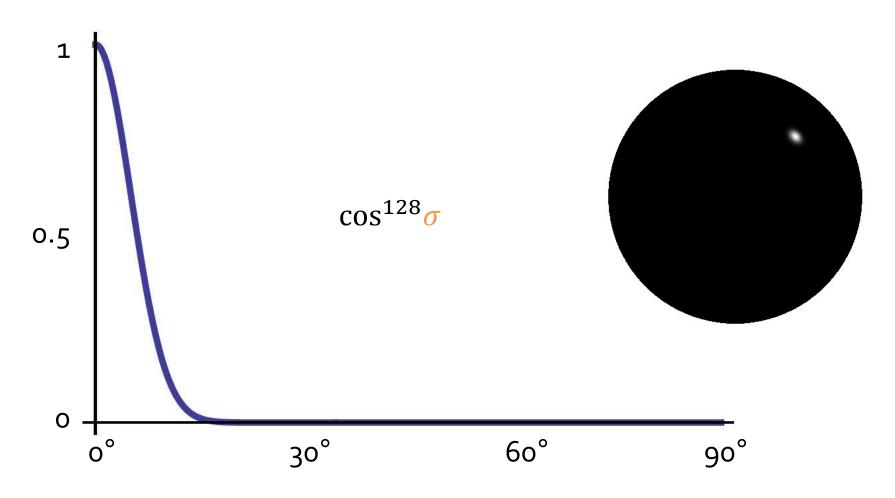
# Specular Reflection Coefficient p=8



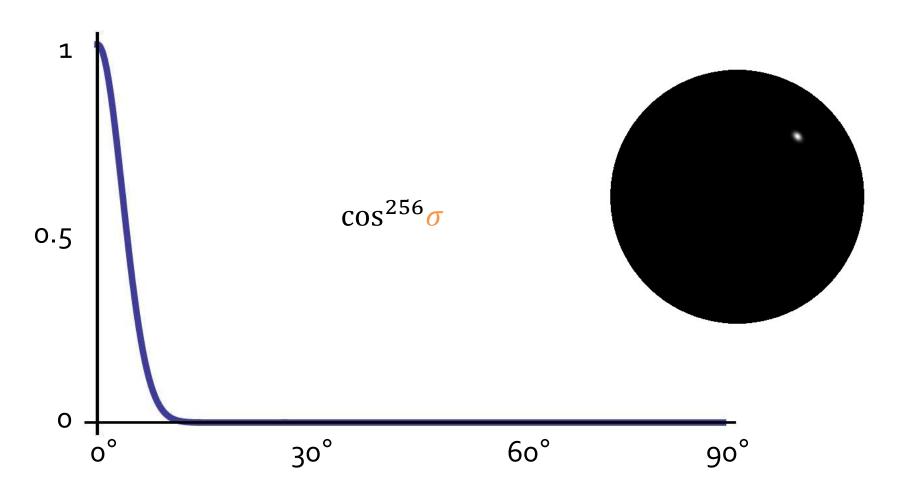
# Specular Reflection Coefficient p = 64



# Specular Reflection Coefficient p=128

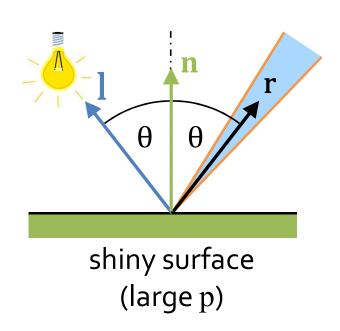


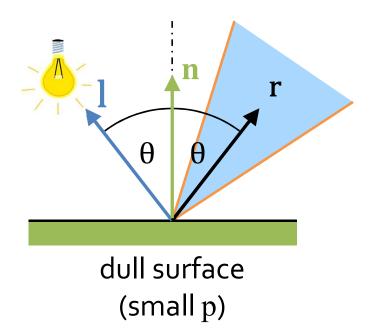
# **Specular Reflection Coefficient** p=256



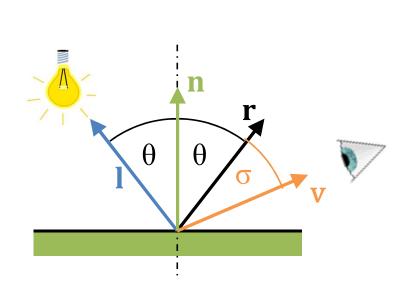
# **Specular Reflection Coefficient – Shininess**

•  $specular = M_{spec} * S_{spec} \cdot cos^p \sigma$ 

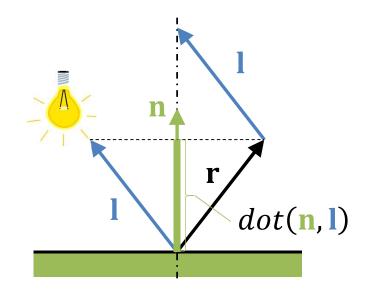




### **Specular Reflection Calculation**

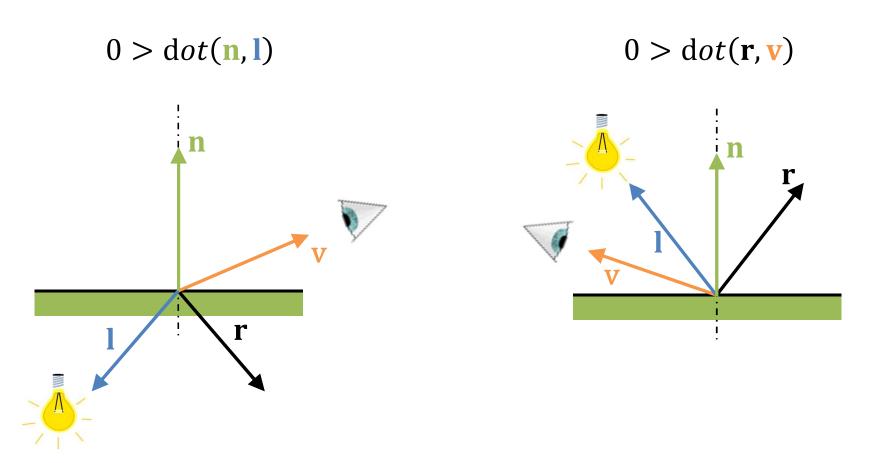


$$specular = M_{spec} * S_{spec} \cdot cos^{p} \sigma$$
$$= M_{spec} * S_{spec} \cdot dot(\mathbf{r}, \mathbf{v})^{p}$$



$$\mathbf{r} + \mathbf{l} = 2 \cdot dot(\mathbf{n}, \mathbf{l}) \cdot \mathbf{n}$$
  
 $\mathbf{r} = 2 \cdot dot(\mathbf{n}, \mathbf{l}) \cdot \mathbf{n} - \mathbf{l}$ 

# Do not apply Specular when

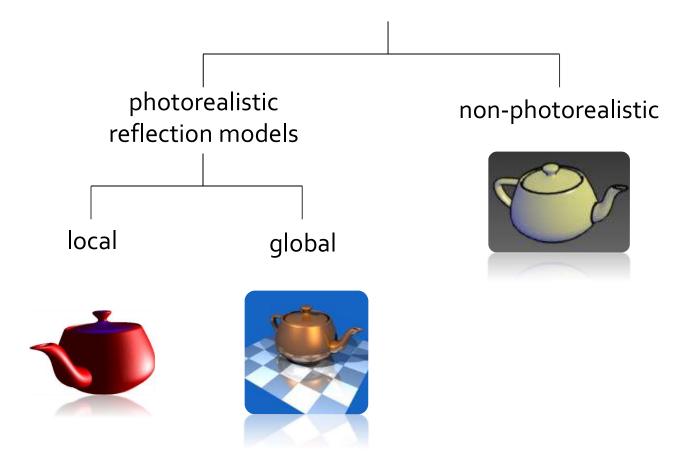


### **Phong Illumination Model**

ambient + diffuse + specular =

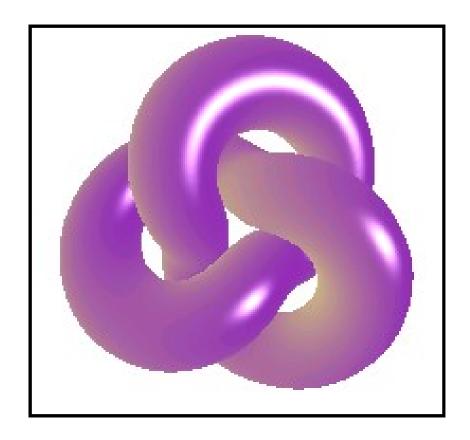
$$= M_{amb} * S_{amb} + M_{diff} * S_{diff} \cdot dot(\mathbf{n}, \mathbf{l}) + M_{spec} * S_{spec} \cdot dot(\mathbf{r}, \mathbf{v})^{p}$$

## **Lighting Models**



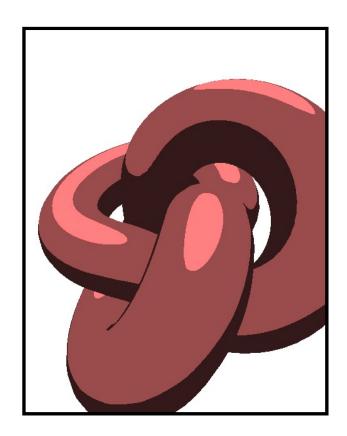
### Gooch

Blend between a cool and a warm color



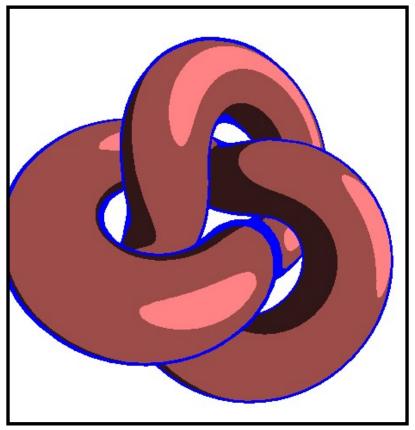
# **Toon shading**

Discrete color steps for diffuse



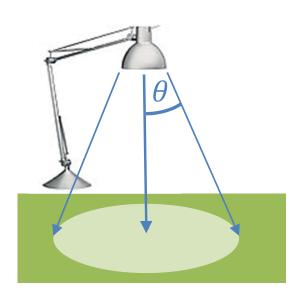
# **Cel shading**

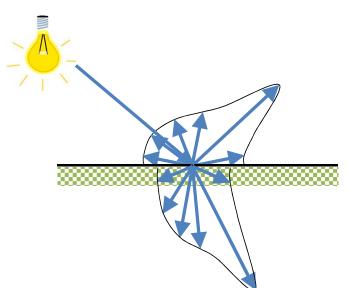
Detect edges and color them

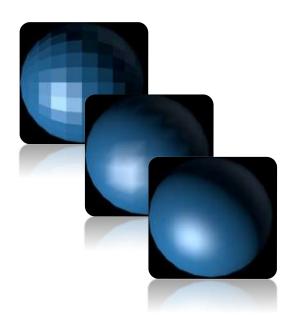


**Light Sources** 

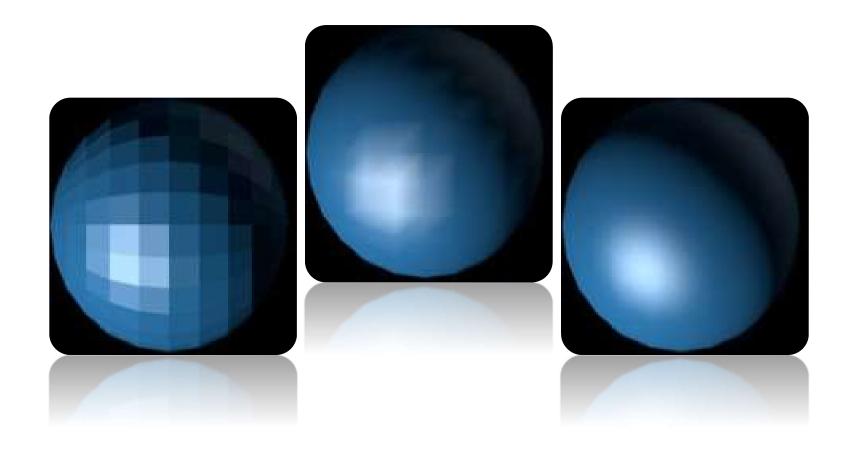
Reflection Models Shading Models







# **Shading Models**



## **Shading model**

- Shading ≠ shadows (shadowing)
- Coloring / shading the model
- When to evaluate lighting model



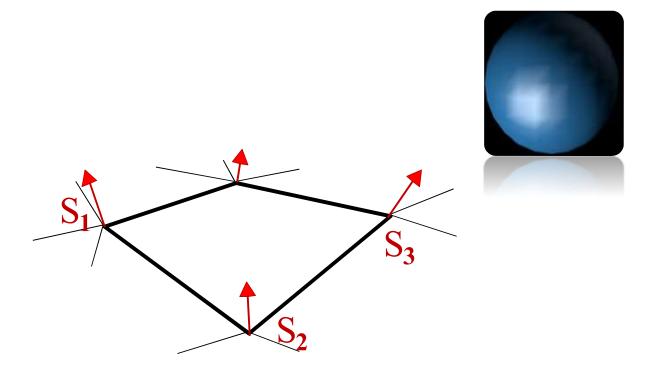
## Flat-shading

- 1 color for the mesh (polygon)
- Really fast
- Really ugly
- If an object really is faceted, is this accurate?
- No:
  - Point light sources
    - Direction to light varies across the facet
  - Specular reflectance
    - Direction to eye varies across the facet



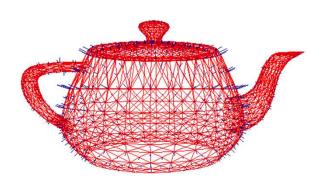
## Gouraud shading

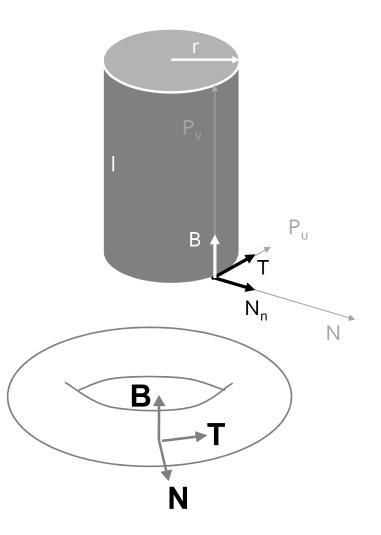
- 1. Calculate the normal vector for each vertex
- 2. Calculate the intensitity for each vertex



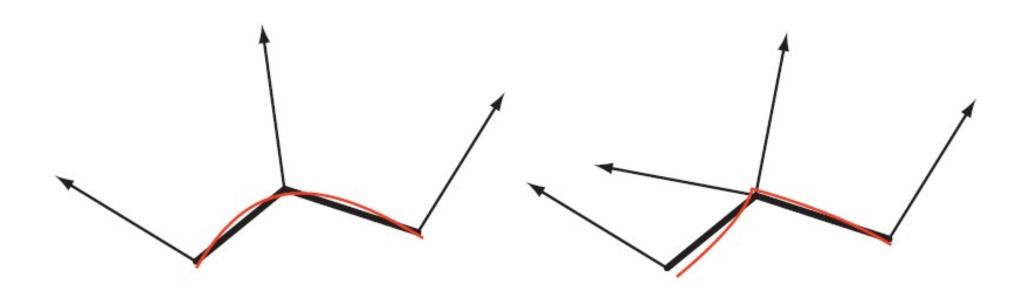
#### **Vertex Normals**

- Vertex normals may be
  - Provided with the model
    - Artist
    - 3d program
  - Computed from first principles
    - Mathematic description of model



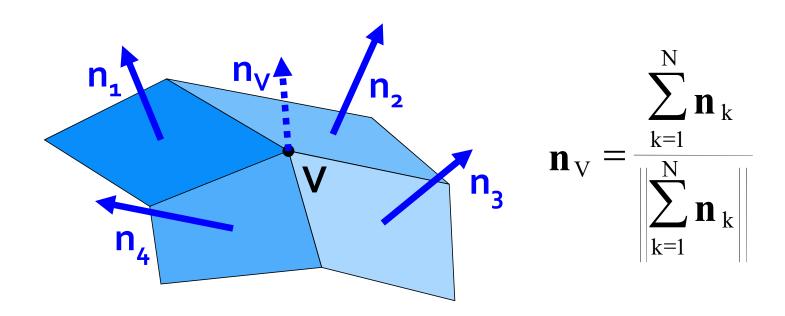


# **Sharp Edges and Normals**



#### **Vertex Normals**

Approximated by averaging the normals of the facets that share the vertex



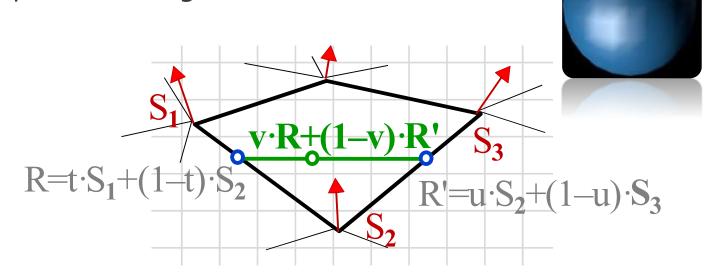
## Gouraud shading

- 1. Calculate the normal vector for each vertex
- 2. Calculate the intensitity for each vertex

3. Color interpolation along edges  $R=t\cdot S_1+(1-t)\cdot S_2$   $R!=u\cdot S_2+(1-u)\cdot S_3$ 

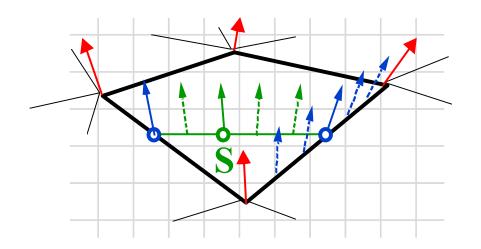
## Gouraud shading

- 1. Calculate the normal vector for each vertex
- 2. Calculate the intensitity for each vertex
- 3. Color interpolation along edges
- 4. Color interpolation along scanline



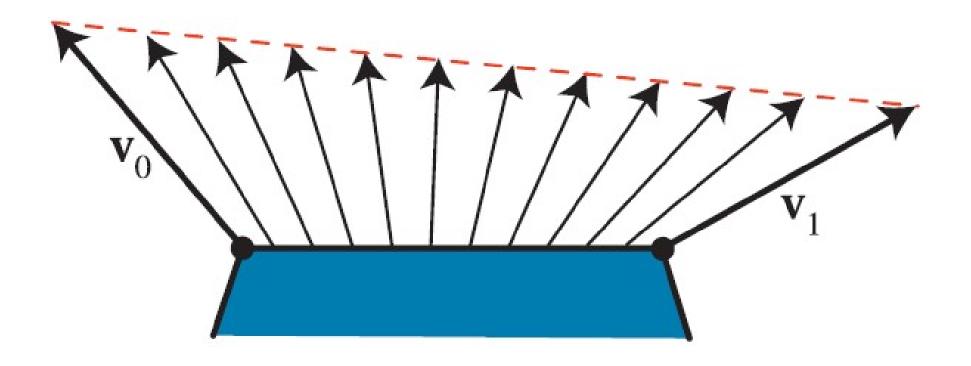
#### **Phong Shading Model**

- 1. Normal Vector for each vertex
- 2. Normal vectors are interpolated along the edge
- 3. Normal vectors are interpolated along the scanline
- 4. Calulate the intensity using the normal vectors





# **Normal Interpolation**



# Flat / Gouraud / Phong Comparison



## **Transforming Normals**

- Differential scaling changes shape and normals
- If **M** transforms points, then (**M**<sup>T</sup>)<sup>-1</sup> transforms normals

