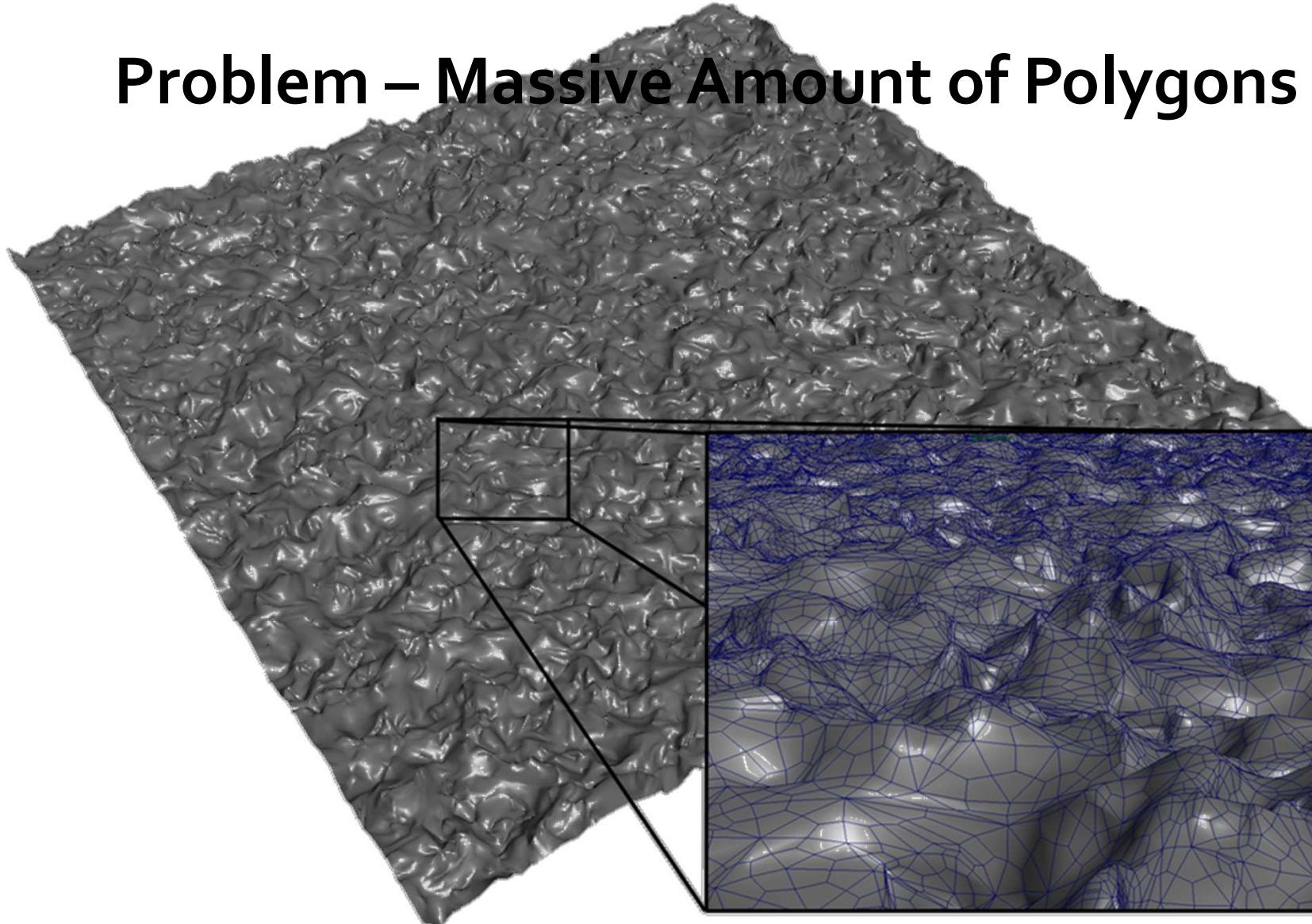
The background image is a detailed, monochromatic rendering of a textured surface. It features deep, dark shadows and bright highlights that create a sense of depth and physicality. The texture appears to be a combination of fine, wavy lines and larger, more pronounced folds, resembling the surface of a soft material like velvet or a highly detailed stone. The lighting is dramatic, coming from the upper right, which emphasizes the ridges and valleys of the surface.

Rendering Surface Details

Problem – Massive Amount of Polygons



Idea

- Highly detailed surface look without huge models



+

Detail
information

=



Approaches

- Geometric
 - Displacement Mapping
 - Volume slice rendering
 - Ray tracing
- Image Space
 - Normal mapping
 - Parallax mapping
 - Relief textures
 - BRDFs (Bidirectional Reflectance Distribution Functions)

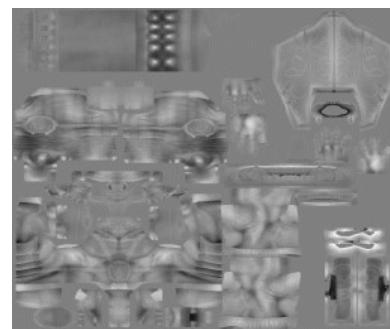
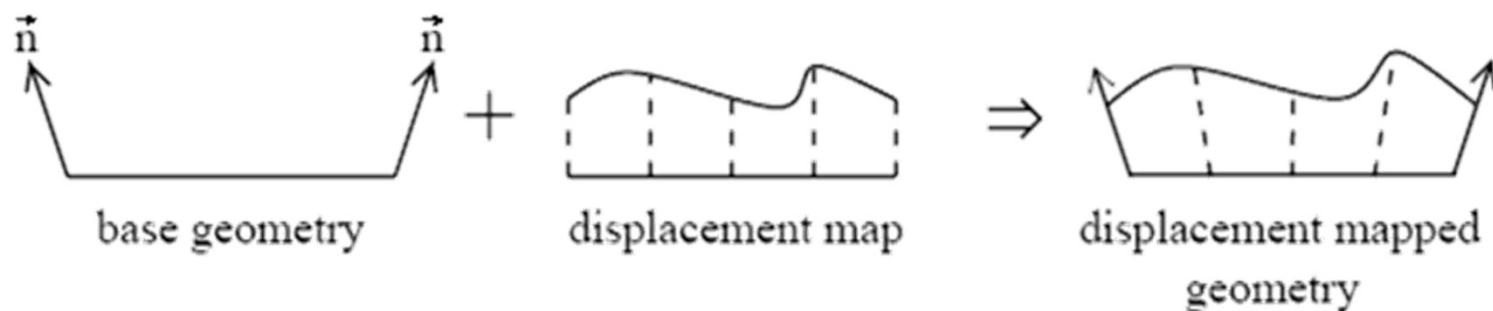


Rendering Surface Details

Displacement Mapping

Displacement Mapping

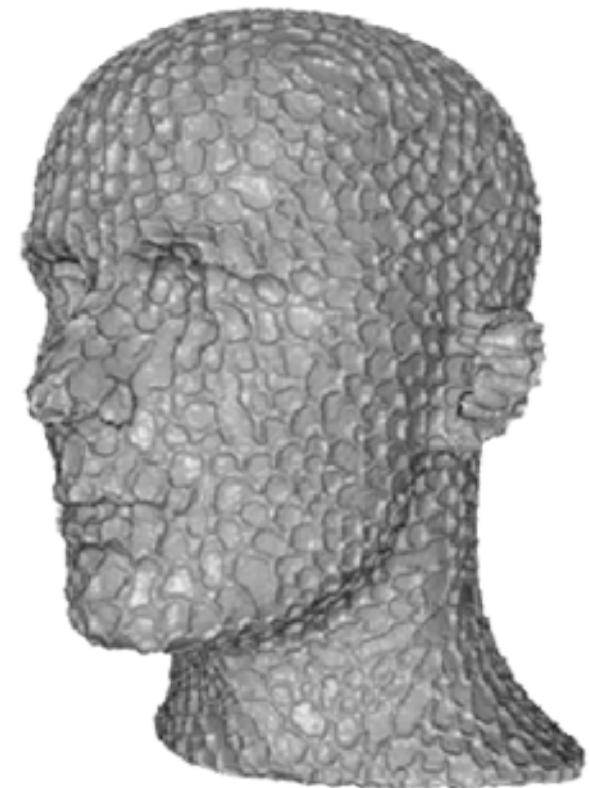
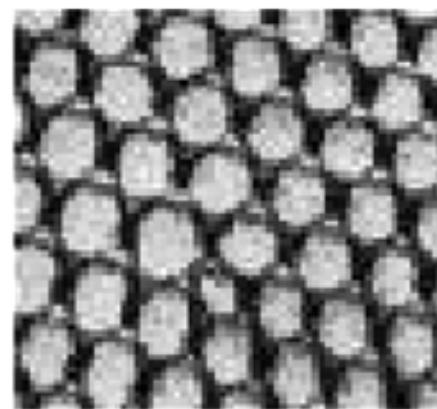
- A displacement map specifies displacement in the direction of the surface normal, for each point on a surface





Displacement Mapping – Idea

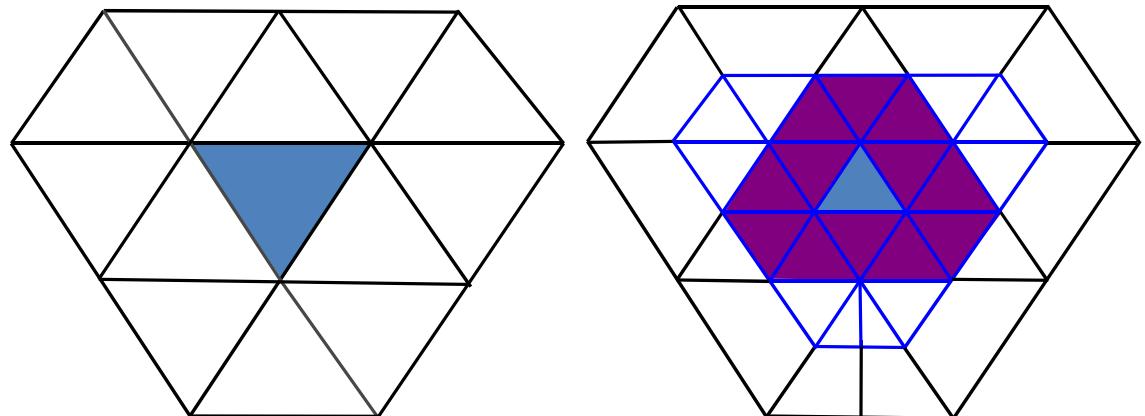
- Shift all points on the surface along their normal vectors
- $p' = p + \text{displacementTex}(p) * n$
- How can we render a model given as a set of polygons, and a displacement map?





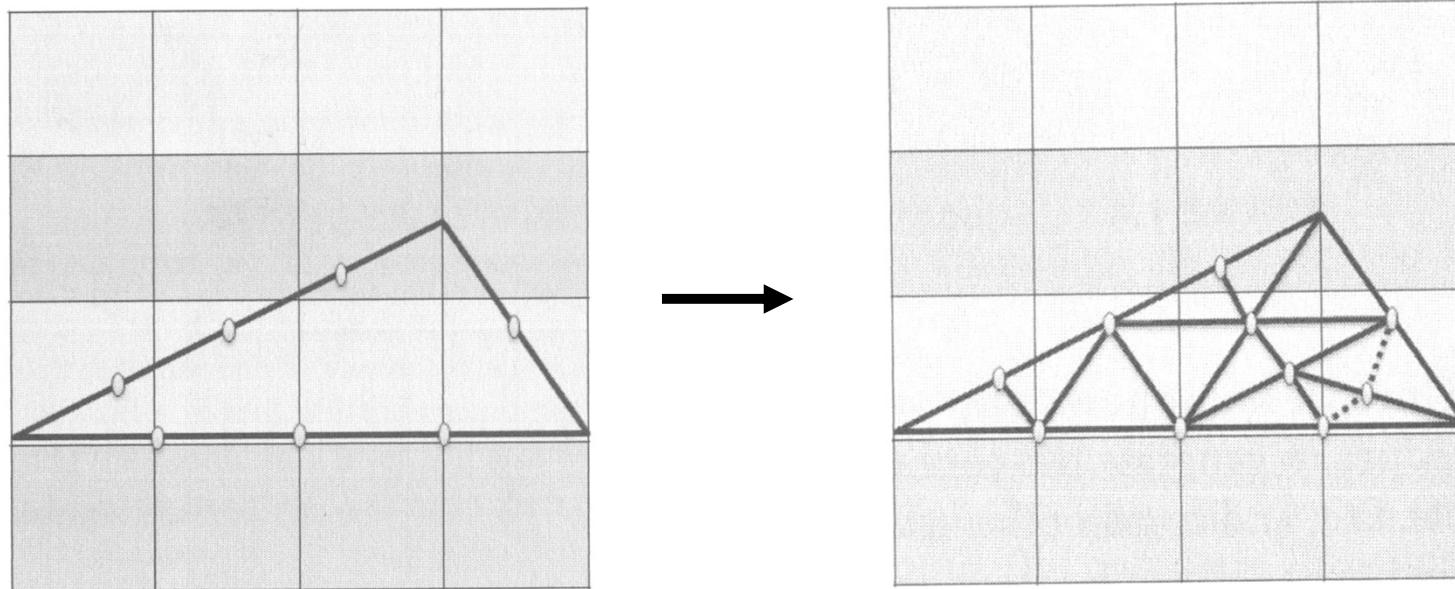
Subdivide and Displace

- Subdivide each polygon, till?
- Displace each vertex along normal using displacement map
- Many new vertices and triangles
- Improvements
 - Adaptive subdivision



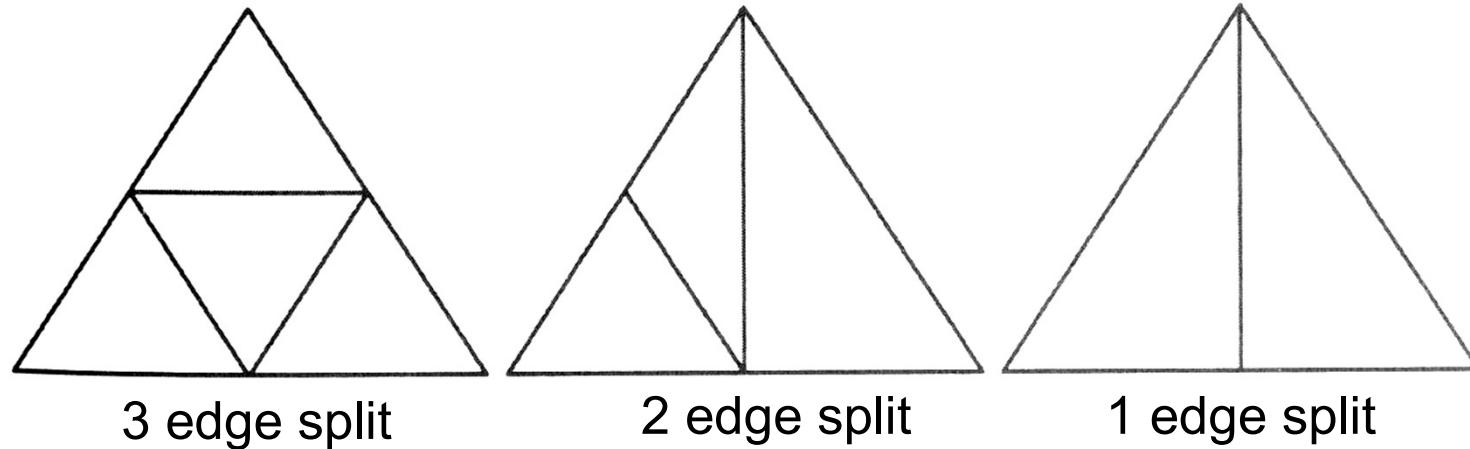
Simple Adaptive Subdivision

- Idea: subdivision based on edge length
- At least one triangle per pixel
- Efficient?



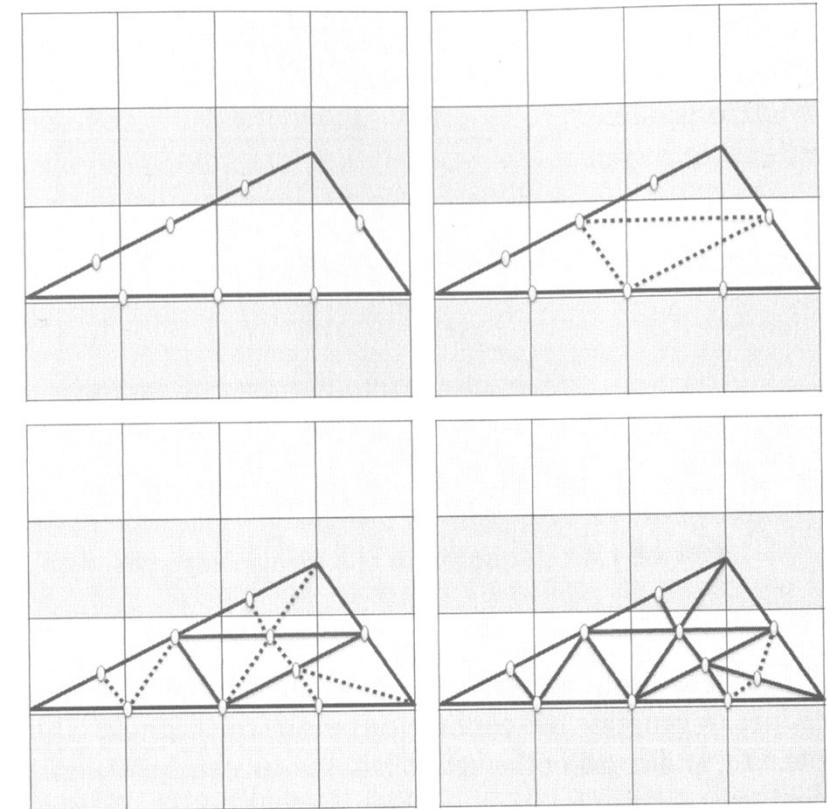
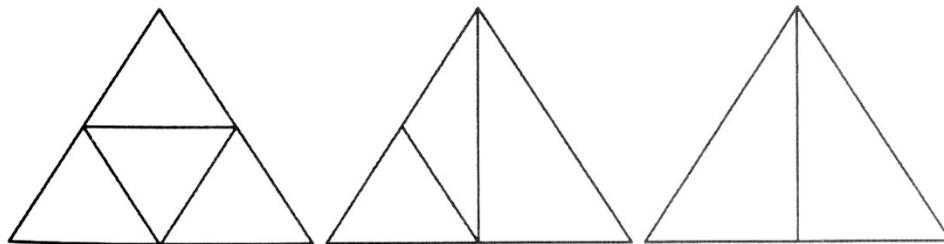
Simple Adaptive Subdivision

- Pre-computed tessellation patterns
 - 7 possible patterns
 - 3 if we do rotation in code



Simple Adaptive Subdivision

- Precomputed tessellation patterns
- Recursive subdivision





Rendering Surface Details

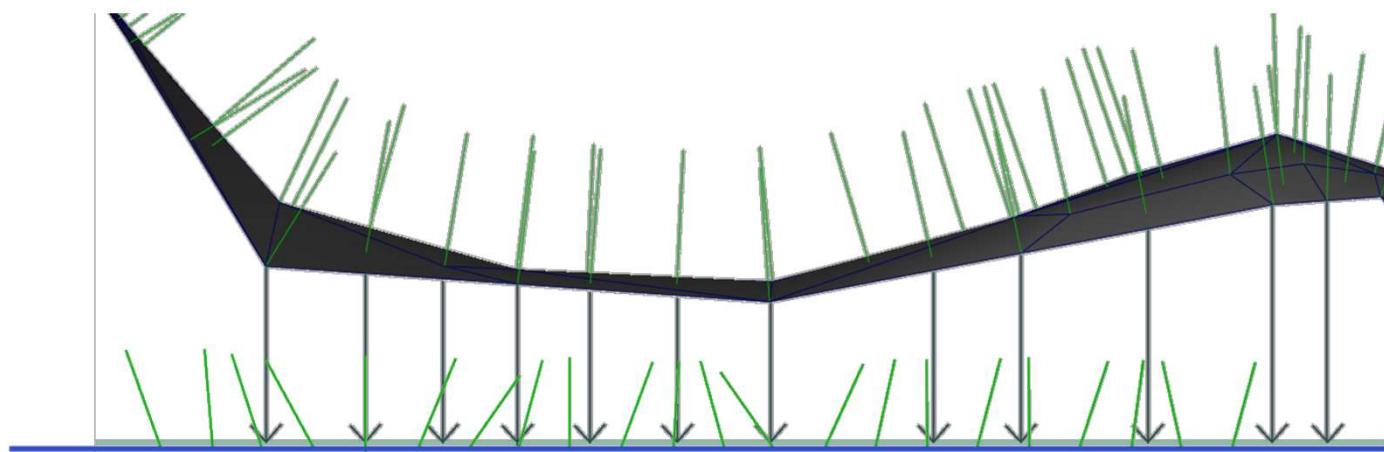
Normal(Bump) Mapping

Normal Mapping

- Bump/normal mapping invented by Blinn 1978.
- Efficient rendering of structured surfaces
- Enormous visual Improvement without additional geometry
- Is a local method
 - Does not know anything about surrounding except lights
- Heavily used method
- Realistic AAA games normal map every surface

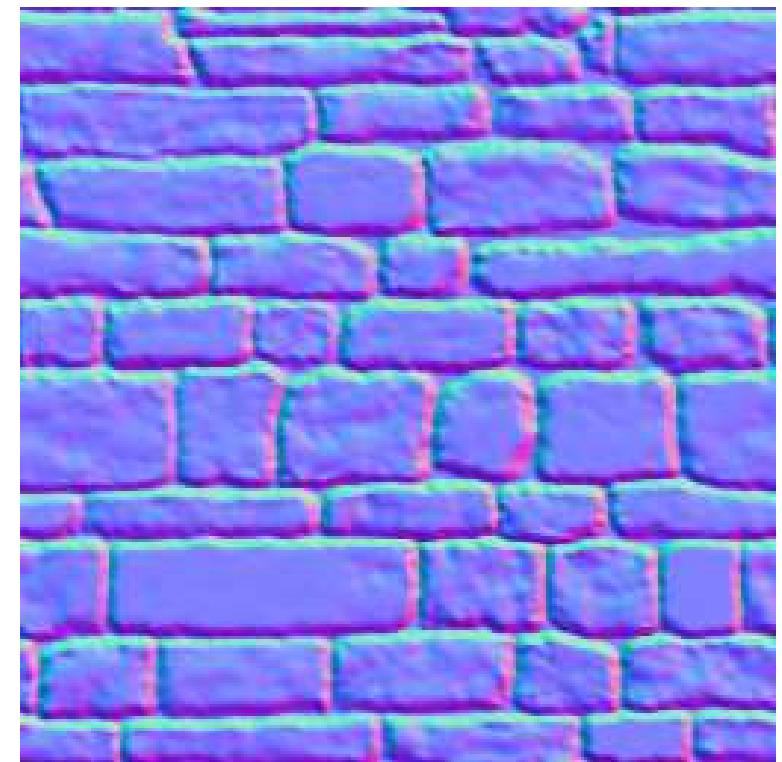
Normal Mapping

- Idea: illumination is not directly dependent on position
- Position can be approximated by carrier geometry
- Idea: transfer normal to carrier geometry



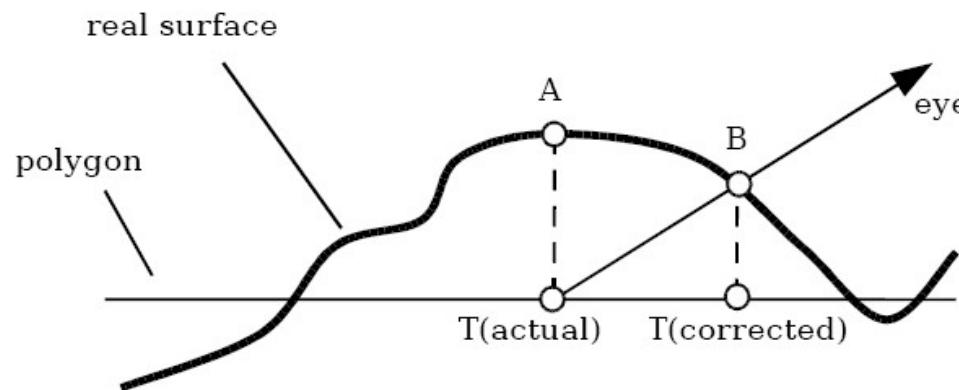
Normal Mapping

- Result: Texture that contains the normals as vectors
 - Red X
 - Green Y
 - Blue Z
 - Saved as range compressed bitmap
([-1..1] mapped to [0..1])
- Directions instead of polygons!



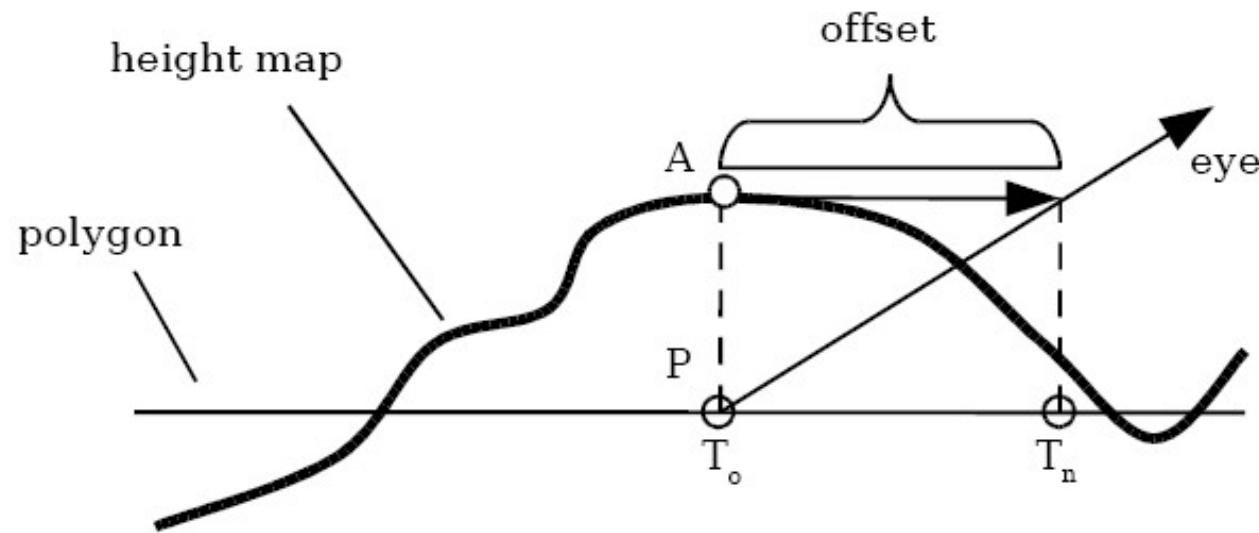
Parallax-Normal Mapping

- Normal mapping does not use the height field
 - No parallax effect, surface is still flattened
- Idea: distort texture lookup according to view vector and height field
 - Good approximation of original geometry



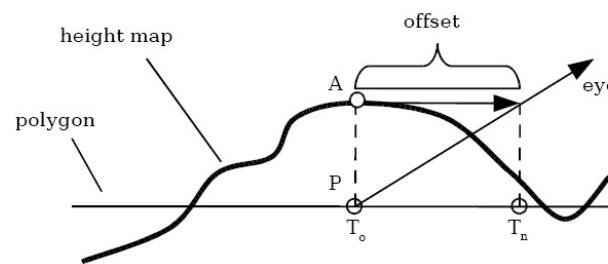
Parallax-Normal Mapping

- We want to calculate the offset to lookup color and normals from the corrected position T_n to do shading there



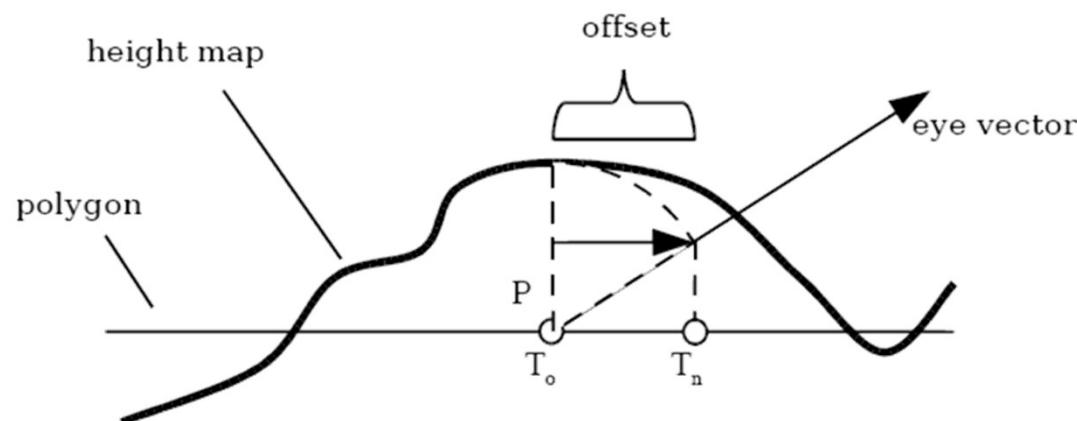
Parallax-Normal Mapping

- Rescale height map h to appropriate values:
 $hn = h*s - 0.5s$
($s = \text{scale} = 0.01$)
- Assume height field is locally constant
 - Lookup height field at T_o
- Trace ray from T_o to eye with eye vector V to height and add offset:
 - $T_n = T_o + (hn * Vx, y/Vz)$



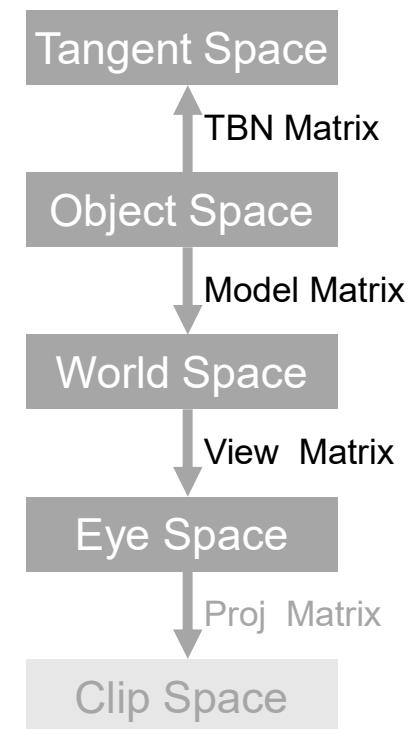
Offset Limited Parallax-Normal Mapping

- Problem: At steep viewing angles, Vz goes to zero
 - Offset values approach infinity
 - Solution: we leave out Vz division:
 $T_n = T_o + (h_n * Vx, y)$
- Effect: offset is limited



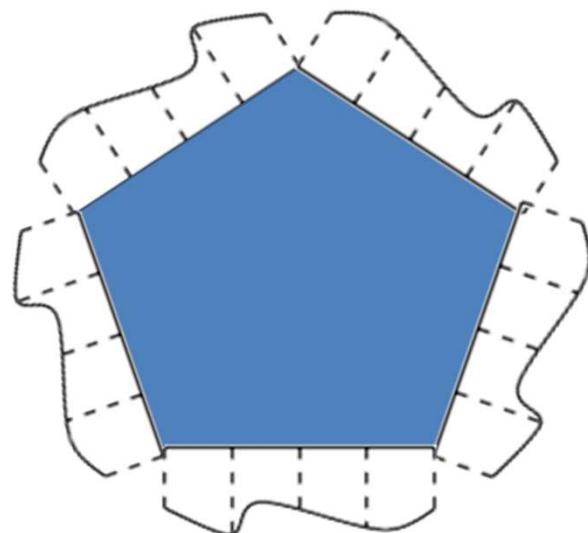
Coordinate Systems

- Problem: where to calculate lighting?
- Object coordinates
 - Native space for normals (N)
- World coordinates
 - Native space for light vector (L), env-maps
 - Not explicit in OpenGL!
- Eye Coordinates
 - Native space for view vector (V)
- Tangent Space
 - Native space for normal maps



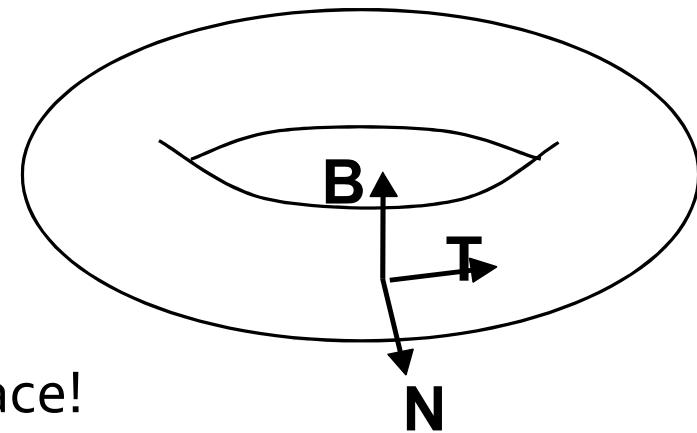
Why Tangent Space?

- Normals are in coordinate system of texture
- Not in coordinate system of model



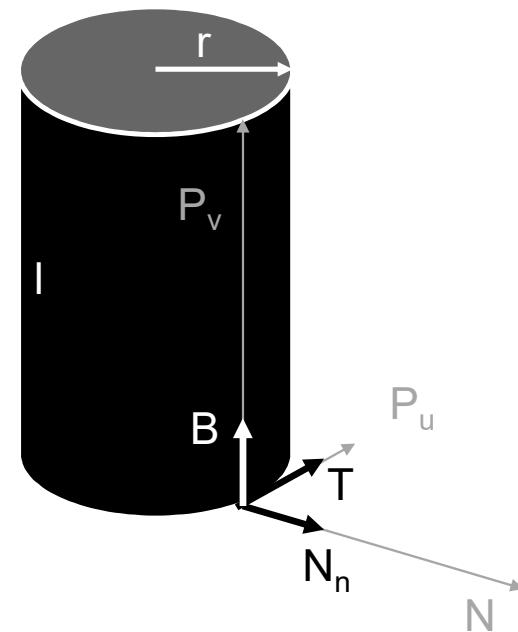
Tangent Space

- Concept from differential geometry
- Set of all tangents on a surface
- Orthonormal coordinate system (frame) for each point on the surface:
$$N_n(u,v) = P_u \times P_v / |P_u \times P_v|$$
$$T = P_u / |P_u|$$
$$B = N_n \times T$$
- A natural space for normal maps
 - Vertex normal $N = (0,0,1)$ in this space!



Parametric Example

- Cylinder Tangent Space:
 $N_n(u,v) = P_u \times P_v / |P_u \times P_v|$
 $T = P_u / |P_u|$
 $B = N_n \times T$
- Tangent space matrix:
TBN column vectors
 - Transforms from tangent
into object space



Creating Tangent Space

- Trivial for analytically defined surfaces
 - Calculate P_u, P_v at vertices
- Use ***texture space*** for polygonal meshes
 - P_u aligned with u direction and P_v with v
 - Origin is texture coordinate of vertex
- Transformation from object space to tangent space (if TBN is a orthonormal matrix)

$$\begin{matrix} L_{tx} & L_{ty} & L_{tz} \end{matrix} = \begin{matrix} L_{ox} & L_{oy} & L_{oz} \end{matrix} \begin{matrix} T_x & B_x & N_x \\ T_y & B_y & N_y \\ T_z & B_z & N_z \end{matrix}$$

Creating Tangent Space for a Mesh

- Calc tangent for a triangle P_0, P_1, P_2
 - With texture coordinates $(u_0, v_0), (u_1, v_1), (u_2, v_2)$
 - Work relative to P_0
 - $Q_1 = P_1 - P_0 \quad (s_1, t_1) = (u_1 - u_0, v_1 - v_0)$
 - $Q_2 = P_2 - P_0 \quad (s_2, t_2) = (u_2 - u_0, v_2 - v_0)$
 - Need to solve
 - $Q_1 = s_1T + t_1B$
 - $Q_2 = s_2T + t_2B$
 - Solve linear System with 6 unknowns and 6 equations
- Vertex tangents by averaging tangents of all triangles sharing the vertex

Creating Tangent Space for a Mesh

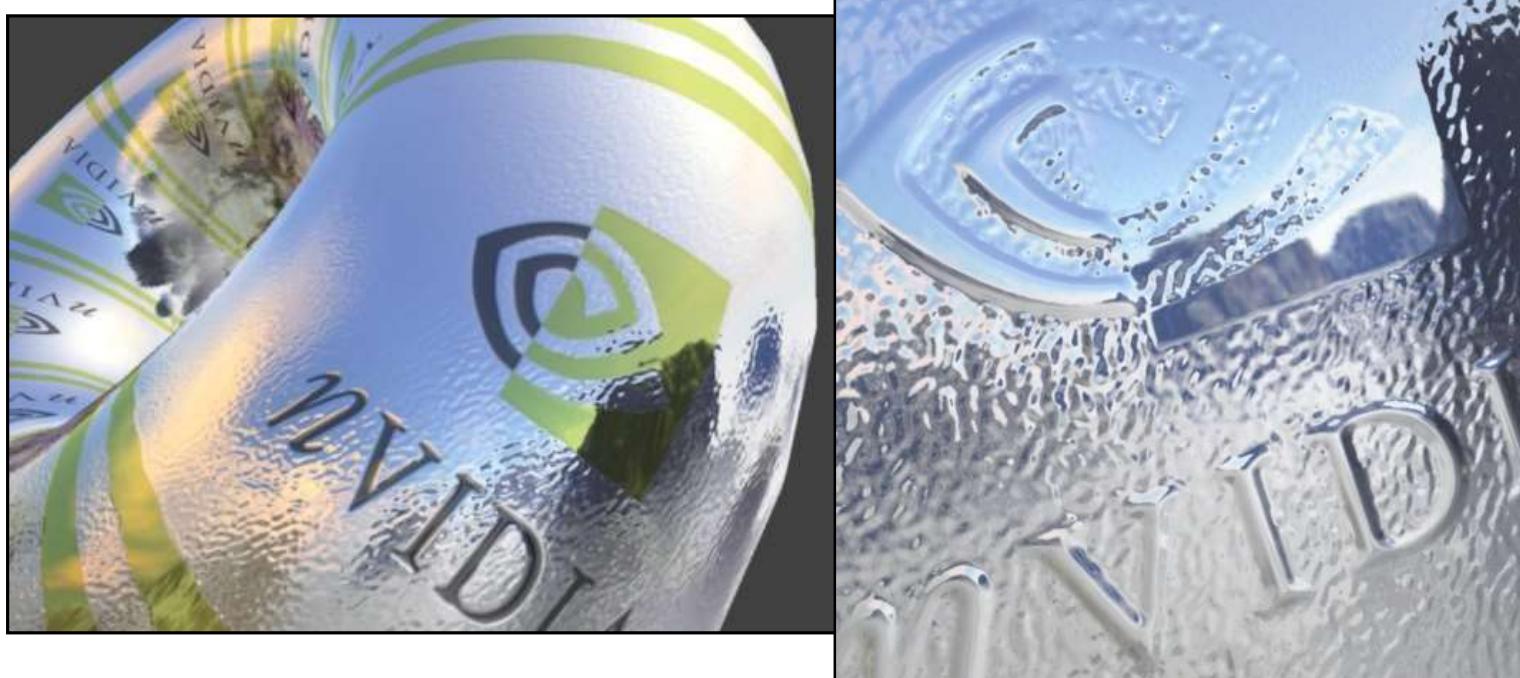
- Need to orthogonalize resulting tangents for inverting with transpose
 - Gram-Schmidt
- If only one tangent is stored we need to account for handedness.
- Code and details at
<http://www.terathon.com/code/tangent.html>

Fast Algorithm (Tangent Space)

- For each vertex
 - Transform light direction L and eye vector V to tangent space and normalize
 - Compute normalized half vector H
- For each fragment
 - Interpolate L and H
 - Renormalize L and H
 - Fetch $N' = \text{texture}(s, t)$ (normal map)
 - Use N' in shading

Normal Mapping + Environment Mapping

- Normal and parallax mapping combines beautifully with environment mapping



EMNM (World Space)

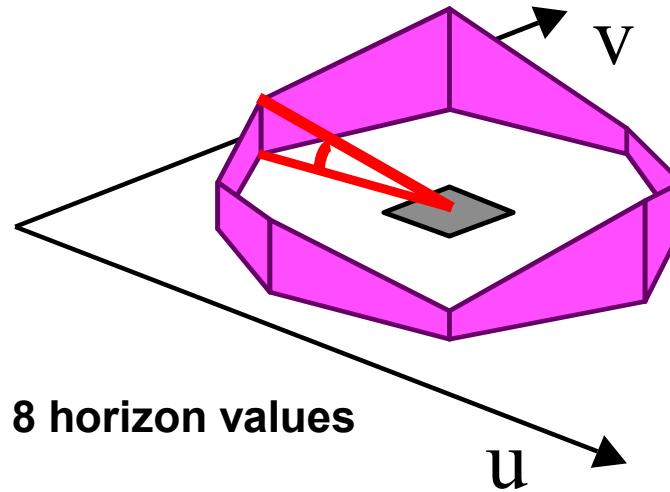
- For each vertex
 - Transform V to world space
 - Compute tangent space to world space transform (T, B, N)
- For each fragment
 - Interpolate and renormalize V
 - Interpolate frame (T, B, N)
 - Lookup $N' = \text{texture}(s, t)$
 - Transform N' from tangent space to world space
 - Compute reflection vector R (in world space) using N'
 - Lookup $C = \text{cubemap}(R)$

Normal and Parallax Normal Map Issues

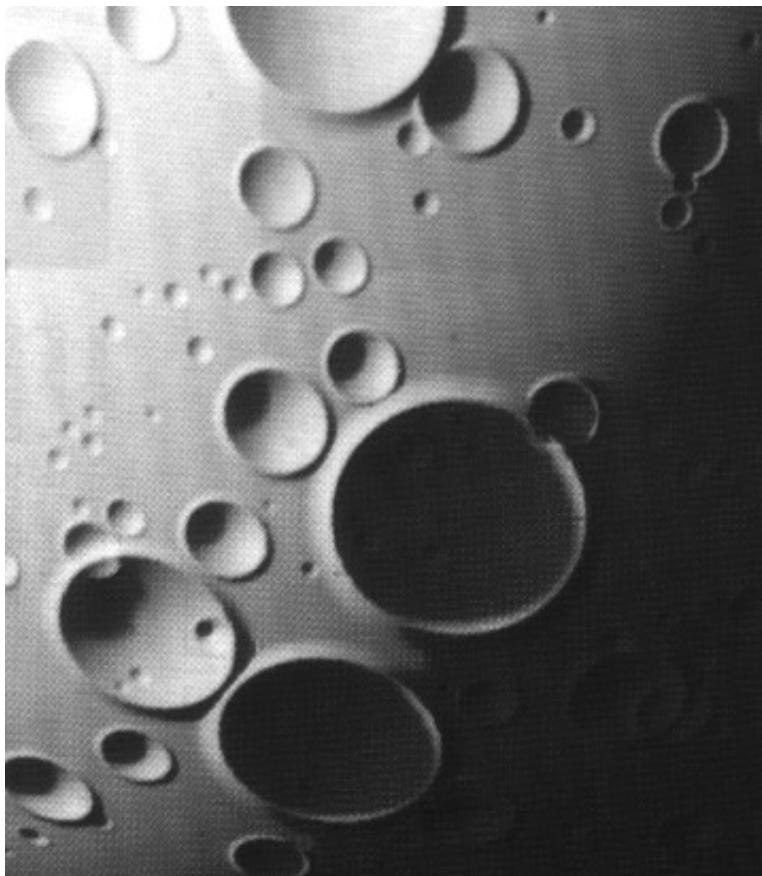
- Artifacts
 - No inter-shadowing
 - Silhouettes still edgy
 - No parallax for normal mapping
- Parallax normal mapping
 - No occlusion, just distortion
 - Not accurate for high frequency height fields
(local constant height field assumption does not work)
 - No silhouettes

Horizon Mapping

- Improve normal mapping with (local) shadows
- Preprocess: compute n horizon values per texel
- Runtime:
 - Interpolate horizon values
 - Shadow accordingly



Horizon Mapping Examples

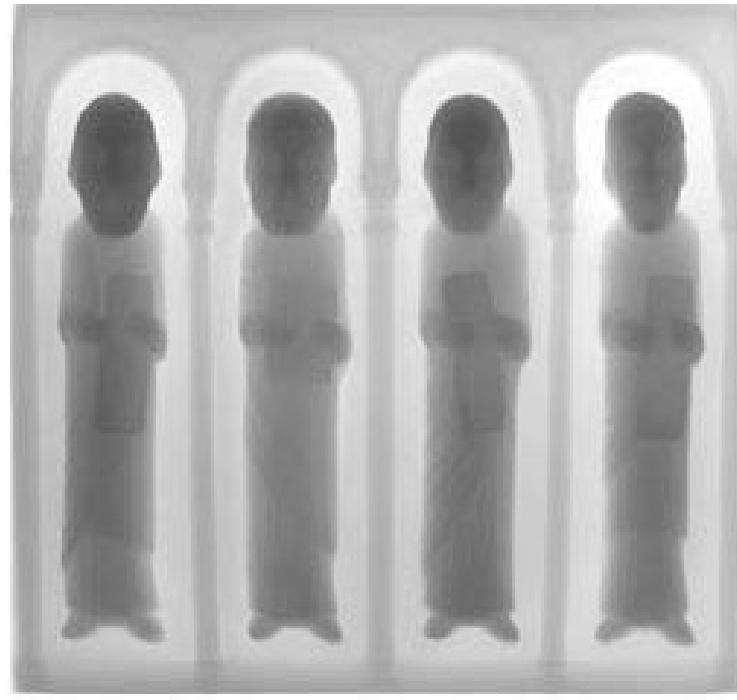


Relief Mapping



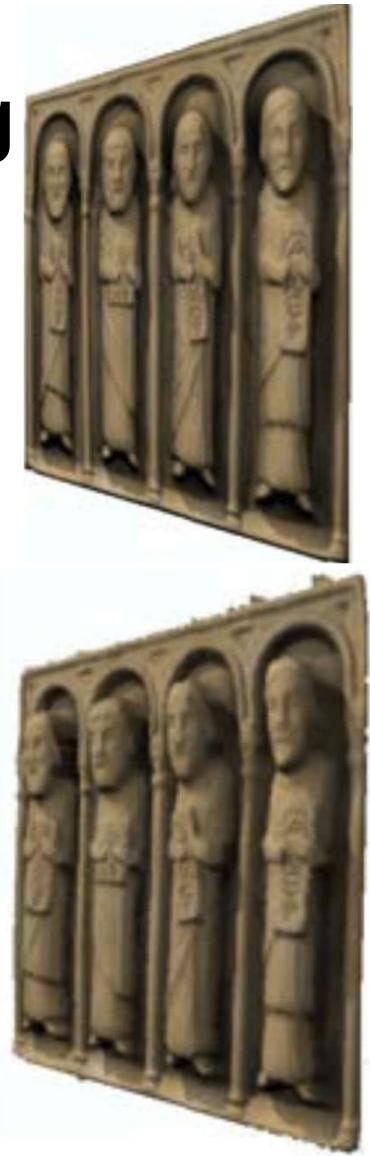
Relief Texture Mapping

- Uses image warping techniques and per-texel depth to create the illusion of geometric detail



Relief Texture Mapping

- Rendering of a height field requires search for closest polygon along viewing ray
- Two-pass method:
 - Convert height field to 2D texture using forward projection
 - Render texture
- Texels move horizontal and vertical in texture space based on their orthogonal displacements and the viewing direction



Relief Mapping Examples



Texture mapping



Parallax mapping

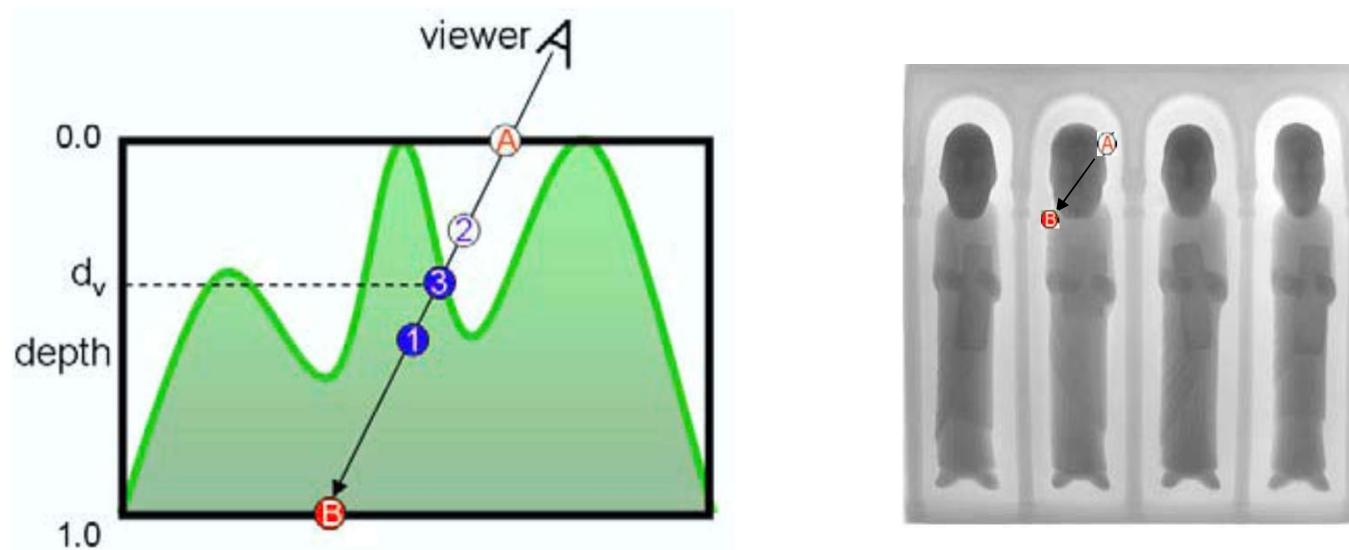


Relief mapping



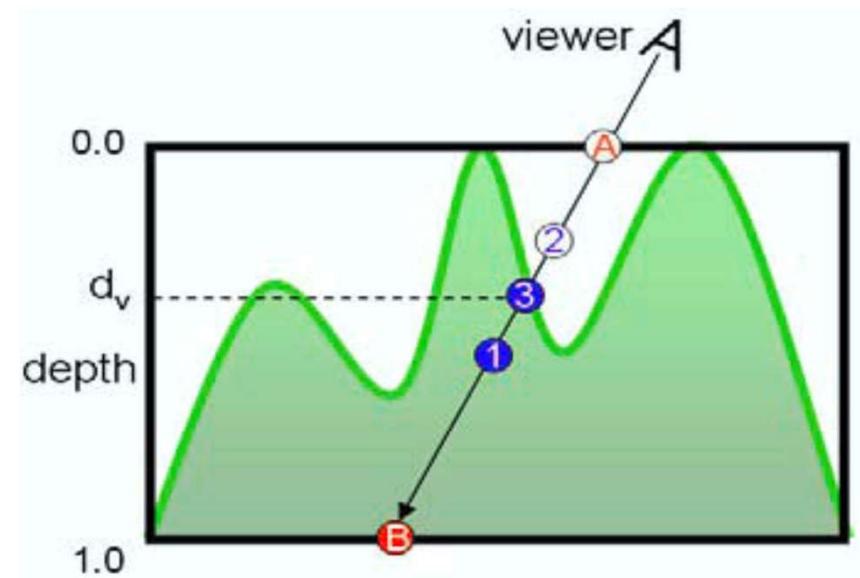
Mapping Relief Data

- Compute viewing direction, VD
- Transform VD to tangent space of fragment
- Use VD' and texture coords (s, t) to compute the texture coords where VD' hits depth of 1



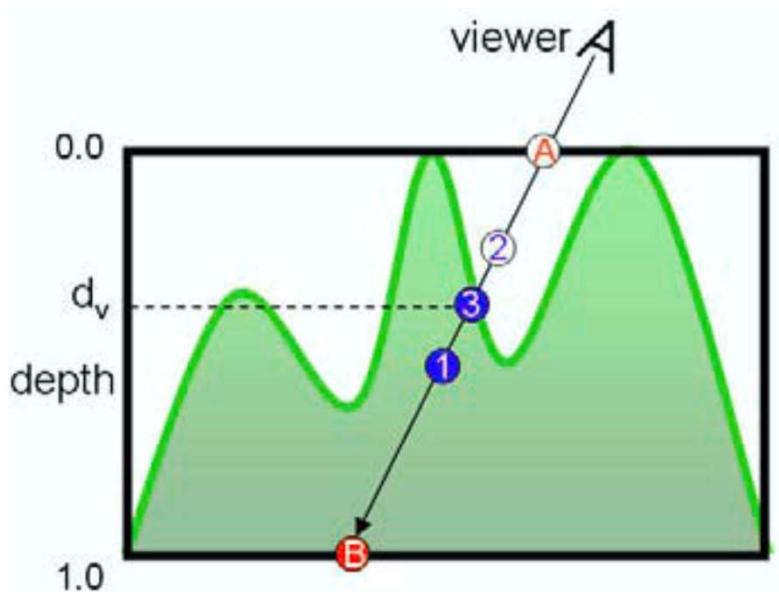
Mapping Relief Data

- Compute intersection between VD' and height-field surface using binary search starting with A and B
- Perform shading of the fragment using the attributes associated with the texture coordinates of the computed intersection point.



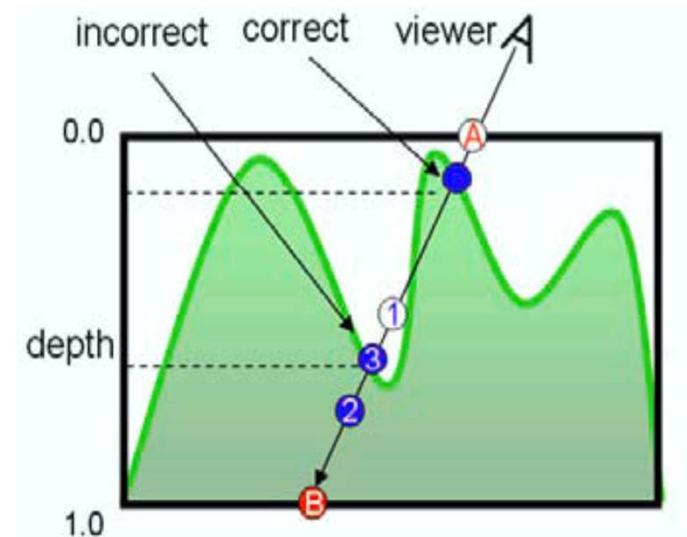
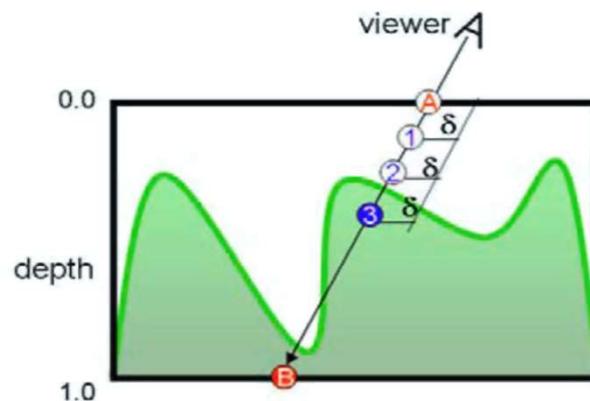
Binary Search

- Start with A-B line
- At each step:
 - Compute middle of interval
 - Assign averaged endpoint texture coordinates and depth
 - Use averaged tex coords to access depth map
 - If stored depth value is less than computed depth value, the point is inside the surface
 - Proceed with one endpoint in and one out



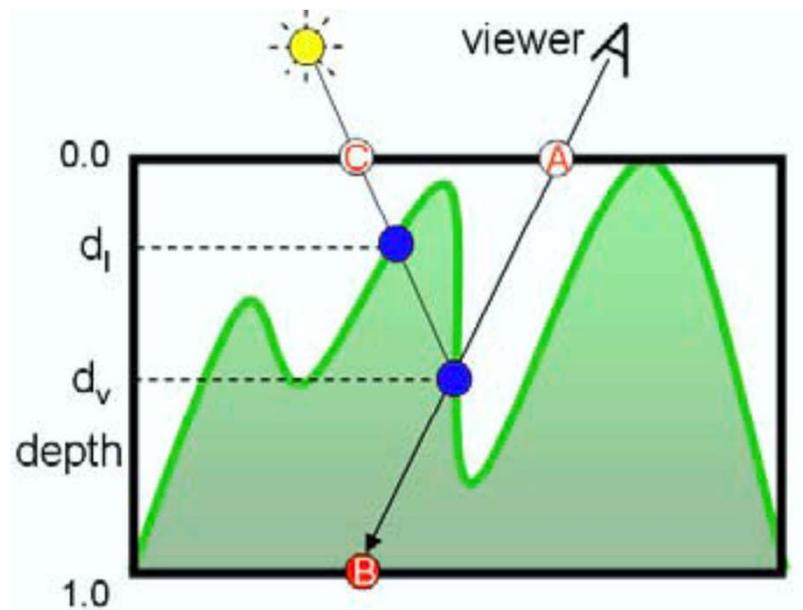
Combined Search

- To find first point under surface, start at A, advance ray by δ
- δ is a function of the angle between VD' and interpolated fragment normal
- Proceed with binary search
(with less iterations)



Shadowing

- Visibility problem
- Determine if light ray intersects surface
- Do not need to know the exact point

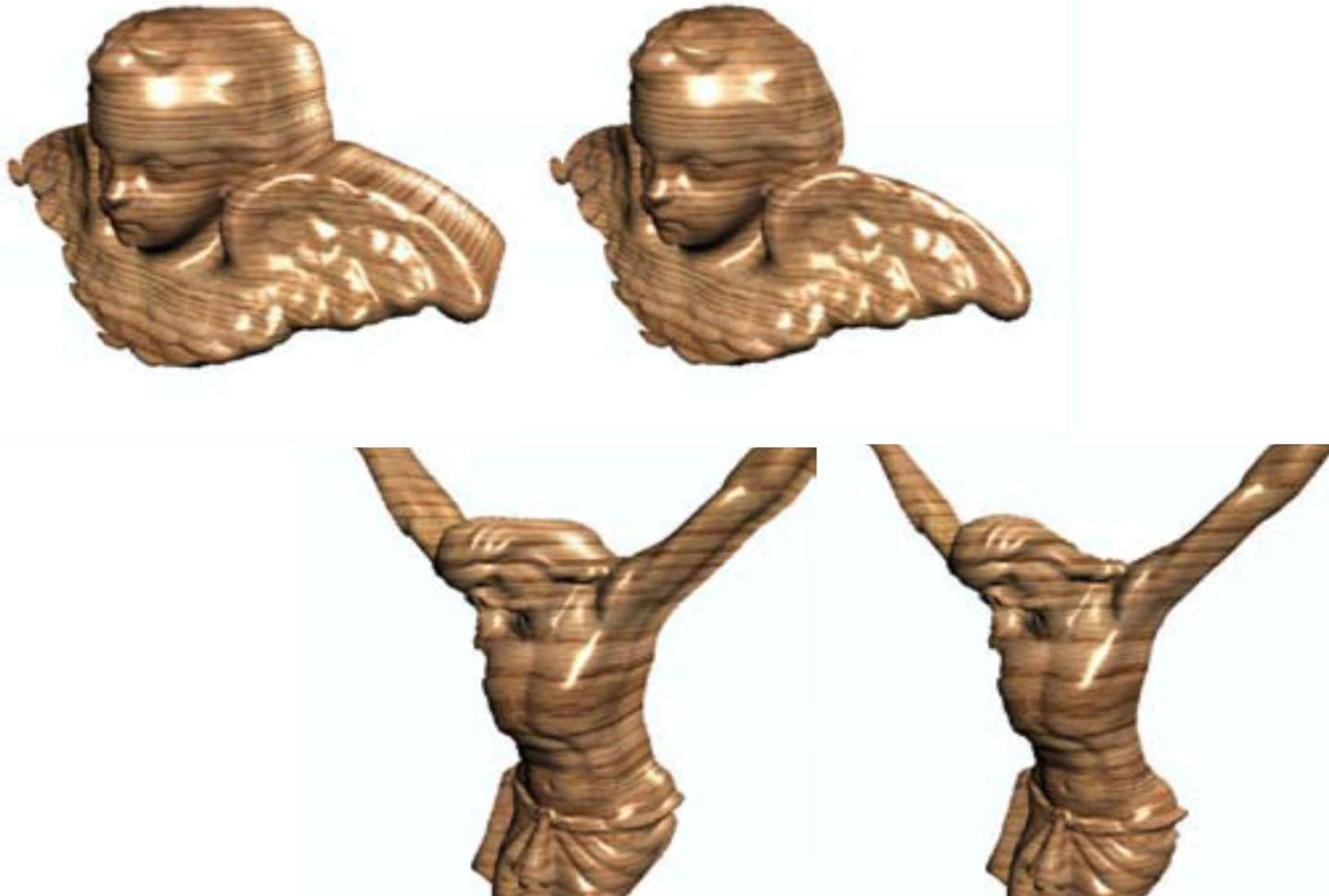


Dual Depth Relief Textures

- Represent opaque, closed surfaces with only one texture
- Second “back” layer is not used for rendering, but as a constraint for ray-height-field intersection



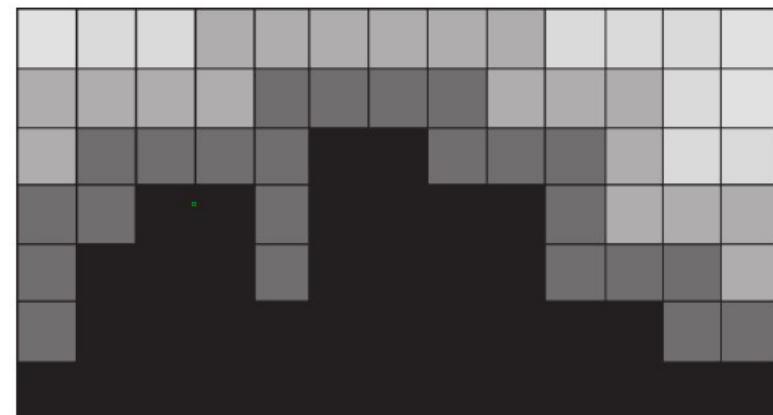
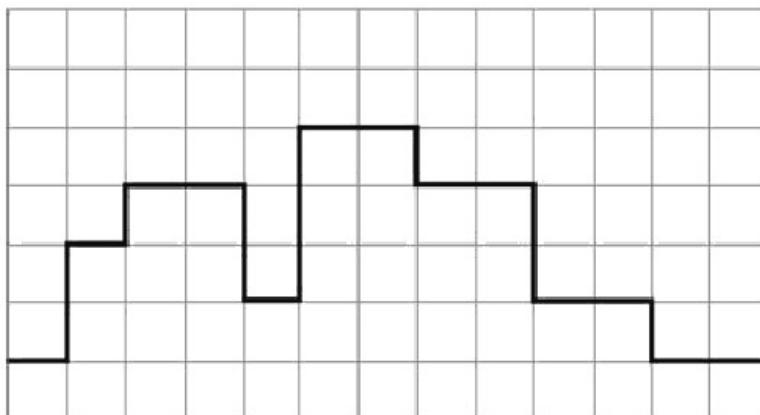
Dual Depth Relief Textures



Sphere Tracing

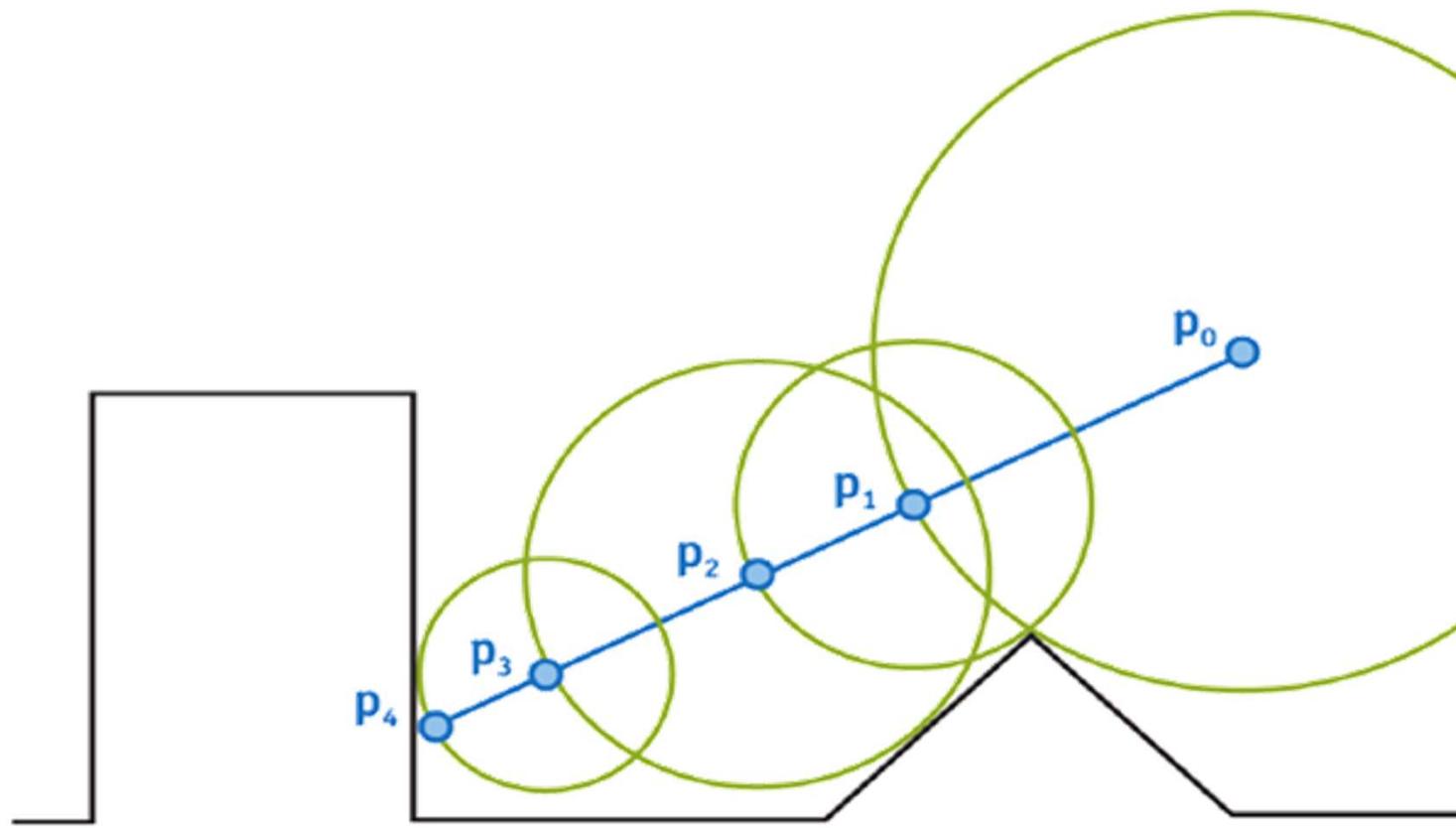
- Store distance to closest surface in 3D map

1	3	4	4	2	5	5	4	4	2	2	1	1
---	---	---	---	---	---	---	---	---	---	---	---	---



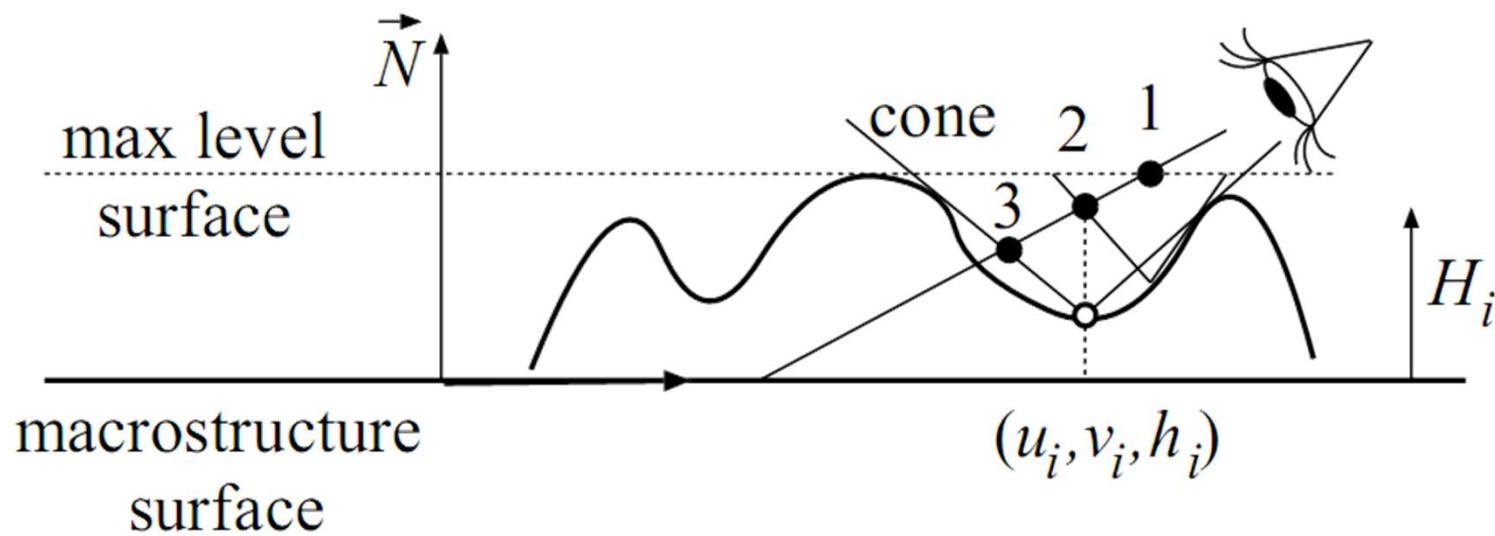
Sphere Tracing

- Distance is sphere radius for search step



Cone Stepping

- Texel stores cone of empty space above
- Only store opening angle (2D texture suffices!)





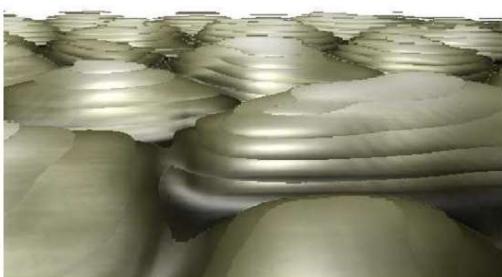
texture mapping



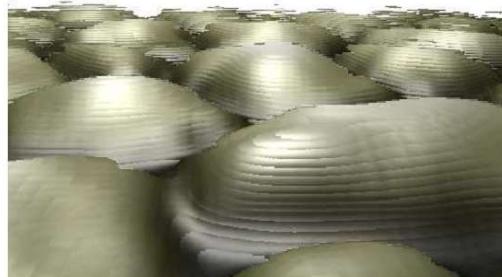
bump mapping



parallax mapping



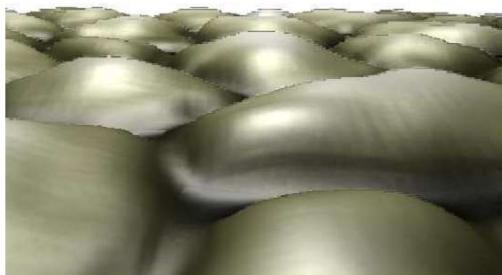
ray marching



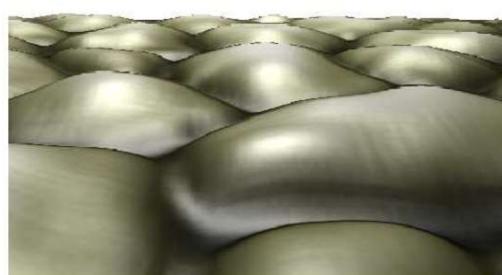
binary search



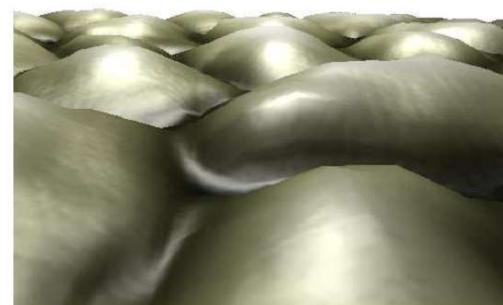
sphere tracing



relief mapping



cone stepping

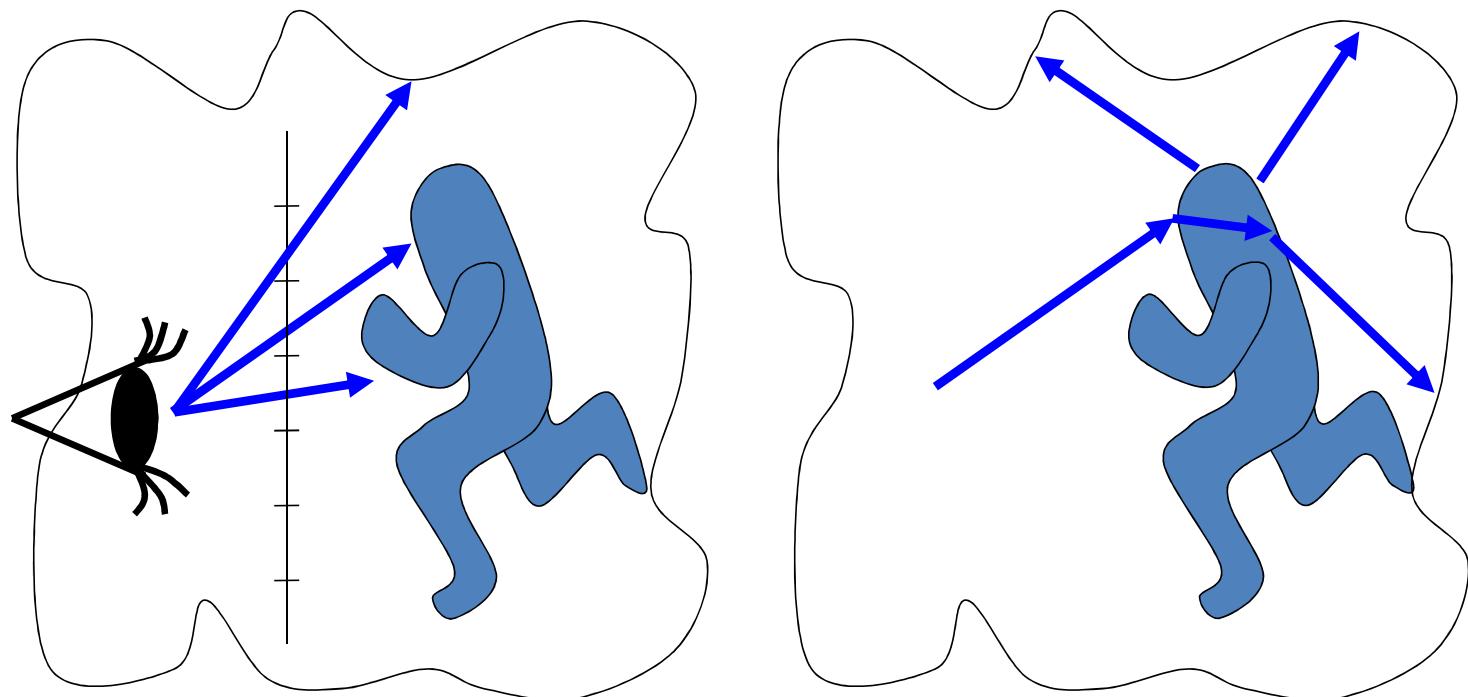


per-vertex displacement mapping

Speed considerations

- Parallax-normal mapping
 - ~ 20 ALU instructions
- Relief-mapping
 - Marching and binary search:
 - ~300 ALU instructions
 - + lots of texture lookups

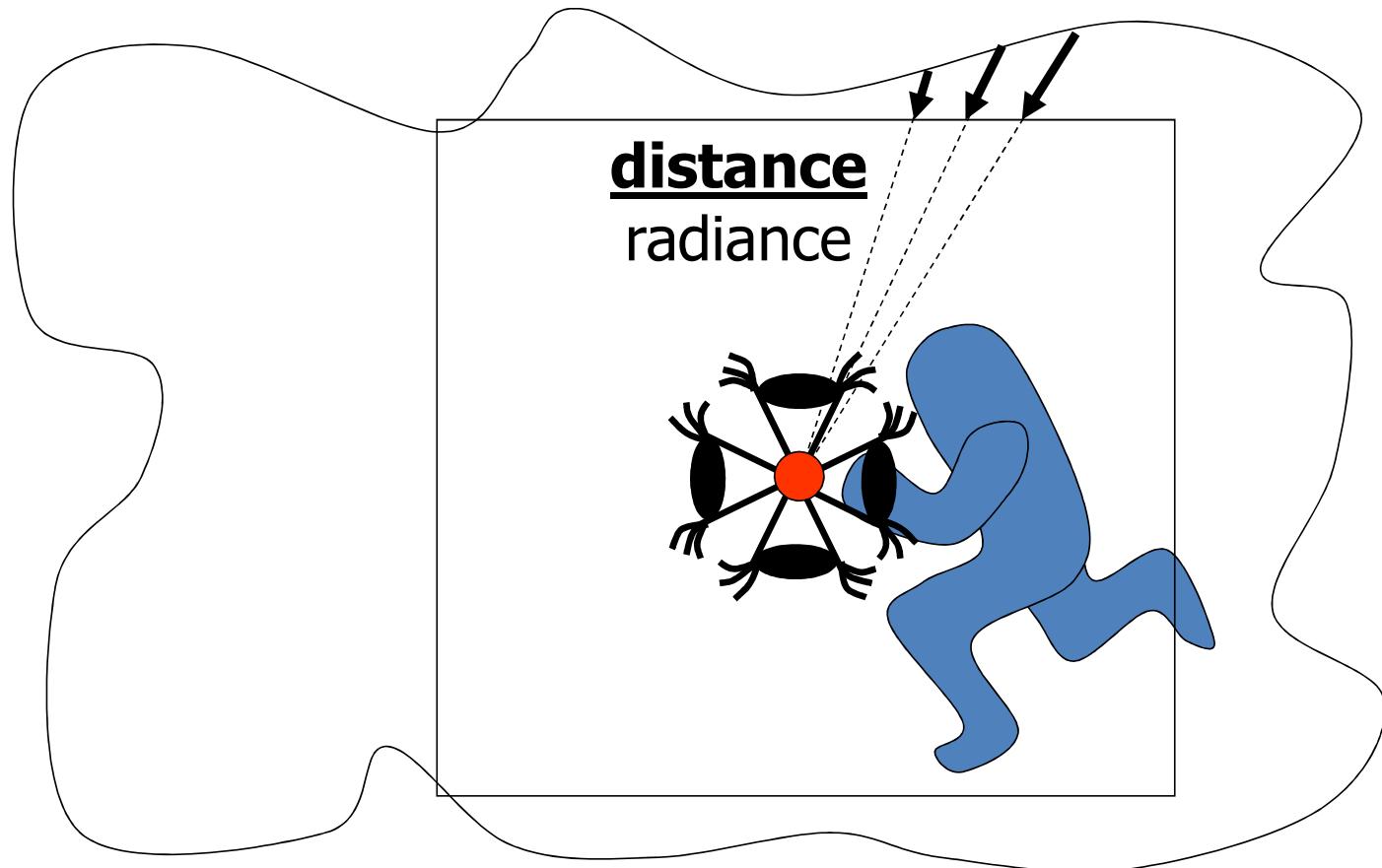
Rasterization versus Ray-Tracing



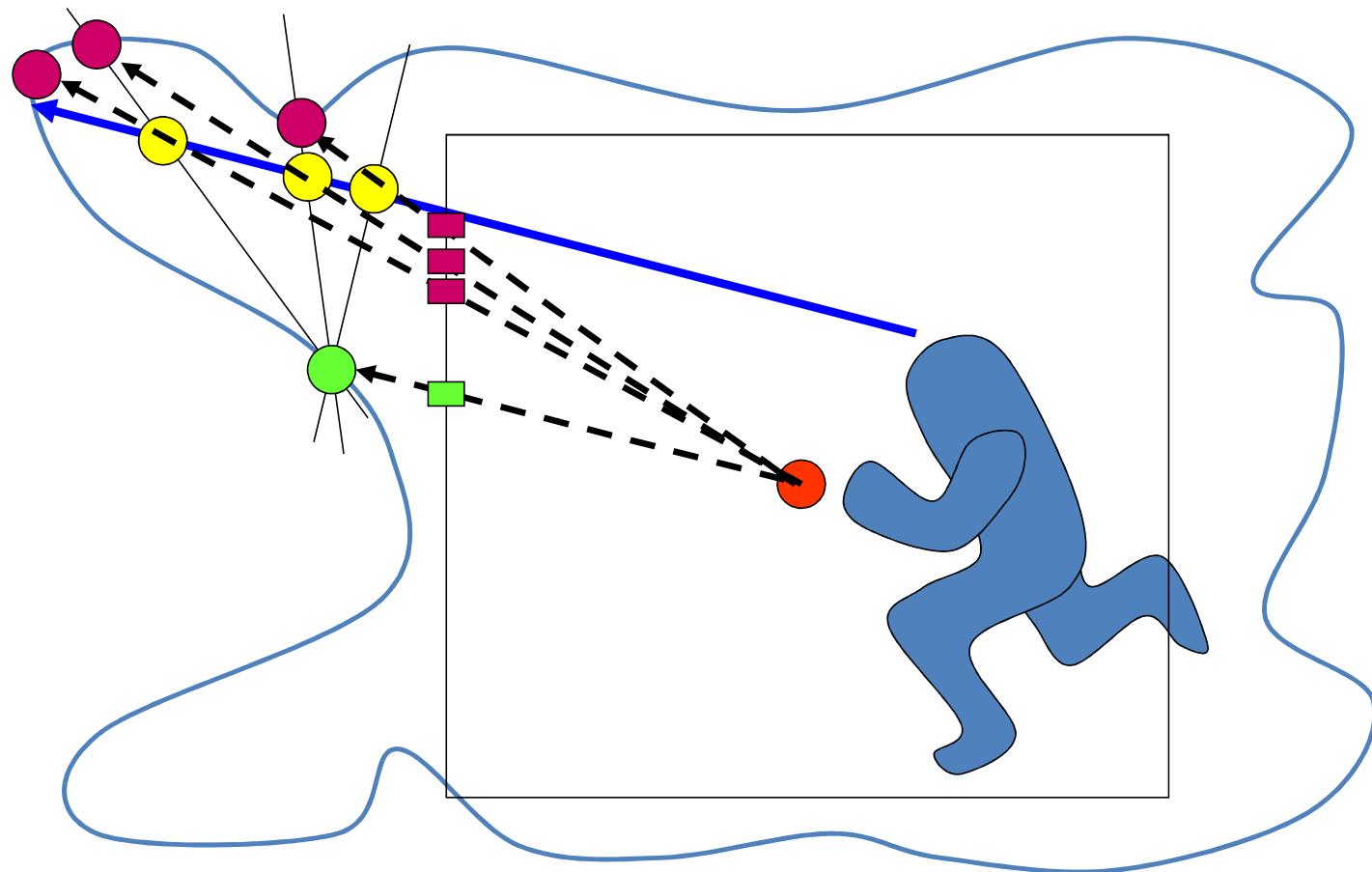
Incremental rendering
on the GPU

Non-coherent
Ray tracing

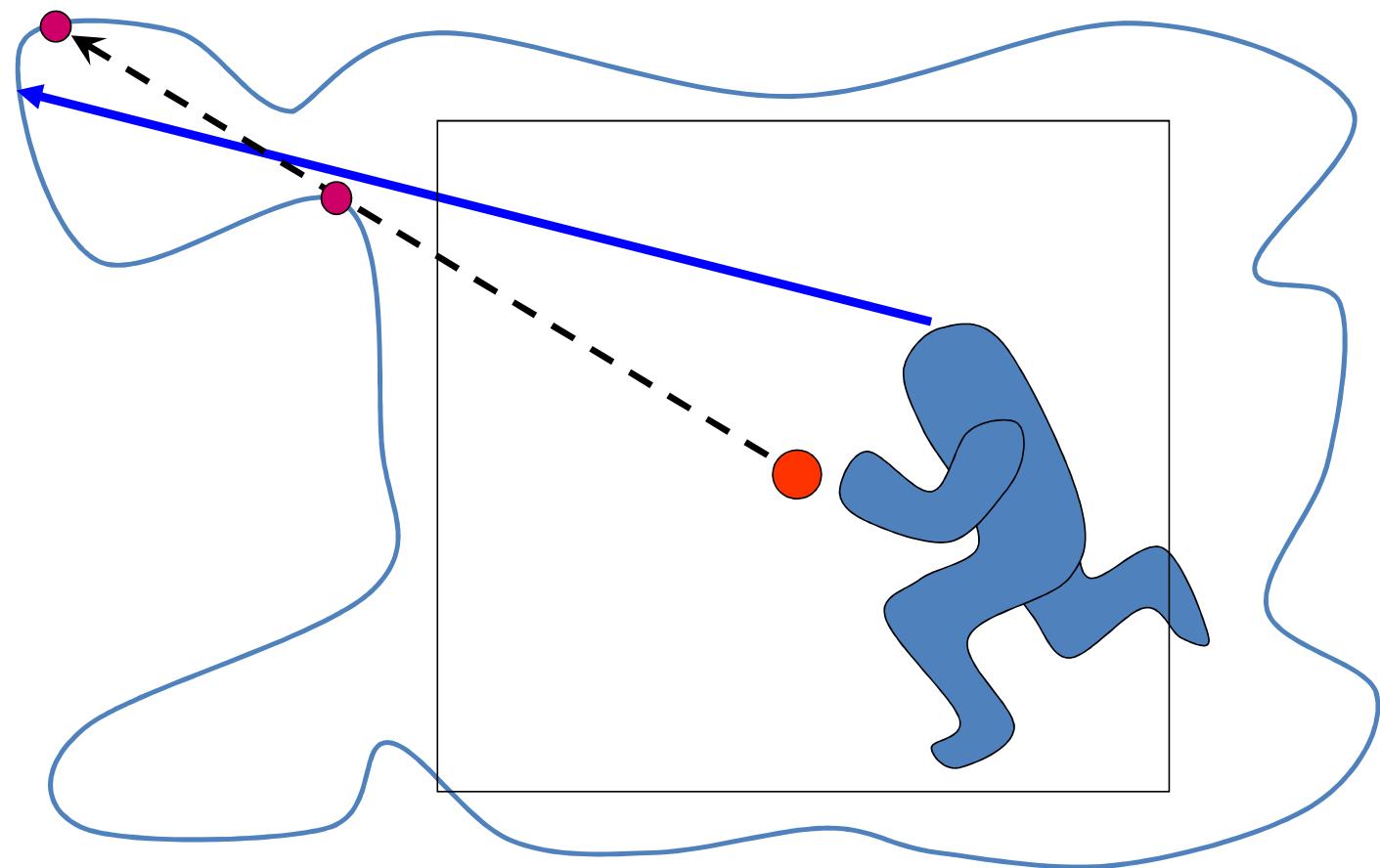
Distance Impostors



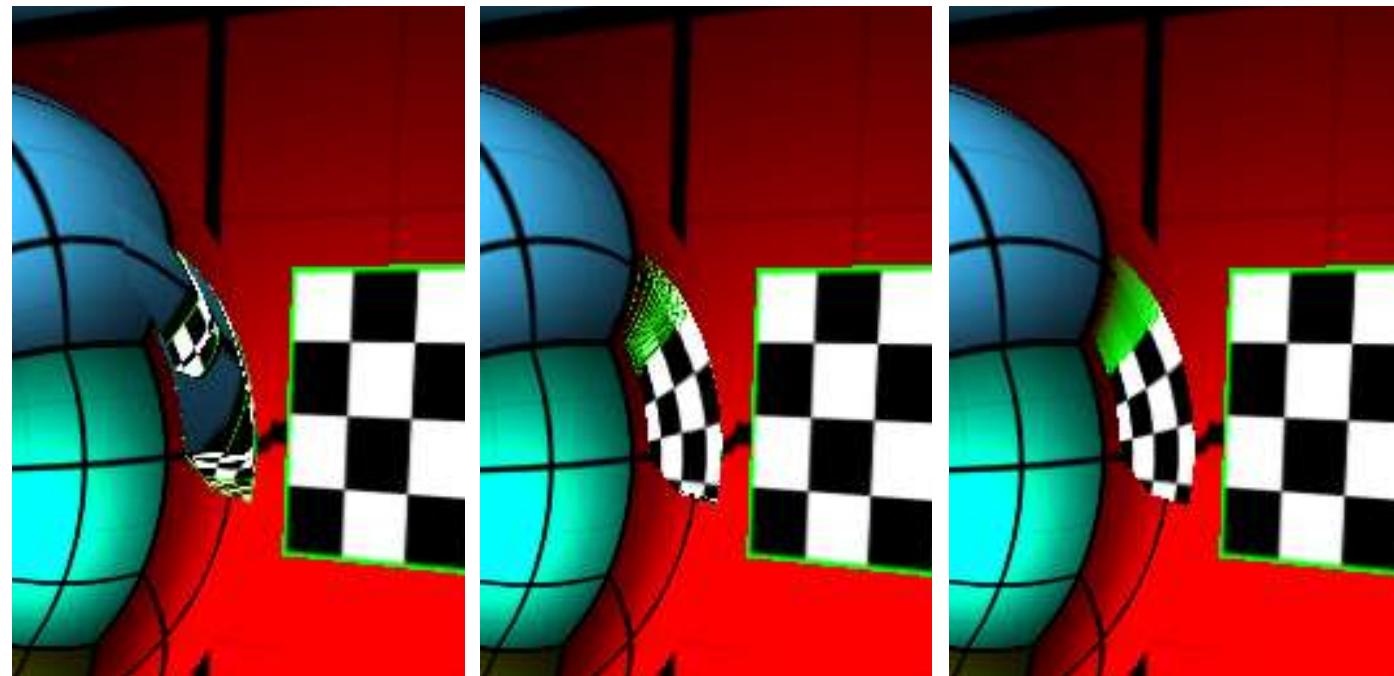
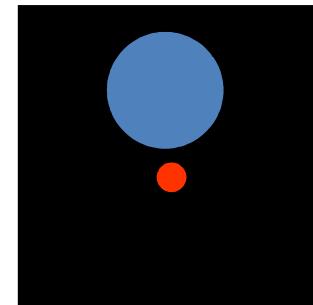
Ray-Tracing with Distance Impostors



Approximation



Approximation Error

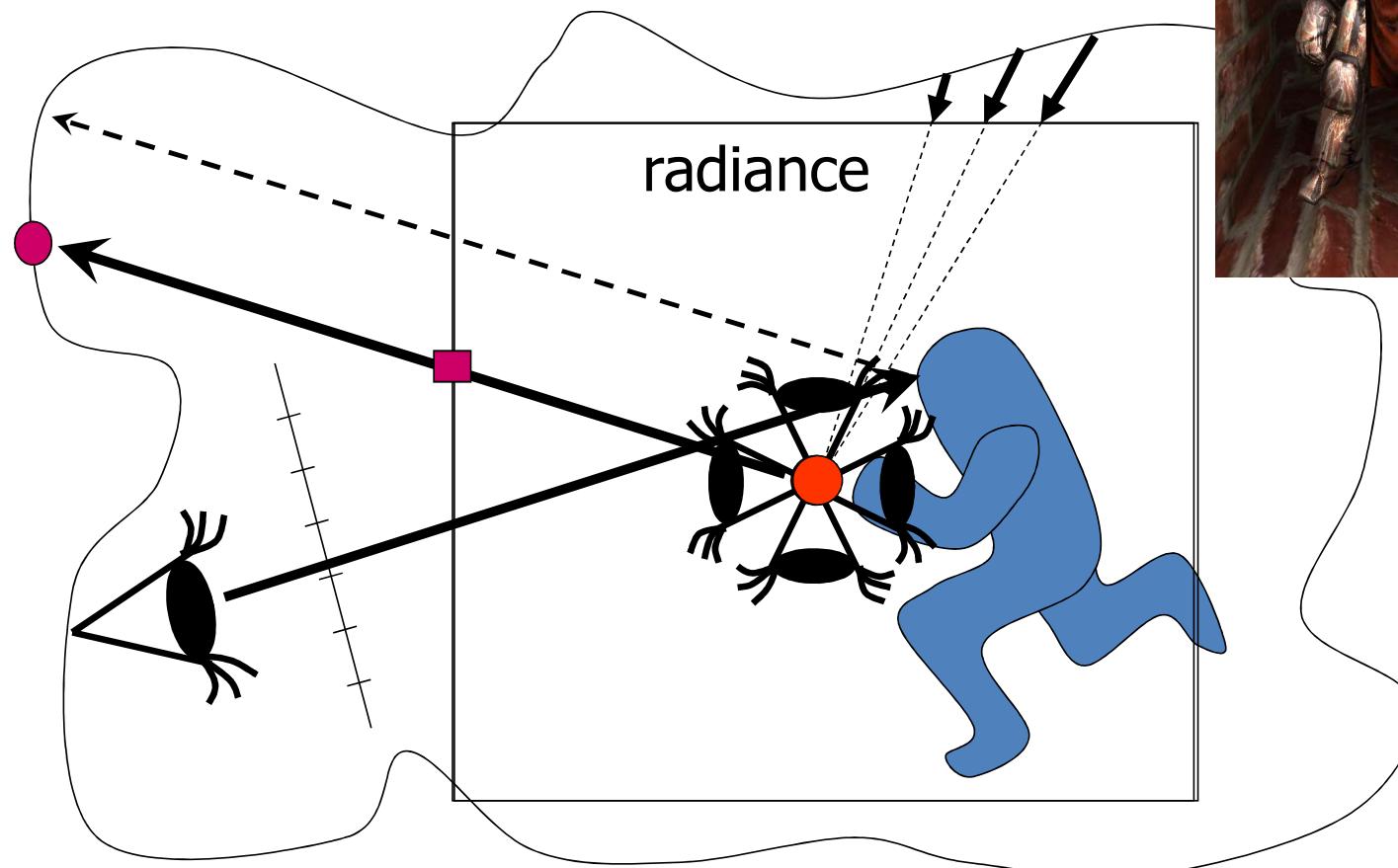


1 iteration

4 iterations

8 iterations

Reflections



Problems of environment map based reflections

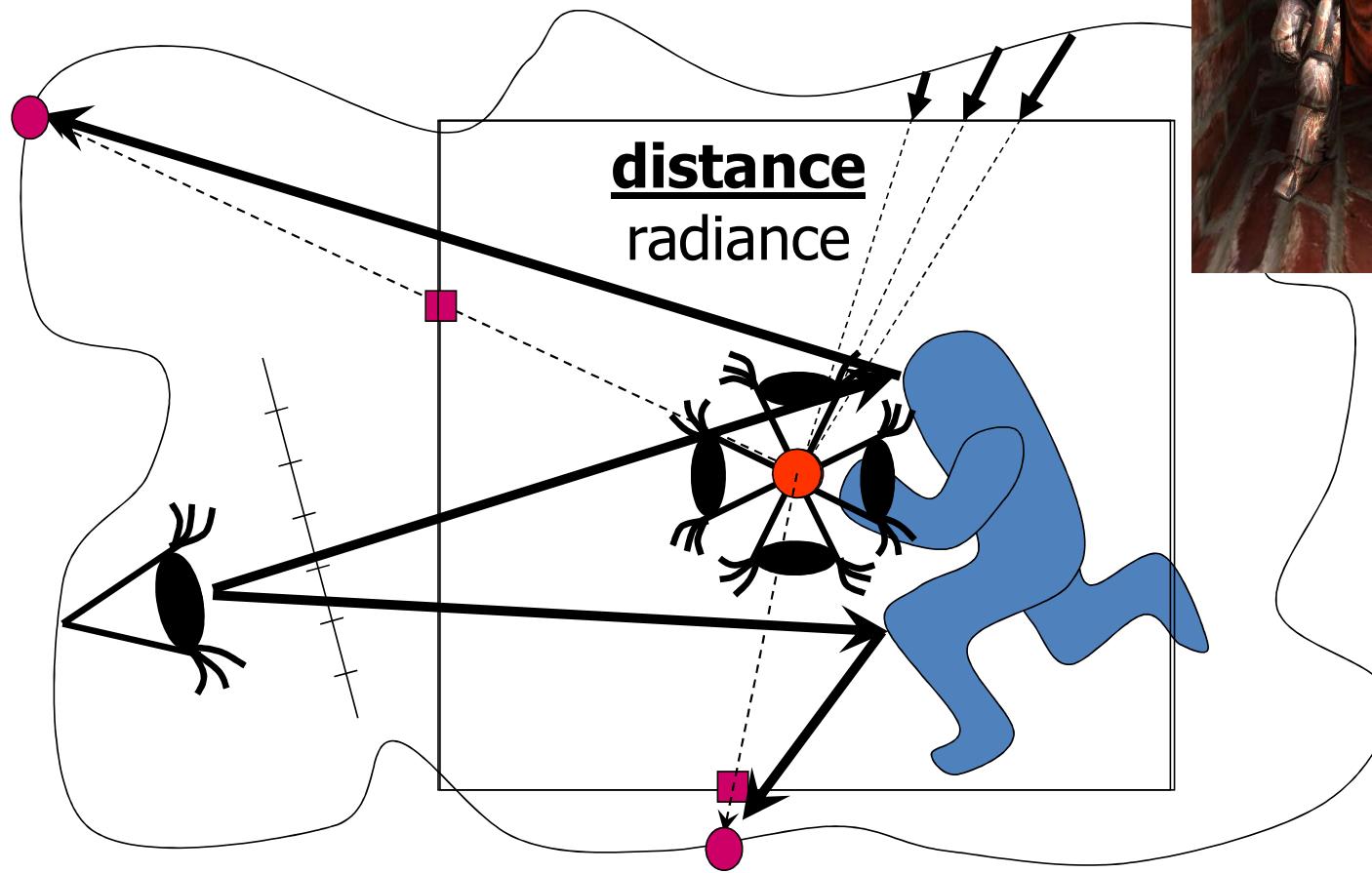


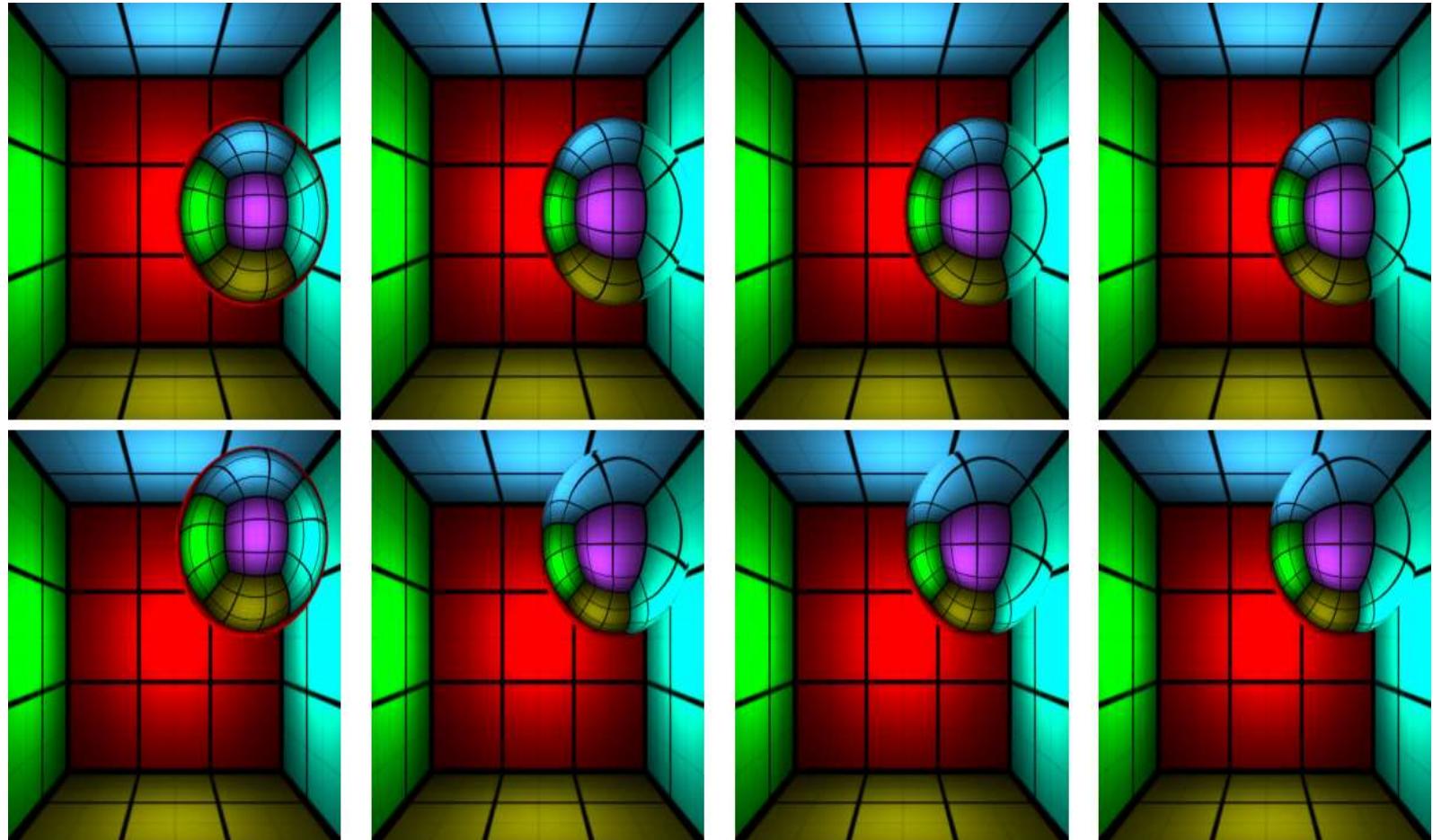
Environment map



Reference

Localized Reflections





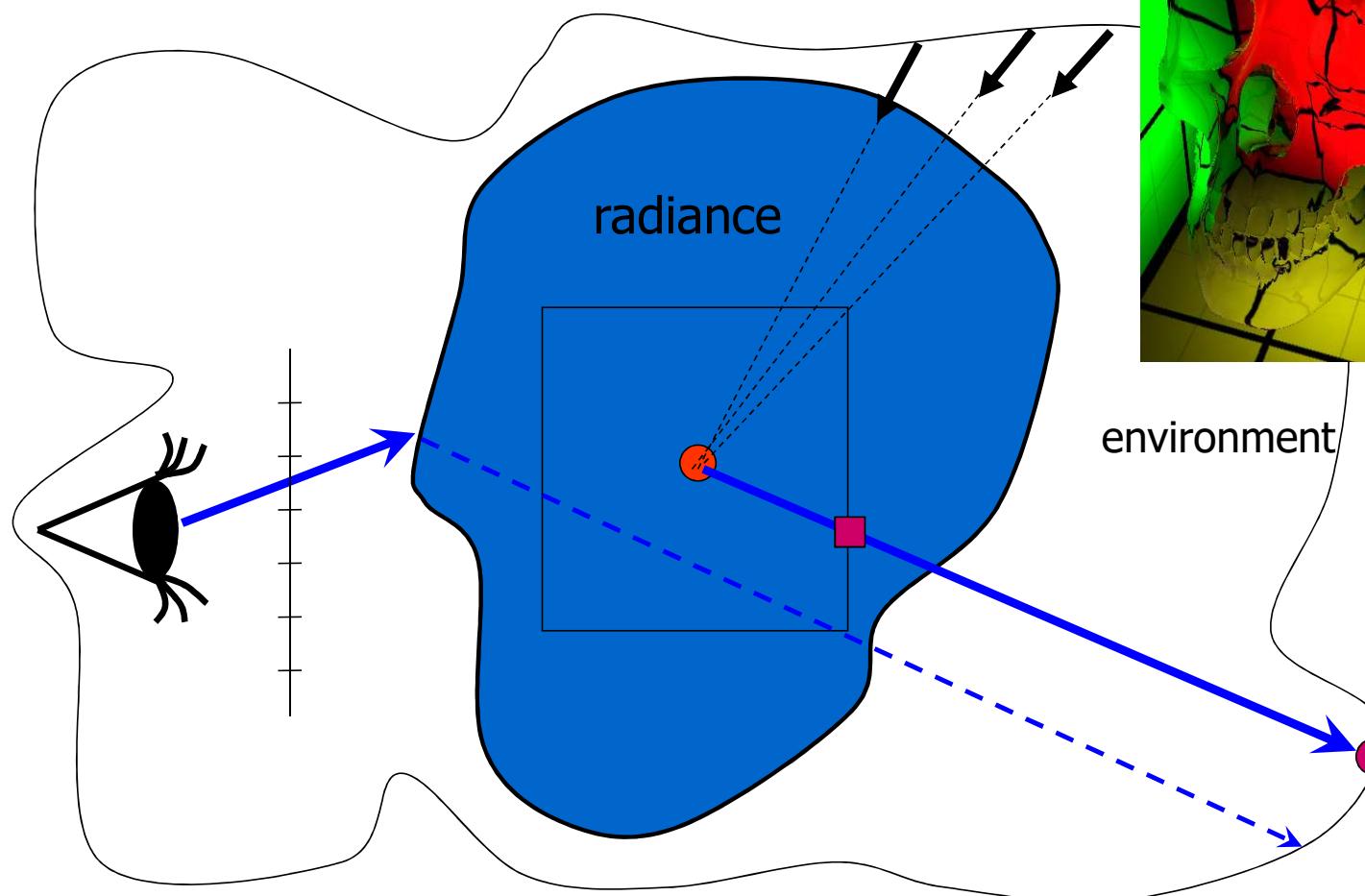
classical environment map
642 FPS

distance impostor
447 FPS

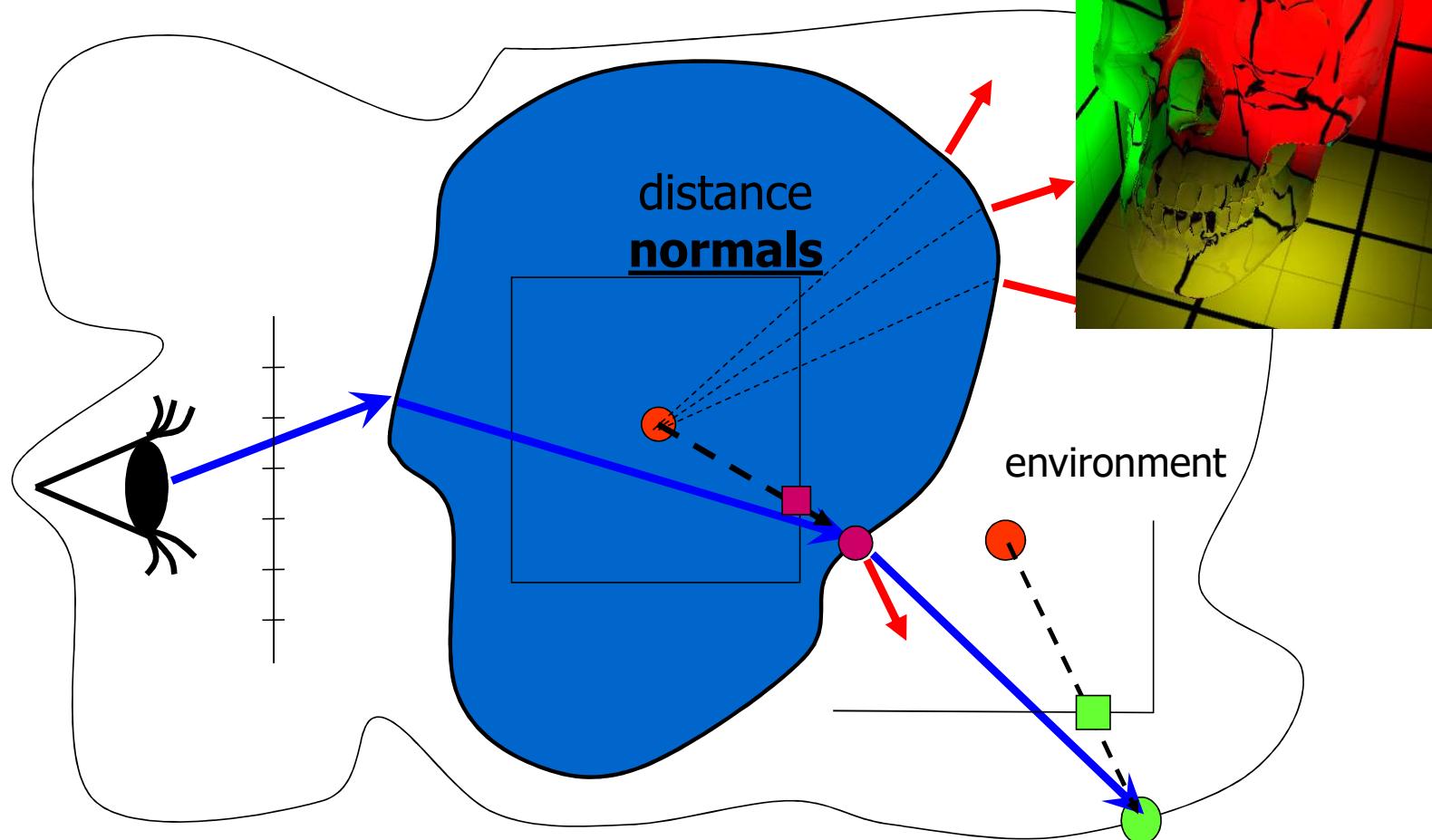
+1 iteration
323 FPS

ray traced reference

Refractions



Multiple Localized Refract



Multiple Localized Refractions

