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In [1]: from pycoingecko import CoinGeckoAPI
import pandas as pd
import numpy as np
import seaborn as sns
from statsmodels.tsa.stattools import adfuller, acf
from statsmodels.graphics.tsaplots import plot_acf
from sklearn.decomposition import FactorAnalysis
from sklearn.preprocessing import MinMaxScaler
from sklearn.decomposition import PCA
from factor_analyzer import FactorAnalyzer
from sklearn.cluster import KMeans
import matplotlib.pyplot as plt
from sklearn.linear_model import LinearRegression
from factor_analyzer.factor_analyzer import calculate_bartlett_sphericity
from factor_analyzer.factor_analyzer import calculate_kmo
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In [2]: # Calling Coin Gecko API
## Import the data
#cg = CoinGeckoAPI()
#coins_market = cg.get_coins_markets('usd')
#df_coins_market = pd.DataFrame(coins_market)
```

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In [3]: ## Get the prices for each crypto for 365 days (01.01.19 - 31.12.19)
)
#prices = []
#for i in df_coins_market['id']:
#    a = cg.get_coin_market_chart_range_by_id(i, 'usd', 1546300800, 1577750400)
#    b = a['prices']
#    c = []
#    for j in range(len(b)):
#        c.append(b[j][1])
#    prices.append([i, c])
#del a, b, c, i, j

## Creating the prices, returns and market caps dataframes

#frame = pd.DataFrame(prices)
#coins = frame[1].apply(pd.Series)
#frame = coins.set_index(frame[0])
#frame = frame.dropna(axis=0).transpose()
#frame.to_csv('CC_Prices.csv', index=True, header=True)

# Returns
#returns_data = np.log(frame) - np.log(frame.shift(1))
#returns_data = returns_data[1:]
#returns_data.to_csv('CC_LogReturns.csv', index=True, header=True)

# To ensure working with same figures, we will not generate above df each time.
# Then, we saved them into csv to import them just below.

# Importing different df
# Prices
prices_data = pd.read_csv('CC_Prices.csv')
prices_data = prices_data.drop(['Unnamed: 0'], axis = 1)
# Returns
returns_data = pd.read_csv('CC_LogReturns.csv')
returns_data = returns_data.drop(['Unnamed: 0'], axis = 1)
# Market caps
market_cap = pd.read_csv('CC_MarketCaps.csv')
market_cap = market_cap.drop(['Unnamed: 0'], axis = 1)
```

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In [4]: # Exploratory Analysis

# 1) Plotting the prices over the period of various combinations of coins
# 2) CCs returns and market caps
# 3) Stationarity test
# 4) Autocorrelation test
# 5) Statistical summary of cc
# 6) Scatterplot of correlated cc
# 7) Explorative Clustering with K-Means
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In [5]: # Exploratory Analysis
# 1) Plotting the prices over the period of various combinations of
coins

plt.plot(prices_data['bitcoin'])
plt.title('Price Bitcoin')
plt.xlabel('Time in Days')
plt.ylabel('Price in USD')
plt.show()
plt.savefig('Data_Analysis/Bitcoin.jpeg', bbox_inches='tight')
plt.clf()

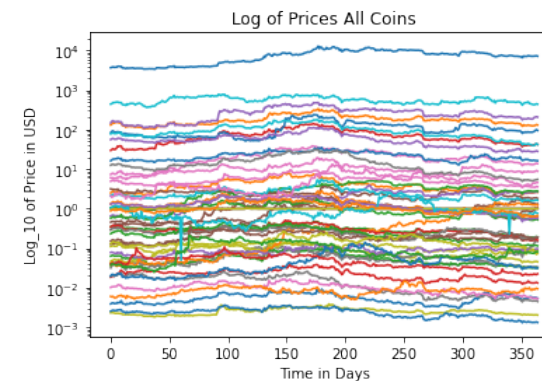
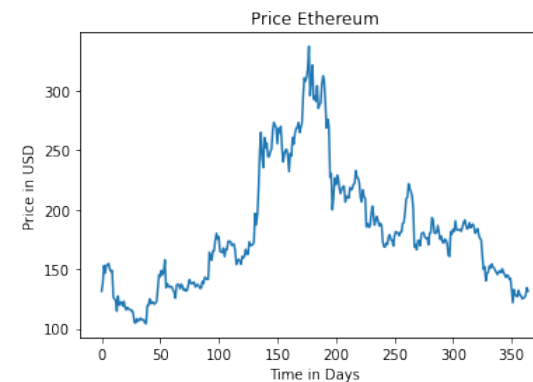
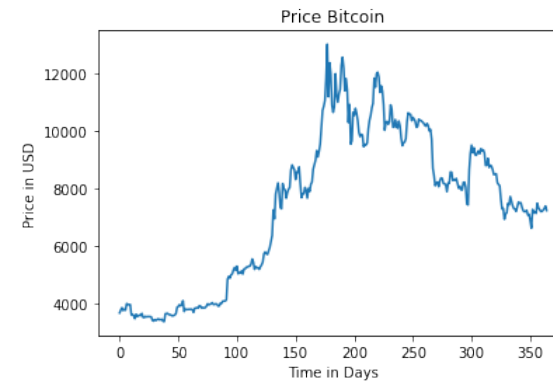
plt.plot(prices_data['ethereum'])
plt.title('Price Ethereum')
plt.xlabel('Time in Days')
plt.ylabel('Price in USD')
plt.show()
plt.savefig('Data_Analysis/Ether.jpeg', bbox_inches='tight')
plt.clf()

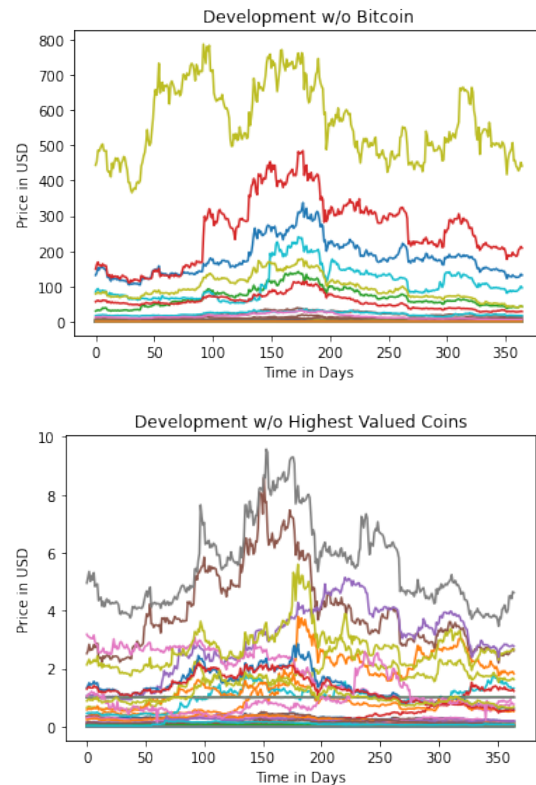
plt.plot(prices_data)
plt.yscale('log')
plt.title('Log of Prices All Coins')
plt.xlabel('Time in Days')
plt.ylabel('Log10 of Price in USD')
plt.show()
plt.savefig('Data_Analysis/Log_All_coins.jpeg', bbox_inches='tight')
plt.clf()

plt.plot(prices_data.drop('bitcoin', axis=1))
plt.title('Development w/o Bitcoin')
plt.xlabel('Time in Days')
plt.ylabel('Price in USD')
plt.show()
plt.savefig('Data_Analysis/w_o_Bitcoin.jpeg',bbox_inches='tight')
plt.clf()

plt.plot(prices_data.drop(['bitcoin', 'ethereum', 'dash', 'neo', 'z
cash', 'maker', 'bitcoin-cash', 'litecoin', 'bitcoin-cash-sv', 'dec
red', 'bitcoin-gold', 'quant-network', 'binancecoin'], axis=1))
plt.title('Development w/o Highest Valued Coins')
plt.xlabel('Time in Days')
plt.ylabel('Price in USD')
plt.show()
plt.savefig('Data_Analysis/w_o_highest.jpeg', bbox_inches='tight')
plt.clf()

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In [6]: # Exploratory Analysis
# 2) CCs logreturns and prices/market caps

# 2.A) CCs logreturns

mean_returns = returns_data.mean(axis=0) # mean of 2019 log returns
for each cc
cum_returns = returns_data.sum(axis=0) # cumulative log returns in
2019 for each cc

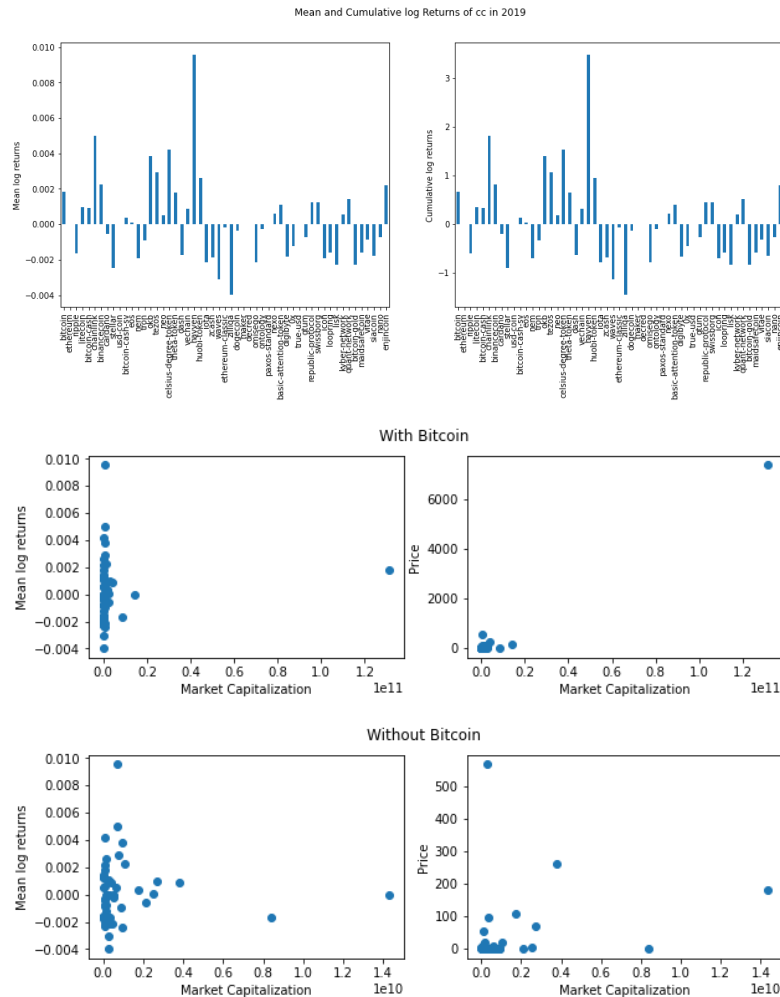
# Plotting mean and cumulative returns of 2019 for each cc
fig, axes = plt.subplots(nrows=1, ncols=2, figsize=(10,3))
mean_returns.plot(ax=axes[0], kind='bar')
axes[0].set_ylabel('Mean log returns')
cum_returns.plot(ax=axes[1], kind='bar')
axes[1].set_ylabel('Cumulative log returns')
fig.set_size_inches(16, 6)
fig.suptitle('Mean and Cumulative log Returns of cc in 2019')
fig.savefig('Data_Analysis/returns.jpeg', transparent=True, bbox_in
ches='tight')

# 2.B) Market Caps consideration with mean returns and prices

mean_price = prices_data.mean()

# 2.B.i) Scatter plots of MarketCap-MeanReturns and MarketCaps-Pri
ces (with bitcoin)
fig, axes = plt.subplots(nrows=1, ncols=2, figsize=(10,3))
axes[0].scatter(market_cap, mean_returns)
axes[0].set_xlabel('Market Capitalization')
axes[0].set_ylabel('Mean log returns')
axes[1].scatter(market_cap, mean_price)
axes[1].set_xlabel('Market Capitalization')
axes[1].set_ylabel('Price')
fig.suptitle('With Bitcoin')
fig.savefig('Data_Analysis/scatter.jpeg', transparent=True, bbox_in
ches='tight')

# 2.B.ii) Scatter plots of MarketCap-MeanReturns and MarketCaps-Pri
ces (without bitcoin)
fig, axes = plt.subplots(nrows=1, ncols=2, figsize=(10,3))
axes[0].scatter(market_cap[1:], mean_returns[1:])
axes[0].set_xlabel('Market Capitalization')
axes[0].set_ylabel('Mean log returns')
axes[1].scatter(market_cap[1:], mean_price[1:])
axes[1].set_xlabel('Market Capitalization')
axes[1].set_ylabel('Price')
fig.suptitle('Without Bitcoin')
fig.savefig('Data_Analysis/scatter_without.jpeg', transparent=True,
bbox_inches='tight')
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In [7]: # Exploratory Analysis
# 3) Stationarity Test

# initialization
cc_names = returns_data.columns # columns names of returns db (= cr
yptos)
nb_cc = len(cc_names) # number of cc

# testing stationarity, from https://www.hackdeploy.com/augmented-d
ickey-fuller-test-in-python/

class StationarityTests: # implementing a class of functions to tes
t stationarity
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def __init__(self, significance=.05):
    self.SignificanceLevel = significance
    self.pValue = None
    self.isStationary = None

def ADF_Stationarity_Test(self, timeseries, printResults = True
):

    #Dickey-Fuller test:
    adfTest = adfuller(timeseries, autolag='AIC')

    self.pValue = adfTest[1]

    if (self.pValue<self.SignificanceLevel):
        self.isStationary = True
    else:
        self.isStationary = False

    if printResults:
        dfResults = pd.Series(adfTest[0:4], index=[ 'ADF Test St
atistic', 'P-Value', '# Lags Used', '# Observations Used'])

        #Add Critical Values
        for key,value in adfTest[4].items():
            dfResults['Critical Value (%)'%key] = value

        print('Augmented Dickey-Fuller Test Results:')
        print(dfResults)

statio_cc = [] # creating a matrix which will give if cc are statio
nary or not
for i in cc_names:
    sTest = StationarityTests()
    sTest.ADF_Stationarity_Test(returns_data[i],printResults = True
)
    print("Is the time series stationary? {0}".format(sTest.isStati
onary))
    statio_cc.append([i,sTest.isStationary])

statio_cc = pd.DataFrame(statio_cc) # converting it to a panda df
statio_cc.index = cc_names; statio_cc.columns = ["cc","Stationary"]
statio_cc = statio_cc['Stationary']

# exporting it to a csv
statio_cc.to_csv('Data_Analysis/statio_cc.csv',index = True,header
= True)

del i,sTest # deleting useless variables
```

```
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -19.786298
P-Value                 0.000000
# Lags Used             0.000000
# Observations Used     363.000000
Critical Value (1%)     -3.448494
Critical Value (5%)     -2.869535
Critical Value (10%)    -2.571029
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dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -20.576621
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -1.510723e+01
P-Value                  7.787822e-28
# Lags Used              1.000000e+00
# Observations Used      3.620000e+02
Critical Value (1%)      -3.448544e+00
Critical Value (5%)      -2.869557e+00
Critical Value (10%)     -2.571041e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -18.924694
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -19.712866
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -20.545566
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -19.175157
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000

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Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -20.227707
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -1.411358e+01
P-Value                  2.495172e-26
# Lags Used              1.000000e+00
# Observations Used      3.620000e+02
Critical Value (1%)      -3.448544e+00
Critical Value (5%)      -2.869557e+00
Critical Value (10%)     -2.571041e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -1.349253e+01
P-Value                  3.086296e-25
# Lags Used              3.000000e+00
# Observations Used      3.600000e+02
Critical Value (1%)      -3.448646e+00
Critical Value (5%)      -2.869602e+00
Critical Value (10%)     -2.571065e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -5.752633e+00
P-Value                  5.917885e-07
# Lags Used              8.000000e+00
# Observations Used      3.550000e+02
Critical Value (1%)      -3.448906e+00
Critical Value (5%)      -2.869716e+00
Critical Value (10%)     -2.571126e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -20.972097
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -6.853173e+00

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P-Value          1.674041e-09
# Lags Used       4.000000e+00
# Observations Used 3.590000e+02
Critical Value (1%) -3.448697e+00
Critical Value (5%) -2.869625e+00
Critical Value (10%) -2.571077e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic -18.957967
P-Value           0.000000
# Lags Used       0.000000
# Observations Used 363.000000
Critical Value (1%) -3.448494
Critical Value (5%) -2.869535
Critical Value (10%) -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic -1.829869e+01
P-Value           2.289063e-30
# Lags Used       0.000000e+00
# Observations Used 3.630000e+02
Critical Value (1%) -3.448494e+00
Critical Value (5%) -2.869535e+00
Critical Value (10%) -2.571029e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic -8.310567e+00
P-Value           3.798940e-13
# Lags Used       5.000000e+00
# Observations Used 3.580000e+02
Critical Value (1%) -3.448749e+00
Critical Value (5%) -2.869647e+00
Critical Value (10%) -2.571089e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic -19.004528
P-Value           0.000000
# Lags Used       0.000000
# Observations Used 363.000000
Critical Value (1%) -3.448494
Critical Value (5%) -2.869535
Critical Value (10%) -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic -1.667601e+01
P-Value           1.530571e-29
# Lags Used       1.000000e+00
# Observations Used 3.620000e+02
Critical Value (1%) -3.448544e+00
Critical Value (5%) -2.869557e+00
Critical Value (10%) -2.571041e+00
dtype: float64
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Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic -9.293486e+00
P-Value           1.162775e-15
# Lags Used       3.000000e+00
# Observations Used 3.600000e+02
Critical Value (1%) -3.448646e+00
Critical Value (5%) -2.869602e+00
Critical Value (10%) -2.571065e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic -1.820070e+01
P-Value           2.406276e-30
# Lags Used       0.000000e+00
# Observations Used 3.630000e+02
Critical Value (1%) -3.448494e+00
Critical Value (5%) -2.869535e+00
Critical Value (10%) -2.571029e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic -20.673967
P-Value           0.000000
# Lags Used       0.000000
# Observations Used 363.000000
Critical Value (1%) -3.448494
Critical Value (5%) -2.869535
Critical Value (10%) -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic -1.575759e+01
P-Value           1.202422e-28
# Lags Used       1.000000e+00
# Observations Used 3.620000e+02
Critical Value (1%) -3.448544e+00
Critical Value (5%) -2.869557e+00
Critical Value (10%) -2.571041e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic -1.862336e+01
P-Value           2.060393e-30
# Lags Used       0.000000e+00
# Observations Used 3.630000e+02
Critical Value (1%) -3.448494e+00
Critical Value (5%) -2.869535e+00
Critical Value (10%) -2.571029e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic -20.825826
P-Value           0.000000
# Lags Used       0.000000
# Observations Used 363.000000
Critical Value (1%) -3.448494
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Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -21.129376
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -21.190128
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -20.580488
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -20.057417
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -7.968188e+00
P-Value                  2.827586e-12
# Lags Used              8.000000e+00
# Observations Used      3.550000e+02
Critical Value (1%)      -3.448906e+00
Critical Value (5%)      -2.869716e+00
Critical Value (10%)     -2.571126e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -20.263258
P-Value                  0.000000

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# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -20.951633
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -19.296688
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -20.111680
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -1.403604e+01
P-Value                  3.368036e-26
# Lags Used              3.000000e+00
# Observations Used      3.600000e+02
Critical Value (1%)      -3.448646e+00
Critical Value (5%)      -2.869602e+00
Critical Value (10%)     -2.571065e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -1.301100e+01
P-Value                  2.568073e-24
# Lags Used              2.000000e+00
# Observations Used      3.610000e+02
Critical Value (1%)      -3.448595e+00
Critical Value (5%)      -2.869580e+00
Critical Value (10%)     -2.571053e+00
dtype: float64
Is the time series stationary? True

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Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -21.177564
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -1.302811e+01
P-Value                  2.376157e-24
# Lags Used              2.000000e+00
# Observations Used      3.610000e+02
Critical Value (1%)      -3.448595e+00
Critical Value (5%)      -2.869580e+00
Critical Value (10%)     -2.571053e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -20.451431
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -7.985504e+00
P-Value                  2.555473e-12
# Lags Used              8.000000e+00
# Observations Used      3.550000e+02
Critical Value (1%)      -3.448906e+00
Critical Value (5%)      -2.869716e+00
Critical Value (10%)     -2.571126e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -1.503771e+01
P-Value                  9.694212e-28
# Lags Used              1.000000e+00
# Observations Used      3.620000e+02
Critical Value (1%)      -3.448544e+00
Critical Value (5%)      -2.869557e+00
Critical Value (10%)     -2.571041e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -8.871350e+00
P-Value                  1.395223e-14
# Lags Used              5.000000e+00
# Observations Used      3.580000e+02
Critical Value (1%)      -3.448749e+00
Critical Value (5%)      -2.869647e+00

```

```

Critical Value (10%)     -2.571089e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -21.238390
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -21.837875
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -20.711441
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -7.902592e+00
P-Value                  4.146848e-12
# Lags Used              4.000000e+00
# Observations Used      3.590000e+02
Critical Value (1%)      -3.448697e+00
Critical Value (5%)      -2.869625e+00
Critical Value (10%)     -2.571077e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -1.042857e+01
P-Value                  1.633222e-18
# Lags Used              4.000000e+00
# Observations Used      3.590000e+02
Critical Value (1%)      -3.448697e+00
Critical Value (5%)      -2.869625e+00
Critical Value (10%)     -2.571077e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -20.653101
P-Value                  0.000000
# Lags Used              0.000000

```



```

# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -19.794544
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -7.405633e+00
P-Value                  7.357744e-11
# Lags Used              6.000000e+00
# Observations Used      3.570000e+02
Critical Value (1%)      -3.448801e+00
Critical Value (5%)      -2.869670e+00
Critical Value (10%)     -2.571101e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -1.398303e+01
P-Value                  4.144550e-26
# Lags Used              3.000000e+00
# Observations Used      3.600000e+02
Critical Value (1%)      -3.448646e+00
Critical Value (5%)      -2.869602e+00
Critical Value (10%)     -2.571065e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -8.227295e+00
P-Value                  6.196857e-13
# Lags Used              6.000000e+00
# Observations Used      3.570000e+02
Critical Value (1%)      -3.448801e+00
Critical Value (5%)      -2.869670e+00
Critical Value (10%)     -2.571101e+00
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:
ADF Test Statistic      -22.333999
P-Value                  0.000000
# Lags Used              0.000000
# Observations Used      363.000000
Critical Value (1%)      -3.448494
Critical Value (5%)      -2.869535
Critical Value (10%)     -2.571029
dtype: float64
Is the time series stationary? True
Augmented Dickey-Fuller Test Results:

```

```

ADF Test Statistic      -4.063051
P-Value                  0.001114
# Lags Used              10.000000
# Observations Used      353.000000
Critical Value (1%)      -3.449011
Critical Value (5%)      -2.869763
Critical Value (10%)     -2.571151
dtype: float64
Is the time series stationary? True

```

```

In [8]: # printing last df of interest: all cryptos seem to be stationary =
        good news
        print("True means that the considered cc is stationary while False
        means the opposite...")
        print("Houra. All cryptos seem to be stationary. Then, we can keep
        working with these time series.")

        print(statio_cc)

```

True means that the considered cc is stationary while False means the opposite...
 Houra. All cryptos seem to be stationary. Then, we can keep working with these time series.

bitcoin	True
ethereum	True
ripple	True
litecoin	True
bitcoin-cash	True
chainlink	True
binancecoin	True
cardano	True
stellar	True
usd-coin	True
bitcoin-cash-sv	True
eos	True
nem	True
tron	True
okb	True
tezos	True
neo	True
celsius-degree-token	True
theta-token	True
dash	True
vechain	True
havven	True
huobi-token	True
iota	True
zcash	True
waves	True
ethereum-classic	True
zilliqa	True
dogecoin	True
maker	True
decred	True
omisego	True
ontology	True
paxos-standard	True

nexo	True
basic-attention-token	True
digibyte	True
0x	True
true-usd	True
qtum	True
republic-protocol	True
swissborg	True
icon	True
loopring	True
lisk	True
kyber-network	True
quant-network	True
bitcoin-gold	True
maidsafecoin	True
vitae	True
siacoin	True
nano	True
enjincoin	True
Name: Stationary, dtype: bool	

```
In [9]: # Exploratory Analysis
# 4) Autocorrelation Test

# In this section, the autocorrelation of each cc is computed with
20 lags
# Autocorrelation plots will be shown for autocorrelated cc

#plot_acf(returns_data['bitcoin'], lags = 20, alpha = 0.05)
#ac_bitcoin = acf(returns_data['bitcoin'],nlags=20)

#for i in range(len(ac_bitcoin)):
#    if (ac_bitcoin[i]<0.035):
#        print(ac_bitcoin[i])

lags_names = [] # useful for below
for i in range(0,21):
    lags_names.append('lag' + str(i))

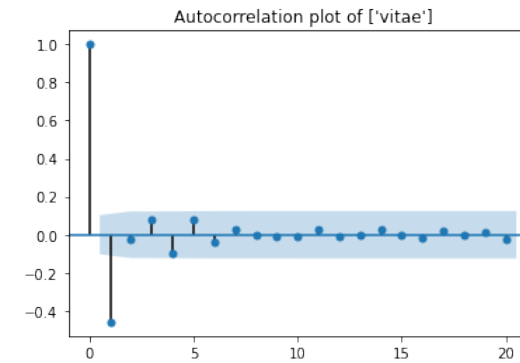
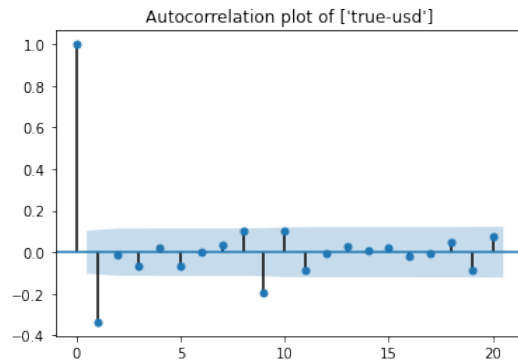
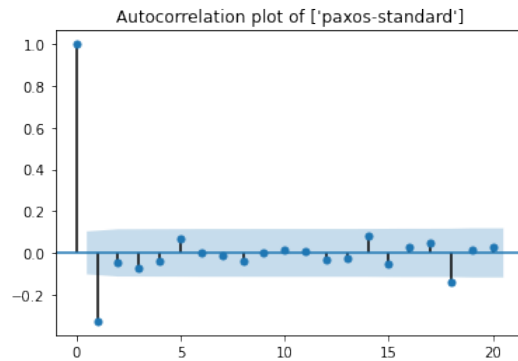
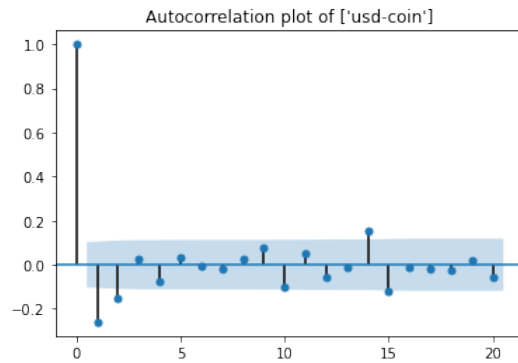
autocorr_cc = pd.DataFrame(np.zeros((21,nb_cc))) # creating autocorrelation matrix
autocorr_cc.columns = cc_names # adding cryptos names
autocorr_cc.index = lags_names # adding lags names
autocorrelated_cc = [] # creating a list to add the autocorrelated cryptos

for i in range(nb_cc): # making a loop to determine which cryptos are autocorrelated and add them to the list
    ccname = cc_names[i]
    autocorr_cc[ccname] = acf(returns_data[ccname],nlags = 20, fft=False)
    for j in range(len(autocorr_cc)):
        lagnb = 'lag'+ str(j)
        ac = autocorr_cc[ccname][lagnb]
        if ((ac >= 0.25 or ac <= -0.25) and ac != 1.):
            autocorrelated_cc.append([ccname])
    del ccname

print(str(len(autocorrelated_cc))+ " cryptocurrencies show autocorrelation with at least one of their last 20 lags.")

for i in range(len(autocorrelated_cc)): # autocorrelation plots for cryptos in the list
    ccname = autocorrelated_cc[i]
    plot_acf(returns_data[ccname], lags = 20, alpha = 0.05,title = 'Autocorrelation plot of ' + str(ccname))
    plt.savefig('Data_Analysis/acplt'+ str(ccname) + '.jpeg',transparent=True)
```

4 cryptocurrencies show autocorrelation with at least one of their last 20 lags.



```
In [10]: # Exploratory Analysis
# 5) Statistical summary of cc

# statistical summary of cryptos
summary_cc = returns_data.describe();
print(summary_cc)
summary_cc = summary_cc.transpose();

# plotting the histogram of logreturns mean for all cc
fig = plt.figure()
plt.hist(summary_cc['mean'])
plt.xlabel('Mean logreturn')
plt.ylabel('Frequency')
plt.title('Histogram of mean logreturns for all cc')
plt.xlim(-0.004, 0.010)
plt.ylim(0, 19)
plt.savefig('Data_Analysis/LogReturnsMean_Histogram.jpeg',transpare
nt=True)
plt.show()

# plotting the histogram of logreturns std for all cc
fig = plt.figure()
plt.hist(summary_cc['std'])
plt.xlabel('Logreturns Standard Deviation')
plt.ylabel('Frequency')
plt.title('Histogram of logreturns std for all cc')
plt.xlim(-0.004, 0.010)
plt.ylim(0, 19)
plt.savefig('Data_Analysis/LogReturnsStd_Histogram.jpeg',transparen
t=True)
plt.show()
```

	bitcoin	ethereum	ripple	litecoin	bitcoin-c
count	364.000000	3.640000e+02	364.000000	364.000000	364.000000
mean	0.001850	7.129810e-08	-0.001626	0.000961	0.000923
std	0.035509	4.246187e-02	0.036729	0.048855	0.053251

min	-0.150643	-1.753563e-01	-0.130690	-0.159533	-0.280
861					
25%	-0.013290	-1.824251e-02	-0.016664	-0.025892	-0.020
805					
50%	0.001023	-7.617596e-04	-0.001335	-0.000842	-0.002
254					
75%	0.017332	1.888169e-02	0.011610	0.024168	0.023
530					
max	0.159276	1.477720e-01	0.226891	0.261960	0.364
697					

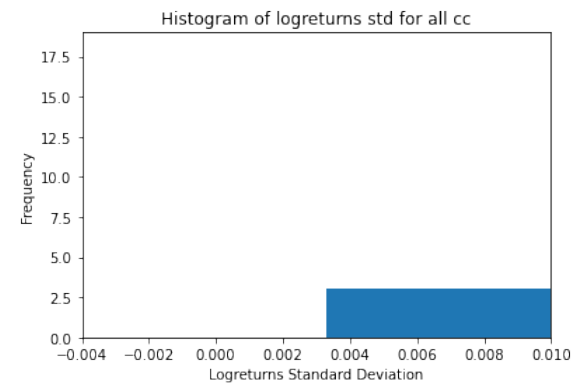
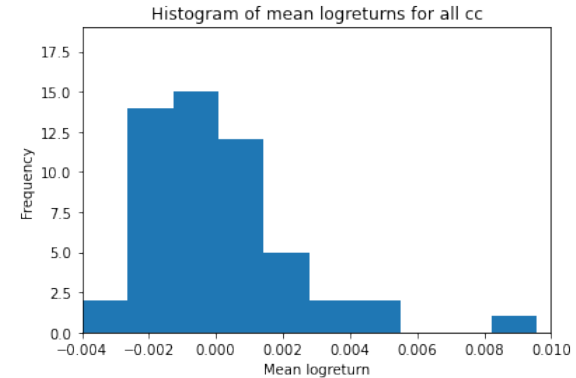
	chainlink	binancecoin	cardano	stellar	usd-coin
...					
count	364.000000	364.000000	364.000000	364.000000	364.000000
...					
mean	0.004992	0.002261	-0.000532	-0.002448	0.000010
...					
std	0.065036	0.044104	0.046071	0.041849	0.003273
...					
min	-0.208088	-0.154145	-0.180399	-0.130523	-0.019772
...					
25%	-0.032302	-0.023766	-0.025893	-0.023299	-0.001420
...					
50%	-0.001832	-0.000275	0.001846	-0.003477	0.000166
...					
75%	0.032873	0.026335	0.022196	0.017211	0.001593
...					
max	0.476072	0.176847	0.191987	0.258028	0.015020
...					

	loopring	lisk	kyber-network	quant-network	bitco
in-gold					
count	364.000000	364.000000	364.000000	364.000000	364
.000000					
mean	-0.001591	-0.002260	0.000545	0.001428	-0
.002284					
std	0.057431	0.041671	0.061801	0.077367	0
.041670					
min	-0.192991	-0.182994	-0.201941	-0.231459	-0
.205101					
25%	-0.030804	-0.024331	-0.030000	-0.042156	-0
.023119					
50%	0.000114	-0.002035	-0.003271	-0.007291	-0
.000368					
75%	0.024985	0.019425	0.027482	0.035867	0
.020749					
max	0.409660	0.158836	0.358089	0.414337	0
.160100					

	maidsafecoin	vitae	siacoin	nano	enjincoi
n					
count	364.000000	364.000000	364.000000	364.000000	364.000000
0					
mean	-0.001609	-0.000865	-0.001795	-0.000732	0.00218
6					
std	0.056445	0.233123	0.043664	0.048957	0.08068
2					

min	-0.443581	-2.517366	-0.192094	-0.144826	-0.20958
3					
25%	-0.022910	-0.055540	-0.025023	-0.027692	-0.03368
9					
50%	-0.001002	-0.003625	-0.000540	-0.002657	-0.00053
2					
75%	0.023601	0.052783	0.022080	0.023005	0.02967
7					
max	0.229984	2.522906	0.159691	0.211709	0.75121
9					

[8 rows x 53 columns]



```

In [11]: # Exploratory Analysis
# 6) Scatterplot of correlated cc

# correlation matrix of all cryptos logreturns
corr_matrix = pd.DataFrame(np.zeros((nb_cc,nb_cc)))
corr_matrix.index = corr_matrix.columns = cc_names
corr_matrix = returns_data.corr()
corr_matrix = round(corr_matrix,3)

# exporting it to csv and excel (useful for reporting)
corr_matrix.to_csv('Data_Analysis/cc_corrmatrix.csv', index=True, header=True)
corr_matrix.to_excel('Data_Analysis/cc_corrmatrix.xlsx',index=True, header=True)

# scatter plot between highly (negatively or positively) correlated cryptos

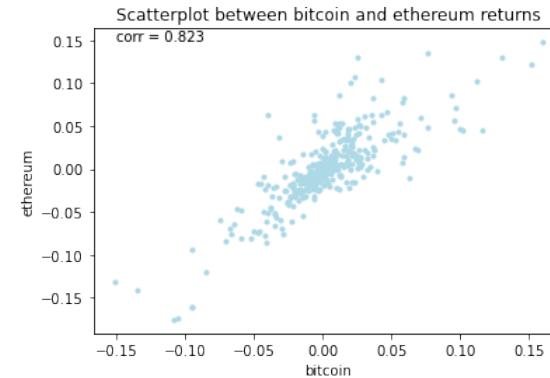
highcorr_matrix = pd.DataFrame(np.zeros((nb_cc,nb_cc)))
highcorr_matrix.index = highcorr_matrix.columns = cc_names
highcorr_cc = []
print("16 pairs of cryptocurrencies are highly correlated in their log returns")
for i in range(nb_cc): # just a for loop to determine what are the correlated cryptos
    abc = cc_names[i]
    for j in range(nb_cc):
        if (i<j):
            dcb = cc_names[j]
            corr = corr_matrix[abc][dcb]
            if ((corr >= 0.8 or corr <= -0.8) and corr != 1):
                highcorr_matrix[abc][dcb] = corr_matrix[abc][dcb]
                print(abc + ' is strongly correlated to ' + dcb)
                corr_str = str(round(corr,3))
                fig = plt.figure()
                ax = fig.add_subplot(111)
                ax.scatter(returns_data[abc],returns_data[dcb], color='lightblue', marker='.')
                ax.set(title='Scatterplot between '+abc+' and '+dcb+' returns',ylabel=dcb,xlabel=abc)
                ax.annotate('corr = '+corr_str,xy=(-0.15,0.15))
                plt.savefig('Data_Analysis/sc_'+ abc + '_' + dcb + '.jpeg',transparent=True)
                plt.show()
                highcorr_cc.append([abc,dcb,corr])

highcorr_cc = pd.DataFrame(highcorr_cc)
highcorr_cc.columns = ["Crypto 1","Crypto 2","Pair correlation"]
highcorr_cc.to_csv('Data_Analysis/highcorr_cc.csv', index=True, header=True)
#sns.regplot(x=abc,y=dcb,ci = None,data=ret_cc)

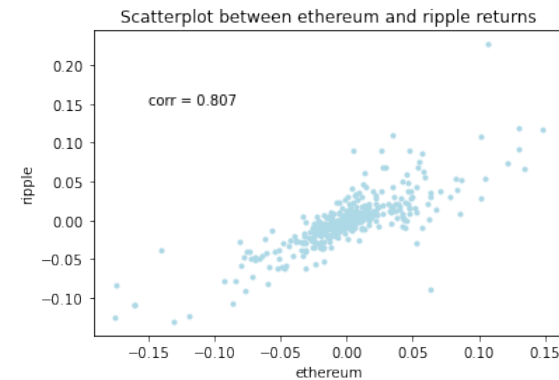
```

16 pairs of cryptocurrencies are highly correlated in their log returns

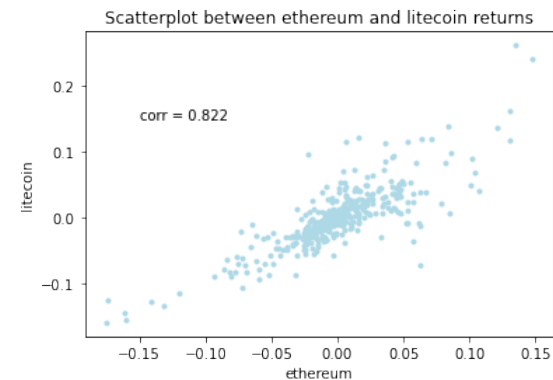
bitcoin is strongly correlated to ethereum



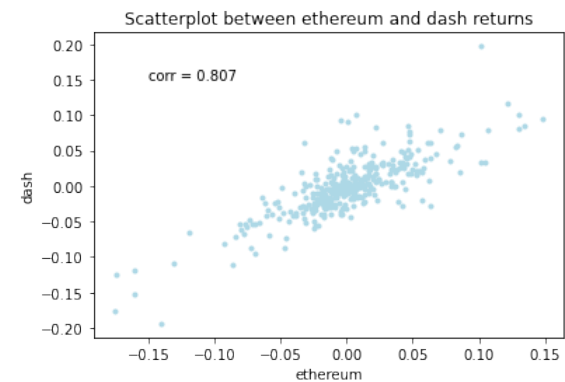
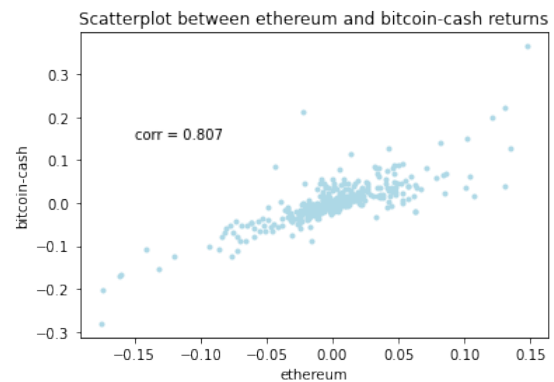
ethereum is strongly correlated to ripple



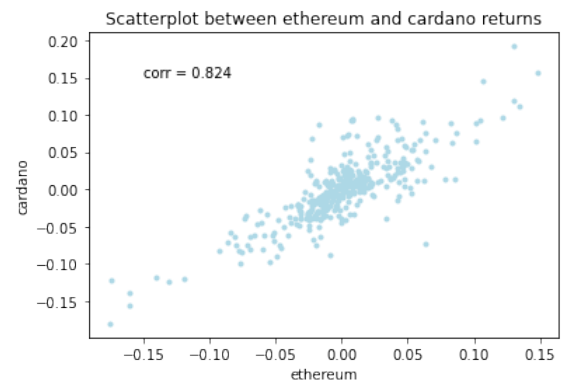
ethereum is strongly correlated to litecoin



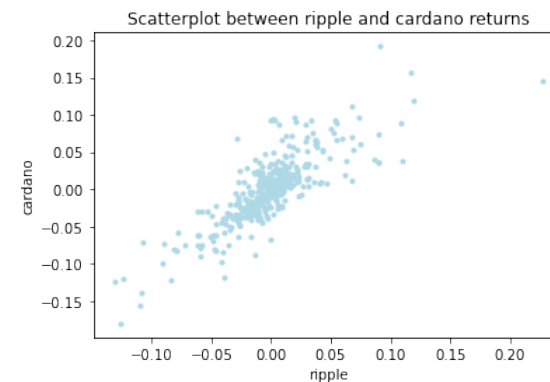
ethereum is strongly correlated to bitcoin-cash



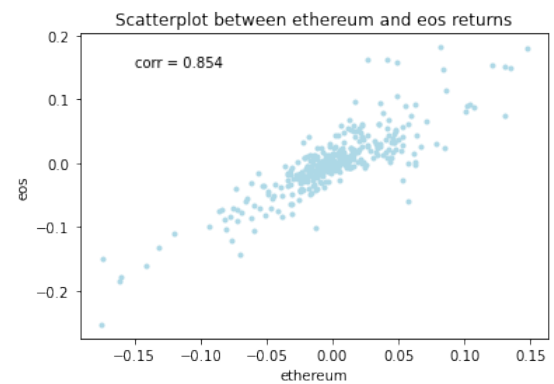
ethereum is strongly correlated to cardano



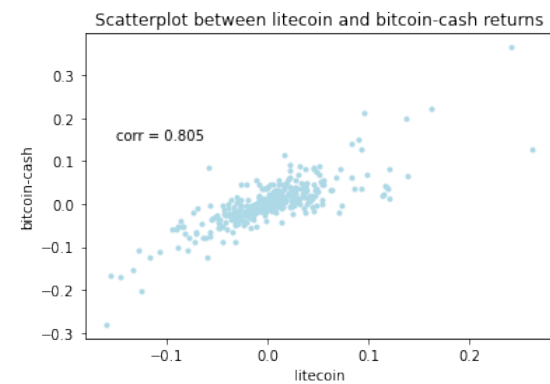
ripple is strongly correlated to cardano



ethereum is strongly correlated to eos

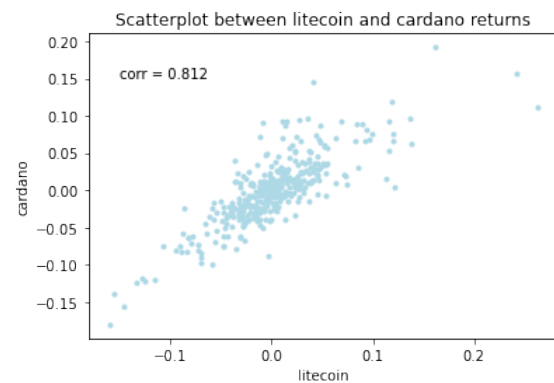


litecoin is strongly correlated to bitcoin-cash

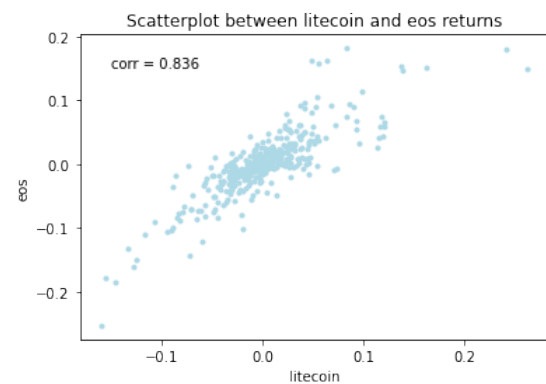


ethereum is strongly correlated to dash

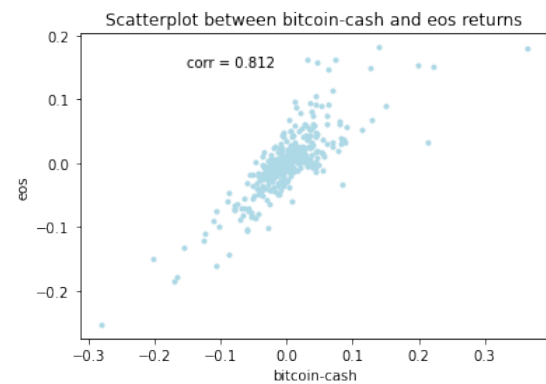
litecoin is strongly correlated to cardano



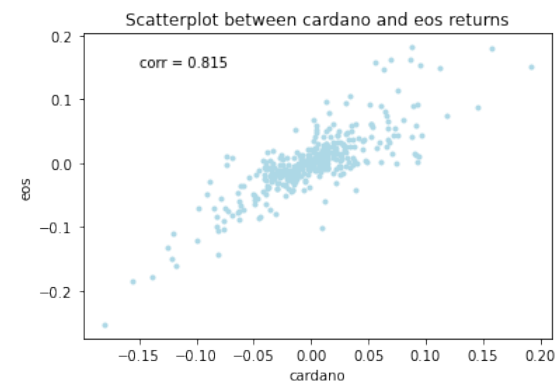
litecoin is strongly correlated to eos



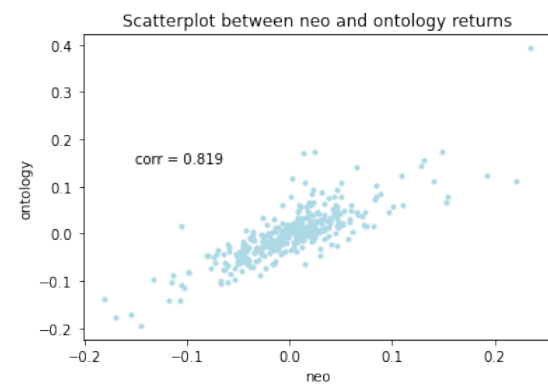
bitcoin-cash is strongly correlated to eos



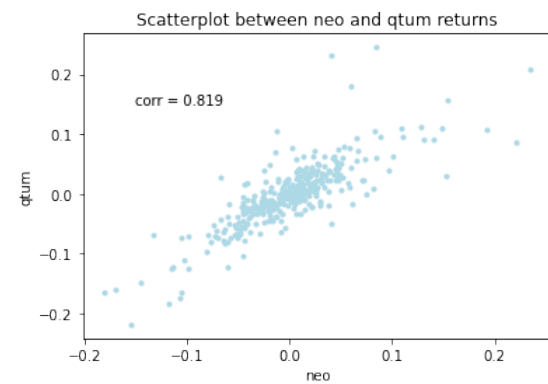
cardano is strongly correlated to eos



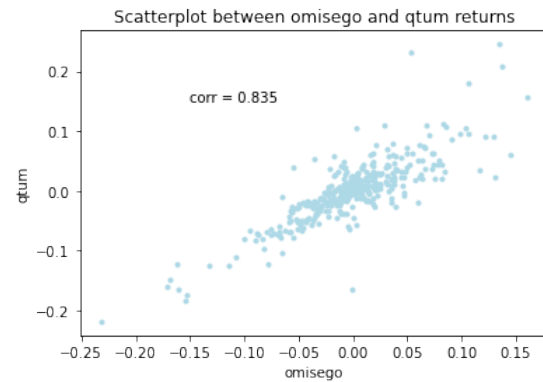
neo is strongly correlated to ontology



neo is strongly correlated to qtum



omisego is strongly correlated to qtum



In [12]: highcorr_cc

Out[12]:

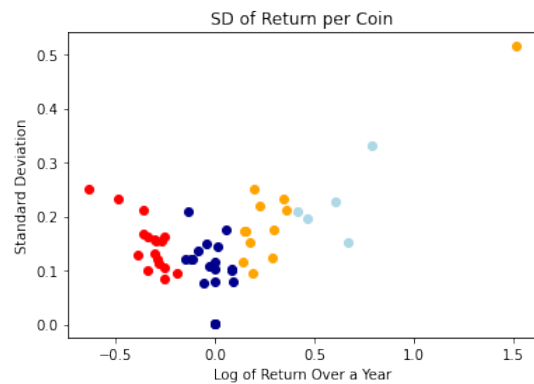
	Crypto 1	Crypto 2	Pair correlation
0	bitcoin	ethereum	0.823
1	ethereum	ripple	0.807
2	ethereum	litecoin	0.822
3	ethereum	bitcoin-cash	0.807
4	ethereum	cardano	0.824
5	ethereum	eos	0.854
6	ethereum	dash	0.807
7	ripple	cardano	0.814
8	litecoin	bitcoin-cash	0.805
9	litecoin	cardano	0.812
10	litecoin	eos	0.836
11	bitcoin-cash	eos	0.812
12	cardano	eos	0.815
13	neo	ontology	0.819
14	neo	qtum	0.819
15	omisego	qtum	0.835

```
In [13]: #Preparing the data
log_frame = np.log10(prices_data)
log_return = list()
volatility = list()
for i in range(0, prices_data.shape[1]):
    log_return.append(i)
    volatility.append(i)
    log_return[i]= log_frame.iloc[364][i] - log_frame.iloc[0][i]
    aux = np.std(log_frame.iloc[:,[i]]) #change here to get other d
iagram
    volatility[i] = aux[0]

#### Creating the Clusters
db_vol_ret =pd.DataFrame(data=log_return,columns=['return'])
db_vol_ret['volatillity'] = volatility
n_kmeans = 5
km = KMeans(n_clusters=n_kmeans)
y_predicted = km.fit_predict(db_vol_ret)
cols=prices_data.columns
db_vol_ret.index=cols
db_vol_ret['cluster'] = y_predicted

##plotting the result
df = db_vol_ret
df1= df[df.cluster == 0]
df2= df[df.cluster == 1]
df3= df[df.cluster == 2]
df4= df[df.cluster == 3]
df5= df[df.cluster == 4]

plt.scatter(df1['return'],df1['volatillity'],color='lightblue')
plt.scatter(df2['return'],df2['volatillity'],color='red')
plt.scatter(df3['return'],df3['volatillity'],color='orange')
plt.scatter(df4['return'],df4['volatillity'],color='darkblue')
plt.scatter(df5['return'],df5['volatillity'],color='orange')
plt.xlabel('Log of Return Over a Year')
plt.ylabel('Standard Deviation')
plt.title('SD of Return per Coin')
plt.savefig('Data_Analysis/K-Means_Explorative.jpeg',transparent=True)
ue)
```

```
In [14]: # Clustering

# 1) Rolling windows computation for each variable
# 2) PCA: Principal Components Analysis followed by a k-means clustering algorithm on its components
# 2.a) Application on a single window
# 2.b) Application on all rolling windows
# 3) LFM: Linear Factor Model followed by a k-means clustering algorithm on its factors
# 3.a) Application on a single window
# 3.b) Application on all rolling windows
```

```
In [15]: # Clustering

# 1) Rolling windows computation for each variable

window_size = 25 # determining the size of the rolling windows we are going to compute

# Mean
window_mean = returns_data.rolling(window=window_size).mean()
window_mean = window_mean.dropna(axis=0)

# Variance
window_var = returns_data.rolling(window=window_size).var()
window_var = window_var.dropna(axis=0)

# Skewness (IMPORTANT: need to take rolling window of 3 to calculate it)
window_skew = returns_data.rolling(window=window_size).skew()
window_skew = window_skew.dropna(axis=0)

# Kurtosis (IMPORTANT: need to take rolling window of 4 to calculate it)
window_kurt = returns_data.rolling(window=window_size).kurt()
window_kurt = window_kurt.dropna(axis=0)

# Quantile 0.05
window_005_quantile = returns_data.rolling(window=window_size).quantile(0.05)
window_005_quantile = window_005_quantile.dropna(axis=0)

# Quantile 0.10
window_010_quantile = returns_data.rolling(window=window_size).quantile(0.10)
window_010_quantile = window_010_quantile.dropna(axis=0)

# Quantile 0.15
window_015_quantile = returns_data.rolling(window=window_size).quantile(0.15)
window_015_quantile = window_015_quantile.dropna(axis=0)

# Quantile 0.85
window_085_quantile = returns_data.rolling(window=window_size).quantile(0.85)
window_085_quantile = window_085_quantile.dropna(axis=0)

# Quantile 0.90
window_090_quantile = returns_data.rolling(window=window_size).quantile(0.90)
window_090_quantile = window_090_quantile.dropna(axis=0)

# Quantile 0.95
window_095_quantile = returns_data.rolling(window=window_size).quantile(0.95)
window_095_quantile = window_095_quantile.dropna(axis=0)
```

In [16]: # Clustering

```
# 2) PCA: Principal Components Analysis followed by a k-means clustering algorithm on its components
# 2.a) Application on a single window

# Initialization: Df creation for the first window
frames = [window_mean.iloc[0], window_var.iloc[0], window_skew.iloc[0],
          window_kurt.iloc[0], window_005_quantile.iloc[0], window_010_quantile.iloc[0],
          window_015_quantile.iloc[0], window_085_quantile.iloc[0],
          window_090_quantile.iloc[0],
          window_095_quantile.iloc[0]]
frames = pd.concat(frames, axis=1)

scaler = MinMaxScaler()
scaler.fit(frames)
frames_norm = pd.DataFrame(scaler.transform(frames), index=frames.index)
frames_norm.columns = ("Mean", "Variance", "Skewness", "Kurtosis", "Q.05", "Q.10", "Q.15", "Q.085", "Q.090", "Q.095")
frames_norm # final dataframe of the different variables (moments + quantiles) for each cc
```

Out[16]:

	Mean	Variance	Skewness	Kurtosis	Q.05	Q.10	Q.15	Q.085	Q.090	Q.095
bitcoin	0.452785	0.036397	0.331646	0.533070	0.866977	0.857108	0.795706	0.126108	0.126108	0.126108
ethereum	0.373463	0.126541	0.490807	0.381679	0.717934	0.703016	0.617143	0.228108	0.228108	0.228108
ripple	0.394568	0.045151	0.243746	0.543274	0.828487	0.798767	0.754050	0.152108	0.152108	0.152108
litecoin	0.555107	0.127172	0.459584	0.269824	0.743675	0.729847	0.569958	0.324108	0.324108	0.324108
bitcoin-cash	0.350650	0.117031	0.310603	0.456292	0.745819	0.704867	0.573326	0.252108	0.252108	0.252108
chainlink	0.857243	0.285613	0.766090	0.086631	0.688798	0.631513	0.457865	0.571108	0.571108	0.571108
binancecoin	0.557537	0.078890	0.476226	0.248050	0.750718	0.795175	0.787277	0.247108	0.247108	0.247108
cardano	0.517659	0.135110	0.411017	0.281094	0.687142	0.687088	0.667592	0.344108	0.344108	0.344108
stellar	0.395852	0.063071	0.277525	0.586199	0.842281	0.811095	0.695320	0.152108	0.152108	0.152108
usd-coin	0.484375	0.000076	0.519645	0.000000	0.994371	0.990759	0.987988	0.006108	0.006108	0.006108
bitcoin-cash-sv	0.379381	0.098485	0.524917	0.378820	0.720022	0.702363	0.715194	0.141108	0.141108	0.141108
eos	0.450602	0.140224	0.250159	0.512511	0.714111	0.656757	0.630455	0.273108	0.273108	0.273108
nem	0.365815	0.056671	0.000000	1.000000	0.864951	0.818855	0.723256	0.086108	0.086108	0.086108
tron	0.770416	0.169139	0.783793	0.254763	0.672338	0.677591	0.708745	0.477108	0.477108	0.477108
okb	0.440298	0.063585	0.401350	0.249096	0.810168	0.783890	0.679960	0.232108	0.232108	0.232108
tezos	0.393754	0.062071	0.415455	0.227131	0.726126	0.716814	0.705144	0.167108	0.167108	0.167108
neo	0.495926	0.129943	0.506314	0.230482	0.718625	0.699737	0.566782	0.322108	0.322108	0.322108
celsius-										

degree-token	0.570627	0.396070	0.686168	0.032444	0.530491	0.349559	0.135969	0.781108	0.781108	0.781108
theta-token	0.622234	0.097213	0.400937	0.223484	0.750082	0.765116	0.709763	0.344108	0.344108	0.344108
dash	0.414075	0.080756	0.132420	0.653051	0.787047	0.748551	0.687504	0.203108	0.203108	0.203108
vechain	0.554601	0.142732	0.407833	0.333851	0.790151	0.774625	0.663902	0.414108	0.414108	0.414108
havven	0.665166	1.000000	0.739511	0.291345	0.000000	0.463509	0.362429	1.000108	1.000108	1.000108
huobi-token	0.468196	0.019779	0.281235	0.390303	0.825736	0.929264	0.914674	0.108108	0.108108	0.108108
iota	0.314220	0.109169	0.283378	0.492814	0.711080	0.725876	0.606744	0.187108	0.187108	0.187108
zcash	0.415513	0.052098	0.489467	0.190111	0.788733	0.760545	0.708519	0.160108	0.160108	0.160108
waves	0.373286	0.097996	0.620151	0.195245	0.660518	0.610567	0.651526	0.173108	0.173108	0.173108
ethereum-classic	0.368525	0.088621	0.299894	0.191444	0.647977	0.620735	0.534614	0.235108	0.235108	0.235108
zilliqa	0.582904	0.164631	0.427396	0.216618	0.636559	0.752141	0.596247	0.403108	0.403108	0.403108
dogecoin	0.381843	0.013755	0.338410	0.410453	0.918119	0.886395	0.830606	0.061108	0.061108	0.061108
maker	0.518546	0.081290	0.464392	0.304803	0.784596	0.805196	0.685902	0.202108	0.202108	0.202108
decred	0.511717	0.092068	0.192923	0.435792	0.719274	0.697971	0.717630	0.235108	0.235108	0.235108
omisego	0.418226	0.118135	0.244667	0.445809	0.695275	0.712865	0.609747	0.243108	0.243108	0.243108
ontology	0.523413	0.164460	0.294581	0.482852	0.724299	0.711107	0.685501	0.383108	0.383108	0.383108
paxos-standard	0.479212	0.000756	0.661242	0.201102	0.983101	0.974438	0.961012	0.006108	0.006108	0.006108
nexo	0.261813	0.107989	0.677696	0.104169	0.695444	0.661039	0.498435	0.271108	0.271108	0.271108
basic-attention-token	0.472470	0.076096	0.227172	0.364998	0.707767	0.791544	0.696162	0.205108	0.205108	0.205108
digibyte	0.415516	0.087528	0.375215	0.495065	0.806204	0.759969	0.679434	0.142108	0.142108	0.142108
0x	0.466866	0.086281	0.389634	0.288530	0.818995	0.751255	0.613172	0.247108	0.247108	0.247108
true-usd	0.481884	0.000000	0.560671	0.336334	1.000000	1.000000	1.000000	0.000108	0.000108	0.000108
qtum	0.450330	0.105988	0.291503	0.350532	0.700734	0.676025	0.573238	0.248108	0.248108	0.248108
republic-protocol	0.429244	0.147351	0.223370	0.515597	0.707584	0.682968	0.593466	0.324108	0.324108	0.324108
swissborg	0.438780	0.153354	0.707793	0.288496	0.684259	0.578432	0.322368	0.177108	0.177108	0.177108
icon	0.449165	0.115217	0.252734	0.499565	0.806919	0.745133	0.640403	0.317108	0.317108	0.317108
loopring	1.000000	0.571763	1.000000	0.625049	0.521136	0.662301	0.515390	0.633108	0.633108	0.633108
lisk	0.431322	0.060039	0.304863	0.353564	0.796203	0.776220	0.645435	0.165108	0.165108	0.165108
kyber-network	0.393132	0.130373	0.331460	0.294902	0.675333	0.606811	0.482169	0.313108	0.313108	0.313108
quant-network	0.307977	0.345017	0.743336	0.086841	0.464331	0.358161	0.072315	0.474108	0.474108	0.474108
bitcoin-gold	0.364782	0.041147	0.475113	0.222223	0.824513	0.784611	0.710499	0.156108	0.156108	0.156108
maidsafecoin	0.400714	0.152884	0.335370	0.229302	0.502005	0.685862	0.547440	0.336108	0.336108	0.336108

vitae	0.000000	0.642389	0.459100	0.254114	0.096983	0.000000	0.000000	0.296
siacoin	0.456635	0.077417	0.483797	0.133857	0.732783	0.721068	0.615132	0.260
nano	0.598563	0.103888	0.312633	0.374919	0.756824	0.791224	0.752652	0.324
enjincoin	0.422799	0.115993	0.234280	0.437748	0.657322	0.716010	0.605453	0.260

In [17]: # Clustering

```
# 2) PCA: Principal Components Analysis followed by a k-means clustering algorithm on its components
# 2.a) Application on a single window

# PCA is firstly made
pca = PCA(n_components=3, random_state=123) # calling PCA function
pca.fit(frames_norm)
print(pca.explained_variance_)
principal_components = pd.DataFrame(pca.fit_transform(frames_norm),
                                   index=frames_norm.index)

# from these variances, the number of components is determined
n_components = 3 #as the third component still explains more than 10% of the variance

loadings = pca.components_ # inspired by https://reneshbedre.github.io/blog/pca_3d.html
num_pc = pca.n_features_
pc_list = ["PC"+str(i) for i in list(range(1, num_pc+1))]
loadings_df = pd.DataFrame.from_dict(dict(zip(pc_list, loadings)))
loadings_df['variable'] = frames_norm.columns.values
loadings_df = loadings_df.set_index('variable')
loadings_df
ax = sns.heatmap(loadings_df, annot=True, cmap='Spectral')
plt.title('Correlation map between three first components and variables')
plt.savefig('Clusters/pca_corrmap.jpeg',transparent=True)
plt.show()

# projecting log returns on two first components
plt.scatter(principal_components.iloc[:,0], principal_components.iloc[:,1])
plt.xlabel('1st Principal Component',fontSize=10)
plt.ylabel('2nd Principal Component',fontSize=10)
plt.title("Principal Component Analysis of Cryptos",fontSize=12)
plt.savefig('Clusters/pca.jpeg',transparent=True)
plt.show()

# Then, the k-means algorithm may be applied on this time-step

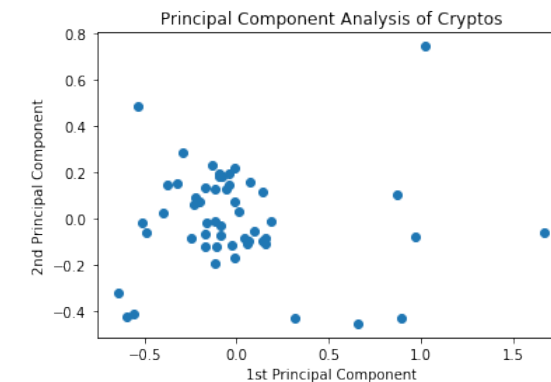
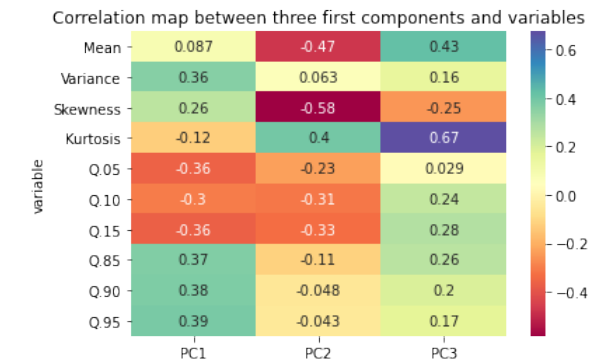
# To check the number of clusters needed
sse = []
for k in range(1, 11):
    kmeans = KMeans(n_clusters=k, init = "random", n_init=10, max_iter = 300,
                    random_state = 123)
    kmeans.fit(principal_components)
```

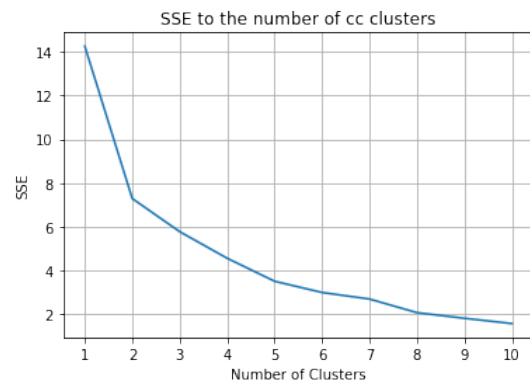
```
sse.append(kmeans.inertia_)

plt.plot(range(1, 11), sse)
plt.xticks(range(1, 11))
plt.xlabel("Number of Clusters")
plt.ylabel("SSE")
plt.title("SSE to the number of cc clusters",fontSize=12)
plt.grid(True)
plt.savefig('Clusters/pca_nb_kmeans.jpeg',transparent=True)
plt.show()

print("By looking through the different windows, taking 4 clusters would be on average appropriate ")
n_kmeans = 4
kmeans = KMeans(n_clusters=n_kmeans,random_state=123) # defining the function kmeans with the
```

[0.18880196 0.04837439 0.03711979]





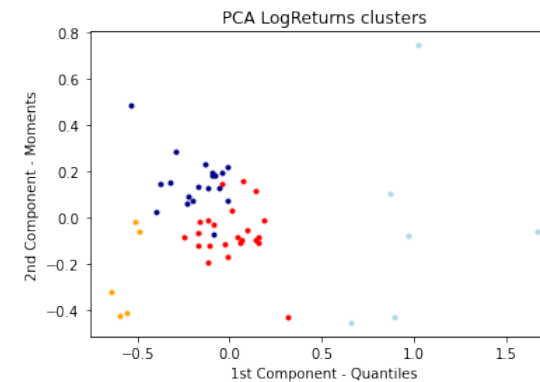
By looking through the different windows, taking 4 clusters would be on average appropriate

```
In [18]: # clustering the first rolling window
print("Let's try to divide the first window into four clusters:")
label = kmeans.fit_predict(principal_components)
#print(label)

filtered_label0 = principal_components[label == 0]
filtered_label1 = principal_components[label == 1]
filtered_label2 = principal_components[label == 2]
filtered_label3 = principal_components[label == 3]

#Plotting the results
fig = plt.figure()
ax = fig.add_subplot(111)
ax.scatter(filtered_label0[0],filtered_label0[1], color='red', marker='.')
ax.scatter(filtered_label1[0],filtered_label1[1], color='lightblue', marker='.')
ax.scatter(filtered_label2[0],filtered_label2[1], color='orange', marker='.')
ax.scatter(filtered_label3[0],filtered_label3[1], color='darkblue', marker='.')
ax.set(title='PCA LogReturns clusters',ylabel='2nd Component - Moments',xlabel='1st Component - Quantiles')
plt.savefig('Clusters/PCA_clusters.jpeg',transparent=True)
plt.show()
```

Let's try to divide the first window into four clusters:



```
In [19]: del filtered_label0,filtered_label1,filtered_label2,filtered_label3
```

In [20]: # Clustering

```
# 2) PCA: Principal Components Analysis followed by a k-means clustering algorithm on its components
# 2.b) Application on all rolling windows

kmeans = KMeans(n_clusters=n_kmeans,random_state=123) # defining the function kmeans with the
# optimal number of clusters found in last part

# Loop on the windows
labels = [] # creating a labels df for later
nt = len(window_mean);nb_cc; # time indices
timed_PCA = np.zeros((nt,nb_cc,n_components)) # 3D matrix for the PCA components at each time-step (days*nb_cc*nb_pc)
timed_PCA_label = np.zeros((nt,nb_cc)) # matrix for labels= in which cluster is a cc
#df = frames_norm

for i in range(nt):
    win_frames = []
    win_frames = [window_mean.iloc[i], window_var.iloc[i],
                  window_skew.iloc[i], window_kurt.iloc[i],
                  window_005_quantile.iloc[i], window_010_quantile.
iloc[i],
                  window_015_quantile.iloc[i], window_085_quantile.
iloc[i], window_090_quantile.iloc[i],
                  window_095_quantile.iloc[i]] # computation of the
rolling windows through time
    win_frames = pd.concat(win_frames, axis=1)
    win_frames_norm = pd.DataFrame scaler.transform(win_frames),
index=win_frames.index)

# all rolling windows are created
pca.fit(win_frames_norm) # the pca is initialized
timed_PCA[i] = pca.fit_transform(win_frames_norm) # pca is done
timed_PCA_label[i] = kmeans.fit_predict(timed_PCA[i]) # clusters labels are assigned to each cc

timed_PCA_label = pd.DataFrame(timed_PCA_label)
timed_PCA_label.columns = cc_names

# instead of analyzing each time-step, let's analyze the distribution of clusters assignation for each cc
index = pd.DataFrame([frames.index])
table = []
for i in index.transpose()[0]:
    y = timed_PCA_label[i].value_counts(normalize=True)
    table.append(y)
pca_km_table = pd.DataFrame(table)
del y,table;

print(pca_km_table) # printing table of interest
```

	0.0	1.0	2.0	3.0
bitcoin	0.458824	0.158824	0.170588	0.211765
ethereum	0.461765	0.173529	0.185294	0.179412
ripple	0.447059	0.167647	0.191176	0.194118
litecoin	0.458824	0.170588	0.191176	0.179412
bitcoin-cash	0.552941	0.167647	0.141176	0.138235
chainlink	0.408824	0.167647	0.235294	0.188235
binancecoin	0.514706	0.152941	0.185294	0.147059
cardano	0.494118	0.147059	0.208824	0.150000
stellar	0.517647	0.164706	0.161765	0.155882
usd-coin	0.370588	0.123529	0.208824	0.297059
bitcoin-cash-sv	0.458824	0.191176	0.205882	0.144118
eos	0.417647	0.191176	0.211765	0.179412
nem	0.461765	0.214706	0.152941	0.170588
tron	0.488235	0.161765	0.205882	0.144118
okb	0.391176	0.214706	0.214706	0.179412
tezos	0.394118	0.191176	0.294118	0.120588
neo	0.488235	0.164706	0.208824	0.138235
celsius-degree-token	0.238235	0.232353	0.317647	0.211765
theta-token	0.420588	0.188235	0.232353	0.158824
dash	0.500000	0.173529	0.179412	0.147059
vechain	0.405882	0.194118	0.214706	0.185294
havven	0.155882	0.300000	0.291176	0.252941
huobi-token	0.414706	0.167647	0.208824	0.208824
iota	0.535294	0.144118	0.185294	0.135294
zcash	0.505882	0.167647	0.176471	0.150000
waves	0.485294	0.150000	0.208824	0.155882
ethereum-classic	0.467647	0.211765	0.173529	0.147059
zilliqa	0.441176	0.173529	0.252941	0.132353
dogecoin	0.488235	0.173529	0.176471	0.161765
maker	0.467647	0.214706	0.167647	0.150000
decred	0.502941	0.188235	0.158824	0.150000
omisego	0.514706	0.161765	0.200000	0.123529
ontology	0.461765	0.179412	0.200000	0.158824
paxos-standard	0.373529	0.123529	0.205882	0.297059
nexo	0.352941	0.214706	0.238235	0.194118
basic-attention-token	0.408824	0.179412	0.244118	0.167647
digibyte	0.479412	0.170588	0.202941	0.147059
0x	0.461765	0.197059	0.200000	0.141176
true-usd	0.361765	0.129412	0.211765	0.297059
qtum	0.494118	0.197059	0.161765	0.147059
republic-protocol	0.297059	0.244118	0.264706	0.194118
swissborg	0.329412	0.247059	0.244118	0.179412
icon	0.494118	0.200000	0.164706	0.141176
loopring	0.391176	0.223529	0.214706	0.170588
lisk	0.476471	0.191176	0.182353	0.150000
kyber-network	0.276471	0.258824	0.258824	0.205882
quant-network	0.194118	0.273529	0.282353	0.250000
bitcoin-gold	0.602941	0.132353	0.164706	0.100000
maidsafecoin	0.461765	0.220588	0.197059	0.120588
vitae	0.108824	0.438235	0.241176	0.211765
siacoin	0.500000	0.173529	0.185294	0.141176
nano	0.452941	0.191176	0.208824	0.147059
enjincoin	0.294118	0.264706	0.279412	0.161765

```

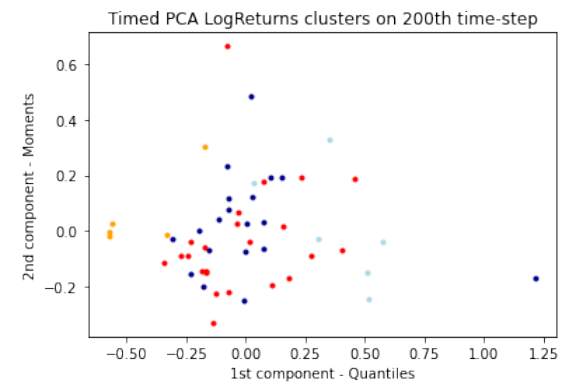
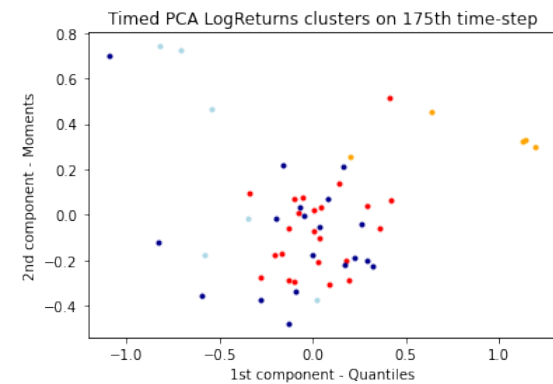
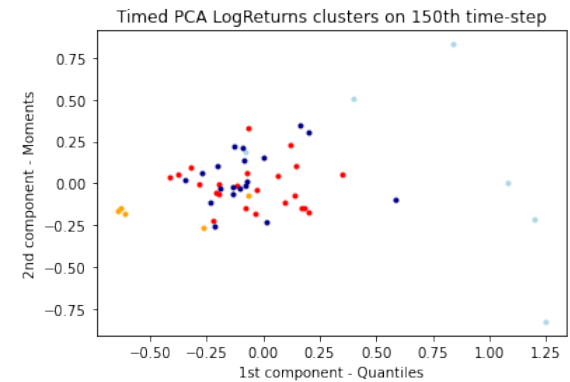
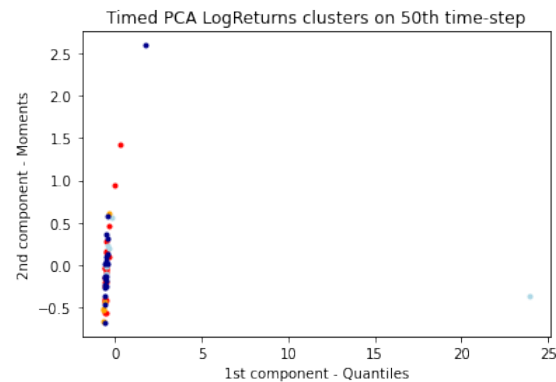
In [21]: # Plotting the results for some rolling windows
print("Let's see how cc log returns are clustered for some rolling
windows")
rw_choice = [50,150,175,200,300]
rw_choice

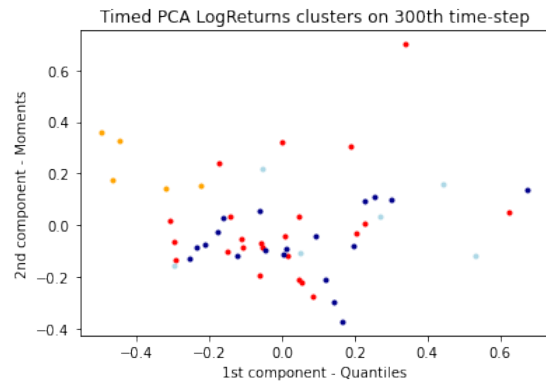
for r in rw_choice:
    selected_ts = r
    filtered_data = timed_PCA[selected_ts]
    filtered_label0 = filtered_data[label == 0]
    filtered_label1 = filtered_data[label == 1]
    filtered_label2 = filtered_data[label == 2]
    filtered_label3 = filtered_data[label == 3]

    #Plotting the results
    fig = plt.figure()
    ax = fig.add_subplot(111)
    ax.scatter(filtered_label0[:,0],filtered_label0[:,1], color='red', marker='.')
    ax.scatter(filtered_label1[:,0],filtered_label1[:,1], color='lightblue', marker='.')
    ax.scatter(filtered_label2[:,0],filtered_label2[:,1], color='orange', marker='.')
    ax.scatter(filtered_label3[:,0],filtered_label3[:,1], color='darkblue', marker='.')
    ax.set(title='Timed PCA LogReturns clusters on '+str(selected_ts) + 'th time-step',ylabel='2nd component - Moments',xlabel='1st component - Quantiles')
    plt.savefig('Clusters/timedpca_clusters'+str(selected_ts)+'rw.jpg',transparent=True)
    plt.show()

```

Let's see how cc log returns are clustered for some rolling windows





```
In [22]: del r, rw_choice, filtered_label0, filtered_label1, filtered_label2, label
```

```
In [23]: # Distribution of cc log returns in clusters
pca_km_table = pca_km_table.round(2)

print("Here is the distribution of cc log returns in each cluster:")
print(pca_km_table)

pca_km_table1 = pd.DataFrame(pca_km_table[:17])
pca_km_table2 = pd.DataFrame(pca_km_table[17:34])
pca_km_table3 = pd.DataFrame(pca_km_table[34:])

pca_km_table1.to_csv('Clusters/pca_km_table1.csv', index=True, header=True)
pca_km_table2.to_csv('Clusters/pca_km_table2.csv', index=True, header=True)
pca_km_table3.to_csv('Clusters/pca_km_table3.csv', index=True, header=True)
```

Here is the distribution of cc log returns in each cluster:

	0.0	1.0	2.0	3.0
bitcoin	0.46	0.16	0.17	0.21
ethereum	0.46	0.17	0.19	0.18
ripple	0.45	0.17	0.19	0.19
litecoin	0.46	0.17	0.19	0.18
bitcoin-cash	0.55	0.17	0.14	0.14
chainlink	0.41	0.17	0.24	0.19
binancecoin	0.51	0.15	0.19	0.15
cardano	0.49	0.15	0.21	0.15
stellar	0.52	0.16	0.16	0.16
usd-coin	0.37	0.12	0.21	0.30
bitcoin-cash-sv	0.46	0.19	0.21	0.14
eos	0.42	0.19	0.21	0.18
nem	0.46	0.21	0.15	0.17
tron	0.49	0.16	0.21	0.14
okb	0.39	0.21	0.21	0.18
tezos	0.39	0.19	0.29	0.12
neo	0.49	0.16	0.21	0.14
celsius-degree-token	0.24	0.23	0.32	0.21
theta-token	0.42	0.19	0.23	0.16
dash	0.50	0.17	0.18	0.15
vechain	0.41	0.19	0.21	0.19
havven	0.16	0.30	0.29	0.25
huobi-token	0.41	0.17	0.21	0.21
iota	0.54	0.14	0.19	0.14
zcash	0.51	0.17	0.18	0.15
waves	0.49	0.15	0.21	0.16
ethereum-classic	0.47	0.21	0.17	0.15
zilliqa	0.44	0.17	0.25	0.13
dogecoin	0.49	0.17	0.18	0.16
maker	0.47	0.21	0.17	0.15
decred	0.50	0.19	0.16	0.15
omisego	0.51	0.16	0.20	0.12
ontology	0.46	0.18	0.20	0.16
paxos-standard	0.37	0.12	0.21	0.30
nexo	0.35	0.21	0.24	0.19
basic-attention-token	0.41	0.18	0.24	0.17
digibyte	0.48	0.17	0.20	0.15
0x	0.46	0.20	0.20	0.14
true-usd	0.36	0.13	0.21	0.30
qtum	0.49	0.20	0.16	0.15
republic-protocol	0.30	0.24	0.26	0.19
swissborg	0.33	0.25	0.24	0.18
icon	0.49	0.20	0.16	0.14
loopring	0.39	0.22	0.21	0.17
lisk	0.48	0.19	0.18	0.15
kyber-network	0.28	0.26	0.26	0.21
quant-network	0.19	0.27	0.28	0.25
bitcoin-gold	0.60	0.13	0.16	0.10
maidsafecoin	0.46	0.22	0.20	0.12
vitae	0.11	0.44	0.24	0.21
siacoin	0.50	0.17	0.19	0.14
nano	0.45	0.19	0.21	0.15
enjincoin	0.29	0.26	0.28	0.16

```

In [24]: # Clustering

# 3) LFM: Linear Factor Model followed by a k-means clustering algo
rithm on its factors
# 3.a) Application on a single window

# Initialization: Firstly, test if it makes sense to make a LFM

# It checks whether variables are correlated or not. If significant
, ok. If not, a factor
# analysis should not be done.
chi_square_value,p_value = calculate_bartlett_sphericity(frames_nor
m)
chi_square_value, p_value
# It seems to be statistically significant so we can continue.

# It computes a score of the suitability of the data to a Factor An
alysis
kmo_all,kmo_model=calculate_kmo(frames_norm)
kmo_model
# 0.715 seems ok

# Creating factor analysis object and perform factor analysis
fa = FactorAnalyzer()
fa_test = fa.analyze(frames_norm, 4)

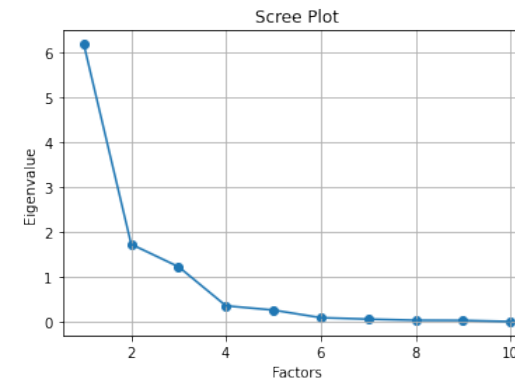
# Checking eigen values: it will show us the number of significant
factors

# Computing Eigenvalues
ev, v = fa.get_eigenvalues()
ev

# Creating a scree plot to display the different eigen values
plt.scatter(range(1,frames_norm.shape[1]+1),ev)
plt.plot(range(1,frames_norm.shape[1]+1),ev)
plt.title('Scree Plot')
plt.xlabel('Factors')
plt.ylabel('Eigenvalue')
plt.grid()
plt.savefig('Clusters/lfm_scree.jpeg',transparent=True)
plt.show()

n_factors = 3
fa = FactorAnalyzer()
fa_test = fa.analyze(frames_norm, n_factors)
print("The number of variables should be reduced to three since it'
s the number of eigen values above 1 (which signifies that a factor
is able to explain more than a single variable).")

```



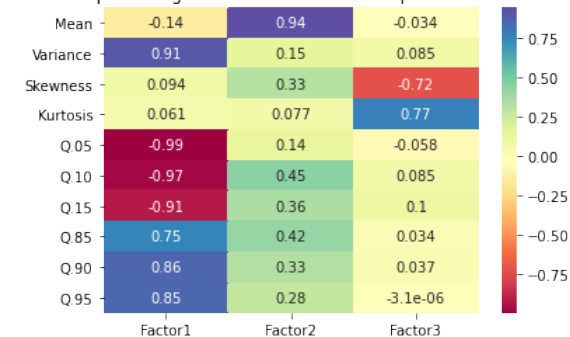
The number of variables should be reduced to three since it's the number of eigen values above 1 (which signifies that a factor is able to explain more than a single variable).

```

In [25]: loadings_lfm = pd.DataFrame(fa.loadings)
ax = sns.heatmap(loadings_lfm, annot=True, cmap='Spectral')
plt.title('Heat map showing how three first factors explain the var
iables')
plt.savefig('Clusters/lfm_heatmap.jpeg',transparent=True)
plt.show()

```

Heat map showing how three first factors explain the variables



```

In [26]: del sse,k,kmeans,n_kmeans

```

```

In [27]: # Linear Factor model estimation

# Application on the first rolling window

frames_norm_np = np.array(frames_norm)

fanalysis = FactorAnalysis(n_components=n_factors)
df_3d = fanalysis.fit_transform(frames_norm_np); df_3d = pd.DataFra
me(df_3d)

```



```

df_3d.columns = ["Factor1", "Factor2", "Factor3"]
df_3d.index = cc_names

fig = plt.figure()
ax = fig.add_subplot(111)
ax.scatter(df_3d['Factor1'], df_3d['Factor2'], color='lightblue', marker='.')
ax.set(title='Returns scatterplot on 2 first factors (1st rolling window)', ylabel='2nd factor - moments', xlabel='1st factor - quantile s')
plt.savefig('Clusters/lfm_sc.jpeg', transparent=True)
plt.show()

mu = np.mean(frames_norm.transpose())
Y = returns_data.iloc[0]; Y
X = np.zeros((len(frames_norm), 3))
X[:, 0] = df_3d['Factor1']; X[:, 1] = df_3d['Factor2']; X[:, 2] = mu
mlr = LinearRegression().fit(X, Y)

regressor = LinearRegression()
regressor.fit(X, Y)
regressor.coef_

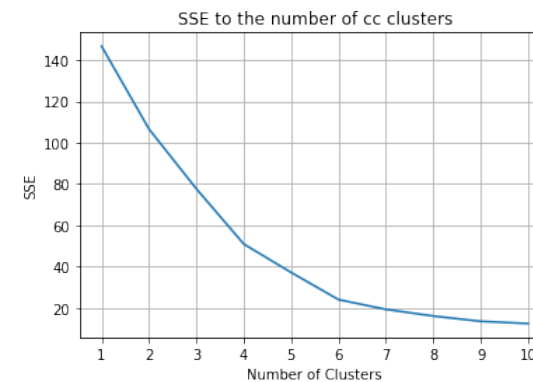
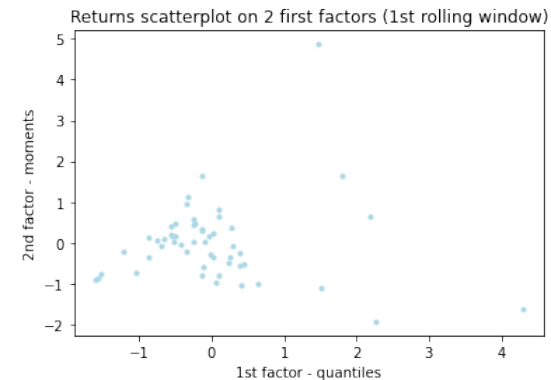
# Then, the k-means algorithm may be applied on this time-step

# To check the number of clusters needed. The criteria is the sse (sum of squared errors).
# Searching for the smallest one, a tradeoff needs to be found between a small sse but a small number of kmeans.
sse = []
for k in range(1, 11):
    kmeans = KMeans(n_clusters=k, init="random", n_init=10, max_iter=300,
                    random_state=123)
    kmeans.fit(df_3d)
    sse.append(kmeans.inertia_)

plt.plot(range(1, 11), sse)
plt.xticks(range(1, 11))
plt.xlabel("Number of Clusters")
plt.ylabel("SSE")
plt.title("SSE to the number of cc clusters", fontsize=12)
plt.grid(True)
plt.savefig('Clusters/lfm_nb_kmeans.jpeg', transparent=True)
plt.show()

print("Again, taking 4 clusters seems to be a good tradeoff between precision and differentiation")
n_kmeans = 4

```



Again, taking 4 clusters seems to be a good tradeoff between precision and differentiation

```
In [28]: # Now we know the number of clusters we want, let's try it for the
         # first rolling window.

         # initialize kmeans class object
kmeans = KMeans(n_clusters = n_kmeans,random_state=123) # defining
the function kmeans
#predict the labels of clusters.
label = kmeans.fit_predict(df_3d)
print(label)

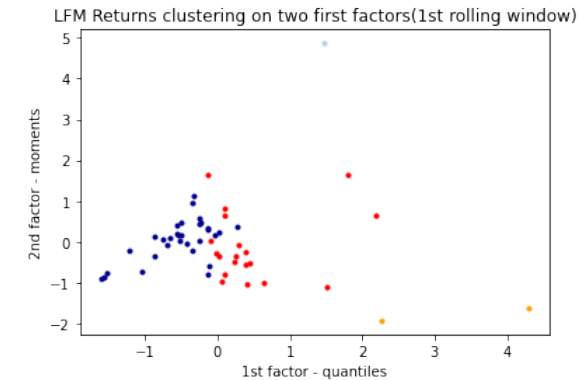
#Getting unique labels

u_labels = np.unique(label)

#filter rows of original data: it separates the data into the diffe
rent clusters
filtered_label0 = df_3d[label == 0]
filtered_label1 = df_3d[label == 1]
filtered_label2 = df_3d[label == 2]
filtered_label3 = df_3d[label == 3]

#Plotting the results
fig = plt.figure()
ax = fig.add_subplot(111)
ax.scatter(filtered_label0['Factor1'],filtered_label0['Factor2'], c
olor='red', marker='.')
ax.scatter(filtered_label1['Factor1'],filtered_label1['Factor2'], c
olor='lightblue', marker='.')
ax.scatter(filtered_label2['Factor1'],filtered_label2['Factor2'], c
olor='orange', marker='.')
ax.scatter(filtered_label3['Factor1'],filtered_label3['Factor2'], c
olor='darkblue', marker='.')
ax.set(title='LFM Returns clustering on two first factors(1st rolli
ng window)',ylabel='2nd factor - moments',xlabel='1st factor - quan
tiles')
plt.savefig('Clusters/lfm_clusters.jpeg',transparent = True)
plt.show()
```

```
[3 3 3 0 3 0 3 0 3 3 3 3 0 3 3 0 0 0 3 0 2 3 3 3 3 0 3 3 3 3 0
3 0 3 3
0 3 3 0 0 0 2 3 0 0 3 3 1 0 0 3]
```



```
In [29]: # Clustering

# 3) LFM: Linear Factor Model followed by a k-means clustering algo
rithm on its factors
# 3.b) Application on all rolling windows

# Timed linear factor model
nt = len(window_mean)
nb_cc = len(frames_norm)
labels = []
timed_LFM = np.zeros((nt,nb_cc,n_factors)) # 3D matrix for the proj
ection of cc returns on two factors
timed_label = np.zeros((nt,nb_cc)) # output matrix with the cluster
s labels for each cc

for i in range(nt):
    win_frames = []
    win_frames = [window_mean.iloc[i],window_var.iloc[i], window_sk
ew.iloc[i],
                  window_kurt.iloc[i], window_005_quantile.iloc[i],
window_010_quantile.iloc[i],
                  window_015_quantile.iloc[i], window_085_quantile.
iloc[i], window_090_quantile.iloc[i],
                  window_095_quantile.iloc[i]]
    win_frames = pd.concat(win_frames, axis=1)
    win_frames_norm = pd.DataFrame(scaler.transform(win_frames),
                                  index=win_frames.index)
    timed_LFM[i] = fanalysis.fit_transform(win_frames_norm)
    timed_label[i] = kmeans.fit_predict(timed_LFM[i])

timed_label = pd.DataFrame(timed_label)
timed_label.columns = cc_names
```

```

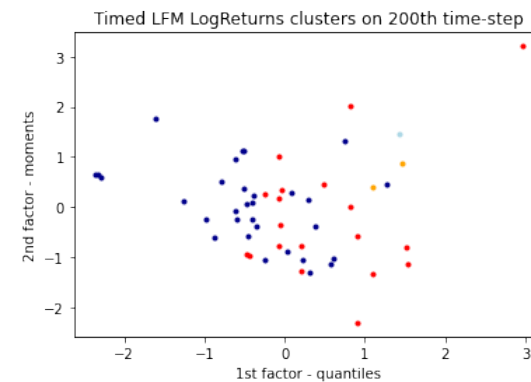
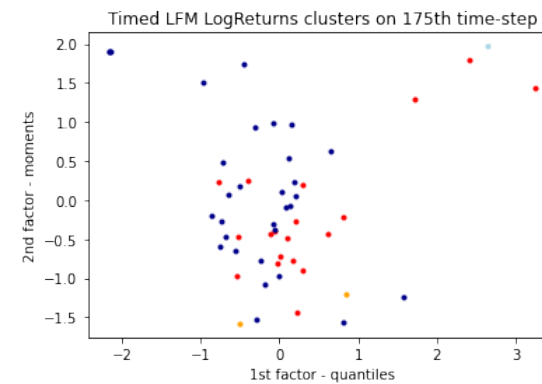
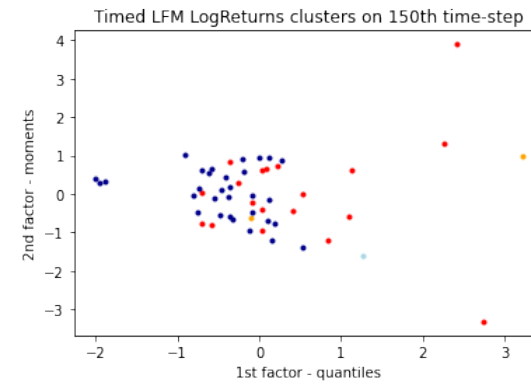
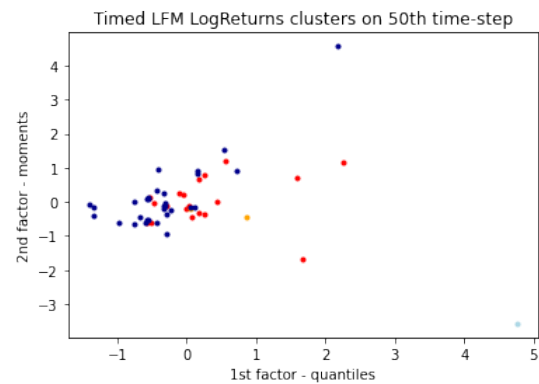
In [30]: # Plotting the results for some rolling windows
print("Let's see how cc log returns are clustered for some rolling
windows")
rw_choice = [50,150,175,200,300]
rw_choice

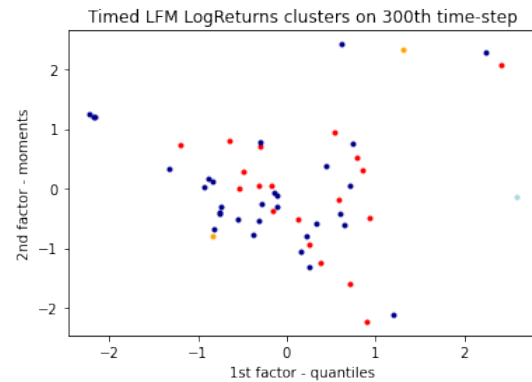
for r in rw_choice:
    selected_ts = r
    filtered_data = timed_LFM[selected_ts]
    filtered_label0 = filtered_data[label == 0]
    filtered_label1 = filtered_data[label == 1]
    filtered_label2 = filtered_data[label == 2]
    filtered_label3 = filtered_data[label == 3]

    #Plotting the results
    fig = plt.figure()
    ax = fig.add_subplot(111)
    ax.scatter(filtered_label0[:,0],filtered_label0[:,1], color='red', marker='.')
    ax.scatter(filtered_label1[:,0],filtered_label1[:,1], color='lightblue', marker='.')
    ax.scatter(filtered_label2[:,0],filtered_label2[:,1], color='orange', marker='.')
    ax.scatter(filtered_label3[:,0],filtered_label3[:,1], color='darkblue', marker='.')
    ax.set(title='Timed LFM LogReturns clusters on '+str(selected_ts) + 'th time-step',ylabel='2nd factor - moments',xlabel='1st factor - quantiles')
    plt.savefig('Clusters/timedlfm_clusters'+str(selected_ts)+'rw.'+str(rw_choice[rw_choice.index(r)]+'.png'),transparent=True)
    plt.show()

```

Let's see how cc log returns are clustered for some rolling windows





In [31]: *# Distribution of cc log returns in clusters*

```
index = pd.DataFrame([frames.index])
lfm_distribution = []
for i in index.transpose()[0]:
    y = timed_label[i].value_counts(normalize=True)
    lfm_distribution.append(y)
lfm_distribution = pd.DataFrame(lfm_distribution); lfm_distribution
= lfm_distribution.round(2)
lfm_distribution.columns = ["Cluster1", "Cluster2", "Cluster3", "Cluster4"]

print("Here is the distribution of cc log returns in each cluster:")
)
print(lfm_distribution)

lfm_distribution1 = pd.DataFrame(lfm_distribution[:17])
lfm_distribution2 = pd.DataFrame(lfm_distribution[17:34])
lfm_distribution3 = pd.DataFrame(lfm_distribution[34:])

lfm_distribution1.to_csv('Clusters/LFM_distribution1.csv', index=True,
header=True)
lfm_distribution2.to_csv('Clusters/LFM_distribution2.csv', index=True,
header=True)
lfm_distribution3.to_csv('Clusters/LFM_distribution3.csv', index=True,
header=True)
```

Here is the distribution of cc log returns in each cluster:

	Cluster1	Cluster2	Cluster3	Cluster4
bitcoin	0.45	0.23	0.15	0.17
ethereum	0.44	0.25	0.14	0.17
ripple	0.42	0.24	0.15	0.19
litecoin	0.46	0.22	0.17	0.15
bitcoin-cash	0.49	0.21	0.14	0.16
chainlink	0.35	0.24	0.20	0.21
binancecoin	0.47	0.21	0.14	0.18
cardano	0.44	0.30	0.12	0.13
stellar	0.43	0.23	0.15	0.19
usd-coin	0.40	0.19	0.15	0.27
bitcoin-cash-sv	0.38	0.21	0.23	0.17
eos	0.41	0.26	0.15	0.18
nem	0.41	0.24	0.16	0.19
tron	0.40	0.26	0.17	0.17
okb	0.35	0.26	0.20	0.19
tezos	0.44	0.22	0.18	0.16
neo	0.45	0.26	0.17	0.13
celsius-degree-token	0.25	0.27	0.28	0.20
theta-token	0.36	0.28	0.16	0.20
dash	0.47	0.23	0.12	0.18
vechain	0.34	0.22	0.24	0.21
havven	0.23	0.21	0.32	0.24
huobi-token	0.34	0.26	0.20	0.21
iota	0.46	0.21	0.14	0.19
zcash	0.48	0.23	0.14	0.15
waves	0.40	0.24	0.17	0.19
ethereum-classic	0.45	0.26	0.15	0.14
zilliqa	0.39	0.25	0.17	0.19
dogecoin	0.39	0.24	0.16	0.21
maker	0.40	0.22	0.18	0.21
decred	0.41	0.22	0.16	0.21
omisego	0.45	0.24	0.16	0.15
ontology	0.39	0.25	0.17	0.19
paxos-standard	0.40	0.18	0.15	0.27
nexo	0.30	0.26	0.20	0.24
basic-attention-token	0.33	0.20	0.26	0.21
digibyte	0.39	0.22	0.20	0.19
0x	0.30	0.29	0.21	0.21
true-usd	0.40	0.18	0.15	0.27
qtum	0.39	0.29	0.17	0.14
republic-protocol	0.29	0.26	0.21	0.24
swissborg	0.29	0.31	0.19	0.20
icon	0.39	0.28	0.16	0.17
loopring	0.35	0.31	0.17	0.17
lisk	0.36	0.25	0.19	0.19
kyber-network	0.26	0.31	0.19	0.23
quant-network	0.18	0.33	0.25	0.24
bitcoin-gold	0.52	0.22	0.11	0.15
maidsafecoin	0.35	0.27	0.19	0.19
vitae	0.12	0.29	0.27	0.31
siacoin	0.44	0.20	0.19	0.17
nano	0.41	0.26	0.18	0.15
enjincoin	0.26	0.33	0.20	0.20

In []: