Assignment 3, Part 1, Specification

SFWR ENG 2AA4

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This Module Interface Specification (MIS) document contains modules, types and methods for implementing the state of a game of Forty Thieves solitaire.

[The parts that you need to fill in are marked by comments, like this one. In several of the modules local functions are specified. You can use these local functions to complete the missing specifications. —SS]

[As you edit the tex source, please leave the `wss` comments in the file. Put your answer **before** the comment. This will make grading easier. —SS]

Card Types Module

Module

CardTypes

Uses

N/A

Syntax

Exported Constants

TOTAL_CARDS = 104
ACE = 1
JACK = 11
QUEEN = 12
KING = 13

Exported Types

SuitT = {Heart, Diamond, Club, Spade}
RankT = [1..13]
CategoryT = {Tableau, Foundation, Deck, Waste}
CardT = tuple of (s: SuitT, r: RankT)

Exported Access Programs

None

Semantics

State Variables

None

State Invariant

None

Generic Stack Module

Generic Template Module

Stack(T)

Uses

N/A

Syntax

Exported Types

Stack = ?[What should be written here? —SS]

Exported Constants

None

Exported Access Programs

Routine name	In	Out	Exceptions
new Stack	seq of T	Stack	none
push	T	Stack	none
pop		Stack	out_of_range
top		T	out_of_range
size		ℕ	
toSeq		seq of T	

Semantics

State Variables

S: Seq of T [What is the type of the state variable? —SS]

State Invariant

None

Assumptions & Design Decisions

- The Stack(T) constructor is called for each object instance before any other access routine is called for that object. The constructor can only be called once.

- Though the toSeq() method violates the essential property of the stack object, since this could be achieved by calling top and pop many times, this method is provided as a convenience to the client. In fact, it increases the property of separation of concerns since this means that the client does not have to worry about details of building their own sequence from the sequence of pops.

Access Routine Semantics

new Stack(s):

- transition: $S := s$

- output: $out := self$

- exception: none

push(e):

- output: $out :=$ new Stack($S \ || \ \langle e \rangle$)

- exception: none

pop():

- output: $out :=$ new Stack($S \ - \ S[|S| - 1]$)[What should go here? —SS]

- exception: ($|S| = 0 \Rightarrow$ out_of_range)[What should go here? —SS]

top():

- output: $out := S[|S| - 1]$

- exception: ($|S| = 0 \Rightarrow$ out_of_range)[What should go here? —SS]

size():

- output: $out := |S|$[What should go here? —SS]

- exception: None

toSeq():

- output: $out := S$

- exception: None

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CardStack Module

Template Module

CardStackT is Stack(CardT)[What should go here? —SS]

Game Board ADT Module

Template Module

BoardT

Uses

CardTypes
CardStack

Syntax

Exported Access Programs

Routine name	In	Out	Exceptions
new BoardT	seq of CardT	BoardT	invalid_argument
is_valid_tab_mv	CategoryT, $\mathbb{N}$, $\mathbb{N}$	$\mathbb{B}$	out_of_range
is_valid_waste_mv	CategoryT, $\mathbb{N}$	$\mathbb{B}$	invalid_argument, out_of_range
is_valid_deck_mv		$\mathbb{B}$	
tab_mv	CategoryT, $\mathbb{N}$, $\mathbb{N}$		invalid_argument
waste_mv	CategoryT, $\mathbb{N}$		invalid_argument
deck_mv			invalid_argument
get_tab	$\mathbb{N}$	CardStackT	out_of_range
get_foundation	$\mathbb{N}$	CardStackT	out_of_range
get_deck		CardStackT	
get_waste		CardStackT	
valid_mv_exists		$\mathbb{B}$	
is_win_state		$\mathbb{B}$	

Semantics

State Variables

T: SeqCrdStckT # *Tableau*
F: SeqCrdStckT # *Foundation*
D: CardStackT # *Deck*
W: CardStackT # *Waste*

State Invariant

$|T| = 10$[What goes here? $- - - SS$]
$|F| = 8$[What goes here? $- - - SS$]
cnt_cards(T, F, D, W, lamda f: True[What goes here? —SS]) = TOTAL_CARDS
two_decks(T, F, D, W) # *each card appears twice in the combined deck*

Assumptions & Design Decisions

- The BoardT constructor is called before any other access routine is called on that instance. Once a BoardT has been created, the constructor will not be called on it again.

- The Foundation stacks must start with an ace, but any Foundation stack can start with any suit. Once an Ace of that suit is placed there, this Foundation stack becomes that type of stack and only those type of cards can be placed there.

- Once a card has been moved to a Foundation stack, it cannot be moved again.

- For better scalability, this module is specified as an Abstract Data Type (ADT) instead of an Abstract Object. This would allow multiple games to be created and tracked at once by a client.

- The getter function is provided, though violating the property of being essential, to give a would-be view function easy access to the state of the game. This ensures that the model is able to be easily integrated with a game system in the future. Although outside of the scope of this assignment, the view function could be part of a Model View Controller design pattern implementation (https://blog.codinghorror.com/understanding-model-view-controller/)

- A function will be available to create a double deck of cards that consists of a random permutation of two regular decks of cards (TOTAL_CARDS cards total). This double deck of cards can be used to build the game board.

Access Routine Semantics

GameBoard(*deck*):

- transition:

  $T, F, D, W := \text{tab\_deck}(deck[0..39]), \text{init\_seq}(8), \text{CardStackT}(deck[40..103]), \text{CardStackT}(\langle\rangle)$

- exception: $exc := (\neg\text{two\_decks}(\text{init\_seq}(10), \text{init\_seq}(8), \text{CardStackT}(deck), \text{CardStackT}(\langle\rangle)) \Rightarrow$ invalid_argument)

is_valid_tab_mv(c, n_0, n_1):

- output:

	$out :=$
$c = $ Tableau	valid_tab_tab(n_0, n_1)
$c = $ Foundation	valid_tab_foundation(n_0, n_1)
$c = $ Deck	False[What goes here? —SS]
$c = $ Waste	False[What goes here? —SS]

- exception:

	$exc :=$
$c = $ Tableau $\wedge \neg($is_valid_pos$($Tableau$, n_0) \wedge$ is_valid_pos$($Tableau$, n_1))$	out_of_range
$c = $ Foundation $\wedge \neg($is_valid_pos$($Tableau$, n_0) \wedge$ is_valid_pos$($Foundation$, n_1))$	out_of_range

is_valid_waste_mv(c, n):

- output:

	$out :=$
$c = $ Tableau	valid_waste_tab(n)
$c = $ Foundation	valid_waste_foundation(n)
$c = $ Deck	False[What goes here? —SS]
$c = $ Waste	False[What goes here? —SS]

- exception:

	$exc :=$
W.size$() = 0$	invalid_argument
$c = $ Tableau $\wedge \neg$is_valid_pos$($Tableau$, n)$	out_of_range
$c = $ Foundation $\wedge \neg$is_valid_pos$($Foundation$, n)$	out_of_range

is_valid_deck_mv():

- output: $out := |D| > 0 \Rightarrow$ True [What goes here? The deck moves involves moving a card from the deck stack to the waste stack. —SS]

- exception: None

tab_mv(c, n_0, n_1):

- transition:

$c = $ Tableau	T$[n_0]$, T$[n_1] := $ T$[n_0]$.pop(), T$[n_1]$.push(T$[n_0]$.top())[What goes here? —SS]
$c = $ Foundation	T$[n_0]$, F$[n_1] := $ T$[n_0]$.pop(), F$[n_1]$.push(T$[n_0]$.top())[What goes here? —SS]

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- exception: $exc := (\neg$is_valid_tab_mv$(c, n_0, n_1) \Rightarrow$ invalid_argument$)$

waste_mv(c, n):

- transition:

$c = $ Tableau	W, T$[n]$:= W.pop(), T$[n]$.push(W.top())[What goes here? —SS]
$c = $ Foundation	W, F$[n]$:= W.pop(), F$[n]$.push(W.top())[What goes here? —SS]

- exception: $exc := (\neg$is_valid_waste_mv$(c, n) \Rightarrow$ invalid_argument$)$

deck_mv():

- transition: D, W := D.pop(), W.push(D.top())[What goes here? —SS]

- exception: $exc := (\neg$is_valid_deck_mv$() \Rightarrow$ invalid_argument$)$

get_tab(i):

- output: $out := T[i]$

- exception: $exc : (\neg$is_valid_pos$($Tableau$, i) \Rightarrow$ out_of_range$)$

get_foundation(i):

- output: $out := F[i]$

- exception: $exc : (\neg$is_valid_pos$($Foundation$, i) \Rightarrow$ out_of_range$)$

get_deck():

- output: $out := D$

- exception: None

get_waste():

- output: $out := W$

- exception: None

valid_mv_exists():

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- output: $out :=$ valid_tab_mv $\lor$ valid_waste_mv $\lor$ is_valid_deck_mv() where

    valid_tab_mv $\equiv (\exists c : \text{CategoryT}, n_0 : \mathbb{N}, n_1 : \mathbb{N} | \neg(c = \text{Waste}) \land \neg(c = \text{Deck}) \land 0 \leq n_0 \leq |c| \land 0 \leq n_1 \leq |c|[\text{What goes here?} --- SS] : \text{is\_valid\_tab\_mv}(c, n_0, n_1))$

    valid_waste_mv $\equiv (\exists c : \text{CategoryT}, n : \mathbb{N} | \neg(c = \text{Waste}) \land \neg(c = \text{Deck}) \land 0 \leq n \leq |c|[\text{What goes here?} --- SS] : \text{is\_valid\_waste\_mv}(c, n))$

- exception: None

is_win_state():

- output: $out := \neg(\text{valid\_mv\_exists}()) \land \text{cnt\_cards\_seq}(T, f) = 0 \land \text{cnt\_cards\_seq}(F, f) = 104 \land \text{cnt\_cards\_stack}(D, f) = 0 \land \text{cnt\_cards\_stack}(W, f) = 0$ [What goes here? —SS]

- exception: None

Local Types

SeqCrdStckT = seq of CardStackT

Local Functions

two_decks : SeqCrdStckT $\times$ SeqCrdStckT $\times$ CardStackT $\times$ CardStackT $\to \mathbb{B}$
two_decks$(T, F, D, W) \equiv$ [This function returns True if there is two of each card in the game —SS]

$(\forall st : \text{SuitT}, rk : \text{RankT} | st \in \text{SuitT} \land rk \in \text{RankT} : \text{cnt\_cards}(T, F, D, W, \text{lambda } c : c.s = st \land c.r = rk) = 2)$[Wha

cnt_cards_seq : SeqCrdStckT $\times$ (CardT $\to \mathbb{B}$) $\to \mathbb{N}$
cnt_cards_seq$(S, f) \equiv (+s : \text{CardStackT} | s \in S : \text{cnt\_cards\_stack}(s, f))$

cnt_cards_stack : CardStackT $\times$ (CardT $\to \mathbb{B}$) $\to \mathbb{N}$
cnt_cards_stack$(s, f) \equiv (+card : \text{CardT} | card \in s \land f(card) : 1)$[What goes here? —SS]

cnt_cards : SeqCrdStckT $\times$ SeqCrdStckT $\times$ CardStackT $\times$ CardStackT $\times$ (CardT $\to \mathbb{B}$) $\to \mathbb{N}$
cnt_cards$(T, F, D, W, f) \equiv$ cnt_cards_seq(T, f)+cnt_cards_seq(F, f)+cnt_cards_stack(D, f)+
cnt_cards_stack(W, f)

init_seq : $\mathbb{N} \to$ SeqCrdStckT

init_seq(n) $\equiv s$ such that $(|s| = n \wedge (\forall\, i \in [0..n-1] : s[i] = \text{CardStackT}(\langle\rangle))$

tab_deck : (seq of CardT) $\to$ SeqCrdStckT

tab_deck($deck$) $\equiv T$ such that $(\forall i : \mathbb{N} | i \in [0..9] : T[i].\text{toSeq}() = deck[4*i, 4*(i+1), 4*(i+2), 4*(i+3)$[What goes here? $---SS$]])

is_valid_pos: CategoryT $\times \mathbb{N} \to \mathbb{B}$

is_valid_pos(c, n) $\equiv (c = \text{Tableau} \Rightarrow n \in [0..9] | c = \text{Foundation} \Rightarrow n \in [0..7] | \text{True} \Rightarrow \text{True})$

valid_tab_tab: $\mathbb{N} \times \mathbb{N} \to \mathbb{B}$

valid_tab_tab $(n_0, n_1) \equiv$

$T[n_0].\text{size}() > 0$	$T[n_1].\text{size}() > 0$	tab_placeable(T[n_0].top(),T[n_1].top())[What goes here? —SS]
	$T[n_1].\text{size}() = 0$	True[What goes here? —SS]
$T[n_0].\text{size}() = 0$	$T[n_1].\text{size}() > 0$	False[What goes here? —SS]
	$T[n_1].\text{size}() = 0$	False[What goes here? —SS]

valid_tab_foundation: $\mathbb{N} \times \mathbb{N} \to \mathbb{B}$

valid_tab_foundation(n_0, n_1) $\equiv$

$T[n_0].\text{size}() > 0$	$F[n_1].\text{size}() > 0$	foundation_placeable(T[n_0].top(),F[n_1].top())
	$F[n_1].\text{size}() = 0$	$T[n_0].\text{top}().r = \text{ACE}$
$T[n_0].\text{size}() = 0$	$F[n_1].\text{size}() > 0$	False
	$F[n_1].\text{size}() = 0$	False

[What goes here? You may need a table? —SS]

valid_waste_tab: $\mathbb{N} \to \mathbb{B}$

valid_waste_tab $(n) \equiv$

$T[n].\text{size}() > 0$	tab_placeable(W.top(), T[n].top())
$T[n].\text{size}() = 0$	True

valid_waste_foundation: $\mathbb{N} \to \mathbb{B}$

valid_waste_foundation $(n) \equiv$

$F[n].\text{size}() > 0$	foundation_placeable(W.top(), F[n].top())
$F[n].\text{size}() = 0$	$\text{W.top}().r = \text{ACE}$

tab_placeable: $\mathrm{CardT} \times \mathrm{CardT} \to \mathbb{B}$

tab_placeable $(c_0, c_1) \equiv c_0.s = c_1.s \land c_0.r = c_1.r - 1$[Complete this specification —SS]

foundation_placeable: $\mathrm{CardT} \times \mathrm{CardT} \to \mathbb{B}$

foundation_placeable $(c_0, c_1) \equiv c_0.s = c_1.s \land c_0.r = c_1.r - 1$[Complete this specification —SS]

Critique of Design

Overall the interface for the modules is very thorough and sometimes was a little difficult to keep track of what was going on.

The Card Types Module was very straightforward and easy to follow with descriptive constant names. The exported types are also straightforward and it seems intuitive as to how we would implement this in code.

The Generic Stack Module also was very straightforwards and easy to follow. The exported type is a Stack which could be of any type. The exported access programs all seem rather intuitive to the stack data structure that we have learned and should be rather simple to implement. The semantics for this module are all easy to follow and come up with.

CardStack Module is just a specific instance of the Generic Stack Module that uses CardT as its type.

Now comes the much more complicated Game Board ADT Module. This module had its challenges mostly based on intimidation. Seeing the amount of methods and pages that needed to be filled was quite scary. But after taking time with the specification and understanding the mechanics of the game then the module was not too bad. This meant time was needed before hand to at least research the game and its rules a little.

Although I have my concerns, the only thing that I might consider changing/modifying is the Game Board ADT Module. I would break it down to at least 2 modules if possible, this would have the affect of being less daunting and might come of as more manageable. Other than this one little detail I do not think there is anything that I would consider changing in this specification.