

# Impoverishment & Aid in the United States

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# Background

- The Supplemental Nutrition Assistance Program (SNAP) provides food subsidies to those earning income at or below 130% of the federal poverty line.
- In 2020 was reported to have:
  - Provided benefits to ~39.9 million people.
    - Assisted ~20.5 million households.
  - Spent \$74.2 billion in direct aid.
- Of those assisted:
  - 81% had income below the federal poverty line (pre-pandemic).
  - 36% had income less than half the federal poverty line
    - 54% of spending went to these individuals.

One of many types of subsidies available to struggling families in the US.

# Poverty Line

How is it defined?

## Federal Poverty Line:

- Single Individual: \$16,770
- Per additional person: +\$5,910
  - In 2022, ~37.9 million Americans estimated to be impoverished.

## Supplemental Poverty Threshold:

- Looks at income, subsidies, taxes, and other expenses.
  - Household of 4:
    - Renting: \$34,518
    - Mortgage: \$34,235
    - Owning w/o Mortgage: \$28,909
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# Effects of Poverty

According to the US Office of Disease Prevention and Health Promotion (OASH):

- Impoverished individuals have an increased risk of developing mental illness or chronic disease.
  - Reduced life expectancy.
- Poverty is often area-based and out of individual control.
- Represents systemic issues:
  - Discrimination
  - Sustainable housing
  - Nutrition
  - Neighborhood safety
  - Education
  - Employment

# 2021 American Community Survey

Data collected by US Census Bureau from 3,092,744 individuals selected by random household sampling.

- We reduced this to 2,137,708 observations of 34 variables.

|           |               |                   |                          |                                       |                       |                     |                     |                      |                 |
|-----------|---------------|-------------------|--------------------------|---------------------------------------|-----------------------|---------------------|---------------------|----------------------|-----------------|
| age       | education     | income            | state tax                | Supplemental health insurance premium | medicare part b       | child care expenses | number of kids      | SNAP                 | WIC subsidy     |
| sex       | marriage      | agi               | eitc                     | medical expenses                      | capped total expenses | mortgage status     | cohabiting couples? | school lunch subsidy | housing subsidy |
| race      | spm threshold | federal tax       | fica                     | medical out of pocket                 | work expenses         | number of adults    | unidentified kids?  | energy subsidy       | group           |
| hispanic? | spm resources | tax before credit | health insurance premium |                                       |                       |                     |                     |                      |                 |

# Group

Target Variable

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Poor Group: 261,978 Observations

Aid Group: 427,112 Observations

No Group: 1,448,618 Observations

- Poor
    - Any individual classified as poor in data set.
      - Both federal poverty and SPM poverty.
  - Aid
    - Any individual with nonzero SNAP, slunch, energy, house\_sub, or WIC not in poverty group.
  - No
    - All other observations.
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# Sample

- 50-30-20 Split

Train:

- Variable analysis
- Misclassification

Test:

- Retrain to test variable validity

Validation:

- Final misclassification rates.

| Sample     | Count     |
|------------|-----------|
| Train      | 1,068,854 |
| Test       | 641,312   |
| Validation | 427,543   |

# Methods

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Principal Components, Discriminant Analysis,  
Logistic Regression



# Principal Components

Unsupervised Learning Method

Analyze Group Variance  
Explanation

Compute eigenvectors of data correlation matrix and use as weights for creating new variables.

- Explain amount of variance equal to eigenvalue.
- Typically used to create variable combinations for dimension reduction.

# Discriminant Analysis

Supervised Classification

—  
Geometric Division

Create classification regions for which probability of a class is maximized based on prior probabilities.

- Assumes normality.

Linear:

- Assumes equal covariance matrices among groups.

Quadratic:

- Does not assume equal covariance matrices.
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# Logistic Regression

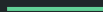
Supervised Classification

—

Classification by Odds

Optimize  $k-1$  logit functions and assigns observations to group of maximum probability.

- Utilizes Bernoulli probability distribution for groups.



# Metrics

## Principal Components:

- Component Matching
  - Variables of coefficient greater than  $1/\sqrt{k}$  are considered significant.
  - **Perfect Match (PM)**: Match component and position.
  - **Component Match (CM)**: Match component.
- Cosine Similarity
  - Vector dot product divided by product of lengths.
  - **CS**: Base cosine similarity.
  - **aCS**: Cosine similarity of absolute-value vectors.
  - **wCS**: Weighted similarity based on component contribution.

## Classification:

- **Accuracy**: Number correct divided by total observances.
- **Recall**: Number correct in Aid group divided by total Aid group in test.
- **Precision**: Number correct in Aid group divided by total predicted in Aid group.
- **F1**:  $2 * (\text{Recall} * \text{Precision}) / (\text{Recall} + \text{Precision})$
- Misclassification Analysis

# Results

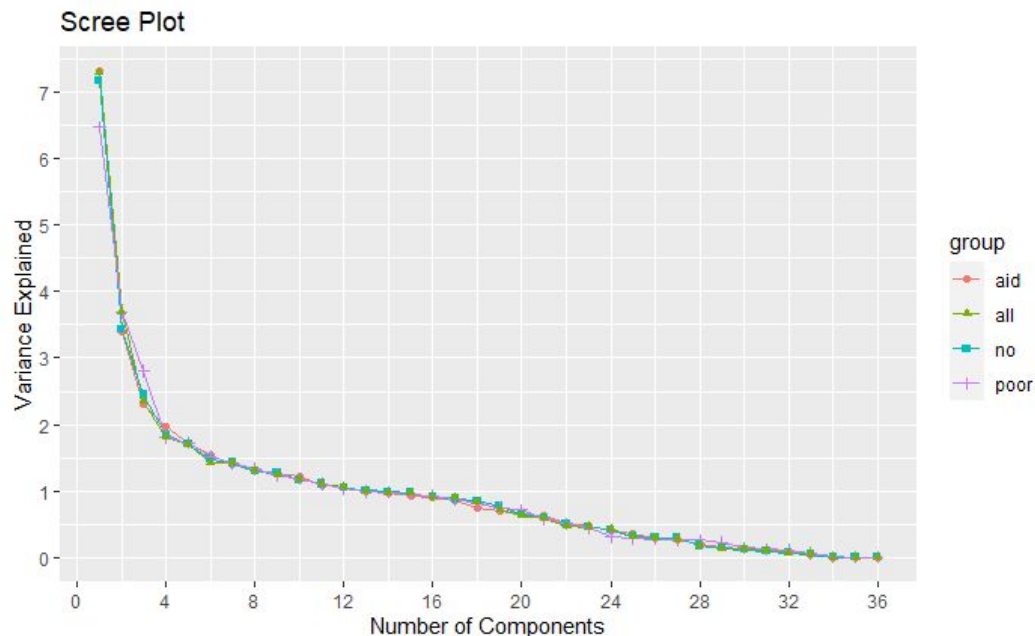
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# Principal Components - Variance Explanation

Similar rates of explanation.

- PC 1: Income, Tax, Expenses
- PC 2: Household, Expenses, Tax
- PC 3: Medical Expenses
- PC 4: Marriage, Housing, Health Insurance

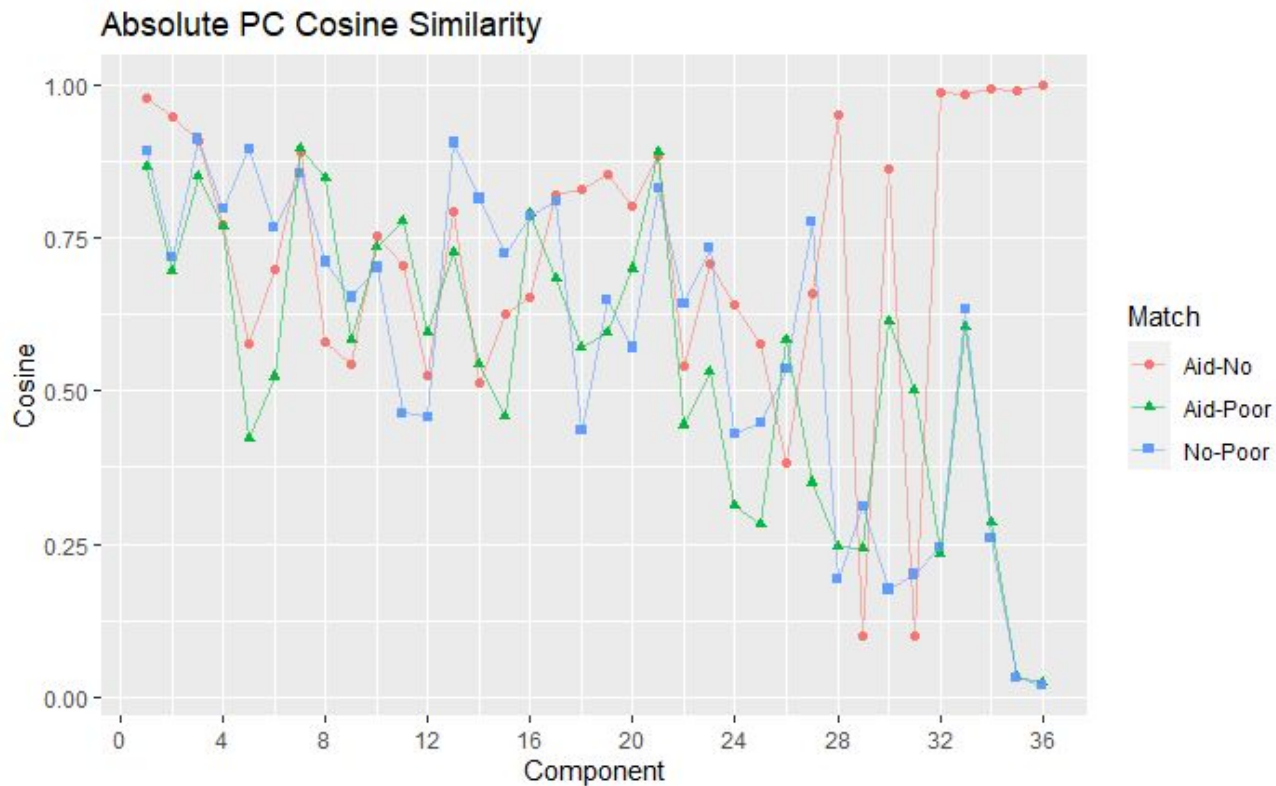
First 4 explain ~41% of total variance.



# Principal Components - Similarity

| Metric | Aid-No   | Aid-Poor | No-Poor  | Aid-Aid  | No-No   | Poor-Poor |
|--------|----------|----------|----------|----------|---------|-----------|
| PM     | 0.14634  | 0.06130  | 0.06654  | 0.78210  | 0.72793 | 0.51224   |
| CM     | 0.54409  | 0.35632  | 0.38817  | 0.96109  | 0.94775 | 0.84746   |
| CS     | -0.12623 | 0.02001  | -0.02923 | -0.66538 | 0.94101 | 0.81058   |
| aCS    | 0.72648  | 0.55025  | 0.58295  | 0.99745  | 0.99558 | 0.93428   |
| wCS    | 0.78652  | 0.70013  | 0.75263  | 0.99794  | 1.00000 | 1.00000   |

# Principal Components - Absolute Cosine Similarity





# Discriminant Analysis - Confusion Matrices

| LD       |      | Predicted |        |       |
|----------|------|-----------|--------|-------|
|          |      | Aid       | No     | Poor  |
| Observed | Aid  | 38142     | 39523  | 7757  |
|          | No   | 10699     | 275555 | 3470  |
|          | Poor | 3193      | 11143  | 38060 |

| QD       |      | Predicted |        |       |
|----------|------|-----------|--------|-------|
|          |      | Aid       | No     | Poor  |
| Observed | Aid  | 47582     | 20367  | 17473 |
|          | No   | 18797     | 253435 | 17492 |
|          | Poor | 1593      | 3307   | 47496 |

| LD-B     |      | Predicted |        |       |
|----------|------|-----------|--------|-------|
|          |      | Aid       | No     | Poor  |
| Observed | Aid  | 52616     | 18007  | 14799 |
|          | No   | 23738     | 247281 | 18705 |
|          | Poor | 2488      | 1869   | 48039 |

| QD-B     |      | Predicted |        |       |
|----------|------|-----------|--------|-------|
|          |      | Aid       | No     | Poor  |
| Observed | Aid  | 37986     | 28127  | 19309 |
|          | No   | 30841     | 226660 | 32223 |
|          | Poor | 1947      | 2861   | 47588 |

# Discriminant Analysis - Metrics

Highest Accuracy: LD

Highest Recall: LD-B

Highest Precision: LD

Highest F1: LD-B

- LD likely leverages size of No Group.
- QD assumptions best fit scenario.

|           | LD      | LD-B    | QD      | QD-B    |
|-----------|---------|---------|---------|---------|
| Accuracy  | 0.82274 | 0.81381 | 0.81516 | 0.73030 |
| Recall    | 0.44651 | 0.61595 | 0.55702 | 0.44469 |
| Precision | 0.73302 | 0.66736 | 0.70002 | 0.53672 |
| F1        | 0.55497 | 0.64043 | 0.62039 | 0.48639 |

# Logistic Regression

Metrics:

- Accuracy: 0.91860
- Recall: 0.72552
- Precision: 0.93683
- F1: 0.81774

Highest performance on all metrics.

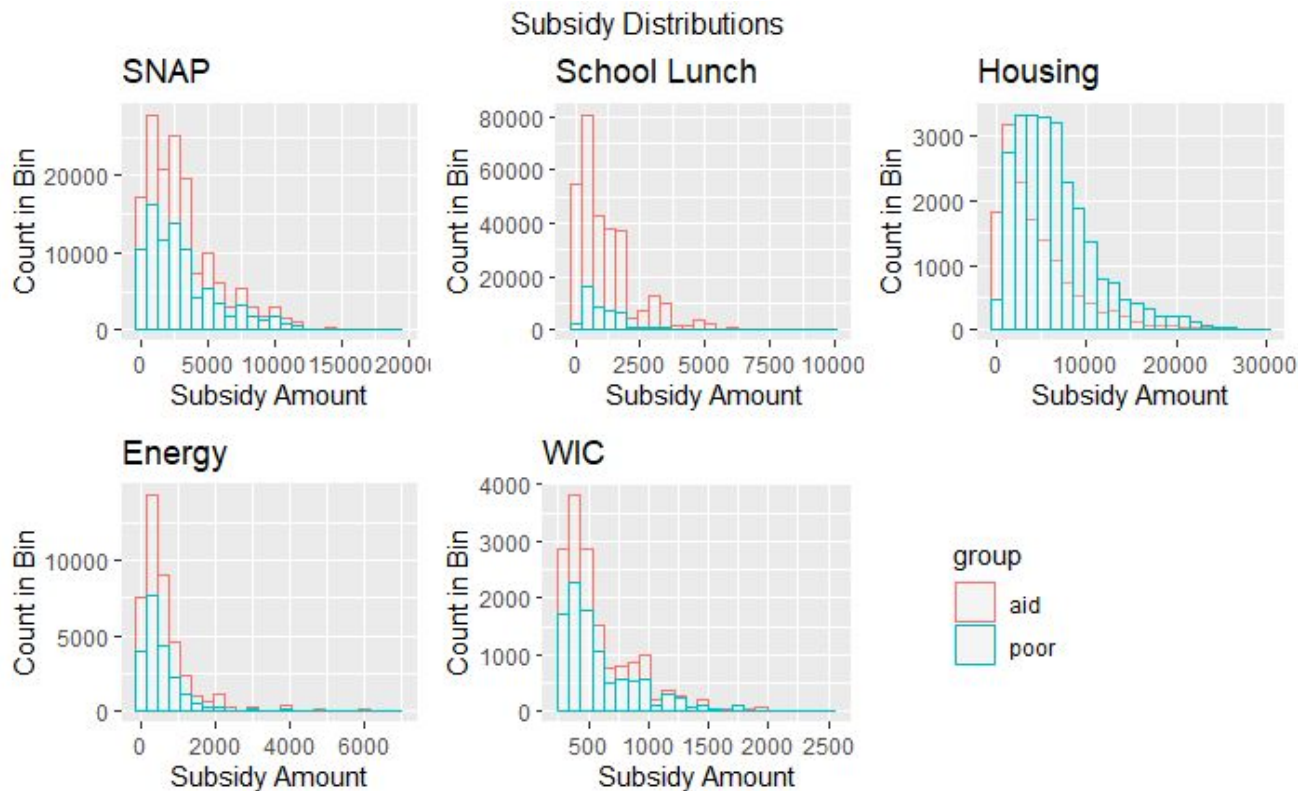
Tending to misclassify Aid Group into No Group.

| Logistic |      | Predicted |        |       |
|----------|------|-----------|--------|-------|
|          |      | Aid       | No     | Poor  |
| Observed | Aid  | 61975     | 18064  | 5383  |
|          | No   | 2236      | 285668 | 1820  |
|          | Poor | 1943      | 5357   | 45096 |

# Conclusion

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# A Note From Exploratory Analysis



# Conclusion

All modeling approaches implied the Aid Group was most similar to the No Group.

## Limitations:

- School Lunch Subsidy inclusion
- Multicollinearity
- Normality
  - Possible Transformations
- Not statistically rigorous

## Implications:

- No action should be taken.
- Cannot justify poor classification for aid group.

## Further Research:

- Subsidy Analysis
- Aid Group Prediction

Thank You!

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